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In [41]: import math
from mpl_toolkits.mplot3d import Axes3D
import matplotlib.pyplot as plt
from matplotlib import cm
from matplotlib.ticker import LinearLocator, FormatStrFormatter
import numpy as np
import random
```

```
In [42]: def get_points(num, minval = -1.0, maxval = 1.0, dim = 2):
    points = np.asarray([[None for i in range(dim)] for j in range(num)
    ])
    for i in range(dim):
        for j in range(num):
            points[j,i] = random.uniform(minval, maxval)
    return np.asarray(points)
```

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In [43]: def get_target_fn(points):
    #  $y = mx + b$ 
    #returns m, b
    x1 = points[0,0]
    y1 = points[0,1]
    x2 = points[1,0]
    y2 = points[1,1]
    m = (y2-y1)/(x2-x1)
    b = y1 - m*(x1)
    return m, b
```

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In [44]: def add_bias_to_x(x):
    bias = np.ones(len(x[:,0]))
    x = np.c_[x,bias]
    return x
```

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In [45]: def eval_target_fn(datapoints,m,b):
    y = np.zeros(len(datapoints))
    for i in range(len(datapoints)):
        if datapoints[i,1] < datapoints[i,0]*m + b:
            y[i] = -1
        else:
            y[i] = 1
    return y
```

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In [46]: def get_sign(vec):
    sign = np.zeros(len(vec))
    for i in range(len(vec)):
        if vec[i] == 0:
            sign[i] = 0.0
        else:
            if vec[i] < 0:
                sign[i] = -1.0
            else:
                sign[i] = 1.0
    return sign
```

In [47]: **def** get_target(N,minval = -1.0, maxval = 1.0, dim = 2):

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target_fn_points = get_points(dim)
m, b = get_target_fn(target_fn_points)
x = get_points(N)
y = eval_target_fn(x,m,b)
return m,b,x,y
```

In [48]: **def** plot_target(m,b,x,y):

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plt.plot((-1,1), (get_y(-1,m,b), get_y(1,m,b)))
plt.xlim([-1,1])
plt.ylim([-1,1])
neg_x = [x[i,0] for i in range(len(x[:,0])) if y[i] < 0]
pos_x = [x[i,0] for i in range(len(x[:,0])) if y[i] > 0]
neg_y = [x[i,1] for i in range(len(x[:,1])) if y[i] < 0]
pos_y = [x[i,1] for i in range(len(x[:,1])) if y[i] > 0]
plt.plot(neg_x, neg_y, 'r*')
plt.plot(pos_x, pos_y, 'b*')
plt.title('Target data')
plt.show()
```

In [157]: **def** plot_iter(m,b,x,y,w, iteration):

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plt.plot((-1,1), (get_y(-1,m,b), get_y(1,m,b)), 'g', label = 'target_
fn')
print(w)
plt.plot((-1,1), ((w[0]-w[2])/w[1], (-w[0]-w[2])/w[1]), 'c', label='le
arned_fn')
plt.xlim([-1,1])
plt.ylim([-1,1])
neg_x = [x[i,0] for i in range(len(x[:,0])) if w.dot(x[i,:].transpos
e()) <= 0]
pos_x = [x[i,0] for i in range(len(x[:,0])) if w.dot(x[i,:].transpos
e()) > 0]
neg_y = [x[i,1] for i in range(len(x[:,1])) if w.dot(x[i,:].transpos
e()) <= 0]
pos_y = [x[i,1] for i in range(len(x[:,1])) if w.dot(x[i,:].transpos
e()) > 0]
plt.plot(neg_x, neg_y, 'r*')
plt.plot(pos_x, pos_y, 'b*')
plt.title('Logistic Regression, iter. '+str(iteration))
plt.xlabel('x_1')
plt.ylabel('x_2')
plt.legend()
plt.savefig('Logistic_Regression.jpg')
plt.show()
```

In [85]: **def** get_y(x,m,b):

