OpenCMISS-iron examples and tests used by OpenCMISS developers at University of Stuttgart, Germany

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> June 27, 2017 18:43

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1 INTRODUCTION

This document contains information about examples used for testing *OpenCMISS-iron*. Read: How-to¹ and [1].

- 1.1 Cmgui files for cmgui-2.9
- 1.2 Variations to consider
 - Geometry and topology

1D, 2D, 3D

Length, width, height

Number of elements

Interpolation order

Generated or user meshes

quad/hex or tri/tet meshes

- Initial conditions
- Load cases

Dirichlet BC

Neumann BC

Volume force

Mix of previous items

- Sources, sinks
- Time dependence

Static

Quasi-static

Dynamic

Material laws

Linear

Nonlinear (Mooney-Rivlin, Neo-Hookean, Ogden, etc.)

Active (Stress, strain)

- Material parameters, anisotropy
- Solver

Direct

Iterative

Test cases

Numerical reference data

Analytical solution

• A mix of previous items

¹ https://bitbucket.org/hessenthaler/opencmiss-howto

1.3 Folder structure

TBD..

HOW TO WORK ON THIS DOCUMENT

In the Google Doc at https://docs.google.com/spreadsheets/d/1RGKj8vVPqQ-PH0UwMX_ e9TAzqaYavKi0z0D4pKY9RGI/edit#gid=0 please indicate what you are working on or if a given example was finished

- no mark: to be done
- x: currently working on it
- xx: done

Initials	Full name
СВ	Christian Bleiler
AH	Andreas Hessenthaler
TK	Thomas Klotz
AK	Aaron Krämer
BM	Benjamin Maier
SM	Sergio Morales
MM	Mylena Mordhorst
HS	Harry Saini

 Table 1: Initials of people working on examples, in alphabetical order (surnames).

3 DIFFUSION EQUATION

3.1 Equation in general form

The governing equation is,

$$\partial_t \mathbf{u} + \nabla \cdot [\boldsymbol{\sigma} \nabla \mathbf{u}] = \mathbf{f}, \tag{1}$$

with conductivity tensor $\boldsymbol{\sigma}.$ The conductivity tensor is,

- defined in material coordinates (fibre direction),
- diagonal,
- defined per element.

3.2 Example-0001

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.2.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \qquad \qquad \Omega = [0, 2] \times [0, 1], \tag{2}$$

with boundary conditions

$$u = 0 x = y = 0, (3)$$

$$u = 1$$
 $x = 2, y = 1.$ (4)

No material parameters to specify.

3.2.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla \mathbf{u} = 0 \qquad \qquad \Omega = [0, 2] \times [0, 1] \times [0, 1], \tag{5}$$

with boundary conditions

$$u = 0 \qquad \qquad x = y = z = 0, \tag{6}$$

$$u = 1$$
 $x = 2, y = z = 1.$ (7)

No material parameters to specify.

3.2.3 Computational model

• Commandline arguments are:

float: length along x-direction float: length along y-direction

float: length along z-direction (set to zero for 2D)

integer: number of elements in x-direction integer: number of elements in y-direction

integer: number of elements in z-direction (set to zero for 2D)

interger: interpolation order (1: linear; 2: quadratic)

integer: solver type (o: direct; 1: iterative)

Commandline arguments for tests are:

2.0 1.0 0.0 2 1 0 1 0

2.0 1.0 0.0 4 2 0 1 0

2.0 1.0 0.0 8 4 0 1 0

2.0 1.0 0.0 2 1 0 2 0

2.0 1.0 0.0 4 2 0 2 0

2.0 1.0 0.0 8 4 0 2 0

2.0 1.0 0.0 2 1 0 1 1

2.0 1.0 0.0 4 2 0 1 1

3.2.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

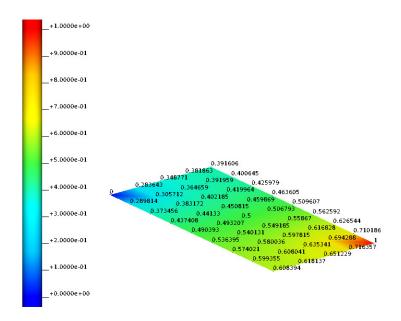


Figure 1: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 o].

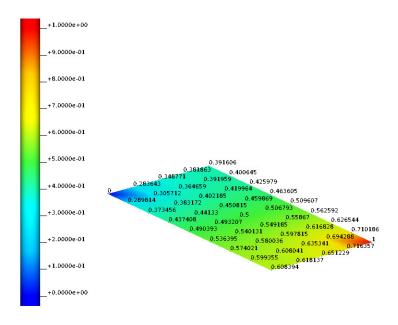


Figure 2: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

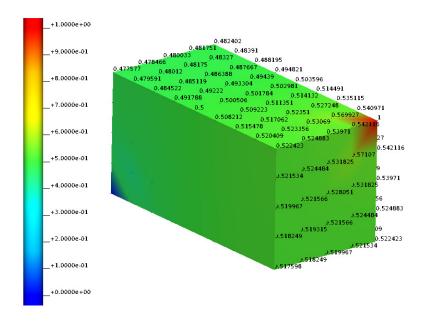


Figure 3: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 o].

