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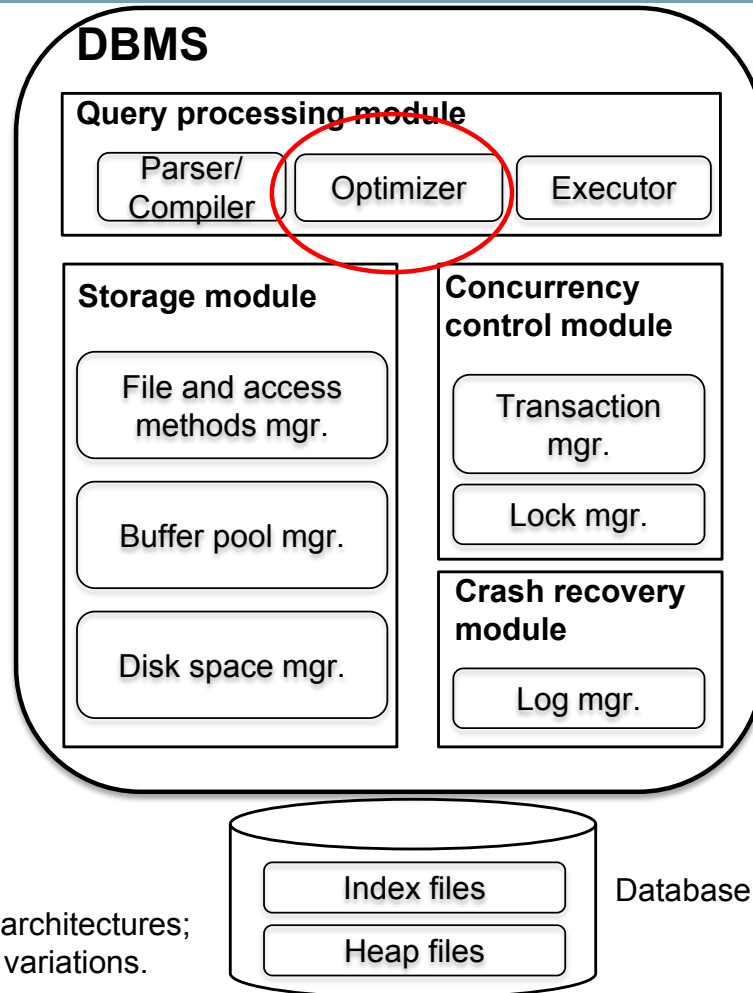
INFO20003 Database Systems

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Lecture 13
Query Optimization Part I

Week 7

Remember this? Components of a DBMS



**TODAY &
Next time**

This is one of several possible architectures; each system has its own slight variations.



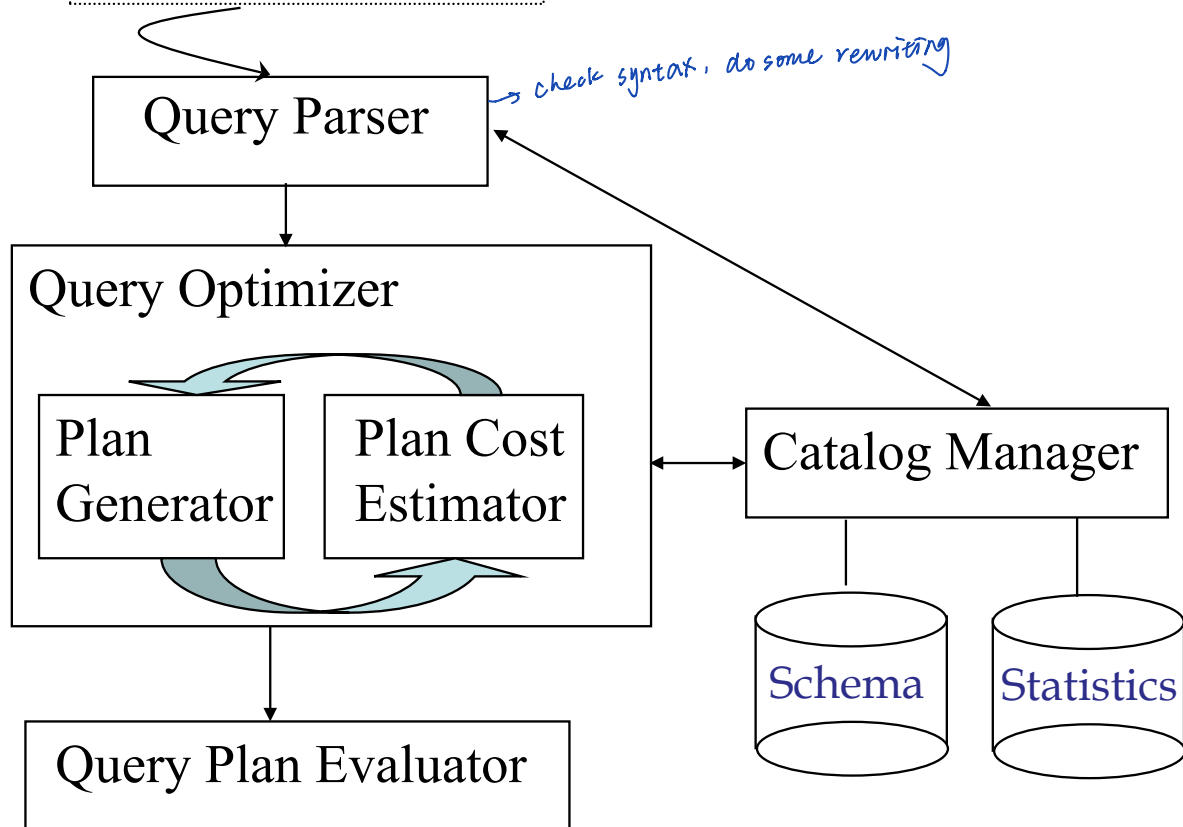
- Overview
- Query optimization
- Cost estimation