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return m*x + b
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In [86]: **def** init_weights(dim=2):

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return np.zeros(dim+1)
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In [87]: def update_weights(w,x,y,idx):
         w = w + y[idx]*x[idx]
         return w
```

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In [88]: def get_misclassified_point_idx(sign, y):
         idx = []
         for i in range(len(sign)):
             if sign[i] != y[i]:
                 idx.append(i)
         return idx
```

```
In [89]: def estimate_disagreement(w, m, b, num_test_points = 100):
         test_x = get_points(num_test_points)
         test_y = eval_target_fn(test_x,m,b)
         test_x = add_bias_to_x(test_x)
         vec = w.dot(test_x.transpose())
         sign = get_sign(vec)
         idx = get_misclassified_point_idx(sign,test_y)
         disagreement_prob = float(len(idx))/float(num_test_points)
         return disagreement_prob
```

```
In [139]: def logistic_regression_sgd(N, lr = 0.01, threshold = 0.01, minval = -1.0
, maxval = 1.0, dim = 2, plot_fn = False):
         m,b,x,y = get_target(N)
         x = add_bias_to_x(x)
         w = init_weights()
         iter_count = 0
         diff = 100
         while diff > threshold: #while there are misclassified points
             iter_count += 1
             rand_N = list(range(N))
             random.shuffle(rand_N)
             w_prev = np.copy(w)
             w_ = np.copy(w)
             for n in rand_N:
                 #print(n)
                 x_n = x[n,:]
                 y_n = y[n]
                 err = (y_n*x_n)/(1+np.exp(y_n*np.dot(w_,x_n)))
                 w_ = w_ + lr*err
             w = np.copy(w_)
             diff = np.linalg.norm(w-w_prev)

         e_out = estimate_disagreement(w,m,b)
         if plot_fn:
             plot_iter(m,b,x,y,w,iter_count)
         return iter_count, e_out
```

```

In [137]: N = 100
iterations = 100
num_iters = []
disagreement_probs = []
for i in range(iterations):
    iter_count, disagreement = logistic_regression_sgd(N)
    num_iters.append(iter_count)
    #print(iter_count)
    disagreement_probs.append(disagreement)

print(len(num_iters))
print(np.mean(num_iters))
print(np.mean(disagreement_probs))

```

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100
338.93
0.0234

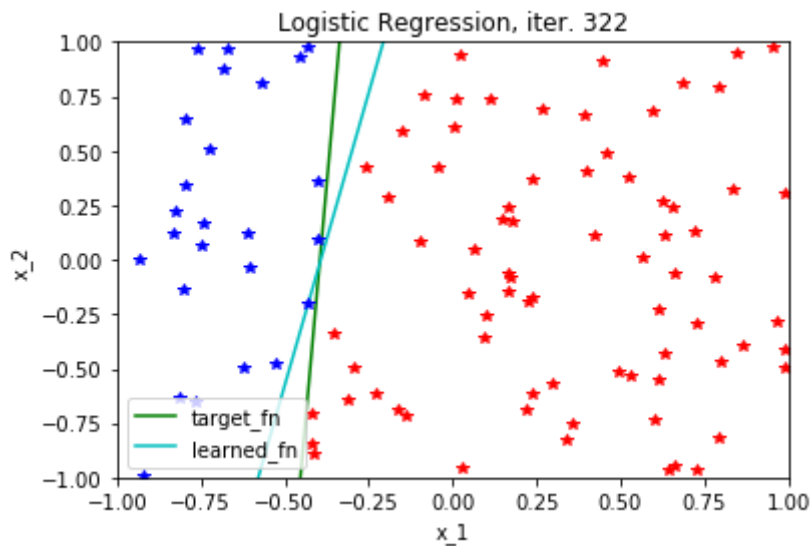
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In [160]: iter_count, disagreement = logistic_regression_sgd(N, plot_fn=True)

[-8.178366450004003  1.5241806426943323 -3.212555981907816]

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In []:

In []: