

OpenCMISS-iron examples and tests used by *OpenCMISS* developers at University of Stuttgart, Germany

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CONTENTS

1	Introduction	4
1.1	Cmgui files for cmgui-2.9	4
1.2	Variations to consider	4
1.3	Folder structure	5
2	How to work on this document	5
3	Diffusion equation	6
3.1	Equation in general form	6
3.2	Example-0001	7
3.2.1	Mathematical model - 2D	7
3.2.2	Mathematical model - 3D	7
3.2.3	Computational model	7
3.2.4	Result summary	8
3.3	Example-0001-u	11
3.3.1	Mathematical model - 2D	11
3.3.2	Mathematical model - 3D	11
3.3.3	Computational model	11
3.3.4	Result summary	12
3.4	Example-0002	15
3.4.1	Mathematical model - 2D	15
3.4.2	Mathematical model - 3D	15
3.4.3	Computational model	15
3.4.4	Result summary	16
3.5	Example-0003	19

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3.5.1	Mathematical model - 2D	19
3.5.2	Mathematical model - 3D	19
3.5.3	Computational model	19
3.5.4	Result summary	20
3.6	Example-0011	23
3.6.1	Mathematical model - 2D	23
3.6.2	Mathematical model - 3D	23
3.6.3	Computational model	23
3.6.4	Result summary	24
4	Linear elasticity	27
4.1	Equation in general form	27
4.2	Example-0101	28
4.2.1	Mathematical model	28
4.2.2	Computational model	28
4.2.3	Results	28
4.2.4	Validation	28
5	Finite elasticity	31
6	Navier-Stokes flow	32
7	Monodomain	33
8	CellML model	34

LIST OF FIGURES

Figure 1	2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	8
Figure 2	2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	9
Figure 3	3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	9
Figure 4	3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	10
Figure 5	2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	12
Figure 6	2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	13
Figure 7	3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	13
Figure 8	3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	14
Figure 9	2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	16
Figure 10	2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	17
Figure 11	3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	17
Figure 12	3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	18
Figure 13	2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	21
Figure 14	2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].	21

Figure 15	3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	22
Figure 16	3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].	22
Figure 17	2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0 1 1].	25
Figure 18	2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0 1 1].	25
Figure 19	3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 1 1 1].	26
Figure 20	3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 1 1 1].	26
Figure 21	Results, analytical solution.	28
Figure 22	Results, Abaqus reference.	29
Figure 23	Results, iron reference.	29
Figure 24	Results, current run.	30

LIST OF TABLES

Table 1	Initials of people working on examples, in alphabetical order (surnames).	5
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1 INTRODUCTION

This document contains information about examples used for testing *OpenCMISS-iron*. Read: How-to¹ and [1].

1.1 Cmgui files for cmgui-2.9

1.2 Variations to consider

- Geometry and topology
 - 1D, 2D, 3D
 - Length, width, height
 - Number of elements
 - Interpolation order
 - Generated or user meshes
 - quad/hex or tri/tet meshes
- Initial conditions
- Load cases
 - Dirichlet BC
 - Neumann BC
 - Volume force
 - Mix of previous items
- Sources, sinks
- Time dependence
 - Static
 - Quasi-static
 - Dynamic
- Material laws
 - Linear
 - Nonlinear (Mooney-Rivlin, Neo-Hookean, Ogden, etc.)
 - Active (Stress, strain)
- Material parameters, anisotropy
- Solver
 - Direct
 - Iterative
- Test cases
 - Numerical reference data
 - Analytical solution
- A mix of previous items

¹ <https://bitbucket.org/hessenthaler/opencmisshowto>

1.3 Folder structure

TBD..

2 HOW TO WORK ON THIS DOCUMENT

In the Google Doc at https://docs.google.com/spreadsheets/d/1RGKj8vVPqQ-PH0UwMX_e9TAzqaYavKi0z0D4pKY9RGI/edit#gid=0 please indicate what you are working on or if a given example was finished

- no mark: to be done
- x: currently working on it
- xx: done

Initials	Full name
CB	Christian Bleiler
AH	Andreas Hessenthaler
TK	Thomas Klotz
AK	Aaron Krämer
BM	Benjamin Maier
SM	Sergio Morales
MM	Mylena Mordhorst
HS	Harry Saini

Table 1: Initials of people working on examples, in alphabetical order (surnames).

3 DIFFUSION EQUATION

3.1 Equation in general form

The governing equation is,

$$\partial_t u + \nabla \cdot [\sigma \nabla u] = f, \quad (1)$$

with conductivity tensor σ . The conductivity tensor is,

- defined in material coordinates (fibre direction),
- diagonal,
- defined per element.

3.2 Example-0001

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.2.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1], \quad (2)$$

with boundary conditions

$$u = 0 \quad x = y = 0, \quad (3)$$

$$u = 1 \quad x = 2, y = 1. \quad (4)$$

No material parameters to specify.

3.2.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1] \times [0, 1], \quad (5)$$

with boundary conditions

$$u = 0 \quad x = y = z = 0, \quad (6)$$

$$u = 1 \quad x = 2, y = z = 1. \quad (7)$$

No material parameters to specify.