Readings: Chapter 12 and 15, Ramakrishnan & Gehrke, Database Systems

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Query

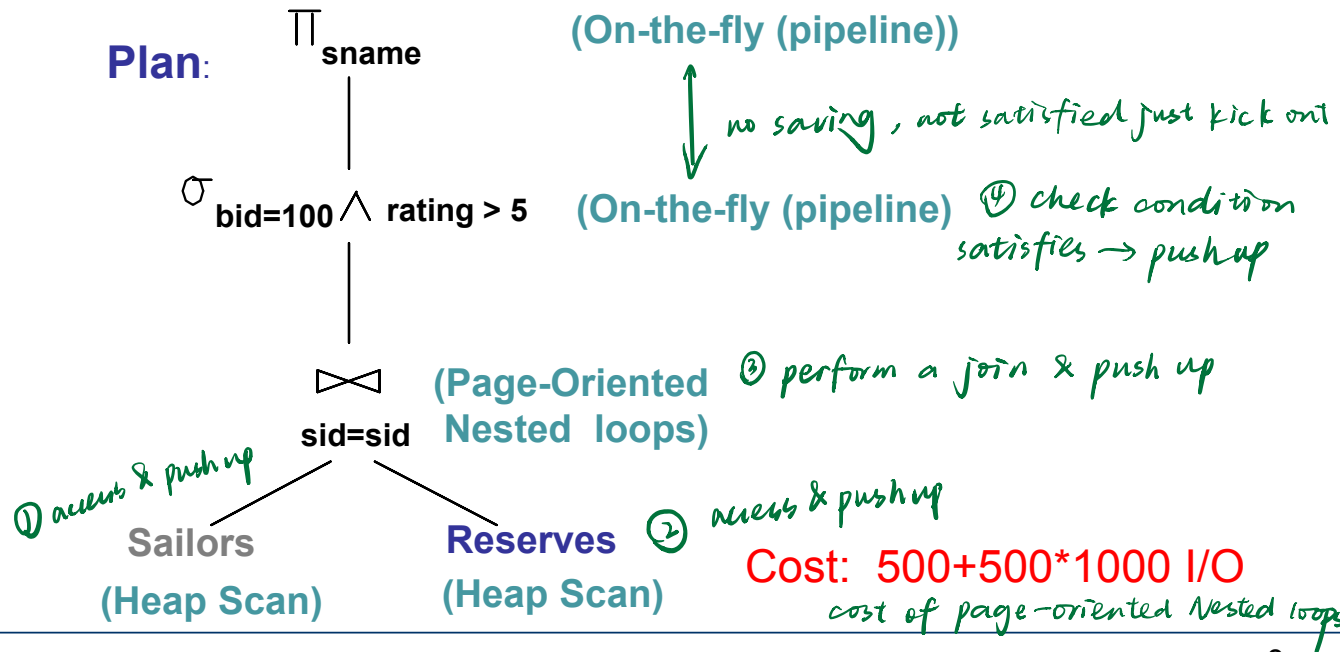
```
Select *  
From Blah B  
Where B.blah = "foo"
```