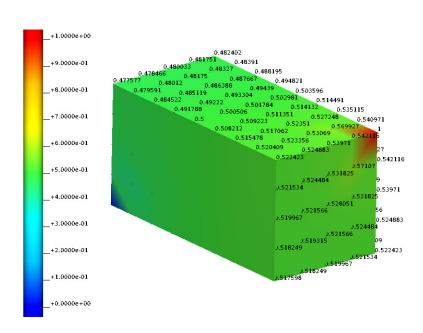


Figure 4: 3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].

3.3 Example-0001-u

Example uses user-defined regular meshes in CHeart mesh format and solves a static problem, i.e., applies the boundary conditions in one step.

3.3.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \qquad \qquad \Omega = [0, 2] \times [0, 1], \tag{8}$$

with boundary conditions

$$u = 0 x = y = 0, (9)$$

$$u = 1$$
 $x = 2, y = 1.$ (10)

No material parameters to specify.

3.3.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla \mathbf{u} = \mathbf{0} \qquad \qquad \Omega = [0, 2] \times [0, 1] \times [0, 1], \tag{11}$$

with boundary conditions

$$u = 0 \qquad \qquad x = y = z = 0, \tag{12}$$

$$u = 1$$
 $x = 2, y = z = 1.$ (13)

No material parameters to specify.

3.3.3 Computational model

Commandline arguments are:

float: length along x-direction float: length along y-direction

float: length along z-direction (set to zero for 2D)

integer: number of elements in x-direction integer: number of elements in y-direction

integer: number of elements in z-direction (set to zero for 2D)

interger: interpolation order (1: linear; 2: quadratic)

integer: solver type (o: direct; 1: iterative)

Commandline arguments for tests are:

2.0 1.0 0.0 2 1 0 1 0

2.0 1.0 0.0 4 2 0 1 0

2.0 1.0 0.0 8 4 0 1 0

2.0 1.0 0.0 2 1 0 2 0

2.0 1.0 0.0 4 2 0 2 0

2.0 1.0 0.0 8 4 0 2 0

2.0 1.0 0.0 2 1 0 1 1

2.0 1.0 0.0 4 2 0 1 1

```
2.0 1.0 0.0 8 4 0 1 1
2.0 1.0 0.0 2 1 0 2 1
2.0 1.0 0.0 4 2 0 2 1
2.0 1.0 0.0 8 4 0 2 1
2.0 1.0 1.0 2 1 1 1 0
2.0 1.0 1.0 4 2 2 1 0
2.0 1.0 1.0 8 4 4 1 0
2.0 1.0 1.0 2 1 1 2 0
2.0 1.0 1.0 4 2 2 2 0
2.0 1.0 1.0 8 4 4 2 0
2.0 1.0 1.0 2 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1
2.0 1.0 1.0 8 4 4 1 1
2.0 1.0 1.0 2 1 1 2 1
2.0 1.0 1.0 4 2 2 2 1
2.0 1.0 1.0 8 4 4 2 1
```

• Note: Binary uses command line arguments to search for the relevant mesh files.

3.3.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

Passed tests: 18 / 24

Failed tests:

```
current_run/l2x1x0_n2x1x0_i2_s0/Example.part0.exnode
                                                           | CHeart - Iron |_2 = 0.79700
current_run/l2x1x0_n4x2x0_i2_s0/Example.part0.exnode
                                                           | CHeart - Iron |_{2} = 1.08989
current_run/l2x1x0_n8x4x0_i2_s0/Example.part0.exnode
                                                           | CHeart - Iron |_{2} = 1.65507
                                                           | CHeart - Iron |_{-2} = 0.79700
current_run/l2x1x0_n2x1x0_i2_s1/Example.part0.exnode
current_run/l2x1x0_n4x2x0_i2_s1/Example.part0.exnode
                                                           | CHeart - Iron |_2 = 1.08989
current_run/l2x1x0_n8x4x0_i2_s1/Example.part0.exnode
                                                           | CHeart - Iron |_2 = 1.65507
```

3.4 Example-0011

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.4.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot [\sigma \nabla u] = 0 \qquad \qquad \Omega = [0, 2] \times [0, 1], \tag{14}$$

with boundary conditions

$$u = 0 x = y = 0, (15)$$

$$u = 1$$
 $x = 2, y = 1.$ (16)

The conductivity tensor is defined as,

$$\sigma(x,t) = \sigma = I. \tag{17}$$

3.4.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot [\boldsymbol{\sigma} \nabla \boldsymbol{u}] = 0 \qquad \qquad \Omega = [0, 2] \times [0, 1] \times [0, 1], \tag{18}$$

with boundary conditions

$$u = 0 \qquad \qquad x = y = z = 0, \tag{19}$$

$$u = 1$$
 $x = 2, y = z = 1.$ (20)

