P8131 HW5

Brian Jo Hsuan Lee

3/15/2022

Load packages

```
library(tidyverse)
library(pscl)
```

Problem 1: Crab Satellite Count

Import and tidy data

```
# txt file read in using read_delim(), separated grouped values, and corrected column types
crab_data =
    read_delim("HW5-crab.txt", delim = "\t") %>%
    mutate(
        number = str_trim(number, side = c("both"))
      ) %>%
      separate(number, c("number", "C", "S", "W", "Wt", "Sa"), sep = " +") %>%
      mutate(
        across(where(is.character), as.numeric)
      )
```

a) Fit a simple Poisson model, check the goodness of fit and interpret the model

```
# m1 model fit
crab_m1 = glm(Sa ~ W, family = poisson, data = crab_data)
summary(crab_m1)
```

```
##
## Call:
## glm(formula = Sa ~ W, family = poisson, data = crab_data)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -2.8526 -1.9884 -0.4933
                             1.0970
                                       4.9221
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.30476
                          0.54224 -6.095 1.1e-09 ***
               0.16405
                          0.01997
                                    8.216 < 2e-16 ***
## W
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
```

[1] "Reject the null with significant data suggesting the poisson fit is not good"

Fit M1 shows the log count of a female horseshoe crab's satellite increases by 0.164 per unit increase of its carapace width. The coefficient for carapace width is significant at p-value < 2e-16, despite the simple poisson model does not provide a good fit to the data.

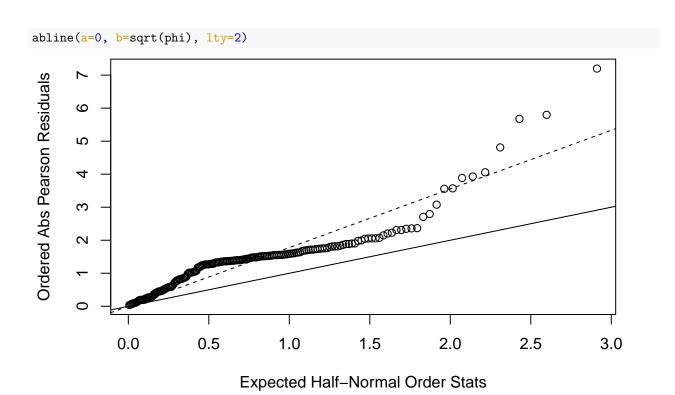
b) Fit a Poisson model with 2 predictors, compare it with the previous model and interpret it

```
# m2 model fit
crab_m2 = glm(Sa ~ W + Wt, family = poisson, data = crab_data)
summary(crab m2)
##
## Call:
## glm(formula = Sa ~ W + Wt, family = poisson, data = crab_data)
##
## Deviance Residuals:
                     Median
      Min
                 1Q
                                   3Q
                                           Max
  -2.9308 -1.9705 -0.5481
                               0.9700
##
                                        4.9905
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
                                   -1.436 0.15091
## (Intercept) -1.29168
                           0.89929
## W
                0.04590
                           0.04677
                                     0.981
                                           0.32640
                0.44744
                                     2.820 0.00479 **
## Wt
                           0.15864
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 632.79 on 172 degrees of freedom
## Residual deviance: 559.89 on 170 degrees of freedom
## AIC: 921.18
##
## Number of Fisher Scoring iterations: 6
```

Fit M2 shows the log count of a female horseshoe crab's satellite increases by 0.0459 per unit increase of its carapace width while adjusting for its weight, and it increases by 0.447 per unit increase of its weight, holding carapace width fixed. Only the weight predictor is significant.

```
# use chisq test and evaluate the nested models m1 and m2,
# with df = 171 m1 predictors - 170 m2 predictors = 1
m1_m2_stat = crab_m1$deviance - crab_m2$deviance
m1_m2_pval = 1 - pchisq(m1_m2_stat, df = 171-170)
ifelse(m1_m2_pval > 0.05,
       'Failed to reject the null, since no significant evidence suggest the larger model has a better
       'Reject the null with significant evidence suggesting the larger model fits the data better')
## [1] "Reject the null with significant evidence suggesting the larger model fits the data better"
Per the results of the deviance analysis, M2 has a significantly better fit and is preferred to M1. Likewise, M2
also has a lower AIC than M1, suggesting its better fit.
  c) Estimate overdispersion and interpret under the assumption of overdispersion
# obtain dispersion paramater using m3's pearson's chisq residual
# with df = 173 observations - 3 predictors = 170
crab_m2_pchisq = sum(residuals(crab_m2, 'pearson')^2)
phi = crab_m2_pchisq/170; phi
## [1] 3.156449
# the following code yields a similar phi estimate
## alt_phi = crab_m2$deviance/crab_m2$df.residual; alt_phi
For count models, overdispersion occurs when Var[X] > E[X] = \lambda, and it is shown with \phi = 3.16 > 1.
summary(crab m2, dispersion = phi)
##
## Call:
## glm(formula = Sa ~ W + Wt, family = poisson, data = crab_data)
##
## Deviance Residuals:
                      Median
##
       Min
                 1Q
                                    3Q
                                            Max
## -2.9308 -1.9705 -0.5481
                                0.9700
                                         4.9905
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -1.29168
                            1.59771 -0.808
                                               0.419
                                                0.581
## W
                0.04590
                            0.08309
                                      0.552
## Wt
                0.44744
                            0.28184
                                      1.588
                                               0.112
##
## (Dispersion parameter for poisson family taken to be 3.156449)
##
##
       Null deviance: 632.79 on 172 degrees of freedom
## Residual deviance: 559.89 on 170 degrees of freedom
## AIC: 921.18
##
## Number of Fisher Scoring iterations: 6
res = residuals(crab_m2, type='pearson')
plot(qnorm((173+1:173+0.5)/(2*173+1.125)),
     sort(abs(res)),
     xlab='Expected Half-Normal Order Stats',
     ylab='Ordered Abs Pearson Residuals')
```

abline(a=0, b=1)