- Typically there are many ways of executing a given query, all giving the same answer
- Cost of alternative methods often **varies enormously**
- Query optimization aims to find the execution strategy with the lowest cost
- We will cover:
 - Relational algebra equivalences
 - Cost estimation
 - Result size estimation and reduction factors
 - Enumeration of alternative plans

- A tree, with relational algebra operators as nodes and access paths as leaves
- Each operator labeled with a choice of algorithm

SELECT sname from Sailors NATURAL JOIN Reserves
WHERE bid = 100 and rating > 5





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Sailors (*sid*: integer, *sname*: string, *rating*: integer, *age*: real)

Reserves (*sid*: integer, *bid*: integer, *day*: dates, *rname*: string)

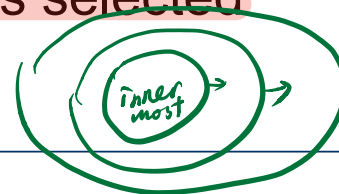
Boats (*bid*: integer, *bname*: string, *color*: string)

Example:

```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```

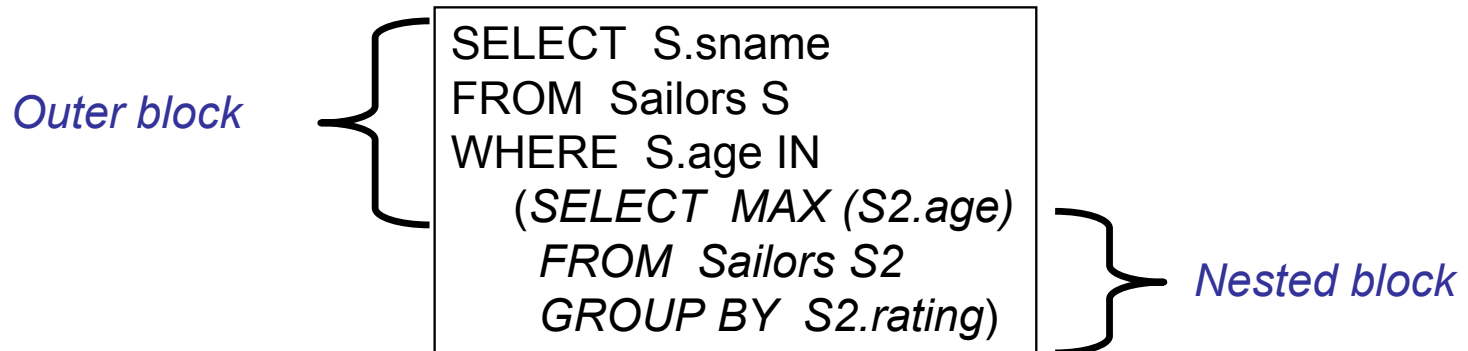
Query optimization steps:

1. Query first broken into “blocks” → *every individual part start with SELECT is a block*
2. Each block converted to relational algebra
3. Then, for each block, several alternative query plans are considered
4. Plan with the lowest estimated cost is selected
per block



Step 1: Break query into query blocks

- Query block is any statement starting with select
- **Query block = unit of optimization**
- Typically inner most block is optimized first, then moving towards outers



Step 2: Convert query block into relational algebra expression

Query:

```
SELECT S.sid  
FROM Sailors S, Reserves R, Boats B  
WHERE S.sid = R.sid AND R.bid = B.bid AND B.color = "red"
```

Relational algebra:

$$\pi_{S.sid}(\sigma_{B.color = \text{"red"}}(Sailors \bowtie Reserves \bowtie Boats))$$

Step 3: Relational Algebra Equivalences

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sailors $\sigma_{age > 50 \wedge rating = 10} \longleftrightarrow \sigma_{rating = 10} \downarrow \text{Hil also OK}$

- **Selections**: $\sigma_{c_1 \wedge \dots \wedge c_n}(R) \equiv \sigma_{c_1} \left(\dots \left(\sigma_{c_n}(R) \right) \right)$ (Cascade) 传递

$$\sigma_{c_1} \left(\sigma_{c_2}(R) \right) \equiv \sigma_{c_2} \left(\sigma_{c_1}(R) \right) \quad (\text{Commute})$$

- **Projections**: $\pi_{a_1}(R) \equiv \pi_{a_1} \left(\dots \left(\pi_{a_n}(R) \right) \right)$ (Cascade)

ID	age	name

a_i is a set of attributes of R and $a_i \subseteq a_{i+1}$ for $i = 1 \dots n - 1$

$$\pi_{ID} \left(\pi_{ID, age, name(s)} \right)$$

- These equivalences allow us to 'push' selections and projections ahead of joins.

Selection:

$$\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors})$$

$$\longleftrightarrow \sigma_{\text{age} < 18} (\sigma_{\text{rating} > 5} (\text{Sailors}))$$

$$\longleftrightarrow \sigma_{\text{rating} > 5} (\sigma_{\text{age} < 18} (\text{Sailors}))$$

Projection:

not a subset

$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \not\supseteq \pi_{\text{age}} (\pi_{\text{rating}} (\text{Sailors})) \quad ?$$

↑ lost age

$$\pi_{\text{age}, \text{rating}} (\text{Sailors}) \longleftrightarrow \pi_{\text{age}, \text{rating}} (\pi_{\text{age}, \text{rating}, \text{sid}} (\text{Sailors}))$$

- A projection commutes with a selection that only uses attributes retained by the projection

