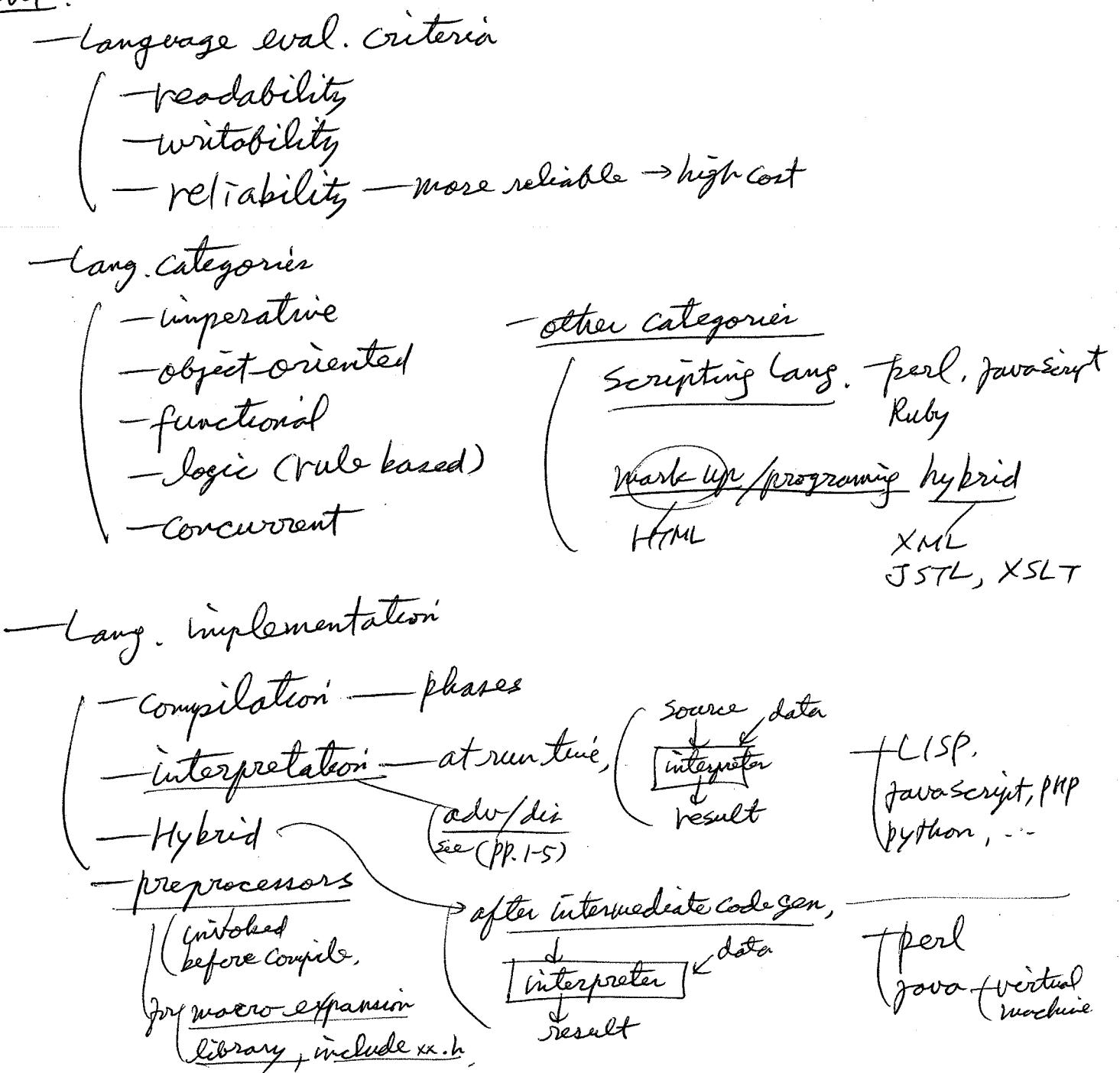


## review for Exam

### Ch1.



### Ch2 - skip

### Ch3 - Syntax & Semantics

## — token / lexeme

Token / Lexeme

```

graph TD
    Token[Token / Lexeme] --> Index[Index]
    Token --> Lexemes[Lexemes]
    Index --> id1[id]
    Index --> plusOp1[plus op]
    Index --> multOp1[mult op]
    Lexemes --> intLiteral1[int-literal]
    Lexemes --> tokens[tokens]
    tokens --> id2[id]
    tokens --> plusOp2[plus op]
    tokens --> multOp2[mult op]
    tokens --> intLiteral2[int-literal]
  
```

4)  $\text{Index} = 2 \times \text{Count} + 17;$

lexemes actual  
instance  
(value)

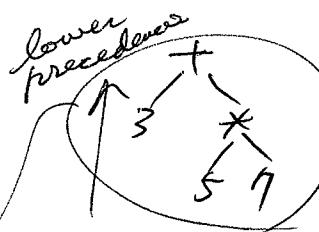
## expression notation

```

graph TD
    Infix["Infix - 3 + 5 * 7"] --> Prefix["prefix - +3*5 7"]
    Infix --> Postfix["postfix - 3 5 7 * +"]
    Infix --> AST["AST - "]

```

Can use (1)

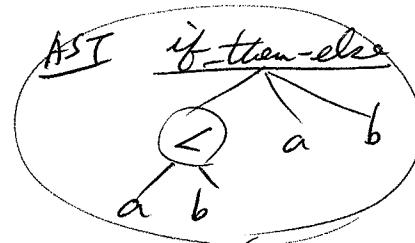


parse tree  
Should resemble AST

mixfix -> if  $a < b$  then  $a$  else  $b$

+ precedence — lower prec. high

associativity  $\left[ \begin{array}{l} \text{left-assoc.} \rightarrow \underline{\text{left-rec G}} \\ \text{right-assoc.} \rightarrow \underline{\text{right-rec G}} \end{array} \right]$



- GFG = (V, T, P, S)

— parse tree — G and String (AST — string only)

derivation - rightmost

all terminals /

## Syntactic ambiguity

$$g) E \rightarrow E-E$$

10/11--19

Strij 2-4-5

→ multiple parse tree (or derivations)

8)  $E \rightarrow E+F | E-T | T$   
 $T \rightarrow T \times F | T/F | F$   
 9)  $F \rightarrow \text{Num}$   
 $\text{Num} \rightarrow 0/1/-19$

3

Writing unambiguous G

- keep precedence
  - reflect associativity

$$e \rightarrow e - e'$$

E1 → 01.1--19

~~left-also~~ → left-red

right assoc.  $\rightarrow$  right rec.

