The xypdf package

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Abstract

The xypdf package improves the output quality of the Xy-pic package when PDF documents are generated. It produces generic PDF code for graphical elements like lines, curves and circles instead of approximating these elements with glyphs in special fonts as the original Xy-pic package does. The xypdf package works with both T_EX and E^TEX in the occurrences of pdfTEX, X_TTEX and ε -TEX with dvipdfm(x) to generate PDF files. xypdf is being integrated and distributed together with X_T -pic, starting with X_T -pic version 3.8.

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1 Introduction

The Xy-pic package is a utility for typesetting diagrams in TEX and IATEX documents. The authors of the Xy-pic package put much effort into the feature that most graphical elements are coded within the limited possibilities of the device independent file format (DVI). The diagrams can thus be generated with even the most basic TEX systems and displayed universally by all device drivers. For example, diagonal lines are composed of short dashes, which are glyphs in a special font. Since there are dashes in 127 discrete directions in the font xydash10, diagonal lines which do not match one of these slopes look slightly rugged when they are magnified.

For a better output quality in Postscript files, the authors of the Xy-pic package provided a Postscript backend for DVI-to-Postscript drivers. These extensions draw lines and curves by generic Postscript commands, thus trading a much better output quality against universality of the produced DVI files.

The development of the present package was based on Xy-pic version 3.7, from 1999, where there is no support for pdfTeX. In order to produce PDF files with high-quality Xy-pic diagrams, users had to use so far the Postscript file format as an intermediate step or embed the diagrams as external graphics. However, since many users directly generate PDF files from the TeX or DVI files (with bookmarks, hyperlinks and other PDF features), it is highly desirable to also have the possibility of directly generating Xy-pic diagrams with high-quality PDF graphics elements.

The PDF driver provided by the xypdf package adapts the output routines of the Xy-pic package to generate high-quality graphics for PDF output. It works with both pdfTEX and the two-step compilation TEX \rightarrow dvipdfm(x) with an intermediate DVI file. Thus, it also works with X \equiv TEX since this program internally uses a modification of dvipdfmx. Note that some version of ε -TEX is needed (which is anyway used by default in modern TEX installations). Figure 1 compares the output quality of a small Xy-pic diagram.

The xypdf package is very similar to the Postscript drivers for Xy-pic. It does not have (yet) all of their features (see Section 4) but is much more powerful in other respects, e.g. when drawing multiple curves. In general, it greatly improves graphics quality. Currently, the following features are implemented:

- Both straight lines and curves (solid, dashed, dotted and squiggled) are drawn by generic PDF commands.
- Xy-pic automatically draws the symbols of which lines and curves are composed at the very beginning and end of a segment. It then distributes the inner symbols evenly

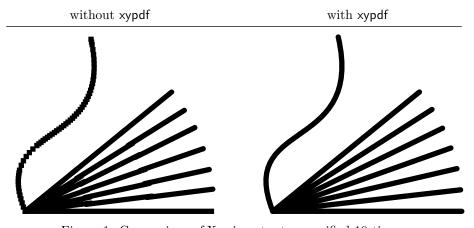


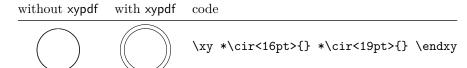
Figure 1: Comparison of Xy-pic output, magnified 10 times.

across the segment. Since the arc length of a Bézier curve is normally not proportional to its parameter, this is a nontrivial task in the case of curves. The xypdf package handles this better than the original code. Compare the output in Figure 2.

 As a highlight, xypdf features a Bézier curve offset algorithm, producing high-quality curves with two or three parallel strokes.

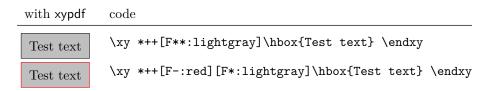


• The \cir object draws circles of arbitrary radius.



• xypdf supports the "rotate" extension of Xy-pic.

• xypdf supports the "frame" extension of Xy-pic. The only intended difference to the Postscript drivers is the appearance of the {**} fill style. The postscript drivers fill the frame and stroke it with a line of thickness 0. The PDF driver strokes the region instead with a black line which is half as thick as the normal lines. Tip: If you want a colored boundary, overlay two frames.



• xypdf supports the "color" extension of Xy-pic. As described in the Xy-pic Reference Manual, colors can be defined by the \newcycolor command, e.g.

```
\newxycolor{mygreen}{.5 0 1 .5 cmyk}
```

In addition, if the command \color is defined, e.g. if the color¹ or xcolor² package has been loaded, xypdf recognizes the named colors from these packages and uses the mechanisms from these packages to set colors in the output DVI or PDF file.

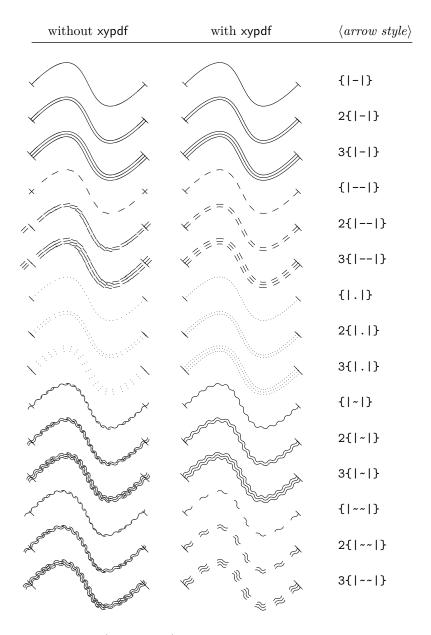
An example:

Orange Green

This was generated by \usepackage{xcolor} in the document preamble and the following code:

¹http://www.ctan.org/tex-archive/macros/latex/required/graphics/

²http://www.ctan.org/tex-archive/macros/latex/contrib/xcolor/



Code: \xy (0,0) \ar $@(arrow\ style)@`\{(20,20),(10,-20)\}\ (30,0) \$

Figure 2: Comparison of Xy-pic output for curves with various line styles.

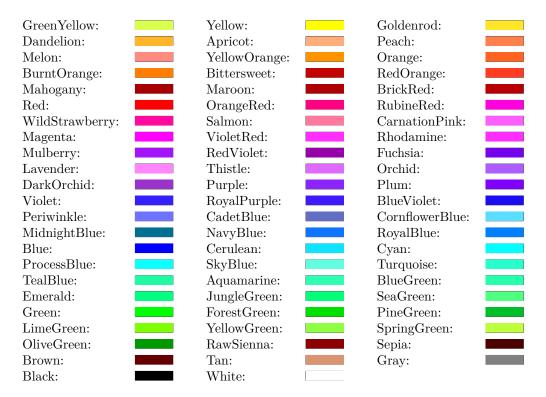


Figure 3: Additional color names provided by \UseCrayolaColors.

```
\definecolor{mygreen}{cmyk}{.5 0 1 .5}
\xymatrix{*+[orange] [F-:blue]\hbox{Orange}
& *[mygreen]\hbox{Green}}
```

When a named color has been defined by both \newxycolor and by a color package command like \definecolor, the Xy-pic definition overrides the general one.

The Xy-pic command \UseCrayolaColors defines a set of color names, as explained in the Xy-pic Reference Manual. Figure 3 lists these colors.

If you notice any unwanted behavior, please generate a minimal example and e-mail it to the author of this package. Current contact details are available at http://math.stanford.edu/~muellner. Please report situations where the algorithms produce arithmetic overflows. Also, the code is not really optimized for speed but for accuracy, so feel free to report a significant slowdown of the compiling process for your thesis/paper/book.

2 Usage

```
Use pdf as an option to the Xy-pic package, as in \usepackage[pdf]{xy}
or
\usepackage{xy}
\xyoption{pdf}
for IATEX and
```

\input xy
\xyoption{pdf}

for plain TEX. Do not use one of the other driver options to XY-pic like dvips, since combining two drivers will most likely result in mutilated diagrams.

The xypdf functionality can be switched off and on within the document by \xypdfoff and \xypdfon.

When you use plain TEX, make sure that xypdf is loaded after any global changes to the math fonts.

3 Acknowledgements

Since the xypdf package extends Xy-pic, some ideas are adopted from this package and its Postscript backend, and the author gratefully acknowledges the service which Kristoffer H. Rose and Ross Moore did to the mathematical community with their original package.

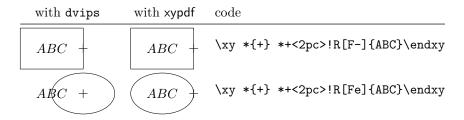
4 To do

• Support for the "line" extension.

5 Differences between xypdf and the dvips backend

Most users of xypdf will have used the dvips backend before. In this section, we list the the intentional differences between xypdf's behavior and the dvips driver. If you see further differences which are not mentioned here, this could be a bug, and please notify the author, Daniel Müllner.

• xypdf draw frames always around the current point c.



• The center of rotation and scaling is always the current point c.

with dvips with xypdf code
$$\frac{ABCDEF}{ABCDEF} = \frac{ABCDEF}{ABCDEF} = \frac{ABCDEF}{ABCDEF$$

• Line frames which are drawn as \frm objects are always black with the dvips backend, as opposed to filled frames. xypdf changes the color for both line and filled frames.

with dvips	with xypdf	code
		\xy *+<2pc,1pc>[o]{} *[orange]\frm{e} \endxy
	'	<pre>\xy *+<2pc,1pc>[o]{} *[orange]\frm{**} \endxy</pre>

The [F...] object modifiers give the same colors to frames with both drivers.

6 The fine print: curves with multiple segments

Since the dashes in Bézier segments are aligned to the boundary points, this would result in dashes of double length when a curve is composed of several Bézier segments, as shown in the upper left diagram in Figure 4. To avoid this, xypdf records the end point of each segment and adapts the dash pattern whenever the starting point of a segment coincides with the end point of the previous one (see the upper right diagram). Analogous improvements apply to the "dotted" and "squiggled" line styles.

Since this mechanism does not exist in the original Xy-pic, it can be switched on and off by \xypdfcontpatternon and \xypdfcontpatternoff. By default, it is switched on.

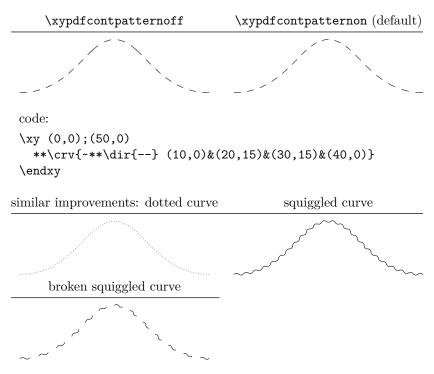


Figure 4: Seamless patterns for curves with multiple segments.

7 Troubleshooting

 \bullet I get the error message pdfTeX version 1.40.0 or higher is needed for the xypdf package with PDF output

You seem the use an old version of pdfTEX. If you cannot update your TEX system for some reason, you may still use the xypdf package in DVI mode and produce a PDF file via dvipdfm(x). The pathway TEX \rightarrow dvipdfm(x) is preferable in many cases anyway since it usually produces much smaller PDF files.

• I get the error message eTeX is needed for the xypdf package.

In your TEX installation, the ε -TEX features are not enabled, although they most certainly can be in any reasonably modern TEX installation. You must probably rebuild the TEX and LATEX format files with ε -TEX enabled. Please consult the documentation of your TEX distribution on how to rebuild the format files.

8 Copyright, license and disclaimer

The copyright for the xypdf package is by its author, Daniel Müllner. Current contact details will be maintained at http://math.stanford.edu/~muellner.

The xypdf package is free software: you can redistribute it and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation, either version 2 of the License, or (at your option) any later version. This license is available at http://www.gnu.org/licenses.

This program is distributed in the hope that it will be useful, but without any warranty; without even the implied warranty of merchantability or fitness for a particular purpose. See the GNU General Public License for more details.

9 Implementation

This is the code for the file xypdf.tex. From version 1.4 on, it is loaded as the option pdf to Xy-pic.

```
\xypdfversion
                 \xyprovide defines \xypdfversion.
     \xypdfdate
                    1 (*basic)
                    2 \ifx\xyloaded\undefined\input xy \fi
                    3 \xyprovide{pdf}{PDF driver}{1.7}%
                    4 {Daniel M\"ullner\newline}%
                    5 {\url{http://math.stanford.edu/~muellner}}{}
                    6 \ifx\makeatletter\undefined\input miniltx \fi
                    7 \newcommand*\xypdfdate{2011/03/20}
                    8 \newdriver{%
                       \xyaddsupport{pdf}\xP@pdf@on
                   10
                       \xyaddsupport{color}\xP@color@on
                       \xyaddsupport{curve}\xP@curve@on
                   11
                       \xyaddsupport{frame}\xP@frame@on
                   12
                   13 % \xyaddsupport{line}\xP@line@on
                   14 \xyaddsupport{rotate}\xP@rotate@on
                   16 \xyaddunsupport{pdf}\xP@pdf@off
                   17 \xyaddunsupport{color}\xP@color@off
                   18 \xyaddunsupport{curve}\xP@curve@off
                   19 \xyaddunsupport{frame}\xP@frame@off
                   20 %\xyaddunsupport{line}\xP@line@off
                   21 \xyaddunsupport{rotate}\xP@rotate@off
                 See the end of the file for the code that loads the other files xypdf-*.tex.
       \xypdfon
                 Commands for switching the driver on and off.
      \xypdfoff
                   22 \newcommand*\xypdfon{%
                       \xP@pdf@on
                   23
                   24 \xP@color@on
                   25
                       \xP@curve@on
                   26
                       \xP@frame@on
                        \xP@line@on
                   27
                   28
                       \xP@rotate@on
                   29 }
                   30 \newcommand*\xypdfoff{%
                       \xP@pdf@off
                   31
                       \xP@color@off
                   32
                       \xP@curve@off
                      \xP@frame@off
                       \xP@line@off
                   35
                       \xP@rotate@off
                   36
                   37 }
                 Test for \varepsilon-T<sub>F</sub>X
                   38 \ifx\unexpanded\@undefined
                       \PackageError{xypdf}{eTeX is needed for the xypdf package}{}
                   40 \fi
\xP@testpdfsave Test for \pdfsave, which was introduced in pdfTFX version 1.40.0.
                   41 \newcommand*\xP@testpdfsave{%
                        \ifpdf
                   42
                          \ifx\pdfsave\@undefined
                   43
```

```
\PackageError{xypdf}{pdfTeX version 1.40.0 or higher is needed for the %
                  44
                  45
                             xypdf^^J%
                  46
                             package with PDF output}{}%
                         \fi
                  47
                      \fi
                  48
                      \let\xP@testpdfsave\@undefined
                  49
                  50 }
   \xP@warning Check for \PackageWarning.
                  51 \ifx\PackageWarning\@undefined
                      \newcommand*\xP@warning[2]{{%
                         \newlinechar'\^^J%
                  53
                         \@warning{Package #1 Warning: #2\@empty.}%
                  54
                      }}
                  55
                  56 \else
                  \tt 57 \qquad \verb|\newcommand*| xP@warning{\PackageWarning}|
                  58 \fi
    \xP@pdf@on The following initializations are necessary for each supported extension, otherwise the
   \xP@pdf@off
                \xP@hook commands will not work.
                  59 \newcommand*\xP@pdf@on{}
                  60 \newcommand*\xP@pdf@off{}
  \xP@color@on
 \xP@color@off
                  61 \newcommand*\xP@color@on{}
                  62 \newcommand*\xP@color@off{}
  \xP@curve@on
 \xP@curve@off
                  63 \newcommand*\xP@curve@on{}
                  64 \newcommand*\xP@curve@off{}
  \xP@frame@on
 \xP@frame@off
                  65 \newcommand*\xP@frame@on{}
                  66 \newcommand*\xP@frame@off{}
  \xP@line@on
  \xP@line@off
                  67 \newcommand*\xP@line@on{}
                  68 \newcommand*\xP@line@off{}
 \xP@rotate@on
\xP@rotate@off
                  69 \newcommand*\xP@rotate@on{}
                  70 \newcommand*\xP@rotate@off{}
      \xP@hook Commands for switching the driver on and off.
                  71 \newcommand*\xP@hook[2]{%
                      \edef\next@{%
                  73
                         \let\expandafter\noexpand\csname xP@old@#2\endcsname
                           \expandafter\noexpand\csname#2\endcsname}%
                  74
                  75
                      \expandafter\edef\csname xP@#1@on\endcsname{%
                  76
                         \unexpanded\expandafter\expandafter\expandafter{\csname xP@#1@on\endcsname}%
                  77
                  78
                         \let\expandafter\noexpand\csname#2\endcsname
                  79
                           \expandafter\noexpand\csname xP@#2\endcsname
                  80
                      }%
                      \expandafter\edef\csname xP@#1@off\endcsname{%
                  81
```

```
82
                           \unexpanded\expandafter\expandafter\expandafter{\csname xP@#1@off\endcsname}%
                     83
                            \let\expandafter\noexpand\csname#2\endcsname
                     84
                              \expandafter\noexpand\csname xP@old@#2\endcsname
                     85
                         }%
                     86 }
                   Two possibilities to insert literal PDF commands, one for pdftex and one for dvipdfm(x).
\xP@defpdfliteral
                   The command \xP@cm changes the current transformation matrix.
      \xP@literal
           \xP@cm
                     87 \newcommand*\xP@defpdfliteral{%
     \xP@setcolor
                     88 \ifpdf
   \xP@resetcolor
                          \newcommand*\xP@literal[1]{\pdfsave\pdfliteral{##1}\pdfrestore}
                     89
                          \newcommand*\xP@cm[5]{%
                     90
                     91
                            \pdfsave
                     92
                            \pdfsetmatrix{##1 ##2 ##3 ##4}%
                     93
                            ##5%
                     94
                            \pdfrestore
                     95
                         }
                   Mimick pdftex.def from the graphicx package.
                          \@ifundefined{@pdfcolorstack}{%
                            \def\@pdfcolorstack{\z@}%
                     97
                         }{}%
                     98
                          \newcommand*\xP@setcolor[3]{%
                     99
                    100
                            \pdfcolorstack\@pdfcolorstack push{##1 ##2 ##1 ##3}}
                    101
                          \newcommand*\xP@resetcolor{\pdfcolorstack\@pdfcolorstack pop\relax}%
                    102 \else
                          \newcommand*\xP@literal{%
                    103
                            \xP@warning{xypdf}{%
                    104
                            The produced DVI file is NOT PORTABLE. Convert it with ^ J%
                    105
                            dvipdfm(x) to the PDF format but do not expect the DVI file itself to be^^J%
                    106
                            displayed correctly\@gobble}%
                    107
                            \global\let\xP@literal\xP@literal@
                    108
                            \xP@literal
                    109
                         }
                    110
                          \newcommand*\xP@literal@[1]{\special{pdf:content ##1}}
                    111
                          \newcommand*\xP@cm[5]{%
                    112
                    113
                            \special{pdf:btrans matrix ##1 ##2 ##3 ##4 0 0}%
                    114
                            ##5%
                            \special{pdf:etrans}%
                    115
                         }
                    116
                          \newcommand*\xP@setcolor[3]{\special{pdf:bcolor[##1]}}
                    117
                          \newcommand*\xP@resetcolor{\special{pdf:ecolor}}%
                    118
                    119 \fi
                    120 \let\xP@defpdfliteral\@undefined
                   Rely on the ifpdf package to test for PDF output. The \AtEndOfPackage is necessary if
                   xypdf is loaded as an option in \sp = (options)  {xy}. If it is called as a plain \sp = T_E X
                   package, the commands below can be executed immediately.
                    122 \DN@{\@firstofone}
                    123 \DNii@{xy}
                    124 \ifx\@currname\nextii@
                    125
                         \ifx\AtEndOfPackage\@undefined
                    126
                          \else
                            \DN@{\AtEndOfPackage}%
                    127
                    128
                         \fi
```

```
129 \fi
                130 \next@
                131 {\RequirePackage{ifpdf}%
                     \xP@testpdfsave
                132
                     \xP@defpdfliteral}
               Set the precision for dimension output according to pdfTFX's \pdfdecimaldigits. If this
  \xP@digits
               number is not defined, use dvipdfm's default precision, which is two decimals.
                134 \ifx\pdfdecimaldigits\@undefined
                135
                     \newcommand*\xP@digits{2}
                136 \else
                137
                    \@ifdefinable\xP@digits\relax
                138
                     \xdef\xP@digits{\the\pdfdecimaldigits}
                139
                     \ifnum\pdfdecimaldigits<2
                140
                       \xP@warning{xypdf}{%
                141
                         The precision in \string\pdfdecimaldigits\space is only \xP@digits\space
                142
                         decimals.^^J%
                         It is recommended to set \string\pdfdecimaldigits\space to 2 or 3 for %
                143
                         best output quality\@gobble}
                144
                145 \fi
                146 \fi
      \xP@dim Conversion between TFX points (pt) and PDF/Postscript points (bp)
                147 \newcommand*\xP@dim[1]{%
                     \expandafter\xP@removePT\the\dimexpr(#1)*800/803\relax\space}
               Precise conversion between T<sub>F</sub>X points (pt) and PDF/Postscript points (bp). No truncation.
                149 \newcommand*\xP@precdim[1]{\xP@EARPT\dimexpr(#1)*800/803\relax\space}
    \xP@EARPT
                150 \newcommand*\xP@EARPT{\expandafter\removePT@\the}
    \xP@coor Coordinates: two dimensions
                151 \newcommand*\xP@coor[1]{\xP@dim{#1}\xP@dim}
\xP@removePT
               The following two macros round and truncate a dimension to the desired number of decimal
               digits.
                152 \@ifdefinable\xP@removePT\relax
                153 {\@makeother\p\@makeother\t\gdef\xP@removePT#1pt{\xP@removePT@#10000@}}
\xP@removePT@
                154 \@ifdefinable\xP@removePT@\relax
                155 \ifcase\xP@digits
               0 decimals
                     \def\xP@removePT@#1.#2#3@{%
                156
                157
                       \int ifnum#2<5
                         #1%
                158
                       \else
                159
                         \theta = 1-\epsilon - 1-\epsilon
                160
                161
                    }
                162
                163 \or
```

```
1 decimal
164
      \def\xP@removePT@#1#2.#3#4#5@{%
165
        \int \frac{1}{100} 44<5
166
          #1#2%
167
          \if#30%
          \else
168
            .#3%
169
          \fi
170
        \else
171
 172
          \expandafter\xP@removePT
          173
174
175
      }
176 \or
2 decimals
177
      \def\xP@removePT@#1#2.#3#4#5#6@{%
178
        \int \frac{1}{100} 
          #1#2%
179
          \if#40%
180
            \if#30%
181
            \else
182
 183
               .#3%
            \fi
 184
          \else
185
            .#3#4%
186
          \fi
187
        \else
188
          \expandafter\xP@removePT
 189
190
          \theta^{1}=\frac{1}{2}.#3#4pt+\inf^{1}-\frac{1}{8}sp\
191
        \fi
    }
192
193 \or
3 decimals
      \def\xP@removePT@#1#2.#3#4#5#6#7@{%
195
        \infnum#6<5
196
          #1#2%
          \if#50%
197
            \if#40%
198
199
              \if#30%
200
              \else
201
                 .#3%
              \fi
202
            \else
203
              .#3#4%
204
            \fi
205
          \else
206
            .#3#4#5%
207
208
          \fi
209
        \else
210
          \expandafter\xP@removePT
          \theta^{1-\frac{1}{2}.\#3\#4\#5pt}
211
212
        \fi
      }
213
214 \or
4 decimals
```

```
\def\xP@removePT@#1#2.#3#4#5#6#7#8@{%
215
216
        \int \frac{\pi}{7}
217
          #1#2%
          \if#60%
218
            \if#50%
219
              \if#40%
220
                 \if#30%
221
                 \else
222
223
                   .#3%
                 \fi
224
               \else
225
                 .#3#4%
226
              \fi
227
            \else
228
 229
               .#3#4#5%
 230
            \fi
          \else
231
             .#3#4#5#6%
232
          \fi
233
234
        \else
          \expandafter\xP@removePT
235
          \theta^{1--fi8sp\relax}
236
237
        \fi
     }
238
239 \else
5 or more decimals: no truncation
240 \let\xP@dim\xP@precdim
241 \fi
```

\xP@lw Find out the default line width in the math fonts. This is done at the beginning of the \xP@preclw document, when hopefully all potential changes to math fonts have taken place.

242 \AtBeginDocument{%

Initialize math fonts

```
243 {\setboxz@h{$ $}}%
244 \@ifdefinable\xP@lw\relax
245 \@ifdefinable\xP@preclw\relax
246 \edef\xP@preclw{\the\fontdimen8\textfont3}%
247 \edef\xP@lw{\xP@dim\xP@preclw}%
248 \PackageInfo{xypdf}{Line width: \xP@preclw}%
249}
```

9.1 Straight lines

\line@ Also change the code for \dir{-} as an object. Now these dashes are not drawn from the dash font any more but by generic PDF line commands.

```
250 \xP@hook{pdf}{line@}
251 \newcommand*\xP@line@{%
     \setboxz@h{%
252
       \xP@setsolidpat
253
       \xP@stroke{0 0 m \xP@coor{\cosDirection\xydashl@}{\sinDirection\xydashl@}1}%
254
255
     \U@c\sinDirection\xydashl@
256
257
     D@c\z@
     \ifdim\U@c<\z@
258
       \multiply\U@c\m@ne
259
```

```
\xP@swapdim\U@c\D@c
                  ^{260}
                  261
                       \fi
                  ^{262}
                       \t \t \z \ \U \c
                       \dp\z@\D@c
                  263
                       \R@c\cosDirection\xydashl@
                  264
                       L@c\z@
                  265
                       \left( \frac{R@c}{z@} \right)
                  266
                          \multiply\R@c\m@ne
                  267
                  268
                          \xP@swapdim\L@c\R@c
                       \fi
                  269
                  270
                       \hskip\L@c\boxz@\hskip\R@c
                       271
                  272
                       \tmp@
                       \Edge@c={\rectangleEdge}%
                  273
                  274
                       \edef\Upness@{\ifdim\z@<\U@c1\else0\fi}%
                       \edf\Leftness @{\ifdim\z @<\L @c1\else 0\fi}\%
                       \def\Drop@@{\styledboxz@}%
                  276
                       \def\Connect@@{\solid@}%
                  277
                  278 }
        \solid@
                 This is the hook for solid straight lines. Derived from \xyPSsolid@ in xyps.tex.
     \xP@solid@
                  279 \xP@hook{pdf}{solid@}
                  280 \newcommand*\xP@solid@{\straight@\xP@solidSpread}
\xP@solidSpread
                  281 \ensuremath{\verb|Qifdefinable|xP@solidSpread|relax}
                  282 \def\xP@solidSpread#1\repeat@{{%
                 Neglect zero-length lines.
                       \@tempswatrue
                  283
                       \ifdim\X@p=\X@c
                  284
                  285
                       \left( Y@p=\right) Y@c
                  286
                         \@tempswafalse
                       \fi
                  287
                       \fi
                  288
                  289
                       \if@tempswa
                         \xP@setsolidpat
                  290
                  291
                          \xP@stroke{\xP@coor\X@p\Y@p m \xP@coor\X@c\Y@c 1}%
                  292
                       \fi
                  293 }}
    \xP@pattern
                  294 \newcommand*\xP@pattern{}
                 Pattern for solid lines
\xP@setsolidpat
                  295 \newcommand*\xP@setsolidpat{%
                       \def\xP@pattern{1 J 1 j []0 d}%
                       \global\let\xP@lastpattern\xP@solidmacro
                  298 }
     \xP@stroke
                  299 \newcommand*\xP@stroke[1]{\xP@literal{\xP@lw w \xP@pattern\space#1 S}}
         \dash@
                 This is the hook for dashed straight lines. Derived from \xyPSdashed@ in xyps.tex.
      \xP@dash@
                  300 \xP@hook{pdf}{dash@}
                  301 \newcommand\xP@dash@{\line@\def\Connect@@{\straight@\xP@dashedSpread}}
```

\xP@dashedSpread

```
302 \ensuremath{\mbox{\sc 0}}\ensuremath{\mbox{\sc 0}}\ensuremath{\mb
      303 \def\xP@dashedSpread#1\repeat@{{%
      304
                                                       \xP@veclen
Neglect zero-length lines.
                                                         \ifdim\@tempdimb>\z@
      305
      306
                                                                              \xP@setdashpat
      307
                                                                              \xP@savec
                                                                              \xP@stroke{\xP@coor\X@p\Y@p m \xP@coor\X@c\Y@c 1}%
      308
      309
                                                       \fi
      310 }}
```

\xP@setdashpat The formula for the dash length is the same as in the dashed operator in xypsdict.tex:

$$(\text{dash length}) = \frac{l}{2 \cdot \text{round} \left(\frac{l+d}{2d}\right) - 1},$$

where l is the length of the line and d is the minimal dash length.