The estimated intercept and coefficients for the new fit are equivalent to those of the original fit, as shown in the summaries, and therefore have the same interpretation as for the original fit. The half-normal plot visualizes $\phi > 1$ by displaying the data deviance (linear regression as the dashed line) from the solid x = y reference line in a $\phi^{-1}(\frac{n+i+0.5}{2n+1.125})$ vs $|r_{(i)}|$ plot, where r is Pearson's residuals.

Problem 2: Fish Parasite Count

```
# txt file read in using read_delim() and dropped 'NA' rows and o 'omit' columns
para_data =
    read_delim("HW5-parasite.txt", delim = "\t") %>%
    select(c('Intensity', 'Year', 'Length', 'Area')) %>%
    mutate(
        Year = factor(Year),
        Area = factor(Area)
) %>%
    drop_na()
```

a) Fit a simple Poisson model, check the goodness of fit and interpret the model

```
# m1 model fit
para_m1 = glm(Intensity ~ Year + Area + Length, family = poisson, data = para_data)
summary(para_m1)

##
## Call:
## glm(formula = Intensity ~ Year + Area + Length, family = poisson,
## data = para_data)
##
## Deviance Residuals:
## Min 1Q Median 3Q Max
```

```
## -9.3632 -2.7158 -2.0142 -0.4731 30.2492
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                2.6431709
                          0.0542838
                                     48.692
                                              < 2e-16 ***
                                      23.954
## Year2000
                0.6702801
                           0.0279823
                                              < 2e-16 ***
## Year2001
               -0.2181393
                           0.0287535
                                      -7.587 3.29e-14 ***
## Area2
               -0.2119557
                           0.0491691
                                      -4.311 1.63e-05 ***
## Area3
               -0.1168602
                           0.0428296
                                      -2.728
                                              0.00636 **
## Area4
                1.4049366
                           0.0356625
                                      39.395
                                              < 2e-16 ***
## Length
               -0.0284228
                           0.0008809 -32.265
                                              < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 25797
                             on 1190
                                      degrees of freedom
## Residual deviance: 19153
                             on 1184
                                      degrees of freedom
## AIC: 21089
##
## Number of Fisher Scoring iterations: 7
```

The fit shows the log count of parasites is 2.64 in year 1999, in area 1 and at fish length 0. The count increases by $e^{0.670}=1.95$ times of year 1999 in 2000, but is $e^{-0.218}=0.804$ times of year 1999 in 2001 while adjusting for area and body length; the count response is $e^{-0.212}=.809$ and $e^{-0.117}=0.890$ times of area 1 in area 2 and area 3, respectively, and $e^{-0.140}=4.06$ times area 1 in area 4 while adjusting for year and body length; the count increases by $1-e^{0.0284}=0.03$ in percentage per unit increase in length while adjusting for year and area. The predictors, including the intercept and all coefficients, are significant at $\alpha=0.05$.

b) Goodness of fit and conclusions

[1] "Reject the null with significant data suggesting the poisson fit is not good"

Though the coefficients are significant, it is a poor fitting model for the data. We may speculate the issue to be that the data actually falls in a zero-inflated, zero-truncated, or multi-modal poisson distribution, and question if the overdispersion parameter equals 1.

c) Fit a zero-inflated poisson model and interpret it

```
# m2 model fit
para_m2 = zeroinfl(Intensity ~ Year + Area + Length, data = para_data)
summary(para_m2)
##
## Call:
## zeroinfl(formula = Intensity ~ Year + Area + Length, data = para_data)
##
```

```
## Pearson residuals:
##
      Min
              1Q Median
                            30
                                   Max
## -2.1278 -0.8265 -0.5829 -0.1821 25.4837
## Count model coefficients (poisson with log link):
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.8431720 0.0583793 65.831 < 2e-16 ***
             ## Year2000
## Year2001
             -0.0448457 0.0296057 -1.515 0.129831
## Area2
             0.2687838 0.0500467
                                 5.371 7.84e-08 ***
## Area3
             0.1463174 0.0439485
                                   3.329 0.000871 ***
             0.9448070 0.0368342 25.650 < 2e-16 ***
## Area4
             -0.0368067  0.0009747  -37.762  < 2e-16 ***
## Length
##
## Zero-inflation model coefficients (binomial with logit link):
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.552579
                       0.275762
                                2.004 0.04509 *
## Year2000
             -0.752121
                        0.172965 -4.348 1.37e-05 ***
## Year2001
              0.456533
                       0.143962 3.171 0.00152 **
                                3.791 0.00015 ***
## Area2
              0.718680
                       0.189552
## Area3
             ## Area4
             -1.022864
                        0.188201 -5.435 5.48e-08 ***
                        0.004629 -2.136 0.03266 *
## Length
             -0.009889
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Number of iterations in BFGS optimization: 17
## Log-likelihood: -6950 on 14 Df
```