3.2.3 Computational model

- Commandline arguments are:
 - float: length along x-direction
 - float: length along y-direction
 - float: length along z-direction (set to zero for 2D)
 - integer: number of elements in x-direction
 - integer: number of elements in y-direction
 - integer: number of elements in z-direction (set to zero for 2D)
 - integer: interpolation order (1: linear; 2: quadratic)
 - integer: solver type (0: direct; 1: iterative)
- Commandline arguments for tests are:
 - 2.0 1.0 0.0 2 1 0 1 0
 - 2.0 1.0 0.0 4 2 0 1 0
 - 2.0 1.0 0.0 8 4 0 1 0
 - 2.0 1.0 0.0 2 1 0 2 0
 - 2.0 1.0 0.0 4 2 0 2 0
 - 2.0 1.0 0.0 8 4 0 2 0
 - 2.0 1.0 0.0 2 1 0 1 1
 - 2.0 1.0 0.0 4 2 0 1 1

```

2.0 1.0 0.0 8 4 0 1 1
2.0 1.0 0.0 2 1 0 2 1
2.0 1.0 0.0 4 2 0 2 1
2.0 1.0 0.0 8 4 0 2 1
2.0 1.0 1.0 2 1 1 1 0
2.0 1.0 1.0 4 2 2 1 0
2.0 1.0 1.0 8 4 4 1 0
2.0 1.0 1.0 2 1 1 2 0
2.0 1.0 1.0 4 2 2 2 0
2.0 1.0 1.0 8 4 4 2 0
2.0 1.0 1.0 2 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1
2.0 1.0 1.0 8 4 4 1 1
2.0 1.0 1.0 2 1 1 2 1
2.0 1.0 1.0 4 2 2 2 1
2.0 1.0 1.0 8 4 4 2 1

```

3.2.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

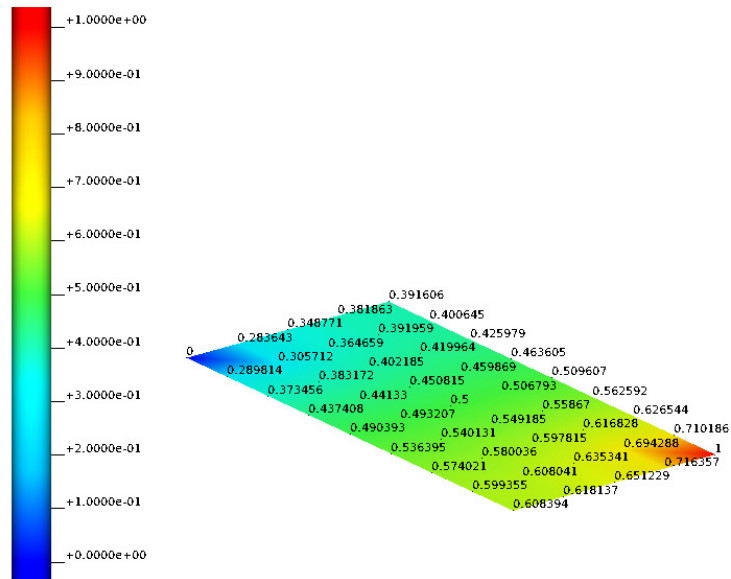


Figure 1: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 o].

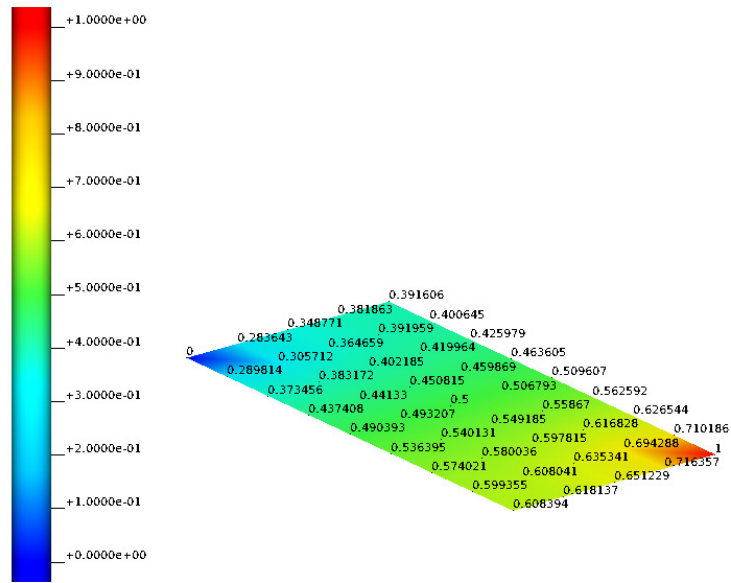


Figure 2: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

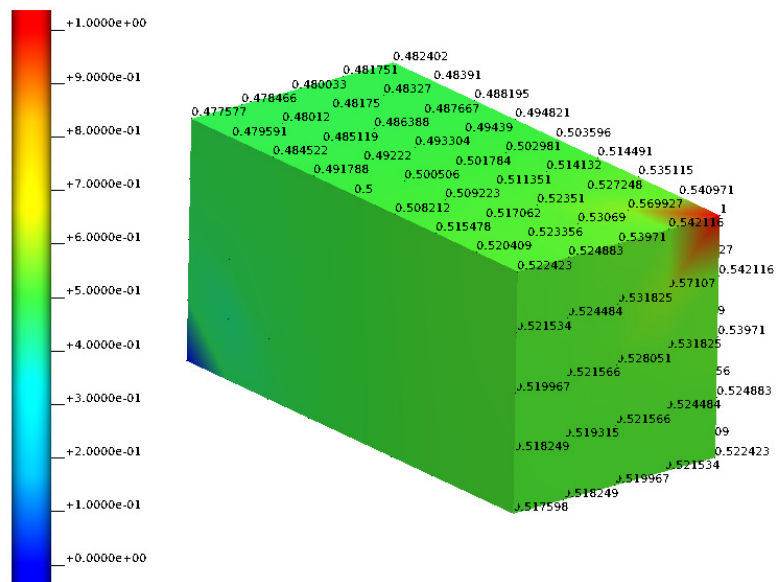


Figure 3: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].

3.3 Example-0001-u

Example uses user-defined regular meshes in CHeart mesh format and solves a static problem, i.e., applies the boundary conditions in one step.

