



We start our study with fluids at rest, such as water in a glass or a lake. Pressure in a fluid increases with depth, a fact that allows less dense objects to float—the pressure underneath is higher than on top. When fluids flow, such as water or air, interesting effects occur because the pressure in the fluid is lower where the fluid velocity is higher (Bernoulli's principle).

The great mass of a glacier's ice (photos here) moves slowly, like a viscous liquid. The dark lines are “moraines,” made up of rock broken off mountain walls by the moving ice, and represent streamlines. The two photos, taken in 1929 and 2009 by Italian expeditions to the mountain K2 (on the right in the distance), show the same glacier has become less thick, presumably due to global warming.

CHAPTER 10

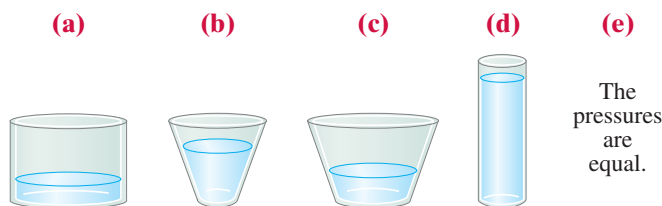
Fluids

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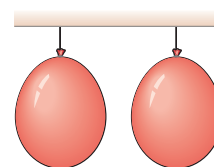
CHAPTER-OPENING QUESTIONS—Guess now!

1. Which container has the largest pressure at the bottom? Assume each container holds the same volume of water.



2. Two balloons are tied and hang with their nearest edges about 3 cm apart. If you blow between the balloons (not *at* the balloons, but at the opening between them), what will happen?

- (a) Nothing.
- (b) The balloons will move closer together.
- (c) The balloons will move farther apart.



In previous Chapters we considered objects that were solid and assumed to maintain their shape except for a small amount of elastic deformation. We sometimes treated objects as point particles. Now we are going to shift our attention to materials that are very deformable and can flow. Such “fluids” include liquids and gases. We will examine fluids both at rest (fluid statics) and in motion (fluid dynamics).

10-1 Phases of Matter

The three common **phases**, or **states**, of matter are solid, liquid, and gas. A simple way to distinguish these three phases is as follows. A **solid** maintains a generally fixed size and shape; usually it requires a large force to change the volume or shape of a solid[†] (although a thin object might bend). A **liquid** does not maintain a fixed shape—it takes on the shape of its container, and it can flow; but like a solid it is not readily compressible, and its volume can be changed significantly only by a very large force. A **gas** has neither a fixed shape nor a fixed volume—it will expand to fill its container. For example, when air is pumped into an automobile tire, the air does not all run to the bottom of the tire as a liquid would; it spreads out to fill the whole volume of the tire.

Because liquids and gases do not maintain a fixed shape, they both have the ability to flow. They are thus referred to collectively as **fluids**.

The division of matter into three phases is not always simple. How, for example, should butter be classified? Furthermore, a fourth phase of matter can be distinguished, the **plasma** phase, which occurs only at very high temperatures and consists of ionized atoms (electrons separated from the nuclei). Some scientists believe that *colloids* (suspensions of tiny particles in a liquid) should also be considered a separate phase of matter. **Liquid crystals**, used in TV, cell phone, and computer screens, can be considered a phase of matter in between solids and liquids. For now, we will be interested in the three ordinary phases of matter.

10-2 Density and Specific Gravity

It is sometimes said that iron is “heavier” than wood. This cannot really be true since a large log clearly weighs more than an iron nail. What we should say is that iron is more *dense* than wood.

The **density**, ρ , of a substance (ρ is the lowercase Greek letter rho) is defined as its mass per unit volume:

$$\rho = \frac{m}{V}, \quad (10-1)$$

where m is the mass of a sample of the substance and V its volume. Density is a characteristic property of any pure substance. Objects made of a particular pure substance, such as pure gold, can have any size or mass, but the density will be the same for each.

We can use the concept of density, Eq. 10-1, to write the mass of an object as

$$m = \rho V,$$

and the weight of an object as

$$mg = \rho Vg.$$

The SI unit for density is kg/m^3 . Sometimes densities are given in g/cm^3 . Note that a density given in g/cm^3 must be multiplied by 1000 to give the result in kg/m^3 [$1 \text{ kg/m}^3 = 1000 \text{ g}/(100 \text{ cm})^3 = 10^3 \text{ g}/10^6 \text{ cm}^3 = 10^{-3} \text{ g/cm}^3$]. For example, the density of aluminum is $\rho = 2.70 \text{ g/cm}^3$, which equals 2700 kg/m^3 . The densities of various substances are given in Table 10-1. The Table specifies temperature and atmospheric pressure because they affect density (the effect is slight for liquids and solids). Note that air is about 1000 times less dense than water.

TABLE 10-1
Densities of Substances[‡]

Substance	Density, ρ (kg/m^3)
<i>Solids</i>	
Aluminum	2.70×10^3
Iron and steel	7.8×10^3
Copper	8.9×10^3
Lead	11.3×10^3
Gold	19.3×10^3
Concrete	2.3×10^3
Granite	2.7×10^3
Wood (typical)	$0.3 - 0.9 \times 10^3$
Glass, common	$2.4 - 2.8 \times 10^3$
Ice (H_2O)	0.917×10^3
Bone	$1.7 - 2.0 \times 10^3$
<i>Liquids</i>	
Water (4°C)	1.000×10^3
Sea water	1.025×10^3
Blood, plasma	1.03×10^3
Blood, whole	1.05×10^3
Mercury	13.6×10^3
Alcohol, ethyl	0.79×10^3
Gasoline	$0.7 - 0.8 \times 10^3$
<i>Gases</i>	
Air	1.29
Helium	0.179
Carbon dioxide	1.98
Water (steam) (100°C)	0.598

[‡]Densities are given at 0°C and 1 atm pressure unless otherwise specified.

EXAMPLE 10-1 Mass, given volume and density. What is the mass of a solid iron wrecking ball of radius 18 cm?

APPROACH First we use the standard formula $V = \frac{4}{3}\pi r^3$ (see inside rear cover) to obtain the sphere's volume. Then Eq. 10-1 and Table 10-1 give us the mass m .

SOLUTION The volume of the sphere is

$$V = \frac{4}{3}\pi r^3 = \frac{4}{3}(3.14)(0.18 \text{ m})^3 = 0.024 \text{ m}^3.$$

From Table 10-1, the density of iron is $\rho = 7800 \text{ kg/m}^3$, so Eq. 10-1 gives

$$m = \rho V = (7800 \text{ kg/m}^3)(0.024 \text{ m}^3) = 190 \text{ kg}.$$

[†]Section 9-5.

The **specific gravity** of a substance is defined as the ratio of the density of that substance to the density of water at 4.0°C. Because specific gravity (abbreviated SG) is a ratio, it is a simple number without dimensions or units. For example (see Table 10–1), the specific gravity of lead is 11.3 $[(11.3 \times 10^3 \text{ kg/m}^3)/(1.00 \times 10^3 \text{ kg/m}^3)]$. The SG of alcohol is 0.79.

The concepts of density and specific gravity are especially helpful in the study of fluids because we are not always dealing with a fixed volume or mass.

10–3 Pressure in Fluids

Pressure and force are related, but they are not the same thing. **Pressure** is defined as force per unit area, where the force F is understood to be the magnitude of the force acting perpendicular to the surface area A :

$$\text{pressure} = P = \frac{F}{A}. \quad (10-2)$$

CAUTION

Pressure is a scalar, not a vector

Although force is a vector, pressure is a scalar. Pressure has magnitude only. The SI unit of pressure is N/m^2 . This unit has the official name **pascal** (Pa), in honor of Blaise Pascal (see Section 10–5); that is, $1 \text{ Pa} = 1 \text{ N/m}^2$. However, for simplicity, we will often use N/m^2 . Other units sometimes used are dynes/cm^2 , and lb/in.^2 (pounds per square inch, abbreviated “psi”). Several other units for pressure are discussed in Sections 10–4 and 10–6, along with conversions between them (see also the Table inside the front cover).

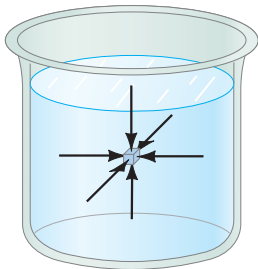
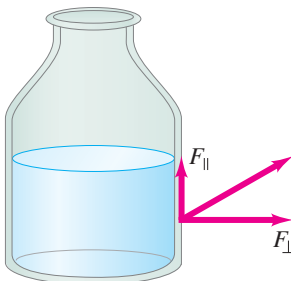


FIGURE 10–1 Pressure is the same in every direction in a nonmoving fluid at a given depth. If this weren’t true, the fluid would be in motion.

FIGURE 10–2 If there were a component of force parallel to the solid surface of the container, the liquid would move in response to it. For a liquid at rest, $F_{\parallel} = 0$.



EXAMPLE 10–2 Calculating pressure. A 60-kg person’s two feet cover an area of 500 cm^2 . (a) Determine the pressure exerted by the two feet on the ground. (b) If the person stands on one foot, what will be the pressure under that foot?

APPROACH Assume the person is at rest. Then the ground pushes up on her with a force equal to her weight mg , and she exerts a force mg on the ground where her feet (or foot) contact it. Because $1 \text{ cm}^2 = (10^{-2} \text{ m})^2 = 10^{-4} \text{ m}^2$, then $500 \text{ cm}^2 = 0.050 \text{ m}^2$.

SOLUTION (a) The pressure on the ground exerted by the two feet is

$$P = \frac{F}{A} = \frac{mg}{A} = \frac{(60 \text{ kg})(9.8 \text{ m/s}^2)}{(0.050 \text{ m}^2)} = 12 \times 10^3 \text{ N/m}^2.$$

(b) If the person stands on one foot, the force is still equal to the person’s weight, but the area will be half as much, so the pressure will be twice as much: $24 \times 10^3 \text{ N/m}^2$.

Pressure is particularly useful for dealing with fluids. It is an experimental observation that *a fluid exerts pressure in every direction*. This is well known to swimmers and divers who feel the water pressure on all parts of their bodies. At any depth in a fluid at rest, the pressure is the same in all directions at that given depth. To see why, consider a tiny cube of the fluid (Fig. 10–1) which is so small that we can consider it a point and can ignore the force of gravity on it. The pressure on one side of it must equal the pressure on the opposite side. If this weren’t true, there would be a net force on the cube and it would start moving. If the fluid is not flowing, then the pressures must be equal.

For a fluid at rest, the force due to fluid pressure always acts *perpendicular* to any solid surface it touches. If there were a component of the force parallel to the surface, as shown in Fig. 10–2, then according to Newton’s third law the solid surface would exert a force back on the fluid, which would cause the fluid to flow—in contradiction to our assumption that the fluid is at rest. Thus the force due to the pressure in a fluid at rest is always perpendicular to the surface.

We now calculate quantitatively how the pressure in a liquid of uniform density varies with depth. Let us look at a depth h below the surface of the liquid as shown in Fig. 10–3 (that is, the liquid's top surface is a height h above this level). The pressure due to the liquid at this depth h is due to the weight of the column of liquid above it. Thus the force due to the weight of liquid acting on the area A is $F = mg = (\rho V)g = \rho Ahg$, where Ah is the volume of the column of liquid, ρ is the density of the liquid (assumed to be constant), and g is the acceleration of gravity. The pressure P due to the weight of liquid is then

$$P = \frac{F}{A} = \frac{\rho Ahg}{A}$$

$$P = \rho gh.$$

[liquid] (10–3a)

Note that the area A doesn't affect the pressure at a given depth. The fluid pressure is directly proportional to the density of the liquid and to the depth within the liquid. In general, *the pressure at equal depths within a uniform liquid is the same.*

EXERCISE A Return to Chapter-Opening Question 1, page 260, and answer it again now. Try to explain why you may have answered differently the first time.

Equation 10–3a is extremely useful. It is valid for fluids whose density is constant and does not change with depth—that is, if the fluid is *incompressible*. This is usually a good approximation for liquids (although at great depths in the ocean, the density of water is increased some by compression due to the great weight of water above).

If the density of a fluid does vary, a useful relation can be found by considering a thin horizontal slab of the fluid of thickness $\Delta h = h_2 - h_1$. The pressure on the top of the slab, at depth h_1 , is $P_1 = \rho gh_1$. The pressure on the bottom of the slab (pushing upward), at depth h_2 , is $P_2 = \rho gh_2$. The difference in pressure is

$$\Delta P = P_2 - P_1 = \rho g(h_2 - h_1)$$

or

$$\Delta P = \rho g \Delta h. \quad [\rho \approx \text{constant over } \Delta h] \quad (10-3b)$$

Equation 10–3b tells us how the pressure changes over a small change in depth (Δh) within a fluid, even if compressible.

Gases are very compressible, and density can vary significantly with depth. For this more general case, in which ρ may vary, we need to use Eq. 10–3b where Δh should be small if ρ varies significantly with depth (or height).

EXAMPLE 10–3 Pressure at a faucet. The surface of the water in a storage tank is 30 m above a water faucet in the kitchen of a house, Fig. 10–4. Calculate the difference in water pressure between the faucet and the surface of the water in the tank.

APPROACH Water is practically incompressible, so ρ is constant even for a $\Delta h = 30$ m when used in Eq. 10–3b. Only Δh matters; we can ignore the “route” of the pipe and its bends.

SOLUTION We assume the atmospheric pressure at the surface of the water in the storage tank is the same as at the faucet. So, the water pressure difference between the faucet and the surface of the water in the tank is

$$\Delta P = \rho g \Delta h = (1.0 \times 10^3 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(30 \text{ m}) = 2.9 \times 10^5 \text{ N/m}^2.$$

NOTE The height Δh is sometimes called the **pressure head**. In this Example, the head of water is 30 m at the faucet. The very different diameters of the tank and faucet don't affect the result—only height does.

EXERCISE B A dam holds back a lake that is 85 m deep at the dam. If the lake is 20 km long, how much thicker should the dam be than if the lake were smaller, only 1.0 km long?

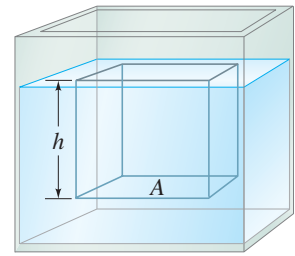
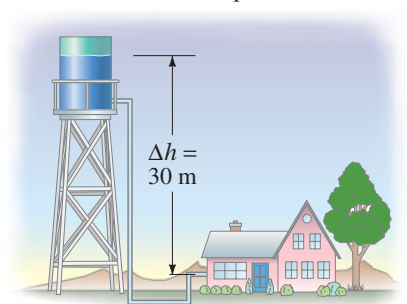


FIGURE 10–3 Calculating the pressure at a depth h in a liquid, due to the weight of the liquid above.

PHYSICS APPLIED

Water supply

FIGURE 10–4 Example 10–3.



10-4 Atmospheric Pressure and Gauge Pressure

Atmospheric Pressure

The pressure of the Earth's atmosphere, as in any fluid, changes with depth. But the Earth's atmosphere is somewhat complicated: not only does the density of air vary greatly with altitude but there is no distinct top surface to the atmosphere from which h (in Eq. 10-3a) could be measured. We can, however, calculate the approximate difference in pressure between two altitudes above Earth's surface using Eq. 10-3b.

The pressure of the air at a given place varies slightly according to the weather. At sea level, the pressure of the atmosphere on average is $1.013 \times 10^5 \text{ N/m}^2$ (or 14.7 lb/in.^2). This value lets us define a commonly used unit of pressure, the **atmosphere** (abbreviated atm):

$$1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2 = 101.3 \text{ kPa}.$$

Another unit of pressure sometimes used (in meteorology and on weather maps) is the **bar**, which is defined as

$$1 \text{ bar} = 1.000 \times 10^5 \text{ N/m}^2.$$

Thus standard atmospheric pressure is slightly more than 1 bar.

The pressure due to the weight of the atmosphere is exerted on all objects immersed in this great sea of air, including our bodies. How does a human body withstand the enormous pressure on its surface? The answer is that living cells maintain an internal pressure that closely equals the external pressure, just as the pressure inside a balloon closely matches the outside pressure of the atmosphere. An automobile tire, because of its rigidity, can maintain internal pressures much greater than the external pressure.



PHYSICS APPLIED

Pressure on living cells

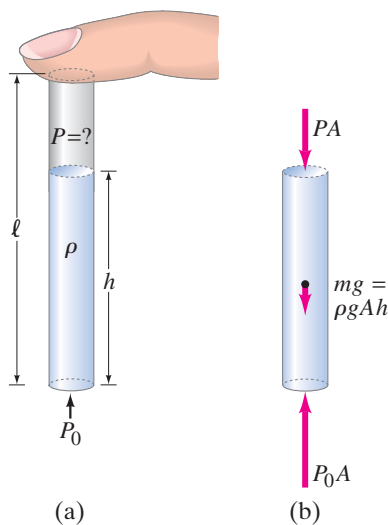


FIGURE 10-5 Example 10-4.