The length l must be in $\backslash \texttt{Otempdimb}$. The dash length is returned in $\backslash \texttt{Otempdima}$.

```
311 \newcommand*\xP@setdashpat{%
312 \xP@testcont\xP@dashmacro
313 \ifxP@splinecont
```

Special pattern in case this line continues another dashed segment.

```
{\count@\numexpr2*((\@tempdimb-\xydashl@/3)/(2*\xydashl@))\relax
315
       \global\dimen@i
         \ifnum\count@>\z@
316
317
           \dimexpr\@tempdimb/\count@\relax
318
         \else
          \z@
319
320
        \fi
       }%
321
       \@tempdima\dimen@i
322
       \edef\xP@pattern{1 J 1 j [%
323
        \ifdim\@tempdima>\z@
324
          \xP@precdim\@tempdima]\xP@precdim\@tempdima
325
        \else
326
          ]0 %
327
        \fi
328
329
       d}%
330
     \else
331
       \@tempdima
        \ifdim\@tempdimb>\xydashl@
332
          333
334
        \else
335
          \z0
        \fi
336
       \edef\xP@pattern{1 J 1 j [%
337
         \ifdim\@tempdima>\z@\xP@precdim\@tempdima\fi
338
      ]0 d}%
339
     \fi
340
     \global\let\xP@lastpattern\xP@dashmacro
341
342 }
```

\xP@setcldashpat Dash pattern for closed paths. Offset is half of the dash length to avoid artifacts.

```
343 \newcommand*\xP@setcldashpat{%
                         {\count@\numexpr2*((\@tempdimb-\xydashl@/3)/(2*\xydashl@))\relax
                         \xdef\@gtempa{1 J 1 j [\ifnum\count@>\z@\xP@precdim{\@tempdimb/\count@}\fi]%
                           \ifnum\count@>\z@\xP@precdim{\@tempdimb*3/2/\count@}\else0 \fi d}%
                   346
                         }%
                   347
                         \edef\xP@pattern{\@gtempa}%
                   348
                   349 }
         \point@
                   This is the hook for points. Derived from \xyPSpoint@ in xyps.tex.
      \xP@point@
                   350 \xP@hook{pdf}{point@}
                   351 \newcommand*\xP@point@{\xP@zerodot\egroup\Invisible@false
                         \Hidden@false\def\Leftness@{.5}\def\U@pness@{.5}\ctipEdge@
                         \def\Drop@@{\styledboxz@}%
                   353
                         \def\Connect@0{\straight@\xP@dottedSpread}%
                   354
                   355 }
     \xP@zerodot
                   356 \newcommand*\xP@zerodot{%
                         \hb@xt@\z@{\hss}
                   357
                           \vbox to\z@{\vss\hrule\@width\xP@preclw\@height\xP@preclw\vss}%
                         \hss}%
                   359
                   360 }
\xP@dottedSpread
                   361 \@ifdefinable\xP@dottedSpread\relax
                   363
                         \xP@veclen
                         \ifdim\@tempdimb>\z@
                   364
                           \xP@setdottedpat
                    365
                    366
                           \xP@savec
                           \xP@stroke{\xP@coor\X@p\Y@p m \xP@coor\X@c\Y@c 1}%
                    367
                         \fi
                   368
                   369 }}
                  The formula for the distance between dots is the same as in the dotted operator in
\xP@setdottedpat
                   xypsdict.tex:
                                              (\text{dot distance}) = \frac{l}{\text{round}\left(\frac{l}{2\text{pt}}\right) + 1},
                   where l is the length of the line.
                      The length l must be in \backslash \texttt{Otempdimb}.
                   370 \newcommand*\xP@setdottedpat{%
                         \xP@testcont\xP@dotmacro
                   371
                         \ifxP@splinecont
                   372
                           \@tempdima\dimexpr\@tempdimb/(\@tempdimb/131072+1)-\xP@preclw\relax
                   373
                           \edef\xP@pattern{%
                   374
```

Advance the offset very slightly by 1sp to really hide the first dot in the viewer. (This improves the display at least in the author's PDF-Xchange viewer.)

379]\xP@precdim{\xP@preclw+1sp}d}%

\ifdim\@tempdima>\z@

Produce a dot pattern only when the segment is long enough.

\xP@precdim\xP@preclw\xP@precdim\@tempdima

0 J [%

375

376

377

378

```
380
                           \else
                             \advance\@tempdimb-\xP@preclw
                     381
                     382
                             \ifdim\@tempdimb<\z@\@tempdimb\z@\fi
                             \@tempdima\dimexpr\@tempdimb/(\@tempdimb/131072+1)-\xP@preclw\relax
                     383
                             \edef\xP@pattern{%
                     384
                               0 J [%
                     385
                    Produce a dot pattern only when the segment is long enough.
                               \ifdim\@tempdima>\z@
                                 \xP@precdim\xP@preclw\xP@precdim\@tempdima
                     387
                               \fi
                     388
                               ]0 d}%
                     389
                           \fi
                     390
                     391
                           \global\let\xP@lastpattern\xP@dotmacro
                     392 }
\xP@setcldottedpat
                    Dotted pattern for closed paths. Offset is half of the dot distance to avoid artifacts.
                     393 \newcommand*\xP@setcldottedpat{%
                     394
                             \@tempdima\dimexpr\@tempdimb/(\@tempdimb/131072+1)-\xP@preclw\relax
                     395
                             \edef\xP@pattern{%
                     396
                               0 J [%
                     397
                               \ifdim\@tempdima>\z@
                                 \xP@precdim\xP@preclw\xP@precdim\@tempdima
                     398
                     399
                               ]\xP@precdim{\dimexpr\xP@preclw+\@tempdima/2\relax}d}%
                     400
                     401 }
                    In contrast to the Postscript drivers for Xy-pic, where some computations are left to the
                    Postscript code, all arithmetic for the PDF output must be done by TFX itself. With TFX's
                    rudimentary fixed-point arithmetic, it is still a pain to compute even the length of a line
                    segment, but things have become considerably easier with \varepsilon-T<sub>F</sub>X.
           \xP@abs
                    Absolute value
                     402 \newcommand*\xP@abs[1]{\ifdim#1<\z@\multiply#1\m@ne\fi}
     \xP@ifabsless
                     403 \newcommand*\xP@ifabsless[2]{\ifpdfabsdim#1<#2}
                     404 \ifx\left(\mbox{ifpdfabsdim}\right)\
                           406
                           \@gobble\fi
                     407 \fi
       \xP@swapdim
                    Works unless parameter #2 is \@tempdima.
                     408 \newcommand*\xP@swapdim[2]{\@tempdima#1#1#2#2\@tempdima}
                    Works unless parameter #2 is \@tempcnta.
       \xP@swapnum
                     409 \newcommand*\xP@swapnum[2]{\@tempcnta#1#1#2#2\@tempcnta}
           \xP@min
                    Maximum of two lengths
                     410 \mbox{newcommand*}\xP0min[2]{\ifdim#1<#2#1\else#2\fi}
                    Maximum of two lengths
           \xP@max
                     411 \mbox{newcommand*}\xP@max[2]{\mbox{ifdim#1>#2#1}else#2}fi}
           \xP@Max Assigns #1 the maximum of #1 and the absolute value of #2.
                     412 \mbox{ newcommand*} \mbox{ P@Max} [2] $$ $$ 11\mbox{ infdim#2<\z@\xP@max#1{-#2}\else\xP@max#1#2\fi} $$
```

Square root algorithm. The argument is in \@tempdima, and the start value for the iteration in \@tempdimc. The result goes into \@tempdimb. 413 \newcommand*\xP@sqrt{% 414 \loop \@tempdimb\dimexpr(\@tempdimc+(\@tempdima*\p@/\@tempdimc))/2\relax 415 ε -T_FX's \unless instead of \else since the plain T_FX \loop cannot deal with \else. \unless\ifdim\@tempdimc=\@tempdimb iterate: (old approx.) := (new approx.)\@tempdimc\@tempdimb\relax 418 \repeat 419 } Absolute length of the vector (\d@X, \d@Y). The result goes into the register \@tempdimb. \xP@veclen Several LATEX registers are used as temporary registers, so this function is called safely within a group. (Maybe it is not necessary to scale the coordinates so much as it is done here, and a simpler code would be fine as well.) 420 \newcommand*\xP@veclen{{% \xP@veclen@ 421 \global\dimen@i\@tempdimb 422 423 }\@tempdimb\dimen@i 424 } \xP@veclen@ 425 \newcommand*\xP@veclen@{% \xP@abs\d@Y 1) Strictly vertical vector $\left(\frac{d}{d} = \frac{20}{2}\right)$ 427 \@tempdimb\d@Y 428 \else 429 \xP@abs\d@X 430 2) Strictly horizontal vector $\left(\frac{d^{2}}{d^{2}}\right)$ 431 432 \@tempdimb\d@X 433 \else 3) Diagonal vector. $5931642\text{sp} = \sqrt{\text{maxdimen}/2}$. Test whether the components are small enough so that their sum of squares does not generate an arithmetic overflow. 434 \@tempswatrue 435 \ifdim\d@X>5931641sp\relax\@tempswafalse\fi 436 \ifdim\d@Y>5931641sp\relax\@tempswafalse\fi \if@tempswa 3a) Small vector. \count@ contains a scaling factor for a precise fixed-point arithmetic. \count@\@ne 438 439 \loop \@tempdima\dimexpr\d@X*\d@X/\p@+\d@Y*\d@Y/\p@\relax 440 If the coordinates are small enough, scale them up to improve precision. \ifdim\@tempdima<4096pt 441

442

443

444

445

\else\tw@\fi

\multiply\d@X\@tempcnta

\multiply\d@Y\@tempcnta

\@tempcnta\ifdim\@tempdima<1024pt\ifdim\@tempdima<256pt8\else4\fi%

```
\multiply\count@\@tempcnta
446
447
             \repeat
Starting value for the square root algorithm
             \ensuremath{\tt Qtempdimc\dimexpr(\d@X+\d@Y)*3/4\relax}
449
             \xP@sqrt
Rescale
450
             \@tempdimb\dimexpr\@tempdimb/\count@\relax
451
          \else
452
             \ifdim\d@X>83042982sp\relax\@tempswatrue\fi
453
             \ifdim\d@Y>83042982sp\relax\@tempswatrue\fi
454
             \if@tempswa
3b) Large vector. Scale the coordinates down to avoid an overflow. 11927552sp = 182pt
               \@tempdima\dimexpr\d@X/182*\d@X/11927552+\d@Y/182*\d@Y/11927552\relax
455
456
               \ensuremath{\tt 0}tempdimc\ensuremath{\tt dimexpr(\d0X+\d0Y)*3/728\relax}
457
               \xP@sqrt
               \multiply\@tempdimb182\relax
458
 459
             \else
3c) Medium vector. Also scale the coordinates down. 12845056\text{sp} = 196\text{pt} = 14^2\text{pt}
               460
               \ensuremath{\tt Qtempdimc\dimexpr(\dQX+\dQY)*3/56\relax}
461
 462
               \xP@sqrt
               \multiply\@tempdimb14\relax
 463
464
             \fi
          \fi
465
         \fi
466
      \fi
 467
 468 }
```

9.2 Squiggled lines

\squiggledSpread@ \xP@squiggledSpread@

```
This is the hook for squiggled straight lines.
```

- 469 \xP@hook{pdf}{squiggledSpread@}
- $470 \verb|\difdefinable\xP@squiggledSpread@\relax| \\$
- $471 \ensuremath{\mbox{\sc 471 \ensuremath{\mbox{\sc 471 \ensuremath{\mbox{\sc 471 \ensuremath{\mbox{\sc 471 \ensuremath{\sc 471 \ensuremath{\sc$
- 472 \xP@veclen

Neglect zero-length lines.

- 473 \ifdim\@tempdimb>\z@
- 474 \edef\@tempa{\xP@coor\X@p\Y@p m }%
- 475 \toks@\expandafter{\@tempa}%

- 478 \Otempdima\dimexpr\dOX/\Otempcnta\relax
- 479 \@tempdimc\dimexpr\d@Y/\@tempcnta\relax

Reverse the direction of the little arcs, if the last squiggle from the previous segment makes it necessary.

```
480 \xP@testcont\xP@oddsquigglemacro

481 \ifxP@splinecont

482 \def\xP@squigsign{-}%

483 \else

484 \let\xP@squigsign\@empty

485 \fi
```

```
487
                         \loop
                The fraction is the continuous fraction approximation for the best spline approximation to
                a quarter circle (147546029/534618434 \approx \frac{1}{2} \cdot 0.55196760761152504532).
                 488
                         \xP@append\toks@{%
                           \xP@coor{\X@p+\d@X*\count@/\@tempcnta+(\@tempdima
                 489
                             -\xP@squigsign\tiond\count@-\fi\@tempdimc)*147546029/534618434}\%
                 490
                 491
                           {\Y@p+\d@Y*\count@/\@tempcnta+(\@tempdimc
                 492
                             +\xP@squigsign\ifodd\count@-\fi\@tempdima)*147546029/534618434}%
                 493
                 494
                         \advance\count@\@ne
                         \xP@append\toks@{%
                 495
                           \xP@coor{\X@p+\d@X*\count@/\@tempcnta-(\@tempdima
                 496
                 497
                             -\xP@squigsign\ifodd\count@-\fi\@tempdimc)*147546029/534618434}%
                 498
                           {\Y@p+\d@Y*\count@/\@tempcnta-(\@tempdimc
                             +\xP@squigsign\ifodd\count@-\fi\@tempdima)*147546029/534618434}%
                 499
                 500
                           \xP@coor{\X@p+\d@X*\count@/\@tempcnta}%
                 501
                           {\Y@p+\d@Y*\count@/\@tempcnta}%
                 502
                           c }%
                 503
                         \ifnum\count@<\@tempcnta
                 504
                         \repeat
                         \xP@setsolidpat
                 505
                Record the direction of the last squiggle.
                 506
                         \global\expandafter\let\expandafter\xP@lastpattern
                         \ifodd\numexpr\count@\if\xP@squigsign-+1\fi\relax
                 507
                 508
                           \xP@oddsquigglemacro
                 509
                         \else
                 510
                           \xP@evensquigglemacro
                 511
                         \fi
                 512
                         \xP@savec
                         \xP@stroke{\the\toks@}%
                 513
                 514
                 515 }}
\xP@squigsign
                 516 \newcommand*\xP@squigsign{}
   \xP@append
                 517 \newcommand*\xP@append[2]{{%
                       \edgn(0) = {1{\theta}^{2}}%
                       \expandafter}\@tempa
                 520 }
                       Circles
                9.3
   \circhar@@
                Replacement macro for the circle chars.
\xP@circhar@@
                 521 \xP@hook{pdf}{circhar@@}
                 522 \newcommand*\xP@circhar@@[1]{%
                      \expandafter\xP@circhar@@@\ifcase#1 %
                Bézier segments for 1/8 circle. Let
                                  a := \sqrt{1/2} \approx .707106781,
                                  b := \frac{8}{3}\sqrt{2}\cos(\pi/8)\left(1 - \cos(\pi/8)\right) \approx .2652164898,
```

486

 $\count@\z@$

```
c := \frac{1}{3} \left( -3 + 8\cos(\pi/8) - 2\cos^2(\pi/8) \right) \approx .8946431596,
d := \frac{1}{2} b(2 + 3\cos(\pi/8) - \cos^2(\pi/8)) \approx .5195704027.
```

```
(We have \cos(\pi/8) = \frac{1}{2}\sqrt{2 + \sqrt{2}}.)
```

The fractions below are best possible rational approximations (obtained by continued fractions) to the following coordinates:

```
(0,0), (0,-b), (1-c,-d), (1-a,-a)
        00%
524
525
        0{-173517671/654249180}%
526
        {65307479/619869377}{-34221476/65864945}%
        {225058681/768398401}{-543339720/768398401}%
527
528
(0,-a), (a-d,-c), (a-b,-1), (a,-1)
529
        0{-543339720/768398401}%
        {181455824/967576667}{-554561898/619869377}%
530
        {826676217/1870772527}{-1}%
531
        {543339720/768398401}{-1}%
532
533
(0,-1), (b,-1), (d,-c), (a,-a)
        0{-1}%
534
        {173517671/654249180}{-1}%
535
        {34221476/65864945}{-554561898/619869377}%
536
        {543339720/768398401}{-543339720/768398401}%
537
     \or
538
(0,-a), (c-a,-d), (1-a,-b), (1-a,0)
        0{-543339720/768398401}%
539
        {181455824/967576667}{-34221476/65864945}%
540
        {225058681/768398401}{-173517671/654249180}%
541
542
        {225058681/768398401}0%
543
     \or
(0,a), (c-a,d), (1-a,b), (1-a,0)
        0{543339720/768398401}%
        {181455824/967576667}{34221476/65864945}%
545
        {225058681/768398401}{173517671/654249180}%
546
        {225058681/768398401}0%
547
548
     \or
(0,1), (b,1), (d,c), (a,a)
549
        01%
        {173517671/654249180}1%
550
551
        {34221476/65864945}{554561898/619869377}%
552
        {543339720/768398401}{543339720/768398401}%
553
      \or
(0,a), (a-d,c), (a-b,1), (a,1)
        0{543339720/768398401}%
554
        {181455824/967576667}{554561898/619869377}%
555
        {826676217/1870772527}1%
556
557
        {543339720/768398401}1%
558
(0,0), (0,b), (1-c,d), (1-a,a)
559
        0{173517671/654249180}%
560
```

```
{65307479/619869377}{34221476/65864945}%
                                                     561
                                                     562
                                                                      {225058681/768398401}{543339720/768398401}%
                                                     563
                                                                 \fi}
                                                   Draw the arc of 1/8 circle and use the same space as the chars from the circle font do.
               \xP@circhar@@@
                                                     564 \newcommand\xP@circhar@@@[8]{%
                                                                \xP@setsolidpat
                                                               \xP@stroke{\xP@coor{\R@*#1}{\R@*#2}m}
                                                     566
                                                                 \xP@coor{\R@*#3}{\R@*#4}\xP@coor{\R@*#5}{\R@*#6}%
                                                     567
                                                     568
                                                                 \xP@coor{\R@*#7}{\R@*#8}c}%
                                                     569
                                                                 \vrule width\z@ height\R@ depth\R@
                                                                 \kern\dimexpr\R@*#7\relax
                                                      570
                                                     571 }
                \cirrestrict@@
                                                   Basically, \cirrestrict@@ is turned into a no-op and does not change the radius.
         \xP@cirrestrict@@
                                                     572 \xP@hook{pdf}{cirrestrict@@}
                                                     573 \newcommand*\xP@cirrestrict@@{\count@\z@\relax}
                                                     574 (/basic)
                                                    9.4
                                                                  Rotation and scaling
                                                     575 (*rotate)
                                                     576 \xycatcodes
           \xypdf-ro@loaded
                                                     577 \expandafter\let\csname xypdf-ro@loaded\endcsname\@empty
                                                   Scale the box 0 to the factors in #1 and #2.
                         \xyscale@@
                  \xP@xyscale@@
                                                     578 \xP@hook{rotate}{xyscale@@}
                                                     579 \newcommand*\xP@xyscale@@[2]{%
                                                     580
                                                                 \setboxz@h{%
                                                                      \hskip\L@c
                                                     581
                                                                      \hskip-\R@p
                                                      582
                                                                      \label{lower_U0phbox{xP0cm}#1}00{\#2}%
                                                      583
                                                                          {\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{\colored{
                                                     584
                                                                     }%
                                                      585
                                                      586
                                                                 }%
                                                     587
                                                                 \global\let\xP@lastpattern\@empty
                                                      588 }
                                                   Rotation in the direction #1.
                      \xyRotate@@
               \xP@xyRotate@@
                                                     589 \xP@hook{rotate}{xyRotate@@}
                                                     590 \newcommand\xP@xyRotate@@{\xP@rotate@\xP@trigfromdir}
       \doSpecialRotate@@
                                                    Rotation by the angle in #1.
\xP@doSpecialRotate@@
                                                     591 \xP@hook{rotate}{doSpecialRotate@@}
                                                     592 \@ifdefinable\xP@doSpecialRotate@@\relax
                                                     593 \def\xP@doSpecialRotate@@#1@@{\xP@rotate@\xP@trig{#1}}
                                                   Common code for both rotations: rotate the box 0.
                      \xP@rotate@
                                                     594 \newcommand*\xP@rotate@[2]{%
                                                                 \setboxz@h{%
                                                                      #1{#2}%
                                                     596
                                                     597
                                                                      \hskip\L@c
                                                                      \hskip-\R@p
                                                     598
                                                                      \lower\U@p\hbox{\xP@cm\cosDirection\sinDirection
                                                     599
```

```
{\if-\sinDirection\else-\sinDirection\fi}\cosDirection
 600
 601
           {\raise\U@p\hb@xt@\z@{\hskip-\L@c\hskip\R@p\boxz@\hss}}%
        }%
 602
 603
      }%
      \global\let\xP@lastpattern\@empty
 604
 605 }
Calculate sine and cosine from the angle in #1.
 606 \newcommand*\xP@trig[1]{%
 607
      \@tempdima\dimexpr#1pt\relax
Translate the argument into the interval [0pt, 360pt].
      \@tempdimb\@tempdima
23592960 = 360 \cdot 65536
      \divide\@tempdimb23592960
 609
      \advance\@tempdima-23592960\@tempdimb
 610
      \ifdim\@tempdima<\z@\advance\@tempdima360pt\fi
 612
      \@tempdimb\@tempdima
5898240 = 90 \cdot 65536
      \divide\@tempdimb5898240
It's enough to know sin between 0° and 90°. The cos and the values in the other quadrants
can be derived from that.
      \ifcase\@tempdimb
 614
        \xP@sinpoly
 615
 616
        \edef\sinDirection{\xP@EARPT\@tempdimb}%
 617
        \@tempdima\dimexpr90pt-\@tempdima\relax
        \xP@sinpoly
 618
        \edef\cosDirection{\xP@EARPT\@tempdimb}%
 619
 620
      \or
        \@tempdima\dimexpr180pt-\@tempdima\relax
 621
 622
        \xP@sinpoly
 623
        \edef\sinDirection{\xP@EARPT\@tempdimb}%
 624
        \@tempdima\dimexpr90pt-\@tempdima\relax
 625
        \edef\cosDirection{\xP@EARPT\dimexpr-\@tempdimb\relax}%
 626
 627
      \or
        \@tempdima\dimexpr\@tempdima-180pt\relax
 628
 629
        \xP@sinpoly
        \edef\sinDirection{\xP@EARPT\dimexpr-\@tempdimb\relax}%
 630
        \@tempdima\dimexpr90pt-\@tempdima\relax
 631
 632
        \xP@sinpoly
        \edef\cosDirection{\xP@EARPT\dimexpr-\@tempdimb\relax}%
 633
 634
      \or
        \@tempdima\dimexpr360pt-\@tempdima\relax
 635
 636
        \xP@sinpoly
        \edef\sinDirection{\xP@EARPT\dimexpr-\@tempdimb\relax}%
 637
        \@tempdima\dimexpr90pt-\@tempdima\relax
 638
        \xP@sinpoly
 639
        \edef\cosDirection{\xP@EARPT\@tempdimb}%
 640
      \else
 641
        \PackageError{xypdf}{Unexpected case in sin/cos calculation}%
 642
 643
          {Feel free to contact the author of the xypdf package with a minimal %
           example.}%
 644
      \fi
 645
 646 }
```

```
Polynomial approximation to the sine in the interval [0pt, 90pt]. The deviation should be
    \xP@sinpoly
                   \pm 1sp maximal (but no guarantee). (3rd order, 4 subintervals, exact values for 0pt and 90pt)
                   647 \newcommand*\xP@sinpoly{{%
                         \ifdim\@tempdima<49pt
                   648
                   649
                            \ifdim\@tempdima<27pt
                              \@tempdimb\dimexpr((\@tempdima*-529771058/16039085-1384933sp)%
                   650
                                *\@tempdima/268756075+10714164sp)*\@tempdima/613777813\relax
                   651
                            \else
                   652
                              \advance\@tempdima-27pt
                   653
                              \@tempdimb\dimexpr(((\@tempdima*-743101305/20672414-238989613sp)%
                   654
                                *\ensuremath{\tt 00975565+42661556sp})*\ensuremath{\tt 00975565+42661556sp})*\ensuremath{\tt 00975565+42661556sp})
                   655
                                *157520747/693945047\relax
                   656
                            \fi
                   657
                         \else
                   658
                            \ifdim\@tempdima<70pt
                   659
                              \advance\@tempdima-49pt
                   660
                              \@tempdimb\dimexpr(((\@tempdima*-348406699/107952940-55079229sp)%
                   661
                                *\ensuremath{\tt 0}tempdima/866635628+408805sp)*\ensuremath{\tt 0}tempdima/26926757+\ensuremath{\tt 0}%
                   662
                                *135751711/179873976\relax
                   663
                   664
                              \advance\@tempdima-70pt
                   665
                              \@tempdimb\dimexpr(((\@tempdima*-1015850353/137849442-460519207sp)%
                   666
                                {\tt *\tt0tempdima/8742349+142263941sp)*\tt0tempdima/972432199+23\ttp0)\%}
                   667
                                *31253604/764969669\relax
                   668
                   669
                            \fi
                         \fi
                   670
                   671
                          \global\dimen@i\@tempdimb
                   672
                         }\@tempdimb\dimen@i
                   673 }
                      End of the section for Xy-pic's "rotate" option. The macro \xP@trigfromdir below is
                   also used for the {-} directional.
                   674 \xyendinput
                   675 (/rotate)
                   676 (*basic)
\xP@trigfromdir
                   Calculate sine and cosine from the direction number in #1.
                   677 \newcommand*\xP@trigfromdir[1]{{%
                         \Direction#1\relax
                   \Direction mod 2048
                   679
                         \count@-\Direction
                         \advance\count@4096
                   680
                         \divide\count@2048
                   681
                   Assign the slope in the right way.
                         \ifcase\count@
                   682
                   683
                            \d@X\K@\p@
                   684
                            \d@Y\numexpr\Direction-3*\K@\relax\p@
                   685
                            \d@X\numexpr\Direction-\K@\relax\p@
                   686
                            \d@Y-\K@\p@
                   687
                   688
                            \d0X-\K0\p0
                   689
                            \d@Y\numexpr-\Direction-\K@\relax\p@
                   690
                         \or
                   691
                            \d@X\numexpr-\Direction-3*\K@\relax\p@
                   692
```

```
\d@Y\K@\p@
693
     \else
694
695
       \PackageError{xypdf}{Unexpected case in direction calculation}%
        {Feel free to contact the author of the xypdf package with a minimal %
696
697
        example.}%
     \fi
698
Bring the pair (\d@X, \d@Y) to norm 1.
     \xP@veclen
700
     \xdef\@gtempa{%
701
       \def\noexpand\cosDirection{\xP@EARPT\dimexpr\d@X*\p@/\@tempdimb\relax}%
       702
     ጉ%
703
     }\@gtempa
704
705 }
```

9.5 Temporary registers

\xP@newdimen

```
Remove the \outer from \newdimen. (This applies for plain TeX.)
706 \outer\def\@tempa{\alloc@1\dimen\dimendef\insc@unt}
707 \let\xP@newdimen\newdimen
708 \ifx\newdimen\@tempa
      \def\xP@newdimen{\alloc@1\dimen\dimendef\insc@unt}
709
710 \fi
711 \outer\def\@tempa#1{\count@=\escapechar\escapechar=-1
        \expandafter\expandafter\expandafter
712
713
        \def\@if#1{true}{\let#1=\iftrue}%
        \expandafter\expandafter\expandafter
714
        \def\@if#1{false}{\let#1=\iffalse}%
715
        \@if#1{false}\escapechar=\count@}
716
717 \let\@tempa\relax
The next section is for the "curve" extension!
```

\xypdf-cu@loaded

721 \expandafter\let\csname xypdf-cu@loaded\endcsname\@empty

\xP@tempvar

718 $\langle \text{/basic} \rangle$ 719 $\langle *\text{curve} \rangle$ 720 $\backslash \text{xycatcodes}$

In order to save registers, xypdf shares Xy-pic's and IATEX dimension and counter registers but uses different, more descriptive names. Every macro that uses these temporary variables must be safely encapsulated in a group so that the registers are not changed from the outside scope!

The xypdf package uses several sets of temporary variable names for different modules. Since it is important that these assignments do not overlap and that the variables are only used encapsulated within groups, the macros which use temporary variables are marked by colored bullets $\bullet 1$, $\bullet 2$, $\bullet 3$, $\bullet 4$, $\bullet 5$, $\bullet 6$, $\bullet 7$ with one color for each set of variables.

