

cat | printf "%d\n" 79

lv 4

Min

79

cat | printf "Max"

Max

cat | printf "%d\n" 49

lv 3

Min

49

79

cat | printf "Max"

Max

cat | printf "%d\n" 12

lv 2

Min

12

23

49

79

cat | printf "Max"

Max

cat | printf "%d\n" 12

lv 1

Min

12

23

49

79

98

cat | printf "Max"

Max

cat | printf "%d\n" 11

lv 0

Min

11

12

23

45

49

71

79

98

cat | printf "Max"

Max

Skip list (5 levels)

Find(26)

Remove(82)

trougnouf@tp:~/pres

[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot

1 2 3

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (079% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.18 | 2016-03-16 11:08:45

cat printf... cat printf "Min"	lv 4	Min	cat printf "Max"	Max
cat printf... cat printf "Min"	lv 3	Min	cat printf "Max"	Max
cat printf... cat printf "Min"	lv 2	Min	cat printf "Max"	Max
cat printf... cat printf "Min"	lv 1	Min	cat printf "Max"	Max
cat printf... cat printf "Min"	lv 0	Min	cat printf "Max"	Max

Skip list (5 levels)

Skip list (5 levels)

```
trougnouf@tp:~/pres
(xpad:5189): Gtk-WARNING **: Unknown tag '('
(xpad:5189): Gtk-WARNING **: Unknown tag ')'
(xpad:5189): Gtk-WARNING **: Unknown tag '('
[trougnouf@tp pres]$ scrot
```



Skip list (5 levels)

Insert(23)

trougnouf@tp:~/pres

```
(xpad:5189): Gtk-WARNING **: Unknown tag ' )'  
(xpad:5189): Gtk-WARNING **: Unknown tag ' ('  
[trougnouf@tp pres]$ scrot  
[trougnouf@tp pres]$ scrot
```

cat | printf... cat | printf "Min"

lv4

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv3

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv2

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv1

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv0

Min

23

23

cat | printf "Max"

Max

Skip list (5 levels)

Insert(23)

trougnouf@tp:~/pres

(xpad:5189): Gtk-WARNING **: Unknown tag '
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ xpad &
[19] 5200
[trougnouf@tp pres]\$ scrot

123

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (073% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.34 | 2016-03-16 10:46:20

cat | printf... cat | printf "Min"

lv4

Min

cat | printf... cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv3

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv2

Min

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv1

Min

23

cat | printf "Max"

Max

cat | printf... cat | printf "Min"

lv0

Min

23

cat | printf "Max"

Max

Skip list (5 levels)

Insert(23) flipCoin(): 1

trougnouf@tp:~/pres

[trougnouf@tp pres]\$ scrot
[19]+ Done xpad
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ xpad &
[19] 5206
[trougnouf@tp pres]\$ scrot

1 2 3

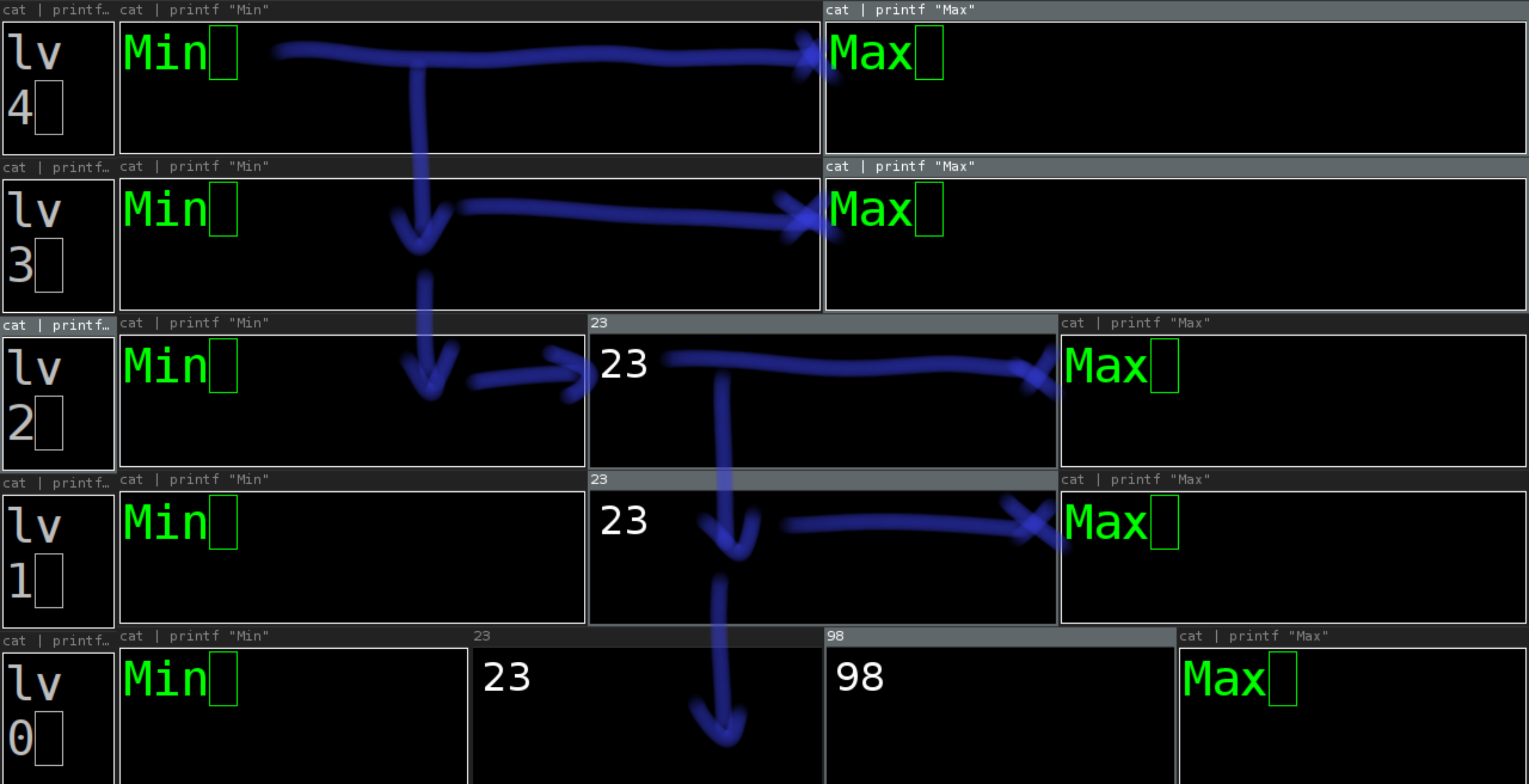
no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (073% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.19 | 2016-03-16 10:47:10

cat printf "%d\n" 4	cat printf "Min"		cat printf "Max"	
cat printf "%d\n" 3	cat printf "Min"		cat printf "Max"	
cat printf "%d\n" 2	cat printf "Min"	23	cat printf "Max"	
cat printf "%d\n" 1	cat printf "Min"	23	cat printf "Max"	
cat printf "%d\n" 0	cat printf "Min"	23	cat printf "Max"	