CONCEPTUAL EXAMPLE 10-4 **Finger holds water in a straw.** You insert a straw of length ℓ into a tall glass of water. You place your finger over the top of the straw, capturing some air above the water but preventing any additional air from getting in or out, and then you lift the straw from the water. You find that the straw retains most of the water (Fig. 10-5a). Does the air in the space between your finger and the top of the water have a pressure P that is greater than, equal to, or less than, the atmospheric pressure P_0 outside the straw?

RESPONSE Consider the forces on the column of water (Fig. 10-5b). Atmospheric pressure outside the straw pushes upward on the water at the bottom of the straw, gravity pulls the water downward, and the air pressure inside the top of the straw pushes downward on the water. Since the water is in equilibrium, the upward force due to atmospheric pressure P_0 must balance the two downward forces. The only way this is possible is for the air pressure P inside the straw at the top to be *less than* the atmosphere pressure outside the straw. (When you initially remove the straw from the water glass, a little water may leave the bottom of the straw, thus increasing the volume of trapped air and reducing its density and pressure.)

Gauge Pressure

It is important to note that tire gauges, and most other pressure gauges, register the pressure above and beyond atmospheric pressure. This is called **gauge pressure**. Thus, to get the **absolute pressure**, P , we must add the atmospheric pressure, P_0 , to the gauge pressure, P_G :

$$P = P_G + P_0.$$

If a tire gauge registers 220 kPa , the absolute pressure within the tire is $220 \text{ kPa} + 101 \text{ kPa} = 321 \text{ kPa}$, equivalent to about 3.2 atm (2.2 atm gauge pressure).

10-5 Pascal's Principle

The Earth's atmosphere exerts a pressure on all objects with which it is in contact, including other fluids. External pressure acting on a fluid is transmitted throughout that fluid. For instance, according to Eq. 10-3a, the pressure due to the water at a depth of 100 m below the surface of a lake is $P = \rho g \Delta h = (1000 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(100 \text{ m}) = 9.8 \times 10^5 \text{ N/m}^2$, or 9.7 atm. However, the total pressure at this point is due to the pressure of water plus the pressure of the air above it. Hence the total pressure (if the lake is near sea level) is 9.7 atm + 1.0 atm = 10.7 atm. This is just one example of a general principle attributed to the French philosopher and scientist Blaise Pascal (1623–1662).

Pascal's principle states that *if an external pressure is applied to a confined fluid, the pressure at every point within the fluid increases by that amount.*

A number of practical devices make use of Pascal's principle. One example is the hydraulic lift, illustrated in Fig. 10-6a, in which a small input force is used to exert a large output force by making the area of the output piston larger than the area of the input piston. To see how this works, we assume the input and output pistons are at the same height (at least approximately). Then the external input force F_{in} , by Pascal's principle, increases the pressure equally throughout. Therefore, at the same level (see Fig. 10-6a),

$$P_{\text{out}} = P_{\text{in}}$$

where the input quantities are represented by the subscript “in” and the output by “out.” Since $P = F/A$, we write the above equality as

$$\frac{F_{\text{out}}}{A_{\text{out}}} = \frac{F_{\text{in}}}{A_{\text{in}}},$$

or

$$\frac{F_{\text{out}}}{F_{\text{in}}} = \frac{A_{\text{out}}}{A_{\text{in}}}.$$

The quantity $F_{\text{out}}/F_{\text{in}}$ is called the **mechanical advantage** of the hydraulic lift, and it is equal to the ratio of the areas. For example, if the area of the output piston is 20 times that of the input cylinder, the force is multiplied by a factor of 20. Thus a force of 200 lb could lift a 4000-lb car.

FIGURE 10-6 Applications of Pascal's principle: (a) hydraulic lift; (b) hydraulic brakes in a car.

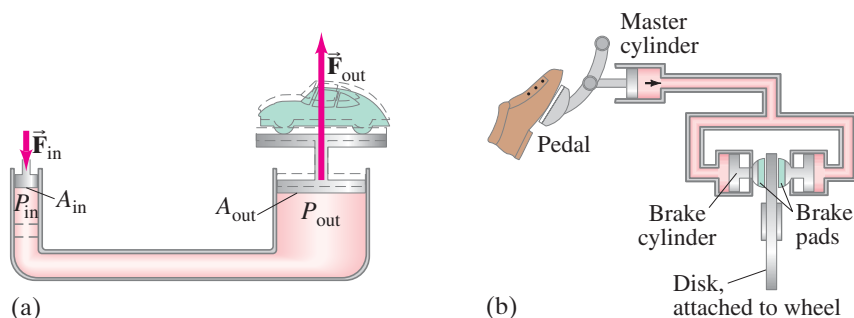


Figure 10-6b illustrates the brake system of a car. When the driver presses the brake pedal, the pressure in the master cylinder increases. This pressure increase occurs throughout the brake fluid, thus pushing the brake pads against the disk attached to the car's wheel.



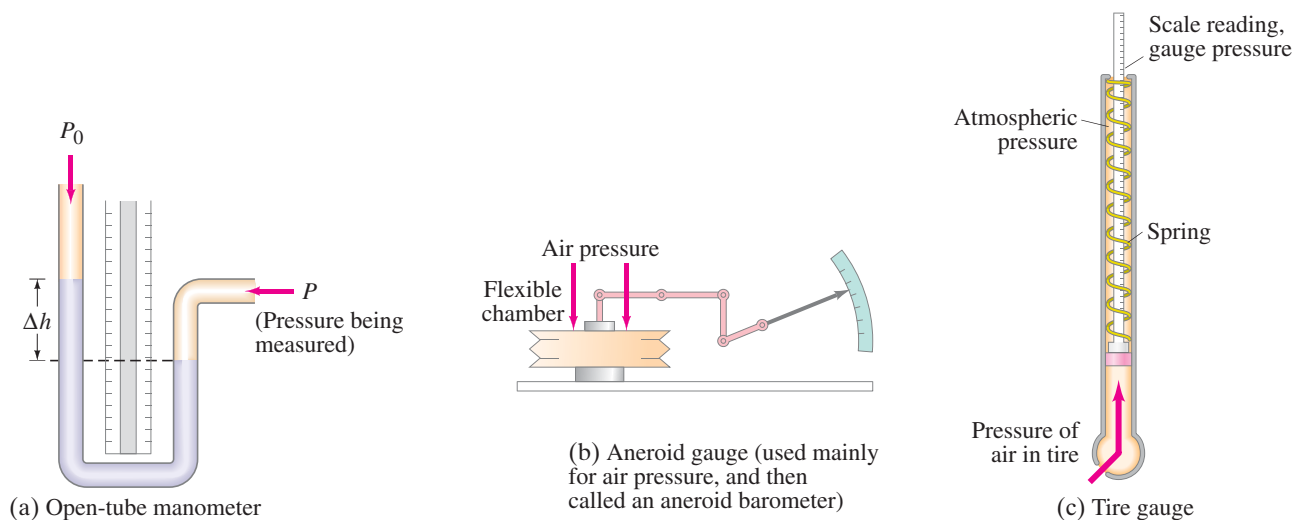


FIGURE 10-7 Pressure gauges: (a) open-tube manometer, (b) aneroid gauge, and (c) common tire pressure gauge.

10-6 Measurement of Pressure; Gauges and the Barometer

Many devices have been invented to measure pressure, some of which are shown in Fig. 10-7. The simplest is the *open-tube manometer* (Fig. 10-7a) which is a U-shaped tube partially filled with a liquid, usually mercury or water. The pressure P being measured is related (by Eq. 10-3b) to the difference in height Δh of the two levels of the liquid by the relation

$$P = P_0 + \rho g \Delta h, \quad [\text{manometer}] \quad (10-3c)$$

where P_0 is atmospheric pressure (acting on the top of the liquid in the left-hand tube), and ρ is the density of the liquid. Note that the quantity $\rho g \Delta h$ is the gauge pressure—the amount by which P exceeds atmospheric pressure P_0 . If the liquid in the left-hand column were lower than that in the right-hand column, P would have to be less than atmospheric pressure (and Δh would be negative).

Instead of calculating the product $\rho g \Delta h$, sometimes only the change in height Δh is specified. In fact, pressures are sometimes specified as so many “millimeters of mercury” (mm-Hg) or “mm of water” (mm-H₂O). The unit mm-Hg is equivalent to a pressure of 133 N/m², because $\rho g \Delta h$ for 1 mm ($= 1.0 \times 10^{-3}$ m) of mercury gives

$$\begin{aligned} \rho g \Delta h &= (13.6 \times 10^3 \text{ kg/m}^3)(9.80 \text{ m/s}^2)(1.00 \times 10^{-3} \text{ m}) \\ &= 1.33 \times 10^2 \text{ N/m}^2. \end{aligned}$$



PROBLEM SOLVING

Use SI unit in calculations:
1 Pa = 1 N/m²

The unit mm-Hg is also called the **torr** in honor of Evangelista Torricelli (1608–1647), a student of Galileo’s who invented the barometer (see top of next page). Conversion factors among the various units of pressure (an incredible nuisance!) are given in Table 10-2. It is important that only N/m² = Pa, the proper SI unit, be used in calculations involving other quantities specified in SI units.

Another type of pressure gauge is the **aneroid gauge** (Fig. 10-7b) in which the pointer is linked to the flexible ends of an evacuated thin metal chamber. In electronic gauges, the pressure may be applied to a thin metal diaphragm whose resulting deformation is translated into an electrical signal by a transducer. A common tire gauge uses a spring, as shown in Fig. 10-7c.

TABLE 10–2 Conversion Factors Between Different Units of Pressure

In Terms of $1 \text{ Pa} = 1 \text{ N/m}^2$	1 atm in Different Units
$1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2$ $= 1.013 \times 10^5 \text{ Pa} = 101.3 \text{ kPa}$	$1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2$
$1 \text{ bar} = 1.000 \times 10^5 \text{ N/m}^2$	$1 \text{ atm} = 1.013 \text{ bar}$
$1 \text{ dyne/cm}^2 = 0.1 \text{ N/m}^2$	$1 \text{ atm} = 1.013 \times 10^6 \text{ dyne/cm}^2$
$1 \text{ lb/in.}^2 = 6.90 \times 10^3 \text{ N/m}^2$	$1 \text{ atm} = 14.7 \text{ lb/in.}^2$
$1 \text{ lb/ft}^2 = 47.9 \text{ N/m}^2$	$1 \text{ atm} = 2.12 \times 10^3 \text{ lb/ft}^2$
$1 \text{ cm-Hg} = 1.33 \times 10^3 \text{ N/m}^2$	$1 \text{ atm} = 76.0 \text{ cm-Hg}$
$1 \text{ mm-Hg} = 133 \text{ N/m}^2$	$1 \text{ atm} = 760 \text{ mm-Hg}$
$1 \text{ torr} = 133 \text{ N/m}^2$	$1 \text{ atm} = 760 \text{ torr}$
$1 \text{ mm-H}_2\text{O} (4^\circ\text{C}) = 9.80 \text{ N/m}^2$	$1 \text{ atm} = 1.03 \times 10^4 \text{ mm-H}_2\text{O} (4^\circ\text{C})$ $\approx 10 \text{ m of water}$

Atmospheric pressure can be measured by a modified kind of mercury manometer with one end closed, called a mercury **barometer** (Fig. 10–8). The glass tube is completely filled with mercury and then inverted into the bowl of mercury. If the tube is long enough, the level of the mercury will drop, leaving a vacuum at the top of the tube, since atmospheric pressure can support a column of mercury only about 76 cm high (exactly 76.0 cm at standard atmospheric pressure). That is, a column of mercury 76 cm high exerts the same pressure as the atmosphere[†]:

$$P = \rho g \Delta h$$

$$= (13.6 \times 10^3 \text{ kg/m}^3)(9.80 \text{ m/s}^2)(0.760 \text{ m}) = 1.013 \times 10^5 \text{ N/m}^2 = 1.00 \text{ atm}.$$

Household barometers are usually of the aneroid type (Fig. 10–7b), either mechanical (with dial) or electronic.

A calculation similar to that just done will show that atmospheric pressure can maintain a column of water 10.3 m high in a tube whose top is under vacuum (Fig. 10–9). No matter how good a vacuum pump is, water cannot be made to rise more than about 10 m under normal atmospheric pressure. To pump water out of deep mine shafts with a vacuum pump requires multiple stages for depths greater than 10 m. Galileo studied this problem, and his student Torricelli was the first to explain it. The point is that a pump does not really suck water up a tube—it merely reduces the pressure at the top of the tube. Atmospheric air pressure *pushes* the water up the tube if the top end is at low pressure (under a vacuum), just as it is air pressure that pushes (or maintains) the mercury 76 cm high in a barometer. [Force pumps, Section 10–14, can push higher.]

CONCEPTUAL EXAMPLE 10–5

Suction. A novice engineer proposes suction cup shoes for space shuttle astronauts working on the exterior of a spacecraft. Having just studied this Chapter, you gently remind him of the fallacy of this plan. What is it?

RESPONSE Suction cups work by pushing out the air underneath the cup. What holds the suction cup in place is the air pressure outside it. (This can be a substantial force when on Earth. For example, a 10-cm-diameter suction cup has an area of $7.9 \times 10^{-3} \text{ m}^2$. The force of the atmosphere on it is $(7.9 \times 10^{-3} \text{ m}^2)(1.0 \times 10^5 \text{ N/m}^2) \approx 800 \text{ N}$, about 180 lbs!) But in outer space, there is no air pressure to push the suction cup onto the spacecraft.

We sometimes mistakenly think of suction as something we actively do. For example, we intuitively think that we pull the soda up through a straw. Instead, what we do is lower the pressure at the top of the straw, and the atmosphere *pushes* the soda up the straw.

[†]This calculation confirms the entry in Table 10–2, $1 \text{ atm} = 76.0 \text{ cm-Hg}$.

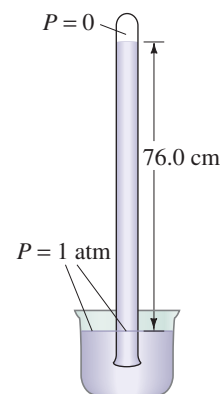


FIGURE 10–8 A mercury barometer, invented by Torricelli, is shown here when the air pressure is standard atmospheric, 76.0 cm-Hg.

FIGURE 10–9 A water barometer: a full tube of water (longer than 10 m), closed at the top, is inserted into a tub of water. When the submerged bottom end of the tube is unplugged, some water flows out of the tube into the tub, leaving a vacuum at the top of the tube above the water's upper surface. Why? Because air pressure can support a column of water only 10 m high.

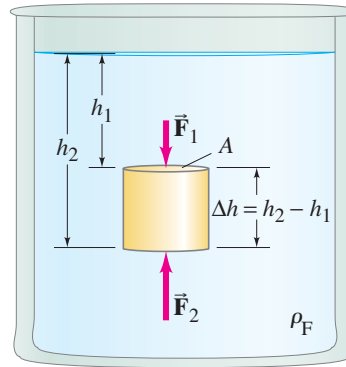


10-7 Buoyancy and Archimedes' Principle

Objects submerged in a fluid appear to weigh less than they do when outside the fluid. For example, a large rock that you would have difficulty lifting off the ground can often be easily lifted from the bottom of a stream. When you lift the rock through the surface of the water, it suddenly seems to be much heavier. Many objects, such as wood, float on the surface of water. These are two examples of **buoyancy**. In each example, the force of gravity is acting downward. But in addition, an upward *buoyant force* is exerted by the liquid. The buoyant force on fish and underwater divers almost exactly balances the force of gravity downward, and allows them to “hover” in equilibrium.

The buoyant force occurs because the pressure in a fluid increases with depth. Thus the upward pressure on the bottom surface of a submerged object is greater than the downward pressure on its top surface. To see this effect, consider a cylinder of height Δh whose top and bottom ends have an area A and which is completely submerged in a fluid of density ρ_F , as shown in Fig. 10-10. The fluid exerts a pressure $P_1 = \rho_F g h_1$ at the top surface of the cylinder (Eq. 10-3a).

FIGURE 10-10 Determination of the buoyant force.



