Conditional Language Modeling

Chris Dyer





Review: Unconditional LMs

A language model assigns probabilities to sequences of words, $\mathbf{w} = (w_1, w_2, \dots, w_\ell)$.

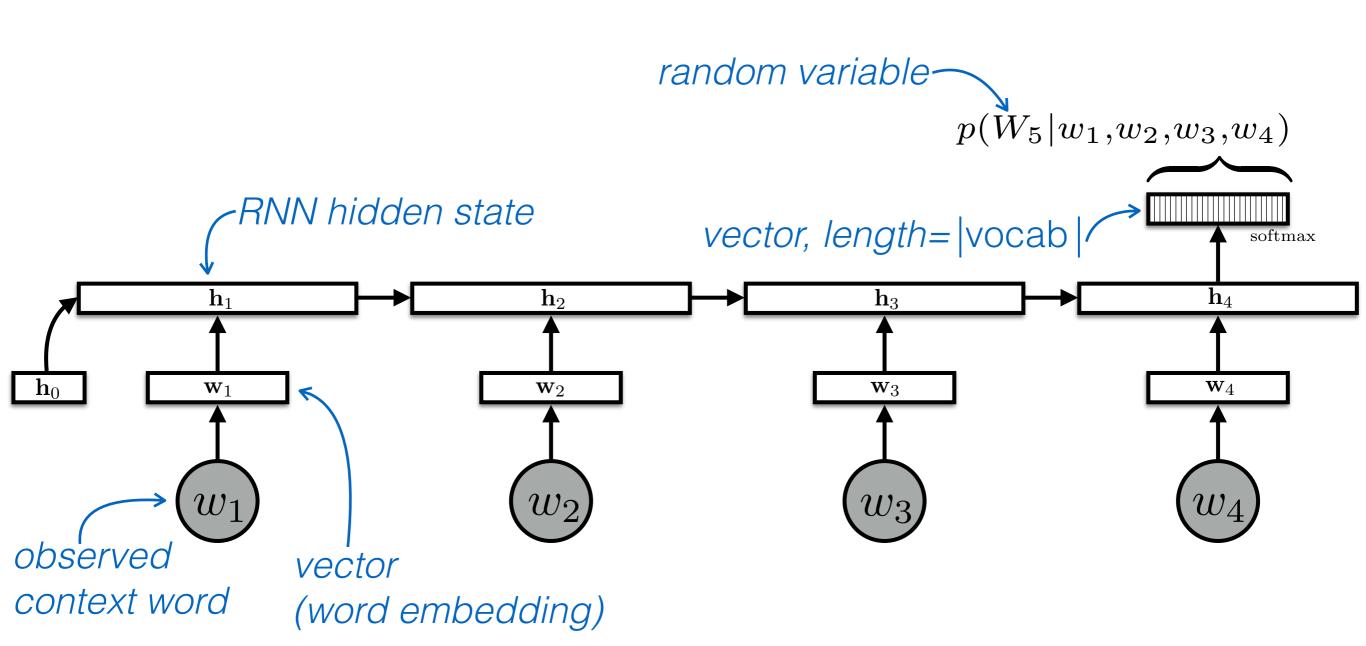
We saw that it is helpful to decompose this probability using the chain rule, as follows:

$$p(\boldsymbol{w}) = p(w_1) \times p(w_2 \mid w_1) \times p(w_3 \mid w_1, w_2) \times \cdots \times p(w_\ell \mid w_1, \dots, w_{\ell-1})$$

$$= \prod_{t=1}^{|\boldsymbol{w}|} p(w_t \mid w_1, \dots, w_{t-1})$$

This reduces the language modeling problem to **modeling** the probability of the next word, given the history of preceding words.

Unconditional LMs with RNNs



A conditional language model assigns probabilities to sequences of words, $\mathbf{w} = (w_1, w_2, \dots, w_\ell)$, given some conditioning context, \mathbf{x} .

As with unconditional models, it is again helpful to use the chain rule to decompose this probability:

$$p(\mathbf{w} \mid \mathbf{x}) = \prod_{t=1}^{\ell} p(w_t \mid \mathbf{x}, w_1, w_2, \dots, w_{t-1})$$

What is the probability of the next word, given the history of previously generated words **and** conditioning context x?

$oldsymbol{x}$ "input"	$oldsymbol{w}$ " text output"
An author	A document written by that author
A topic label	An article about that topic
{SPAM, NOT_SPAM}	An email
A sentence in French	Its English translation
A sentence in English	Its French translation
A sentence in English	Its Chinese translation
An image	A text description of the image
A document	Its summary
A document	Its translation
Meterological measurements	A weather report
Acoustic signal	Transcription of speech
Conversational history + database	Dialogue system response
A question + a document	Its answer
A question + an image	Its answer

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Data for training conditional LMs

To train conditional language models, we need *paired* samples, $\{(\boldsymbol{x}_i, \boldsymbol{w}_i)\}_{i=1}^N$.

Data availability varies. It's easy to think of tasks that could be solved by conditional language models, but the data just doesn't exist.

Relatively large amounts of data for:

Translation, summarisation, caption generation, speech recognition

Algorithmic challenges

We often want to find the most likely \boldsymbol{w} given some \boldsymbol{x} . This is unfortunately generally an *intractable problem*.

$$\boldsymbol{w}^* = \arg\max_{\boldsymbol{w}} p(\boldsymbol{w} \mid \boldsymbol{x})$$

We therefore approximate it using a **beam search** or with Monte Carlo methods since $\mathbf{w}^{(i)} \sim p(\mathbf{w} \mid \mathbf{x})$ is often computationally easy.

Improving search/inference is an open research question.

How can we search more effectively?

Can we get guarantees that we have found the max?

Can we limit the model a bit to make search easier?

Evaluating conditional LMs

How good is our conditional language model?

These are language models, we can use **cross-entropy** or **perplexity**. *okay to implement, hard to interpret*

Task-specific evaluation. Compare the model's most likely output to human-generated expected output using a task-specific evaluation metric L.

$$\boldsymbol{w}^* = \arg \max_{\boldsymbol{w}} p(\boldsymbol{w} \mid \boldsymbol{x}) \qquad L(\boldsymbol{w}^*, \boldsymbol{w}_{ref})$$

Examples of L: BLEU, METEOR, WER, ROUGE. easy to implement, okay to interpret

Human evaluation.

hard to implement, easy to interpret

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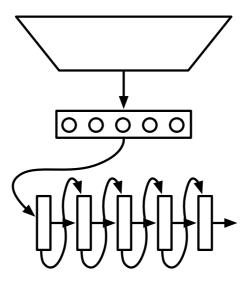
hard to implement, easy to interpret

Lecture overview

 \boldsymbol{w}

The rest of this lecture will look at "encoder-decoder" models that learn a function that maps \boldsymbol{x} into a fixed-size vector and then uses a language model to "decode" that vector into a sequence of words, \boldsymbol{w} .