Skip list (5 levels)

Insert(23) flipCoin(): 1,1,0

```
trougnouf@tp:~/pres
[trougnouf@tp pres]$ scrot
[trougnouf@tp pres]$ xpad &
[19] 5213
[trougnouf@tp pres]$ scrot
[19]+  Done                  xpad
[trougnouf@tp pres]$ scrot
```



Skip list (5 levels)

Insert(23) flipCoin(): 1,1,0

Insert(98)

```
trougnouf@tp:~/pres
[trougnouf@tp pres]$ scrot
[19]+  Done                                xpad
[trougnouf@tp pres]$ scrot
[trougnouf@tp pres]$ xpad &
[19] 5225
[trougnouf@tp pres]$ scrot
```

cat printf "%d\n" 4	cat printf "Min"	cat printf "Max"		
lv 4	Min	Max		
cat printf "%d\n" 3	cat printf "Min"	cat printf "Max"		
lv 3	Min	Max		
cat printf "%d\n" 2	cat printf "Min"	23	cat printf "Max"	
lv 2	Min	23	Max	
cat printf "%d\n" 1	cat printf "Min"	23	98	cat printf "Max"
lv 1	Min	23	98	Max
cat printf "%d\n" 0	cat printf "Min"	23	98	cat printf "Max"
lv 0	Min	23	98	Max

Skip list (5 levels)

Insert(23)

flipCoin(): 1,1,0

Insert(98)

flipCoin(): 1,0

trougnouf@tp:~/pres
2016-03-16-104739_1280x800_scrout.png
2016-03-16-104750_1280x800_scrout.png
2016-03-16-104809_1280x800_scrout.png
2016-03-16-104853_1280x800_scrout.png
2016-03-16-104942_1280x800_scrout.png
[trougnouf@tp pres]\$ scrot

cat printf "%d\n" 4	cat printf "Min"			cat printf "Max"	
lv 4	Min			Max	
cat printf "%d\n" 3	cat printf "Min"			cat printf "Max"	
lv 3	Min			Max	
cat printf "%d\n" 2	cat printf "Min"	23		cat printf "Max"	
lv 2	Min	23		Max	
cat printf "%d\n" 1	cat printf "Min"	23	98	cat printf "Max"	
lv 1	Min	23	98	Max	
cat printf "%d\n" 0	cat printf "Min"	23	45	98	cat printf "Max"
lv 0	Min	23	45	98	Max

Skip list (5 levels)

Insert(98)
Insert(45)

flipCoin(): 1,0
flipCoin(): 0

trougnouf@tp:~/pres
2016-03-16-104853_1280x800_scrout.png
2016-03-16-104942_1280x800_scrout.png
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ xpad &
[19] 5238
[trougnouf@tp pres]\$ scrot

cat | printf "%d\n" 4

lv4

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 3

lv3

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 2

lv2

cat | printf "Min"

Min

23

23

cat | printf "Max"

Max

cat | printf "%d\n" 1

lv1

cat | printf "Min"

Min

23

98

cat | printf "Max"

Max

cat | printf "%d\n" 0

lv0

cat | printf "Min"

Min

23

45

71

98

cat | printf "Max"

Max

Skip list (5 levels)

Insert(45)

Insert(71)

flipCoin(): 0

flipCoin(): 0

trougnouf@tp:~/pres

[19] 5238

[trougnouf@tp pres]\$ scrot

[19]+ Done

[trougnouf@tp pres]\$ xpad &

[19] 5242

[trougnouf@tp pres]\$ scrot

1

2

3

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (078% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.26 | 2016-03-16 10:51:35

cat | printf "%d\n" 4

lv4

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 3

lv3

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 2

lv2

cat | printf "Min"

Min

23

23

cat | printf "Max"

Max

cat | printf "%d\n" 1

lv1

cat | printf "Min"

Min

23

23

98

98

cat | printf "Max"

Max

cat | printf "%d\n" 0

lv0

cat | printf "Min"

Min

11

23

45

71

98

cat | printf "Max"

Max

Skip list (5 levels)

Insert(71)

flipCoin(): 0

Insert(11)

flipCoin(): 0

trougnouf@tp:~/pres

[19] 5242
[trougnouf@tp pres]\$ scrot
[19]+ Done
[trougnouf@tp pres]\$ xpad &
[19] 5252
[trougnouf@tp pres]\$ scrot

1

2

3

no IPv6

132.5 GiB

DHCP: yes

VPN: no

W: (077% at OnNetworks11)

192.168.1.4

E: down

FULL 102.23%

0.22

2016-03-16 10:52:25

cat | printf "%d\n" 4

lv4

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 3

lv3

cat | printf "Min"

Min

49

cat | printf "Max"

Max

cat | printf "%d\n" 2

lv2

cat | printf "Min"

Min

23

49

cat | printf "Max"

Max

cat | printf "%d\n" 1

lv1

cat | printf "Min"

Min

23

49

98

cat | printf "Max"

Max

cat | printf "%d\n" 0

lv0

cat | printf "Min"

Min

11

23

45

49

71

98

cat | printf "Max"

Max

Skip list (5 levels)

Insert(11)

flipCoin(): 0

Insert(49)

flipCoin(): 1,1,1,0

trougnouf@tp:~/pres

[21] 5262

[20] Done

[trougnouf@tp pres]\$ xpad &

[22] 5265

[21] Done

[trougnouf@tp pres]\$ scrot

1

2

3

no IPv6

132.5 GiB

DHCP: yes

VPN: no

W: (077% at OnNetworks11)

192.168.1.4

E: down

FULL 102.23%

0.18

2016-03-16 10:53:45

cat | printf "%d\n" 4

lv4

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 3

lv3

cat | printf "Min"

Min

49

cat | printf "Max"

Max

cat | printf "%d\n" 2

lv2

cat | printf "Min"

Min

23

49

cat | printf "Max"

Max

cat | printf "%d\n" 1

lv1

cat | printf "Min"

Min

23

49

82

98

cat | printf "Max"

Max

cat | printf "%d\n" 0

lv0

cat | printf "Min"

Min

11

23

45

49

71

82

98

cat | printf "Max"

Max

Skip list (5 levels)

Insert(49)

flipCoin(): 1,1,1,0

Insert(82)

flipCoin(): 1,0

trougnouf@tp:~/pres

[trougnouf@tp pres]\$ xpad &

[19] 5270

[trougnouf@tp pres]\$ xpad &

[20] 5273

[19] Done

[trougnouf@tp pres]\$ scrot

1

2

3

no IPv6

132.5 GiB

DHCP: yes

VPN: no

W: (076% at OnNetworks11)

192.168.1.4

E: down

FULL 102.23%

0.30

2016-03-16 10:54:40

cat | printf "%d\n" 4

lv4

cat | printf "Min"

Min

cat | printf "Max"

Max

cat | printf "%d\n" 3

lv3

cat | printf "Min"

Min

49

cat | printf "Max"

Max

cat | printf "%d\n" 2

lv2

cat | printf "Min"

Min

12

23

49

cat | printf "Max"

Max

cat | printf "%d\n" 1

lv1

cat | printf "Min"

Min

12

23

49

82

98

cat | printf "Max"

Max

cat | printf "%d\n" 0

lv0

cat | printf "Min"

Min

11

12

23

45

49

71

82

98

cat | printf "Max"

Max

Skip list (5 levels)

Insert(82)

flipCoin(): 1,0

Insert(12)