The force due to this pressure on top of the cylinder is $F_1 = P_1 A = \rho_F g h_1 A$, and it is directed downward. Similarly, the fluid exerts an upward force on the bottom of the cylinder equal to $F_2 = P_2 A = \rho_F g h_2 A$. The net force on the cylinder exerted by the fluid pressure, which is the **buoyant force**, \vec{F}_B , acts upward and has the magnitude

$$\begin{aligned} F_B &= F_2 - F_1 = \rho_F g A (h_2 - h_1) \\ &= \rho_F g A \Delta h \\ &= \rho_F V g \\ &= m_F g, \end{aligned}$$

where $V = A \Delta h$ is the volume of the cylinder; the product $\rho_F V$ is the mass of the fluid displaced, and $\rho_F V g = m_F g$ is the weight of fluid which takes up a volume equal to the volume of the cylinder. Thus the buoyant force on the cylinder is equal to the weight of fluid displaced by the cylinder.

This result is valid no matter what the shape of the object. Its discovery is credited to Archimedes (287?–212 B.C.), and it is called **Archimedes' principle**:

the buoyant force on an object immersed in a fluid is equal to the weight of the fluid displaced by that object.

By “fluid displaced,” we mean a volume of fluid equal to the submerged volume of the object (or that part of the object that is submerged). If the object is placed in a glass or tub initially filled to the brim with water, the water that flows over the top represents the water displaced by the object.

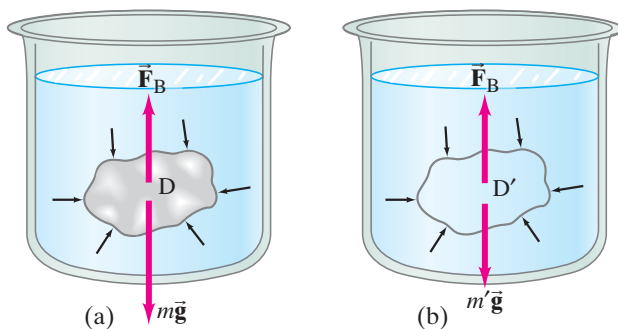


FIGURE 10-11
Archimedes' principle.

We can derive Archimedes' principle in general by the following simple but elegant argument. The irregularly shaped object D shown in Fig. 10-11a is acted on by the force of gravity (its weight, $m\vec{g}$, downward) and the buoyant force, \vec{F}_B , upward. We wish to determine F_B . To do so, we next consider a body (D' in Fig. 10-11b), this time made of the fluid itself, with the same shape and size as the original object, and located at the same depth. You might think of this body of fluid as being separated from the rest of the fluid by an imaginary membrane. The buoyant force F_B on this body of fluid will be exactly the same as that on the original object since the surrounding fluid, which exerts F_B , is in exactly the same configuration. This body of fluid D' is in equilibrium (the fluid as a whole is at rest). Therefore, $F_B = m'g$, where $m'g$ is the weight of the body of fluid D' . Hence the buoyant force F_B is equal to the weight of the body of fluid whose volume equals the volume of the original submerged object, which is Archimedes' principle.

Archimedes' discovery was made by experiment. What we have done is show that Archimedes' principle can be derived from Newton's laws.

CONCEPTUAL EXAMPLE 10-6 Two pails of water. Consider two identical pails of water filled to the brim. One pail contains only water, the other has a piece of wood floating in it. Which pail has the greater weight?

RESPONSE Both pails weigh the same. Recall Archimedes' principle: the wood displaces a volume of water with weight equal to the weight of the wood. Some water will overflow the pail, but Archimedes' principle tells us the spilled water has weight equal to the weight of the wood; so the pails have the same weight.

EXAMPLE 10-7 Recovering a submerged statue. A 70-kg ancient statue lies at the bottom of the sea. Its volume is $3.0 \times 10^4 \text{ cm}^3$. How much force is needed to lift it (without acceleration)?

APPROACH The force F needed to lift the statue is equal to the statue's weight mg minus the buoyant force F_B . Figure 10-12 is the free-body diagram.

SOLUTION We apply Newton's second law, $\Sigma F = ma = 0$, which gives $F + F_B - mg = 0$ or

$$F = mg - F_B.$$

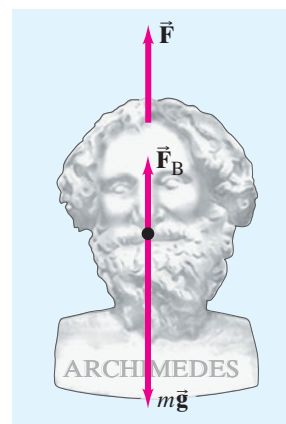
The buoyant force on the statue due to the water is equal to the weight of $3.0 \times 10^4 \text{ cm}^3 = 3.0 \times 10^{-2} \text{ m}^3$ of water (for seawater, $\rho = 1.025 \times 10^3 \text{ kg/m}^3$):

$$\begin{aligned} F_B &= m_{\text{H}_2\text{O}} g = \rho_{\text{H}_2\text{O}} V g = (1.025 \times 10^3 \text{ kg/m}^3)(3.0 \times 10^{-2} \text{ m}^3)(9.8 \text{ m/s}^2) \\ &= 3.0 \times 10^2 \text{ N}, \end{aligned}$$

where we use the chemical symbol for water, H_2O , as a subscript. The weight of the statue is $mg = (70 \text{ kg})(9.8 \text{ m/s}^2) = 6.9 \times 10^2 \text{ N}$. Hence the force F needed to lift it is $690 \text{ N} - 300 \text{ N} = 390 \text{ N}$. It is as if the statue had a mass of only $(390 \text{ N})/(9.8 \text{ m/s}^2) = 40 \text{ kg}$.

NOTE Here $F = 390 \text{ N}$ is the force needed to lift the statue without acceleration when it is under water. As the statue comes *out* of the water, the force F increases, reaching 690 N when the statue is fully out of the water.

FIGURE 10-12 Example 10-7. The force needed to lift the statue is \vec{F} .



Archimedes is said to have discovered his principle in his bath while thinking how he might determine whether the king's new crown was pure gold or a fake. Gold has a specific gravity of 19.3, somewhat higher than that of most metals, but a determination of specific gravity or density is not readily done directly because, even if the mass is known, the volume of an irregularly shaped object is not easily calculated. However, if the object is weighed in air ($= w$) and also “weighed” while it is under water ($= w'$), the density can be determined using Archimedes' principle, as the following Example shows. The quantity w' is called the **apparent weight** in water, and is what a scale reads when the object is submerged in water (see Fig. 10–13); w' equals the true weight ($w = mg$) minus the buoyant force.

EXAMPLE 10–8 Archimedes: Is the crown gold? When a crown of mass 14.7 kg is submerged in water, an accurate scale reads only 13.4 kg. Is the crown made of gold?

APPROACH If the crown is gold, its density and specific gravity must be very high, $SG = 19.3$ (see Section 10–2 and Table 10–1). We determine the specific gravity using Archimedes' principle and the two free-body diagrams shown in Fig. 10–13.

SOLUTION The *apparent weight* of the submerged object (the crown) is w' (what the scale reads), and is the force pulling down on the scale hook. By Newton's third law, w' equals the force F'_T that the scale exerts on the crown in Fig. 10–13b. The sum of the forces on the crown is zero, so w' equals the actual weight $w (= mg)$ minus the buoyant force F_B :

$$w' = F'_T = w - F_B$$

so

$$w - w' = F_B.$$

Let V be the volume of the completely submerged object and ρ_O the object's density (so $\rho_O V$ is its mass), and let ρ_F be the density of the fluid (water). Then $(\rho_F V)g$ is the weight of fluid displaced ($= F_B$). Now we can write

$$\begin{aligned} w &= mg = \rho_O Vg \\ w - w' &= F_B = \rho_F Vg. \end{aligned}$$

We divide these two equations and obtain

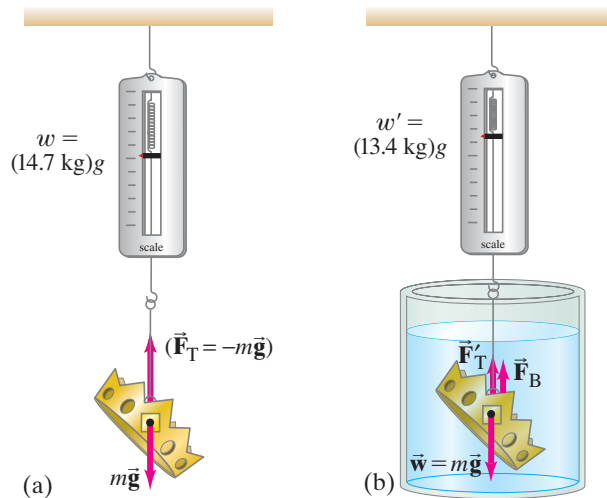
$$\frac{w}{w - w'} = \frac{\rho_O Vg}{\rho_F Vg} = \frac{\rho_O}{\rho_F}.$$

We see that $w/(w - w')$ is equal to the specific gravity of the object (the crown) if the fluid in which it is submerged is water ($\rho_F = 1.00 \times 10^3 \text{ kg/m}^3$). Thus

$$\frac{\rho_O}{\rho_{\text{H}_2\text{O}}} = \frac{w}{w - w'} = \frac{(14.7 \text{ kg})g}{(14.7 \text{ kg} - 13.4 \text{ kg})g} = \frac{14.7 \text{ kg}}{1.3 \text{ kg}} = 11.3.$$

This corresponds to a density of $11,300 \text{ kg/m}^3$. The crown is not gold, but seems to be made of lead (see Table 10–1).

FIGURE 10–13 (a) A scale reads the mass of an object in air—in this case the crown of Example 10–8. All objects are at rest, so the tension F_T in the connecting cord equals the weight w of the object: $F_T = mg$. We show the free-body diagram of the crown, and F_T is what causes the scale reading (it is equal to the net downward force on the scale, by Newton's third law). (b) Submerged, the crown has an additional force on it, the buoyant force F_B . The net force is zero, so $F'_T + F_B = mg (= w)$. The scale now reads $m' = 13.4 \text{ kg}$, where m' is related to the effective weight by $w' = m'g$. Thus $F'_T = w' = w - F_B$.



Archimedes' principle applies equally well to objects that float, such as wood. In general, *an object floats on a fluid if its density (ρ_O) is less than that of the fluid (ρ_F)*. This is readily seen from Fig. 10–14a, where a submerged log of mass m_O will experience a net upward force and float to the surface if $F_B > m_O g$; that is, if $\rho_F V g > \rho_O V g$ or $\rho_F > \rho_O$. At equilibrium—that is, when floating—the buoyant force on an object has magnitude equal to the weight of the object. For example, a log whose specific gravity is 0.60 and whose volume is 2.0 m^3 has a mass

$$m_O = \rho_O V = (0.60 \times 10^3 \text{ kg/m}^3)(2.0 \text{ m}^3) = 1200 \text{ kg}.$$

If the log is fully submerged, it will displace a mass of water

$$m_F = \rho_F V = (1000 \text{ kg/m}^3)(2.0 \text{ m}^3) = 2000 \text{ kg}.$$

Hence the buoyant force on the log will be greater than its weight, and it will float upward to the surface (Fig. 10–14). The log will come to equilibrium when it displaces 1200 kg of water, which means that 1.2 m^3 of its volume will be submerged. This 1.2 m^3 corresponds to 60% of the volume of the log ($= 1.2/2.0 = 0.60$), so 60% of the log is submerged.

In general when an object floats, we have $F_B = m_O g$, which we can write as (see Fig. 10–15)

$$\begin{aligned} F_B &= m_O g \\ \rho_F V_{\text{displ}} g &= \rho_O V_O g, \end{aligned}$$

where V_O is the full volume of the object and V_{displ} is the volume of fluid it displaces (= volume submerged). Thus

$$\frac{V_{\text{displ}}}{V_O} = \frac{\rho_O}{\rho_F}.$$

That is, the fraction of the object submerged is given by the ratio of the object's density to that of the fluid. If the fluid is water, this fraction equals the specific gravity of the object.

EXAMPLE 10–9 Hydrometer calibration. A **hydrometer** is a simple instrument used to measure the specific gravity of a liquid by indicating how deeply the instrument sinks in the liquid. A particular hydrometer (Fig. 10–16) consists of a glass tube, weighted at the bottom, which is 25.0 cm long and 2.00 cm^2 in cross-sectional area, and has a mass of 45.0 g. How far from the weighted end should the 1.000 mark be placed?

APPROACH The hydrometer will float in water if its density ρ is less than $\rho_{\text{H}_2\text{O}} = 1.000 \text{ g/cm}^3$, the density of water. The fraction of the hydrometer submerged ($V_{\text{displaced}}/V_{\text{total}}$) is equal to the density ratio $\rho/\rho_{\text{H}_2\text{O}}$.

SOLUTION The hydrometer has an overall density

$$\rho = \frac{m}{V} = \frac{45.0 \text{ g}}{(2.00 \text{ cm}^2)(25.0 \text{ cm})} = 0.900 \text{ g/cm}^3.$$

Thus, when placed in water, it will come to equilibrium when 0.900 of its volume is submerged. Since it is of uniform cross section, $(0.900)(25.0 \text{ cm}) = 22.5 \text{ cm}$ of its length will be submerged. The specific gravity of water is defined to be 1.000, so the mark should be placed 22.5 cm from the weighted end.

NOTE Hydrometers can be used to measure the density of liquids like car antifreeze coolant, car battery acid (a measure of its charge), wine fermenting in casks, and many others.

EXERCISE C Which of the following objects, submerged in water, experiences the largest magnitude of the buoyant force? (a) A 1-kg helium balloon; (b) 1 kg of wood; (c) 1 kg of ice; (d) 1 kg of iron; (e) all the same.

EXERCISE D Which of the following objects, submerged in water, experiences the largest magnitude of the buoyant force? (a) A 1-m^3 helium balloon; (b) 1 m^3 of wood; (c) 1 m^3 of ice; (d) 1 m^3 of iron; (e) all the same.

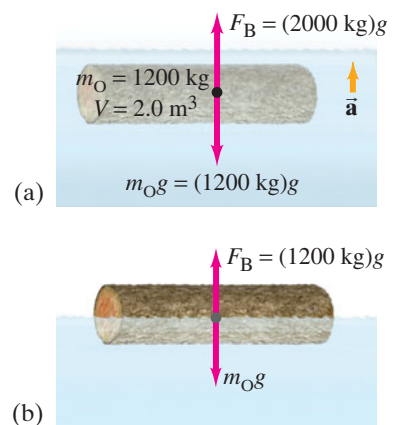


FIGURE 10–14 (a) The fully submerged log accelerates upward because $F_B > m_O g$. It comes to equilibrium (b) when $\Sigma F = 0$, so $F_B = m_O g = (1200 \text{ kg})g$. Then 1200 kg, or 1.2 m^3 , of water is displaced.

FIGURE 10–15 An object floating in equilibrium: $F_B = m_O g$.

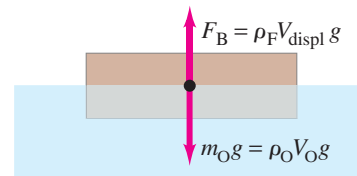
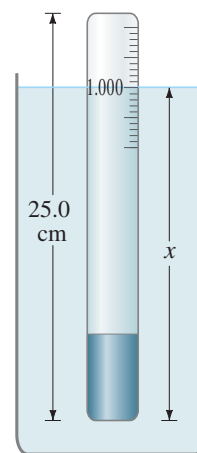


FIGURE 10–16 A hydrometer. Example 10–9.



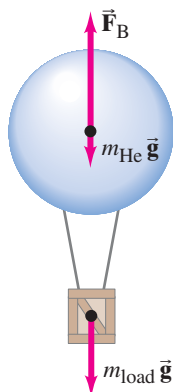


FIGURE 10-17 Example 10-10.

Archimedes' principle is also useful in geology. According to the theories of plate tectonics and continental drift, the continents float on a fluid "sea" of slightly deformable rock (mantle rock). Some interesting calculations can be done using very simple models, which we consider in the Problems at the end of the Chapter.

Air is a fluid, and it too exerts a buoyant force. Ordinary objects weigh less in air than they do in a vacuum. Because the density of air is so small, the effect for ordinary solids is slight. There are objects, however, that *float* in air—helium-filled balloons, for example, because the density of helium is less than the density of air.

EXAMPLE 10-10 Helium balloon. What volume V of helium is needed if a balloon is to lift a load of 180 kg (including the weight of the empty balloon)?

APPROACH The buoyant force on the helium balloon, F_B , which is equal to the weight of displaced air, must be at least equal to the weight of the helium plus the weight of the balloon and load (Fig. 10-17). Table 10-1 gives the density of helium as 0.179 kg/m^3 .