$$\pi_{\text{age, rating, sid}} (\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors}))$$

$$\longleftrightarrow \sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\pi_{\text{age, rating, sid}} (\text{Sailors}))$$

$$\pi_{\text{age, sid}} (\sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\text{Sailors}))$$

~~$$\longleftrightarrow \sigma_{\text{age} < 18 \wedge \text{rating} > 5} (\pi_{\text{age, sid}} (\text{Sailors}))$$~~

lost rating

?

$$R \bowtie (S \bowtie T) \equiv (R \bowtie S) \bowtie T \quad (\text{Associative})$$

$$(R \bowtie S) \equiv (S \bowtie R) \quad (\text{Commutative})$$

- These equivalences allow us to choose **different join orders**

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- Converting selection + ^{expensive} cross-product to join

$$\sigma_{S.sid = R.sid} (Sailors \times Reserves)$$

cross product + selection
→ natural join

$$\leftrightarrow Sailors \bowtie_{S.sid = R.sid} Reserves$$

- Selection on just attributes of S commutes with $R \bowtie S$

$$\sigma_{S.age < 18} (Sailors \bowtie_{S.sid = R.sid} Reserves)$$

first selection
→ then join

$$\leftrightarrow (\sigma_{S.age < 18} (Sailors)) \bowtie_{S.sid = R.sid} Reserves$$

- We can also “push down” projection (but be careful...)

$$\pi_{S.sname} (Sailors \bowtie_{S.sid = R.sid} Reserves)$$

↑
careful about the attribute keep

$$\leftrightarrow \pi_{S.sname} (\pi_{sname, sid}(Sailors) \bowtie_{S.sid = R.sid} \pi_{sid}(Reserves))$$



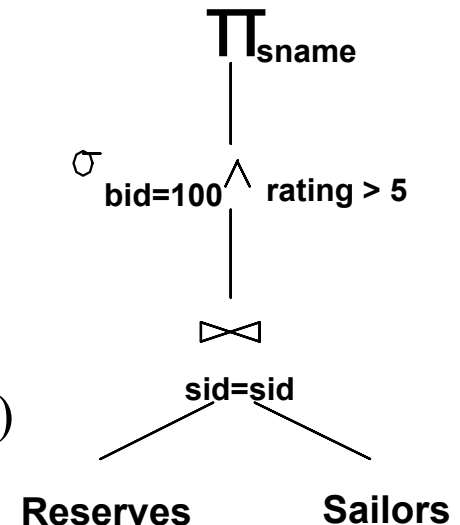
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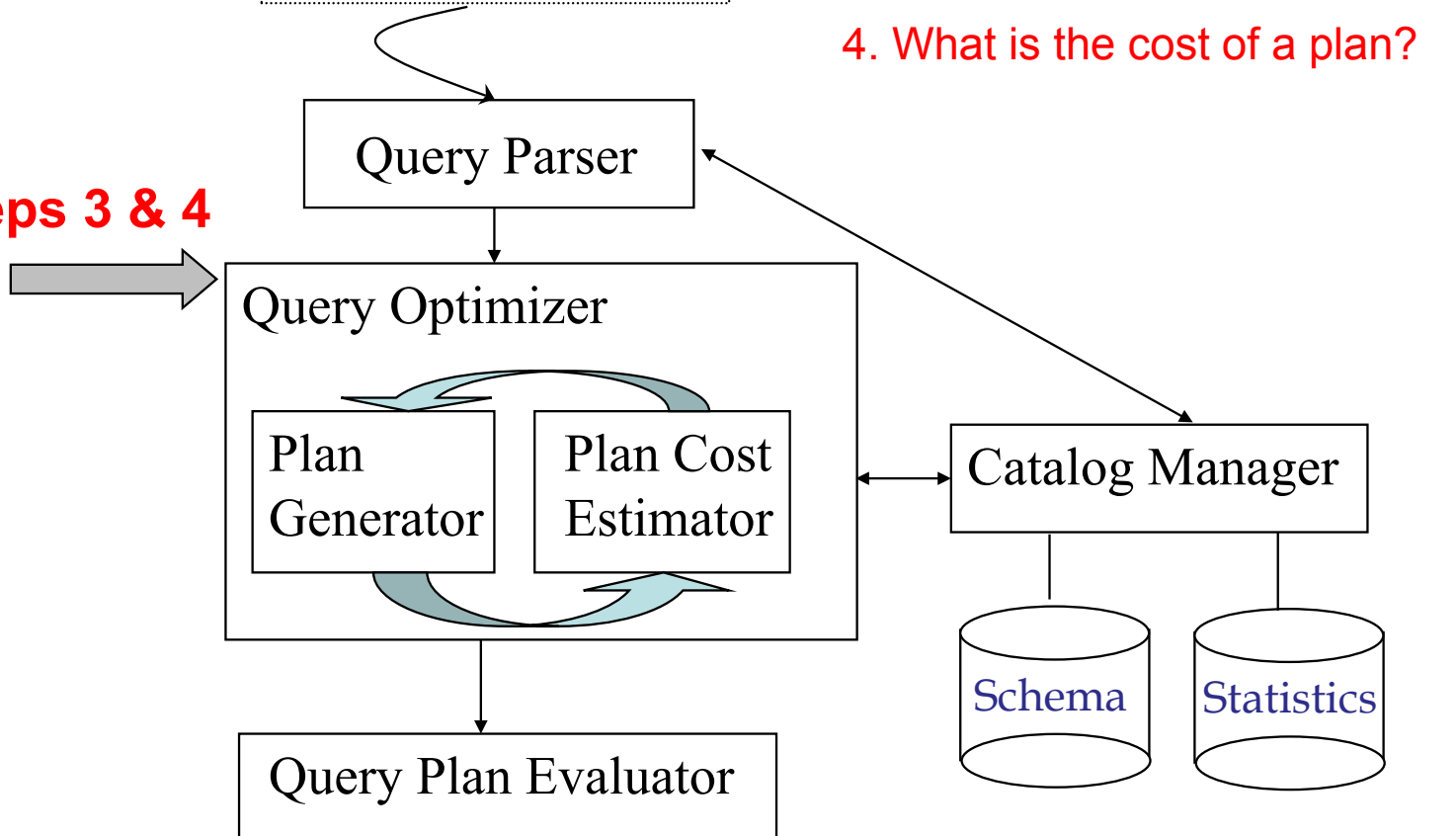
```
SELECT S.sname
FROM Reserves R, Sailors S
WHERE R.sid=S.sid AND
      R.bid=100 AND S.rating>5
```

$\pi_{(sname)} \sigma_{(bid=100 \wedge rating > 5)} (Reserves \bowtie Sailors)$



Queries