The conductivity tensor is defined as,

$$\sigma(x,t) = \sigma = I. \tag{21}$$

3.4.3 Computational model

• Commandline arguments are:

float: length along x-direction float: length along y-direction

float: length along z-direction (set to zero for 2D)

integer: number of elements in x-direction integer: number of elements in y-direction

integer: number of elements in z-direction (set to zero for 2D)

integer: interpolation order (1: linear; 2: quadratic)

integer: solver type (o: direct; 1: iterative)

float: σ_{11} float: σ_{22}

float: σ_{33} (ignored for 2D)

• Commandline arguments for tests are:

3.4.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

Passed tests: 24 / 24

No failed tests.

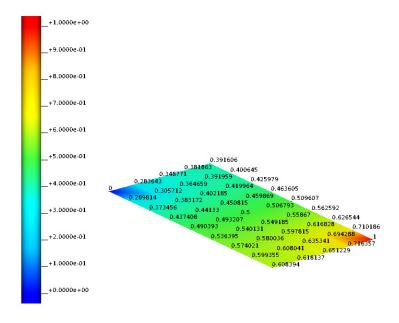


Figure 5: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 011].

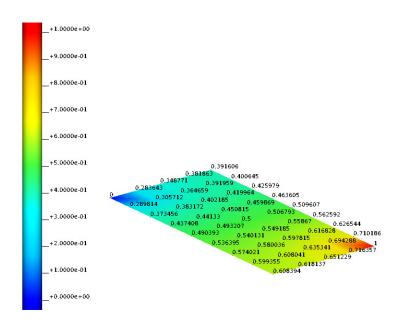


Figure 6: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0 1 1].

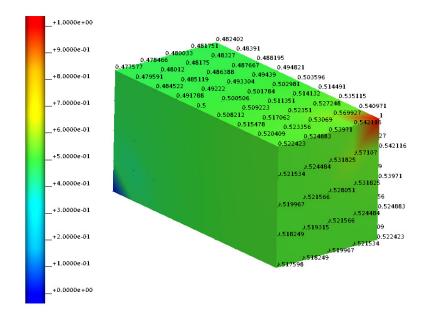


Figure 7: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 1 1 1].

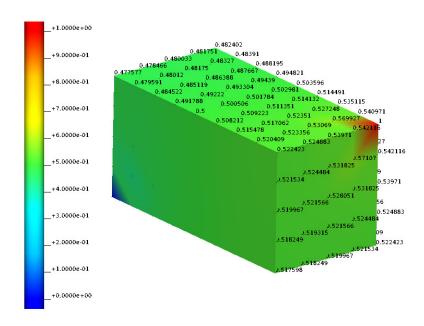


Figure 8: 3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 111].

4 LINEAR ELASTICITY

4.1 Equation in general form

$$\label{eq:delta_theta_$$

4.2 Example-0101

4.2.1 Mathematical model

We solve the following equation,

$$\nabla \cdot \boldsymbol{\sigma}(\boldsymbol{u},t) = \boldsymbol{0} \qquad \qquad \boldsymbol{\Omega} = [0,160] \times [0,120], t \in [0,5], \tag{23}$$

with time step size $\Delta_t = 1$ and boundary conditions

$$\dots$$
 (25)

2D: specify thickness, Young's modulus and Poisson's ratio.

4.2.2 Computational model

- Length, width, height
- Direct/iterative solver
- Generated/user mesh
- Number of elements
- Interpolation order
- Number of solver steps (time steps, load steps)

4.2.3 Results

Figure 9: Results, analytical solution.

4.2.4 Validation

CHeart rev. 6328, Abaqus 2017, analytical reference solution, whatever...

Figure 10: Results, Abaqus reference.

Figure 11: Results, iron reference.

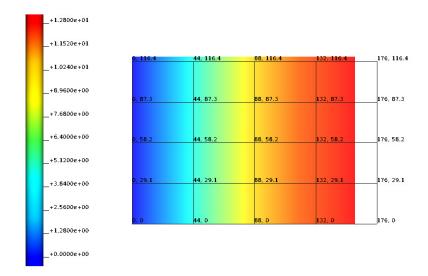


Figure 12: Results, current run.

5 FINITE ELASTICITY

6 NAVIER-STOKES FLOW

7 MONODOMAIN

8 CELLML MODEL

REFERENCES

[1] Chris Bradley, Andy Bowery, Randall Britten, Vincent Budelmann, Oscar Camara, Richard Christie, Andrew Cookson, Alejandro F Frangi, Thiranja Babarenda Gamage, Thomas Heidlauf, et al. Opencmiss: a multi-physics & multi-scale computational infrastructure for the vph/physiome project. Progress in biophysics and molecular biology, 107(1):32-47, 2011.