SOLUTION The buoyant force must have a minimum value of

$$F_B = (m_{\text{He}} + 180 \text{ kg})g.$$

This equation can be written in terms of density using Archimedes' principle:

$$\rho_{\text{air}} V g = (\rho_{\text{He}} V + 180 \text{ kg})g.$$

Solving now for V , we find

$$V = \frac{180 \text{ kg}}{\rho_{\text{air}} - \rho_{\text{He}}} = \frac{180 \text{ kg}}{(1.29 \text{ kg/m}^3 - 0.179 \text{ kg/m}^3)} = 160 \text{ m}^3.$$

NOTE This is the minimum volume needed near the Earth's surface, where $\rho_{\text{air}} = 1.29 \text{ kg/m}^3$. To reach a high altitude, a greater volume would be needed since the density of air decreases with altitude.

CONCEPTUAL EXAMPLE 10-11 Throwing a rock overboard. A rowboat carrying a large granite rock floats in a small lake. If the rock ($\text{SG} \approx 3$, Table 10-1) is thrown overboard and sinks, does the lake level drop, rise, or stay the same?

RESPONSE Together the boat and rock float, so the buoyant force on them equals their total weight. The boat and rock displace a mass of water whose weight is equal to the weight of boat plus rock. When the rock is thrown into the lake, it displaces only its own volume, which is smaller than the volume of water the rock displaced when in the boat ($\approx \frac{1}{3}$ as much because the rock's density is ≈ 3 times greater than water). So less lake water is displaced and the water level of the lake *drops* when the rock is in the lake.

Maybe numbers can help. Suppose the boat and the rock each has a mass of 60 kg. Then the boat carrying the rock displaces 120 kg of water, which is a volume of 0.12 m^3 ($\rho = 1000 \text{ kg/m}^3$ for water, Table 10-1). When the rock is thrown into the lake, the boat alone now displaces 0.06 m^3 . The rock displaces only its own volume of 0.02 m^3 ($\rho = m/V \approx 3$ so $V \approx 0.06 \text{ m}^3/3$). Thus a total of 0.08 m^3 of water is displaced. Less water is displaced so the water level of the lake drops.

EXERCISE E If you throw a flat 60-kg aluminum plate into water, the plate sinks. But if that aluminum is shaped into a rowboat, it floats. Explain.

10-8 Fluids in Motion; Flow Rate and the Equation of Continuity

We now turn to the subject of fluids in motion, which is called **fluid dynamics**, or (especially if the fluid is water) **hydrodynamics**.

We can distinguish two main types of fluid flow. If the flow is smooth, such that neighboring layers of the fluid slide by each other smoothly, the flow is said to be **streamline** or **laminar flow**.[†] In streamline flow, each particle of the fluid follows a smooth path, called a **streamline**, and these paths do not cross one another (Fig. 10-18a).

[†]The word laminar means "in layers."

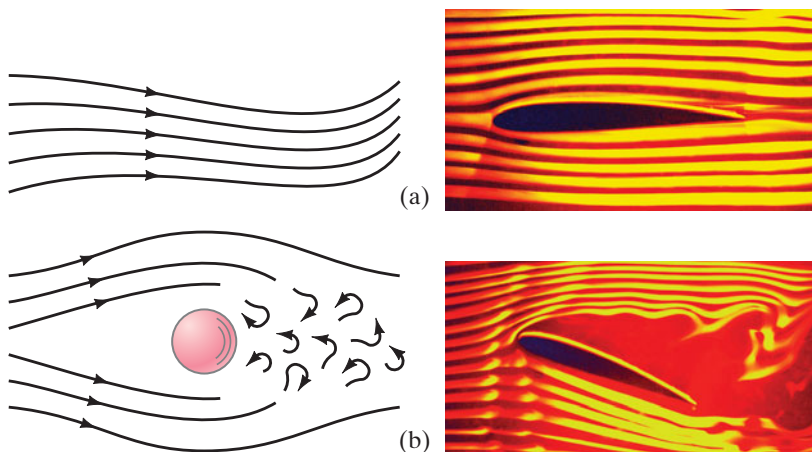


FIGURE 10-18 (a) Streamline, or laminar, flow; (b) turbulent flow. The photos show airflow around an airfoil or airplane wing (more in Section 10-10).

Above a certain speed, the flow becomes turbulent. **Turbulent flow** is characterized by erratic, small, whirlpool-like circles called *eddy currents* or *eddies* (Fig. 10-18b). Eddies absorb a great deal of energy, and although a certain amount of internal friction called **viscosity** is present even during streamline flow, it is much greater when the flow is turbulent. A few tiny drops of ink or food coloring dropped into a moving liquid can quickly reveal whether the flow is streamline or turbulent.

Let us consider the steady laminar flow of a fluid through an enclosed tube or pipe as shown in Fig. 10-19. First we determine how the speed of the fluid changes when the diameter of the tube changes. The mass **flow rate** is defined as the mass Δm of fluid that passes a given point per unit time Δt :

$$\text{mass flow rate} = \frac{\Delta m}{\Delta t}.$$

In Fig. 10-19, the volume of fluid passing point 1 (through area A_1) in a time Δt is $A_1 \Delta \ell_1$, where $\Delta \ell_1$ is the distance the fluid moves in time Δt . The velocity[†] of fluid (density ρ_1) passing point 1 is $v_1 = \Delta \ell_1 / \Delta t$. Then the mass flow rate $\Delta m_1 / \Delta t$ through area A_1 is

$$\frac{\Delta m_1}{\Delta t} = \frac{\rho_1 \Delta V_1}{\Delta t} = \frac{\rho_1 A_1 \Delta \ell_1}{\Delta t} = \rho_1 A_1 v_1,$$

where $\Delta V_1 = A_1 \Delta \ell_1$ is the volume of mass Δm_1 . Similarly, at point 2 (through area A_2), the flow rate is $\rho_2 A_2 v_2$. Since no fluid flows in or out the sides of the tube, the flow rates through A_1 and A_2 must be equal. Thus

$$\frac{\Delta m_1}{\Delta t} = \frac{\Delta m_2}{\Delta t},$$

and

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2. \quad (10-4a)$$

This is called the **equation of continuity**.

If the fluid is incompressible (ρ doesn't change with pressure), which is an excellent approximation for liquids under most circumstances (and sometimes for gases as well), then $\rho_1 = \rho_2$, and the equation of continuity becomes

$$A_1 v_1 = A_2 v_2. \quad [\rho = \text{constant}] \quad (10-4b)$$

The product Av represents the *volume rate of flow* (volume of fluid passing a given point per second), since $\Delta V / \Delta t = A \Delta \ell / \Delta t = Av$, which in SI units is m^3/s . Equation 10-4b tells us that where the cross-sectional area is large, the velocity is small, and where the area is small, the velocity is large. That this is reasonable can be seen by looking at a river. A river flows slowly through a meadow where it is broad, but speeds up to torrential speed when passing through a narrow gorge.

[†]If there were no viscosity, the velocity would be the same across a cross section of the tube. Real fluids have viscosity, and this internal friction causes different layers of the fluid to flow at different speeds. In this case v_1 and v_2 represent the average speeds at each cross section.

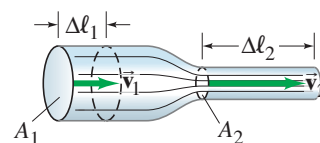
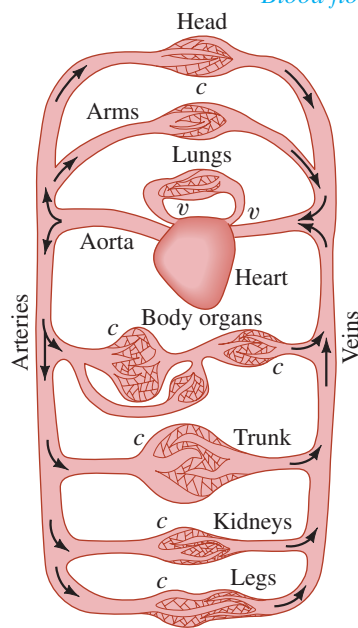


FIGURE 10-19 Fluid flow through a pipe of varying diameter.

PHYSICS APPLIED

Blood flow



v = valves
 c = capillaries

FIGURE 10-20 Human circulatory system.

PHYSICS APPLIED

Heating duct

FIGURE 10-21 Example 10-13.

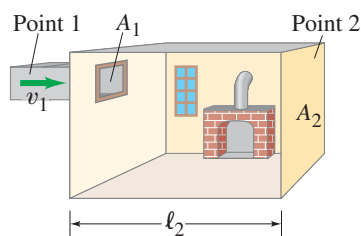
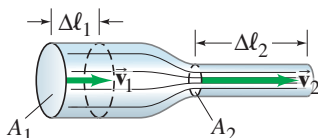


FIGURE 10-19 (Repeated.) Fluid flow through a pipe of varying diameter.



EXAMPLE 10-12 ESTIMATE Blood flow. In humans, blood flows from the heart into the aorta, from which it passes into the major arteries, Fig. 10-20. These branch into the small arteries (arterioles), which in turn branch into myriads of tiny capillaries. The blood returns to the heart via the veins. The radius of the aorta is about 1.2 cm, and the blood passing through it has a speed of about 40 cm/s. A typical capillary has a radius of about 4×10^{-4} cm, and blood flows through it at a speed of about 5×10^{-4} m/s. Estimate the number of capillaries that are in the body.

APPROACH We assume the density of blood doesn't vary significantly from the aorta to the capillaries. By the equation of continuity, the volume flow rate in the aorta must equal the volume flow rate through *all* the capillaries. The total area of all the capillaries is given by the area of a typical capillary multiplied by the total number N of capillaries.

SOLUTION Let A_1 be the area of the aorta and A_2 be the area of *all* the capillaries through which blood flows. Then $A_2 = N\pi r_{\text{cap}}^2$, where $r_{\text{cap}} \approx 4 \times 10^{-4}$ cm is the estimated average radius of one capillary. From the equation of continuity (Eq. 10-4b), we have

$$v_2 A_2 = v_1 A_1$$

$$v_2 N\pi r_{\text{cap}}^2 = v_1 \pi r_{\text{aorta}}^2$$

so

$$N = \frac{v_1 r_{\text{aorta}}^2}{v_2 r_{\text{cap}}^2} = \left(\frac{0.40 \text{ m/s}}{5 \times 10^{-4} \text{ m/s}} \right) \left(\frac{1.2 \times 10^{-2} \text{ m}}{4 \times 10^{-6} \text{ m}} \right)^2 \approx 7 \times 10^9,$$

or on the order of 10 billion capillaries.

EXAMPLE 10-13 Heating duct to a room. What area must a heating duct have if air moving 3.0 m/s along it can replenish the air every 15 minutes in a room of volume 300 m^3 ? Assume the air's density remains constant.

APPROACH We apply the equation of continuity at constant density, Eq. 10-4b, to the air that flows through the duct (point 1 in Fig. 10-21) and then into the room (point 2). The volume flow rate in the room equals the volume of the room divided by the 15-min replenishing time.

SOLUTION Consider the room as a large section of the duct, Fig. 10-21, and think of air equal to the volume of the room as passing by point 2 in $t = 15 \text{ min} = 900 \text{ s}$. Reasoning in the same way we did to obtain Eq. 10-4a (changing Δt to t), we write $v_2 = \ell_2/t$ so $A_2 v_2 = A_2 \ell_2/t = V_2/t$, where V_2 is the volume of the room. Then the equation of continuity becomes $A_1 v_1 = A_2 v_2 = V_2/t$ and

$$A_1 = \frac{V_2}{v_1 t} = \frac{300 \text{ m}^3}{(3.0 \text{ m/s})(900 \text{ s})} = 0.11 \text{ m}^2.$$

NOTE If the duct is square, then each side has length $\ell = \sqrt{A} = 0.33 \text{ m}$, or 33 cm. A rectangular duct $20 \text{ cm} \times 55 \text{ cm}$ will also do.

10-9 Bernoulli's Equation

Have you ever wondered why an airplane can fly, or how a sailboat can move against the wind? These are examples of a principle worked out by Daniel Bernoulli (1700–1782) concerning fluids in motion. In essence, **Bernoulli's principle** states that *where the velocity of a fluid is high, the pressure is low, and where the velocity is low, the pressure is high*. For example, if the pressure in the fluid is measured at points 1 and 2 of Fig. 10-19, it will be found that the pressure is lower at point 2, where the velocity is greater, than it is at point 1, where the velocity is smaller. At first glance, this might seem strange; you might expect that the greater speed at point 2 would imply a higher pressure. But this cannot be the case:

if the pressure in the fluid at point 2 were higher than at point 1, this higher pressure would slow the fluid down, whereas in fact it has sped up in going from point 1 to point 2. Thus the pressure at point 2 must be less than at point 1, to be consistent with the fact that the fluid accelerates.

To help clarify any misconceptions, a faster fluid might indeed exert a greater force bouncing off an obstacle placed in its path. But that is not what we mean by the pressure in a fluid. We are examining smooth streamline flow, with no obstacles that interrupt the flow. The fluid pressure is exerted on the walls of a tube or pipe, or on the surface of a material the fluid passes over.

Bernoulli developed an equation that expresses this principle quantitatively. To derive Bernoulli's equation, we assume the flow is steady and laminar, the fluid is incompressible, and the viscosity is small enough to be ignored. To be general, we assume the fluid is flowing in a tube of nonuniform cross section that varies in height above some reference level, Fig. 10–22. We will consider the volume of fluid shown in color and calculate the work done to move it from the position shown in Fig. 10–22a to that shown in Fig. 10–22b. In this process, fluid entering area A_1 flows a distance $\Delta\ell_1$ and forces the fluid at area A_2 to move a distance $\Delta\ell_2$. The fluid to the left of area A_1 exerts a pressure P_1 on our section of fluid and does an amount of work

$$W_1 = F_1 \Delta\ell_1 = P_1 A_1 \Delta\ell_1,$$

(since $P = F/A$). At point 2, the work done on our section of fluid is

$$W_2 = -P_2 A_2 \Delta\ell_2.$$

The negative sign is present because the force exerted on the fluid is opposite to the displacement. Work is also done on the fluid by the force of gravity. The net effect of the process shown in Fig. 10–22 is to move a mass m of volume $A_1 \Delta\ell_1$ ($= A_2 \Delta\ell_2$, since the fluid is incompressible) from point 1 to point 2, so the work done by gravity is

$$W_3 = -mg(y_2 - y_1),$$

where y_1 and y_2 are heights of the center of the tube above some (arbitrary) reference level. In the case shown in Fig. 10–22, this term is negative since the motion is uphill against the force of gravity. The net work W done on the fluid is thus

$$W = W_1 + W_2 + W_3$$

$$W = P_1 A_1 \Delta\ell_1 - P_2 A_2 \Delta\ell_2 - mgy_2 + mgy_1.$$

According to the work-energy principle (Section 6–3), the net work done on a system is equal to its change in kinetic energy. Hence

$$\frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2 = P_1 A_1 \Delta\ell_1 - P_2 A_2 \Delta\ell_2 - mgy_2 + mgy_1.$$

The mass m has volume $A_1 \Delta\ell_1 = A_2 \Delta\ell_2$ for an incompressible fluid. Thus we can substitute $m = \rho A_1 \Delta\ell_1 = \rho A_2 \Delta\ell_2$, and then divide through by $A_1 \Delta\ell_1 = A_2 \Delta\ell_2$, to obtain

$$\frac{1}{2}\rho v_2^2 - \frac{1}{2}\rho v_1^2 = P_1 - P_2 - \rho gy_2 + \rho gy_1,$$

which we rearrange to get

$$P_2 + \frac{1}{2}\rho v_2^2 + \rho gy_2 = P_1 + \frac{1}{2}\rho v_1^2 + \rho gy_1. \quad (10-5) \quad \text{Bernoulli's equation}$$

This is **Bernoulli's equation**. Since points 1 and 2 can be any two points along a tube of flow, Bernoulli's equation can be written as

$$P + \frac{1}{2}\rho v^2 + \rho gy = \text{constant}$$

at every point in the fluid, where y is the height of the center of the tube above a fixed reference level. [Note that if there is no flow ($v_1 = v_2 = 0$), then Eq. 10–5 reduces to the hydrostatic equation, Eq. 10–3b or c: $P_1 - P_2 = \rho g(y_2 - y_1)$.]

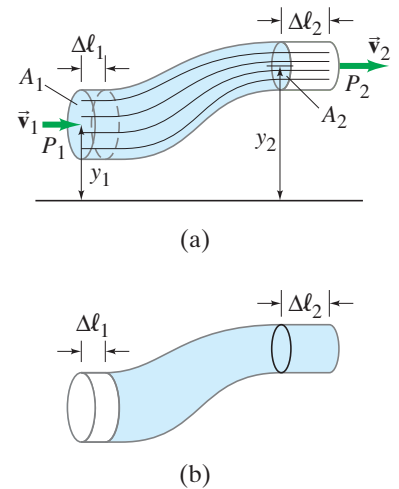


FIGURE 10–22 Fluid flow: for derivation of Bernoulli's equation.

