

Introductory Macroeconomics

Lecture 13: savings and capital formation

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This Lecture

- Savings and capital formation
 - concepts of saving and its determinants
 - concepts of investment and its determinants
 - equilibrium interest rate, savings, and investment
- BOFAH chapter 4

Saving and the Saving rate

- *Saving* is defined as current income minus spending on current needs

national savings

private saving

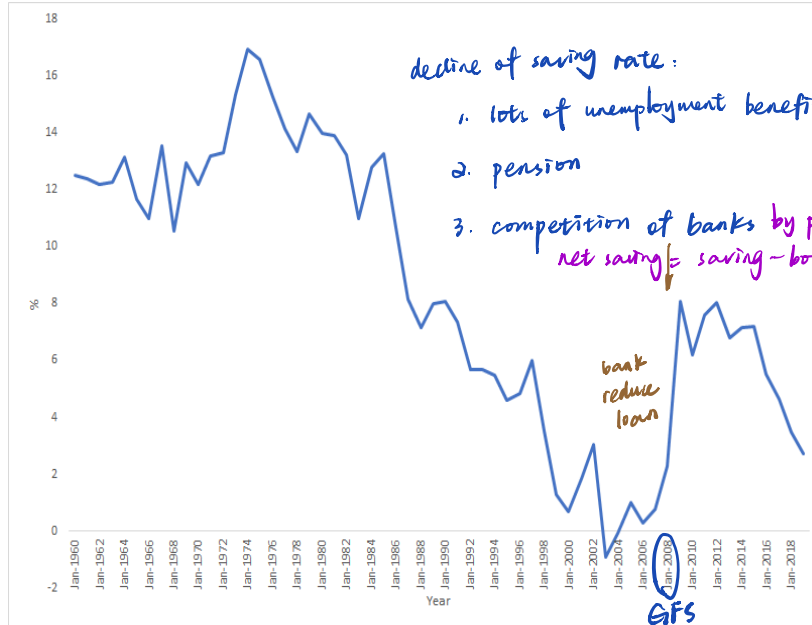
public saving

- household saving *deposit income* *unemployment benefit*
 - * income: wages, interest, dividends, transfer
 - * spending: consumption of goods and services, expenditure on depreciation → *durable goods*
- firm saving
 - * income: sale of goods and services *eg. financial bank*
 - * spending: payment of wages, raw materials, interest, dividend, etc
- government saving (= *primary fiscal surplus* [?])
 - * income: tax from households and firms
 - * spending: government purchases of goods and services, transfer

- *Saving rate* of an economic unit is its saving divided by its income

$$\text{saving rate} = \frac{\text{saving}}{\text{income}}$$

Household Saving Rate in Australia



decline of saving rate :

1. lots of unemployment benefit
 2. pension
 3. competition of banks by providing more loans.
- less worried & save less
- net saving = saving - borrowing ↑

bank
reduce
loan

GFS

Reasons for Saving

- Lifecycle saving (savings against predictable events)
 - saving to meet long-term objectives such as paying off student loans, house purchase, retirement
- Precautionary saving (savings against unpredictable events)
 - saving for unexpected events such as job loss, medical emergency
- Bequest saving
 - saving for the next generation
- Other reasons
 - culture, aging society, peer effect

Saving and the Real Interest Rate

- Whatever the one's saving motive is the amount of saving depends on the *real interest rate*

- positive effect: increases the reward for saving $r \uparrow$ reward for saving \uparrow

- negative effect: fewer savings are needed to reach the target saving

- empirical evidence suggests that the positive effect dominates

reduce saving
since can reach
target saving with less
saving

S & r positively correlated
saving

Decomposition of National Saving

- Recalling that T refers to a net tax, national savings NS

$$NS = \underbrace{(Y - T - C)}_{\text{private saving}} + \underbrace{(T - G)}_{\text{public saving}}$$

\downarrow app \rightarrow disposable income by private agent
 $\text{net tax} = \text{tax} - \text{transfer}$
 $\text{tax} - (\text{transfer} + G)$
 \downarrow income \quad spending

- What is the national saving?