flipCoin(): 1,1,0

trougnouf@tp:~/pres

[20] 5283

[19] Done

[trougnouf@tp pres]\$ xpad &

[21] 5286

[20] Done

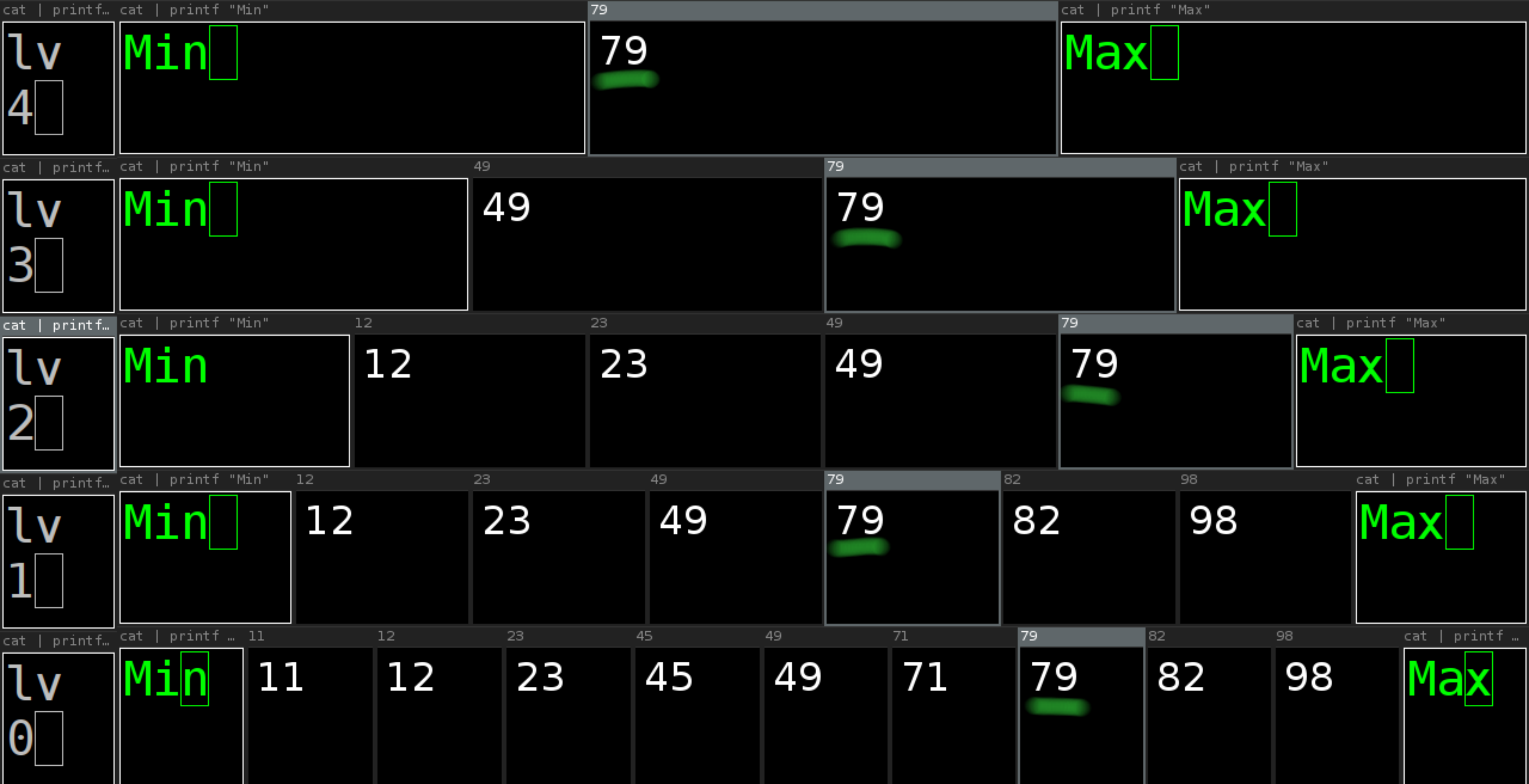
[trougnouf@tp pres]\$ scrot

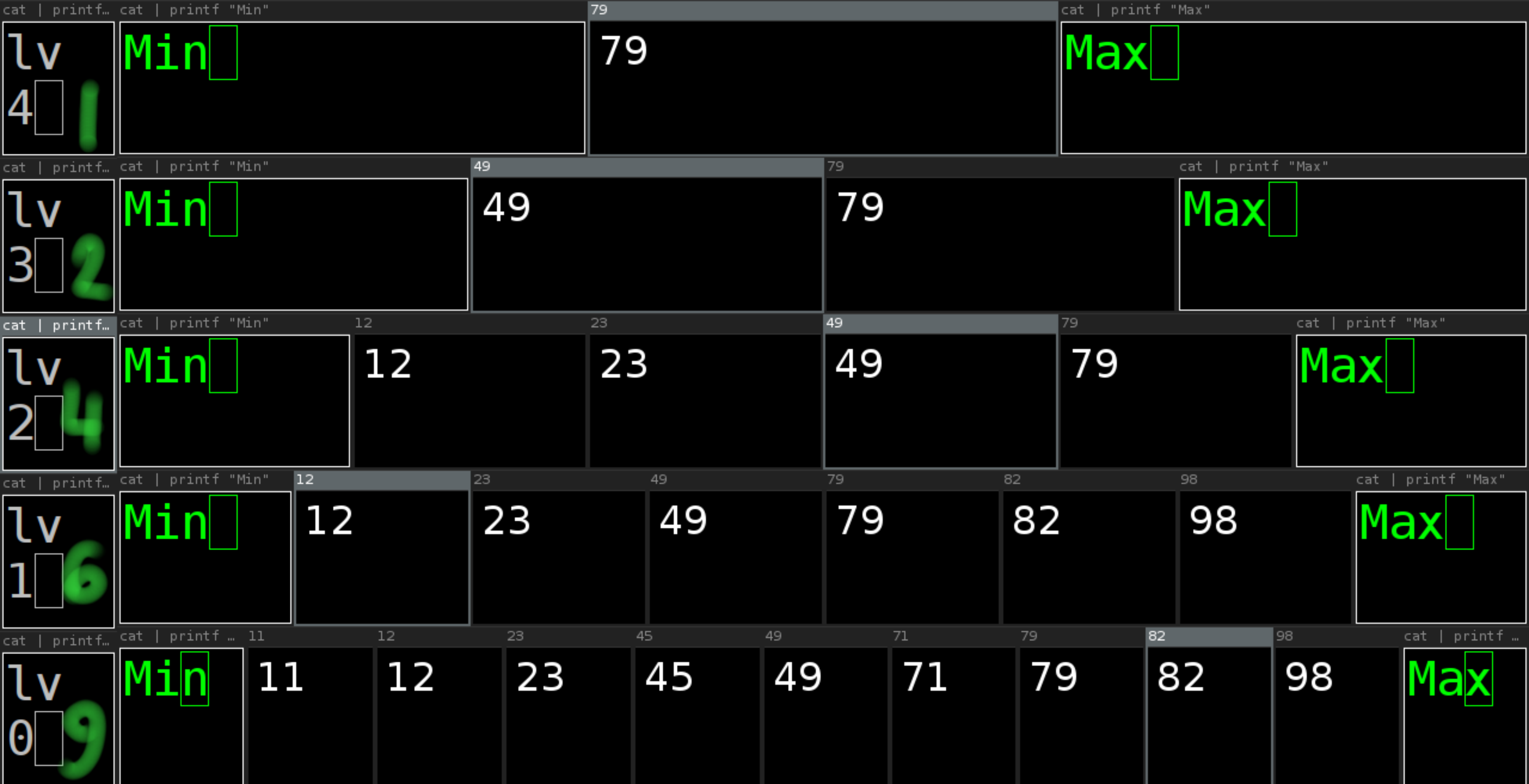
1

2

3

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (077% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.10 | 2016-03-16 10:56:20