Bernoulli's equation is an expression of the law of energy conservation, since we derived it from the work-energy principle.

EXERCISE F As water in a level pipe passes from a narrow cross section of pipe to a wider cross section, how does the pressure against the walls change?

PHYSICS APPLIED
Hot-water heating system

EXAMPLE 10-14 Flow and pressure in a hot-water heating system.

Water circulates throughout a house in a hot-water heating system. If the water is pumped at a speed of 0.50 m/s through a 4.0-cm-diameter pipe in the basement under a pressure of 3.0 atm, what will be the flow speed and pressure in a 2.6-cm-diameter pipe on the second floor 5.0 m above? Assume the pipes do not divide into branches.

APPROACH We use the equation of continuity at constant density to determine the flow speed on the second floor, and then Bernoulli's equation to find the pressure.

SOLUTION We take v_2 in the equation of continuity, Eq. 10-4, as the flow speed on the second floor, and v_1 as the flow speed in the basement. Noting that the areas are proportional to the radii squared ($A = \pi r^2$), we obtain

$$v_2 = \frac{v_1 A_1}{A_2} = \frac{v_1 \pi r_1^2}{\pi r_2^2} = (0.50 \text{ m/s}) \frac{(0.020 \text{ m})^2}{(0.013 \text{ m})^2} = 1.2 \text{ m/s}.$$

To find the pressure on the second floor, we use Bernoulli's equation (Eq. 10-5):

$$\begin{aligned} P_2 &= P_1 + \rho g(y_1 - y_2) + \frac{1}{2} \rho (v_1^2 - v_2^2) \\ &= (3.0 \times 10^5 \text{ N/m}^2) + (1.0 \times 10^3 \text{ kg/m}^3)(9.8 \text{ m/s}^2)(-5.0 \text{ m}) \\ &\quad + \frac{1}{2} (1.0 \times 10^3 \text{ kg/m}^3)[(0.50 \text{ m/s})^2 - (1.2 \text{ m/s})^2] \\ &= (3.0 \times 10^5 \text{ N/m}^2) - (4.9 \times 10^4 \text{ N/m}^2) - (6.0 \times 10^2 \text{ N/m}^2) \\ &= 2.5 \times 10^5 \text{ N/m}^2 = 2.5 \text{ atm}. \end{aligned}$$

NOTE The velocity term contributes very little in this case.

10-10 Applications of Bernoulli's Principle: Torricelli, Airplanes, Baseballs, Blood Flow

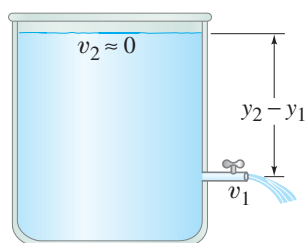


FIGURE 10-23 Torricelli's theorem: $v_1 = \sqrt{2g(y_2 - y_1)}$.

Bernoulli's equation can be applied to many situations. One example is to calculate the velocity, v_1 , of a liquid flowing out of a spigot at the bottom of a reservoir, Fig. 10-23. We choose point 2 in Eq. 10-5 to be the top surface of the liquid. Assuming the diameter of the reservoir is large compared to that of the spigot, v_2 will be almost zero. Points 1 (the spigot) and 2 (top surface) are open to the atmosphere, so the pressure at both points is equal to atmospheric pressure: $P_1 = P_2$. Then Bernoulli's equation becomes

$$\frac{1}{2} \rho v_1^2 + \rho g y_1 = \rho g y_2$$

or

$$v_1 = \sqrt{2g(y_2 - y_1)}. \quad (10-6)$$

This result is called **Torricelli's theorem**. Although it is seen to be a special case of Bernoulli's equation, it was discovered a century earlier by Evangelista Torricelli. Equation 10-6 tells us that the liquid leaves the spigot with the same speed that a freely falling object would attain if falling from the same height. This should not be too surprising since the derivation of Bernoulli's equation relies on the conservation of energy.

Another special case of Bernoulli's equation arises when a fluid is flowing horizontally with no appreciable change in height; that is, $y_1 = y_2$. Then Eq. 10-5 becomes

$$P_1 + \frac{1}{2}\rho v_1^2 = P_2 + \frac{1}{2}\rho v_2^2, \quad (10-7)$$

which tells us quantitatively that the speed is high where the pressure is low, and vice versa. It explains many common phenomena, some of which are illustrated in Figs. 10-24 to 10-30. The pressure in the air blown at high speed across the top of the vertical tube of a perfume atomizer (Fig. 10-24a) is less than the normal air pressure acting on the surface of the liquid in the bowl. Thus atmospheric pressure in the bowl pushes the perfume up the tube because of the lower pressure at the top. A Ping-Pong ball can be made to float above a blowing jet of air (a hair dryer or a vacuum cleaner that can also blow air), Fig. 10-24b; if the ball begins to leave the jet of air, the higher pressure in the still air outside the jet pushes the ball back in.

EXERCISE G Return to Chapter-Opening Question 2, page 260, and answer it again now. Try to explain why you may have answered differently the first time. Try it and see.

Airplane Wings and Dynamic Lift

Airplanes experience a “lift” force on their wings, keeping them up in the air, if they are moving at a sufficiently high speed relative to the air and the wing is tilted upward at a small angle (the “attack angle”). See Fig. 10-25, where streamlines of air are shown rushing by the wing (we are in the reference frame of the wing, as if sitting on the wing). The upward tilt, as well as the rounded upper surface of the wing, causes the streamlines to be forced upward and to be crowded together above the wing. The area of air flowing between any two streamlines is smaller as the streamlines get closer together, so from the equation of continuity ($A_1v_1 = A_2v_2$), the air speed increases above the wing where the streamlines are squished together. (Recall also how the crowded streamlines in a pipe constriction, Fig. 10-19, indicate the velocity is higher in the constriction.) Thus the air speed is greater above the wing than below it, so the pressure above the wing is less than the pressure below the wing (Bernoulli's principle). Hence there is a net upward force on the wing called **dynamic lift**. Experiments show that the speed of air above the wing can even be double the speed of the air below it. (Friction between the air and wing exerts a *drag force*, toward the rear, which must be overcome by the plane's engines.)

A flat wing, or one with symmetric cross section, will experience lift as long as the front of the wing is tilted upward (attack angle). The wing shown in Fig. 10-25 can experience lift even if the attack angle is zero, because the rounded upper surface deflects air up, squeezing the streamlines together. Airplanes can fly upside down, experiencing lift, if the attack angle is sufficient to deflect streamlines up and closer together.

Our picture considers streamlines; but if the attack angle is larger than about 15° , turbulence sets in (Fig. 10-18b) leading to greater drag and less lift, causing the plane to “stall” and then to drop.

From another point of view, the upward tilt of a wing means the air moving horizontally in front of the wing is deflected downward; the change in momentum of the rebounding air molecules results in an upward force on the wing (Newton's third law).

Sailboats

A sailboat can move “against” the wind, with the aid of the Bernoulli effect, by setting the sails at an angle, as shown in Fig. 10-26. The air traveling rapidly over the bulging front surface of the mainsail exerts a smaller pressure than the relatively still air behind the sail. The result is a net force on the sail, \vec{F}_{wind} , as shown in Fig. 10-26b. This force would tend to make the boat move sideways if it weren't for the keel that extends vertically downward beneath the water: the water exerts a force (\vec{F}_{water}) on the keel nearly perpendicular to the keel. The resultant of these two forces (\vec{F}_R) is almost directly forward as shown.

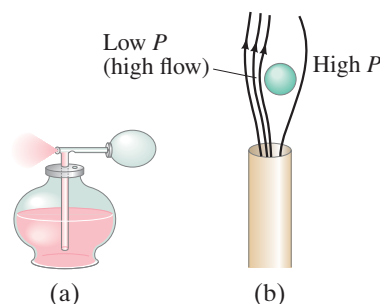
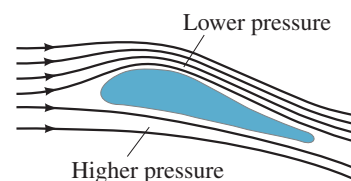


FIGURE 10-24 Examples of Bernoulli's principle: (a) atomizer, (b) Ping-Pong ball in jet of air.

FIGURE 10-25 Lift on an airplane wing. We are in the reference frame of the wing, seeing the air flow by.



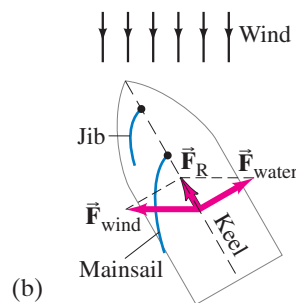
PHYSICS APPLIED

Airplanes and dynamic lift

FIGURE 10-26 Sailboat (a) sailing against the wind with (b) analysis.



(a)



(b)

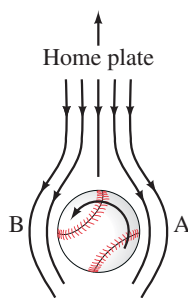
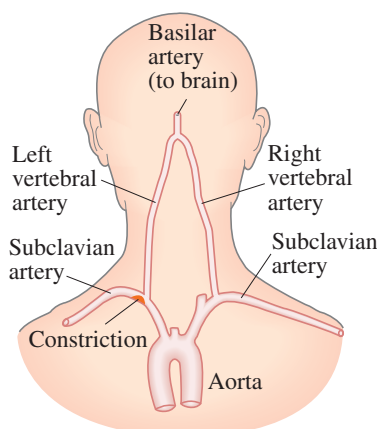


FIGURE 10-27 Looking down on a pitched baseball heading toward home plate. We are in the reference frame of the baseball, with the air flowing by.

FIGURE 10-28 Rear of the head and shoulders showing arteries leading to the brain and to the arms. High blood velocity past the constriction in the left subclavian artery causes low pressure in the left vertebral artery, in which a reverse (downward) blood flow can then occur, resulting in a TIA, a loss of blood to the brain.



Baseball Curve

Why a spinning pitched baseball (or tennis ball) curves can also be explained using Bernoulli's principle. It is simplest if we put ourselves in the reference frame of the ball, with the air rushing by, just as we did for the airplane wing. Suppose the ball is rotating counterclockwise as seen from above, Fig. 10–27. A thin layer of air (“boundary layer”) is being dragged around by the ball. We are looking down on the ball, and at point A in Fig. 10–27, this boundary layer tends to slow down the oncoming air. At point B, the air rotating with the ball adds its speed to that of the oncoming air, so the air speed is higher at B than at A. The higher speed at B means the pressure is lower at B than at A, resulting in a net force toward B. The ball's path curves toward the left (as seen by the pitcher).

Lack of Blood to the Brain—TIA

In medicine, one of many applications of Bernoulli's principle is to explain a TIA, a *transient ischemic attack* (meaning a temporary lack of blood supply to the brain). A person suffering a TIA may experience symptoms such as dizziness, double vision, headache, and weakness of the limbs. A TIA can occur as follows. Blood normally flows up to the brain at the back of the head via the two vertebral arteries—one going up each side of the neck—which meet to form the basilar artery just below the brain, as shown in Fig. 10–28. Each vertebral artery connects to the subclavian artery, as shown, before the blood passes to the arms. When an arm is exercised vigorously, blood flow increases to meet the needs of the arm's muscles. If the subclavian artery on one side of the body is partially blocked, however, as in arteriosclerosis (hardening of the arteries), the blood velocity will have to be higher on that side to supply the needed blood. (Recall the equation of continuity: smaller area means larger velocity for the same flow rate, Eqs. 10–4.) The increased blood velocity past the opening to the vertebral artery results in lower pressure (Bernoulli's principle). Thus, blood rising in the vertebral artery on the “good” side at normal pressure can be *diverted down* into the other vertebral artery because of the low pressure on that side, instead of passing upward to the brain. Hence the blood supply to the brain is reduced.

Other Applications

A **venturi tube** is essentially a pipe with a narrow constriction (the throat). The flowing fluid speeds up as it passes through this constriction, so the pressure is lower in the throat. A **venturi meter**, Fig. 10–29, is used to measure the flow speed of gases and liquids, including blood velocity in arteries. The velocity v_1 can be determined by measuring the pressure P_1 and P_2 , the areas A_1 and A_2 , as well as the density of the fluid. (The formula is given in Problem 56.)

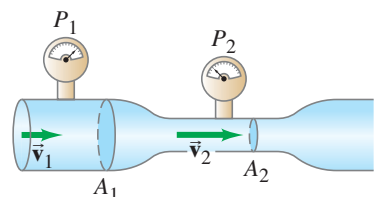


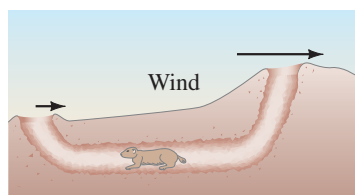
FIGURE 10-29 Venturi meter.



PHYSICS APPLIED

Smoke up a chimney
Underground air circulation

FIGURE 10-30 Bernoulli's principle explains air flow in underground burrows.



Why does smoke go up a chimney? It's partly because hot air rises (it's less dense and therefore buoyant). But Bernoulli's principle also plays a role. When wind blows across the top of a chimney, the pressure is less there than inside the house. Hence, air and smoke are pushed up the chimney by the higher indoor pressure. Even on an apparently still night there is usually enough ambient air flow at the top of a chimney to assist upward flow of smoke.

If gophers, prairie dogs, rabbits, and other animals that live underground are to avoid suffocation, the air must circulate in their burrows. The burrows always have at least two entrances (Fig. 10–30). The speed of air flow across different holes will usually be slightly different. This results in a slight pressure difference, which forces a flow of air through the burrow via Bernoulli's principle. The flow of air is enhanced if one hole is higher than the other (animals often build mounds) since wind speed tends to increase with height.

Bernoulli's equation ignores the effects of friction (viscosity) and the compressibility of the fluid. The energy that is transformed to internal (or potential) energy due to compression and to thermal energy by friction can be taken into account by adding terms to Eq. 10–5. These terms are difficult to calculate theoretically and are normally determined empirically for given situations. They do not significantly alter the explanations for the phenomena described above.

* 10–11 Viscosity

Real fluids have a certain amount of internal friction called **viscosity**, as mentioned in Section 10–8. Viscosity exists in both liquids and gases, and is essentially a frictional force between adjacent layers of fluid as the layers move past one another. In liquids, viscosity is due to the electrical cohesive forces between the molecules. In gases, it arises from collisions between the molecules.

The viscosity of different fluids can be expressed quantitatively by a *coefficient of viscosity*, η (the Greek lowercase letter eta), which is defined in the following way. A thin layer of fluid is placed between two flat plates. One plate is stationary and the other is made to move, Fig. 10–31. The fluid directly in contact with each plate is held to the surface by the adhesive force between the molecules of the liquid and those of the plate. Thus the upper surface of the fluid moves with the same speed v as the upper plate, whereas the fluid in contact with the stationary plate remains stationary. The stationary layer of fluid retards the flow of the layer just above it, which in turn retards the flow of the next layer, and so on. Thus the velocity varies continuously from 0 to v , as shown. The increase in velocity divided by the distance over which this change is made—equal to v/ℓ —is called the *velocity gradient*. To move the upper plate requires a force, which you can verify by moving a flat plate across a puddle of syrup on a table. For a given fluid, it is found that the force required, F , is proportional to the area of fluid in contact with each plate, A , and to the speed, v , and is inversely proportional to the separation, ℓ , of the plates: $F \propto vA/\ell$. For different fluids, the more viscous the fluid, the greater is the required force. The proportionality constant for this equation is defined as the coefficient of viscosity, η :

$$F = \eta A \frac{v}{\ell}. \quad (10-8)$$

Solving for η , we find $\eta = F\ell/vA$. The SI unit for η is $\text{N} \cdot \text{s}/\text{m}^2 = \text{Pa} \cdot \text{s}$ (pascal·second). In the cgs system, the unit is $\text{dyne} \cdot \text{s}/\text{cm}^2$, which is called a *poise* (P). Viscosities are often given in centipoise ($1 \text{ cP} = 10^{-2} \text{ P} = 10^{-3} \text{ Pa} \cdot \text{s}$). Table 10–3 lists the coefficient of viscosity for various fluids. The temperature is also specified, since it has a strong effect; the viscosity of liquids such as motor oil, for example, decreases rapidly as temperature increases.[‡]

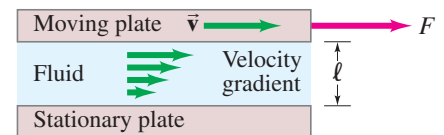


FIGURE 10–31 Determination of viscosity.