- nation's income Y is the income of private (non-government) sector
- private saving is by households and firms
- recall that public saving equals primary fiscal surplus

$$\begin{aligned}
 T > G & \quad \text{fiscal surplus} \\
 T < G & \quad \text{fiscal deficit} \\
 T = G & \quad \text{balanced budget}
 \end{aligned}$$

Stock and Flow

- *Flow* is a measure that is defined (within a time window)
 - example: Chris's saving is \$20 per week
 - Chris's weekly saving is a flow variable
- *Stock* is a measure that is defined at a point in time
 - example: Chris has a savings account balance of \$80 as of January 28th 2020
 - Chris's balance as of January 28th 2020 is a stock variable

Jan 28th 10pm \$20 \Rightarrow Jan 29th 9am

$$\text{Stock}_{t+1} = \text{Flow}_t + \text{Stock}_t$$

Chris saving
29th = \$100



Chris's saving balance Jan 28th = \$80
at the same day
make additional saving \$20

Investment and Capital Formulation

- Relationship between capital K and investment
 - capital is a stock: the amount of equipment and machines that exist at a point time
 - investment is a flow: the purchases of equipment and machines that have been made within a time window

$$K_{t+1} = \underbrace{(1 - \delta)K_t}_{\text{depreciated capital}} + I_t$$

KE: undep capital

- δ is the depreciation rate
- this equation implies that investment made in time t is a spending on future needs (i.e., time $t + 1$)
- capital in time $t + 1$ is used to produce outputs in time $t + 1$

Determinants of Investment

recall AD: $I = \bar{I} - \delta_1 Y$

- Firms base investment decisions to maximise profits
- Let's make a few assumptions to define profits

- firms rent capital at the real interest rate r

- firms produce output using capital as an input, $Y = K^{1/3}$

- firms must make up the worn-out capital, which depreciates at δ

- output is sold at a price p

\$1000 rent*

\$100,000 price of house

rental rate = real interest rate 1%

②.

$K \uparrow \rightarrow Y \uparrow$

Determinants of Investment

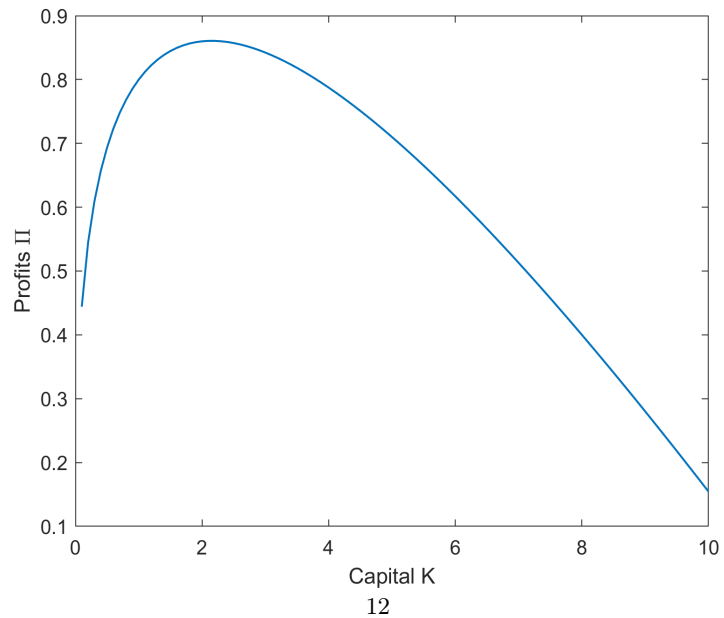
- Firm's profits Π

$$\begin{aligned}\Pi &= pK^{1/3} - rK - \delta K \\ &= \underbrace{pK^{1/3}Y}_{\text{total revenue}} - \underbrace{(r + \delta)K}_{\text{total cost}}\end{aligned}$$

Handwritten annotations:
- Above $pK^{1/3}$: quantity Y price p
- Above rK : \sim rent
- Above δK : \sim depreciate cost

- What is the profit-maximising capital?
 - for illustration, let $p = 1$, $r = 0.1$ and $\delta = 0.1$.

