

## Part One: Short answer questions

1. The number of possible passwords:

$$21 \times 5 \times 21 \times 10^3 \times 5^2 = 55125000.$$

$$\text{Entropy} = \log_2 55125000 = \frac{\log_{10}^{55125000}}{\log_{10} 2} \approx 25.7162$$

When apply whirlpool hash function to get a 128 bit hex string, there will be at most 55125000 possible different output. But the whirlpool may incur collision, so the practical different output may be less than 55125000. As a result, the entropy of the output is equal to or less than the entropy of passwords.

2. (1) Subjects: Alice; Bob; Chris; Dan

Objects: walls; fences; doors; Alice

Actions: climb; jump; push; open

(2)

Object Subject	walls	fences	doors	Alice
Alice	climb	jump		
Bob	push		push	
Chris	jump	push		push
Dan			open	jump

3. (a) They have a set  $\{a_1 a_2 a_3 a_4 \mid a_i \in \{0, 1\}\}$  and a partial order like  $(0100) \text{ dom } (0000)$ . This order meets reflexive, antisymmetric and transitive relation. So they can be regarded as lattices and they are same lattices.
- (b) 1011
- (c) 0111
- (d) 1110
- (e) Each digit can be interpreted as a privilege. If level  $X$  dominates level  $Y$ , then level  $X$  has all privileges that level  $Y$  has and has extra privileges. But if level  $X$  and level  $Y$  are connected by one line and level  $X$  dominates level  $Y$ , then level  $X$  only has one extra privilege compared with level  $Y$ . This complies with principle of least privilege and is also the partial order of this lattice.

4. 1<sup>st</sup>: e53999a51b1df69f10708334ea7503ff

2<sup>nd</sup>: 2b846f93a9bb9044c2277ff2c92425eb

10<sup>th</sup>: Alice5083898

5. (a) The diagram doesn't define a good lattice.

It contains a set  $L \subseteq \{A \dots K\}$  and a partial order. But there are at least 2 redundant relationships in the diagram. In addition, it seems like an error that  $H \text{ dom } G$ . Generally, if  $H \text{ dom } G$ ,  $H$  should be higher than  $G$  in the diagram. Besides, if  $H \text{ dom } G$ , relationship between  $J$  and  $G$  is redundant as well. So although this diagram contains the essential components of a lattice, a set and a partial order, it is still not a well-formed lattice.

(b)  $C \leftarrow K$  and  $A \leftarrow D$  are redundant, because

$C \leftarrow D \leftarrow K$  and  $A \leftarrow B \leftarrow D$ . This property is called transitivity.