TABLE 10–3
Coefficients of Viscosity

Fluid (temperature in °C)	Coefficient of Viscosity, η (Pa·s) [†]
Water (0°)	1.8×10^{-3}
(20°)	1.0×10^{-3}
(100°)	0.3×10^{-3}
Whole blood (37°)	$\approx 4 \times 10^{-3}$
Blood plasma (37°)	$\approx 1.5 \times 10^{-3}$
Ethyl alcohol (20°)	1.2×10^{-3}
Engine oil (30°) (SAE 10)	200×10^{-3}
Glycerine (20°)	1500×10^{-3}
Air (20°)	0.018×10^{-3}
Hydrogen (0°)	0.009×10^{-3}
Water vapor (100°)	0.013×10^{-3}

[†]1 Pa·s = 10 poise (P) = 1000 cP.

* 10–12 Flow in Tubes: Poiseuille's Equation, Blood Flow

If a fluid had no viscosity, it could flow through a level tube or pipe without a force being applied. Viscosity acts like a sort of friction (between fluid layers moving at slightly different speeds), so a pressure difference between the ends of a level tube is necessary for the steady flow of any real fluid, be it water or oil in a pipe, or blood in the circulatory system of a human.

[‡]The Society of Automotive Engineers assigns numbers to represent the viscosity of oils: 30-weight (SAE 30) is more viscous than 10-weight. Multigrade oils, such as 20–50, are designed to maintain viscosity as temperature increases; 20–50 means the oil acts like 20-weight when cool and is like 50-weight when it is hot (engine running temperature). In other words, the viscosity does not drop precipitously as the oil warms up, as a simple 20-weight oil would.

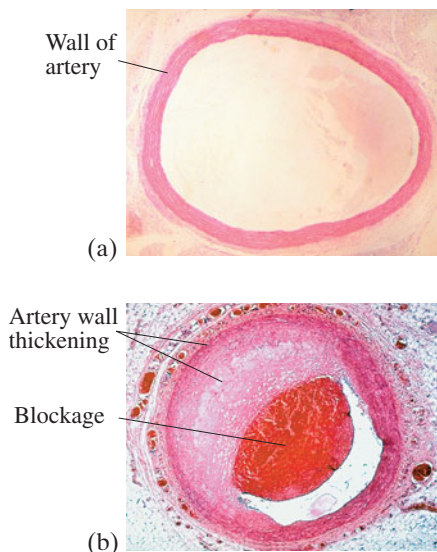


FIGURE 10-32 A cross section of a human artery that (a) is healthy, (b) is partly blocked as a result of arteriosclerosis.



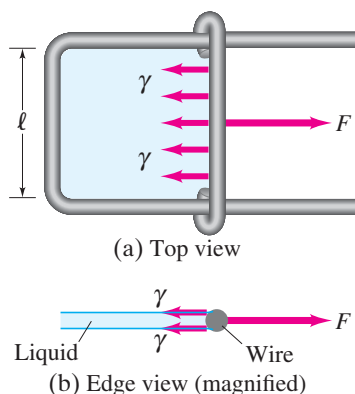
PHYSICS APPLIED

*Medicine—
blood flow and
heart disease*

FIGURE 10-33 Spherical water droplets, dew on a blade of grass.



FIGURE 10-34 U-shaped wire apparatus holding a film of liquid to measure surface tension ($\gamma = F/2\ell$).



The French scientist J. L. Poiseuille (1799–1869), who was interested in the physics of blood circulation (and after whom the “poise” is named), determined how the variables affect the flow rate of an incompressible fluid undergoing laminar flow in a cylindrical tube. His result, known as **Poiseuille’s equation**, is:

$$Q = \frac{\pi R^4 (P_1 - P_2)}{8\eta\ell}, \quad (10-9)$$

where R is the inside radius of the tube, ℓ is the tube length, $P_1 - P_2$ is the pressure difference between the ends, η is the coefficient of viscosity, and Q is the volume rate of flow (volume of fluid flowing past a given point per unit time which in SI has units of m^3/s). Equation 10–9 applies only to laminar (streamline) flow.

Poiseuille’s equation tells us that the flow rate Q is directly proportional to the “pressure gradient,” $(P_1 - P_2)/\ell$, and it is inversely proportional to the viscosity of the fluid. This is just what we might expect. It may be surprising, however, that Q also depends on the *fourth* power of the tube’s radius. This means that for the same pressure gradient, if the tube radius is halved, the flow rate is decreased by a factor of 16! Thus the rate of flow, or alternately the pressure required to maintain a given flow rate, is greatly affected by only a small change in tube radius.

An interesting example of this R^4 dependence is *blood flow* in the human body. Poiseuille’s equation is valid only for the streamline flow of an incompressible fluid. So it cannot be precisely accurate for blood whose flow is not without turbulence and that contains blood cells (whose diameter is almost equal to that of a capillary). Nonetheless, Poiseuille’s equation does give a reasonable first approximation. Because the radius of arteries is reduced as a result of arteriosclerosis (thickening and hardening of artery walls, Fig. 10–32) and by cholesterol buildup, the pressure gradient must be increased to maintain the same flow rate. If the radius is reduced by half, the heart would have to increase the pressure by a factor of about $2^4 = 16$ in order to maintain the same blood-flow rate. The heart must work much harder under these conditions, but usually cannot maintain the original flow rate. Thus, high blood pressure is an indication both that the heart is working harder and that the blood-flow rate is reduced.

* 10–13 Surface Tension and Capillarity

The *surface* of a liquid at rest behaves in an interesting way, almost as if it were a stretched membrane under tension. For example, a drop of water on the end of a dripping faucet, or hanging from a thin branch in the early morning dew (Fig. 10–33), forms into a nearly spherical shape as if it were a tiny balloon filled with water. A steel needle can be made to float on the surface of water even though it is denser than the water. The surface of a liquid acts like it is under tension, and this tension, acting along the surface, arises from the attractive forces between the molecules. This effect is called **surface tension**. More specifically, a quantity called the *surface tension*, γ (the Greek letter gamma), is defined as the force F per unit length ℓ that acts perpendicular to any line or cut in a liquid surface, tending to pull the surface closed:

$$\gamma = \frac{F}{\ell}. \quad (10-10)$$

To understand this, consider the U-shaped apparatus shown in Fig. 10–34 which encloses a thin film of liquid (such as a liquid soap film). Because of surface tension, a force F is required to pull the movable wire and thus increase the surface area of the liquid. The liquid contained by the wire apparatus is a thin film having both a top and a bottom surface. Hence the total length of the surface being increased is 2ℓ , and the surface tension is $\gamma = F/2\ell$. A delicate apparatus of this type can be used to measure the surface tension of various liquids. The surface tension of water is 0.072 N/m at 20°C . Table 10–4 (next page) gives the values for several substances. Note that temperature has a considerable effect on the surface tension.

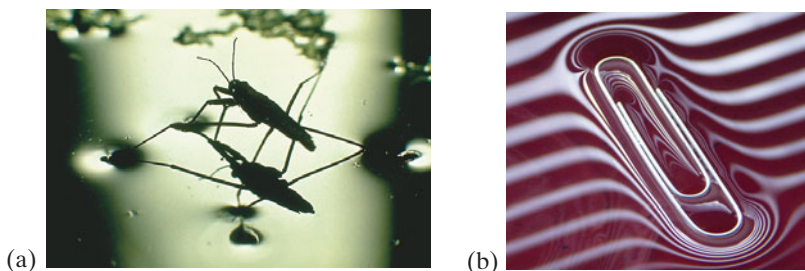


FIGURE 10-35 (a) Water strider. (b) Paper clip (light coming through window blinds).

Because of surface tension, some insects (Fig. 10–35a) can walk on water, and objects more dense than water, such as a paper clip (Fig. 10–35b), can float on the surface. Figure 10–36a shows how the surface tension can support the weight w of an object. Actually, the object sinks slightly into the fluid, so w is the “effective weight” of that object—its true weight less the buoyant force.

EXAMPLE 10-15 ESTIMATE Insect walks on water. The base of an insect’s leg is approximately spherical in shape, with a radius of about 2.0×10^{-5} m. The 0.0030-g mass of the insect is supported equally by its six legs. Estimate the angle θ (see Fig. 10–36) for an insect on the surface of water. Assume the water temperature is 20°C .

APPROACH Since the insect is in equilibrium, the upward surface tension force is equal to the pull of gravity downward on each leg. We ignore buoyant forces for this estimate.

SOLUTION For each leg, we assume the surface tension force acts all around a circle of radius r , at an angle θ , as shown in Fig. 10–36a. Only the vertical component, $\gamma \cos \theta$, acts to balance the weight mg . We set the length ℓ in Eq. 10–10 equal to the circumference of the circle, $\ell \approx 2\pi r$. Then the net upward force due to surface tension is $F_y \approx (\gamma \cos \theta) \ell \approx 2\pi r \gamma \cos \theta$. We set this surface tension force equal to one-sixth the weight of the insect since it has six legs:

$$\begin{aligned} 2\pi r \gamma \cos \theta &\approx \frac{1}{6} mg \\ (6.28)(2.0 \times 10^{-5} \text{ m})(0.072 \text{ N/m}) \cos \theta &\approx \frac{1}{6} (3.0 \times 10^{-6} \text{ kg})(9.8 \text{ m/s}^2) \\ \cos \theta &\approx 0.54. \end{aligned}$$

So $\theta \approx 57^\circ$. If $\cos \theta$ had come out greater than 1, the surface tension would not have been great enough to support the insect’s weight.

NOTE Our estimate ignored the buoyant force and ignored any difference between the radius of the insect’s “foot” and the radius of the surface depression.

Soaps and detergents lower the surface tension of water. This is desirable for washing and cleaning since the high surface tension of pure water prevents it from penetrating easily between the fibers of material and into tiny crevices. Substances that reduce the surface tension of a liquid are called *surfactants*.

*Capillarity

Surface tension plays a role in another interesting phenomenon, *capillarity*. It is a common observation that water in a glass container rises up slightly where it touches the glass, Fig. 10–37a. The water is said to “wet” the glass. Mercury, on the other hand, is depressed when it touches the glass, Fig. 10–37b; the mercury does not wet the glass. Whether a liquid wets a solid surface is determined by the relative strength of the cohesive forces between the molecules of the liquid compared to the adhesive forces between the molecules of the liquid and those of the container. **Cohesion** refers to the force between molecules of the same type, whereas **adhesion** refers to the force between molecules of different types. Water wets glass because the water molecules are more strongly attracted to the glass molecules than they are to other water molecules. The opposite is true for mercury: the cohesive forces are stronger than the adhesive forces.

TABLE 10-4 Surface Tension of Some Substances

Substance	Surface Tension (N/m)
Mercury (20°C)	0.44
Blood, whole (37°C)	0.058
Blood, plasma (37°C)	0.073
Alcohol, ethyl (20°C)	0.023
Water (0°C)	0.076
(20°C)	0.072
(100°C)	0.059
Benzene (20°C)	0.029
Soap solution (20°C)	≈ 0.025
Oxygen (-193°C)	0.016

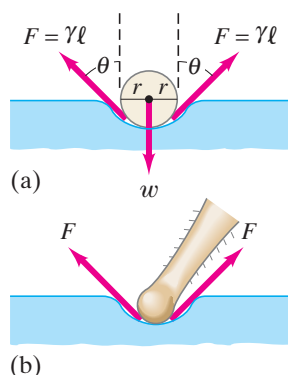
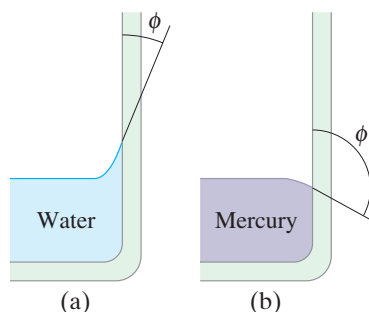


FIGURE 10-36 Surface tension acting on (a) a sphere, and (b) an insect leg. Example 10–15.

PHYSICS APPLIED

Soaps and detergents

FIGURE 10-37 (a) Water “wets” the surface of glass, whereas (b) mercury does not “wet” the glass.



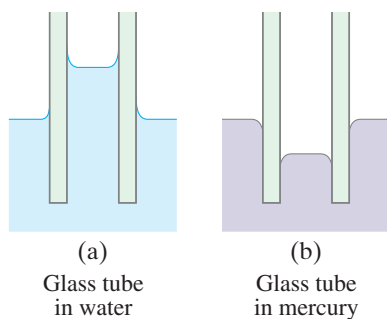
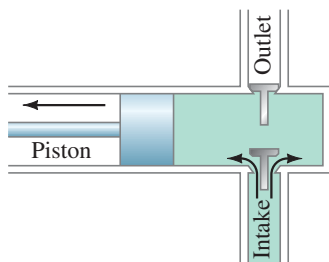


FIGURE 10-38 Capillarity.

FIGURE 10-39 One kind of pump (reciprocating type): the intake valve opens and air (or fluid that is being pumped) fills the empty space when the piston moves to the left. When the piston moves to the right (not shown), the outlet valve opens and fluid is forced out.



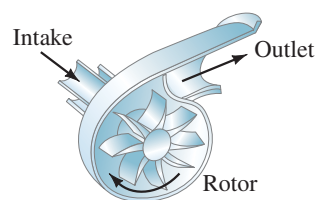
In tubes having very small diameters, liquids are observed to rise or fall relative to the level of the surrounding liquid. This phenomenon is called **capillarity**, and such thin tubes are called **capillaries**. Whether the liquid rises or falls (Fig. 10–38) depends on the relative strengths of the adhesive and cohesive forces. Thus water rises in a glass tube, whereas mercury falls. The actual amount of rise (or fall) depends on the surface tension—which is what keeps the liquid surface from breaking apart.

* 10–14 Pumps, and the Heart

We conclude this Chapter with a brief discussion of pumps, including the heart. Pumps can be classified into categories according to their function. A *vacuum pump* is designed to reduce the pressure (usually of air) in a given vessel. A *force pump*, on the other hand, is a pump that is intended to increase the pressure—for example, to lift a liquid (such as water from a well) or to push a fluid through a pipe. Figure 10–39 illustrates the principle behind a simple reciprocating pump. It could be a vacuum pump, in which case the intake is connected to the vessel to be evacuated. A similar mechanism is used in some force pumps, and in this case the fluid is forced under increased pressure through the outlet.

Another type of pump is the centrifugal pump, shown in Fig. 10–40. It, or any force pump, can be used as a *circulating pump*—that is, to circulate a fluid around a closed path, such as the cooling water or lubricating oil in an automobile.

FIGURE 10-40 Centrifugal pump: the rotating blades force fluid through the outlet pipe; this kind of pump is used in vacuum cleaners and as a water pump in automobiles.

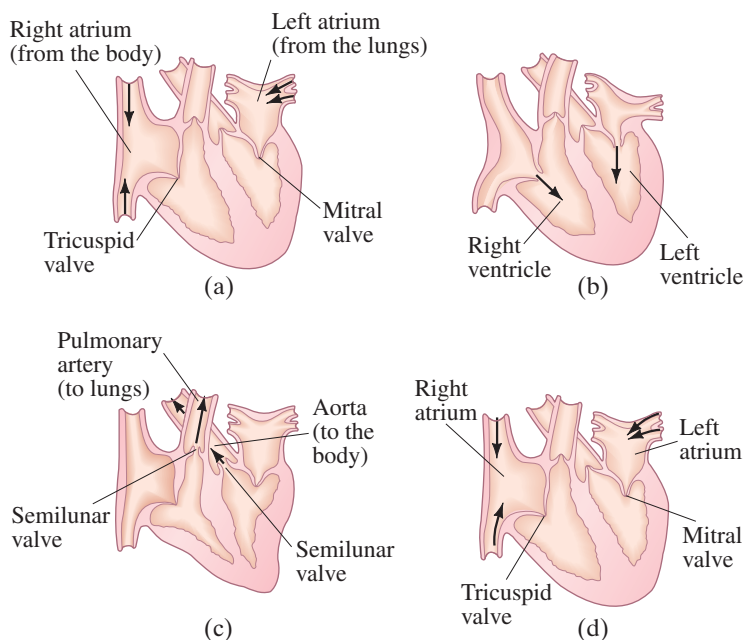


PHYSICS APPLIED

Heart as a pump

The heart of a human (and of other animals as well) is essentially a circulating pump. The action of a human heart is shown in Fig. 10–41. There are actually two separate paths for blood flow. The longer path takes blood to the parts of the body, via the arteries, bringing oxygen to body tissues and picking up carbon dioxide, which it carries back to the heart via veins. This blood is then pumped to the lungs (the second path), where the carbon dioxide is released and oxygen is taken up. The oxygen-laden blood is returned to the heart, where it is again pumped to the tissues of the body.