```
Select *  
From Blah B  
Where B.blah = "foo"
```

Steps 3 & 4

- For each plan considered, must estimate cost:
 - Must estimate size of result for each operation in tree
 - Use information about input relations (from the system catalogs), and apply rules (discussed next)
 - Must estimate cost of each operation in plan tree
 - Depends on input cardinalities
 - We've already discussed how to estimate the cost of operations (sequential scan, index scan, joins)
 - Next time we will calculate the cost of entire plans...
- output for this query will be an input for next step*

- To decide on the cost, the optimizer needs information about the relations and indexes involved. This information is stored in the **system catalogs**.

*keep
metadata
(description
of data)*

- **Catalogs** typically contain at least:

- # tuples (**NTuples**) and # pages (**NPages**) per relation

- # **distinct** key values (**NKeys**) for each **index** (or relation attribute)

- low/high key values (**Low/High**) for each **index** (or relation attribute)

- Index height (**Height(I)**) for each tree index

- # index pages (**NPages(I)**) for each index

- Statistics in catalogs are updated periodically

not necessary 100% accurate

*eg
sort or ranking
1...10
Nkeys 10
(distinct
key value)
domain of
value*

- Consider a query block:

```
SELECT attribute list
FROM relation list
WHERE predicate1 AND ... AND predicate_k
```
- Maximum number of tuples in the result is the **product** of the cardinalities of relations in the FROM clause
- Reduction factor (RF)** associated with each predicate reflects the impact of the predicate in reducing the result size. RF is also called **selectivity**.

- Single table selection:

$$\mathbf{ResultSize} = NTuples(R) \prod_{i=1..n} RF_i$$

- Joins (over k tables):

$$\mathbf{ResultSize} = \prod_{j=1..k} NTuples(R_j) \prod_{i=1..n} RF_i$$

- If there are no selections (no predicates), reduction factors are simply ignored, i.e. they are ==1

Calculating Reduction Factors(RF)

- Depend on the type of the predicate:

1. Col = value

$$RF = 1 / \text{NKeys}(\text{Col})$$

↓
distinct value

2. Col > value

$$RF = (\text{High}(\text{Col}) - \text{value}) / (\text{High}(\text{Col}) - \text{Low}(\text{Col}))$$

3. Col < value

$$RF = (\text{val} - \text{Low}(\text{Col})) / (\text{High}(\text{Col}) - \text{Low}(\text{Col}))$$

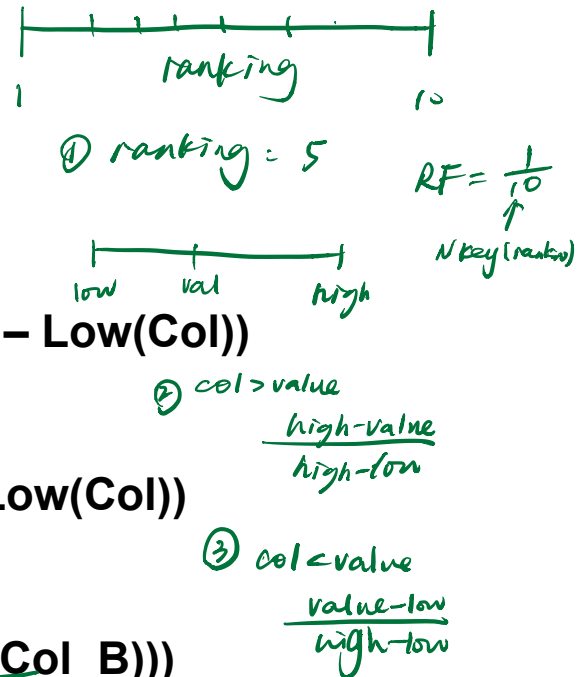
4. Col_A = Col_B (for joins)

$$RF = 1 / (\text{Max}(\text{NKeys}(\text{Col}_A), \text{NKeys}(\text{Col}_B)))$$

max of distinct value

5. In no information about Nkeys or interval, use a “magic number” 1/10

$$RF = 1/10$$



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Sailors (S): NTuples(S) = 1000, Nkeys(rating) = 10 interval [1-10],
age interval [0-100], Nkeys(sid) = 1000

$RF = \frac{1}{10}$ $RF = \frac{50}{100} = \frac{1}{2}$
*SELECT * FROM Sailors WHERE rating = 3 AND age > 50;*

Calculate result size:

$$\begin{aligned} & NTuple \cdot RF(rating) \cdot RF(age > 50) \\ & = 1000 \times \frac{1}{10} \times \frac{1}{2} = 50 \text{ tuple.} \end{aligned}$$

$$NTuples(S) = 1000$$

$$RF(rating) = 1/10 = 0.1$$

$$RF(age) = (100-50)/(100-0) = 0.5$$

$$\begin{aligned} \underline{\text{ResultSize} = NTuples(S) \cdot RF(rating) \cdot RF(age)} \quad \checkmark \\ = 1000 \cdot 0.1 \cdot 0.5 = 50 \text{ tuples} \end{aligned}$$



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- What is query optimization/describe steps?
- Equivalence classes
- Result size estimation
- Important for Assignment 3 as well



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- Query optimization Part II
 - Plan enumeration