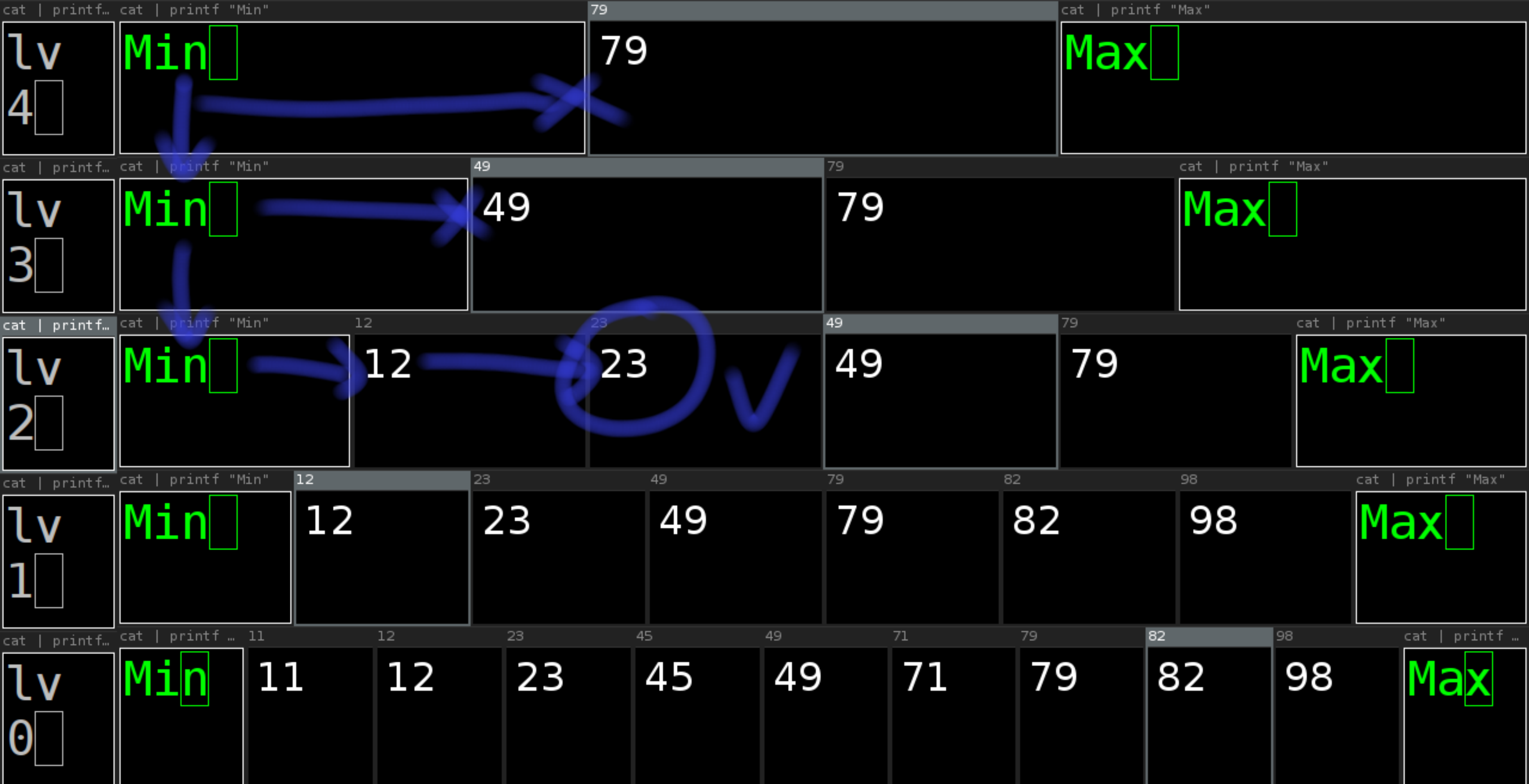


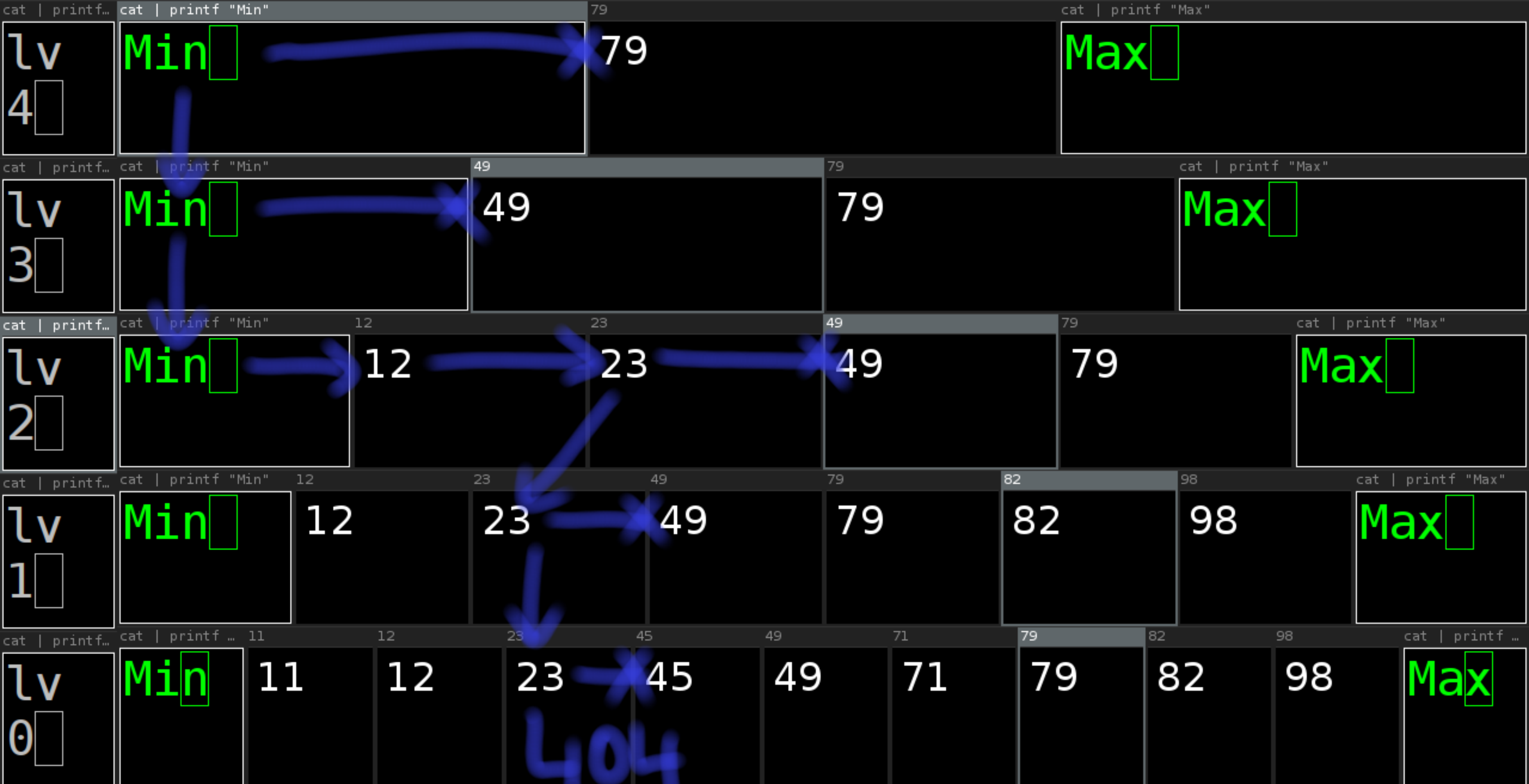


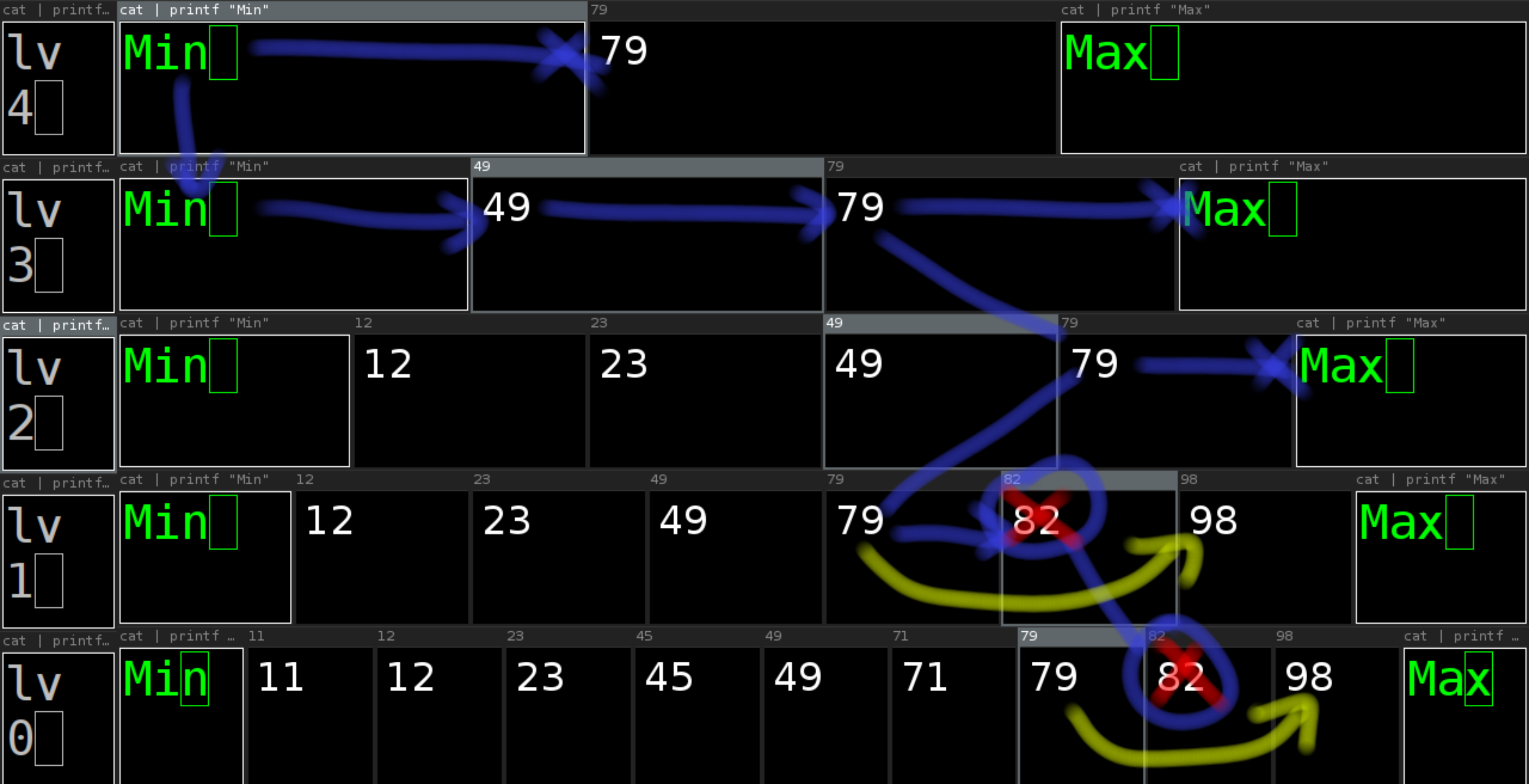
Skip list (5 levels)

1 / 2^(#lv) probability of reaching the top
4 levels: 1/16. 16 levels: 1/65536

```
trougnouf@tp:~/pres
[23] 5302
[22] Done
[trougnouf@tp pres]$ scrot
[23]+ Done
[trougnouf@tp pres]$ scrot
[trougnouf@tp pres]$ scrot
```





Skip list (5 levels)

Find(26)

Remove(82)

1 2 3

trougnouf@tp:~/pres

[23]+ Done

xpad

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (074% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.16 | 2016-03-16 11:06:50

lv4

Min

79

Max

lv3

Min

49

79

Max

lv2

Min

12

23

49

79

Max

lv1

Min

12

23

49

79

98

Max

lv0

Min

11

12

23

45

49

71

79

98

Max

Skip list (5 levels)

Find(26)

Remove(82)

123no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (068%: 40

Open

+

*Unsaved Do...

Save

≡

-

□

×

```
typedef struct slNode_ {
    uint32_t key;
    struct slNode_ ** next;
} slNode;
```

cat | printf...

lv

4

cat | printf "Min"

Min

79

cat | printf "Max"

Max

cat | printf...

lv

3

cat | printf "Min"

Min

49

79

cat | printf "Max"

Max

cat | printf...

lv

2

cat | printf "Min"

Min

12

23

49

79

cat | printf "Max"

Max

cat | printf...

lv

1

cat | printf "Min"

Min

12

23

49

79

98

cat | printf "Max"

Max

cat | printf...

lv

0

cat | printf "M.. 11"