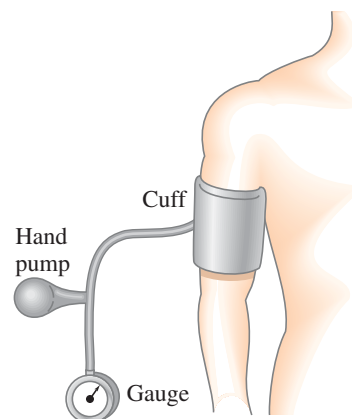
FIGURE 10-41 Pumping human heart. (a) In the diastole phase, the heart relaxes between beats. Blood moves into the heart; both atria fill rapidly. (b) When the atria contract, the systole or pumping phase begins. The contraction pushes the blood through the mitral and tricuspid valves into the ventricles. (c) The contraction of the ventricles forces the blood through the semilunar valves into the pulmonary artery, which leads to the lungs, and to the aorta (the body's largest artery), which leads to the arteries serving all the body. (d) When the heart relaxes, the semilunar valves close; blood fills the atria, beginning the cycle again.



Blood pressure is measured using one of the types of gauge mentioned earlier (Section 10–6), and it is usually calibrated in mm-Hg. The gauge is attached to a closed, air-filled cuff that is wrapped around the upper arm at the level of the heart, Fig. 10–42. Two values of blood pressure are measured: the maximum pressure when the heart is pumping, called *systolic pressure*; and the pressure when the heart is in the resting part of the cycle, called *diastolic pressure*. Initially, the air pressure in the cuff is increased high above the systolic pressure by a pump, compressing the main (brachial) artery in the arm and briefly cutting off the flow of blood. The air pressure is then reduced slowly until blood again begins to flow into the arm; it can be detected by listening with a stethoscope to the characteristic tapping sound[†] of the blood returning to the forearm. At this point, systolic pressure is just equal to the air pressure in the arm cuff which can be read off the gauge. The air pressure is subsequently reduced further, and the tapping sound disappears when blood at low pressure can enter the artery. At this point, the gauge indicates the diastolic pressure. Normal systolic pressure is around 120 mm-Hg, whereas normal diastolic pressure is around 70 or 80 mm-Hg. Blood pressure is reported in the form 120/70.

[†]When the blood starts flowing through the constriction caused by the tight cuff, its velocity is high and the flow is turbulent. It is the turbulence that causes the tapping sound.

FIGURE 10–42 Device for measuring blood pressure.



Summary

The three common phases of matter are **solid**, **liquid**, and **gas**. Liquids and gases are collectively called **fluids**, meaning they have the ability to flow. The **density** of a material is defined as its mass per unit volume:

$$\rho = \frac{m}{V}. \quad (10-1)$$

Specific gravity (SG) is the ratio of the density of the material to the density of water (at 4°C).

Pressure is defined as force per unit area:

$$P = \frac{F}{A}. \quad (10-2)$$

The pressure P at a depth h in a liquid of constant density ρ , due to the weight of the liquid, is given by

$$P = \rho gh, \quad (10-3a)$$

where g is the acceleration due to gravity.

Pascal's principle says that an external pressure applied to a confined fluid is transmitted throughout the fluid.

Pressure is measured using a **manometer** or other type of gauge. A **barometer** is used to measure atmospheric pressure. Standard **atmospheric pressure** (average at sea level) is $1.013 \times 10^5 \text{ N/m}^2$. **Gauge pressure** is the total (absolute) pressure minus atmospheric pressure.

Archimedes' principle states that an object submerged wholly or partially in a fluid is buoyed up by a force equal to the weight of fluid it displaces ($F_B = m_F g = \rho_F V_{\text{displ}} g$).

Fluid flow can be characterized either as **streamline** (also called **laminar**), in which the layers of fluid move smoothly and regularly along paths called **streamlines**, or as **turbulent**, in which case the flow is not smooth and regular but is characterized by irregularly shaped whirlpools.

Fluid flow rate is the mass or volume of fluid that passes a given point per unit time. The **equation of continuity** states that for an incompressible fluid flowing in an enclosed tube, the product of the velocity of flow and the cross-sectional area of the tube remains constant:

$$Av = \text{constant}. \quad (10-4)$$

Bernoulli's principle tells us that where the velocity of a fluid is high, the pressure in it is low, and where the velocity is low, the pressure is high. For steady laminar flow of an incompressible and nonviscous fluid, **Bernoulli's equation**, which is based on the law of conservation of energy, is

$$P_2 + \frac{1}{2}\rho v_2^2 + \rho g y_2 = P_1 + \frac{1}{2}\rho v_1^2 + \rho g y_1, \quad (10-5)$$

for two points along the flow.

[***Viscosity** refers to friction within a fluid and is essentially a frictional force between adjacent layers of fluid as they move past one another.]

[*Liquid surfaces hold together as if under tension (**surface tension**), allowing drops to form and objects like needles and insects to stay on the surface.]

Questions

1. If one material has a higher density than another, must the molecules of the first be heavier than those of the second? Explain.
2. Consider what happens when you push both a pin and the blunt end of a pen against your skin with the same force. Decide what determines whether your skin is cut—the net force applied to it or the pressure.
3. A small amount of water is boiled in a 1-gallon metal can. The can is removed from the heat and the lid put on. As the can cools, it collapses and looks crushed. Explain.
4. An ice cube floats in a glass of water filled to the brim. What can you say about the density of ice? As the ice melts, will the water overflow? Explain.
5. Will an ice cube float in a glass of alcohol? Why or why not?

6. A submerged can of Coke® will sink, but a can of Diet Coke® will float. (Try it!) Explain.
7. Why don't ships made of iron sink?
8. A barge filled high with sand approaches a low bridge over the river and cannot quite pass under it. Should sand be added to, or removed from, the barge? [Hint: Consider Archimedes' principle.]
9. Explain why helium weather balloons, which are used to measure atmospheric conditions at high altitudes, are normally released while filled to only 10–20% of their maximum volume.
10. Will an empty balloon have precisely the same apparent weight on a scale as a balloon filled with air? Explain.
11. Why do you float higher in salt water than in fresh water?
12. Why does the stream of water from a faucet become narrower as it falls (Fig. 10–43)?



FIGURE 10–43 Question 12.
Water coming from a faucet.

17. If you dangle two pieces of paper vertically, a few inches apart (Fig. 10–44), and blow between them, how do you think the papers will move? Try it and see. Explain.



FIGURE 10–44
Question 17.

18. Why does the canvas top of a convertible bulge out when the car is traveling at high speed? [Hint: The windshield deflects air upward, pushing streamlines closer together.]
19. Roofs of houses are sometimes “blown” off (or are they pushed off?) during a tornado or hurricane. Explain using Bernoulli's principle.
20. Explain how the tube in Fig. 10–45, known as a **siphon**, can transfer liquid from one container to a lower one even though the liquid must flow uphill for part of its journey. (Note that the tube must be filled with liquid to start with.)

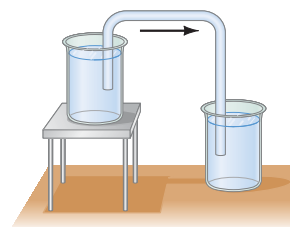


FIGURE 10–45
Question 20.
A siphon.

- *21. When blood pressure is measured, why must the arm cuff be held at the level of the heart?

MisConceptual Questions

1. You hold a piece of wood in one hand and a piece of iron in the other. Both pieces have the same volume, and you hold them fully under water at the same depth. At the moment you let go of them, which one experiences the greater buoyancy force?
 - (a) The piece of wood.
 - (b) The piece of iron.
 - (c) They experience the same buoyancy force.
 - (d) More information is needed.
2. Three containers are filled with water to the same height and have the same surface area at the base, but the total weight of water is different for each (Fig. 10–46). In which container does the water exert the greatest force on the bottom of the container?
 - (a) Container A.
 - (b) Container B.
 - (c) Container C.
 - (d) All three are equal.



FIGURE 10–46
MisConceptual Question 2.

3. Beaker A is filled to the brim with water. Beaker B is the same size and contains a small block of wood which floats when the beaker is filled with water to the brim. Which beaker weighs more?
 - (a) Beaker A.
 - (b) Beaker B.
 - (c) The same for both.
4. Why does an ocean liner float?
 - (a) It is made of steel, which floats.
 - (b) Its very big size changes the way water supports it.
 - (c) It is held up in the water by large Styrofoam compartments.
 - (d) The average density of the ocean liner is less than that of seawater.
 - (e) Remember the *Titanic*—ocean liners do not float.
5. A rowboat floats in a swimming pool, and the level of the water at the edge of the pool is marked. Consider the following situations. (i) The boat is removed from the water. (ii) The boat in the water holds an iron anchor which is removed from the boat and placed on the shore. For each situation, the level of the water will
 - (a) rise.
 - (b) fall.
 - (c) stay the same.

6. You put two ice cubes in a glass and fill the glass to the rim with water. As the ice melts, the water level
 - (a) drops below the rim.
 - (b) rises and water spills out of the glass.
 - (c) remains the same.
 - (d) drops at first, then rises until a little water spills out.
7. Hot air is less dense than cold air. Could a hot-air balloon be flown on the Moon, where there is no atmosphere?
 - (a) No, there is no cold air to displace, so no buoyancy force would exist.
 - (b) Yes, warm air always rises, especially in a weak gravitational field like that of the Moon.
 - (c) Yes, but the balloon would have to be filled with helium instead of hot air.
8. An object that can float in both water and in oil (whose density is less than that of water) experiences a buoyant force that is
 - (a) greater when it is floating in oil than when floating in water.
 - (b) greater when it is floating in water than when floating in oil.
 - (c) the same when it is floating in water or in oil.
9. As water flows from a low elevation to a higher elevation through a pipe that changes in diameter,
 - (a) the water pressure will increase.
 - (b) the water pressure will decrease.
 - (c) the water pressure will stay the same.
 - (d) Need more information to determine how the water pressure changes.
10. Water flows in a horizontal pipe that is narrow but then widens and the speed of the water becomes less. The pressure in the water moving in the pipe is
 - (a) greater in the wide part.
 - (b) greater in the narrow part.
 - (c) the same in both parts.
 - (d) greater where the speed is higher.
 - (e) greater where the speed is lower.
11. When a baseball curves to the right (a curveball), air is flowing
 - (a) faster over the left side than over the right side.
 - (b) faster over the right side than over the left side.
 - (c) faster over the top than underneath.
 - (d) at the same speed all around the baseball, but the ball curves as a result of the way the wind is blowing on the field.
12. How is the smoke drawn up a chimney affected when a wind is blowing outside?
 - (a) Smoke rises more rapidly in the chimney.
 - (b) Smoke rises more slowly in the chimney.
 - (c) Smoke is forced back down the chimney.
 - (d) Smoke is unaffected.

For assigned homework and other learning materials, go to the MasteringPhysics website.



Problems

10–2 Density and Specific Gravity

1. (I) The approximate volume of the granite monolith known as El Capitan in Yosemite National Park (Fig. 10–47) is about 10^8 m^3 . What is its approximate mass?



FIGURE 10–47 Problem 1.

2. (I) What is the approximate mass of air in a living room $5.6 \text{ m} \times 3.6 \text{ m} \times 2.4 \text{ m}$?
3. (I) If you tried to smuggle gold bricks by filling your backpack, whose dimensions are $54 \text{ cm} \times 31 \text{ cm} \times 22 \text{ cm}$, what would its mass be?

4. (I) State your mass and then estimate your volume. [Hint: Because you can swim on or just under the surface of the water in a swimming pool, you have a pretty good idea of your density.]
5. (II) A bottle has a mass of 35.00 g when empty and 98.44 g when filled with water. When filled with another fluid, the mass is 89.22 g. What is the specific gravity of this other fluid?
6. (II) If 4.0 L of antifreeze solution (specific gravity = 0.80) is added to 5.0 L of water to make a 9.0-L mixture, what is the specific gravity of the mixture?
7. (III) The Earth is not a uniform sphere, but has regions of varying density. Consider a simple model of the Earth divided into three regions—inner core, outer core, and mantle. Each region is taken to have a unique constant density (the average density of that region in the real Earth):

Region	Radius (km)	Density (kg/m^3)
Inner Core	0–1220	13,000
Outer Core	1220–3480	11,100
Mantle	3480–6380	4400

- (a) Use this model to predict the average density of the entire Earth. (b) If the radius of the Earth is 6380 km and its mass is $5.98 \times 10^{24} \text{ kg}$, determine the actual average density of the Earth and compare it (as a percent difference) with the one you determined in (a).

10-3 to 10-6 Pressure; Pascal's Principle

8. (I) Estimate the pressure needed to raise a column of water to the same height as a 46-m-tall pine tree.
9. (I) Estimate the pressure exerted on a floor by (a) one pointed heel of area $= 0.45 \text{ cm}^2$, and (b) one wide heel of area 16 cm^2 , Fig. 10-48. The person wearing the shoes has a mass of 56 kg.



FIGURE 10-48 Problem 9.

10. (I) What is the difference in blood pressure (mm-Hg) between the top of the head and bottom of the feet of a 1.75-m-tall person standing vertically?
11. (I) (a) Calculate the total force of the atmosphere acting on the top of a table that measures $1.7 \text{ m} \times 2.6 \text{ m}$. (b) What is the total force acting upward on the underside of the table?
12. (II) How high would the level be in an alcohol barometer at normal atmospheric pressure?
13. (II) In a movie, Tarzan evades his captors by hiding under water for many minutes while breathing through a long, thin reed. Assuming the maximum pressure difference his lungs can manage and still breathe is -85 mm-Hg , calculate the deepest he could have been.
14. (II) The maximum gauge pressure in a hydraulic lift is 17.0 atm . What is the largest-size vehicle (kg) it can lift if the diameter of the output line is 25.5 cm ?
15. (II) The gauge pressure in each of the four tires of an automobile is 240 kPa . If each tire has a "footprint" of 190 cm^2 (area touching the ground), estimate the mass of the car.
16. (II) (a) Determine the total force and the absolute pressure on the bottom of a swimming pool 28.0 m by 8.5 m whose uniform depth is 1.8 m . (b) What will be the pressure against the side of the pool near the bottom?
17. (II) A house at the bottom of a hill is fed by a full tank of water 6.0 m deep and connected to the house by a pipe that is 75 m long at an angle of 61° from the horizontal (Fig. 10-49). (a) Determine the water gauge pressure at the house. (b) How high could the water shoot if it came vertically out of a broken pipe in front of the house?

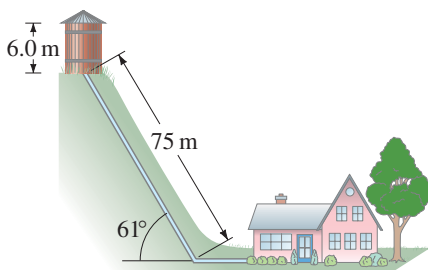


FIGURE 10-49 Problem 17.

18. (II) Water and then oil (which don't mix) are poured into a U-shaped tube, open at both ends. They come to equilibrium as shown in Fig. 10-50. What is the density of the oil? [Hint: Pressures at points a and b are equal. Why?]

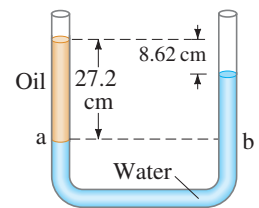


FIGURE 10-50 Problem 18.

19. (II) How high would the atmosphere extend if it were of uniform density throughout, equal to half the present density at sea level?
20. (II) Determine the minimum gauge pressure needed in the water pipe leading into a building if water is to come out of a faucet on the fourteenth floor, 44 m above that pipe.
21. (II) A **hydraulic press** for compacting powdered samples has a large cylinder which is 10.0 cm in diameter, and a small cylinder with a diameter of 2.0 cm (Fig. 10-51). A lever is attached to the small cylinder as shown. The sample, which is placed on the large cylinder, has an area of 4.0 cm^2 . What is the pressure on the sample if 320 N is applied to the lever?

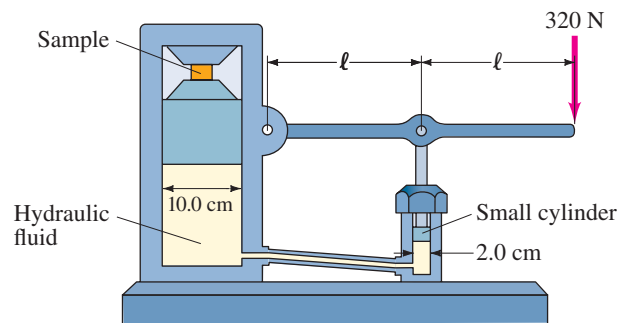


FIGURE 10-51 Problem 21.