3.3.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1], \quad (8)$$

with boundary conditions

$$u = 0 \quad x = y = 0, \quad (9)$$

$$u = 1 \quad x = 2, y = 1. \quad (10)$$

No material parameters to specify.

3.3.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1] \times [0, 1], \quad (11)$$

with boundary conditions

$$u = 0 \quad x = y = z = 0, \quad (12)$$

$$u = 1 \quad x = 2, y = z = 1. \quad (13)$$

No material parameters to specify.

3.3.3 Computational model

- Commandline arguments are:
 - float: length along x-direction
 - float: length along y-direction
 - float: length along z-direction (set to zero for 2D)
 - integer: number of elements in x-direction
 - integer: number of elements in y-direction
 - integer: number of elements in z-direction (set to zero for 2D)
 - integer: interpolation order (1: linear; 2: quadratic)
 - integer: solver type (0: direct; 1: iterative)
- Commandline arguments for tests are:
 - 2.0 1.0 0.0 2 1 0 1 0
 - 2.0 1.0 0.0 4 2 0 1 0
 - 2.0 1.0 0.0 8 4 0 1 0
 - 2.0 1.0 0.0 2 1 0 2 0
 - 2.0 1.0 0.0 4 2 0 2 0
 - 2.0 1.0 0.0 8 4 0 2 0
 - 2.0 1.0 0.0 2 1 0 1 1
 - 2.0 1.0 0.0 4 2 0 1 1

```

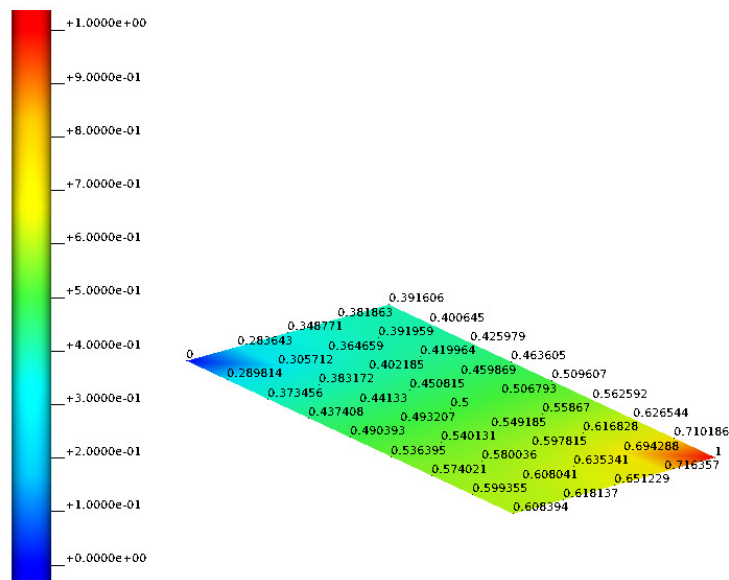
2.0 1.0 0.0 8 4 0 1 1
2.0 1.0 0.0 2 1 0 2 1
2.0 1.0 0.0 4 2 0 2 1
2.0 1.0 0.0 8 4 0 2 1
2.0 1.0 1.0 2 1 1 1 0
2.0 1.0 1.0 4 2 2 1 0
2.0 1.0 1.0 8 4 4 1 0
2.0 1.0 1.0 2 1 1 2 0
2.0 1.0 1.0 4 2 2 2 0
2.0 1.0 1.0 8 4 4 2 0
2.0 1.0 1.0 2 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1
2.0 1.0 1.0 8 4 4 1 1
2.0 1.0 1.0 2 1 1 2 1
2.0 1.0 1.0 4 2 2 2 1
2.0 1.0 1.0 8 4 4 2 1

```

- Note: Binary uses command line arguments to search for the relevant mesh files.

3.3.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.