The table in Figure 5 lists all variable assignments in these sets. It can be seen from the table which sets of variables can be used together. For example, set •1 consisting of \xP@bigdim can be used together with all other temporary variables, while •2 and •4 must never be used together.

```
722 \newcommand*\xP@tempvar[2]{%
723 \@ifdefinable#1\relax
724 \let#1#2%
725 }
```

Xy-pic/LAT _E X										
variable	Set 1	Set 2	Set 3	Set 4	Set 5	Set 6	Set 7			
\quotPTK@ \xP@bigdim										
\L@p		\xP@parA	\xP@A		(\L@p)		(\L@p)			
\U@p		\xP@velA	\xP@B		(\U@p)		(\U@p)			
\R@p		\xP@parB	\xP@C		(\R@p)		(\R@p)			
\D@p		\xP@velB	\xP@D		(\D@p)		(\D@p)			
\X@origin		\xP@parC	\xP@E				\xP@temppar			
\Y@origin		\xP@velC	\xP@F				\xP@tempvel			
\X@xbase		\xP@parD	\xP@G				\xP@posX			
\Y@xbase		\xP@velD	\xP@H				\xP@posY			
\X@ybase		\xP@parE	$\xP@I =$	\xP@a	\xP@a		\xP@oldpar			
\Y@ybase		\xP@velE	$\xP@J =$	\xP@b	\xP@b		\xP@lastpar			
\X @min		\xP@lenA	\xP@K		\xP@c		\xP@tempvel@			
\Y@min		\xP@lenB	\xP@L		\xP@valA		\xP@parinc			
\X@max		\xP@partlen	$\xP@fa$		\xP@valB					
\Y@max		\xP@oldpartlen	\xP@fd		\xP@devA					
\almostz@		\xP@tolerance	$\xP@tm$		\xP@devB		\xP@squiglen			
\K@dXdY			$\xP@xm$		\xP@ti					
\K@dYdX			\xP@ym		\xP@tip					
$\splineval@$			$\xP@off$		(\xP@off)					
\splinedepth@			\xP@ta							
$\splinetol@$			$\xP@tb$							
\splinelength@			\xP@tc							
\L@			\xP@M							
\normallineskiplimit \xP@oldobj										
\@savsk				\xP@Tax		\xP@s	a			
\lower@bound				\xP@Tay		\xP@s	b			
\upper@bound				\xP@Tdx \xP@sc		С				
\leftmargin				\xP@Tdy		\xP@Ab				
$\$ rightmargin				\xP@Tmx		\xP@A	Ab			
\listparinden	t			\xP@Tmy		\xP@A	ba			
\itemindent				\xP@xa	$(\xP@xa)$	\xP@A	bb			
\label width				\xP@ya	(xP@ya)	\xP@A	bc			
\labelsep				\xP@xb	(\xP@xb)	\xP@A				
$\label{linewidth}$				\xP@yb	(\xP@yb)	\xP@A				
\@totalleftma:	rgin			\xP@xc	(\xP@xc)	\xP@A	Abc			
\leftmargini				\xP@yc	(\xP@yc)	\xP@d	ta			
\leftmarginii				\xP@xd	(\xP@xd)	\xP@d				
\leftmarginii	i			\xP@yd	(\xP@yd)	\xP@d	tc			

Figure 5: Temporary dimension registers in xypdf.

```
Either reuse an existing dimension register if the name is defined or allocate a new dimension
\xP@oldornewdimen
                    register. This makes it possible to selectively reuse IATEX dimension registers or allocate
                    new registers in plain T<sub>F</sub>X mode.
                     726 \newcommand*\xP@oldornewdimen[2]{%
                          \@ifundefined{#2}%
                     727
                     728
                             {\xP@newdimen#1}%
                             {\expandafter\xP@tempvar\expandafter#1\csname#2\endcsname}%
                     729
                     730 }
                    •1 A big constant less than \frac{1}{3}\maxdimen \approx 5461pt and having many small prime factors.
       \xP@bigdim
                     731 \xP@tempvar\xP@bigdim\quotPTK@
                    •2 Second set of temporary variables: for the arc length algorithm.
         \xP@parA
         \xP@velA
                     732 \xP@tempvar\xP@parA\L@p
         \xP@parB
                     733 \xP@tempvar\xP@velA\U@p
         \xP@velB
                     734 \xP@tempvar\xP@parB\R@p
                     735 \xP@tempvar\xP@velB\D@p
         \xP@parC
                     736 \xP@tempvar\xP@parC\X@origin
         \xP@velC
                     737 \xP@tempvar\xP@velC\Y@origin
         \xP@parD
                     738 \xP@tempvar\xP@parD\X@xbase
         \xP@velD
                     739 \xP@tempvar\xP@velD\Y@xbase
         \xP@parE
                     740 \xP@tempvar\xP@parE\X@ybase
         \xP@velE
                     741 \xP@tempvar\xP@velE\Y@ybase
         \xP@lenA
                     742 \xP@tempvar\xP@lenA\X@min
         \xP@lenB
                     743 \xP@tempvar\xP@lenB\Y@min
      \xP@partlen
                     744 \xP@tempvar\xP@partlen\X@max
   \xP@oldpartlen
                     745 \xP@tempvar\xP@oldpartlen\Y@max
    \xP@tolerance
                     746 \xP@tempvar\xP@tolerance\almostz@
            \xP@A
                    •3 Third set of temporary registers: Bézier offset algorithm and solving linear equations.
            \xP@B
                     747 \xP@tempvar\xP@A\L@p
            \xP@C
                     748 \xP@tempvar\xP@B\U@p
            \xP@D
                     749 \xP@tempvar\xP@C\R@p
                     750 \xP@tempvar\xP@D\D@p
            \xP@E
                     751 \xP@tempvar\xP@E\X@origin
            \xP@F
                     752 \xP@tempvar\xP@F\Y@origin
            \xP@G
                     753 \xP@tempvar\xP@G\X@xbase
            \xP@H
                     754 \xP@tempvar\xP@H\Y@xbase
            \xP@I
                     755 \xP@tempvar\xP@I\X@ybase
            \xP@J
                     756 \xP@tempvar\xP@J\Y@ybase
            \xP@K
                     757 \xP@tempvar\xP@K\X@min
            \xP@L
                     758 \xP@tempvar\xP@L\Y@min
           \xP@fa
                     759 \xP@tempvar\xP@fa\X@max
           \xP@fd
                     760 \xP@tempvar\xP@fd\Y@max
           \xP@tm
                     761 \xP@tempvar\xP@tm\almostz@
                     762 \xP@tempvar\xP@xm\K@dXdY
           \xP@xm
                     763 \xP@tempvar\xP@ym\K@dYdX
           \xP@ym
                     764 \xP@tempvar\xP@off\splineval@
          \xP@off
                     765 \xP@tempvar\xP@ta\splinedepth@
           \xP@ta
                     766 \xP@tempvar\xP@tb\splinetol@
           \xP@tb
                     767 \xP@tempvar\xP@tc\splinelength@
           \xP@tc
                     768 \xP@tempvar\xP@M\L@
            \xP@M
                    •3 We need 15 more temporary registers. If possible, we use exisiting LATEX dimension
       \xP@oldobj
          \xP@Tax
                    registers. If XY-pic is used in plain TEX mode, there are hopefully still free slots for dimension
          \xP@Tay
          \xP@Tdx
          \xP@Tdy
                                                                28
          \xP@Tmx
```

\xP@Tmy \xP@xa \xP@ya \xP@xb \xP@vb

```
registers. We take them for the temporary variables but release them afterwards so that
other packages can use them.
```

```
769 \@tempcnta\count11\relax
               770 \xP@oldornewdimen\xP@oldobj{normallineskiplimit}
               771 \xP@oldornewdimen\xP@Tax{@savsk}
               772 \xP@oldornewdimen\xP@Tay{lower@bound}
               773 \xP@oldornewdimen\xP@Tdx{upper@bound}
               774 \xP@oldornewdimen\xP@Tdy{leftmargin}
               775 \xP@oldornewdimen\xP@Tmx{rightmargin}
               776 \xP@oldornewdimen\xP@Tmy{listparindent}
               777 \xP@oldornewdimen\xP@xa{itemindent}
               778 \xP@oldornewdimen\xP@ya{labelwidth}
               779 \xP@oldornewdimen\xP@xb{labelsep}
               780 \xP@oldornewdimen\xP@yb{linewidth}
               781 \xP@oldornewdimen\xP@xc{@totalleftmargin}
               782 \xP@oldornewdimen\xP@yc{leftmargini}
               783 \xP@oldornewdimen\xP@xd{leftmarginii}
               784 \xP@oldornewdimen\xP@yd{leftmarginiii}
               785 \count11\@tempcnta
       \xP@a
              •5 Fifth set of temporary variables: Parameters for drawing part of a spline segment.
       \xP@b
               786 \xP@tempvar\xP@a\X@ybase
       \xP@c
               787 \xP@tempvar\xP@b\Y@ybase
    \xP@valA
               788 \xP@tempvar\xP@c\X@min
               789 \xP@tempvar\xP@valA\Y@min
   \xP@valB
               790 \xP@tempvar\xP@valB\X@max
    \xP@devA
               791 \xP@tempvar\xP@devA\Y@max
    \xP@devB
               792 \xP@tempvar\xP@devB\almostz@
      \xP@ti
               793 \xP@tempvar\xP@ti\K@dXdY
     \xP@tip
               794 \xP@tempvar\xP@tip\K@dYdX
      \xP@sa
              •6 Sixth set of temporary variables: Solving a linear system approximately.
      \xP@sb
               795 \xP@tempvar\xP@sa\xP@Tax
      \xP@sc
               796 \xP@tempvar\xP@sb\xP@Tay
      \xP@Ab
              797 \xP@tempvar\xP@sc\xP@Tdx
     \xP@AAb
              798 \xP@tempvar\xP@Ab\xP@Tdy
               799 \xP@tempvar\xP@AAb\xP@Tmx
     \xP@Aba
               800 \xP@tempvar\xP@Aba\xP@Tmy
     \xP@Abb
               801 \xP@tempvar\xP@Abb\xP@xa
     \xP@Abc
               802 \xP@tempvar\xP@Abc\xP@ya
    \xP@AAba
               803 \xP@tempvar\xP@AAba\xP@xb
    \xP@AAbb
               804 \xP@tempvar\xP@AAbb\xP@yb
    \xP@AAbc
               805 \xP@tempvar\xP@AAbc\xP@xc
     \xP@dta
               806 \xP@tempvar\xP@dta\xP@yc
     \xP@dtb
               807 \xP@tempvar\xP@dtb\xP@xd
     \xP@dtc
               808 \xP@tempvar\xP@dtc\xP@yd
\xP@temppar
              • 7 Seventh set of temporary registers: For multiple dotted splines.
\xP@tempvel
               809 \xP@tempvar\xP@temppar\X@origin
   \xP@posX
               810 \xP@tempvar\xP@tempvel\Y@origin
    \xP@posY
               811 \xP@tempvar\xP@posX\X@xbase
               812 \xP@tempvar\xP@posY\Y@xbase
 \xP@oldpar
               813 \xP@tempvar\xP@oldpar\X@ybase
\xP@lastpar
               814 \xP@tempvar\xP@lastpar\Y@ybase
\xP@tempvel@
  \xP@parinc
\xP@squiglen
```

```
815 \xP@tempvar\xP@tempvel@\X@min
                    816 \xP@tempvar\xP@parinc\Y@min
                    817 \xP@tempvar\xP@squiglen\almostz@
                   We also use temporary numerical registers for scaling factors in \xP@solvelinearsystem.
     \xP@scaleone
     \xP@scaletwo
                    818 \xP@tempvar\xP@scaleone\K@
   \xP@scalethree
                    819 \xP@tempvar\xP@scaletwo\KK@
                    820 \xP@tempvar\xP@scalethree\Direction
                   9.6
                          Bézier curves
                   These are the hooks for single-stroke splines (solid, dashed and dotted).
   \splinesolid@
   \splinedashed@
                    821 \xP@hook{curve}{splinesolid@}
   \splinedotted@
                    822 \newcommand*\xP@splinesolid@{\xP@spline\xP@setsolidpat}
                    823 \xP@hook{curve}{splinedashed@}
                    824 \newcommand*\xP@splinedashed@{\xP@spline\xP@setdashpat}
                    825 \xP@hook{curve}{splinedotted@}
                    826 \newcommand*\xP@splinedotted@{\xP@spline\xP@setdottedpat}
                   Output a spline segment. Parameter: Macro for the dash pattern generation.
                    827 \newcommand*\xP@spline[1]{%
                         \readsplineparams@
                   Neglect splines which are drawn "backwards". Somehow Xy-pic draws curves forward and
                   backward, but we need it to be drawn only once.
                          \ifdim\dimen5<\dimen7
                    829
                            \xP@preparespline
                    830
                   Neglect splines of length zero.
                            \ifdim\@tempdimb>\z@
                   Set the dash pattern.
                    832
                              #1%
                   Draw the spline.
                    833
                              \xP@stroke{\xP@coor\X@p\Y@p m %
                                \xP@coor\L@c\U@c\xP@coor\R@c\D@c\xP@coor\X@c\Y@c c}%
                    834
                   Record the end point for pattern continuation.
                                \xP@savec
                            \fi
                    836
                    837
                          \fi
                    838 }
\xP@preparespline
                    839 \newcommand*\xP@preparespline{%
                   If we have a quadratic Bézier segment, convert it to a cubic one.
                            \ifx\splineinfo@\squineinfo@
                    840
                              \L@c\dimexpr(\X@p+2\A@)/3\relax
                    841
                    842
                              \U@c\dimexpr(\Y@p+2\B@)/3\relax
                    843
                              \R@c\dimexpr(\X@c+2\A@)/3\relax
                    844
                              \D@c\dimexpr(\Y@c+2\B@)/3\relax
                    845
                   Cut the spline according to that start and end parameters in \dimen5 and \dimen7.
```

\xP@shavespline

846

Determine the spline length (for the pattern generation; unnecessary for solid splines).

```
847 \xP@bezierlength
848 }
```

\xP@inibigdim

•1 Initialize \xP@bigdim every time a macro that uses this register is called. See e.g. \xP@shaveprec.

```
849 \newcommand*\xP@inibigdim\{xP@bigdim5040pt\}
```

\xP@shavespline

Shave a cubic spline at both ends at the parameter values in $\dim 5$ and $\dim 7$. For normal use, the parameters fulfill $0pt \leq \dim 5 < \dim 7 \leq 1pt$.

(Note that $\xP@bigdim$ only occurs in the arguments to $\xP@shaveprec$, so this use is safe.)

\xP@shaveprec

•1 Shave a cubic spline at both ends at the parameter values in #1 and #2. For normal use, the parameters fulfill $0pt \le \#1 < \#2 \le \xP@bigdim$. The control points for the cubic Bézier curve are (\X@p,\Y@p), (\L@c,\U@c), (\R@c,\D@c), (\X@c,\Y@c). The Xy-pic registers \A@, \B@, \L@p, \U@p, \R@p, \D@p, \X@min and \Y@min are used as temporary registers, but safely encapsulated in a group.

```
853 \newcommand*\xP@shaveprec[2]{{%

854 \xP@inibigdim

855 \A@\dimexpr#1\relax

856 \B@\dimexpr#2\relax
```

Shortcut in case the spline is not changed.

```
857
     \@tempswatrue
     \ifdim\A@=\z@\ifdim\B@=\xP@bigdim\@tempswafalse\fi\fi
858
859
     \if@tempswa
       \L@p\dimexpr\L@c-\X@p\relax
860
       \U0p\dim\expR0c-L0p-L0c\operatorname{ax}
861
862
       \R@p\dim\expX@c-3\R@c+3\L@c-X@p\Gammaax
863
       \D@p\dimexpr\U@c-\Y@p\relax
       \X@min\dimexpr\D@c-\D@p-\U@c\relax
864
865
       \Y@min\dimexpr\Y@c-3\D@c+3\U@c-\Y@p\relax
866
       \xdef\@gtempa{%
867
         \X@p\the\dimexpr\X@p+(3\L@p+(3\U@p+\R@p*\A@/\xP@bigdim)%
868
           *\A@/\xP@bigdim)*\A@/\xP@bigdim\relax
         \Y@p\the\dimexpr\Y@p+(3\D@p+(3\X@min+\Y@min*\A@/\xP@bigdim)%
869
870
           *\A@/\xP@bigdim)*\A@/\xP@bigdim\relax
         871
872
           *\U@p/\xP@bigdim+\R@p*\A@/\xP@bigdim*\B@/\xP@bigdim)%
           *\A0/\xP@bigdim\relax
873
874
         \label{local-the} $$ \U@c\the\dimexpr\Y@p+(2\A@+\B@)*\D@p/\xP@bigdim+((\A@+2\B@)%) $$
           *\X@min/\xP@bigdim+\Y@min*\A@/\xP@bigdim*\B@/\xP@bigdim)%
875
876
           *\A@/\xP@bigdim\relax
877
         \R@c\the\dimexpr\X@p+(2\B@+\A@)*\L@p/\xP@bigdim+((\B@+2\A@)%)
878
           *\U@p/\xP@bigdim+\R@p*\B@/\xP@bigdim*\A@/\xP@bigdim)%
879
           *\B@/\xP@bigdim\relax
         \label{location} $$ \D@c\theta^{Y@p+(2\B@+\A@)*\D@p/\xP@bigdim+((\B@+2\A@)%)} $$
880
           *\X@min/\xP@bigdim+\Y@min*\B@/\xP@bigdim*\A@/\xP@bigdim)%
881
882
           *\B@/\xP@bigdim\relax
         \X@c\the\dimexpr\X@p+(3\L@p+(3\U@p+\R@p*\B@/\xP@bigdim)%
883
           *\B@/\xP@bigdim)*\B@/\xP@bigdim\relax
884
         \Y@c\the\dimexpr\Y@p+(3\D@p+(3\X@min+\Y@min*\B@/\xP@bigdim)%
885
```

```
886 *\B@/\xP@bigdim)*\B@/\xP@bigdim\relax}%
887 \else
888 \global\let\@gtempa\relax
889 \fi
890 }\@gtempa
891 }
```

\xP@bezierlength

•1 •2 Compute the arc length of a cubic Bézier segment.

The following algorithm is used: The velocity for a partial segment is fitted at three points (A-C-E) by a quadratic function, and the arc length is approximated by the integral over this quadratic function.

Each interval is recursively divided in halves (A-B-C, C-D-E) as long as the result for the arc length changes more than the precision parameter \xP@tolerance. If the desired precision is reached, the arc length in the small interval is added to the total arc length, and the next interval is considered.

The result goes into \Otempdimb.

```
892 \newcommand*\xP@bezierlength{{%
     \xP@inibigdim
893
894
     \@tempdimb\z@
     \xP@parA\z@
895
     \xP@velocity\z@\xP@velA
896
     \xP@parC.5\xP@bigdim
897
898
     \xP@velocity\xP@parC\xP@velC
899
     \xP@velocity\xP@bigdim\xP@velE
Arc length (integral over the quadratic approximation)
     Tolerance parameter: It is set to 1/100000 of the approximate arc length, but at least 1sp.
     Initiate the recursive algorithm with the interval [0, 1].
902
     \xP@arclength\xP@parC\xP@velC\xP@bigdim\xP@velE\xP@oldpartlen
Pass the result to outside the group.
     \global\dimen@i\@tempdimb
903
904
     }\@tempdimb\dimen@i
905 }
•1 Compute the velocity at the point #1 on a cubic Bézier curve. Needs: Bézier control
```

\xP@velocity

•1 Compute the velocity at the point #1 on a cubic Bézier curve. Needs: Bézier control points \X@p,...,\Y@c. Parameter #2: dimension register for the result. Temporary: \L@p, \U@p, \d@X, \d@Y.

```
906 \newcommand*\xP@velocity[2]{{%
907 \@tempdima\dimexpr#1\relax
908 \xP@tangent
909 \global\dimen@i\@tempdimb
910 }#2\dimen@i
911 }
```

\xP@tangent •

```
912 \newcommand*\xP@tangent{%

913 \d@X3\xP@precbeziertan\X@p\L@c\X@c\@tempdima

914 \d@Y3\xP@precbeziertan\Y@p\U@c\D@c\Y@c\@tempdima

915 \xP@veclen

916}
```

\xP@tangentvec •1 Tangent vector on a Bézier curve. Parameter #1: Parameter on the segment. Needs: Bézier parameters \XQp,...,\YQc. Returns: vector in (\dQX, \dQY), norm in \Qtempdimb.

```
917 \newcommand*\xP@tangentvec[1]{{%
       \@tempdima#1\relax
918
       \xP@tangent
919
```

If the velocity is zero at some point, take the second derivative for the tangent vector.

```
920
    \ifdim\@tempdimb=\z@
921
     \L@p\dimexpr\X@c-\X@p+(\L@c-\R@c)*3\relax
     \U@p\dimexpr\Y@c-\Y@p+(\U@c-\D@c)*3\relax
922
923
     924
     \xP@veclen
925
```

Or even the third derivative.

```
\ifdim\@tempdimb=\z@
926
            \d@X\L@p
927
928
            \d@Y\U@p
929
            \xP@veclen
            \ifdim\@tempdimb=\z@
930
              \xP@warning{xypdf}{Cannot determine a tangent vector to a curve}%
931
              \@tempdimb\p@
932
            \fi
933
          \fi
934
935
        \fi
        \global\dimen@i\d@X
936
937
        \global\dimen3\d@Y
        \global\dimen5\@tempdimb
938
     ጉ%
939
     \d@X\dimen@i
940
     \d@Y\dimen3\relax
941
942
     \@tempdimb\dimen5\relax
943 }
```

\xP@arclength

•2 The recursive step for the arc length computation.

Needs: \xP@tolerance, \xP@parA, \xP@velA. Parameter: #1 is the middle parameter, #2 the velocity at #1, #3 the third parameter, #4 the velocity at #3, #5 the approximate arc length in the interval from \xP@parA to #3.

```
944 \newcommand*\xP@arclength[5]{%
      \xP@parE#3%
945
      \xP@velE#4%
946
      \xP@parC#1%
947
      \xP@velC#2\%
948
      \xP@oldpartlen#5%
Compute two more pairs (parameter, velocity) at positions \frac{1}{4} and \frac{3}{4} of the interval.
      \xP@parB\dimexpr(\xP@parC+\xP@parA)/2\relax
950
      \xP@velocity\xP@parB\xP@velB
951
      \xP@parD\dimexpr(\xP@parE+\xP@parC)/2\relax
952
      \xP@velocity\xP@parD\xP@velD
Compute the approximations for the arc length on the two smaller parameter intervals
```

(A-B-C) and (C-D-E).

```
954
     \xP@lenA
       \dimexpr(\xP@velA+4\xP@velB+\xP@velC)/6*(\xP@parC-\xP@parA)/\xP@bigdim\relax
955
956
       \dimexpr(\xP@velC+4\xP@velD+\xP@velE)/6*(\xP@parE-\xP@parC)/\xP@bigdim\relax
957
958
     \xP@partlen\dimexpr\xP@lenA+\xP@lenB\relax
```

Check whether the approximation for the arc length has changed more than the precision parameter. The code is a hack to compare the absolute value without occupying another dimension register.

```
{\@tempdima\dimexpr\xP@oldpartlen-\xP@partlen\relax
960
     \expandafter}\ifdim\ifdim\@tempdima<\z@-\fi\@tempdima>\xP@tolerance
Yes?
    Subdivide the interval. The input queue serves as a LIFO stack here!
       \edef\next@{%
961
         \noexpand\xP@arclength\xP@parB\xP@velB\xP@parC\xP@velC\xP@lenA
962
         963
         {\the\xP@velE}{\the\xP@lenB}%
964
       }%
965
     \else
966
No? Proceed to the next parameter interval.
       \xP@parA\xP@parE
967
       \xP@velA\xP@velE
968
969
       \advance\@tempdimb\xP@partlen
       \DN@{}%
970
971
     \fi
     \next@
972
973 }
```

9.7 New improved curve styles

```
Extend the list of curve styles for which special routines exist. New curve styles: 3{.}, {~},
   \@crv@
           2{~}, 3{~}, {~~}, 2{~~}, 3{~~}
\xP@@crv@
            974 \xP@hook{curve}{@crv@}
            975 \newcommand*\xP@@crv@[2]{\DN@{#1#2}%
                  \ifx\next@\@empty \edef\next@{\crv@defaultshape}%
            976
                  \ifx\bstartPLACE@\@empty\xdef\crvSTYLE@@{{\crv@defaultshape}}\fi
            977
            978
                  \else
                  \ifx\bstartPLACE@\@empty\gdef\crvSTYLE@@{#1{#2}}\fi
            979
            980
                  \ifx\next@\@empty\crv@noobject \DN@{\crv@{}{\xy@@crvaddstack@}}%
            981
                  \else\def\tmp@{-}\ifx\next@\tmp@ \DN@{\crv@{}{\xy@@crvaddstack@}}%
            982
                  \else\def\tmp@{=}\ifx\next@\tmp@
            983
            984
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir{=}}}%
                  \left(2-\right) ifx\left(tmp0\right)
            985
            986
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir{2.}}}%
            987
                  \left(3-\right) ifx\left(tmp0{3-}\right)
            988
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir{3.}}}%
                  \else\def\tmp@{--}\ifx\next@\tmp@
            989
                  \DN@{\expandafter\crv@\crv@specialtemplate@{--}}%
            990
                  \else\def\tmp@{==}\ifx\next@\tmp@
            991
            992
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir2{--}}}%
                  \left(\frac{2--}{ifx}\right)
            993
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir2{--}}}%
            994
                  \else\def\tmp@{3--}\ifx\next@\tmp@
            995
                  \label{lem:lambda} $$ DNO{\operatorname{\crv}Onormaltemplate}\dir3{--}}\% $$ Pooline{\operatorname{\crv}Onormaltemplate}. $$
            996
                  \else\def\tmp@{.}\ifx\next@\tmp@
            997
                  \DN@{\expandafter\crv@\crv@specialtemplate@{.}}%
            998
                  \else\def\tmp@{:}\ifx\next@\tmp@
            999
            1000
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir{:}}}%
           1001
                  \else\def\tmp@{2.}\ifx\next@\tmp@
                  \DN@{\expandafter\crv@\crv@normaltemplate{\dir{:}}}%
           1002
```

```
\else\def\tmp@{3.}\ifx\next@\tmp@
                          1003
                          1004
                               \DN@{\expandafter\crv@\crv@normaltemplate{\dir3{.}}}%
                          1005
                                \else\def\tmp@{~}\ifx\next@\tmp@
                                \DNO{\expandafter\crv@\crv@normaltemplate{\dir{~}}}%
                          1006
                          1007
                                \left(2^{\infty}\right)
                               \DN@{\expandafter\crv@\crv@normaltemplate{\dir2{~}}}%
                          1008
                               \else\def\tmp@{3~}\ifx\next@\tmp@
                          1009
                               \DN@{\expandafter\crv@\crv@normaltemplate{\dir3{~}}}%
                          1010
                          1011
                               \else\def\tmp@{~~}\ifx\next@\tmp@
                               \DNO{\expandafter\crv@\crv@normaltemplate{\dir{~~}}}}%
                          1012
                          1013
                               \left(2^{-}\right) ifx\left(tmp@\left(2^{-}\right)\right)
                               \DNO{\expandafter\crv@\crv@normaltemplate{\dir2{~~}}}%
                          1014
                               \end{area} $$ \left(3^{-}\right) ifx\left(tmp@\end{area}\right) $$
                          1015
                                \DNO{\expandafter\crv@\crv@normaltemplate{\dir3{~~}}}%
                          1016
                          1017
                                \else\def\tmp@{..}\ifx\next@\tmp@
                          1018
                               \DN@{\expandafter\crv@\crv@specialtemplate@{.}}%
                          1019
                                \DNO{\expandafter\crv@\crv@othertemplate{\dir#1{#2}}}%
                          1020
                               1021
  \xysplinespecialcases@
                          \dir2{~~}, \dir3{~~}
\xP@xysplinespecialcases@
                          1022 \xP@hook{curve}{xysplinespecialcases@}
                          1023 \newcommand*\xP@xysplinespecialcases@{%
                          1024
                               \ifx\@empty\xycrvdrop@
                          1025
                               \ifx\@empty\xycrvconn@\DN@{\splinesolid@}%
                          1026
                               \else\DN@{\dir{-}}\ifx\next@\xycrvconn@\DN@{\splinesolid@}%
                          1027
                               \else\DNO{ \dir2{-}}\ifx\next@\xycrvconn@\DNO{\splinedoubled@}%
                               \else\DN@{\dir{=}}\ifx\next@\xycrvconn@\DN@{\splineribboned@}%
                          1028
                          1029
                               \else\DN@{\dir{2.}}\ifx\next@\xycrvconn@\DN@{\splinedoubled@}%
                               \else\DNO{ \dir3{-}}\ifx\next@\xycrvconn@\DNO{\splinetrebled@}%
                          1030
                          1031
                               \else\DN@{\dir{3.}}\ifx\next@\xycrvconn@\DN@{\splinetrebled@}%
                               \else\DN0{ \dir{--}}\ifx\next@\xycrvconn@\DN@{\splinedashed@}%
                          1032
                          1033
                               \else\DNO{ \dir{.}}\ifx\next@\xycrvconn@\DNO{\splinedotted@}%
                               \else\DN@{\dir{:}}\ifx\next@\xycrvconn@\DN@{\splinedbldotted@}%
                          1034
                          The next line does not occur in Xy-pic for an unknown reason. However, it seems reasonable
                          to define the special pattern \dir2{.} in the same way as for straight lines.
                          1035
                                \else\DN@{\dir2{.}}\ifx\next@\xycrvconn@\DN@{\splinedbldotted@}%
                          1036
                                \else\DN@{\dir3{.}}\ifx\next@\xycrvconn@\DN@{\xP@splinetrbldotted}%
                          1037
                                \else\DN0{ \dir2{--}}\ifx\next@\xycrvconn@\DN0{\xP@splinedbldashed}%
                          1038
                               \else\DN@{\dir3{--}}\ifx\next@\xycrvconn@\DN@{\xP@splinetrbldashed}%
                                \else\DN0{ \dir{~}}\ifx\next@\xycrvconn@\DN0{\xP@splinesquiggled}%
                          1040
                               \else\DN@{\dir2{~}}\ifx\next@\xycrvconn@\DN@{\xP@splinedblsquiggled}%
                          1041
                               \else\DN@{\dir3{~}}\ifx\next@\xycrvconn@\DN@{\xP@splinetrblsquiggled}%
                               \else\DN@{\dir{~~}}\ifx\next@\xycrvconn@\DN@{\xP@splinebrokensquiggled}%
                          1042
                               \else\DN@{\dir2{~~}}\ifx\next@\xycrvconn@\DN@{\xP@splinebrokendblsquiggled}%
                          1043
                          1044
                               \else\DN@{\dir3{~~}}\ifx\next@\xycrvconn@\DN@{\xP@splinebrokentrblsquiggled}%
                               \else\ifdim\splinetol@>\z@\else\splinedefaulttol@\fi
                          1045
                          1046
                               1047
                          1048
                               \DN@{\splineset@@}%
                          1049
                               \ifInvisible@\DN@{}\fi
                          1050
                          1051
                                \next@
                          1052 }
```

9.8 Multiple solid curves

```
\xP@splinedoubled@
                      1053 \xP@hook{curve}{splinedoubled@}
                      1054 \newcommand*\xP@splinedoubled@{%
                            \xP@checkspline\xP@splinemultsolid\xP@doublestroke}
\xP@splineribboned@
                      1056 \xP@hook{curve}{splineribboned@}
                      1057 \@ifdefinable\xP@splineribboned@\relax
                      1058 \let\xP@splineribboned@\xP@splinedoubled@
 \xP@splinetrebled@
                      1059 \xP@hook{curve}{splinetrebled@}
                      1060 \newcommand*\xP@splinetrebled@{%
                            \xP@checkspline\xP@splinemultsolid\xP@trblstroke}
                      Offset parameters for double lines and curves
   \xP@doublestroke
                      1062 \verb|\newcommand*\xP@doublestroke{\xydashh@/2,-\xydashh@/2}|
     \xP@trblstroke
                      Offset parameters for treble lines and curves
                      1063 \newcommand*\xP@trblstroke{\xydashh@,\z@,-\xydashh@}
                      Get and check spline parameters before the macro in #1 is executed.
    \xP@checkspline
                      1064 \newcommand*\xP@checkspline[1] {%
                            \readsplineparams@
                      Neglect splines which are drawn "backwards". Somehow Xy-pic draws curves forward and
                      backward, but we need it to be drawn only once.
                            \let\next@\@gobble
                      1066
                            \ifdim\dimen5<\dimen7
                      1067
                      1068
                               \xP@preparespline
                      Neglect splines of zero length.
                               \ifdim\@tempdimb>\z@
                      If the path length is less than twice the line width, just draw a solid path.
                      1070
                                 \ifdim\@tempdimb<2\dimexpr\xP@preclw\relax
                      1071
                                   \let\next@\xP@splinemultsolid
                      1072
                                 \else
                                   \let\next@#1%
                      1073
                      1074
                                 \fi
                               \fi
                      1075
                            \fi
                      1076
                      1077
                            \next@
                      1078 }
\xP@splinemultsolid
                      •1
                      1079 \newcommand*\xP@splinemultsolid[1]{{%
                            \xP@inibigdim
                      1080
                            \ensuremath{\tt Qtemptokena{}}\%
                      1081
                            \xP@setsolidpat
                      1082
                      The \Offor loop does the multiple strokes. \Otempa records the respective offset distance.
                            \@for\@tempa:={#1}\do{\xP@paintsolid\z@\xP@bigdim}%
                      1083
                            \xP@stroke{\the\@temptokena}%
                      1084
                      1085 }}
```

\xP@paintsolid •1 •5 Draw a solid spline in the parameter interval [#1, #2] ⊆ [0pt, \xP@bigdim] with a certain offset. The offset distance is expected in \@tempa.