Profit Function



Profit-Maximising Capital

$$\pi = p k^{1/3} - (r + \delta)k$$

$$\frac{d\pi}{dk} = \frac{1}{3} p k^{-2/3} - (r + \delta) = 0$$

$$\frac{1}{3} p k^{-2/3} = \underbrace{r + \delta}$$

$$\frac{d(\text{total revenue})}{dk} = \frac{d(\text{total cost})}{dk}$$

$$\text{MRPK} = \text{marginal cost}$$

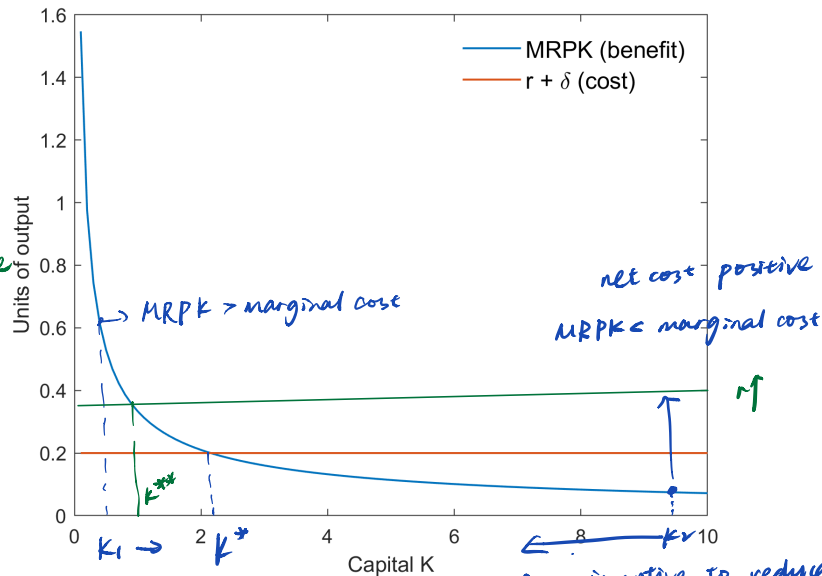
- Mathematically, it is a point at which the slope of the profit function is zero (i.e., $\frac{\partial \pi}{\partial K} = 0$)

$$\begin{aligned} \frac{\partial(\text{total revenue})}{\partial K} &= \frac{\partial(\text{total cost})}{\partial K} \\ \frac{1}{3} p K^{-2/3} &= (r + \delta) \end{aligned}$$

- LHS is the *marginal revenue product of capital* (MRPK) which is defined as the extra revenue received from selling the output produced from adding an extra unit of capital
- RHS is the extra cost incurred from adding an extra unit of capital, which is the factor price
- Firm's profit-maximizing capital is a point that equates the benefit of an extra unit of capital with its cost

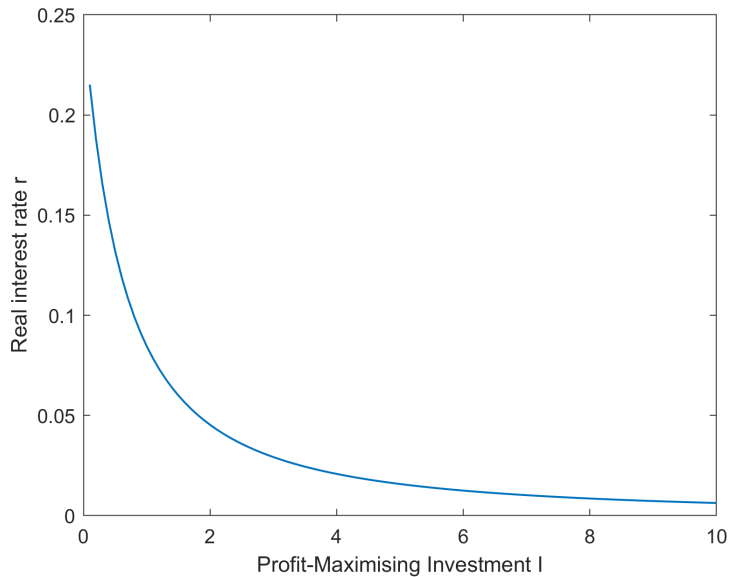
Profit-Maximising Capital

case when $r \uparrow$
 $\Rightarrow r \uparrow \rightarrow K \downarrow$
 capital is increase/decrease
 depending on investment
 $K \downarrow$ $I \downarrow$