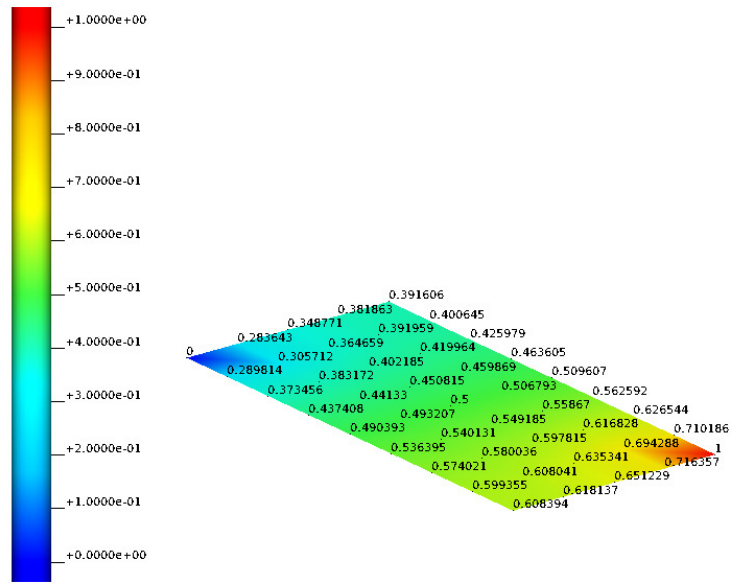


Figure 6: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

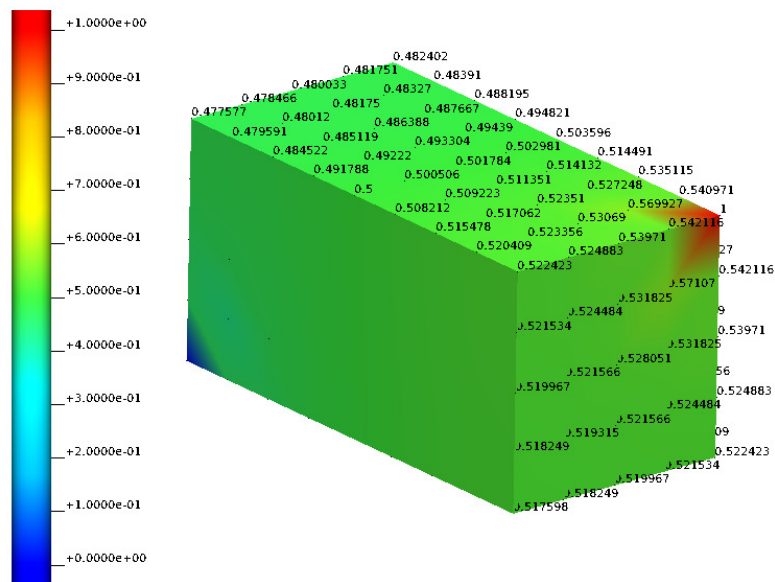


Figure 7: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].

3.4 Example-0002

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.4.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1], \quad (14)$$

with boundary conditions

$$u = 15y \quad x = 0, \quad (15)$$

$$u = 25 - 18y \quad x = 2. \quad (16)$$

No material parameters to specify.

3.4.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1] \times [0, 1], \quad (17)$$

with boundary conditions

$$u = 15y \quad x = 0, \quad (18)$$

$$u = 25 - 18y \quad x = 2. \quad (19)$$

No material parameters to specify.

3.4.3 Computational model

- Commandline arguments are:
 - float: length along x-direction
 - float: length along y-direction
 - float: length along z-direction (set to zero for 2D)
 - integer: number of elements in x-direction
 - integer: number of elements in y-direction
 - integer: number of elements in z-direction (set to zero for 2D)
 - integer: interpolation order (1: linear; 2: quadratic)
 - integer: solver type (0: direct; 1: iterative)
- Commandline arguments for tests are:
 - 2.0 1.0 0.0 2 1 0 1 0
 - 2.0 1.0 0.0 4 2 0 1 0
 - 2.0 1.0 0.0 8 4 0 1 0
 - 2.0 1.0 0.0 2 1 0 2 0
 - 2.0 1.0 0.0 4 2 0 2 0
 - 2.0 1.0 0.0 8 4 0 2 0
 - 2.0 1.0 0.0 2 1 0 1 1
 - 2.0 1.0 0.0 4 2 0 1 1

```

2.0 1.0 0.0 8 4 0 1 1
2.0 1.0 0.0 2 1 0 2 1
2.0 1.0 0.0 4 2 0 2 1
2.0 1.0 0.0 8 4 0 2 1
2.0 1.0 1.0 2 1 1 1 0
2.0 1.0 1.0 4 2 2 1 0
2.0 1.0 1.0 8 4 4 1 0
2.0 1.0 1.0 2 1 1 2 0
2.0 1.0 1.0 4 2 2 2 0
2.0 1.0 1.0 8 4 4 2 0
2.0 1.0 1.0 2 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1
2.0 1.0 1.0 8 4 4 1 1
2.0 1.0 1.0 2 1 1 2 1
2.0 1.0 1.0 4 2 2 2 1
2.0 1.0 1.0 8 4 4 2 1

```

3.4.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

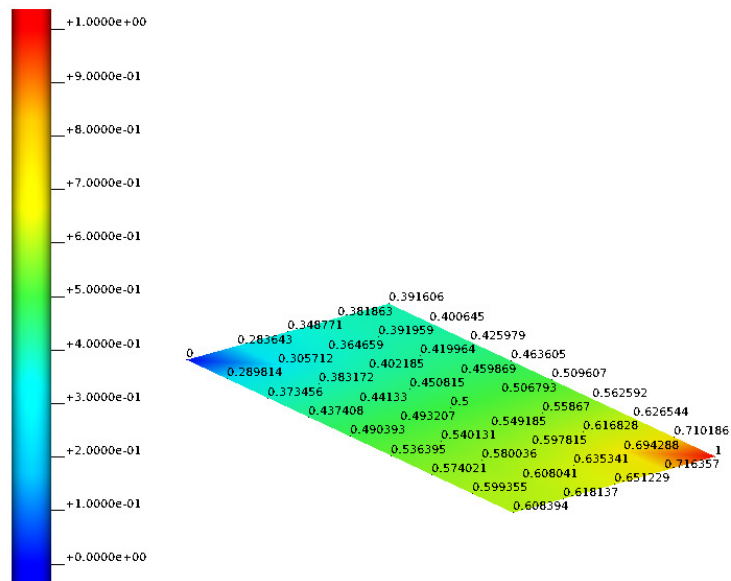


Figure 9: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 o].