Min

11

12

23

45

4

71

79

98

cat | printf "M.."

Max

Skip list (5 levels)

Find(26)

Remove(82)

123no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: 16:10

Open

*Unsaved Docu...

Save

typedef struct sListNode_ {
 uint32_t key;
 struct sListNode_ ** next;
 struct sListNode_ * previous;
} sListNode;

lv4

cat | printf "Min"

79

cat | printf "Max"

lv3

cat | printf "Min"

49

79

cat | printf "Max"

lv2

cat | printf "Min"

12

23

49

79

cat | printf "Max"

lv1

cat | printf "Min"

12

23

49

79

98

cat | printf "Max"

lv0

cat | printf "Min"

11

12

23

45

cat | printf "Max"

Skip list (5 levels)

Insert(45)

Open

*Unsaved Document 1

Save

flipCoin()
Generate one random integer
// 255248010
Use each bit as a coin
// 1111001101101100011010001010
// 1,1,1,1,0

1

2

3

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (076% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.11 | 2016-03-16 11:23:05

cat | printf...

lv4

cat | printf "Min"

Min

79

cat | printf "Max"

Max

cat | printf...

lv3

cat | printf "Min"

Min

49

79

cat | printf "Max"

Max

cat | printf...

lv2

cat | printf "Min"

Min

12

23

49

79

cat | printf "Max"

Max

cat | printf...

lv1

cat | printf "Min"

Min

12

23

49

79

98

cat | printf "Max"

Max

cat | printf...

lv0

cat | printf "M...

Min

11

12

23

45

49

71

79

98

cat | printf "M...