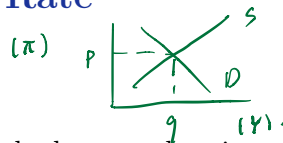


$\leftarrow K \downarrow$
 firm incentive to reduce capital

Investment and Real Interest Rate

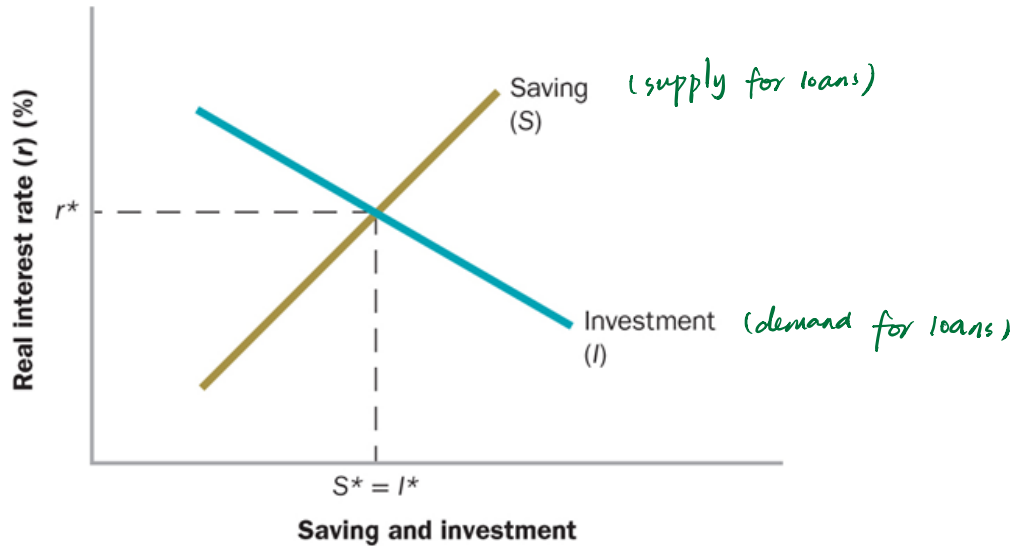


Equilibrium Real Interest Rate

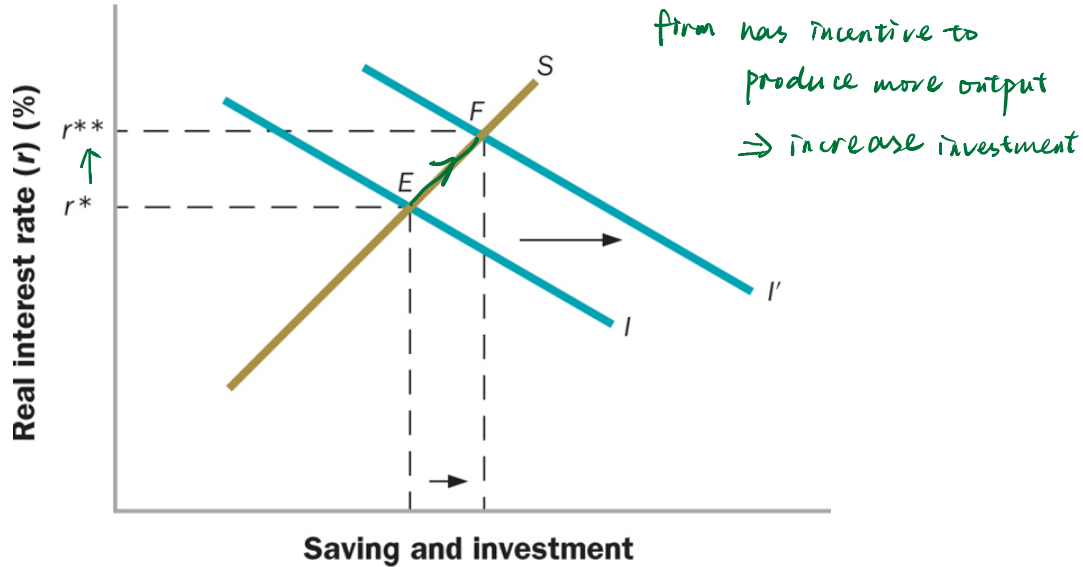


- Equilibrium real interest rate is determined in the loan market, in which those who supply loans and those who demand loans meet
 - those who demand loans are firms that use the saving to make investment = demand for loans
 - those who supply loans are households through savings
 - equilibrium interest rate in a closed economy is determined in a way that equates the supply and demand for loans

Equilibrium Real Interest Rate



Effects of New Technology



Next Lecture

- Overview of economic growth
 - facts about the world's economic growth
 - main economic factors that lead to economic growth