

School of Mathematics and Statistics  
MAST20009 Vector Calculus, Semester 1 2020  
Assignment 1 and Cover Sheet

<i>Student Name</i>	<i>Student Number</i>
<i>Tutor's Name</i>	<i>Tutorial Day/Time</i>

**Submit your assignment to your tutor's MAST20009 assignment box  
before 11am on Tuesday 24th March.**

- This assignment is worth 5% of your final MAST20009 mark.
- Assignments must be neatly handwritten in blue or black pen on A4 paper. Diagrams can be drawn in pencil.
- You must complete the plagiarism declaration on the LMS before submitting your assignment.
- Full working must be shown in your solutions.
- Marks will be deducted for incomplete working, insufficient justification of steps, incorrect mathematical notation and for messy presentation of solutions.

1. Consider the function

$$f(x, y) = \begin{cases} \frac{xy^6}{3x^4 + 4y^6}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0). \end{cases}$$

(a) Evaluate

$$\lim_{(x,y) \rightarrow (0,0)} f(x, y)$$

along the path  $y = kx$ , where  $k \in \mathbb{R} \setminus \{0\}$ .

(b) Evaluate

$$\lim_{(x,y) \rightarrow (0,0)} f(x, y)$$

if it exists or justify why the limit does not exist.

(c) Find  $\frac{\partial f}{\partial x}$  and  $\frac{\partial f}{\partial y}$  for all  $(x, y) \in \mathbb{R}^2$ .

(d) Determine where  $f$  is  $C^1$ . Justify your answer, referring to any theorems you use.

2. Consider the function

$$g(x, y) = (3y - x)^{\frac{3}{2}}.$$

(a) Determine the second order Taylor polynomial for  $g$  about  $(2, 1)$ .

(b) Using part (a), approximate  $g(2.1, 0.9)$ .

(c) Using Taylor's remainder formula, determine an upper bound for the error in your approximation of  $g(2.1, 0.9)$ .

(d) Calculate the actual error in your approximation of  $g(2.1, 0.9)$ . How does the actual error compare to your approximate error in part(c)?