Max

Skip list (5 levels)

Insert(45)

Insert(71)

flipCoins(): 0

trougnouf@tp: ~/pres

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

[trougnouf@tp pres]\$ scrot

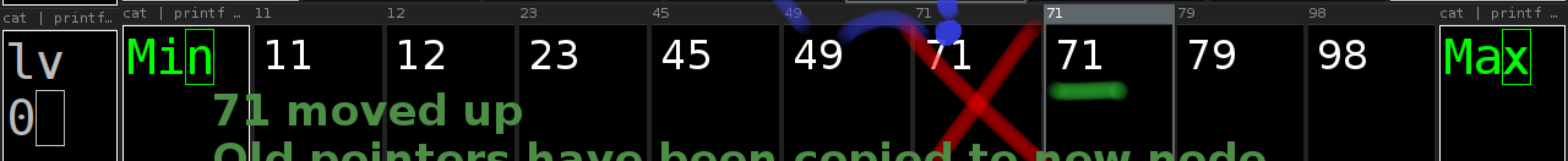
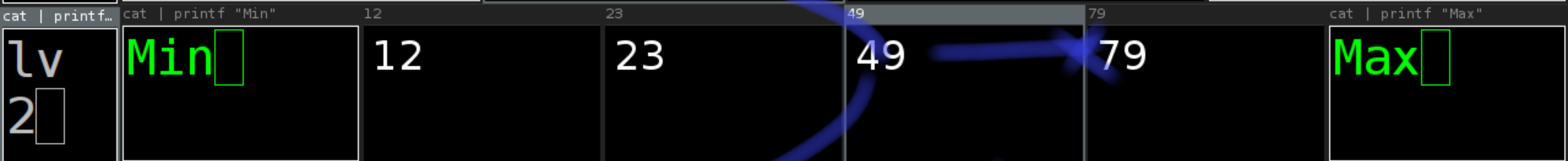
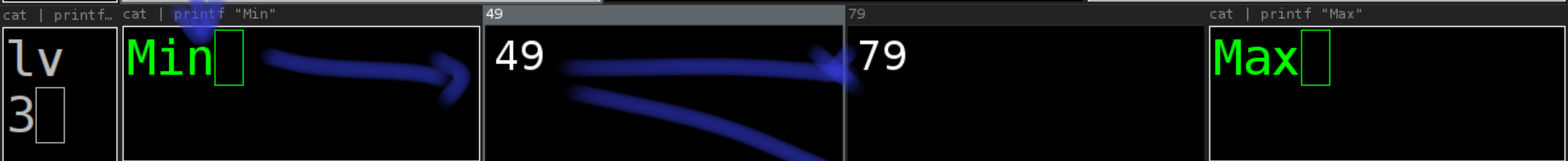
[trougnouf@tp pres]\$ scrot

1

2

3

no IPv6 | 132.5 GiB | DHCP: yes | VPN: no | W: (075% at OnNetworks11) 192.168.1.4 | E: down | FULL 102.23% | 0.20 | 2016-03-16 11:24:55



Skip list (5 levels)

Insert(71)
InsertMerge(71) flipCoins():1,0

71 moved up
Old pointers have been copied to new node
Old node is freed

```
trougnouf@tp:~/pres
[19] 5433
[trougnouf@tp pres]$ scrot
[19]+  Done
[trougnouf@tp pres]$ xpad &
[19] 5439
[trougnouf@tp pres]$ scrot
```


cat | printf...

lv

4

cat | printf "Min"

Min

79

cat | printf "Max"

Max

23 was found before Insertion began
Nothin happened

cat | printf...

lv

3

cat | printf "Min"

Min

49

79

cat | printf "Max"

Max

cat | printf...

lv

2

cat | printf "Min"

Min

12

23

49

79

cat | printf "Max"

Max

cat | printf...

lv

1

cat | printf "Min"

Min

12

23

49

71

79

98

cat | printf "Max"

Max

cat | printf...

lv

0

cat | printf "M.. 11"

Min

11

12

23

45

49

71

79

98

cat | printf "M.."

Max

Skip list (5 levels)

InsertMerge(71)

flipCoins():1,0

InsertMerge(23)

flipCoins():1,0

trougnouf@tp:~/pres

[trougnouf@tp pres]\$ xpad &
[19] 5439
[trougnouf@tp pres]\$ scrot
[19]+ Done xpad
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot

cat | printf...
lv
4

cat | printf "Min"
Min

79

cat | printf "Max"
Max

5 was inserted without wasting time finding it beforehand

cat | printf...
lv
3

cat | printf "Min"
Min

49

79

cat | printf "Max"
Max

cat | printf...
lv
2

cat | printf "Min"
Min

12

23

49

79

cat | printf "Max"
Max

cat | printf...
lv
1

cat | printf "Min"
Min

5

12

23

49

71

79

98

cat | printf "Max"
Max

cat | printf...
lv
0

cat | printf "Min"
Min

5

11

12

23

45

49

71

79

98

cat | printf...
Max

Skip list (5 levels)

InsertMerge(23)
InsertMerge(5)

flipCoins():1,0
flipCoins(1,0)

trougnouf@tp:~/pres
[19]+ Done xpad
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ scrot
[trougnouf@tp pres]\$ xpad &
[19] 5468
[trougnouf@tp pres]\$ scrot

cat | printf...
lv
4

cat | printf "Min"
Min

79

cat | printf "Max"
Max

cat | printf...
lv
3

cat | printf "Min"
Min

49

79

cat | printf "Max"
Max

cat | printf...
lv
2

cat | printf "Min"
Min

12

23

49

79

cat | printf "Max"
Max

cat | printf...
lv
1

cat | printf "Min"
Min

12

23

49

cat | printf...
lv
0

cat | printf ...
Min

5

11

12

23

45

Skip list (5 levels)

InsertMerge(23)
InsertMerge(5)

flipCoins():1,0
flipCoins():0

123

no IPv6 | 132.5 GiB | DHCP: yes | VPN:

36:35

Open *Unsaved Document 1 Save

```
typedef struct sListNode_ {  
    uint32_t key;  
    atomic_uintptr_t * next;  
    struct sListNode_ * previous;  
    uint8_t stopflag  
} sListNode;  
  
typedef struct sListNode_obsolete {  
    uint32_t key;  
    struct sListNode_ ** next;  
    struct sListNode_ * previous;  
} sListNode;
```