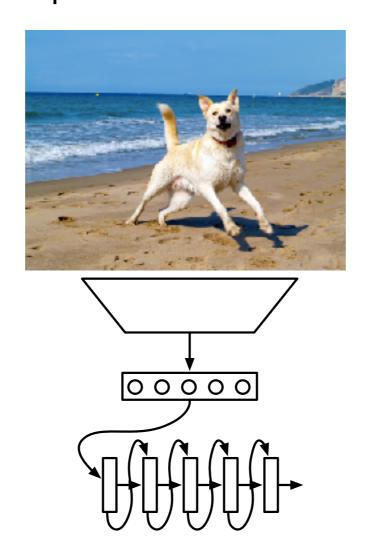
x Kunst kann nicht gelehrt werden...



Artistry can't be taught...

Lecture overview

The rest of this lecture will look at "encoder-decoder" models that learn a function that maps \boldsymbol{x} into a fixed-size vector and then uses a language model to "decode" that vector into a sequence of words, \boldsymbol{w} .



 \boldsymbol{x}

w A dog is playing on the beach.

Lecture overview

- Two questions
 - How do we encode x as a fixed-size vector, c?
 - Problem (or at least modality) specific
 - Think about assumptions
 - How do we condition on c in the decoding model?
 - Less problem specific
 - We will review solution/architectures

Kalchbrenner and Blunsom 2013

Encoder

$$\mathbf{c} = \mathrm{embed}(\boldsymbol{x})$$

$$\mathbf{s} = \mathbf{V}\mathbf{c}$$
Recurrent connection
$$\begin{array}{c} \mathsf{Embedding\ of\ } w_{t-1} \\ \mathsf{Source\ sentence} \\ \mathbf{h}_t = g(\mathbf{W}[\mathbf{h}_{t-1}; \mathbf{w}_{t-1}] + \mathbf{s} + \mathbf{b}]) \\ \mathbf{u}_t = \mathbf{P}\mathbf{h}_t + \mathbf{b}' \quad \mathsf{Learnt\ bias} \end{array}$$

$$p(W_t \mid \boldsymbol{x}, \boldsymbol{w}_{< t}) = \mathrm{softmax}(\mathbf{u}_t)$$

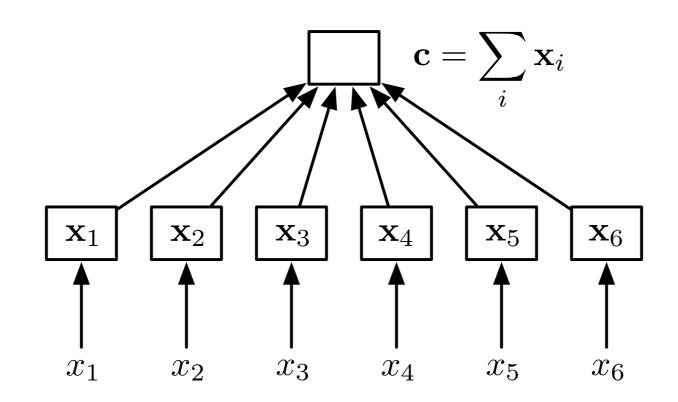
Recall unconditional RNN

$$\mathbf{h}_t = g(\mathbf{W}[\mathbf{h}_{t-1}; \mathbf{w}_{t-1}] + \mathbf{b}])$$

K&B 2013: Encoder

How should we define $\mathbf{c} = \text{embed}(\mathbf{x})$?

The simplest model possible:

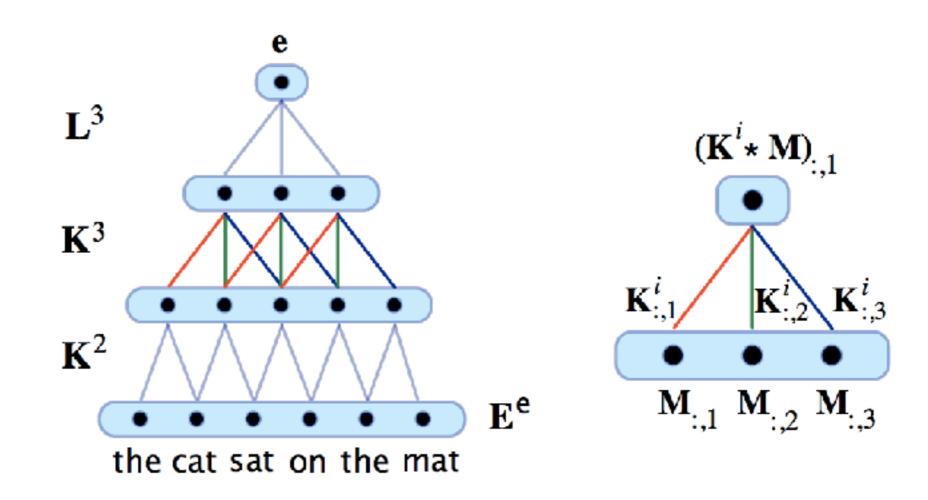


What do you think of this model?

K&B 2013: CSM Encoder

How should we define $\mathbf{c} = \text{embed}(\mathbf{x})$?

Convolutional sentence model (CSM)



K&B 2013: CSM Encoder

Good

- Convolutions learn interactions among features in a local context
- By stacking them, longer range dependencies can be learnt
- Deep ConvNets have a branching structure similar to trees, but no parser is required

Bad

 Sentences have different lengths, need different depth trees; convnets are not usually so dynamic, but see*

^{*} Kalchbrenner et al. (2014). A convolutional neural network for modelling sentences. In Proc. ACL.

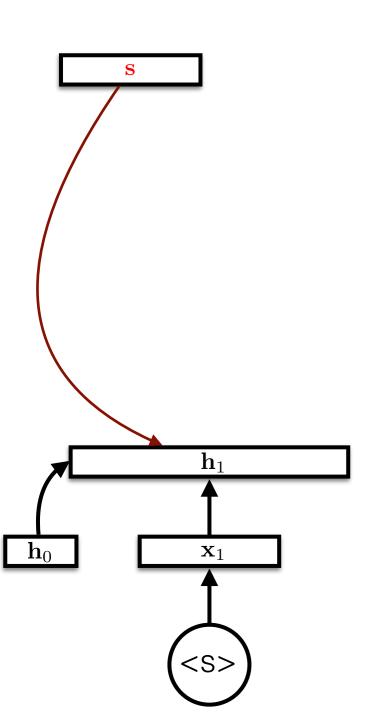
Encoder

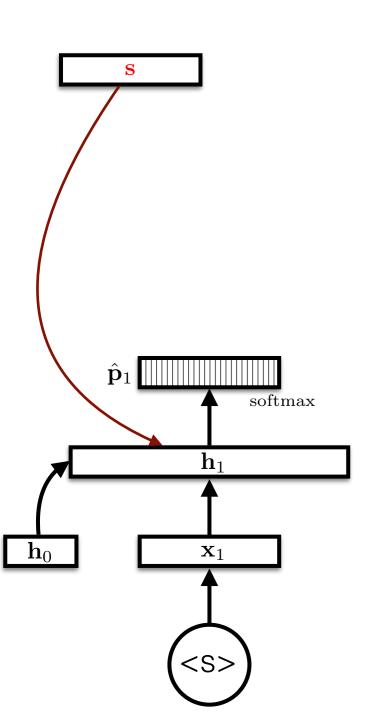
$$\mathbf{c} = \mathrm{embed}(\boldsymbol{x})$$