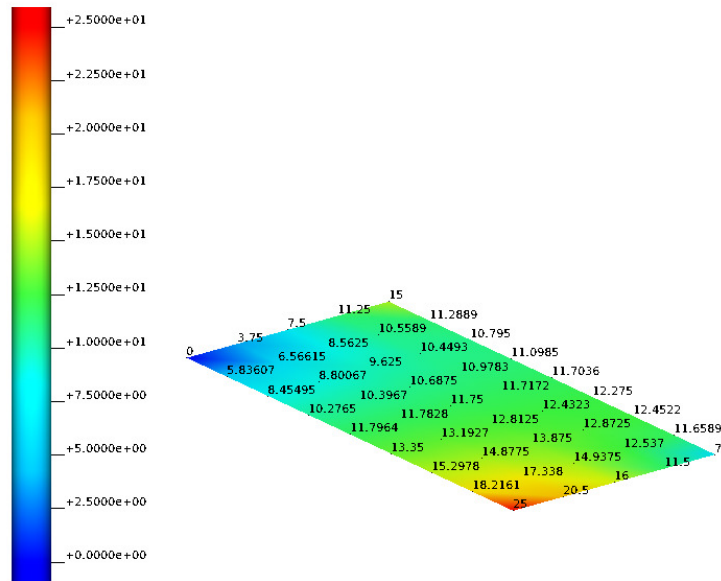


Figure 10: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

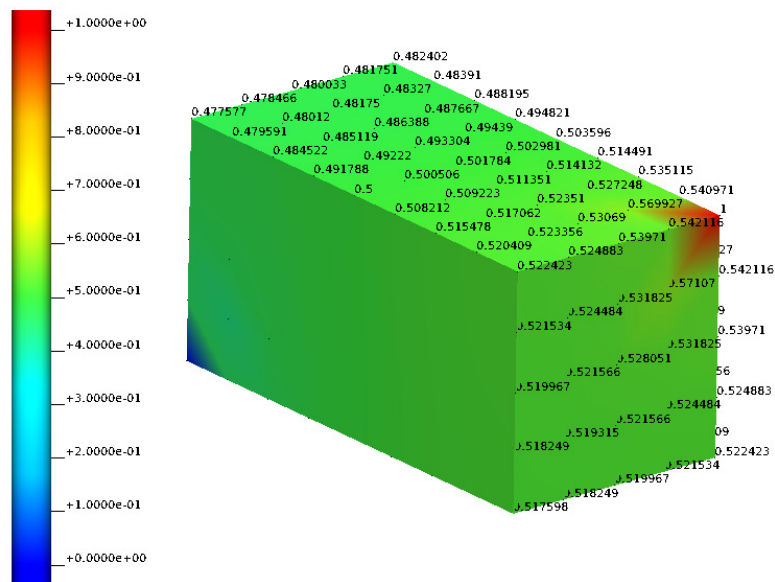


Figure 11: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 1 0].

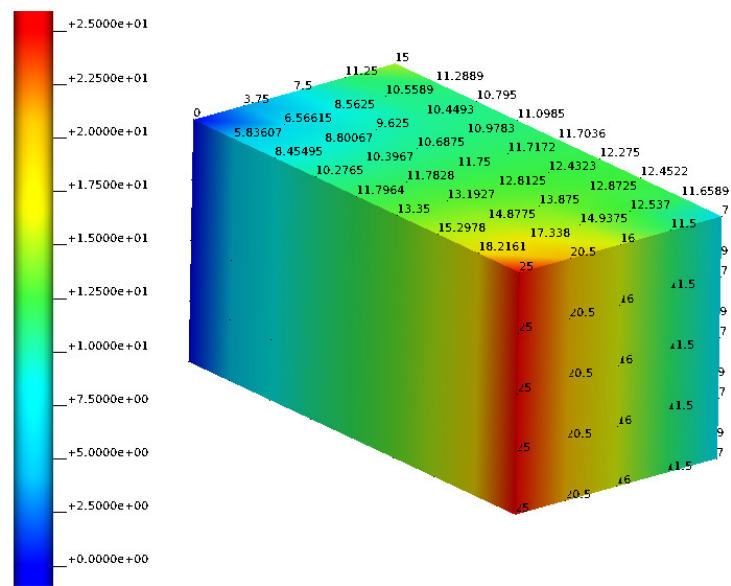


Figure 12: 3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0].

3.5 Example-0003

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.5.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1], \quad (20)$$

with boundary conditions

$$u = 15y \quad x = 0, \quad (21)$$

$$\partial_n u = 25 - 18y \quad x = 2. \quad (22)$$

No material parameters to specify.

3.5.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot \nabla u = 0 \quad \Omega = [0, 2] \times [0, 1] \times [0, 1], \quad (23)$$

with boundary conditions

$$u = 15y \quad x = 0, \quad (24)$$

$$\partial_n u = 25 - 18y \quad x = 2. \quad (25)$$

No material parameters to specify.

3.5.3 Computational model

- Commandline arguments are:
 - float: length along x-direction
 - float: length along y-direction
 - float: length along z-direction (set to zero for 2D)
 - integer: number of elements in x-direction
 - integer: number of elements in y-direction
 - integer: number of elements in z-direction (set to zero for 2D)
 - integer: interpolation order (1: linear; 2: quadratic)
 - integer: solver type (0: direct; 1: iterative)
- Commandline arguments for tests are:
 - 2.0 1.0 0.0 2 1 0 1 0
 - 2.0 1.0 0.0 4 2 0 1 0
 - 2.0 1.0 0.0 8 4 0 1 0
 - 2.0 1.0 0.0 2 1 0 2 0
 - 2.0 1.0 0.0 4 2 0 2 0
 - 2.0 1.0 0.0 8 4 0 2 0
 - 2.0 1.0 0.0 2 1 0 1 1
 - 2.0 1.0 0.0 4 2 0 1 1

```

2.0 1.0 0.0 8 4 0 1 1
2.0 1.0 0.0 2 1 0 2 1
2.0 1.0 0.0 4 2 0 2 1
2.0 1.0 0.0 8 4 0 2 1
2.0 1.0 1.0 2 1 1 1 0
2.0 1.0 1.0 4 2 2 1 0
2.0 1.0 1.0 8 4 4 1 0
2.0 1.0 1.0 2 1 1 2 0
2.0 1.0 1.0 4 2 2 2 0
2.0 1.0 1.0 8 4 4 2 0
2.0 1.0 1.0 2 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1
2.0 1.0 1.0 8 4 4 1 1
2.0 1.0 1.0 2 1 1 2 1
2.0 1.0 1.0 4 2 2 2 1
2.0 1.0 1.0 8 4 4 2 1

```

3.5.4 Result summary

We use CHeart rev. 6292 to produce numerical reference solutions.