Open ▾

📁

*Unsaved Document 1

Save

☰

—

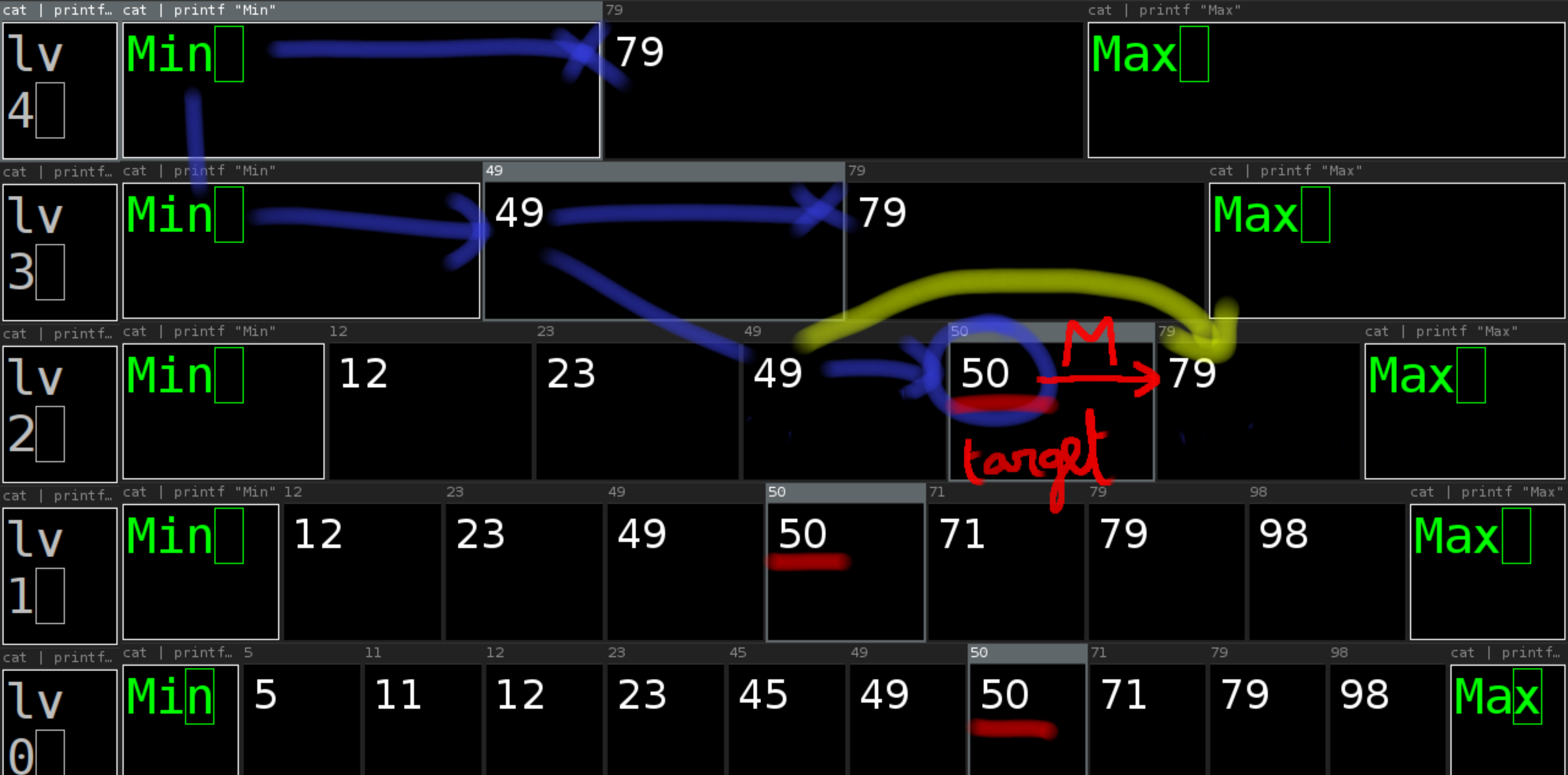
□

×

```

slRemove(slHead, key):
Local pointers: curNode, target, nextNode

- Find target (and its highest level), mark it for deletion
For each level:
  - Mark target's next pointer
    atomic_fetch_or(&target->next[lv], 1)
  - set curNode->next to (unmarked) target->next if curNode->next==target
    CAS(curNode->next[lv], target, target->next[lv])
- Free target
  free(target->next), free(target)
  
```

use CAS to move curNode's next pointer to target's (unmarked) next iff curNode->next = target fails if curNode(->next) has been marked for deletion or curNode->next no longer points to target

Skip list (5 levels)

InsertMerge
RemoveConcurrently

cat printf... lv 4	cat printf "Min" Min	79	cat printf "Max" Max
cat printf... lv 3	cat printf "Min" Min	49	cat printf "Max" Max
cat printf... lv 2	cat printf "Min" Min	12	cat printf "Max" Max
cat printf... lv 2	cat printf "Min" Min	12	cat printf "Max" Max

Open

+

*Unsaved Document 1
~/pres

Save

≡

-

□

×

```

slInsert(slHead, key)
Local pointers: curNode, newNode, nextNode
For each level:
- Find curNode s.t. curNode < newNode < nextNode and curN->next=nextNode
- Set newNode->next to nextNode
- Set curNode->next to newNode if curNode->next == nextNode
  // CAS fails if curNode->next has been marked
  // or nextNode is no longer next
Failure? Find curNode and nextNode again using next
Repeated failure? Reset curNode

```

```
slInsert(slHead, key)
```

```
Local pointers: curNode, newNode, nextNode
```

```
For each level:
```

- Find curNode s.t. $\text{curNode} < \text{newNode} < \text{nextNode}$ and $\text{curNode} \rightarrow \text{next} = \text{nextNode}$
- Set $\text{curNode} \rightarrow \text{next}$ to newNode **if** $\text{curNode} \rightarrow \text{next} == \text{nextNode}$
 - // CAS fails if $\text{curNode} \rightarrow \text{next}$ has been marked
 - // or nextNode is no longer next

```
Failure? Find curNode and nextNode again using curNode's next pointer
```

```
Repeated failure? Reset curNode
```

```
eg:
```

cur	cur->next	next	new
5	->	10	8

```
set new->next to next
```

cur	cur->next	next	new	new->next	10
5	->	10	8	->	10

```
CAS(curnode->next, nextnode, newnode)
```

cur	cur->next	new	new->next	next
5	->	8	->	10

```
// curNode is marked for deletion? Fail.
```

```
// nextNode is no longer next? Fail.
```

```
[ttroughnouv@tp School]$ scrot
```