1086 \newcommand*\xP@paintsolid[2]{{\%}

Record the original anchor points.

```
1087
     \xP@savepts
     \xP@a#1\relax
1088
     \xP@c#2\relax
1089
1090
     \xP@movetotrue
     \xP@paintsolid@
1091
     1092
1093
     \@temptokena\expandafter{\@gtempa}%
1094
1095 }
```

\xP@paintsolid@

●1 **●**5

1096 \newcommand*\xP@paintsolid@{%

These parameters record which part of the spline is currently being offset. They are varied as the spline may be subdivided for a precise offset curve.

```
1097 \xP@b\xP@c

Offset distance

1098 \xP@off\dimexpr\@tempa\relax
1099 \ifdim\xP@off=\z@
1100 \xP@shaveprec\xP@a\xP@c
1101 \else
1102 \loop
```

Restore the original anchor points.

```
1103 \xP@restorepts
```

Compute the approximate offset curve. Note that $\xP@a$ and $\xP@b$ contain the boundary parameters for the partial spline.

```
1104 \xP@offsetsegment
```

Test if the offset curve is good enough.

```
1105 \xP@testoffset
```

If not, shorten the parameter interval by 30%.

```
1106     \unless\ifxP@offsetok
1107     \xP@b\dimexpr\xP@a+(\xP@b-\xP@a)*7/10\relax
1108     \repeat
1109     \fi
```

Append the new segment to the path.

```
1110 \xP@append\@temptokena{\ifxP@moveto\xP@coor\X@p\Y@p m \fi

1111 \xP@coor\L@c\U@c\xP@coor\R@c\D@c\xP@coor\X@c\Y@c c }%

1112 \xP@movetofalse
```

Test if the end of the spline has been reached. If not, offset the rest of the curve.

```
1113 \ifdim\xP@b<\xP@c\relax
1114 \xP@a\xP@b
1115 \expandafter\xP@paintsolid@
1116 \fi
1117 }</pre>
```

\iffxP@moveto We need a PDF moveto operator only for the first partial segment. Additional segments connect seamlessly.

```
1118 \verb|\definable\\ifxP@moveto\\relax|
```

- 1119 \@ifdefinable\xP@movetotrue\relax
- 1120 \@ifdefinable\xP@movetofalse\relax
- 1121 \newif\ifxP@moveto

\xP@savepts

•5 Save the anchor points to the second set of reserved variables.

```
1122 \newcommand*\xP@savepts{%
```

- 1123 \xP@xa\X@p
- 1124 \xP@ya\Y@p
- 1125 \xP@xb\L@c
- 1126 \xP@yb\U@c
- 1127 \xP@xc\R@c
- 1128 \xP@yc\D@c
- 1129 \xP@xd\X@c
- 1130 \xP@yd\Y@c
- 1131 }

\xP@restorepts

•5 Restore the anchor points from the second set of reserved variables.

```
1132 \newcommand*\xP@restorepts{%
```

- 1133 **\X@p\xP@xa**
- 1134 \Y@p\xP@ya
- 1135 \L@c\xP@xb
- 1136 \U@c\xP@yb
- 1137 \R@c\xP@xc
- 1138 \D@c\xP@yc
- 1139 \X@c\xP@xd
- 1140 \Y@c\xP@yd
- 1141 }

9.9 A Bézier curve offset algorithm

First, all control points are offset by the desired distance and in the direction of the normal vectors at the boundary points of the curve. We then adjust the distance of the inner two control points to the boundary control points along the tangents at the boundary points: $x_b = x_a + f_a T_{ax}$, $x_c = x_d + f_d T_{dx}$, and likewise for the y-coordinates. In nondegenerate cases, we have $T_{ax} = x_b - x_a$ and $T_{dx} = x_c - x_d$.

Let P(a, b, c, d, t) denote the Bézier polynomial $a(1-t)^3 + 3bt(1-t)^2 + 3ct^2(1-t) + dt^3$. In order to determine the factors f_a and f_d , we set up a system of three equations.

• Two equations: The old point at parameter $\frac{1}{2}$ plus offset, (x_m, y_m) , is the new point at parameter t_m .

$$x_m = P(x_a, x_a + f_a T_{ax}, x_d + f_d T_{dx}, x_d, t_m)$$

$$y_m = P(y_a, y_a + f_a T_{ay}, y_d + f_d T_{dy}, y_d, t_m)$$

• Third equation: The old tangent at parameter $\frac{1}{2}$ is in the same direction as the new tangent at t_m .

$$\frac{\partial}{\partial t_m} P(x_a, x_a + f_a T_{ax}, x_d + f_d T_{dx}, x_d, t_m) \cdot T_{my}$$

$$= \frac{\partial}{\partial t_m} P(y_a, y_a + f_a T_{ay}, y_d + f_d T_{dy}, y_d, t_m) \cdot T_{mx}$$

Up to a scalar factor of -3/4, (T_{mx}, T_{my}) is the velocity vector to the original curve at parameter $\frac{1}{2}$. We have $T_{mx} = (X_a + X_b - X_c - X_d)/2$ (in the old coordinates!) and T_{my} analogously. The system above is a nonlinear system of three equations in three variables, which we solve by Newton's method. Let f_a , f_d , and t_m be approximate solutions, and denote by Δf_a , Δf_d , and Δt_m the increments to the next approximation. In the first order, the three equations become:

$$x_{m} = P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m}) + \Delta f_{a} \cdot T_{ax} \cdot 3t_{m} (1 - t_{m})^{2} + \Delta f_{d} \cdot T_{dx} \cdot 3t_{m}^{2} (1 - t_{m})$$

$$+ \Delta t_{m} \frac{\partial}{\partial t_{m}} P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m})$$

$$y_{m} = P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m}) + \Delta f_{a} \cdot T_{ay} \cdot 3t_{m} (1 - t_{m})^{2} + \Delta f_{d} \cdot T_{dy} \cdot 3t_{m}^{2} (1 - t_{m})$$

$$+ \Delta t_{m} \frac{\partial}{\partial t_{m}} P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m})$$

$$\left(\frac{\partial}{\partial t_{m}} P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m}) + \Delta f_{a} \cdot T_{ax} \cdot 3(1 - 4t_{m} + 3t_{m}^{2}) + \Delta f_{d} \cdot T_{dx} \cdot 3(2t_{m} - 3t_{m}^{2})\right)$$

$$+ \Delta t_{m} \cdot 6 \left((x_{a} - 2x_{b} + x_{c}) + t_{m}(x_{d} - x_{a} + 3(x_{b} - x_{c}))\right) \cdot T_{my}$$

$$= \left(\frac{\partial}{\partial t_{m}} P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m}) + \Delta f_{a} \cdot T_{ay} \cdot 3(1 - 4t_{m} + 3t_{m}^{2}) + \Delta f_{d} \cdot T_{dy} \cdot 3(2t_{m} - 3t_{m}^{2})\right)$$

$$+ \Delta t_{m} \cdot 6 \left((y_{a} - 2y_{b} + y_{c}) + t_{m}(y_{d} - y_{a} + 3(y_{b} - y_{c}))\right) \cdot T_{mx}$$

Rewrite the equations so that they resemble the TFX code.

$$8P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m}) - 8x_{m} = -\Delta f_{a} \cdot 3T_{ax} \cdot 2t_{m} \cdot (2(1 - t_{m}))^{2}$$

$$-\Delta f_{d} \cdot 3T_{dx} \cdot 4t_{m}^{2} \cdot 2(1 - t_{m}) - \Delta t_{m} \cdot 8\frac{\partial}{\partial t_{m}} P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m})$$

$$8P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m}) - 8y_{m} = -\Delta f_{a} \cdot 3T_{ay} \cdot 2t_{m} \cdot (2(1 - t_{m}))^{2}$$

$$-\Delta f_{d} \cdot 3T_{dy} \cdot 4t_{m}^{2} \cdot 2(1 - t_{m}) - \Delta t_{m} \cdot 8\frac{\partial}{\partial t_{m}} P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m})$$

$$T_{mx} \cdot 8\frac{\partial}{\partial t_{m}} P(y_{a}, y_{b}, y_{c}, y_{d}, t_{m}) - T_{my} \cdot 8\frac{\partial}{\partial t_{m}} P(x_{a}, x_{b}, x_{c}, x_{d}, t_{m})$$

$$= -\Delta f_{a} \cdot (3T_{ay} \cdot 2T_{mx} - 3T_{ax} \cdot 2T_{my}) \cdot 2(1 - 3t_{m}) \cdot 2(1 - t_{m})$$

$$-\Delta f_{d} \cdot (3T_{dy} \cdot 2T_{mx} - 3T_{dx} \cdot 2T_{my}) \cdot 2(2 - 3t_{m}) \cdot 2t_{m}$$

$$-\Delta t_{m} \cdot (((y_{d} - y_{a} + 3(y_{b} - y_{c})) \cdot 2t_{m} + 2(y_{a} - 2y_{b} + y_{c})) \cdot 3 \cdot 8T_{mx}$$

$$-((x_{d} - x_{a} + 3(x_{b} - x_{c})) \cdot 2t_{m} + 2(x_{a} - 2x_{b} + x_{c})) \cdot 3 \cdot 8T_{my})$$

Substitute $2t_m = \tau_m$.

$$\begin{split} 8P(x_{a},x_{b},x_{c},x_{d},t_{m}) - 8x_{m} &= -\Delta f_{a} \cdot 3T_{ax} \cdot \tau_{m}(2-\tau_{m})^{2} \\ - \Delta f_{d} \cdot 3T_{dx} \cdot \tau_{m}^{2}(2-\tau_{m}) - \frac{1}{2}\Delta\tau_{m} \cdot 8\frac{\partial}{\partial t_{m}}P(x_{a},x_{b},x_{c},x_{d},t_{m}) \\ 8P(y_{a},y_{b},y_{c},y_{d},t_{m}) - 8y_{m} &= -\Delta f_{a} \cdot 3T_{ay} \cdot \tau_{m} \cdot (2-\tau_{m})^{2} \\ - \Delta f_{d} \cdot 3T_{dy} \cdot \tau_{m}^{2}(2-\tau_{m}) - \frac{1}{2}\Delta\tau_{m} \cdot 8\frac{\partial}{\partial t_{m}}P(y_{a},y_{b},y_{c},y_{d},t_{m}) \\ T_{mx} \cdot 8\frac{\partial}{\partial t_{m}}P(y_{a},y_{b},y_{c},y_{d},t_{m}) - T_{my} \cdot 8\frac{\partial}{\partial t_{m}}P(x_{a},x_{b},x_{c},x_{d},t_{m}) \\ &= -\Delta f_{a} \cdot (3T_{ay} \cdot 2T_{mx} - 3T_{ax} \cdot 2T_{my}) \cdot (2-3\tau_{m})(2-\tau_{m}) \\ - \Delta f_{d} \cdot (3T_{dy} \cdot 2T_{mx} - 3T_{dx} \cdot 2T_{my}) \cdot (4-3\tau_{m})\tau_{m} \\ -\Delta \tau_{m} \cdot (((y_{d}-y_{a}+3(y_{b}-y_{c})) \cdot \tau_{m}+2(y_{a}-2y_{b}+y_{c})) \cdot 12T_{mx} \\ - ((x_{d}-x_{a}+3(x_{b}-x_{c})) \cdot \tau_{m}+2(x_{a}-2x_{b}+x_{c})) \cdot 12T_{my}) \end{split}$$

The translation into T_EX dimensions:

- $f_a = \xPOfd$
- $\tau_m = \xpQtm$
- $x_a = \xp@xa, \dots, x_d = \xp@xd, \dots, y_d = \xp@yd$
- $8P(x_1, x_2, x_3, x_4, \frac{1}{2}x_5) = \text{\mathbb{Z}}$
- $8x_m = \xp@xm, 8y_m = \xp@ym$
- $3T_{ax} = \xp@Tax$, $3T_{dx} = \xp@Tdx$, $3T_{ay} = \xp@Tay$, $3T_{dy} = \xp@Tdy$
- $8\frac{\partial}{\partial x_5}P(x_1,x_2,x_3,x_4,\frac{1}{2}x_5) = \xP@beziertan#1#2#3#4#5$

Temporary:

- $2 \tau_m = \xpQta$
- $\tau_m(2-\tau_m) = \mathbf{xP@tb}$
- $T_{mx} = \xrpet{Tmx}, T_{my} = \xrpet{Tmy}$
- $2-3\tau_m=\xrper{\text{Qtb}}$
- $4-3\tau_m = \xp@tc$

Since the linear system above tends to be singular or ill-conditioned (think about the frequent case when all control points are nearly collinear!), the Gauss algorithm \xP@solvelinearsystem does not always return a valid solution. In these cases, the system is not solved exactly but approximated iteratively in \xP@applinsys.

```
\xP@tmx
\xP@tmy
\1142 \@ifdefinable\xP@tmx\relax
\1143 \@ifdefinable\xP@tmy\relax
\xP@Tmxy
\xP@Tmxy
\xP@Tmyx
\1144 \newcommand*\xP@Tmxy{*\xP@Tmx/\xP@Tmy}
\1145 \newcommand*\xP@Tmyx{*\xP@Tmy/\xP@Tmx}
\xP@Tmzero
\1146 \newcommand*\xP@Tmzero{*\z@}
```

\xP@offsetsegment

•1 •3 •4 Offset a cubic segment. The offset distance is given in $\xP@off$. The anchor points are given in $\xP@off$. The partial spline in the parameter interval $[\xP@a, \xP@b] \subseteq [0pt, \xP@bigdim]$ is offset. The new Bézier curve is returned in $\xP@xa, ..., \xP@yd$.

1147 \newcommand*\xP@offsetsegment{{%

New first anchor point and tangent vector at 0

- 1148 \xP@tangentvec\xP@a
- 1149 \xP@xa\dimexpr\xP@precbezierpoly\X@p\L@c\R@c\X@c\xP@a/8%
- +\d@Y*\xP@off/\@tempdimb\relax
- ${\tt 1151} \verb|\xP@ya\dimexpr\xP@precbezierpoly\Y@p\U@c\D@c\xP@a/8\%|}$
- 1152 -\d@X*\xP@off/\@tempdimb\relax
- 1153 \xP@scaleT
- 1154 \xP@Tax\d@X
- 1155 \xP@Tay\d@Y
- 1156 $\xP@E\@tempdimb$

New last anchor point and tangent vector at 1

```
1157
      \xP@tangentvec\xP@b
      \xP@xd\dimexpr\xP@precbezierpoly\X@p\L@c\R@c\X@c\xP@b/8%
1158
        +\d@Y*\xP@off/\@tempdimb\relax
1159
      \xP@yd\dimexpr\xP@precbezierpoly\Y@p\U@c\D@c\Y@c\xP@b/8%
1160
        -\d@X*\xP@off/\@tempdimb\relax
1161
1162
      \xP@scaleT
1163
      \xP@Tdx-\d@X
1164
      \xP@Tdy-\d@Y
1165
      \xP@F\@tempdimb
Scalar product of the tangent vectors
      \xP@M\z@
1166
      \xP@Max\xP@M\xP@Tdx
1167
1168
      \xP@Max\xP@M\xP@Tdy
      \xP@L\dimexpr\xP@Tax*\xP@Tdx/\xP@M+\xP@Tay*\xP@Tdy/\xP@M\relax
1169
      \xP0tm\dimexpr(\xP0a+\xP0b)/2\relax
1170
      \in \xPQL>\dimexpr\xPQE*\xPQF/\xPQM*49/50\relax
1171
```

Trick to improve the offset algorithm near sharp bends and cusps: If the tangent vectors (T_{ax}, T_{ay}) and (T_{dx}, T_{dy}) point nearly in the same direction, we do not use the true tangent vector for (T_{mx}, T_{my}) at the middle point but a fake one. (The exact condition is that their normed scalar product is greater that 49/50. For a straight line, the vectors would point in opposite directions.) The fake tangent vector is defined to be $(T_{ax} + T_{dx}, T_{ay} + T_{dy})$ rotated by $\pm 90^{\circ}$. Its direction is chosen such that the scalar product with $(X_d - X_a, Y_d - Y_a)$ is nonnegative. (Use $(X_c - X_b, Y_c - Y_b)$ in the degenerate case $(X_d - X_a, Y_d - Y_a) = (0, 0)$.)

Rationale: In the presence of a sharp bend or cusp, the offset algorithm will hardly meet the tip. Since the tangent/normal at the tip is needed for a good offset curve, we provide this artificially.

```
\d@X-\dimexpr\xP@Tay+\xP@Tdy\relax
1172
         \d@Y\dimexpr\xP@Tax+\xP@Tdx\relax
1173
         \xP@veclen
1174
         \xP@A\dimexpr\X@c-\X@p\relax
1175
1176
         \xP@B\dimexpr\Y@c-\Y@p\relax
         \xP@M\z@
1177
         \xP@Max\xP@M\xP@A
1178
         \xP@Max\xP@M\xP@B
1179
         \ifdim\xP@M=\z@
1180
           \xP@A\dimexpr\R@c-\L@c\relax
1181
1182
           \xP@B\dimexpr\D@c-\U@c\relax
1183
           \xP@Max\xP@M\xP@A
           \xP@Max\xP@M\xP@B
1184
1185
         \xP@M\dimexpr\d@X*\xP@A/\xP@M+\d@Y*\xP@B/\xP@M\relax
1186
         \left| xP@M<\z \right|
1187
           \multiply\d@X\m@ne
1188
1189
           \multiply\d@Y\m@ne
         \fi
1190
      \else
Normal case: tangent vector at the middle point.
1192
         \xP@tangentvec\xP@tm
```

From here on, \xP@a and \xP@b will not be used any more, so these variables can be used under their other names \xP@I, \xP@J for the linear systems below.

8 times (middle point plus offset)

```
\xP@xm\dimexpr\xP@precbezierpoly\X@p\L@c\R@c\X@c\xP@tm%
1194
1195
                      +8\d@Y*\xP@off/\@tempdimb\relax
1196
                \xP@ym\dimexpr\xP@precbezierpoly\Y@p\U@c\D@c\Y@c\xP@tm%
                      -8\d@X*\xP@off/\@tempdimb\relax
1197
Tangent at middle point
                \xP@Tmx\d@X
                \xP@Tmv\d@Y
1199
                \xP@ifabsless\xP@Tmy\xP@Tmx
1200
                      1201
1202
                      \let\xP@tmx\@empty
1203
                \else
                      \ifdim\xP@Tmy=\z@
1204
1205
                           \let\xP@tmx\xP@Tmzero
1206
                           \let\xP@tmy\xP@Tmzero
1207
                      \else
1208
                           \let\xP@tmy\@empty
1209
                           \let\xP@tmx\xP@Tmxy
1210
                      \fi
                \fi
1211
Initial guesses for the tangent vector scalings \xP@fa, \xP@fd and the near-middle position
\xP@tm
1212
                \xP0fa\p0
1213
                \xP@fd\p@
1214
                \xP@tm\p@
The main loop for finding the offset curve
                \count@\z@
1216
                \loop
Set the new control points up.
                      \xP@offsetpoints
1217
1218
                      \@tempswafalse
At most 10 iterations
                      \ifnum10>\count@
Determine the quality of the approximation by an objective function.
1220
                           \xP@objfun\xP@oldobj
1221
                           \ifdim\xP@oldobj>\xP@maxobjfun\relax\@tempswatrue\fi
1222
                      \fi
1223
                \if@tempswa
                      \xP@offsetloop
1224
                \repeat
1225
Return the new anchor points.
                1226
                      \label{location} $$L@c\theta\xP@xb\U@c\theta\xP@yb\R@c\theta\xP@xc\D@c\theta\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP@yc\xP&yc\xP@yc\xP&yc\xP@yc\xP&yc\xP@yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\xP&yc\x
1227
1228
                      1229
                }%
1230
                \@gtempa
1231 }
```

\xP@scale

•1 •3 •4 This macro contains another trick to improve the offset algorithm around sharp bends and cusps. It adjusts the length of the tangent/velocity vectors. Let (\d@X, \d@Y) be the velocity vector to the original curve at some point with velocity v_0 . The velocity at the same point, considered on a partial segment scales linearly with the length of the parameter interval. Hence, the velocity v_1 in the partial segment is $v_1 = v_0 \cdot (xp_0)$

 $\xp@a)/\xp@bigdim$. Additionally the offset curve goes with a radius of $r+\xp@off$ around bends with radius r in the original curve. As an approximation to the velocity in the offset curve, we therefore scale the velocity vector in the end to the norm $v_1 + 2\pi \cdot |\xp@off|$.

```
1232 \newcommand*\xP@scaleT{%
1233
      \xP@B6.28\xP@off
1234
      \xP@abs\xP@B
      \xP@C\dimexpr\d@X*\xP@B/\@tempdimb\relax
1235
      \xP@D\dimexpr\d@Y*\xP@B/\@tempdimb\relax
1236
1237
      \xP@A\dimexpr\xP@b-\xP@a\relax
1238
      \d@X\dimexpr\xP@C+\d@X*\xP@A/\xP@bigdim\relax
      \d@Y\dimexpr\xP@D+\d@Y*\xP@A/\xP@bigdim\relax
Also record the change to the norm of the vector.
      \@tempdimb\dimexpr\xP@B+\@tempdimb*\xP@A/\xP@bigdim\relax
1241 }
•1 •3 •4 The iteration in the offset loop: set up and solve (or approximate) the linear
system.
1242 \newcommand*\xP@offsetloop{%
1243
      \xP@C\dimexpr\xP@C/2\relax
1244
      \xP@G\dimexpr\xP@G/2\relax
1st linear equation
      \xP@ta\dimexpr2\p@-\xP@tm\relax
1245
      \xP@tb\dimexpr\xP@tm*\xP@ta/\p@\relax
1246
1247
      \xP@A\dimexpr\xP@Tax*\xP@tb/\p@*\xP@ta/\p@\relax
      \xP@B\dimexpr\xP@Tdx*\xP@tb/\p@*\xP@tm/\p@\relax
2nd linear equation
      \xP@E\dimexpr\xP@Tay*\xP@tb/\p@*\xP@ta/\p@\relax
      \xP@F\dimexpr\xP@Tdy*\xP@tb/\p@*\xP@tm/\p@\relax
1250
3rd linear equation
      \xP@tb\dimexpr2\p@-3\xP@tm\relax
1251
1252
      \xP@tc\dimexpr\xP@tb+2\p@\relax
      \xP@I\dimexpr(2\xP@Tay\xP@tmx-2\xP@Tax\xP@tmy)*\xP@tb/\p@*\xP@ta/\p@\relax
1254
      \xP@J\dimexpr(2\xP@tmx-2\xP@tdx\xP@tmy)*\xP@tc/\p@*\xP@tm/\p@\relax
      \xP@K\dimexpr((\xP@yd-\xP@ya+(\xP@yb-\xP@yc)*3)
1255
        1256
        -((\xP@xd-\xP@xa+(\xP@xb-\xP@xc)*3)
1257
1258
        *\xPQtm/\pQ+(\xPQxc-2\xPQxb+\xPQxa)*2)*12\xPQtmy\relax
Solve the system.
      \xP@solvelinearsystem
1259
      \ifxP@validsol
Check whether the result is feasible and whether it actually improves the approximation.
        \xP@correctsol
1261
        \left\langle xP@ta=\z@\right\rangle
1262
1263
        \ifdim\xP@tb=\z@
        \left( xP0tc=\z 0\right)
1264
1265
          \xP@validsolfalse
1266
        \fi\fi\fi
1267
      \fi
If the exact solution is not valid, try to at least approximate a solution.
1268
      \ifxP@validsol
      \else
1269
```

\xP@offsetloop

\xP@applinsys

```
This time, the solution is not checked but applied immediately.
                 1271
                          \advance\xP0fa-\xP0ta
                 1272
                          \advance\xP@fd-\xP@tb
                 1273
                          \advance\xP0tm-\xP0tc
                 The near-middle parameter on the curve must not lie outside the segment.
                          \ifdim\xP@tm<\z@\xP@tm\z@\fi
                 1275
                          \left( xP0tm>2\right) xP0tm2\left( fi
                 1276
                       \fi
                 1277
                       \advance\count@\@ne
                 1278 }
                 Heuristic: maximal solution so that no arithmetic overflow is produced.
    \xP@maxsol
                 1279 \newcommand*\xP@maxsol{3pt}
\xP@correctsol •3 •4 Check whether the solution is feasible and actually improves the objective function.
                 1280 \newcommand*\xP@correctsol{%
                 If the solution is too big, scale all variables uniformly.
                       \xP@M\z@
                 1281
                 1282
                       \xP@Max\xP@M\xP@ta
                       \xP@Max\xP@M\xP@tb
                 1283
                 1284
                       \xP@Max\xP@M\xP@tc
                 1285
                       \ifdim\xP@M>\xP@maxsol
                 1286
                          \xP@ta\dimexpr\xP@maxsol*\xP@ta/\xP@M\relax
                          \xP@tb\dimexpr\xP@maxsol*\xP@tb/\xP@M\relax
                 1287
                 1288
                          \xP@tc\dimexpr\xP@maxsol*\xP@tc/\xP@M\relax
                 1289
                       \fi
                 Apply the solution. Save the old value of \xP@tm to be able to restore it.
                 1290
                       \advance\xP@fa-\xP@ta
                       \advance\xP@fd-\xP@tb
                 1291
                       \xP@M\xP@tm
                 1292
                 1293
                       \advance\xP@tm-\xP@tc
                 The near-middle parameter must lie on the segment.
                       \ifdim\xP@tm<\z@\xP@tm\z@\fi
                 1295
                       \left( xP0tm>2\right) xP0tm2\left( p0\right) fi
                 Check whether the solution actually improves the objective function.
                       {\xP@offsetpoints
                 1296
                 1297
                          \xP@objfun\xP@M
                       \expandafter}%
                 If not, restore the old values and declare the solution invalid.
```

```
1299 \ifdim\xP@M>\xP@oldobj
1300 \advance\xP@fa\xP@ta
1301 \advance\xP@fd\xP@tb
1302 \xP@tm\xP@M
1303 \xP@validsolfalse
1304 \fi
1305 }
```

\xP@objfun

 $\bullet 3$ $\bullet 4$ The objective function: sum of squares of the deviation in x- and y-direction and the angular deviation at the middle point. We also compute some terms which will be used in the linear system.

```
\label{limits} $1306 \mbox{$\mbox{$1307$} \mbox{$1307$} $$ \mbox{$\mbox{$1307$} \mbox{$\mbox{$P@xd\xP@xm\relax}$} $$
```

```
\xP@H\dimexpr\xP@bezierpoly\xP@ya\xP@yb\xP@yd\xP@tm-\xP@ym\relax
                     1308
                     1309
                           \xP@C\xP@beziertan\xP@xa\xP@xb\xP@xc\xP@xd\xP@tm
                     1310
                           \xP@G\xP@beziertan\xP@ya\xP@yb\xP@yc\xP@yd\xP@tm
                            \xP@L\dimexpr\xP@G\xP@tmx-\xP@C\xP@tmy\relax
                     1311
                     If the deviation is too big, let the objective function be \maxdimen. Otherwise, compute
                     the sum of squares.
                           #1\z@
                     1312
                     1313
                           \xP@Max#1\xP@D
                           \xP@Max#1\xP@H
                     1314
                           \xP@Max#1\xP@L
                     1315
                     1316
                           #1\ifdim#1>4843165sp
                              \maxdimen
                     1317
                     1318
                              \dimexpr\xP@D*\xP@D/\p@+\xP@H*\xP@H/\p@+\xP@L*\xP@L/\p@\relax
                     1319
                     1320
                           \fi
                     1321 }
                     •3 •4 Compute the new control points from the factors \xP@fa, \xP@fd.
  \xP@offsetpoints
                     1322 \newcommand*\xP@offsetpoints{%
                           \xP0xb\dimexpr\xP0xa+\xP0Tax*\xP0fa/196608\relax
                           \xP@yb\dimexpr\xP@ya+\xP@Tay*\xP@fa/196608\relax
                     1324
                     1325
                           \xP@xc\dimexpr\xP@xd+\xP@Tdx*\xP@fd/196608\relax
                     1326
                           \xP@yc\dimexpr\xP@yd+\xP@Tdy*\xP@fd/196608\relax
                     1327 }
                     Formula for the polynomial 8 (\#1 \cdot (1-t)^3 + 3 \cdot \#2 \cdot t(1-t)^2 + 3 \cdot \#3 \cdot t^2(1-t) + \#4 \cdot t^3).
    \xP@bezierpoly
                     t = \frac{1}{2}#5.
                     1328 \newcommand*\xP@bezierpoly[5]{%
                           \dimexpr(((#4-#1+(#2-#3)*3)*#5/\p@+(#1-2#2+#3)*6)*#5/\p@+(#2-#1)*12)*#5/\p@
                     1330
                              +#1*8\relax
                     1331 }
                     Formula for the polynomial 8 (\#1 \cdot (1-t)^3 + 3 \cdot \#2 \cdot t(1-t)^2 + 3 \cdot \#3 \cdot t^2(1-t) + \#4 \cdot t^3),
\xP@precbezierpoly
                     t = \#5/\xP@bigdim.
                     1332 \newcommand*\xP@precbezierpoly[5]{%
                           \dimexpr(((#4-#1+(#2-#3)*3)*2*#5/\xP@bigdim+(#1-2#2+#3)*6)*2*#5/\xP@bigdim
                              +(#2-#1)*12)*2*#5/\xP@bigdim+#1*8\relax
                     1334
                     1335 }
                     Formula for the polynomial
     \xP@beziertan
                           24(-#1\cdot(1-t)^2 + #2\cdot(3t^2-4t+1) + #3\cdot(-3t^2+2t) + #4\cdot t^2), \quad t = \frac{1}{2}#5.
                     Up to a scalar factor, this is the derivative of the third order Bézier polynomial above.
                     1336 \newcommand*\xP@beziertan[5]{%
                           1337
                     1338 }
                     Formula for the polynomial
 \xP@precbeziertan
                       (-\#1\cdot(1-t)^2 + \#2\cdot(3t^2-4t+1) + \#3\cdot(-3t^2+2t) + \#4\cdot t^2), \quad t = \#5/\xP@bigdim.
                     This is \frac{1}{3} times the derivative of the third order Bézier polynomial.
                     1339 \newcommand*\xP@precbeziertan[5]{%
                           \dimexpr((#4-#1+(#2-#3)*3)*#5/\xP@bigdim+(#1-2#2+#3)*2)*#5/\xP@bigdim
                     1341
                           +#2-#1\relax
                     1342 }
```

\xP@solvelinearsystem •3 The macro \xP@solvelinearsystem solves a system of three linear equations by the Gauss algorithm. The coefficients and desired values are passed in the extended matrix

```
\xP@A \xP@B \xP@C \xP@D \\xP@E \xP@E \xP@G \xP@H \xP@I \xP@L \xP@L
```

The solution is returned in the vector (xP@ta, xP@tb, xP@tc).