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Recurrent connection
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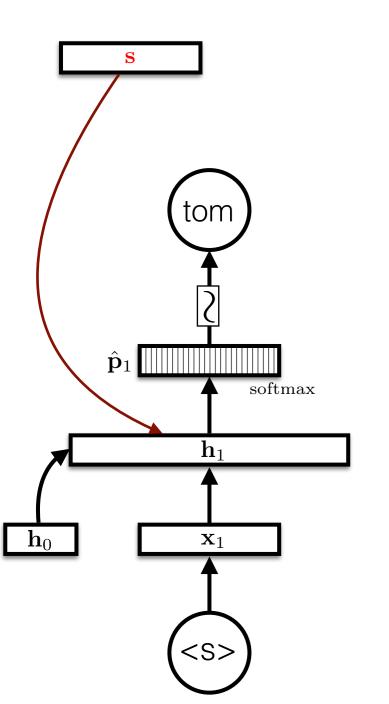
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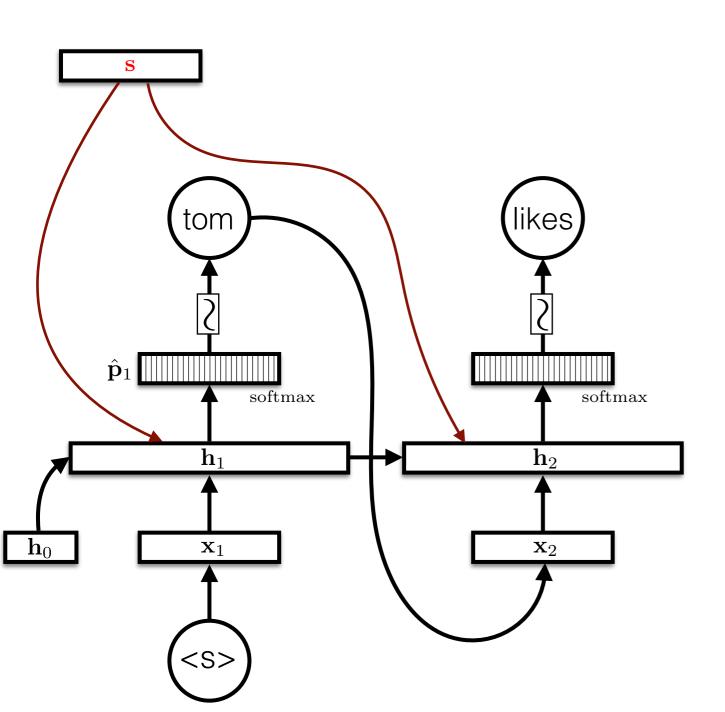




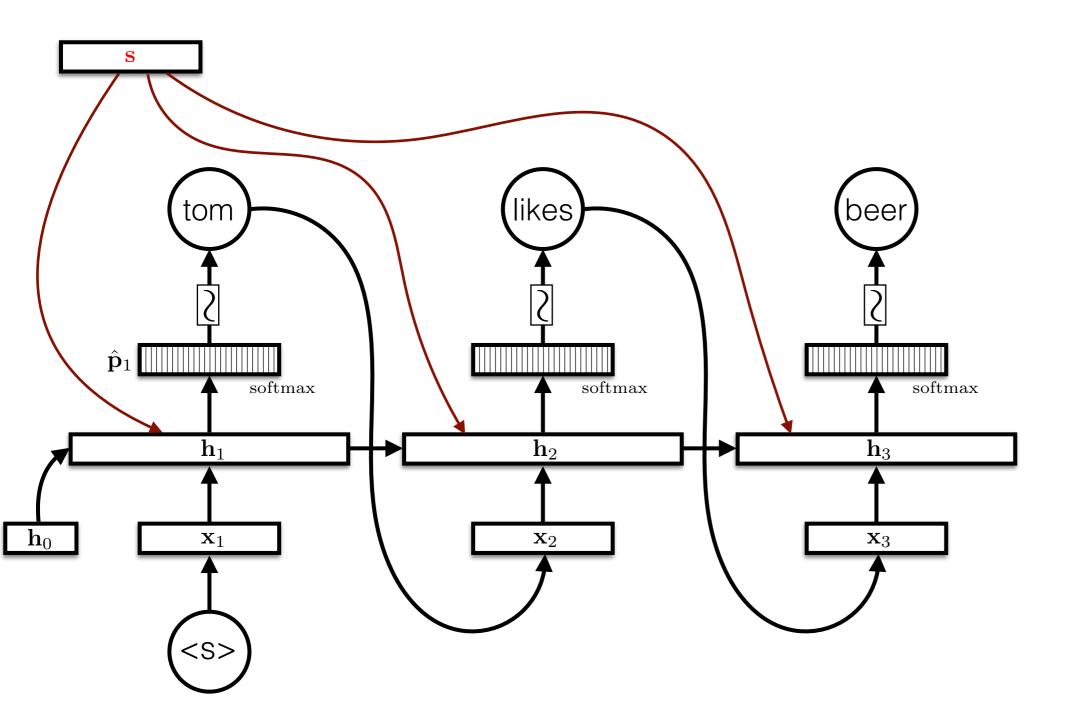
 $p(tom \mid \mathbf{s}, \langle \mathbf{s} \rangle)$



 $p(tom \mid \mathbf{s}, \langle \mathbf{s} \rangle) \times p(likes \mid \mathbf{s}, \langle \mathbf{s} \rangle, tom)$



$$p(tom \mid \mathbf{s}, \langle \mathbf{s} \rangle) \times p(likes \mid \mathbf{s}, \langle \mathbf{s} \rangle, tom) \times p(beer \mid \mathbf{s}, \langle \mathbf{s} \rangle, tom, likes)$$



 $p(tom \mid \mathbf{s}, \langle \mathbf{s} \rangle) \times p(likes \mid \mathbf{s}, \langle \mathbf{s} \rangle, tom)$ $\times p(beer \mid \mathbf{s}, \langle \mathbf{s} \rangle, tom, likes)$ $\times p(\langle \backslash s \rangle \mid s, \langle s \rangle, tom, likes, beer)$ likes </s> beer softmax softmax softmax softmax \mathbf{h}_1 \mathbf{h}_2 \mathbf{h}_4 \mathbf{x}_3 \mathbf{X}_4

LSTM encoder

 $(\mathbf{c}_0, \mathbf{h}_0)$ are parameters

$$(\mathbf{c}_i, \mathbf{h}_i) = \text{LSTM}(\mathbf{x}_i, \mathbf{c}_{i-1}, \mathbf{h}_{i-1})$$

The encoding is $(\mathbf{c}_{\ell}, \mathbf{h}_{\ell})$ where $\ell = |\mathbf{x}|$.

