

ASSIGNMENT 1: MATRIX MULTIPLICATION

Your report must be handed in electronically on Campusnet in PDF format!

Deadline: latest on January 6, 2017 at 16:00!

Background

The BLAS (Basic Linear Algebra Subroutines) is a collection of subroutines which are used as building blocks for linear algebra software. For instance, LAPACK and ScaLAPACK use BLAS.

The BLAS exists in a so-called “model implementation” written in FORTRAN 77. A good source of numerical software is NETLIB at <http://www.netlib.org>.

Most computer vendors deliver a BLAS/LAPACK library that is particularly optimized for their own hardware. There are also different Open Source implementations available, and one of the most common ones is ATLAS (Automatically Tuned Linear Algebra Software).

One of the most important subroutines in the BLAS library is the general matrix-matrix multiplication routine called DGEMM, where D stands for DOUBLE PRECISION, GE for “general” and MM for “matrix matrix.” This routine is the core routine in the HPC Linpack benchmark, that is the basis for the TOP500 list of the fastest computers in the world.

The Assignment

In this assignment, you will have to develop a library of functions, that all carry out matrix-matrix multiplication, as specified below. As a part of this assignment, we provide a framework with a driver program on Campusnet, that can call your routines and print the timings, etc. Your library functions will be evaluated with the same tools, so you have to write your library according to the specifications provided.

For more details about the interface specifications, requirements, different coding styles, etc, see the documentation coming with the tools on Campusnet.

- Write a function, `matmult_nat()`, that performs a matrix-matrix multiplication with double precision matrix operands of suitable, but otherwise arbitrary, shape

$$\begin{matrix} & n \\ & \boxed{C} \\ m & \end{matrix} := \begin{matrix} & k \\ & \boxed{A} \\ m & \end{matrix} * \begin{matrix} & n \\ & \boxed{B} \\ k & \end{matrix}$$

The function takes six arguments: `m`, `n`, and `k`, and the three matrices `A`, `B`, and `C` in row-major format - for the details see the provided specifications.

Compare your results with the results obtained by calling `DGEMM()`, both to check your results, but also to compare the timings later on.

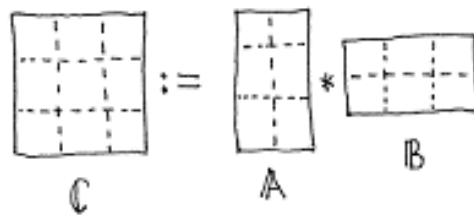
Your code has to work for arbitrary values of m , n , and k , i.e. you should use dynamic memory allocation (cf. lab exercises).

To fulfill the requirements, and to make it easier for the remainder of the project, you should wrap the call to DGEMM into a function `matmult_lib()`, that takes the same arguments as the other functions, i.e. m , n and k as well as A , B , and C .

- Essentially, the matrix-matrix multiplication algorithm consists of three nested loops. In how many ways can the loops be nested?

Write a function for each of the possibilities and use the three letters m , n , and k to label the versions, e.g. “`matmult_mnk`”, “`matmult_nmk`”, etc. Use numerical experiments to determine which of the possibilities is the fastest. Compare the timings without and with (different) compiler optimizations, and report your findings. Apply the techniques learned during lectures and exercises.

- Can you explain the performance differences between the different versions using some analysis tool, e.g. analyzer? Does the tool confirm your expectations?
- Write a blocked version of your matrix-matrix multiplication function, `matmult_blk()`, e.g. optimizing for the L1 cache size. Does blocking improve the performance? It is necessary to experiment with the block size for a given set of m , n , and k , in order to find an approximate optimum (this is a drawback of blocking). Can it be faster than the fastest non-blocked version? Do you think you can beat the compiler or a library supplied function?



On machines with a large cache size it may be necessary to use matrices of substantial size in order to ascertain and measure the performance improvements you want to try. For small matrix sizes, you may want to repeat the calculations many times to get reliable timings (this is e.g. implemented in the driver tools provided). You can achieve this by putting an outer loop around your code and run the calculation N times (N will of course depend on the sizes of your matrices, i.e. m , n , and k).

Hints

1. Write the code for all required functions in the library, and do your experiments. Upload the code as well as a compiled version of the library as a ZIP archive, together with your report as a PDF file, i.e. there are **2 files** that should be uploaded: a ZIP file and a PDF file!
2. Small pieces of code in the report are helpful to illustrate - and make it easier to understand - what you have done.

3. When using figures/tables/illustrations to show results (always nice), remember to explain what they show in the text!
4. Make sure that you answer all questions in the assignment!
5. Notice that relevant numerical experiments (runtimes, cache misses, block sizes, etc.) for large matrix sizes may take a long time to execute!
6. Make sure that you carry out sets of experiments on the same machine, to be able to compare the results. On the Linux machines, you can use the `less /proc/cpuinfo` or `lscpu` commands to get information about cache sizes, clock speed, etc. Please report those numbers in your report, as well as the compiler version you have used.
7. The front page of your report should state the names and the study numbers of all group members.

Goals

During this assignment, you will

1. learn how to write efficient code
2. make use of compiler optimizations
3. apply tuning techniques
4. use modern analysis tools
5. learn how to interface with standard libraries
6. learn how to write a library, given an interface specification
7. analyze and document your findings in a report

Technicalities

- To link to the CBLAS version of ATLAS on the Linux machines, you can use the options `-L/usr/lib64/atlas -lcblas`. If you are programming in C++, you will have to wrap the inclusion of the `cblas.h` header file with `'extern "C"'`, to avoid name mangling.
- With Sun/Oracle Studio the BLAS and LAPACK libraries are part of Performance Library (which is also optimized for Linux). You get access to these libraries by using the compiler option `-xlic_lib=sunperf` with the Sun/Oracle Studio C or C++ compiler.
- Some libraries switch automatically to a parallel mode (multi-threaded), when executed on a multi-core computer. Please check this, since this can make a comparison of the results difficult.