\xP@varone \xP@vartwo

With column swapping in the Gauss algorithm, variable names might be changed. These

macros record the variables. \xP@varthree

1343 \@ifdefinable\xP@varone\relax

1344 \@ifdefinable\xP@vartwo\relax

 $1345 \ensuremath{\mbox{\sc loss}}\ensuremath{\mbox{\sc l$

\ifxP@validsol

Records if a valid solution to the linear system is returned.

1346 \@ifdefinable\ifxP@validsol\relax

 $1347 \ensuremath{\mbox{\sc oltrue}\mbox{\sc relax}}$

1348 \@ifdefinable\xP@validsolfalse\relax

1349 \newif\ifxP@validsol

1350 \newcommand*\xP@solvelinearsystem{{%

Scale the matrix so that the highest absolute value in each row and each column is ≥ 2048 pt and < 4096pt.

1351 \xP@scalerow\xP@A\xP@B\xP@C\xP@D

\xP@scalerow\xP@E\xP@F\xP@G\xP@H 1352

1353 \xP@scalerow\xP@I\xP@J\xP@K\xP@L

1354 \xP@scalecol\xP@A\xP@E\xP@I\xP@scaleone

\xP@scalecol\xP@B\xP@F\xP@J\xP@scaletwo 1355

 $\xP@scalecol\xP@C\xP@G\xP@K\xP@scalethree$ 1356

Record the initial variable-to-column assignment.

\let\xP@varone\xP@ta

1358 \let\xP@vartwo\xP@tb

\let\xP@varthree\xP@tc 1359

Find the pivot position. \xP@M is used temporarily.

\count@\m@ne 1360

1361 \@tempcnta\m@ne

 $\xP@ifabsless\\xP@A\\xP@B\\@tempcnta\\z@\\xP@M\\xP@B$ 1362

\else\xP@M\xP@A\fi 1363

\xP@ifabsless\xP@M\xP@C\@tempcnta\@ne\xP@M\xP@C\fi 1364

\xP@ifabsless\xP@M\xP@E\@tempcnta\m@ne\count@\z@\xP@M\xP@E\fi 1365

\xP@ifabsless\xP@M\xP@F\@tempcnta\z@\count@\z@\xP@M\xP@F\fi 1366

\xP@ifabsless\xP@M\xP@G\@tempcnta\@ne\count@\z@\xP@M\xP@G\fi 1367

\xP@ifabsless\xP@M\xP@I\@tempcnta\m@ne\count@\@ne\xP@M\xP@I\fi 1368

\xP@ifabsless\xP@M\xP@J\@tempcnta\z@\count@\@ne\xP@M\xP@J\fi 1369

1370 \xP@ifabsless\xP@M\xP@K\@tempcnta\@ne\count@\@ne\fi

Swap rows

1371 \ifcase\count@

1372\xP@swapdim\xP@A\xP@E

 $\xP@swapdim\xP@B\xP@F$ 1373

\xP@swapdim\xP@C\xP@G 1374

\xP@swapdim\xP@D\xP@H 1375

\or 1376

 $\xP@swapdim\xP@A\xP@I$ 1377

```
1378
        \xP@swapdim\xP@B\xP@J
1379
        \xP@swapdim\xP@C\xP@K
1380
        \xP@swapdim\xP@D\xP@L
      \fi
1381
Swap columns
      \ifcase\@tempcnta
1382
        \xP@swapdim\xP@A\xP@B
1383
        \xP@swapdim\xP@E\xP@F
1384
        \xP@swapdim\xP@I\xP@J
1385
        \let\xP@varone\xP@tb
1386
1387
        \let\xP@vartwo\xP@ta
        \xP@swapnum\xP@scaleone\xP@scaletwo
1388
1389
      \or
1390
        \xP@swapdim\xP@A\xP@C
        \xP@swapdim\xP@E\xP@G
1391
1392
        \xP@swapdim\xP@I\xP@K
        \let\xP@varone\xP@tc
1393
1394
        \let\xP@varthree\xP@ta
        \xP@swapnum\xP@scaleone\xP@scalethree
1395
      \fi
1396
First elimination
      \multiply\xP@E\m@ne
      \multiply\xP@I\m@ne
Absolute values below are < 8192pt.
1399
      \left| xP@A=\right| z@
1400
      \else
        \advance\xP@F\dimexpr\xP@B*\xP@E/\xP@A\relax
1401
        \advance\xP@G\dimexpr\xP@C*\xP@E/\xP@A\relax
1402
1403
        \advance\xPOH\dimexpr\xPOD*\xPOE/\xPOA\relax
        \advance\xP@J\dimexpr\xP@B*\xP@I/\xP@A\relax
1404
1405
        \advance\xP@K\dimexpr\xP@C*\xP@I/\xP@A\relax
1406
        \advance\xP@L\dimexpr\xP@D*\xP@I/\xP@A\relax
      \fi
1407
Find the second pivot element. \xP@M is used temporarily.
      \count@\m@ne
1408
      1409
        \else\@tempcnta\m@ne\xP@M\xP@F\fi
1410
      \xP@ifabsless\xP@M\xP@J\@tempcnta\m@ne\count@\z@\xP@M\xP@J\fi
1411
1412
      \xP@ifabsless\xP@M\xP@K\@tempcnta\z@\count@\z@\fi
Swap rows
1413
      \ifnum\count@=\z@
        \xP@swapdim\xP@F\xP@J
1414
1415
        \xP@swapdim\xP@G\xP@K
1416
        \xP@swapdim\xP@H\xP@L
      \fi
1417
Swap columns
      \ifnum\@tempcnta=\z@
1418
        \xP@swapdim\xP@B\xP@C
1419
1420
        \xP@swapdim\xP@F\xP@G
1421
        \xP@swapdim\xP@J\xP@K
        \let\@tempa\xP@varthree
1422
1423
        \let\xP@varthree\xP@vartwo
```

\let\xP@vartwo\@tempa

```
1425
        \xP@swapnum\xP@scaletwo\xP@scalethree
1426
      \fi
Second elimination. Absolute values are < 16384pt.
      \left| xP@F=\right| z@
      \else
1428
        \advance\xP@K\dimexpr-\xP@G*\xP@J/\xP@F\relax
1429
        \advance\xP@L\dimexpr-\xP@H*\xP@J/\xP@F\relax
1430
1431
Compute the result from the upper triagonal form. Since the matrix can be singular, we
have to ensure in every step that no overflow occurs. In general, we do not allow any solution
greater than 60pt.
      \xP@ifabsless{\dimexpr\xP@L/60\relax}{\dimexpr\xP@K/\xP@scalethree\relax}%
1432
1433
        \xP@validsoltrue
1434
        \xP@varthree\dimexpr\xP@L*(\xP@scalethree*\p@)/\xP@K\relax
1435
        \xP@validsolfalse
1436
      \fi
1437
      \xP@checkabs{\xP@H/8191}{\xP@F/\xP@scaletwo}\%
1438
1439
      \xP@checkabs{\xP@G/\xP@scalethree/136}{\xP@F/\xP@scaletwo}\%
1440
      \ifxP@validsol
1441
        \xP@vartwo\dimexpr\xP@H*(\xP@scaletwo*\p@)/\xP@F
          -\xP@varthree*\xP@scaletwo/\xP@scalethree*\xP@G/\xP@F\relax
        \xP@checkabs\xP@vartwo{60pt}%
1443
1444
      \fi
1445
      \xP@checkabs{\xP@D/5461}{\xP@A/\xP@scaleone}\%
1446
      \xP0checkabs{\xP0B/\xP0scaletwo/91}{\xP0A/\xP0scaleone}\%
1447
      \xP@checkabs{\xP@C/\xP@scalethree/91}{\xP@A/\xP@scaleone}\%
      \ifxP@validsol
1448
        \xP@varone\dimexpr\xP@D*(\xP@scaleone*\p@)/\xP@A
1449
          -\xP@vartwo*\xP@scaleone/\xP@scaletwo*\xP@B/\xP@A
1450
          -\xP@varthree*\xP@scaleone/\xP@scalethree*\xP@C/\xP@A\relax
1451
        \xP@checkabs\xP@varone{60pt}%
1452
      \fi
1453
Return the result.
      \xdef\@gtempa{%
1454
        \ifxP@validsol
1455
          \xP0ta\the\xP0ta\relax
1456
1457
          \xP0tb\the\xP0tb\relax
1458
          \xP@tc\the\xP@tc\relax
          \noexpand\xP@validsoltrue
1459
1460
           \noexpand\xP@validsolfalse
1461
        \fi
1462
      }%
1463
1464
      }\@gtempa
1465 }
•3 Scale a row of the matrix to improve numerical precision. We scale by a power of two
such that the maximal length is between 2048pt and 4096pt.
1466 \newcommand*\xP@scalerow[4] {%
      \xP@M\z@
1467
      \xP@Max\xP@M#1%
1468
      \xP@Max\xP@M#2%
1469
      \xP@Max\xP@M#3%
1470
```

\xP@scalerow

 $\xP@Max\xP@M#4\%$

```
134217727 = 2048 \cdot 65536 - 1
               1472
                      \count@134217727
               1473
                      \loop
               1474
                        \divide\xP@M\tw@
                      \ifdim\xP@M>\z@
               1475
                        \divide\count@\tw@
               1476
               1477
                      \repeat
               1478
                      \advance\count@\@ne
               1479
                      \multiply#1\count@
               1480
                      \multiply#2\count@
               1481
                      \multiply#3\count@
               1482
                      \multiply#4\count@
               1483 }
               •3 Scale a column of the matrix to improve numerical precision. The scaling factor has to
 \xP@scalecol
               be recorded for the solution assignment later.
               1484 \newcommand*\xP@scalecol[4]{%
                      \xP@M\z@
               1485
                      \xP@Max\xP@M#1%
               1486
               1487
                      \xP@Max\xP@M#2\%
                     \xP@Max\xP@M#3\%
               16777215 = 2048 \cdot 8192 - 1
                     #416777215
                      \loop
               1490
               1491
                        \divide\xP@M\tw@
                      \ifdim\xP@M>\z@
               1492
                        \divide#4\tw@
               1493
               1494
                      \repeat
               1495
                      \advance#4\@ne
                      \multiply#1#4%
               1496
                      \multiply#2#4%
               1497
               1498
                      \multiply#3#4%
               1499 }
 \xP@checkabs
               1500 \newcommand*\xP@checkabs[2]{%
                     •1 •3 •6 This is the second, alternative algorithm for Newton's method in the offset al-
\xP@applinsys
               gorithm. Approximate a solution x for the linear system Ax = b for a (3 \times 3)-matrix A.
               The aim is to make the norm ||Ax - b|| small with small values of ||x||. The approach: Set
               x = \lambda A^t b since the normed scalar product \langle Ax, b \rangle / \|x\| is maximal in this case. The norm
               ||Ax - b|| is then minimal for \lambda = ||A^t b||^2 / ||AA^t b||^2.
                   This approximation is performed between one and three times.
               1502 \newcommand*\xP@applinsys{{%
               First iteration: approximate a solution and record the result.
                      \xP@applinsys@
               1503
                      \xP@ta\xP@dta
               1504
               1505
                      \xP@tb\xP@dtb
                      \xP@tc\xP@dtc
               If the result is nonzero...
                      \xP@checkapp
               1508
                     \if@tempswa
```

```
... modify the objective function by the estimated change, approximate again,...
               1509
                      \xP@modobj
              1510
                      \xP@applinsys@
               ... and test for a nonzero result. If it is nonzero, repeat it a third time.
               1511
                      \xP@checkapp
                      \if@tempswa
              1512
                        \xP@modsol
               1513
                        \xP@modobj
               1514
                        \xP@applinsys@
               1515
               1516
                        \xP@modsol
               1517
                      \fi
                    \fi
              1518
              Return the accumulated approximation from one to three iterations.
                    \xdef\@gtempa{%
                      \xP0ta\the\xP0ta\relax
               1520
               1521
                      \xP@tb\the\xP@tb\relax
                      \xP@tc\the\xP@tc\relax
               1522
                    }}\@gtempa
               1523
              1524 }
              •6 Check whether the solution is nonzero.
 \xP@checkapp
               1525 \newcommand*\xP@checkapp{%
               1526
                    \@tempswatrue
                    \ifdim\xP@dta=\z@
               1527
              1528
                    \ifdim\xP@dtb=\z@
                    \ifdim\xP@dtc=\z@
               1529
                      \@tempswafalse
               1530
               1531
                    \fi\fi\fi
              1532 }
              •3 •6 Modify the objective function by the estimated difference, according to the first-order
   \xP@modobj
              approximation.
              1533 \newcommand*\xP@modobj{%
                    \advance\xP@D
              1534
               1535
                      1536
                    \advance\xP@H
                      1537
               1538
                    \advance\xPQL
               1539
                      1540 }
   \xP@modsol
              •3 •6 Modify the solution vector by the approximation.
               1541 \newcommand*\xP@modsol{%
               1542
                    \advance\xP@ta\xP@dta
               1543
                    \advance\xP@tb\xP@dtb
                    \advance\xP@tc\xP@dtc
               1544
              1545 }
\xP@applinsys@
              •1 •3 •6 The heart of the approximation routine.
               1546 \newcommand*\xP@applinsys@{{%
              Determine scaling factors \xP@sa and \xP@sb to improve numerical precision.
               1547
                    \xP@sa\z@
                    \xP@Max\xP@sa\xP@A
              1548
                    \xP@Max\xP@sa\xP@B
               1549
```

```
1550
     \xP@Max\xP@sa\xP@C
      \xP@Max\xP@sa\xP@E
1551
1552
      \xP@Max\xP@sa\xP@F
1553
      \xP@Max\xP@sa\xP@G
      \xP@Max\xP@sa\xP@I
1554
      \xP@Max\xP@sa\xP@J
1555
     \xP@Max\xP@sa\xP@K
1556
     \xP@sa\ifdim\xP@sa<5460pt\thr@@\xP@sa\else\maxdimen\fi
1557
     \xP@sb\z@
1558
     \xP@Max\xP@sb\xP@D
1559
     \xP@Max\xP@sb\xP@H
1560
     \xP@Max\xP@sb\xP@L
1561
Scale the vector b.
1562
     \ifdim\xP@sb>\z@
        \xP@D\dimexpr\xP@D*\maxdimen/\xP@sb\relax
1563
1564
        \xP@H\dimexpr\xP@H*\maxdimen/\xP@sb\relax
1565
        \xP@L\dimexpr\xP@L*\maxdimen/\xP@sb\relax
1566
     \fi
Vector A^t b (scaled)
      \xP@Aba\dimexpr\xP@A*\xP@D/\xP@sa+\xP@E*\xP@H/\xP@sa+\xP@I*\xP@L/\xP@sa\relax
      \xP@Abb\dimexpr\xP@B*\xP@D/\xP@sa+\xP@F*\xP@H/\xP@sa+\xP@J*\xP@L/\xP@sa\relax
     \xP@Abc\dimexpr\xP@C*\xP@D/\xP@sa+\xP@G*\xP@H/\xP@sa+\xP@K*\xP@L/\xP@sa\relax
1569
Vector AA^tb (scaled)
     +\xP@C*\xP@Abc/\xP@sa\relax
1571
      1572
       +\xP@G*\xP@Abc/\xP@sa\relax
1573
      1574
        +\xP@K*\xP@Abc/\xP@sa\relax
Another scaling factor.
1576
     \xP@sc\z@
     \xP@Max\xP@sc\xP@Aba
1577
1578
     \xP@Max\xP@sc\xP@Abb
1579
     \xP@Max\xP@sc\xP@Abc
     \xP@Max\xP@sc\xP@AAba
1580
1581
      \xP@Max\xP@sc\xP@AAbb
     \xP@Max\xP@sc\xP@AAbc
1582
||A^t b||^2 and ||AA^t b||^2
      \left| xP@sc=\z@
1583
1584
       \xP@AAb\z@
1585
        \xP@Ab\dimexpr\xP@Aba*\xP@bigdim/\xP@sc*\xP@Aba/\xP@sc
1586
                    +\xP@Abb*\xP@bigdim/\xP@sc*\xP@Abb/\xP@sc
1587
                    +\xP@Abc*\xP@bigdim/\xP@sc*\xP@Abc/\xP@sc
1588
        \relax
1589
1590
        \xP@AAb\dimexpr\xP@AAba*\xP@bigdim/\xP@sc*\xP@AAba/\xP@sc
1591
                     +\xP@AAbb*\xP@bigdim/\xP@sc*\xP@AAbb/\xP@sc
                     +\xP@AAbc*\xP@bigdim/\xP@sc*\xP@AAbc/\xP@sc
1592
        \relax
1593
1594
The approximation x = \lambda A^t b with \lambda = ||A^t b||^2 / ||AA^t b||^2.
      \xdef\@gtempa{%
1595
        \ifdim\xP@AAb=\z@
1596
```

```
1597
                        \xP@dta\z@
                        \xP@dtb\z@
              1598
              1599
                        \xP@dtc\z@
              1600
                        \xP@dta\the\dimexpr\xP@Aba*\xP@sb/\xP@sa*\p@/\xP@AAb*\xP@Ab/\maxdimen
              1601
              1602
                        1603
              1604
                        \xP@dtc\the\dimexpr\xP@Abc*\xP@sb/\xP@sa*\p@/\xP@AAb*\xP@Ab/\maxdimen
              1605
              1606
              1607
                      \fi
                    }%
              1608
                    }\@gtempa
              1609
              1610 }
              Switch whether the offset curve is enough
\ifxP@offsetok
              1611 \@ifdefinable\ifxP@offsetok\relax
              1612 \@ifdefinable\xP@offsetoktrue\relax
              1613 \@ifdefinable\xP@offsetokfalse\relax
              1614 \newif\ifxP@offsetok
```

\xP@maxdev

Maximal deviation, measured at 19 points on the curve. The actual tolerance is 1/8 of \xP@maxdev. With the current value 0.1pt, the tolerance is 0.0125pt, which is about 1/32 of the line width for the Computer Modern fonts.

1615 \newcommand*\xP@maxdev{.1pt}

\xP@maxobjfun

Tolerance for the objective function. Recommended value is $\frac{1}{2}(\xp@maxdev)^2$. 1616 \newcommand*\xp@maxobjfun{.005pt}

\xP@testoffset

•1 •5 Test procedure for the offset curve. It tests whether the Bézier curve defined by the control points \X@p,...,\Y@c is a good approximation for the offset curve of the partial curve defined by \xP@xa,...,\xP@yd in the parameter interval [\xP@a, \xP@b] \subseteq [0pt, \xP@bigdim].

The parameter interval is uniformly divided by 20, and the deviation is measured at the 19 inner positions. (Since the boundary points are offset exactly by the algorithm, they do not need to be checked.)

For simplicity, the parameter interval for both curves is normalized to [0,1] in the following explanations. Denote the original curve by $c_1:[0,1]\to\mathbb{R}^2$ and the offset curve by c_2 . The quality test is passed if the offset curve fulfills at each of the 19 test points $t_i\in\{\frac{1}{20},\ldots,\frac{19}{20}\}$ one of the following two conditions:

- Let v be the tangent vector $c_1'(t_i)$. For $w := c_1(t_i) c_2(t_i)$, denote by w_{par} the component parallel to v and by w_{orth} the component orthogonal to v. The test is passed if $|w_{par}| + |w_{orth} \mathbf{xPQoff}| \le \frac{1}{8} \mathbf{xPQmaxdev}$. If ||v|| is very small so that the direction cannot be determined precisely, the condition is $||c_1(t_i) c_2(t_i)|| |\mathbf{xPQoff}|| \le \frac{1}{8} \mathbf{xPQmaxdev}$.
- Compute the normal line at t_i to the curve c_1 and intersect it with c_2 . The intersection point is allowed to have a different parameter $\tilde{t}_i \in [t_i 0.5, t_i + 0.5] \cap [0, 1]$. Then let $w := c_1(t_i) c_2(\tilde{t}_i)$ and test whether $|w_{par}| + |w_{orth} \texttt{xpQoff}| \leq \frac{1}{8} \texttt{xpQmaxdev}$. $(|w_{par}| \text{ is very small in this case and is nonzero only because of limited precision, in particular since <math>\tilde{t}_i$ is determined with an error of $\approx 2^{-17}$ (= $\frac{1}{2}$ sp).)

1617 \newcommand*\xP@testoffset{{%

```
Default values for the return statement and the loop continuation.
      \gdef\xP@afteroffsetok{\xP@offsetoktrue}%
1619
      \def\xP@offsetokif{\ifdim\xP@ti<1.85pt}%
1620
      \xP@ti.1pt
1621
      \loop
\xP@tip = t_i, denormalized for c_1
1622
         \xP@tip\dimexpr\xP@a+(\xP@b-\xP@a)*\xP@ti/131072\relax
Point on the original curve c_1 (scaled by -8)
         \L@p\xP@precbezierpoly\xP@xa\xP@xb\xP@xc\xP@xd\xP@tip
1623
         \U@p\xP@precbezierpoly\xP@ya\xP@yb\xP@yc\xP@yd\xP@tip
1624
8c_2(t_i) - 8c_1(t_i)
         \xP@valA\dimexpr\xP@bezierpoly\X@p\L@c\R@c\X@c\xP@ti-\L@p\relax
1625
         \xP@valB\dimexpr\xP@bezierpoly\Y@p\U@c\D@c\Y@c\xP@ti-\U@p\relax
1626
v
         \d@X3\xP@precbeziertan\xP@xa\xP@xb\xP@xc\xP@xd\xP@tip
1627
         \d@Y3\xP@precbeziertan\xP@ya\xP@yb\xP@yc\xP@yd\xP@tip
1628
1629
         \xP@veclen
Decide if v is big enough (heuristically, may be changed in the future)
         \@tempdimc\dimexpr(\xP@b-\xP@a)*\@tempdimb/\xP@bigdim\relax
1630
1631
         \xP@abs\@tempdimc
         \ifdim.01pt<\@tempdimc
1632
8w_{par}, 8w_{orth} - 8 \times POoff,
           \xP@devA\dimexpr\xP@valA*\d@X/\@tempdimb+\xP@valB*\d@Y/\@tempdimb\relax
           \xP@devB\dimexpr\xP@valA*\d@Y/\@tempdimb-\xP@valB*\d@X/\@tempdimb-8\xP@off
1634
             \relax
1635
           \xP@abs\xP@devA
1636
           \xP@abs\xP@devB
1637
1638
           \@tempdima\dimexpr\xP@devA+\xP@devB\relax
1639
If the velocity is zero, just pass the test.
           \ifdim\@tempdimc=\z@
1640
1641
             \@tempdima\z@
           \else
1642
8||c_1(t_i)-c_2(t_i)||
1643
1644
             \d@X\xP@valA
1645
             \d@Y\xP@valB
1646
             \xP@veclen@
1647
             \global\dimen@i\@tempdimb
1648
             }\@tempdima\dimen@i
1649
             \advance\@tempdima\ifdim\xP@off>\z@-\fi8\xP@off
             \xP@abs\@tempdima
1650
1651
           \fi
1652
If the first condition is not fulfilled, test the second one.
1653
         \ifdim\@tempdima>\xP@maxdev
-c_1(t_i)
           \displaystyle \divide\L@p-8\relax
1654
           \label{local_up-8} $$ \divide\U^0p-8\relax $$
1655
```

Affine transformation of the offset curve: translate by $-c_1(t_i)$ and rotate so that the tangent v to $c_1(t_i)$ becomes the x-axis.

```
      1656
      {%

      1657
      \xP@transformcoor\X@p\Y@p

      1658
      \xP@transformcoor\L@c\U@c

      1659
      \xP@transformcoor\R@c\D@c

      1660
      \xP@transformcoor\X@c\Y@c
```

Find the parameter \tilde{t}_i and decide whether the approximation at \tilde{t}_i is good.

```
1661 \mathbb{xP@findzero}
1662 \mathbb{\%}
1663 \mathbb{fi}
1664 \mathbb{xP@offsetokif}
1665 \mathbb{\advance\mathbb{xP@ti.1pt}}
1666 \mathbb{\repeat}
1667 \expandafter\mathbb{xP@afteroffsetok}
1668 \mathbb{\}
```

\xP@afteroffsetok

1669 \newcommand*\xP@afteroffsetok{}

\xP@offsetokif

1670 \newcommand*\xP@offsetokif{}

\xP@transformcoor

```
1671 \newcommand*\xP@transformcoor[2]{%
1672 \advance#1\L@p
1673 \advance#2\U@p
1674 \@tempdima\dimexpr#1*\d@X/\@tempdimb+#2*\d@Y/\@tempdimb\relax
1675 #2\dimexpr#2*\d@X/\@tempdimb-#1*\d@Y/\@tempdimb\relax
1676 #1\@tempdima
1677 }
```

\xP@findzero

•5 Find the parameter \tilde{t}_i by nested intervals/intermediate value theorem.

```
1678 \newcommand*\xP@findzero{%
1679 \xP@setleftvalue{.05}%
1680 \xP@setrightvalue{.05}%
```

Normalize: function value (x-coordinate) should be nonnegative at the upper end.