4) A power.

Conversion of left-rec G  $\rightarrow$  right-rec G without violating the associativity of operation.

$$A \rightarrow A\alpha/B \Rightarrow \begin{cases} A \rightarrow BA' \\ A' \rightarrow \alpha A'/\epsilon \end{cases} \quad \text{2 prod. case.}$$

$$4) E \rightarrow E + T | T \xrightarrow{\alpha'} \beta' \Rightarrow [E \xrightarrow{\beta} T E' | E' \xrightarrow{\alpha} + T E' | E]$$

— from prog. assignments

include (1) and (2) to the expr G.

— dangling else ambiguity

Solutions f1. if ---- end — Module-2, Ada

2. Compiler matches else to the worstest if - C/C++

3. Java way — separate products for

if state, if else state.

## — BNF / eBNF / Syntax chart

( ) - group  
 { } - for more  
 [ ] - optional

i chart for 1 non T.

$\text{BNF} \rightarrow \text{EBNF}$

2) 2 products ← optional [ ]  
BNF :                   EBNF :

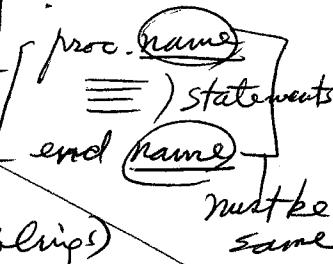
## Semantics

### attribute grammar

### CFG + static semantics

ex) type checking

e.g. Ada



~~for each Syntax rule~~ — production —  
→  $\langle \text{Assign} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

~~predicate (semantic rule)~~ —  
→  $\langle \text{expr} \rangle . \underbrace{\text{expected type}}_{\substack{\text{inherited} \\ \text{synthesiz.}}}$

Static Semantics  
Checking at  
Compilation

dynamic semantics — describing meaning of constructs.

### State of a program

$\sigma$  — set of  $\langle V, \text{val} \rangle$

$\sigma = \{ \langle v_1, \text{val}_1 \rangle, \langle v_2, \text{val}_2 \rangle, \dots \}$

System state

operational semantics — state change defines the meaning  
of the statement

### Axiomatic

based on formal logic (predicate calculus)  
formal verification

## Operational semantics

### Addition operation

$$\boxed{\frac{\Gamma(e_1) \Rightarrow v_1, \Gamma(e_2) \Rightarrow v_2}{\Gamma(e_1 + e_2) \Rightarrow v_1 + v_2}}$$

### Assignment st ( $s.\text{target} = s.\text{source}$ )

$$\boxed{\frac{\Gamma(s.\text{source}) \Rightarrow v}{\Gamma(s.\text{target} = s.\text{source};) \Rightarrow \Gamma \cup \{s.\text{target}, v\}}}$$

Ex)  $\Gamma = \{ \dots, \langle x, 3 \rangle, \dots \}$   
 $\underline{x=5;}$   
 $\Gamma' = \Gamma \cup \{ \langle x, 5 \rangle \} \Rightarrow \underline{\{ \dots, \langle x, 5 \rangle, \dots \}}.$

### Sequence of statements ( $s_1; s_2$ )

### Conditionals ( $\text{if } (s.\text{test}) \text{ then part else } s.\text{else part}$ )

[ true case      ) rules  
 false case ]

### Loops

[ True case      ) rules  
 false case ]

Ex)  $\Gamma = \{ \dots, \langle x, 7 \rangle, \dots \}$

[ while ( $x < 100$ )  
 $x = 2 * x;$

$\Rightarrow$  what is the final state  $\Gamma'$ ?

✓

## Axiomatic Semantics

precond / post cond.

partial correctness proof rules

Composition rule

$$\boxed{\begin{array}{c} \Sigma p_3 S_1 \Sigma Q_3, \Sigma Q_3 S_2 \Sigma R_3 \\ \hline \Sigma p_3 \underline{S_1; S_2} \Sigma R_3 \end{array}} \quad \begin{array}{l} \text{premise} \\ \text{conclusion} \end{array}$$

Conditional rule

$$\boxed{\begin{array}{c} \Sigma p_1 E_3 S_1 \Sigma Q_3, \Sigma p_1 \top E_3 S_2 \Sigma Q_3 \\ \hline \Sigma p_3 \text{ if } E \text{ then } S_1 \text{ else } S_2 \Sigma Q_3 \end{array}}$$

while rule

$$\boxed{\begin{array}{c} \Sigma p_1 E_3 S \Sigma p_3 \\ \hline \Sigma p_3 \text{ while } E \text{ do } S \Sigma p_1 \top E_3 \end{array}}$$

Assignment Axiom

$$\boxed{\begin{array}{c} \text{True} \\ \hline \Sigma Q [\text{target/source}] \Sigma S \Sigma Q_3 \end{array}}$$

rule of consequence

Ex 1

↑

Type systems and Semantics — partly from Ch.6  
exclude — type checking functions ...