Passed tests: 0 / 24

Failed tests:

current_run/l2x1x0_n2x1x0_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 44.2627
current_run/l2x1x0_n4x2x0_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 37.2770
current_run/l2x1x0_n8x4x0_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 32.2165
current_run/l2x1x0_n2x1x0_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 27.3358
current_run/l2x1x0_n4x2x0_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 22.1869
current_run/l2x1x0_n8x4x0_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 19.7449
current_run/l2x1x0_n2x1x0_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 44.2627
current_run/l2x1x0_n4x2x0_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 37.2770
current_run/l2x1x0_n8x4x0_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 32.2165
current_run/l2x1x0_n2x1x0_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 27.3358
current_run/l2x1x0_n4x2x0_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 22.1869
current_run/l2x1x0_n8x4x0_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 19.7449
current_run/l2x1x1_n2x1x1_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 124.749
current_run/l2x1x1_n4x2x2_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 128.672
current_run/l2x1x1_n8x4x4_i1_s0/Example.part0.exnode	CHeart	- Iron	_2 = 143.606
current_run/l2x1x1_n2x1x1_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 94.2619
current_run/l2x1x1_n4x2x2_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 98.7606
current_run/l2x1x1_n8x4x4_i2_s0/Example.part0.exnode	CHeart	- Iron	_2 = 118.047
current_run/l2x1x1_n2x1x1_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 124.749
current_run/l2x1x1_n4x2x2_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 128.672
current_run/l2x1x1_n8x4x4_i1_s1/Example.part0.exnode	CHeart	- Iron	_2 = 143.606
current_run/l2x1x1_n2x1x1_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 94.2619
current_run/l2x1x1_n4x2x2_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 98.7606
current_run/l2x1x1_n8x4x4_i2_s1/Example.part0.exnode	CHeart	- Iron	_2 = 118.047

Figure 13: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

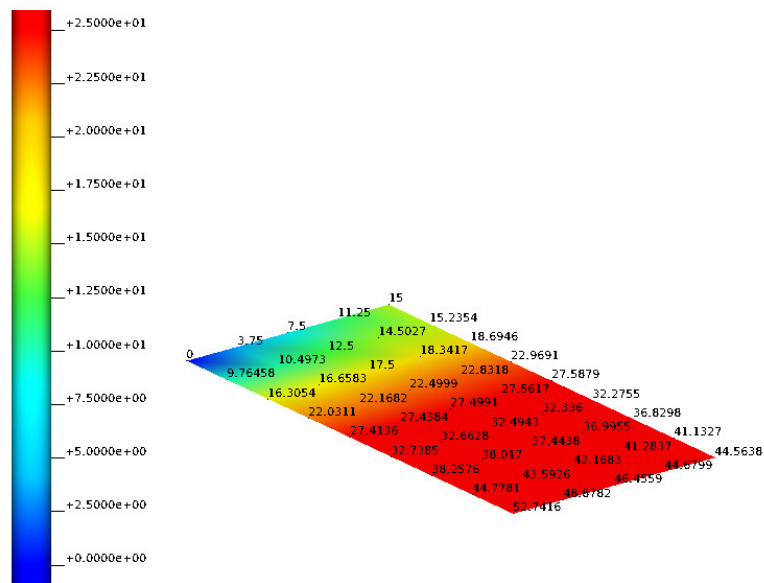
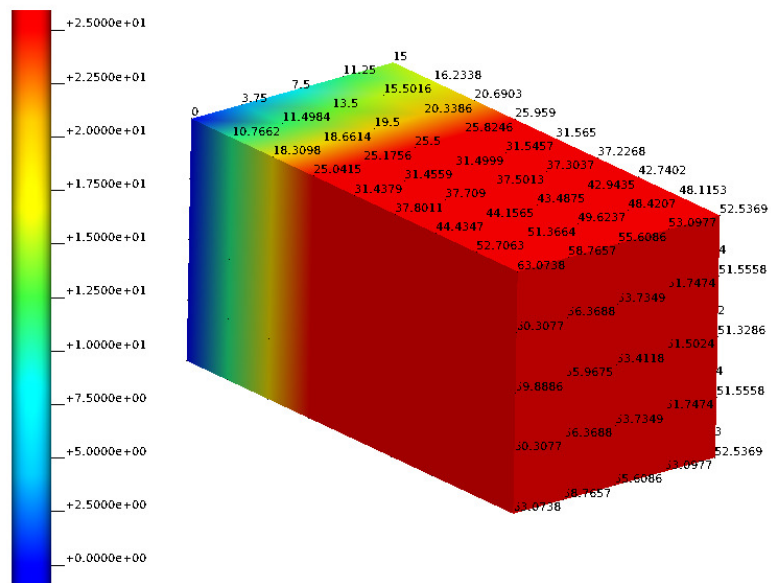


Figure 14: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0].

Figure 15: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 o].



3.6 Example-0011

Example uses generated regular meshes and solves a static problem, i.e., applies the boundary conditions in one step.