1681 \ifdim\xP@valB<\z@\xP@reversecoeff\fi

If the function value at the lower end is also positive, try a smaller parameter interval $t_i \pm \delta$ pt for $\delta \in \{.5, .35, .25, .2, .15, .1, .05\}$. Maybe we have different signs for the x-coordinate for the larger boundary parameters.

```
\ifdim\xP@valA>\z@
1683
        \@tempswatrue
        \@for\@tempa:={.1,.15,.2,.25,.35,.5,1.1}\do{%
1684
1685
          \if@tempswa
1686
            \xP@setleftvalue\@tempa
1687
            \ifdim\xP@valA<\z@\@tempswafalse\fi
1688
            \if@tempswa
1689
               \xP@setrightvalue\@tempa
1690
               \ifdim\xP@valB<\z@
1691
                 \@tempswafalse
```

```
1692
             1693
            1694
                         \fi
                       \fi
            1695
            1696
            Last resort: Try the midpoint.
            1697
                     \if@tempswa
                       \L@p\xP@ti
            1698
                       \xP@valA\xP@bezierpoly\X@p\L@c\R@c\X@c\L@p
            1699
            If the midpoint leads to a negative value, we can proceed with a small interval. Otherwise,
            set both boundary points to the midpoint and effectively skip nested intervals.
                       \ifdim\xP@valA<\z@
            1700
            We had this before, so we know that the value is positive.
            1701
                         \xP@setrightvalue{.05}%
            1702
                       \else
                         \U@p\L@p
            1703
                         \xP@valB\xP@valA
            1704
            1705
            1706
                     \fi
            1707
                   \fi
            The actual nested interval algorithm
            1708
            1709
                   \ifnum\numexpr\U@p-\L@p\relax>\@ne
            1710
                     \xP0ti\dimexpr(\L0p+\U0p)/2\relax
                     \xP@devA\xP@bezierpoly\X@p\L@c\R@c\X@c\xP@ti
            1711
                     \left( xP@devA>\z @
            1712
            1713
                       \U@p\xP@ti
                       \xP@valB\xP@devA
            1714
            1715
            1716
                       \L@p\xP@ti
                       \xP@valA\xP@devA
            1717
            1718
                     \fi
                   \repeat
            Take the left or right boundary point (only 1sp apart), depending on which one yields the
            smaller x-coordinate.
                   \xP@ifabsless\xP@valB\xP@valA
            1721
                     \L@p\U@p
            1722
                     \xP@valA\xP@valB
                   \fi
            1723
            Compare the y-coordinate with \xpQoff.
                   \xP@valB\dimexpr\xP@bezierpoly\Y@p\U@c\D@c\Y@c\L@p+8\xP@off\relax
                   \xP@abs\xP@valA
            1725
                   \xP@abs\xP@valB
            1726
            1727
                   \ifdim\dimexpr\xP@valA+\xP@valB\relax>\xP@maxdev\relax
             1728
                     \xP@failed
            1729
                   \fi
            1730 }
            Break the loop for the t_i in xP@testoffset. Set the return value to false.
\xP@failed
            1731 \newcommand*\xP@failed{%
                   \global\let\xP@offsetokif\iffalse
                   \gdef\xP@afteroffsetok{\xP@offsetokfalse}%
            1733
            1734 }
```

\xP@reversecoeff

```
\xP@reversecoeff Reverse the function for the nested interval algorithm.
                       1735 \newcommand*\xP@reversecoeff{%
                       1736
                               \multiply\X@p\m@ne
                       1737
                               \multiply\L@c\m@ne
                       1738
                               \multiply\R@c\m@ne
                               \multiply\X@c\m@ne
                       1739
                       1740
                               \multiply\xP@valA\m@ne
                       1741
                               \multiply\xP@valB\m@ne
                       1742 }
    \xP@setleftvalue
                      •5
                       1743 \newcommand*\xP@setleftvalue[1]{%
                             \L@p\dimexpr\xP@ti-#1\p@\relax
                       1744
                             \left(\frac{L^{p}-.1pt}{L^{p}-.1pt}\right)
                       1745
                             \xP@valA\xP@bezierpoly\X@p\L@c\R@c\X@c\L@p
                       1746
                       1747 }
   \xP@setrightvalue
                       •5
                       1748 \newcommand*\xP@setrightvalue[1]{%
                             \U@p\dimexpr\xP@ti+#1\p@\relax
                             \ifdim\U@p>2.1\p@\U@p2.1\p@\fi
                       1750
                             \xP@valB\xP@bezierpoly\X@p\L@c\R@c\X@c\U@p
                       1751
                       1752 }
                       9.10
                               Multiple dashed curves
 \xP@splinedbldashed
                       1753 \newcommand*\xP@splinedbldashed{%
                             \xP@checkspline\xP@splinemultdashed\xP@doublestroke}
\xP@splinetrbldashed
                       1755 \newcommand*\xP@splinetrbldashed{%
                             \xP@checkspline\xP@splinemultdashed\xP@trblstroke}
\xP@splinemultdashed
                       1757 \newcommand*\xP@splinemultdashed[1]{%
                       Expected dash number. It is an even number if the spline is the continuation of the previous
                       one, otherwise (default case) an odd number.
                             \xP@testcont\xP@dashmacro
                       1758
                       1759
                             \@tempcnta
                             \ifxP@splinecont
                       1760
                               \numexpr2*((\0tempdimb-\xydashl0/3)/(2*\xydashl0))\relax
                       1761
                       1762
                       1763
                               \numexpr2*((\0tempdimb+\xydashl0)/(2*\xydashl0))-1\relax
                       1764
                       1765
                             \ifnum\@tempcnta>\@ne
                       1766
                               \xP@splinemultdashed@#1%
                             \else
                       1767
                       One dash: paint a solid line. Less than one dash: Leave the segment out, just record the
                       end point.
                       1768
                               \ifnum\@tempcnta=\@ne
                                 \xP@splinemultsolid#1
                       1769
                               \else
                       1770
                                 \xP@savec
                       1771
```

```
\fi
                         1772
                         1773
                               \fi
                         1774
                               \global\let\xP@lastpattern\xP@dashmacro
                         1775 }
\xP@splinemultdashed@
                        •1 •7 Make a list of parameter pairs for the start and end point of a dash.
                         1776 \newcommand*\xP@splinemultdashed@[1]{{%
                               \xP@inibigdim
                         1777
                        Dash length
                         1778
                               \@tempdima\dimexpr\@tempdimb/\@tempcnta\relax
                               \xP@temppar\z@
                         1779
                         1780
                               \toks@{}%
                         1781
                               \xP@savec
                               \ifodd\@tempcnta
                         1782
                         1783
                               \else
                         1784
                                 \xP@slide
                               \fi
                         1785
                               \@tempcnta\z@
                         1786
                         1787
                               \loop
                         1788
                                 \advance\@tempcnta\@ne
                         1789
                                 \xP@append\toks@{\ifodd\@tempcnta\noexpand\xP@paintdash\fi
                         1790
                                   {\the\xP@temppar}}%
                                 \xP@oldpar\xP@temppar
                         1791
                         1792
                                 \xP@slide
                         1793
                               \ifdim\xP@temppar<\xP@bigdim
                         1794
                        The last position is kept as a scaling factor so that the last dot can be drawn at exactly the
                        parameter 1. Use the last or the next-to-last position, depending on the parity of segments.
                         1795
                               \xP@lastpar
                                 \ifodd\@tempcnta
                         1796
                                   \xP@temppar
                         1797
                                   \xP@append\toks@{{\the\xP@temppar}}%
                         1798
                         1799
                         1800
                                    \xP@oldpar
                         1801
                                 \fi
                         Convert the list of parameters to a list of PDF tokens.
                               \@temptokena{}%
                         1802
                         1803
                               \xP@setsolidpat
                               \global\let\xP@lastpattern\xP@dashmacro
                         1804
                               \ensuremath{\tt 0for\ensurema:={\#1}\do{\theta}}\%
                         1805
                         1806
                               \xP@stroke{\the\@temptokena}%
                         1807 }}
        \xP@paintdash
                        •1 •7
                         1808 \newcommand*\xP@paintdash[2]{%
                               \xP@paintsolid{\dimexpr#1*\xP@bigdim/\xP@lastpar\relax}%
                         1810
                                 {\dimexpr#2*\xP@bigdim/\xP@lastpar\relax}%
                         1811 }
                                 Multiple dotted curves
                        9.11
    \splinedbldotted@
 \xP@splinedbldotted@
                         1812 \xP@hook{curve}{splinedbldotted@}
                         1813 \newcommand*\xP@splinedbldotted@{%
```

```
\let\xP@normalmult\@ne
                      1814
                      1815
                            \xP@checkspline\xP@splinemultdotted\xP@doublestroke}
\xP@splinetrbldotted
                      1816 \newcommand*\xP@splinetrbldotted{%
                      1817
                            \let\xP@normalmult\tw@
                            \xP@checkspline\xP@splinemultdotted\xP@trblstroke}
                      1818
                      Dotted lines with multiple strokes are drawn in a different way from single-stroked lines.
 \xP@multidottedpat
                      They are composed of many small, straight lines normal to the curve at every dot position.
                      Hence, the dot pattern for multiple curves has dots which are spaced by the normal distance
                      between strokes.
                      1819 \newcommand*\xP@multidottedpat{%
                            \def\xP@pattern{0 J [\xP@coor\xP@preclw{\xydashh@-\xP@preclw}]0 d}%
                            \global\let\xP@lastpattern\xP@dotmacro
                      1821
                      1822 }
      \xP@normalmult.
                      1823 \@ifdefinable\xP@normalmult\relax
                      •1 •7
\xP@splinemultdotted
                      1824 \newcommand\xP@splinemultdotted[1]{{%
                            \xP@inibigdim
                      1825
                      Make a list of dot positions on the spline segment.
                      1826
                            \xP@temppar\z@
                      1827
                            \xP@testcont\xP@dotmacro
                            \ifxP@splinecont
                      1828
                      Expected dot distance (see the formula in \xP@setdottedpat)
                              \@tempdimc\dimexpr\@tempdimb/(\@tempdimb/131072+1)\relax
                      1829
                              \Otempdima\dimexpr\Otempdimc-\xPOpreclw/2\relax
                      1830
                              \xP@slide
                      1831
                      1832
                              \@tempdima\@tempdimc
                            \else
                      1833
                              \@tempdima\dimexpr\xP@preclw/2\relax
                              \xP@slide
                      1835
                      Expected dot distance (see the formula in \xP@setdottedpat)
                      1836
                              \@tempdima\dimexpr\@tempdimb-\xP@preclw\relax
                      1837
                              \ifdim\@tempdima<\z@\@tempdima\z@\fi
                              \@tempdima\dimexpr\@tempdima/(\@tempdima/131072+1)\relax
                      1838
                            \fi
                      1839
                      1840
                            \xP@savec
                            \t 0
                      1841
                      If the end of the segment is reached before the first dot position, leave the segment out.
                      1842
                            \ifdim\xP@temppar<\xP@bigdim
                      1843
                              \loop
                                1844
                                \xP@oldpar\xP@temppar
                      1845
                      1846
                                \xP@slide
                              \ifdim\xP@temppar<\xP@bigdim
                      1847
                      1848
                              \xP@velocity\xP@bigdim\xP@tempvel
```

Test whether the last or the next-to-last dot is closer to \xP@bigdim. Measure from the end of the dot, hence the contribution of \xP@preclw. Also consider the case that the velocity at the end point is very small. In this case, always choose the next-to-last dot as the final one.

```
\ifdim
            1850
                       \ifdim\xP@preclw<\xP@tempvel
            1851
                         \dimexpr2\xP@bigdim-\xP@oldpar-\xP@preclw*\xP@bigdim/\xP@tempvel\relax
            1852
            1853
            1854
                         -\maxdimen
                       \fi<\xP@temppar
            1855
                       \xP@temppar\xP@oldpar
            1856
            1857
                       \xP@append\toks@{\noexpand\xP@paintdot{\the\xP@temppar}}%
            1858
            1859
                     \@tempdima\dimexpr\xP@preclw/2\relax
            1860
                     \xP@slide
            1861
                     \xP@lastpar\xP@temppar
            1862
            Convert the list of parameters to a list of PDF tokens.
            1863
                     \@temptokena{}%
            1864
                     \the\toks@
            Actually draw the points in the list.
            1865
                     \xP@multidottedpat
                     \xP@stroke{\the\@temptokena}%
            1866
            1867
                  \else
            Leave the segment out because it is too short.
                     \global\let\xP@lastpattern\@empty
            1868
            1869
                  \fi
            1870 }}
            •1 •7 Slide along the Bézier segment by \@tempdima. Needs: Xy-pic spline parameter,
 \xP@slide
            current position parameter \xP@temppar, total spline length \@tempdimb.
            1871 \newcommand*\xP@slide{{%
                  \xP@slide@
            Return the new spline parameter after sliding.
                   \global\dimen@i\xP@temppar
                   }\xP@temppar\dimen@i
            1875 }
\xP@slide@
            •1 •7
            1876 \newcommand*\xP@slide@{%
            Compute the velocity at two points, the starting point and an estimate for the end point.
                   \xP@velocity\xP@temppar\xP@tempvel
            The first estimate for the parameter increment is based on the total spline length.
                   \@tempdimc\dimexpr\xP@bigdim*\@tempdima/\@tempdimb\relax
            1879
                   \count@\z@
                  \@tempswatrue
            1880
            Improve the parameter increment iteratively.
            1881
                  \loop
            Velocity at the estimated end point.
                     \xP@velocity{\xP@temppar+\@tempdimc}\xP@tempvel@
            1882
```

Prevent arithmetic overflow.

```
1883
        \ifdim\dimexpr\@tempdima*4/13\relax>\xP@tempvel@
1884
           \@tempswafalse
1885
        \else
```

Difference to the old parameter increment. This is Newton's method, applied to the estimated spline length based on the velocities \xP@tempvel and \xP@tempvel@ at \xP@temppar and $(\xP@temppar + \@tempdimc)$.

```
\xP@parinc\dimexpr\@tempdima*\xP@bigdim/\xP@tempvel@
1886
1887
            -(\xP@tempvel+\xP@tempvel@)/2*\@tempdimc/\xP@tempvel@\relax
1888
          \advance\@tempdimc\xP@parinc
```

If the estimated parameter increment is bigger than .12, increase the parameter by .1 and slide only partially. This increases the precision if the parameter increment is big.

```
\ifdim\@tempdimc>.12\xP@bigdim
1889
             \@tempswafalse
1890
1891
          \else
```

If the estimate is not improved, break the loop.

```
\ifdim\xP@parinc=\z@
1892
1893
               \@tempswafalse
1894
             \else
```

Also break the loop after 10 iterations.

```
\ifnum\count@=9\relax
1895
1896
                   \@tempswafalse
                 \fi
1897
             \fi
1898
1899
           \fi
1900
         \fi
      \if@tempswa
1901
1902
         \advance\count@\@ne
1903
```

Note that \if@tempswa is always false here.

If the parameter increment would be more than .1 and if the parameter is not too big already, increase the parameter by .1 and slide again.

```
\ifdim\xP@temppar<5461pt
1904
1905
      \ifdim\@tempdimc>.1\xP@bigdim
1906
         \@tempswatrue
1907
      \fi
1908
      \fi
      \if@tempswa
1909
1910
        {%
           \dimen5\xP@temppar
1911
          \advance\xP@temppar.1\xP@bigdim
1912
Cap the end parameter to prevent arithmetic overflows.
```

```
\ifdim\xP@temppar>5461pt\xP@temppar5461pt\fi
1913
          \dimen7\xP@temppar
1914
```

Determine the exact distance of the partial slide.

```
\xP@shaveprec{\dimen5}{\dimen7}%
1915
          \xP@bezierlength
1916
          \global\dimen@i\dimexpr\@tempdima-\@tempdimb\relax
1917
          \global\dimen3\xP@temppar
1918
1919
        \@tempdima\dimen@i
1920
        \xP@temppar\dimen3\relax
1921
```

```
1922
                                \expandafter\xP@slide@
                              \else
                        Finish the slide and return the new parameter.
                                \advance\xP@temppar\@tempdimc
                        1925
                              \fi
                        1926 }
          \xP@paintdot
                        •1 •7
                        1927 \newcommand*\xP@paintdot[1] {%
                        Scale the parameter with a correction factor
                              \@tempdima\dimexpr#1*\xP@bigdim/\xP@lastpar\relax
                        Position at parameter value \xP@temppar
                        1929
                              \xP@tangent
                              1930
                        1931
                              \xP@posY\dimexpr\xP@precbezierpoly\Y@p\U@c\D@c\Y@c\@tempdima/8\relax
                        Normal vector to the curve with length \xydashh@
                              \@tempdima\dimexpr(\xydashh@+\xP@preclw/\xP@normalmult)/2\relax
                        1932
                              1933
                              \U@p\dimexpr-\d@X*\@tempdima/\@tempdimb\relax
                        Append two points on both sides of the curve to the list. (The "multidottedpat" pattern is
                        made to draw points with distance \xydashh@.)
                              \xP@append\@temptokena{\xP@coor{\xP@posX+\L@p*\xP@normalmult}%
                        1935
                                  {\xP@posY+\U@p*\xP@normalmult}m %
                        1936
                        1937
                                \xP@coor{\xP@posX-\L@p*(\xP@normalmult+\@ne)}%
                        1938
                                  {\xP@posY-\U@p*(\xP@normalmult+\@ne)}1 }%
                        1939 }
                        9.12
                                Squiggled curves
   \xP@splinesquiggled
                        1940 \newcommand*\xP@splinesquiggled{%
                             \xP@checkspline\xP@splinesquiggled@\z@}
\xP@splinedblsquiggled
                        1942 \newcommand*\xP@splinedblsquiggled{%
                              \xP@checkspline\xP@splinesquiggled@\xP@doublestroke}
\xP@splinetrblsquiggled
                        1944 \newcommand*\xP@splinetrblsquiggled{%
                             \xP@checkspline\xP@splinesquiggled@\xP@trblstroke}
                        •1 •7
  \xP@splinesquiggled@
                        1946 \newcommand*\xP@splinesquiggled@[1]{{\%
                                  \xP@inibigdim
                        Reverse the direction of the little arcs, if the last squiggle from the previous segment makes
                        it necessary.
                                  \xP@testcont\xP@oddsquigglemacro
                        1948
                        1949
                                  \ifxP@splinecont
                        1950
                                    \def\xP@squigsign{-}%
                        1951
```

Slide again.

```
1952
             \let\xP@squigsign\@empty
1953
           \fi
1954
           \xP@savec
Expected squiggle length
           \@tempcnta=\numexpr\@tempdimb/\xybsqll@\relax
1955
1956
           \ifnum\@tempcnta<\tw@\@tempcnta\tw@\fi
1957
           \multiply\@tempcnta\tw@
           \@tempdima\dimexpr\@tempdimb/\@tempcnta\relax
1958
           \xP@squiglen\@tempdima
1959
Make a list of dot positions on the spline segment.
           \xP@temppar\z@
1961
           \toks@{}%
           \@tempcnta\z@
1962
           \loop
1963
             \advance\@tempcnta\@ne
1964
             \xP@append\toks@{\noexpand\xP@paintsquiggle{\the\xP@temppar}}%
1965
             \xP@oldpar\xP@temppar
1966
1967
             \xP@slide
1968
           \ifdim\xP@temppar<\xP@bigdim
1969
           \repeat
The last position is kept as a scaling factor so that the last dot can be drawn at exactly
the parameter 1. Use the last or the next-to-last position, on the parity of the number of
positions.
1970
           \xP@lastpar
1971
             \ifodd\@tempcnta
1972
               \xP@oldpar
1973
               \advance\@tempcnta\m@ne
1974
             \else
               \xP@temppar
1975
               \xP@append\toks@{\noexpand\xP@paintsquiggle{\the\xP@temppar}}%
1976
1977
Convert the list of parameters to a list of PDF tokens.
1978
           \@temptokena{}%
1979
           \xP@setsolidpat
Record the direction of the last squiggle.
           \global\expandafter\let\expandafter\xP@lastpattern
           \ifodd\numexpr\@tempcnta/2\if\xP@squigsign-+1\fi\relax
1981
             \xP@oddsquigglemacro
1982
           \else
1983
             \xP@evensquigglemacro
1984
1985
           \fi
Draw the squiggles.
           \ensuremath{\texttt{Qfor}\ensurema:=\{\#1}\do{\%}
1986
             \let\xP@dosquiggle\xP@dosquiggle@
1987
1988
             \count@\z@
             \the\toks@
1989
1990
1991
           \xP@stroke{\the\@temptokena}%
1992 }}
•1 •7
```

1993 \newcommand*\xP@paintsquiggle[1]{% \xP@squigglevectors{#1}%

\xP@paintsquiggle

```
1995
                           \xP@dosquiggle
                     1996
                           \ifnum\count@=\thr@@\relax\count@\z@\else\advance\count@\@ne\fi
                     1997 }
\xP@squigglevectors
                     •1 •7
                     1998 \newcommand*\xP@squigglevectors[1]{%
                     Scale the parameter with a correction factor
                           \@tempdima\dimexpr#1*\xP@bigdim/\xP@lastpar\relax
                     Position at parameter value \xP@temppar, offset for multiple curves.
                           \xP@tangent
                     2000
                     2001
                           \xP@posX\dimexpr\xP@precbezierpoly\X@p\L@c\R@c\X@c\@tempdima/8%
                              -\d@Y*(\@tempa)/\@tempdimb\relax
                     2002
                           \xP@posY\dimexpr\xP@precbezierpoly\Y@p\U@c\D@c\Y@c\@tempdima/8%
                     2003
                             +\d@X*(\@tempa)/\@tempdimb\relax
                     2004
                     Tangent vector to the curve with correct length
                     2005
                           \L@p\dimexpr\d@X*\xP@squiglen/\@tempdimb\relax
                     2006
                           \U@p\dimexpr\d@Y*\xP@squiglen/\@tempdimb\relax
                     2007
                           \R@p\dimexpr\L@p*543339720/1311738121\relax
                     2008
                           \D@p\dimexpr\U@p*543339720/1311738121\relax
                     2009
                           2010
                           \Y@min\dimexpr\U@p*362911648/967576667\relax
                     2011
                           \label{local_local_local_local_local} $$X\mathbb{Q}_{\mathbb{Q}}\times\mathbb{Q}_{\mathbb{Q}}\times\mathbb{Q}_{\mathbb{Q}}\times\mathbb{Q}_{\mathbb{Q}}.$$
                     2012
                           \Y@max\dimexpr(\L@p-\xP@squigsign\U@p)*173517671/654249180\relax
                     2013 }
     \xP@dosquiggle
                     •7
                     2014 \@ifdefinable\xP@dosquiggle@\relax
    \xP@dosquiggle@
                     •7
                     2015 \newcommand*\xP@dosquiggle@{%
                           \edef\next0{\xP@coor{\xP@posX}{\xP@posY}m
                     2016
                              \xP@coor{\xP@posX+\Y@max}{\xP@posY+\xP@squigsign\X@max}%
                     2017
                     2018
                     2019
                           \let\xP@dosquiggle\xP@dosquiggle@@
                     2020 }
   \xP@dosquiggle@@
                     •7
                     2021 \newcommand*\xP@dosquiggle@@{%
                     2022
                           \xP@append\@temptokena{\next@\expandafter\xP@coor
                     2023
                              \ifcase\count@
                                {\xP@posX-\Y@max}{\xP@posY-\xP@squigsign\X@max}%
                     2024
                     2025
                                \xP@coor\xP@posX\xP@posY
                     2026
                                {\xP@posX-\xP@squigsign\D@p-\X@min}{\xP@posY+\xP@squigsign\R@p-\Y@min}%
                     2027
                     2028
                               2029
                                {\xP@posX-\X@max}{\xP@posY+\xP@squigsign\Y@max}%
                     2030
                     2031
                               \xP@coor\xP@posX\xP@posY
                     2032
                     2033
                                {\xP@posX+\xP@squigsign\D@p-\X@min}{\xP@posY-\xP@squigsign\R@p-\Y@min}%
                     2034
                                \xP@coor{\xP@posX+\xP@squigsign\D@p}{\xP@posY-\xP@squigsign\R@p}%
                     2035
                              \fi c }%
                           \edef\next@{\expandafter\xP@coor
                     2036
                              \ifcase\count@
                     2037
```

```
2038
          {\xP@posX+\Y@max}{\xP@posY+\xP@squigsign\X@max}%
2039
        \or
2040
          {\xP@posX-\xP@squigsign\D@p+\X@min}{\xP@posY+\xP@squigsign\R@p+\Y@min}%
2041
2042
          {\xP@posX+\X@max}{\xP@posY-\xP@squigsign\Y@max}%
2043
          {\xP@posX+\xP@squigsign\D@p+\X@min}{\xP@posY-\xP@squigsign\R@p+\Y@min}%
2044
2045
      }%
2046
2047 }
2048 \newcommand*\xP@splinebrokensquiggled{%
      \xP@checkspline\xP@splinebrokensquiggled@\z@}
2050 \newcommand*\xP@splinebrokendblsquiggled{%
2051
      \xP@checkspline\xP@splinebrokensquiggled@\xP@doublestroke}
2052 \newcommand*\xP@splinebrokentrblsquiggled{%
      \xP@checkspline\xP@splinebrokensquiggled@\xP@trblstroke}
•1 •7
2054 \newcommand*\xP@splinebrokensquiggled@[1]{{%
          \xP@inibigdim
2055
Start with a space if the last squiggle from the previous segment makes it necessary.
2056
          \xP@testcont\xP@brokensquigglemacro
2057
          \ifxP@splinecont
2058
            \let\xP@squigsign\@firstoftwo
2059
          \else
2060
            \let\xP@squigsign\@secondoftwo
2061
          \fi
2062
          \xP@savec
Expected squiggle length
2063
          \Otempcnta\numexpr(\Otempdimb\xPOsquigsign{}{+2*\xybsqllO})%
2064
            /(4*\xybsqll@)\relax
2065
          \ifnum\@tempcnta<\@ne\@tempcnta\@ne\fi
2066
          \@tempdima\dimexpr\@tempdimb/(8*\@tempcnta\xP@squigsign{}{-4})\relax
2067
          \xP@squiglen\@tempdima
Make a list of dot positions on the spline segment.
2068
          \xP@temppar\z@
          \xP@squigsign{\xP@slide\xP@slide\xP@slide\xP@slide}{}%
2069
          \count@\z@
2070
          \toks@{}%
2071
          \loop
2072
            \xP@append\toks@{\noexpand\xP@paintbrokensquiggle{\the\xP@temppar}}%
2073
2074
2075
            \xP@append\toks@{{\the\xP@temppar}}%
2076
            \xP@slide
2077
            \xP@append\toks@{{\the\xP@temppar}}%
2078
            \xP@slide
            \xP@append\toks@{{\the\xP@temppar}}%
2079
            \xP@slide
2080
```

\xP@splinebrokensquiggled

\xP@splinebrokendblsquiggled

 $\xp{0}$ splinebrokentrblsquiggled

\xP@splinebrokensquiggled@

```
\xP@append\toks@{{\the\xP@temppar}}%
2081
2082
            \xP@lastpar\xP@temppar
2083
            \advance\count@\@ne
          \ifnum\count@<\@tempcnta
2084
2085
            \xP@slide
            \xP@slide
2086
            \xP@slide
2087
            \xP@slide
2088
2089
          \repeat
Convert the list of parameters to a list of PDF tokens.
          \@temptokena{}%
2090
2091
          \xP@setsolidpat
2092
          \global\let\xP@lastpattern\xP@brokensquigglemacro
Draw the squiggles.
          \let\xP@squigsign\@empty
2094
          2095
          \xP@stroke{\the\@temptokena}%
2096 }}
•1 •7
2097 \newcommand*\xP@paintbrokensquiggle[5]{%
2098
      \xP@squigglevectors{#1}%
      \xP@append\@temptokena{%
2099
2100
        \xP@coor\xP@posX\xP@posY m %
2101
        \xP@coor{\xP@posX+\Y@max}{\xP@posY+\X@max}%
      }%
2102
      \xP@squigglevectors{#2}%
2103
2104
      \xP@append\@temptokena{%
2105
        \xP@coor{\xP@posX-\D@p-\X@min}{\xP@posY+\R@p-\Y@min}%
2106
        \xP@coor{\xP@posX-\D@p}{\xP@posY+\R@p}c %
2107
        \xP@coor{\xP@posX-\D@p+\X@min}{\xP@posY+\R@p+\Y@min}%
2108
      \xP@squigglevectors{#3}%
2109
      \xP@append\@temptokena{%
2110
2111
        \xP@coor{\xP@posX-\X@max}{\xP@posY+\Y@max}%
        \xP@coor\xP@posX\xP@posY c %
2112
        \xP@coor{\xP@posX+\X@max}{\xP@posY-\Y@max}%
2113
      }%
2114
      \xP@squigglevectors{#4}%
2115
      \xP@append\@temptokena{%
2116
        \xP@coor{\xP@posX+\D@p-\X@min}{\xP@posY-\R@p-\Y@min}%
2117
2118
        \xP@coor{\xP@posX+\D@p}{\xP@posY-\R@p}c %
2119
        \xP@coor{\xP@posX+\D@p+\X@min}{\xP@posY-\R@p+\Y@min}%
2120
      }%
      \xP@squigglevectors{#5}%
2121
      \xP@append\@temptokena{%
2122
        \xP@coor{\xP@posX-\Y@max}{\xP@posY-\X@max}%
2123
2124
        \xP@coor\xP@posX\xP@posY c %
2125
      }%
2126 }
   End of the section for Xy-pic's "curve" option.
2127 \xyendinput
2128 (/curve)
2129 \langle *basic \rangle
```