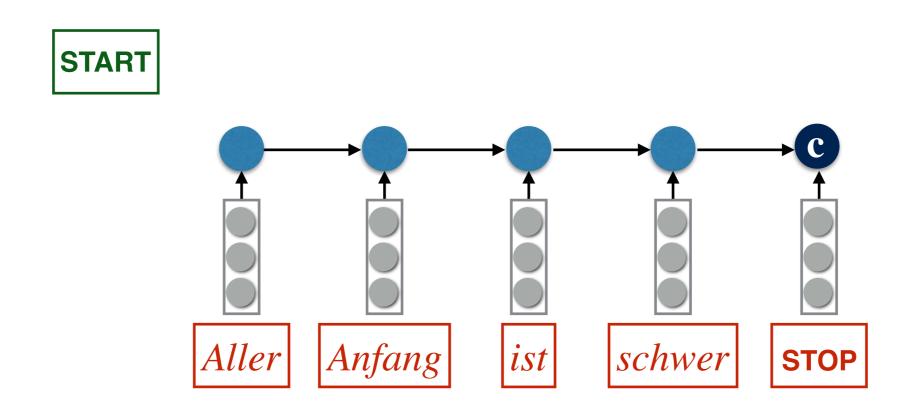
LSTM decoder

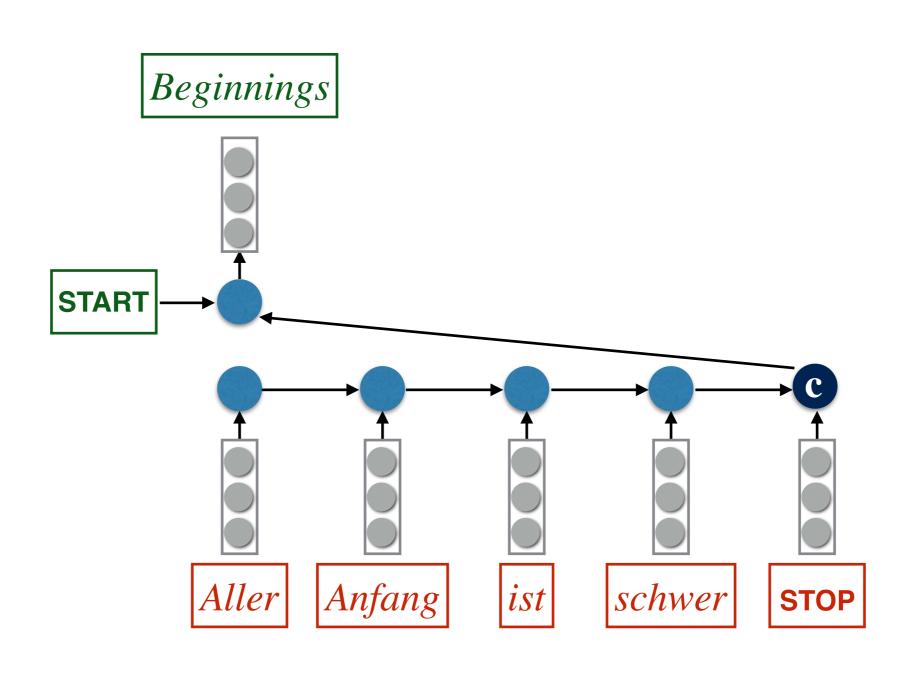
$$w_0 = \langle \mathbf{s} \rangle$$

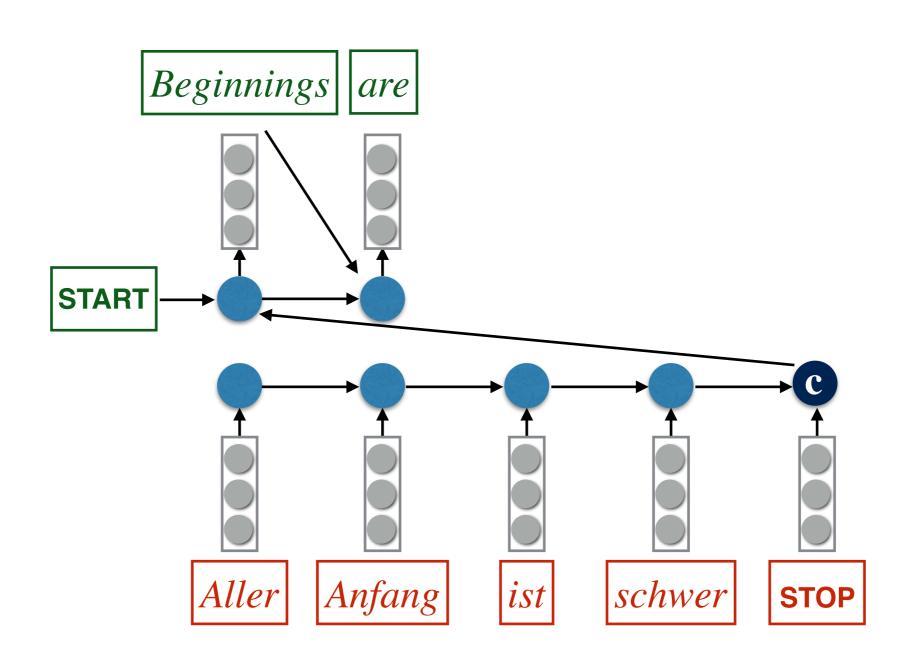
$$(\mathbf{c}_{t+\ell}, \mathbf{h}_{t+\ell}) = \text{LSTM}(w_{t-1}, \mathbf{c}_{t+\ell-1}, \mathbf{h}_{t+\ell-1})$$

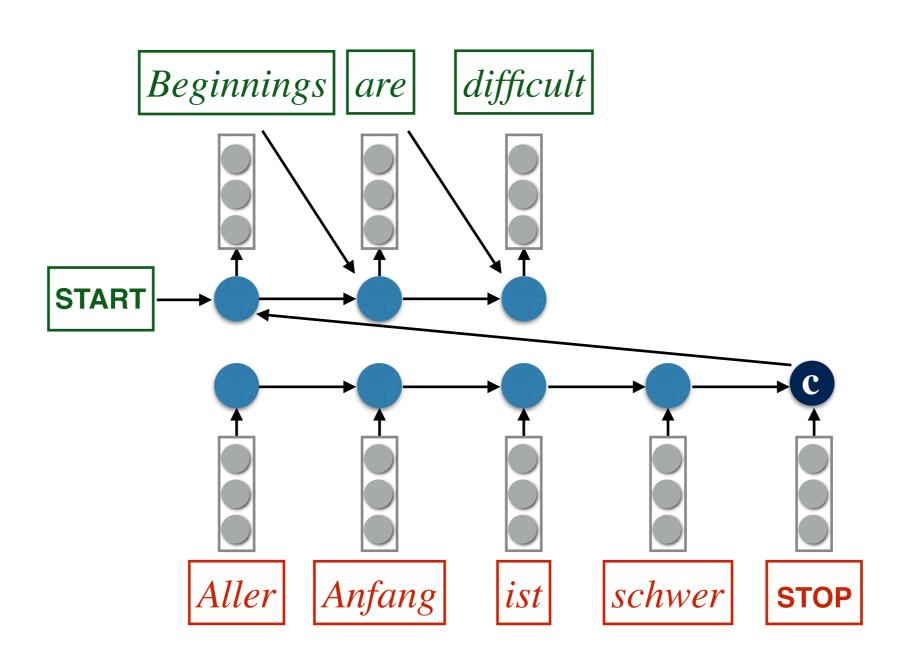
$$\mathbf{u}_t = \mathbf{P}\mathbf{h}_{t+\ell} + \mathbf{b}$$

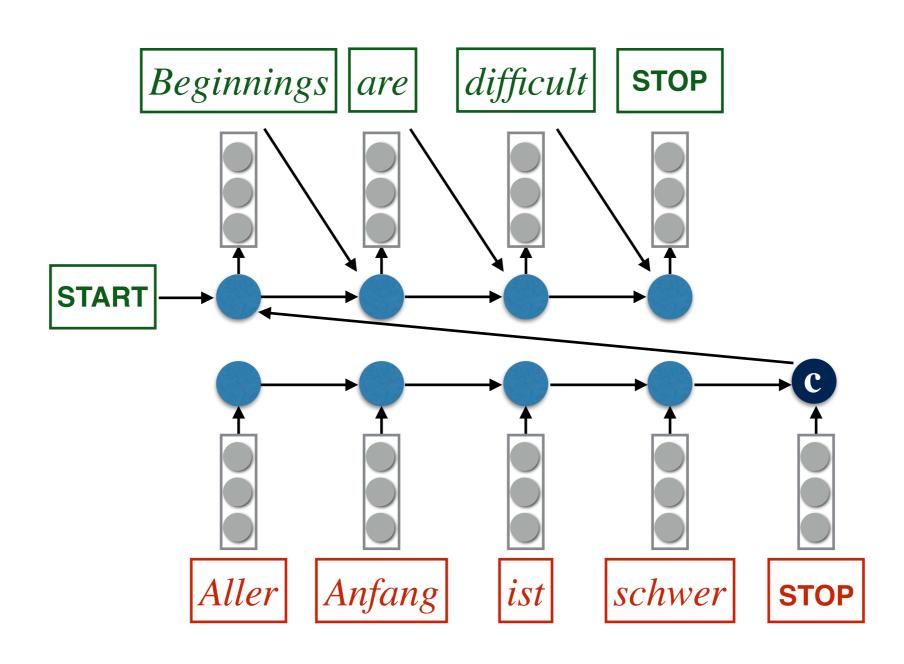
$$p(W_t \mid \mathbf{x}, \mathbf{w}_{< t}) = \text{softmax}(\mathbf{u}_t)$$











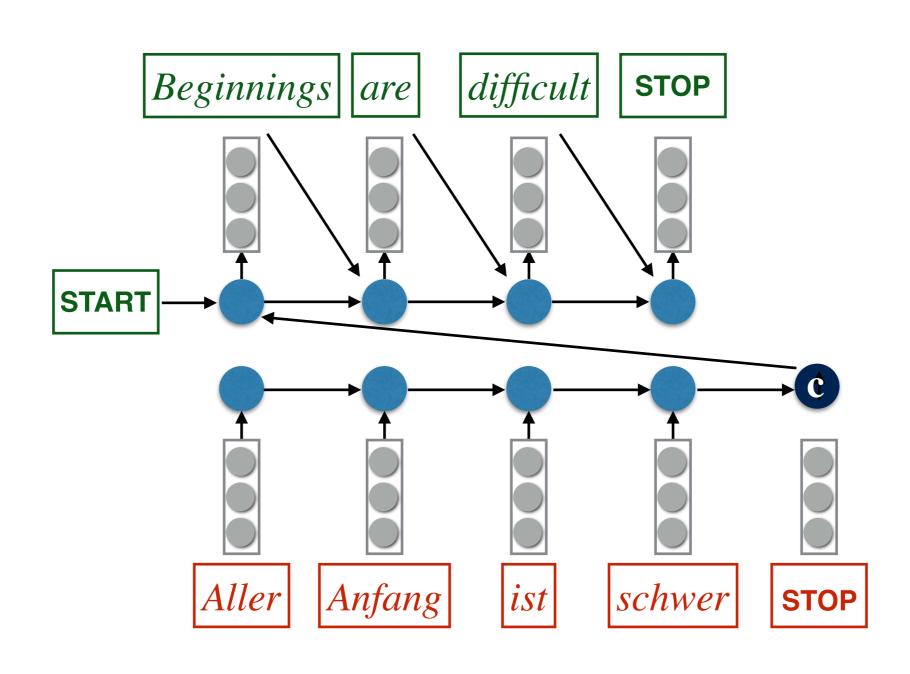
Good

- RNNs deal naturally with sequences of various lengths
- LSTMs in principle can propagate gradients a long distance
- Very simple architecture!

Bad

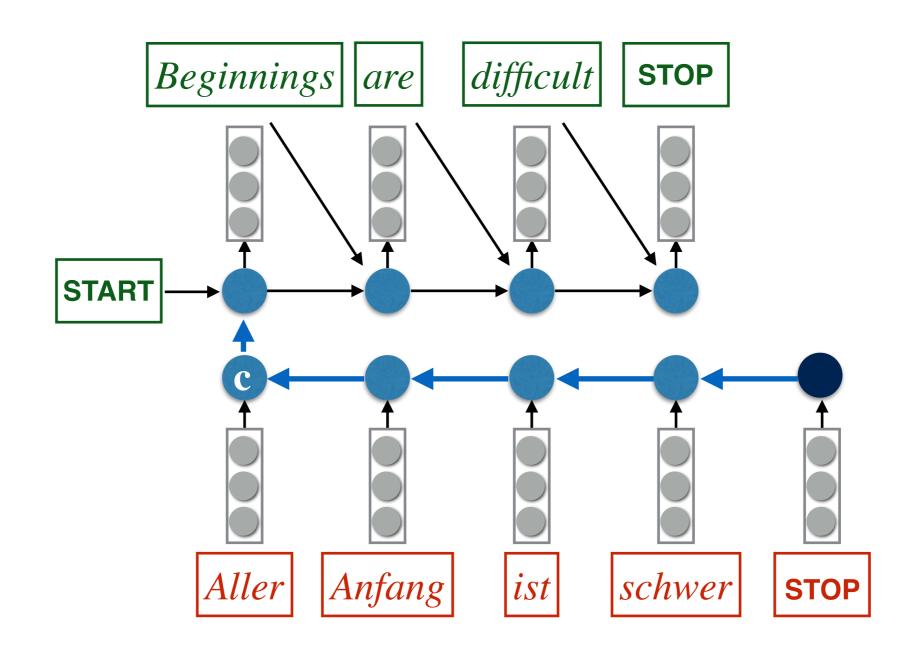
The hidden state has to remember a lot of information!
 (We will return to this problem on Thursday.)

Sutskever et al. (2014): Tricks



Sutskever et al. (2014): Tricks

Read the input sequence "backwards": +4 BLEU



Sutskever et al. (2014): Tricks

Use an ensemble of *J* independently trained models.

Ensemble of 2 models: +3 BLEU

Ensemble of 5 models: +4.5 BLEU

 $p(W_t \mid \boldsymbol{x}, \boldsymbol{w}_{< t}) = \operatorname{softmax}(\mathbf{u}_t)$

Decoder:

$$(\mathbf{c}_{t+\ell}^{(j)}, \mathbf{h}_{t+\ell}^{(j)}) = \text{LSTM}^{(j)}(w_{t-1}, \mathbf{c}_{t+\ell-1}^{(j)}, \mathbf{h}_{t+\ell-1}^{(j)})$$

$$\mathbf{u}_{t}^{(j)} = \mathbf{P}\mathbf{h}_{t}^{(j)} + \mathbf{b}^{(j)}$$

$$\mathbf{u}_{t} = \frac{1}{J} \sum_{j'=1}^{J} \mathbf{u}^{(j')}$$

A word about decoding

In general, we want to find the most probable (MAP) output given the input, i.e.

$$\mathbf{w}^* = \arg \max_{\mathbf{w}} p(\mathbf{w} \mid \mathbf{x})$$

$$= \arg \max_{\mathbf{w}} \sum_{t=1}^{|\mathbf{w}|} \log p(w_t \mid \mathbf{x}, \mathbf{w}_{< t})$$

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This is, for general RNNs, a hard problem. We therefore approximate it with a **greedy search**:

$$w_1^* = \arg \max_{w_1} p(w_1 \mid \boldsymbol{x})$$

$$w_2^* = \arg \max_{w_2} p(w_2 \mid \boldsymbol{x}, w_1^*)$$

$$\vdots$$

$$w_t^* = \arg \max_{w_2} p(w_t \mid \boldsymbol{x}, \boldsymbol{w}_{< t}^*)$$

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undecidable:(
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$$\vdots$$

$$w_t^* = \arg \max_{w_2} p(w_t \mid \boldsymbol{x}, \boldsymbol{w}_{< t}^*)$$

A slightly better approximation is to use a **beam search** with beam size *b*. Key idea: keep track of top b hypothesis.

```
E.g., for b=2:
```

```
x = Bier \ trinke \ ich beer drink I
```

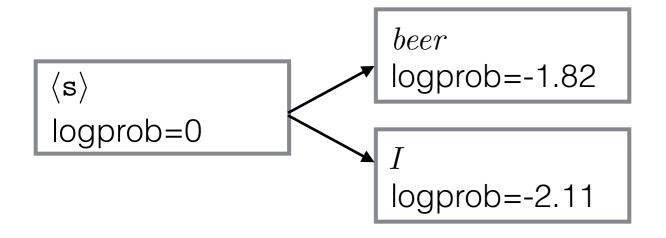
```
(s)
logprob=0
```

 $w_0 \qquad \qquad w_1 \qquad \qquad w_2 \qquad \qquad w_3$

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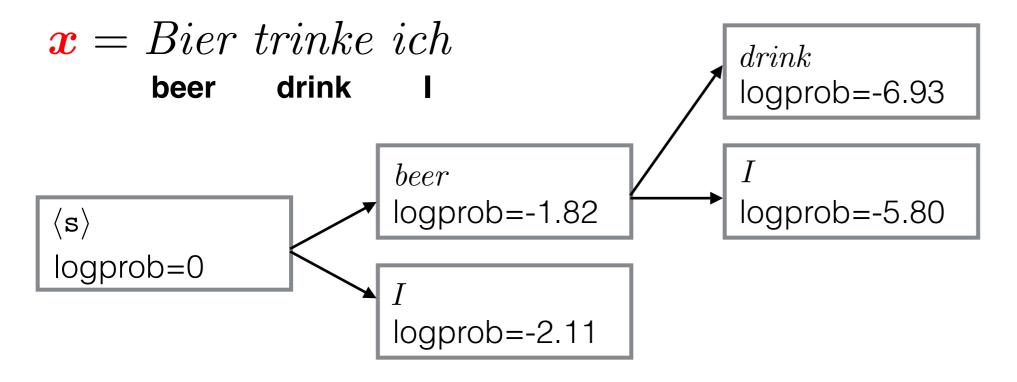
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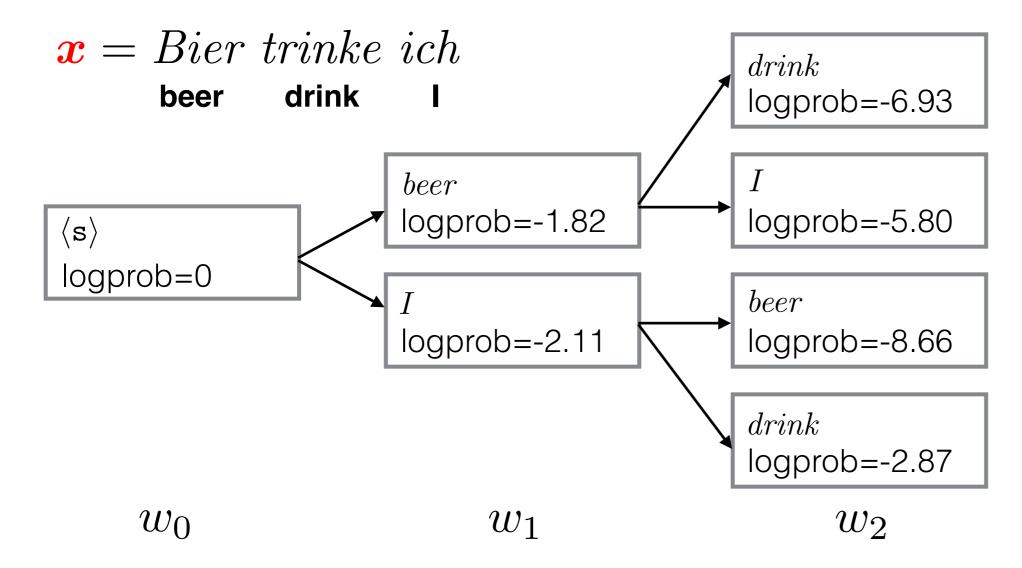
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 $w_0 \qquad \qquad w_1 \qquad \qquad w_2 \qquad \qquad w_3$

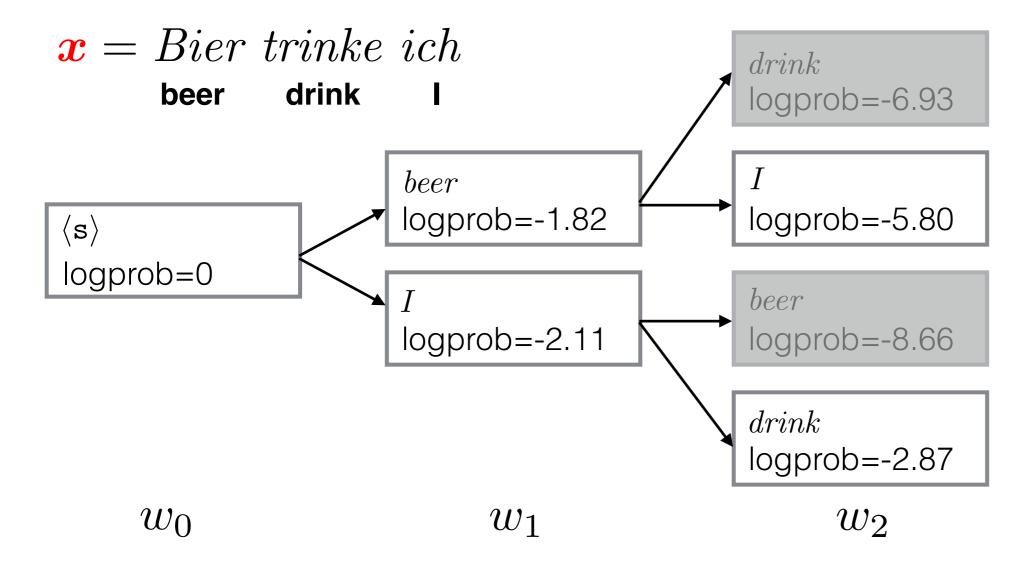
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 W_3