3.6.1 Mathematical model - 2D

We solve the following scalar equation,

$$\nabla \cdot [\sigma \nabla u] = 0 \quad \Omega = [0, 2] \times [0, 1], \quad (26)$$

with boundary conditions

$$u = 0 \quad x = y = 0, \quad (27)$$

$$u = 1 \quad x = 2, y = 1. \quad (28)$$

The conductivity tensor is defined as,

$$\sigma(x, t) = \sigma = \mathbf{I}. \quad (29)$$

3.6.2 Mathematical model - 3D

We solve the following scalar equation,

$$\nabla \cdot [\sigma \nabla u] = 0 \quad \Omega = [0, 2] \times [0, 1] \times [0, 1], \quad (30)$$

with boundary conditions

$$u = 0 \quad x = y = z = 0, \quad (31)$$

$$u = 1 \quad x = 2, y = z = 1. \quad (32)$$

The conductivity tensor is defined as,

$$\sigma(x, t) = \sigma = \mathbf{I}. \quad (33)$$

3.6.3 Computational model

- Commandline arguments are:
 - float: length along x-direction
 - float: length along y-direction
 - float: length along z-direction (set to zero for 2D)
 - integer: number of elements in x-direction
 - integer: number of elements in y-direction
 - integer: number of elements in z-direction (set to zero for 2D)
 - integer: interpolation order (1: linear; 2: quadratic)
 - integer: solver type (0: direct; 1: iterative)
 - float: σ_{11}
 - float: σ_{22}
 - float: σ_{33} (ignored for 2D)

- Commandline arguments for tests are:

```

2.0 1.0 0.0 2 1 0 1 0 1 1
2.0 1.0 0.0 4 2 0 1 0 1 1
2.0 1.0 0.0 8 4 0 1 0 1 1
2.0 1.0 0.0 2 1 0 2 0 1 1
2.0 1.0 0.0 4 2 0 2 0 1 1
2.0 1.0 0.0 8 4 0 2 0 1 1
2.0 1.0 0.0 2 1 0 1 1 1 1
2.0 1.0 0.0 4 2 0 1 1 1 1
2.0 1.0 0.0 8 4 0 1 1 1 1
2.0 1.0 0.0 2 1 0 2 1 1 1
2.0 1.0 0.0 4 2 0 2 1 1 1
2.0 1.0 0.0 8 4 0 2 1 1 1
2.0 1.0 1.0 2 1 1 1 0 1 1 1
2.0 1.0 1.0 4 2 2 1 0 1 1 1
2.0 1.0 1.0 8 4 4 1 0 1 1 1
2.0 1.0 1.0 2 1 1 2 0 1 1 1
2.0 1.0 1.0 4 2 2 2 0 1 1 1
2.0 1.0 1.0 8 4 4 2 0 1 1 1
2.0 1.0 1.0 2 1 1 1 1 1 1 1
2.0 1.0 1.0 4 2 2 1 1 1 1 1
2.0 1.0 1.0 8 4 4 1 1 1 1 1
2.0 1.0 1.0 2 1 1 2 1 1 1 1
2.0 1.0 1.0 4 2 2 2 1 1 1 1
2.0 1.0 1.0 8 4 4 2 1 1 1 1

```

3.6.4 *Result summary*

We use CHeart rev. 6292 to produce numerical reference solutions.

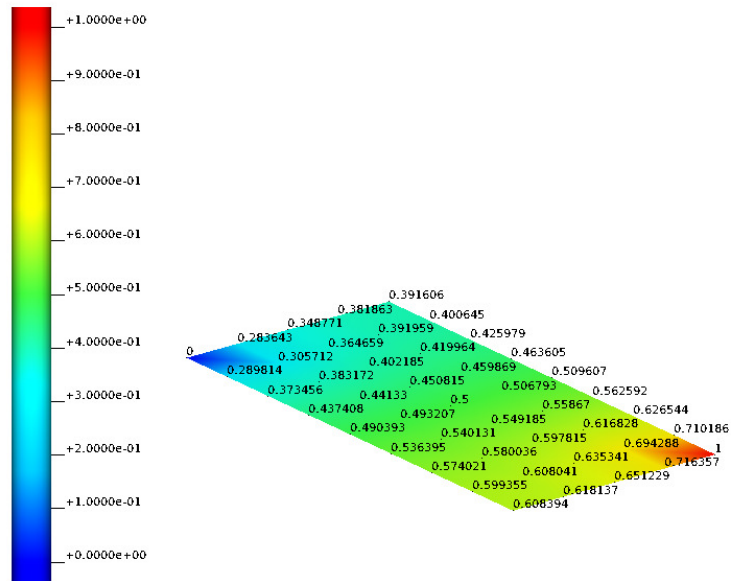


Figure 17: 2D results, iron reference w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0 1 1].

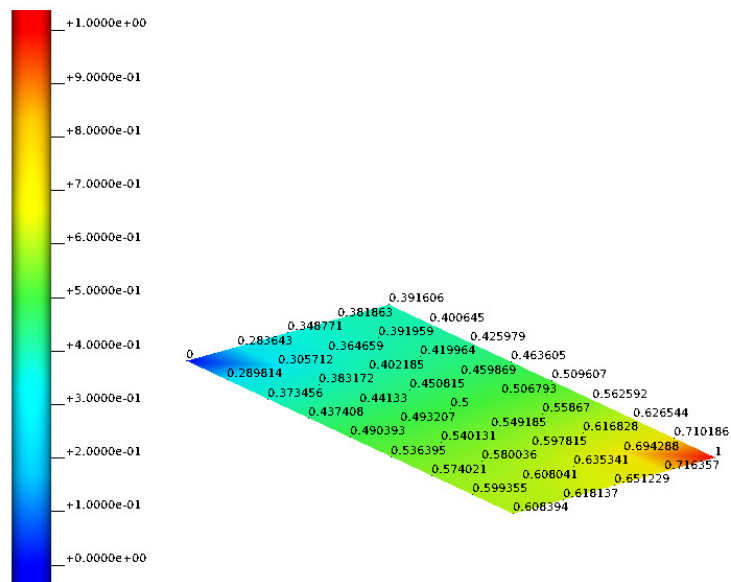


Figure 18: 2D results, current run w/ command line arguments [2.0 1.0 0.0 8 4 0 1 0 1 1].