\xP@paintbrokensquiggle

9.13 Spline continuation

The following code handles the spline continuation (see Section 6). We introduce global macros which store the last end point of a Bézier segment. If the next segment continues at exactly the same coordinates, the dash/dot/squiggle patterns recognize the continuation.

```
\xP@lastX
              \xP@lastY
                          2130 \newcommand*\xP@lastX{}
        \xP@lastpattern
                          2131 \newcommand*\xP@lastY{}
                          2132 \newcommand*\xP@lastpattern{}
         \xP@solidmacro
           \xP@dotmacro
                          2133 \newcommand*\xP@solidmacro{solid}
          \xP@dashmacro
                          2134 \newcommand*\xP@dotmacro{dot}
 \xP@evensquigglemacro
                          2135 \newcommand*\xP@dashmacro{dash}
                          2136 \newcommand*\xP@evensquigglemacro{evensquiggle}
   \xP@oddsquigglemacro
                          2137 \newcommand*\xP@oddsquigglemacro{oddsquiggle}
\xP@brokensquigglemacro
                          2138 \newcommand*\xP@brokensquigglemacro{brokensquiggle}
                          Reset the last position with every new diagram.
             \xyinside@
                          2139 \renewcommand*\xyinside@{%
                                \global\let\xP@lastpattern\@empty
                                \saveXyStyle@ \aftergroup\xycheck@end
                          2141
                          2142
                                \setboxz@h\bgroup
                          2143
                                \plainxy@
                                \label{eq:condition} $$\X@c=\z@\Y@c=\z@\czeroEdge@
                          2144
                          2145
                                \label{local-condition} $$X0p=Z0Y0p=Z0U0p=Z0L0p=Z0R0p=Z0Edgep={zeroEdge}$$
                          2146
                                \X@min=\hsize\X@max=-\hsize\Y@min=\hsize\Y@max=-\hsize
                                \mathsurround=\z0
                          2147
                                \expandafter\POS\everyxy@@
                          2148
                          2149 }
              \xP@savec Save the current end point
                          2150 \newcommand*\xP@savec{%
                                \xdef\xP@lastX{\the\X@c}%
                          2152
                                \xdef\xP@lastY{\the\Y@c}%
                          2153 }
                          Switch: does the next line/spline continue at the end point of the last one?
       \ifxP@splinecont
                          2154 \@ifdefinable\ifxP@splinecont\relax
                          2155 \@ifdefinable\xP@splineconttrue\relax
                          2156 \@ifdefinable\xP@splinecontfalse\relax
                          2157 \newif\ifxP@splinecont
           \xP@testcont
                          Test for \ifxP@splinecont
                          2158 \newcommand*\xP@testcont[1]{%
                                \xP@splinecontfalse
                          2159
                          2160
                                \ifxP@cont
                          2161
                                  \ifx\xP@lastpattern#1%
                          2162
                                     \ifdim\xP@lastX=\X@p
                                       \ifdim\xP@lastY=\Y@p
                          2163
                                         \xP@splineconttrue
                          2164
                          2165
                                       \fi
                                     \fi
                          2166
                          2167
                                  \fi
                          2168
                                \fi
                          2169 }
```

```
\ifxP@cont Switch: shall the spline hack be applied?
                        2170 \@ifdefinable\ifxP@cont\relax
                        2171 \@ifdefinable\xP@conttrue\relax
                        2172 \@ifdefinable\xP@contfalse\relax
                        2173 \newif\ifxP@cont
 \xypdfcontpatternon
\xypdfcontpatternoff
                        2174 \newcommand*\xypdfcontpatternon{\xP@conttrue}
                        2175 \newcommand*\xypdfcontpatternoff{\xP@contfalse}
                        2176 \xP@conttrue
                        2177 (/basic)
                        9.14
                                Color
                        2178 (*color)
                        2179 \xycatcodes
    \xypdf-co@loaded
                        2180 \expandafter\let\csname xypdf-co@loaded\endcsname\@empty
       \xP@colorname
             \verb|\xP@colA| 2181 \verb|\colorname| xP@colorname| relax|
             \xP@colB 2182 \@ifdefinable\xP@colA\relax
             \xP@colC 2183 \@ifdefinable\xP@colB\relax
             \verb|\xP@colD| 2184 \verb|\@ifdefinable\xP@colC\relax| \\
                        2185 \verb|\definable\xP@colD\relax|
         \newxycolor
      \xP@newxycolor
                       2186 \xP@hook{color}{newxycolor}
                        2187 \newcommand*\xP@newxycolor[2]{%
                              \def\xP@colorname{#1}%
                        2188
                        2189
                              \xP@parsecolor#2 0%
                        2190 }
                        Notwithstanding the policy followed by the rest of the package that the xypdf macros are
                        enabled at \begin{document}, we overwrite the \newxycolor macro already here with the
                        new version. This makes it possible to define colors with \newxycolor in the preamble,
                        even if the rest of the driver is activated later.
                        2191 \xP@color@on
      \xP@parsecolor
                        2192 \ensuremath{\verb|Qifdefinable|xP@parsecolor|relax|}
                        2193 \def\xP@parsecolor#1 #2 #3@{%
                        2194
                             \def\xP@colA{#1}%
                        2195
                              \def\xP@colB{#2}%
                        2196
                              \ifx\xP@colB\xP@gray
                                 \xP@newcolor\xP@colorname\xP@colA\xP@gray\newxycolor
                        2197
                        2198
                              \else
                        2199
                                \xP@parsecolor@#3 @%
                        2200
                             \fi
                        2201 }
     \xP@parsecolor@
                        2202 \ensuremath{\verb|Qifdefinable|xP@parsecolor@\ensuremath{\verb|Colorby|}}
```

2203 \def\xP@parsecolor@#1 #2 #3 #40{\%

```
\def\xP@colC{#1}%
                     2204
                     2205
                            \def\xP@colD{#2}%
                     2206
                            \ifx\xP@colD\xP@rgb
                              \xP@newcolor\xP@colorname{\xP@colA,\xP@colB,\xP@colC}\xP@rgb\newxycolor
                     2207
                     2208
                            \else
                              \def\@tempa{#3}%
                     2209
                              \ifx\@tempa\xP@cmyk
                     2210
                                \xP@newcolor\xP@colorname{\xP@colA,\xP@colB,\xP@colC,\xP@colD}{cmyk}%
                     2211
                     2212
                                  \newxycolor
                     2213
                              \else
                                \PackageError{xypdf}{Syntax error in \string\newxycolor}{}%
                     2214
                     2215
                     2216
                            \fi
                     2217 }
          \xP@gray
           \xP@rgb
                     2218 \newcommand*\xP@gray{gray}
          \xP@cmyk
                     2219 \newcommand*\xP@rgb{rgb}
                     2220 \newcommand*\xP@cmyk{cmyk}
     \OBJECT@shape
  \xP@OBJECT@shape
                     2221 \xP@hook{color}{OBJECT@shape}
                     2222 \newcommand*\xP@OBJECT@shape[1]{\DN@{shape [#1]}%
                            \expandafter\let\expandafter\nextii@\csname\codeof\next@\endcsname
                     2223
                     2224
                            \ifx\nextii@\relax\DN@{style [#1]}%
                     2225
                              \expandafter\let\expandafter\nextii@\csname\codeof\next@\endcsname
                     2226
                              \ifx\nextii@\relax\DN@{\xP@checkcolor{#1}}%
                     2227
                              \else\DN@{\nextii@\xyFN@\OBJECT@}%
                     2228
                     2229
                            \else\expandafter\addtotoks@\expandafter{\nextii@}%
                              \DN@{\xyFN@\OBJECT@}%
                     2230
                            \fi \next@}
                     2231
    \xP@checkcolor
                     2232 \newcommand*\xP@checkcolor[1]{%
                            \@ifundefined{\string\color@\detokenize{#1}}%
                     2233
                     2234
                              {\OBJECT@shapei[#1]}%
                     2235
                     2236
                              \xP@append\toks@{\noexpand\xP@color{{\detokenize{#1}}}}%
                     2237
                              \xyFN@\OBJECT@
                     2238
                              }%
                     2239 }
         \xP@color
                     2240 \newcommand*\xP@color[1]{%
                            \def\preStyle@@{\addtostyletoks@{\bgroup\xP@protectedcolor#1}}%
                     2242
                            \def\postStyle@@{\addtostyletoks@{\egroup}}%
                     2243
                            \modXYstyle@
                     2244 }
                     Somehow, \protect\color is not enough, so we use \varepsilon-TEX's way of \protected macro
\xP@protectedcolor
                     definitions.
                     2245 \ensuremath{ \mbox{\tt @ifdefinable}}\ensuremath{ \mbox{\tt P@protectedcolor}}\ensuremath{ \mbox{\tt relax}}
                     2246 \protected\def\xP@protectedcolor{%
                            \@ifundefined{color}\xP@pdfcolor\color
                     2248 }
```

```
\xP@pdfcolor
                                                               2249 \ensuremath{\mbox{\sc olor\relax}}
                                                               2250 \def\xP@pdfcolor[#1]#2{%
                                                               2251
                                                                             \edef\@tempa{#1}%
                                                               2252
                                                                             \ifx\@tempa\xP@gray
                                                                                   \DN@{\xP@graycolor{#2}}%
                                                               2253
                                                               2254
                                                                             \else\ifx\@tempa\xP@rgb
                                                               2255
                                                                                   \DN@{\xP@rgbcolor#2@}%
                                                               2256
                                                                             \else\ifx\@tempa\xP@cmyk
                                                               2257
                                                                                  \DN@{\xP@cmykcolor#2@}%
                                                               2258
                                                                             \fi\fi\fi
                                                               2259
                                                                             \aftergroup\xP@resetcolor
                                                               2260
                                                                             \next@
                                                               2261 }%
                           \xP@graycolor
                                                               2262 \newcommand*\xP@graycolor[1]{\xP@setcolor{#1}gG}%
                             \xP@rgbcolor
                                                               2263 \@ifdefinable\xP@rgbcolor\relax
                                                               2264 \ensuremath{\mbox{\mbox{$\sim$}}} 1, \#2, \#30 \ensuremath{\mbox{\mbox{$\sim$}}} 2864 \ensuremath{\mbox{$\sim$}} 2864 \ensuremath{\mbox{
                           \xP@cmykcolor
                                                               2265 \@ifdefinable\xP@cmykcolor\relax
                                                               2266 \def\xP@cmykcolor#1,#2,#3,#4@{\xP@setcolor{#1 #2 #3 #4}kK}
                             \xP@newcolor
                                                               2267 \newcommand*\xP@newcolor[4] {%
                                                               2268 \ensuremath{\mbox{\csname}}\ \expandafter\let\expandafter\next@\csname shape [#1]\endcsname
                                                               2269
                                                                           \ifx\next@\relax
                                                               2270
                                                                                \@ifundefined{\string\color@#1}\relax
                                                                                     {\xP@warning{xypdf}}{The color '#1' is overridden by %
                                                               2271
                                                               2272
                                                                                           \string#4}}%
                                                               2273
                                                                                \edef\next@{\noexpand\newxystyle{#1}{\noexpand\xP@unnamedcolor{#2}{#3}}}%
                                                               2274 \else
                                                                                \DN@{}%
                                                               2275
                                                               2276 \fi
                                                               2277 \next@\relax}
                   \xP@unnamedcolor
                                                               2278 \newcommand*\xP@unnamedcolor[2]{\xP@color{[#2]{#1}}}
     \xP@definecrayolacolor
                                                               2279 \newcommand\xP@definecrayolacolor[2] {%
                                                                           \xP@newcolor{#1}{#2}{cmyk}\UseCrayolaColors}%
\xP@installCrayolaColors
                                                               2281 \newcommand*\xP@installCrayolaColors{%
                                                                              \xP@definecrayolacolor{GreenYellow}{.15,0,.69,0}%
                                                               2282
                                                               2283
                                                                              \xP@definecrayolacolor{Yellow}{0,0,1,0}%
                                                               2284
                                                                              \xP@definecrayolacolor{Goldenrod}{0,.1,.84,0}%
                                                               2285
                                                                              \xP@definecrayolacolor{Dandelion}{0,.29,.84,0}%
                                                                              \xP@definecrayolacolor{Apricot}{0,.32,.52,0}%
                                                               2286
                                                               2287
                                                                              \xP@definecrayolacolor{Peach}{0,.5,.7,0}%
                                                               2288
                                                                             \xP@definecrayolacolor{Melon}{0,.46,.5,0}%
```

```
2289
      \xP@definecrayolacolor{YellowOrange}{0,.42,1,0}%
2290
      \xP@definecrayolacolor{Orange}{0,.61,.87,0}%
2291
      \xP@definecrayolacolor{BurntOrange}{0,.51,1,0}%
2292
      \xP@definecrayolacolor{Bittersweet}{0,.75,1,.24}%
2293
      \xP@definecrayolacolor{RedOrange}{0,.77,.87,0}%
2294
      \xP@definecrayolacolor{Mahogany}{0,.85,.87,.35}%
      \xP@definecrayolacolor{Maroon}{0,.87,.68,.32}%
2295
2296
      \xP@definecrayolacolor{BrickRed}{0,.89,.94,.28}%
2297
      \xP@definecrayolacolor{Red}{0,1,1,0}%
2298
      \xP@definecrayolacolor{OrangeRed}{0,1,.5,0}%
2299
      \xP@definecrayolacolor{RubineRed}{0,1,.13,0}%
2300
      \xP@definecrayolacolor{WildStrawberry}{0,.96,.39,0}%
2301
      \xPQdefinecrayolacolor{Salmon}{0,.53,.38,0}%
2302
      \xP@definecrayolacolor{CarnationPink}{0,.63,0,0}%
      \xP@definecrayolacolor{Magenta}{0,1,0,0}%
2303
2304
      \xP@definecrayolacolor{VioletRed}{0,.81,0,0}%
2305
      \xP@definecrayolacolor{Rhodamine}{0,.82,0,0}%
2306
      \xP@definecrayolacolor{Mulberry}{.34,.9,0,.02}%
      \xP@definecrayolacolor{RedViolet}{.07,.9,0,.34}%
2307
      \xP@definecrayolacolor{Fuchsia}{.47,.91,0,.08}%
2308
2309
      \xP@definecrayolacolor{Lavender}{0,.48,0,0}%
      \xP@definecrayolacolor{Thistle}{.12,.59,0,0}%
2310
      \xP@definecrayolacolor{Orchid}{.32,.64,0,0}%
2311
2312
      \xP@definecrayolacolor{DarkOrchid}{.4,.8,.2,0}%
2313
      \xP@definecrayolacolor{Purple}{.45,.86,0,0}%
2314
      \xP@definecrayolacolor{Plum}{.5,1,0,0}%
2315
      \xP@definecrayolacolor{Violet}{.79,.88,0,0}%
2316
      \xP@definecrayolacolor{RoyalPurple}{.75,.9,0,0}%
2317
      \xP@definecrayolacolor{BlueViolet}{.86,.91,0,.04}%
2318
      \xP@definecrayolacolor{Periwinkle}{.57,.55,0,0}%
      \xP@definecrayolacolor{CadetBlue}{.62,.57,.23,0}%
2319
2320
      \xP@definecrayolacolor{CornflowerBlue}{.65,.13,0,0}%
      \xP@definecrayolacolor{MidnightBlue}{.98,.13,0,.43}%
2321
2322
      \xP@definecrayolacolor{NavyBlue}{.94,.54,0,0}%
2323
      \xP@definecrayolacolor{RoyalBlue}{1,.5,0,0}%
      \xP@definecrayolacolor{Blue}{1,1,0,0}%
2324
2325
      \xP@definecrayolacolor{Cerulean}{.94,.11,0,0}%
      \xP@definecrayolacolor{Cyan}{1,0,0,0}%
2326
2327
      \xP@definecrayolacolor{ProcessBlue}{.96,0,0,0}%
      \xP@definecrayolacolor{SkyBlue}{.62,0,.12,0}%
2328
2329
      \xP@definecrayolacolor{Turquoise}{.85,0,.2,0}%
2330
      \xP@definecrayolacolor{TealBlue}{.86,0,.34,.02}%
2331
      \xP@definecrayolacolor{Aquamarine}{.82,0,.3,0}%
2332
      \xP@definecrayolacolor{BlueGreen}{.85,0,.33,0}%
2333
      \xP@definecrayolacolor{Emerald}{1,0,.5,0}%
2334
      \xP@definecrayolacolor{JungleGreen}{.99,0,.52,0}%
2335
      \xP@definecrayolacolor{SeaGreen}{.69,0,.5,0}%
2336
      \xP@definecrayolacolor{Green}{1,0,1,0}%
      \xP@definecrayolacolor{ForestGreen}{.91,0,.88,.12}%
2337
2338
      \xP@definecrayolacolor{PineGreen}{.92,0,.59,.25}%
      \xP@definecrayolacolor{LimeGreen}{.5,0,1,0}%
2339
2340
      \xP@definecrayolacolor{YellowGreen}{.44,0,.74,0}%
2341
      \xP@definecrayolacolor{SpringGreen}{.26,0,.76,0}%
2342
      \xP@definecrayolacolor{OliveGreen}{.64,0,.95,.4}%
2343
      \xP@definecrayolacolor{RawSienna}{0,.72,1,.45}%
```

\xP@definecrayolacolor{Sepia}{0,.83,1,.7}%

```
\xP@definecrayolacolor{Brown}{0,.81,1,.6}%
                                                                  2345
                                                                  2346
                                                                                        \xP@definecrayolacolor{Tan}{.14,.42,.56,0}%
                                                                  2347
                                                                                        \xP@definecrayolacolor{Gray}{0,0,0,.5}%
                                                                                        \xP@definecrayolacolor{Black}{0,0,0,1}%
                                                                  2348
                                                                                        2349
                                                                  2350 }
                                                                  2351 \xywithoption{crayon}{%
                                                                                        \xP@installCrayolaColors
                                                                                        \renewcommand*\installCrayolaColors@{}%
                                                                  2353
                                                                  2354 }
                                                                              End of the section for Xy-pic's "color" option.
                                                                  2355 \xyendinput
                                                                  2356 \langle /color \rangle
                                                                  9.15 Frames
                                                                  2357 (*frame)
                                                                  2358 \xyrequire{curve}%
                                                                  2359 \xycatcodes
\xypdf-fr@loaded
                                                                  2360 \expandafter\let\csname xypdf-fr@loaded\endcsname\@empty
           \xP@framedrop
                                                                  2361 \newcommand*\xP@framedrop[1]{%
                                                                                        \expandafter\frmDrop@\expandafter{%
                                                                  2363
                                                                                        \expandafter\def\expandafter\prevEdge@@\expandafter{\prevEdge@@}%
                                                                  2364
                                                                                        \setboxz@h{#1\frmradius@@}%
                                                                  2365
                                                                                        \styledboxz@}%
                                                                  2366 }
                                 frm{-}
                      \xP@frm{-}
                                                                 2367 \xP@hook{frame}{frm{-}}
                                                                  2368 \expandafter\newcommand\expandafter*\csname xP@frm{-}\endcsname{%
                                                                                        \xP@framedrop\xP@solidframe
                                                                  2370 }
       \xP@solidframe
                                                                  2371 \newcommand*\xP@solidframe[1]{%
                                                                  2372 \R@#1\relax
                                                                  2373 \xP@setsolidpat
                                                                  2374 \let\xP@fillorstroke\xP@stroke
                                                                  2376 }
       \xP@ifzerosize
                                                                  2377 \newcommand*\xP@ifzerosize[2]{%
                                                                  2378
                                                                                      \@tempswafalse
                                                                  2379
                                                                                        \label{localize} $$ \left(\frac{20}{160m}R@c=20\right) - \left(\frac{20}{160m}\right) - \left(
                                                                  2380
                                                                                                \@tempswatrue
                                                                  2381
                                                                                        \fi\fi\fi\fi
                                                                                        \if@tempswa#1\else#2\fi
                                                                  2382
                                                                  2383 }
```

```
\xP@frameifnotzero
                                               2384 \newcommand*\xP@frameifnotzero[1]{%
                                               2385
                                                             \setboxz@h{%
                                               2386
                                                                  \hskip\X@c\raise\Y@c\hbox{\xP@ifzerosize{}{#1}}%
                                               2387
                                                             \wd\z@\z@\ht\z@\z@\dp\z@\z@
                                               2388
                                               2389
                                                             \boxz@
                                               2390 }
                       \xP@oval
                                               2391 \newcommand*\xP@oval{%
                                                             \hskip-\L@c
                                               2392
                                                             \lower\D@c\hbox{%
                                               2393
                                                                  \dimen@\dimexpr\L@c+\R@c\relax
                                               2394
                                                                  \dimen@ii\dimexpr\U@c+\D@c\relax
                                               2395
                                               2396
                                                                  \R0\xP0min\R0{.5\dimen0}%
                                               2397
                                                                  \R0\xP0min\R0{.5\dimen0ii}%
                                               Circumference. 696621973/405764219 \approx 8 - 2\pi
                                                                  \ensuremath{\tt 0tempdimb\dimexpr2\dimen0+2\dimen0ii-\R0*696621973/405764219\relax}
                                                                  \left| R0=\right| z0
                                               2399
                                               Sharp corners: draw a rectangle.
                                                                           \xP@fillorstroke{0 0 \xP@coor\dimen@\dimen@ii re}%
                                               2401
                                                                       \else
                                               Rounded corners.
                                               2402
                                                                      \def\@tempa{*119763188/267309217}%
                                               2403
                                                                      \xP@fillorstroke{%
                                               2404
                                                                              2405
                                                                              0 \xP@dim\R@ c \%
                                                                              \ifdim2\R@=\dimen@ii\else
                                               2406
                                               2407
                                                                                  0 \xP@dim{\dimen@ii-\R@}1 %
                                               2408
                                               2409
                                                                              0 \xP@dim{\dimen@ii-\R@\@tempa}\xP@coor{\R@\@tempa}\dimen@ii
                                               2410
                                                                              \xP@coor\R@\dimen@ii c %
                                                                              \ifdim2\R@=\dimen@\else
                                               2411
                                                                                  \xP@coor{\dimen@-\R@}\dimen@ii 1 %
                                               2412
                                               2413
                                                                              \fi
                                               2414
                                                                              \xP@coor{\dimen@-\R@\@tempa}\dimen@ii
                                               2415
                                                                              \xP@coor\dimen@{\dimen@ii-\R@\@tempa}\xP@coor\dimen@{\dimen@ii-\R@} c %
                                               2416
                                                                              \ifdim2\RQ=\dimenQii\else
                                               2417
                                                                                  \xP@coor\dimen@\R@ 1 %
                                               2418
                                               2419
                                                                              \xP@coor\dimen@{\R@\@tempa}\xP@dim{\dimen@-\R@\@tempa}0 \%
                                               2420
                                                                              \xP@dim{\dimen@-\R@}0 c h%
                                               2421
                                                                              }%
                                                                  \fi
                                               2422
                                               2423
                                                             }%
                                               2424 }
                   \frm[o]{-}
            \xP@frm[o]{-}
                                              2425 \xP@hook{frame}{frm[o]{-}}
                                               2426 \expandafter\newcommand\expandafter*\csname xP@frm[o]{-}\endcsname{% of the command of th
                                               2427 \xP@framedrop{\xP@ellipseframe\xP@setsolidpat}%
```

2428 }

```
\xP@ellipseframe
                                                 2429 \newcommand*\xP@ellipseframe[2]{%
                                                2430
                                                              \xP@getradii{#2}%
                                                2431
                                                              \xP@ifzerosize{}{%
                                                2432
                                                                   \def\xP@fillorstroke{#1\xP@stroke}%
                                                                   \setboxz@h{\hskip\X@c\raise\Y@c\hbox{\xP@framedellipse}}%
                                                2433
                                                2434
                                                                   \wd\z0\z0\ht\z0\z0\dp\z0\z0
                                                 2435
                                                                   \boxz@
                                                 2436
                                                             }%
                                                2437 }
                            \frm{.}
                     \xP@frm{.}
                                                2438 \xP@hook{frame}{frm{.}}
                                                2439 \expandafter\newcommand\expandafter*\csname xP0frm{.}\endcsname{\% of the command of the c
                                                2441 }
\xP@rectframedotted
                                                2442 \newcommand*\xP@rectframedotted[1]{%
                                                2443
                                                              \R0#1\relax
                                                              \xP@frameifnotzero{%
                                                2444
                                                                   \left| \frac{R0=\z0}{} \right|
                                                2445
                                                                        \xP@dottedrect
                                                2446
                                                2447
                                                                   \else
                                                                        \xP@dottedoval
                                                 2449
                                                                   \fi
                                                2450
                                                             }%
                                                2451 }
                                                Make sure that there is a dot in every corner of the rectangle.
           \xP@dottedrect
                                                2452 \newcommand*\xP@dottedrect{%
                                                2453
                                                              \hskip-\L@c
                                                2454
                                                              \lower\D@c\hbox{%
                                                 2455
                                                                   \dimen@ii\dimexpr\U@c+\D@c\relax
                                                2456
                                                                   \@tempdimc\dimexpr\xP@preclw/-2\relax
                                                                   \@tempdimb\dimexpr\L@c+\R@c+\xP@preclw\relax
                                                2457
                                                                   \xP@contfalse
                                                2458
                                                                   \xP@setdottedpat
                                                2459
                                                Draw the horizontal lines \frac{1}{2} whitespace longer to eliminate inaccuracies.
                                                                   \dimen@\dimexpr\@tempdimb+\@tempdima/2+\@tempdimc\relax
                                                2460
                                                                   \xP@stroke{\xP@dim\@tempdimc0 m \xP@dim\dimen@0 1 %
                                                2461
                                                2462
                                                                        \xP@coor\@tempdimc\dimen@ii m \xP@coor\dimen@ii 1}%
                                                Ensure pattern continuation.
                                                                   \let\xP@testcont\xP@alwaysconttrue
                                                2463
                                                2464
                                                                   \@tempdimb\dimen@ii
                                                2465
                                                                   \xP@setdottedpat
                                                2466
                                                                   \dimen@\dimexpr\L@c+\R@c\relax
                                                                   \advance\dimen@ii\dimexpr\@tempdimc-\@tempdima/2\relax
                                                2467
                                                                   \multiply\@tempdimc\m@ne
                                                2468
                                                Draw the vertical lines \frac{1}{2} whitespace longer.
                                                                   \xP@stroke{0 \xP@dim\@tempdimc m 0 \xP@dim\dimen@ii 1 %
                                                2469
                                                                        \xP@coor\dimen@\@tempdimc m \xP@coor\dimen@\dimen@ii 1}%
                                                2470
                                                2471
                                                              }%
                                                2472 }
```

```
\xP@dottedoval
                      2473 \newcommand*\xP@dottedoval{%
                      2474 \def\xP@fillorstroke{\xP@setcldottedpat\xP@stroke}%
                      2475 \xP@oval
                      2476 }
         \frm[o]{.}
      \xP@frm[o]{.}
                      2477 \xP@hook{frame}{frm[o]{.}}
                      2478 \expandafter\newcommand\expandafter*\csname xP@frm[o]{.}\
                      2479 \xP@framedrop{\xP@ellipseframe\xP@setcldottedpat}%
                      2480 }
           \frm{--}
        \xP@frm{--}
                      2481 \xP@hook\{frame\}\{frm\{--\}\}
                      2482 \expandafter\newcommand\expandafter*\csname xP@frm\{--\}\endcsname\{\%, \}
                            \xP@framedrop\xP@rectframedashed
                      2484 }
\xP@rectframedashed
                      2485 \newcommand*\xP@rectframedashed[1]{\%
                      2486
                            \R0#1\relax
                      2487
                            \xP@frameifnotzero{%
                      2488
                              \left| \frac{R0}{z0} \right|
                                \xP@dashedrect
                      2489
                      2490
                              \else
                      2491
                                \xP@dashedoval
                      2492
                              \fi
                      2493 }%
                      2494 }
     \xP@dashedrect
                      2495 \newcommand*\xP@dashedrect{%
                            \hskip-\L@c
                      2496
                      2497
                            \lower\D@c\hbox{%
                      2498
                              \dimen@\dimexpr\L@c+\R@c\relax
                              \dimen@ii\dimexpr\U@c+\D@c\relax
                      2499
                      2500
                              \@tempdimb\dimen@
                      2501
                              \xP@contfalse
                      2502
                              \xprec{xP@setdashpat}
                      2503
                              \xP@stroke{0 0 m \xP@dim\dimen@0 1 %}
                      2504
                                0 \xP@dim\dimen@ii m \xP@coor\dimen@\dimen@ii 1}%
                              \@tempdimb\dimen@ii
                      2505
                              \xP@setdashpat
                      2506
                              \xP@stroke{0 0 m 0 \xP@dim\dimen@ii 1 %
                      2507
                                 \xP@dim\dimen@O m \xP@coor\dimen@\dimen@ii 1}%
                      2508
                           }%
                      2509
                      2510 }
     \xP@dashedoval
                      2511 \newcommand*\xP@dashedoval{%
                            \def\xP@fillorstroke{\xP@setcldashpat\xP@stroke}%
                      2513
                            \xP@oval
                      2514 }
        \frm[o]{--}
     \xP@frm[o]{--}
```

```
2515 \xP@hook{frame}{frm[o]{--}}
                      2516 \expandafter\newcommand\expandafter*\csname xP@frm[o]{--}\endcsname{%
                            \xP@framedrop{\xP@ellipseframe\xP@setcldashpat}%
                      2518 }
             \frm{,}
          \xP@frm{,}
                      2519 \xP@hook{frame}{frm{,}}
                      2520 \expandafter\newcommand\expandafter*\csname xP0frm{,}\end{sname}{\%}
                            \xP@framedrop\xP@frameshadow
                      2521
                      2522 }
     \xP@frameshadow
                      2523 \newcommand*\xP@frameshadow[1]{%
                      2524
                            \R0#1\relax
                            \left(\frac{R0=\z0\R01.2pt\relax\fi}{R0}\right)
                      2525
                      2526
                            \xP@frameifnotzero\xP@shadow
                      2527 }
          \xP@shadow
                      2528 \newcommand*\xP@shadow{%
                            \hskip\dimexpr\R@c+\R@/2\relax
                      2530
                            \lower\dimexpr\D@c+\R@/2\relax\hbox{%
                      2531
                              \def\xP@pattern{0 J 0 j []0 d}%
                              \edef\xP@lw{\xP@dim\R@}%
                      2532
                              \xP@stroke{\xP@dim{\R@/2-\L@c-\R@c} 0 m 0 0 1 0 \xP@dim{\D@c+\U@c-\R@/2}1}\%
                      2533
                           }%
                      2534
                      2535 }
            frm{o-}
         \xP@frm{o-}
                      2536 \xP@hook{frame}{frm{o-}}
                      2537 \expandafter\newcommand\expandafter*\csname xP@frm{o-}\endcsname{%
                            \xP@framedrop\xP@roundedrectframe
                      2538
                      2539 }
\xP@roundedrectframe
                      2540 \newcommand*\xP@roundedrectframe[1]{%
                            \R0#1\relax
                            \in R0=\z0\R0\xydashl0\relax\fi
                      2542
                      2543
                            \xP@frameifnotzero\xP@roundedrectangle
                      2544 }
\xP@roundedrectangle
                      2545 \newcommand*\xP@roundedrectangle{%
                      2546
                            \dimen@\dimexpr\L@c+\R@c\relax
                      2547
                            \dimen@ii\dimexpr\U@c+\D@c\relax
                           \R0\xP0min\R0{.5\dimen0}%
                      2548
                           \R@\xP@min\R@{.5\dimen@ii}%
                      2549
                      2550
                            \hskip-\L@c
                           \lower\D@c\hbox{%
                      2551
                      Rounded corners
                              \ensuremath{\tt 0tempdimb\dimexpr2\dimen0+2\dimen0ii-\R0*696621973/405764219\relax}
                      2552
                              \def\@tempa{*119763188/267309217}%
                      2553
                              \xP@setsolidpat
                      2554
                      2555
                              \xP@stroke{%
                      2556
```

```
2558
                         \ifdim2\R@=\dimen@ii\else
             2559
                           0 \xP@dim{\dimen@ii-\R@}m %
             2560
                         0 \xP@dim{\dimen@ii-\R@\@tempa}\xP@coor{\R@\@tempa}\dimen@ii
             2561
                         \xP@coor\R@\dimen@ii c %
             2562
                         \ifdim2\R@=\dimen@\else
             2563
                           \xP@coor{\dimen@-\R@}\dimen@ii m %
             2564
             2565
                         \xP@coor{\dimen@-\R@\@tempa}\dimen@ii
             2566
                         \xP@coor\dimen@{\dimen@ii-\R@\@tempa}\xP@coor\dimen@{\dimen@ii-\R@} c %
             2567
                         \ifdim2\R@=\dimen@ii\else
             2568
                           \xP@coor\dimen@\R@ m %
             2569
                         \fi
             2570
             2571
                         2572
                         \xP@dim{\dimen@-\R@}0 c%
                        }%
             2573
             Upper and lower horizontal dashes.
             2574
                      \xP@contfalse
                      \ensuremath{\tt 0}tempdimb\ensuremath{\tt dimexpr\L0c+\R0c-2\R0\relax}
             2575
             2576
                      \ifdim\@tempdimb<\z@\@tempdimb\z@\fi
             2577
                      \xP@setdashpat
                      \ifdim\@tempdima>\z@
             2578
                        \dimen@\dimexpr\@tempdimb+\R@-\@tempdima/2\relax
             2579
                        \dimen@ii\dimexpr\U@c+\D@c\relax
             2580
                       \xP@stroke{%
             2581
                          \xP@dim{\R@+\@tempdima}0 m \xP@dim\dimen@ 0 1 %
             2582
             2583
                          \xP@coor{\R@+\@tempdima}\dimen@ii m \xP@coor\dimen@\dimen@ii 1%
                       }%
             2585
             Left and right vertical dashes.
                      \ensuremath{\tt 0}\ dimexpr\U@c+\D@c-2\R@\relax
             2586
                      \ifdim\@tempdimb<\z@\@tempdimb\z@\fi
             2587
             2588
                      \xP@setdashpat
                      \ifdim\@tempdima>\z@
             2589
             2590
                        \dimen@\dimexpr\L@c+\R@c\relax
             2591
                        \dimen@ii\dimexpr\@tempdimb+\R@-\@tempdima/2\relax
             2592
                       \xP@stroke{%
             2593
                          0 \xP@dim{\R@+\@tempdima}m 0 \xP@dim\dimen@ii 1 %
             2594
                          \xP@coor\dimen@{\R@+\@tempdima}m \xP@coor\dimen@\dimen@ii 1%
             2595
                       }%
             2596
             2597
                   }%
             2598 }
    frm{=}
 \xP@frm{=}
             2599 \xP@hook{frame}{frm{=}}
             2600 \expandafter\newcommand\expandafter*\csname xP@frm{=}\endcsname{%
             2601
                   \xP@framedrop\xP@dsframe
             2602 }
\xP@dsframe
             2603 \newcommand*\xP@dsframe[1]{%
             2604
                   \R@#1\relax
             2605
                   \xP@frameifnotzero\xP@dsoval
             2606 }
```