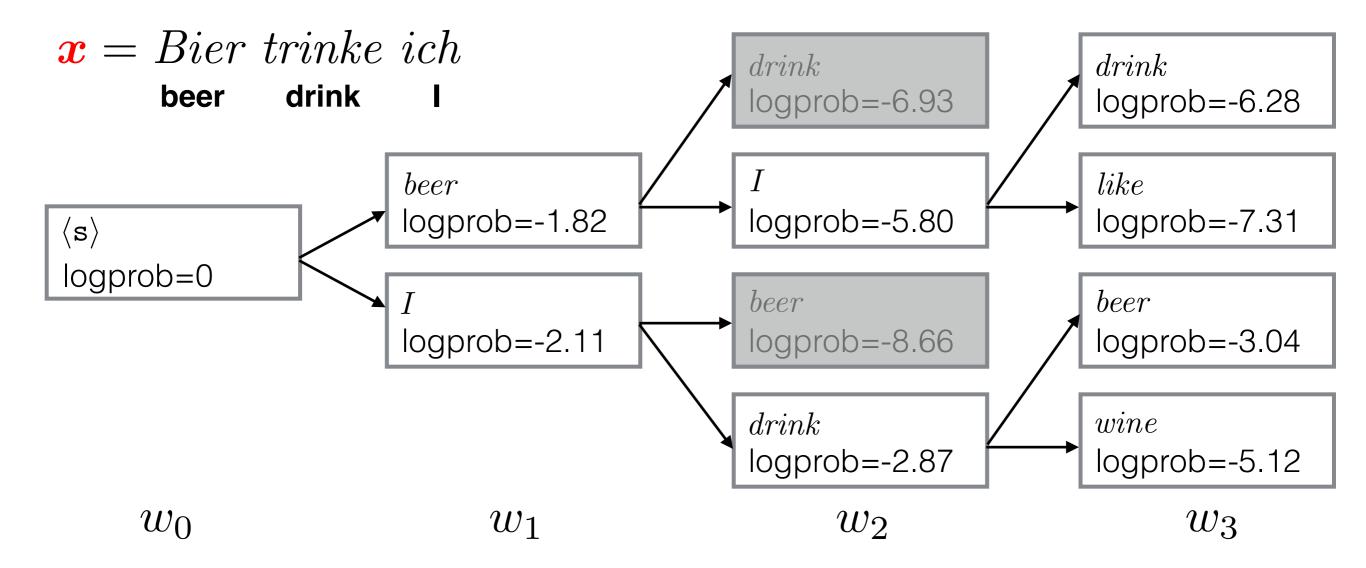


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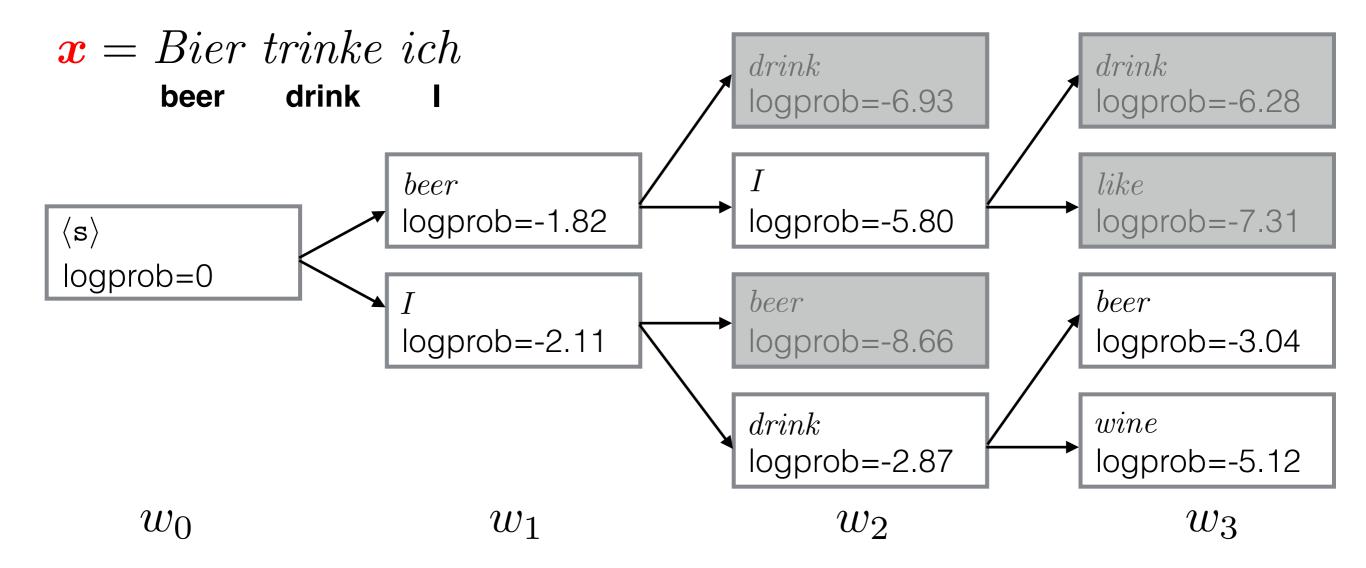
 W_3



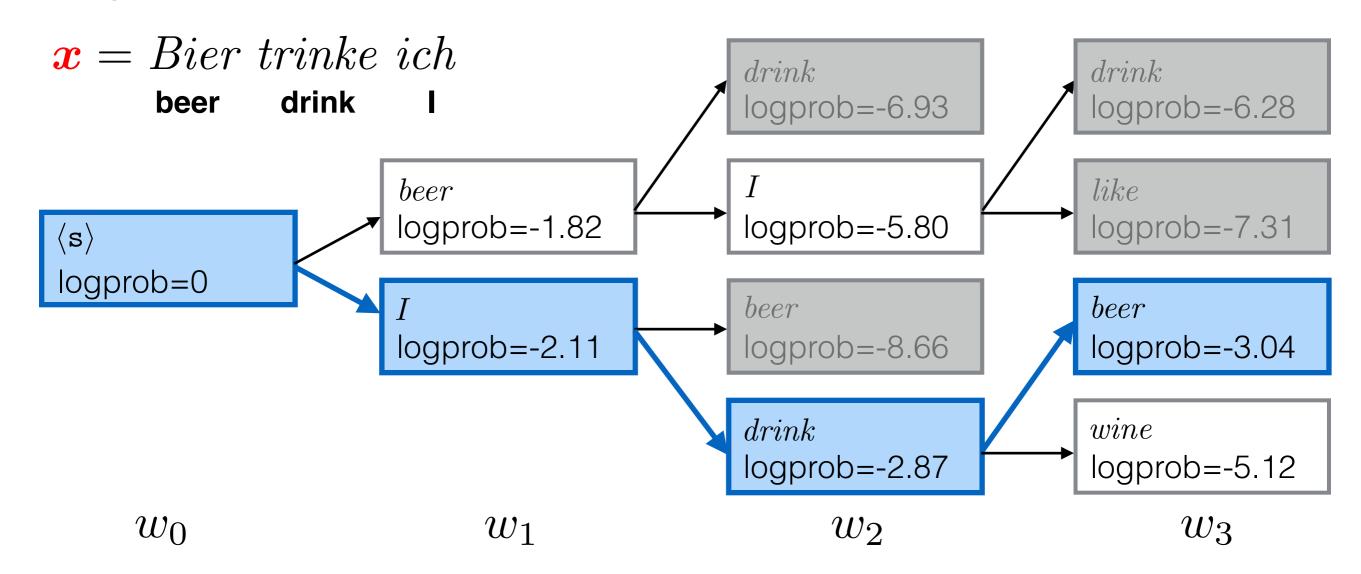
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Sutskever et al. (2014): Tricks