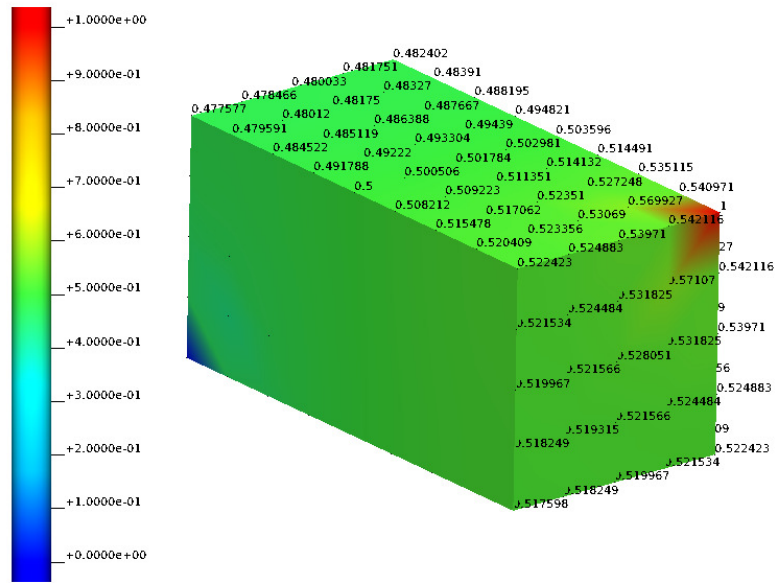


Figure 19: 3D results, iron reference w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 1 1 1].

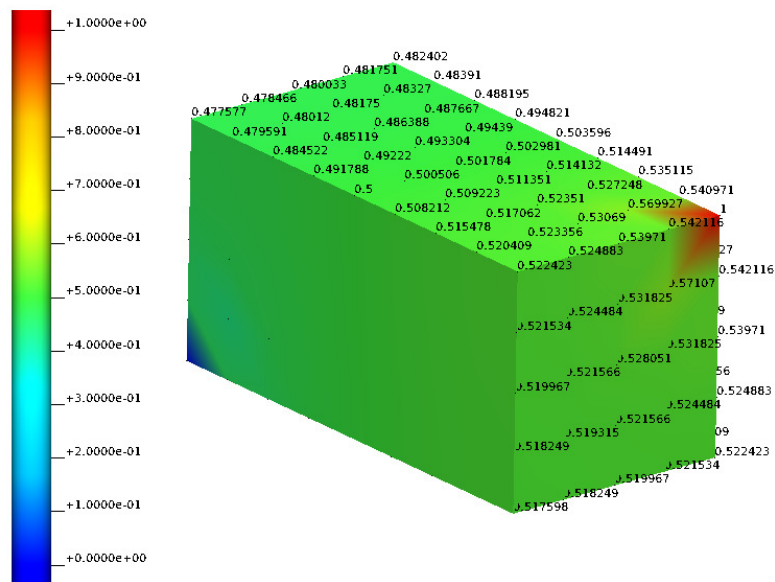


Figure 20: 3D results, current run w/ command line arguments [2.0 1.0 1.0 8 4 4 1 0 1 1 1].

4 LINEAR ELASTICITY

4.1 Equation in general form

$$\partial_{tt}\mathbf{u} + \nabla \cdot \boldsymbol{\sigma}(\mathbf{u}, t) = \mathbf{f}(\mathbf{u}, t) \quad (34)$$

4.2 Example-0101

4.2.1 Mathematical model

We solve the following equation,

$$\nabla \cdot \boldsymbol{\sigma}(\mathbf{u}, t) = \mathbf{0} \quad \Omega = [0, 160] \times [0, 120], t \in [0, 5], \quad (35)$$

with time step size $\Delta_t = 1$ and boundary conditions

$$\dots \quad \dots, \quad (36)$$

$$\dots \quad \dots \quad (37)$$

2D: specify thickness, Young's modulus and Poisson's ratio.

4.2.2 Computational model

- Length, width, height
- Direct/iterative solver
- Generated/user mesh
- Number of elements
- Interpolation order
- Number of solver steps (time steps, load steps)

4.2.3 Results

Figure 21: Results, analytical solution.

4.2.4 Validation

CHeart rev. 6328, Abaqus 2017, analytical reference solution, whatever...

Figure 22: Results, Abaqus reference.

Figure 23: Results, iron reference.

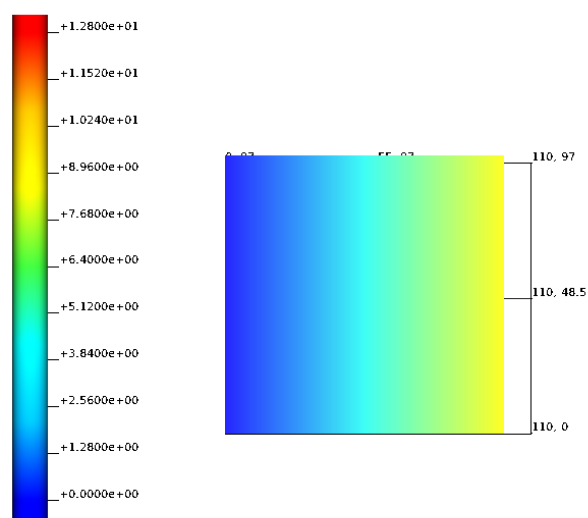


Figure 24: Results, current run.

5 FINITE ELASTICITY

6 NAVIER-STOKES FLOW

7 MONODOMAIN

8 CELLML MODEL

REFERENCES

- [1] Chris Bradley, Andy Bowery, Randall Britten, Vincent Budelmann, Oscar Camara, Richard Christie, Andrew Cookson, Alejandro F Frangi, Thiranjia Babarenda Gamage, Thomas Heidlauf, et al. Openmiss: a multi-physics & multi-scale computational infrastructure for the vph/-physiome project. *Progress in biophysics and molecular biology*, 107(1):32–47, 2011.