 $0 \propto P@dim\R@c %$

2557

```
\xP@dsoval
                                       2607 \newcommand*\xP@dsoval{%
                                                     \dim(\L@c+\R@c)/2\relax
                                       2609
                                                     \ifdim\dimen@<\xydashh@\dimen@\xydashh@\fi
                                       2610
                                                     \dimen@ii\dimexpr(\U@c+\D@c)/2\relax
                                                     \label{limin} $$  \ifdim\dimen@ii<\xydashh@\dimen@ii\xydashh@\fi $$
                                       2611
                                                     \R@\xP@min\R@\dimen@
                                       2612
                                       2613
                                                     \R@\xP@min\R@\dimen@ii
                                                     \xP@setsolidpat
                                       2615
                                                     \let\xP@fillorstroke\xP@stroke
                                       2616
                                                     \xP@oval
                                       2617
                                                    \hskip\L@c
                                       2618
                                                    \advance\L@c-\xydashh@
                                       2619
                                                    \advance\R@c-\xydashh@
                                       2620
                                                   \advance\U@c-\xydashh@
                                                    \advance\D@c-\xydashh@
                                                     \advance\R@-\xydashh@
                                       2622
                                                     \left(\frac{R0}{z0}\right)
                                       2623
                                                     \xP@oval
                                       2624
                                       2625 }
         \frm[o]{=}
  \xP@frm[o]{=}
                                       2626 \xP@hook\{frame\}\{frm[o]{=}\}
                                       2627 \expandafter\newcommand\expandafter*\csname xP@frm[o]{=}\endcsname{% of the content of th
                                                     \xP@framedrop\xP@dsellframe
                                       2629 }
              \frm{ee}
       \xP@frm{ee}
                                       2630 \xP@hook\{frame\}\{frm\{ee\}\}
                                       2631 \expandafter\newcommand\expandafter*\csname xP@frm{ee}\endcsname{%
                                       2632 \xP@framedrop\xP@dsellframe
                                       2633 }
\xP@dsellframe
                                       2634 \newcommand*\xP@dsellframe[1]{%
                                                      \xP@getradii{#1}%
                                       2636
                                                      \xP@frameifnotzero\xP@dsellipse
                                       2637 }
    \xprec{xP@temppath}
                                       2638 \@ifdefinable\xP@temppath\relax
  \xP@dsellipse
                                       2639 \newcommand*\xP@dsellipse{%
                                       2640
                                                     \hskip\dimexpr(\R@c-\L@c)/2\relax
                                       2641
                                                      \lower\dimexpr(\D@c-\U@c)/2\relax
                                       2642
                                                     \hbox{%
                                       2643 % Inner ellipse: true ellipse
                                       2644
                                                           \advance\A@-\xydashh@
                                                           \advance\B@-\xydashh@
                                       2645
                                                          \left(\frac{A0}{z0}\right)
                                       2646
                                       2647
                                                           \left| \frac{B0}{z0}\right|
                                                           \def\xP@fillorstroke{\edef\xP@temppath}%
                                       2648
                                       2649
                                                           \xP@ellipse@
                                       2650 \% Outer curve: offset ellipse
                                       2651
                                                           \xP@inibigdim
```

```
\let\@tempa\xydashh@
                                                                     2652
                                                                     2653
                                                                                                 \xP@offsetellipse
                                                                      2654
                                                                                                 \xP@setsolidpat
                                                                                                 \xP@stroke{\xP@temppath\space\the\@temptokena}%
                                                                      2655
                                                                      2656
                                                                                         }%
                                                                     2657 }
      \xP@offsetellipse
                                                                     TeX grouping: Not necessary, it's in an hbox anyway.
                                                                     2658 \newcommand*\xP@offsetellipse{%
                                                                     2659
                                                                                          \xP@movetotrue
                                                                     2660
                                                                                          \@temptokena{}%
                                                                      2661
                                                                                          \xP@offsetelliptseg\A@\z@\A@{\B@*173517671/654249180}\%
                                                                                                 {\A@*554561898/619869377}{\B@*34221476/65864945}%
                                                                      2662
                                                                     2663
                                                                                                 {\A@*543339720/768398401}{\B@*543339720/768398401}%
                                                                                          \xp@offsetelliptseg{\A@*543339720/768398401}{\B@*543339720/768398401}%
                                                                     2664
                                                                                                 {\Lambda0*34221476/65864945}{B0*554561898/619869377}%
                                                                     2665
                                                                                                 {\A@*173517671/654249180}\B@\z@\B@
                                                                      2666
                                                                     2667
                                                                                         \xP@mirrorpath
                                                                     2668 }
                 \xP@mirrorpath
                                                                      2669 \newcommand*\xP@mirrorpath{%
                                                                      2670
                                                                                          \edef\0tempa{\the\0temptokena\relax\space\space\space\space}%
                                                                     2671
                                                                                          \let\@tempb\@empty
                                                                     2672
                                                                                          \let\@tempc\@empty
                                                                                          \verb|\expandafter| x P@mirror path@ \empa|
                                                                     2673
                                                                     2674 }
             \xP@mirrorpath@
                                                                      2675 \@ifdefinable\xP@mirrorpath@\relax
                                                                      2676 \def\xP@mirrorpath@#1 #2 #3 #4 #5 #6 #7 {%
                                                                      2677
                                                                                         \ifx\relax#4%
                                                                     2678
                                                                                                \xP@append\\@temptokena{\\dtempb\\xP@minus#1 \xP@minus#2 #3 \\@tempc h}%
                                                                     2679
                                                                                         \else
                                                                                                 \edef\@tempb{\xP@minus#6 #7 \xP@minus#4 #5 \xP@minus#1 #2 c \@tempb%
                                                                     2680
                                                                      2681
                                                                                                       \if#3m\else\xP@minus#1 \xP@minus#2 #3 \fi%
                                                                      2682
                                                                                                        \xP@minus#4 \xP@minus#5 \xP@minus#6 \xP@minus#7 }%
                                                                                                 \edef\@tempc{#6 \xP@minus#7 #4 \xP@minus#5 #1 \xP@minus#2 c \@tempc}%
                                                                      2683
                                                                      2684
                                                                                                 \expandafter\xP@mirrorpath@
                                                                                         \fi
                                                                      2685
                                                                     2686 }
                                 \xP@minus
                                                                      2687 \ensuremath{\mbox{\sc 0}} \Gifdefinable\xP@minus\relax
                                                                     2688 \end{argman} $$ \end{ar
          \xP@insertbefore
                                                                     2689 \end{4} \end{4}
\xP@offsetelliptseg
                                                                     2690 \newcommand*\xP@offsetelliptseg[8]{%
                                                                                         \X@p\dimexpr#1\relax
                                                                                         \Y@p\dimexpr#2\relax
                                                                      2692
                                                                      2693
                                                                                         \L@c\dimexpr#3\relax
                                                                                       \U@c\dimexpr#4\relax
                                                                     2694
                                                                                      \R@c\dimexpr#5\relax
                                                                     2695
```

```
\D@c\dimexpr#6\relax
                 2696
                 2697
                        \X@c\dimexpr#7\relax
                 2698
                        \Y@c\dimexpr#8\relax
                        \xP@savepts
                 2699
                 2700
                        \xP@a\z@
                        \xP@c\xP@bigdim
                 2701
                 2702
                        \xP@paintsolid@
                 2703 }
   \xP@getradii
                 2704 \newcommand*\xP@getradii[1]{%
                 2705 \edef\@tempa{#1}%
                        \expandafter\xP@getradii@\@tempa,\maxdimen,@%
                 2707 }
  \xP@getradii@
                 2708 \@ifdefinable\xP@getradii@\relax
                 2709 \def\xP@getradii@#1,#2,#3@{%
                 2710
                       \Lambda0#1\relax
                 2711
                        B@#2\relax
                 2712
                        \ifdim\B@=\maxdimen
                 2713
                          \A@\dim\exp(\L@c+\R@c)/2\relax
                          \B@\dim\exp(\U@c+\D@c)/2\relax
                 2714
                 2715 \fi
                 2716 }
        \frm{o}
     \xP@frm{o}
                 2717 \xP@hook{frame}{frm{o}}
                 2718 \expandafter\newcommand\expandafter*\csname xP0frm{o}\end{sname}{\%}
                 2719
                        \xP@framedrop{\xP@circleframe\xP@setsolidpat}%
                 2720 }
       frm{-o}
    \xP@frm{-o}
                 2721 \xP@hook{frame}{frm{-o}}
                 2722 \expandafter\newcommand\expandafter*\csname xP@frm{-o}\endcsname{%}
                 2723
                        \xP@framedrop{\xP@circleframe\xP@setcldashpat}%
                 2724 }
       \frm{.o}
    \xP@frm{.o}
                 2725 \xP@hook{frame}{frm{.o}}
                 2726 \expandafter\newcommand\expandafter*\csname xP@frm{.o}\endcsname{%
                       \xP@framedrop{\xP@circleframe\xP@setcldottedpat}%
                 2728 }
\xP@circleframe
                 2729 \newcommand*\xP@circleframe[2]{%
                       \R0#2\relax
                 2731
                        \def\xP@fillorstroke{#1\xP@stroke}%
                       \xP@ifzerosize{%
                 2732
                          \left| \frac{R@}{z@} \right|
                 2733
                            \xP@circleframe@
                 2734
                 2735
                          \fi
                       }{%
                 2736
                          \left| \frac{R0}{z} \right|
                 2737
                 2738
                            \A@\dim\exp(\L@c+\R@c)/2\relax
                            \B@\dim\exp(\U@c+\D@c)/2\relax
                 2739
```

```
\R0\xP0max\A0\B0
                      2740
                      2741
                               \fi
                      2742
                               \xP@circleframe@
                            }%
                       2743
                      2744 }
    \xP@circleframe@
                      2745 \newcommand*\xP@circleframe@{%
                             \setboxz@h{\hskip\X@c\raise\Y@c\hbox{\xP@circle}}%
                             \wd\z@\z@\ht\z@\z@\dp\z@\z@
                      2748
                             \boxz@
                      2749 }
             \frm{e}
          \xP@frm{e}
                      2750 \xP@hook{frame}{frm{e}}
                      2751 \expandafter\newcommand\expandafter*\csname xP0frm{e}\
                             \xP@framedrop{\xP@ellipseframe\xP@setsolidpat}%
                      2753 }
            \frm{-e}
         \xP@frm{-e}
                      2754 \xP@hook{frame}{frm{-e}}
                      2755 \expandafter\newcommand\expandafter*\csname xP@frm{-e}\endcsname{%
                       {\tt 2756} \qquad {\tt xP@framedrop{\tt xP@ellipseframe\tt xP@setcldashpat}\%}
                      2757 }
            \frm{.e}
         \xP@frm{.e}
                      2758 \xP@hook{frame}{frm{.e}}
                      2759 \expandafter\newcommand\expandafter*\csname xP@frm{.e}\endcsname{%
                      2760 \xP@framedrop{\xP@ellipseframe\xP@setcldottedpat}%
                      2761 }
           frm2{.e}
        \xP@frm2{.e}
                      2762 \xP@hook{frame}{frm2{.e}}
                       2763 \expandafter\newcommand\expandafter*\csname xP@frm2{.e}\endcsname{%
                      2764
                            \xP@framedrop\xP@dsdottedellframe
                      2765 }
\xP@dsdottedellframe
                      2766 \newcommand*\xP@dsdottedellframe[1]{%
                            \xP@getradii{#1}%
                       2768
                             \xP@frameifnotzero\xP@dsdottedellipse
                      2769 }
 \xP@dsdottedellipse
                      2770 \newcommand*\xP@dsdottedellipse{%
                             \hskip\dimexpr(\R@c-\L@c)/2\relax
                      2771
                      2772
                             \lower\dimexpr(\D@c-\U@c)/2\relax
                      2773
                             \hbox{%}
                      Intermediate ellipse: true ellipse
                               \@tempdima.5\xydashh@\relax
                      2774
                      2775
                               \advance\A@-\@tempdima
                               \advance\B@-\@tempdima
                      2776
                               \ifdim\A@<\@tempdima\A@\@tempdima\fi
                      2777
                      2778
                               \ifdim\B@<\@tempdima\B@\@tempdima\fi
                               \let\xP@normalmult\@ne
                      2779
```

```
\xP@specialellipse{\xP@splinemultdotted\xP@doublestroke}%
                    2781
                           }%
                    2782 }
\xP@specialellipse
                    2783 \newcommand*\xP@specialellipse[1]{%
                    2784
                           \def\@tempa{*147546029/267309217}%
                    2785
                           \X@p\A@
                    2786
                           \Y@p\z@
                    2787
                           \L@c\A@
                    2788
                           \U@c\dimexpr\B@\@tempa\relax
                           \R@c\dimexpr\A@\@tempa\relax
                           \D@c\B@
                    2790
                    2791
                           \X@c\z@
                          \Y@c\B@
                    2792
                    2793
                          \xP@bezierlength
                          \let\xP@testcont\xP@alwaysconttrue
                    2794
                    2795
                    2796
                          \X@p\z@
                    2797
                          \Y@p\B@
                    2798
                           \L@c-\R@c
                    2799
                           \D@c\U@c
                    2800
                           \U@c\B@
                    2801
                           \R@c-\A@
                    2802
                           X@c-A@
                    2803
                           \Y@c\z@
                    2804
                           #1%
                           \X@p-\A@
                    2805
                           \Y@p\z@
                    2806
                           \R@c\L@c
                    2807
                    2808
                          L@c-A@
                    2809
                           \U@c-\D@c
                    2810
                          \D@c-\B@
                    2811
                           \X@c\z@
                          \Y@c-\B@
                    2812
                    2813
                           #1%
                           \X@p\z@
                    2814
                    2815
                           \Y@p-\B@
                    2816
                           \L@c-\R@c
                           \D@c\U@c
                    2817
                          \U@c-\B@
                    2818
                          \R@c\A@
                    2819
                          \X@c\A@
                    2820
                          \Y@c\z@
                    2821
                    2822
                           #1%
                    2823 }
\xP@alwaysconttrue
                    2824 \newcommand*\xP@alwaysconttrue[1]{\xP@splineconttrue}
         frm2{-e}
      \xP@frm2{-e}
                    2825 \xP@hook{frame}{frm2{-e}}
                    2826 \verb|\expandafter\newcommand\expandafter*\csname xP0frm2{-e}\endcsname{\%}
                    2827 \xP@framedrop\xP@dsdashellframe
                    2828 }
```

```
\xP@dsdashellframe
                    2829 \newcommand*\xP@dsdashellframe[1]{%
                          \xP@getradii{#1}%
                    2831
                          \xP@frameifnotzero\xP@dsdashellipse
                    2832 }
  \xP@dsdashellipse
                    2833 \newcommand*\xP@dsdashellipse{%
                    2834
                          \hskip\dimexpr(\R@c-\L@c)/2\relax
                    2835
                          \lower\dimexpr(\D@c-\U@c)/2\relax
                          \h
                    2836
                    Inner ellipse: true ellipse
                            \advance\A@-\xydashh@
                             \advance\B@-\xydashh@
                    2838
                             \left(\frac{A0}{z0}\right)
                    2839
                            \left| \frac{B@<\z@B@\z@fi}{B} \right|
                    2840
                            2841
                    2842
                         }%
                    2843 }
\xP@elldoublestroke
                    2844 \newcommand*\xP@elldoublestroke{\z@,\xydashh@}
          \xP@fill
                    2845 \newcommand*\xP@fill[1]{\xP@literal{#1 f}}
    \xP@fillstroke
                    2846 \newcommand*\xP@fillstroke[1]{\xP@literal{\xP@dim{\xP@preclw/2}w 1 j 0 G #1 b}}
   \xP@fillorstroke
                    2847 \newcommand*\xP@fillorstroke{}
           frm\{*\}
         \xP@frm{*}
                    2848 \xP@hook{frame}{frm{*}}
                    2849 \expandafter\newcommand\expandafter*\csname xP0frm\{*\}\
                          \xP@framedrop{\let\xP@fillorstroke\xP@fill\xP@framefill}%
                    2851 }
          \frm{**}
       \xP@frm{**}
                    2852 \xP@hook{frame}{frm{**}}
                    2853 \expandafter\newcommand\expandafter*\csname xP@frm{**}\endcsname{%
                          \xP@framedrop{\let\xP@fillorstroke\xP@fillstroke\xP@framefill}%
                    2855 }
      \xP@framefill
                    2856 \newcommand*\xP@framefill[1]{%
                    2857
                          \R0#1\relax
                    2858
                          \xP@setsolidpat
                          \setboxz@h{%
                    2859
                             \hskip\X@c\raise\Y@c\hbox{%
                    It would appear to make more sense to examine the token register \Edge@c instead of
```

\prevEdge@@. If I (Daniel) had done so, the code *+<1pc>[o]\frm{*} had given a filled

circle.

This certainly makes sense, but the dvips driver lets the frame be drawn in accordance with the object drawn before. Hence, I copied this behavior. E.g., the following code gives a filled ellipse:

 $xy *[o]{a} *frm{*} \end{xy}$

```
2861
                                 \DN@{\rectangleEdge}%
                      2862
                                 \ifx\next@\prevEdge@@
                      2863
                                    \DN0{\xP@oval}%
                                  \else
                      2864
                      2865
                                    \DN@{\circleEdge}%
                                    \ifx\next@\prevEdge@@
                      2866
                                      \left| R@=\right| z@
                      2867
                                        \DN@{\xP@filledellipse}%
                      2868
                      2869
                                      \else
                      2870
                                        \DN@{\restR@max\xP@circle}%
                      2871
                                      \fi
                      2872
                                    \else
                                      \left| \frac{R0=\z0}{} \right|
                      2873
                                        \DN0{\xP@oval}%
                      2874
                      2875
                                      \else
                      2876
                                        \DN@{\xP@circle}%
                      2877
                                    \fi
                      2878
                      2879
                                 \fi
                                  \next@
                      2880
                      2881
                               }%
                      2882
                            }%
                      2883
                             \wd\z0\z0\ht\z0\z0\dp\z0\z0
                             \boxz@
                      2884
                      2885 }
        \xP@circle
                      2886 \newcommand*\xP@circle{%}
                            \xP@ellipse\R@\R@
                      2887
                      2888 }
\xP@filledellipse
                      2889 \newcommand*\xP@filledellipse{%
                            \xP@ellipse{\dimexpr(\L@c+\R@c)/2\relax}{\dimexpr(\U@c+\D@c)/2\relax}%
                      2891 }
\xP@framedellipse
                      2892 \newcommand*\xP@framedellipse{%
                      2893
                            \xP@ellipse\A@\B@
                      2894 }
      \xP@ellipse
                      2895 \newcommand*\xP@ellipse[2]{%
                             \mbox{\label{local} linear (\R@c-\L@c)/2\relax}
                      2896
                             \label{lowerdimexpr(D@c-U@c)/2} $$ \operatorname{lower}(D@c-U@c)/2\relax $$
                      2897
                             \h
                      2898
                               \A0#1\relax
                      2899
                      2900
                               \B@#2\relax
                      2901
                               \xP@ellipse@
                      2902
                            }%
                      2903 }
```

```
2904 \newcommand*\xP@ellipse@{%
Perimeter, second segment
      \M^0 \times 543339720/768398401 = 1
      \Y@p\dimexpr\B@*543339720/768398401\relax
2906
2907
      \L@c\dimexpr\A@*34221476/65864945\relax
2908
      \U@c\dimexpr\B@*554561898/619869377\relax
      \R@c\dimexpr\A@*173517671/654249180\relax
2909
      \D@c\B@
2910
2911
      \X@c\z@
2912
     \Y@c\B@
      \xP@bezierlength
2913
2914
      \@tempdima\@tempdimb
Perimeter, first segment
      \X@p\A@
2915
2916
      \Y@p\z@
2917
      \L@c\A@
      \U@c\dimexpr\B@*173517671/654249180\relax
2918
2919
      \R@c\dimexpr\A@*554561898/619869377\relax
      \D@c\dimexpr\B@*34221476/65864945\relax
2920
2921
      \X \c \dim \xspr \A @*543339720/768398401 \relax
2922
      \W0c\dim xpr\B0*543339720/768398401\relax
2923
      \xP@bezierlength
      \@tempdimb4\dimexpr\@tempdima+\@tempdimb\relax
2924
2925
      \edef\@tempa{%
2926
        \xP@dim\A@O m
        \xP@coor\L@c\U@c
2927
2928
        \xP@coor\R@c\D@c
        \xP@coor\X@c\Y@c c %
2929
        2930
        \xP@coor{\A@*173517671/654249180}\B@
2931
2932
        0 \propto P@dim\B@ c }
      \@temptokena\expandafter{\@tempa}%
2933
2934
      \xP@mirrorpath
2935
      \xP@fillorstroke{\the\@temptokena}%
2936 }
   End of the section for Xy-pic's "frame" option.
2937 \xyendinput
2938 (/frame)
       Line styles
9.16
2939 (*line)
2940 \xycatcodes
2941 \expandafter\let\csname xypdf-li@loaded\endcsname\@empty
2942 % Dummy file.
   End of the section for Xy-pic's "line" option.
2943 \xyendinput
2944 (/line)
```

Finish the package initialization. The \xywithoption commands are wrapped into \next@ so that they cannot change the catcodes for the next \xywithoption command.

2945 (*basic)

```
2946 \let\@tempa\@undefined
2947 \let\nextii@\@undefined
2948 \DN@{%
      \xywithoption{color}{%
2949
      \message{Xy-pic pdf driver: 'color' extension support}%
2950
      \@ifundefined{xypdf-co@loaded}{\input xypdf-co\relax}{\message{not reloaded}}%
2951
2952
      \xywithoption{curve}{%
2953
      \message{Xy-pic pdf driver: 'curve' extension support}%
2954
      \@ifundefined{xypdf-cu@loaded}{\input xypdf-cu\relax}{\message{not reloaded}}%
2955
2956
      \xywithoption{frame}{%
2957
      \message{Xy-pic pdf driver: 'frame' extension support}%
2958
      \@ifundefined{xypdf-fr@loaded}{\input xypdf-fr\relax}{\message{not reloaded}}%
2959
2960
2961
      \xywithoption{line}{%
      \message{Xy-pic pdf driver: 'line' extension support}%
2962
      \@ifundefined{xypdf-li@loaded}{\input xypdf-li\relax}{\message{not reloaded}}%
2963
2964
      \xywithoption{rotate}{%
2965
      \message{Xy-pic pdf driver: 'rotate' extension support}%
2966
2967
      \@ifundefined{xypdf-ro@loaded}{\input xypdf-ro\relax}{\message{not reloaded}}%
2968
2969 }
2970 \next@
2971 \xyendinput
2972 \langle /\mathsf{basic} \rangle
```

10 Changelog

v1.0 2010/03/24

Initial version

v1.1 2010/03/30

- Added support for the Xy-pic "rotate" extension.
- The parts of the style file dealing with Xy-pic extensions (currently "curve" and "rotate") are only executed when those extension were loaded.
- xypdf does not give an error message when used with Xy-pic options which query the Postscript drivers (e. g. "all" or "color").
- In DVI mode, a warning is issued that the DVI file is not portable, like Xy-pic does when a Postscript driver is in use.

v1.2 2010/04/08

- Improved precision and numerical stability for the offset algorithm around cusps.
- Improved slide algorithm \xP@slide@
- Respect \pdfdecimaldigits when dimensions are written to the PDF file.
- \bullet Correct continuation for dashed/dotted/squiggled curves consisting of more than one segment.
- Code cleanup

v1.3 2010/04/12

- Bug fix: No "Extra \fi" if \ifpdfabsdim is not defined.
- Bug fix: Moved the code for the spline continuation out of the optional section for curves since it is also needed for straight lines.
- Check the version of pdfTFX since \pdfsave is not defined prior to pdfTFX 1.40.0.
- "Troubleshooting" paragraph for T_FX Live without the ε -T_FX features enabled.
- Generic PDF code for the {-} directional object.

v1.4 2010/05/13

- Support for both plain TEX and LATEX, reorganization of the code and splitting into several files. The LATEX style file xypdf.sty has been replaced by xypdf.tex, which is recognized by Xy-pic as a driver.
- Integration into the Xy-pic distribution.
- Support for the "color" and "frame" extensions.
- New supported curve style {~~} (broken squiggled curves).

v1.5 2010/10/11

- Bug fix: Colored curves.
- Bug fix: PDF syntax in double elliptical frames.

v1.6 2011/02/09

The xypdf package was made even more frugal with dimension registers. If it is used as a LATEX package, it can now be loaded even if there is not a single free dimension register. The primary reason for this improvement is that xypdf now works with the "beamer" document class.

v1.7 2011/03/20

- The \newxycolor command is overwritten with the xypdf code in the preamble, not at \begin{document} as before, so that new colors can be defined anytime.
- Improved logic to detect zero-sized frames.
- \newxycolor bug fix.
- Corrected the position of the center of rotation and scaling.
- Colored frame objects.
- New section "Differences between xypdf and the dvips backend" in the documentation.