Use beam search: +1 BLEU

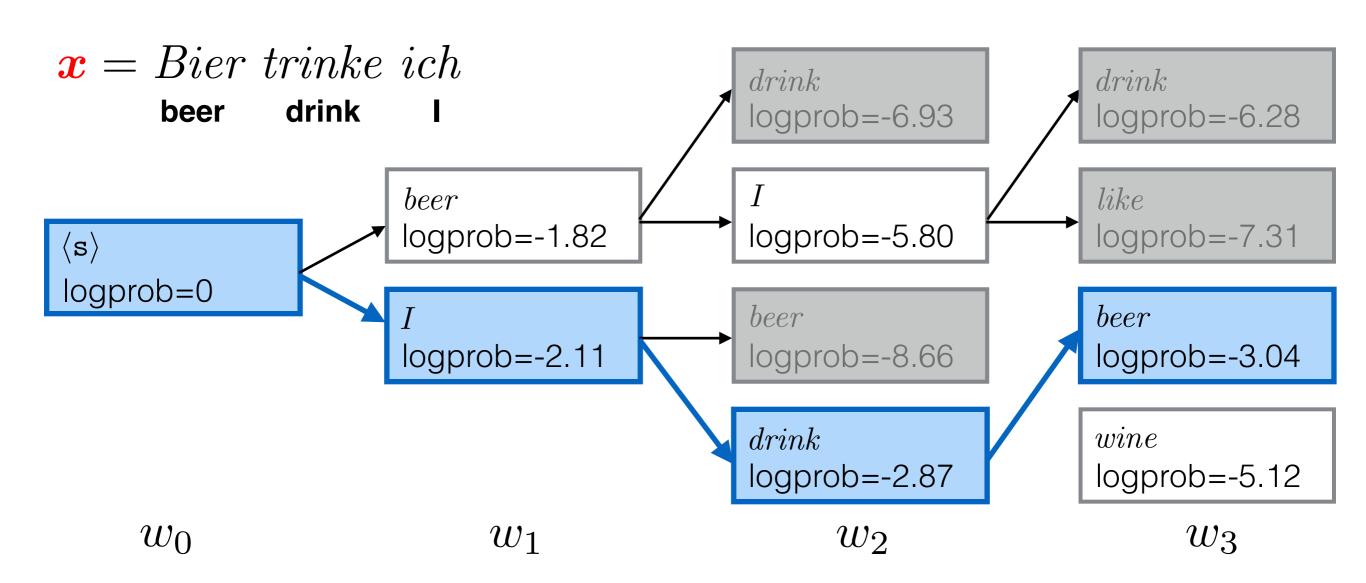


Image caption generation

- Neural networks are great for working with multiple modalities—everything is a vector!
- Image caption generation can therefore use the same techniques as translation modeling
- A word about data
 - Relatively few captioned images are available
 - Pre-train image embedding model using another task, like image identification (e.g., ImageNet)

- Looks a lot like Kalchbrenner and Blunsom (2013)
 - convolutional network on the input
 - n-gram language model on the output
- Innovation: multiplicative interactions in the decoder n-gram model

Encoder $\mathbf{x} = \text{embed}(\mathbf{x})$

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Unconditional *n*-gram LM: Embedding of w_{t-1} , $\mathbf{h}_t = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}]$ $\mathbf{u}_t = \mathbf{P}\mathbf{h}_t + \mathbf{b}$ $p(W_t \mid \mathbf{x}, \mathbf{w}_{t-n+1}^{t-1}) = \operatorname{softmax}(\mathbf{u}_t)$

Encoder $\mathbf{x} = \text{embed}(\mathbf{x})$

Simple conditional *n*-gram LM:

$$\mathbf{h}_t = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}] + \mathbf{C}\mathbf{x}$$
 $\mathbf{u}_t = \mathbf{P}\mathbf{h}_t + \mathbf{b}$

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$$w_i = r_{i,j,w} x_j$$

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$$p(W_t \mid \boldsymbol{x}, \boldsymbol{w}_{t-n+1}^{t-1}) = \operatorname{softmax}(\mathbf{u}_t)$$

$$w_i = r_{i,w}$$
 how big is this tensor? $w_i = r_{i,j,w} x_j$

Encoder $\mathbf{x} = \text{embed}(\mathbf{x})$

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Multiplicative *n*-gram LM:

$$w_i = r_{i,w}$$

$$w_i = r_{i,j,w} x_j$$

what's the intuition here?

Encoder $\mathbf{x} = \text{embed}(\mathbf{x})$

Simple conditional *n*-gram LM:

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$$\mathbf{h}_t = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}] + \mathbf{C}\mathbf{x}$$
$$\mathbf{u}_t = \mathbf{P}\mathbf{h}_t + \mathbf{b}$$

$$p(W_t \mid \boldsymbol{x}, \boldsymbol{w}_{t-n+1}^{t-1}) = \operatorname{softmax}(\mathbf{u}_t)$$

$$w_i = r_{i,w}$$

$$w_i = r_{i,j,w} x_j$$

$$w_i = u_{w,i} v_{i,j} \quad (\mathbf{U} \in \mathbb{R}^{|V| \times d}, \quad \mathbf{V} \in \mathbb{R}^{d \times k})$$

$$\mathbf{r}_t = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}] + \mathbf{C}\mathbf{x}$$

Encoder $\mathbf{x} = \text{embed}(\mathbf{x})$

Simple conditional *n*-gram LM:

$$\mathbf{h}_t = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}] + \mathbf{C}\mathbf{x}$$
 $\mathbf{u}_t = \mathbf{P}\mathbf{h}_t + \mathbf{b}$

$$p(W_t \mid \boldsymbol{x}, \boldsymbol{w}_{t-n+1}^{t-1}) = \operatorname{softmax}(\mathbf{u}_t)$$

$$w_{i} = u_{w,i}v_{i,j} \qquad (\mathbf{U} \in \mathbb{R}^{|V| \times d}, \quad \mathbf{V} \in \mathbb{R}^{d \times k})$$

$$\mathbf{r}_{t} = \mathbf{W}[\mathbf{w}_{t-n+1}; \mathbf{w}_{t-n+2}; \dots; \mathbf{w}_{t-1}] + \mathbf{C}\mathbf{x}$$

$$\mathbf{h}_{t} = (\mathbf{W}^{fr}\mathbf{r}_{t}) \odot (\mathbf{W}^{fx}\mathbf{x})$$

$$\mathbf{u}_{t} = \mathbf{P}\mathbf{h}_{t} + \mathbf{b}$$

$$p(W_{t} \mid \mathbf{x}, \mathbf{w}_{< t}) = \operatorname{softmax}(\mathbf{u}_{t})$$

- Two take-home messages:
 - Feed-forward n-gram models can be used in place of RNNs in conditional models
 - Modeling interactions between input modalities holds a lot of promise
 - Although MLP-type models can approximate higher order tensors, multiplicative models appear to make learning interactions easier

Questions?