22. (II) An open-tube mercury manometer is used to measure the pressure in an oxygen tank. When the atmospheric pressure is 1040 mbar , what is the absolute pressure (in Pa) in the tank if the height of the mercury in the open tube is (a) 18.5 cm higher, (b) 5.6 cm lower, than the mercury in the tube connected to the tank? See Fig. 10-7a.

10-7 Buoyancy and Archimedes' Principle

23. (II) What fraction of a piece of iron will be submerged when it floats in mercury?
24. (II) A geologist finds that a Moon rock whose mass is 9.28 kg has an apparent mass of 6.18 kg when submerged in water. What is the density of the rock?
25. (II) A crane lifts the $18,000\text{-kg}$ steel hull of a sunken ship out of the water. Determine (a) the tension in the crane's cable when the hull is fully submerged in the water, and (b) the tension when the hull is completely out of the water.
26. (II) A spherical balloon has a radius of 7.15 m and is filled with helium. How large a cargo can it lift, assuming that the skin and structure of the balloon have a mass of 930 kg ? Neglect the buoyant force on the cargo volume itself.
27. (II) What is the likely identity of a metal (see Table 10-1) if a sample has a mass of 63.5 g when measured in air and an apparent mass of 55.4 g when submerged in water?

28. (II) Calculate the true mass (in vacuum) of a piece of aluminum whose apparent mass is 4.0000 kg when weighed in air.
29. (II) Because gasoline is less dense than water, drums containing gasoline will float in water. Suppose a 210-L steel drum is completely full of gasoline. What total volume of steel can be used in making the drum if the gasoline-filled drum is to float in fresh water?
30. (II) A scuba diver and her gear displace a volume of 69.6 L and have a total mass of 72.8 kg. (a) What is the buoyant force on the diver in seawater? (b) Will the diver sink or float?
31. (II) The specific gravity of ice is 0.917, whereas that of seawater is 1.025. What percent of an iceberg is above the surface of the water?
32. (II) Archimedes' principle can be used to determine the specific gravity of a solid using a known liquid (Example 10–8). The reverse can be done as well. (a) As an example, a 3.80-kg aluminum ball has an apparent mass of 2.10 kg when submerged in a particular liquid: calculate the density of the liquid. (b) Determine a formula for finding the density of a liquid using this procedure.
33. (II) A 32-kg child decides to make a raft out of empty 1.0-L soda bottles and duct tape. Neglecting the mass of the duct tape and plastic in the bottles, what minimum number of soda bottles will the child need to be able stay dry on the raft?
34. (II) An undersea research chamber is spherical with an external diameter of 5.20 m. The mass of the chamber, when occupied, is 74,400 kg. It is anchored to the sea bottom by a cable. What is (a) the buoyant force on the chamber, and (b) the tension in the cable?
35. (II) A 0.48-kg piece of wood floats in water but is found to sink in alcohol (SG = 0.79), in which it has an apparent mass of 0.047 kg. What is the SG of the wood?
36. (II) A two-component model used to determine percent body fat in a human body assumes that a fraction f (< 1) of the body's total mass m is composed of fat with a density of 0.90 g/cm^3 , and that the remaining mass of the body is composed of fat-free tissue with a density of 1.10 g/cm^3 . If the specific gravity of the entire body's density is X , show that the percent body fat ($= f \times 100$) is given by

$$\% \text{ Body fat} = \frac{495}{X} - 450.$$

37. (II) On dry land, an athlete weighs 70.2 kg. The same athlete, when submerged in a swimming pool and hanging from a scale, has an “apparent weight” of 3.4 kg. Using Example 10–8 as a guide, (a) find the total volume V of the submerged athlete. (b) Assume that when submerged, the athlete's body contains a residual volume $V_R = 1.3 \times 10^{-3} \text{ m}^3$ of air (mainly in the lungs). Taking $V - V_R$ to be the actual volume of the athlete's body, find the body's specific gravity, SG. (c) What is the athlete's percent body fat assuming it is given by the formula $(495/\text{SG}) - 450$?
38. (II) How many helium-filled balloons would it take to lift a person? Assume the person has a mass of 72 kg and that each helium-filled balloon is spherical with a diameter of 33 cm.

39. (III) A scuba tank, when fully submerged, displaces 15.7 L of seawater. The tank itself has a mass of 14.0 kg and, when “full,” contains 3.00 kg of air. Assuming only its weight and the buoyant force act on the tank, determine the net force (magnitude and direction) on the fully submerged tank at the beginning of a dive (when it is full of air) and at the end of a dive (when it no longer contains any air).
40. (III) A 3.65-kg block of wood (SG = 0.50) floats on water. What minimum mass of lead, hung from the wood by a string, will cause the block to sink?

10–8 to 10–10 Fluid Flow, Bernoulli's Equation

41. (I) A 12-cm-radius air duct is used to replenish the air of a room $8.2 \text{ m} \times 5.0 \text{ m} \times 3.5 \text{ m}$ every 12 min. How fast does the air flow in the duct?
42. (I) Calculate the average speed of blood flow in the major arteries of the body, which have a total cross-sectional area of about 2.0 cm^2 . Use the data of Example 10–12.
43. (I) How fast does water flow from a hole at the bottom of a very wide, 4.7-m-deep storage tank filled with water? Ignore viscosity.
44. (I) Show that Bernoulli's equation reduces to the hydrostatic variation of pressure with depth (Eq. 10–3b) when there is no flow ($v_1 = v_2 = 0$).
45. (II) What is the volume rate of flow of water from a 1.85-cm-diameter faucet if the pressure head is 12.0 m?
46. (II) A fish tank has dimensions 36 cm wide by 1.0 m long by 0.60 m high. If the filter should process all the water in the tank once every 3.0 h, what should the flow speed be in the 3.0-cm-diameter input tube for the filter?
47. (II) What gauge pressure in the water pipes is necessary if a fire hose is to spray water to a height of 16 m?
48. (II) A $\frac{5}{8}$ -in. (inside) diameter garden hose is used to fill a round swimming pool 6.1 m in diameter. How long will it take to fill the pool to a depth of 1.4 m if water flows from the hose at a speed of 0.40 m/s?
49. (II) A 180-km/h wind blowing over the flat roof of a house causes the roof to lift off the house. If the house is $6.2 \text{ m} \times 12.4 \text{ m}$ in size, estimate the weight of the roof. Assume the roof is not nailed down.
50. (II) A 6.0-cm-diameter horizontal pipe gradually narrows to 4.5 cm. When water flows through this pipe at a certain rate, the gauge pressure in these two sections is 33.5 kPa and 22.6 kPa, respectively. What is the volume rate of flow?
51. (II) Estimate the air pressure inside a category 5 hurricane, where the wind speed is 300 km/h (Fig. 10–52).



FIGURE 10–52 Problem 51.

52. (II) What is the lift (in newtons) due to Bernoulli's principle on a wing of area 88 m^2 if the air passes over the top and bottom surfaces at speeds of 280 m/s and 150 m/s , respectively?

53. (II) Water at a gauge pressure of 3.8 atm at street level flows into an office building at a speed of 0.78 m/s through a pipe 5.0 cm in diameter. The pipe tapers down to 2.8 cm in diameter by the top floor, 16 m above (Fig. 10–53), where the faucet has been left open. Calculate the flow velocity and the gauge pressure in the pipe on the top floor. Assume no branch pipes and ignore viscosity.

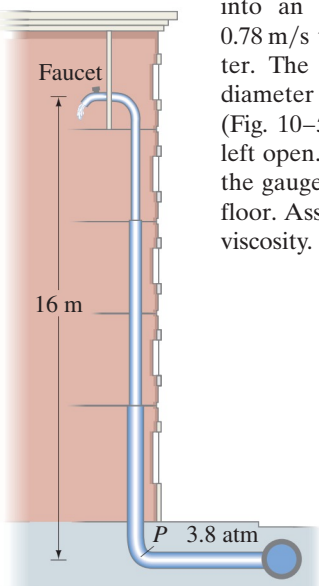


FIGURE 10–53
Problem 53.

54. (II) Show that the power needed to drive a fluid through a pipe with uniform cross-section is equal to the volume rate of flow, Q , times the pressure difference, $P_1 - P_2$. Ignore viscosity.
55. (III) In Fig. 10–54, take into account the speed of the top surface of the tank and show that the speed of fluid leaving an opening near the bottom is

$$v_1 = \sqrt{\frac{2gh}{1 - A_1^2/A_2^2}},$$

where $h = y_2 - y_1$, and A_1 and A_2 are the areas of the opening and of the top surface, respectively. Assume $A_1 \ll A_2$ so that the flow remains nearly steady and laminar.

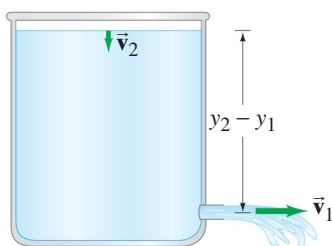


FIGURE 10–54
Problem 55.

56. (III) (a) Show that the flow speed measured by a venturi meter (see Fig. 10–29) is given by the relation

$$v_1 = A_2 \sqrt{\frac{2(P_1 - P_2)}{\rho(A_1^2 - A_2^2)}}.$$

(b) A venturi meter is measuring the flow of water; it has a main diameter of 3.5 cm tapering down to a throat diameter of 1.0 cm . If the pressure difference is measured to be 18 mm-Hg , what is the speed of the water entering the venturi throat?

57. (III) A fire hose exerts a force on the person holding it. This is because the water accelerates as it goes from the hose through the nozzle. How much force is required to hold a 7.0-cm -diameter hose delivering 420 L/min through a 0.75-cm -diameter nozzle?

*10–11 Viscosity

- *58. (II) A viscometer consists of two concentric cylinders, 10.20 cm and 10.60 cm in diameter. A liquid fills the space between them to a depth of 12.0 cm . The outer cylinder is fixed, and a torque of $0.024 \text{ m} \cdot \text{N}$ keeps the inner cylinder turning at a steady rotational speed of 57 rev/min . What is the viscosity of the liquid?

*10–12 Flow in Tubes; Poiseuille's Equation

- *59. (I) Engine oil (assume SAE 10, Table 10–3) passes through a fine 1.80-mm -diameter tube that is 10.2 cm long. What pressure difference is needed to maintain a flow rate of 6.2 mL/min ?
- *60. (I) A gardener feels it is taking too long to water a garden with a $\frac{3}{8}\text{-in.}$ -diameter hose. By what factor will the time be cut using a $\frac{5}{8}\text{-in.}$ -diameter hose instead? Assume nothing else is changed.
- *61. (II) What diameter must a 15.5-m -long air duct have if the ventilation and heating system is to replenish the air in a room $8.0 \text{ m} \times 14.0 \text{ m} \times 4.0 \text{ m}$ every 15.0 min ? Assume the pump can exert a gauge pressure of $0.710 \times 10^{-3} \text{ atm}$.
- *62. (II) What must be the pressure difference between the two ends of a 1.6-km section of pipe, 29 cm in diameter, if it is to transport oil ($\rho = 950 \text{ kg/m}^3$, $\eta = 0.20 \text{ Pa} \cdot \text{s}$) at a rate of $650 \text{ cm}^3/\text{s}$?

- *63. (II) Poiseuille's equation does not hold if the flow velocity is high enough that turbulence sets in. The onset of turbulence occurs when the **Reynolds number**, Re , exceeds approximately 2000. Re is defined as

$$Re = \frac{2\bar{v}r\rho}{\eta},$$

where \bar{v} is the average speed of the fluid, ρ is its density, η is its viscosity, and r is the radius of the tube in which the fluid is flowing. (a) Determine if blood flow through the aorta is laminar or turbulent when the average speed of blood in the aorta ($r = 0.80 \text{ cm}$) during the resting part of the heart's cycle is about 35 cm/s . (b) During exercise, the blood-flow speed approximately doubles. Calculate the Reynolds number in this case, and determine if the flow is laminar or turbulent.

- *64. (II) Assuming a constant pressure gradient, if blood flow is reduced by 65% , by what factor is the radius of a blood vessel decreased?

- *65. (II) Calculate the pressure drop per cm along the aorta using the data of Example 10–12 and Table 10–3.

- *66. (III) A patient is to be given a blood transfusion. The blood is to flow through a tube from a raised bottle to a needle inserted in the vein (Fig. 10–55). The inside diameter of the 25-mm -long needle is 0.80 mm , and the required flow rate is 2.0 cm^3 of blood per minute. How high h should the bottle be placed above the needle? Obtain ρ and η from the Tables. Assume the blood pressure is 78 torr above atmospheric pressure.

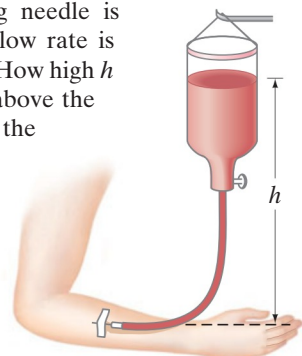


FIGURE 10–55
Problems 66 and 74.

*10–13 Surface Tension and Capillarity

- *67. (I) If the force F needed to move the wire in Fig. 10–34 is 3.4×10^{-3} N, calculate the surface tension γ of the enclosed fluid. Assume $\ell = 0.070$ m.
- *68. (I) Calculate the force needed to move the wire in Fig. 10–34 if it holds a soapy solution (Table 10–4) and the wire is 21.5 cm long.
- *69. (II) The surface tension of a liquid can be determined by measuring the force F needed to just lift a circular platinum ring of radius r from the surface of the liquid. (a) Find a formula for γ in terms of F and r . (b) At 30°C , if $F = 6.20 \times 10^{-3}$ N and $r = 2.9$ cm, calculate γ for the tested liquid.

- *70. (II) If the base of an insect's leg has a radius of about 3.0×10^{-5} m and the insect's mass is 0.016 g, would you expect the six-legged insect to remain on top of the water? Why or why not?
- *71. (III) Estimate the diameter of a steel needle that can just barely remain on top of water due to surface tension.

*10–14 Pumps; the Heart

- *72. (II) A physician judges the health of a heart by measuring the pressure with which it pumps blood. If the physician mistakenly attaches the pressurized cuff around a standing patient's calf (about 1 m below the heart) instead of the arm (Fig. 10–42), what error (in Pa) would be introduced in the heart's blood pressure measurement?

General Problems

73. A 3.2-N force is applied to the plunger of a hypodermic needle. If the diameter of the plunger is 1.3 cm and that of the needle is 0.20 mm, (a) with what force does the fluid leave the needle? (b) What force on the plunger would be needed to push fluid into a vein where the gauge pressure is 75 mm-Hg? Answer for the instant just before the fluid starts to move.
74. Intravenous transfusions are often made under gravity, as shown in Fig. 10–55. Assuming the fluid has a density of 1.00 g/cm^3 , at what height h should the bottle be placed so the liquid pressure is (a) 52 mm-Hg, and (b) 680 mm-H₂O? (c) If the blood pressure is 75 mm-Hg above atmospheric pressure, how high should the bottle be placed so that the fluid just barely enters the vein?
75. A beaker of water rests on an electronic balance that reads 975.0 g. A 2.6-cm-diameter solid copper ball attached to a string is submerged in the water, but does not touch the bottom. What are the tension in the string and the new balance reading?
76. Estimate the difference in air pressure between the top and the bottom of the Empire State Building in New York City. It is 380 m tall and is located at sea level. Express as a fraction of atmospheric pressure at sea level.
77. A hydraulic lift is used to jack a 960-kg car 42 cm off the floor. The diameter of the output piston is 18 cm, and the input force is 380 N. (a) What is the area of the input piston? (b) What is the work done in lifting the car 42 cm? (c) If the input piston moves 13 cm in each stroke, how high does the car move up for each stroke? (d) How many strokes are required to jack the car up 42 cm? (e) Show that energy is conserved.
78. When you ascend or descend a great deal when driving in a car, your ears “pop,” which means that the pressure behind the eardrum is being equalized to that outside. If this did not happen, what would be the approximate force on an eardrum of area 0.20 cm^2 if a change in altitude of 1250 m takes place?
79. Giraffes are a wonder of cardiovascular engineering. Calculate the difference in pressure (in atmospheres) that the blood vessels in a giraffe's head must accommodate as the head is lowered from a full upright position to ground level for a drink. The height of an average giraffe is about 6 m.
80. How high should the pressure head be if water is to come from a faucet at a speed of 9.2 m/s? Ignore viscosity.
81. Suppose a person can reduce the pressure in his lungs to -75 mm-Hg gauge pressure. How high can water then be “sucked” up a straw?
82. A bicycle pump is used to inflate a tire. The initial tire (gauge) pressure is 210 kPa (30 psi). At the end of the pumping process, the final pressure is 310 kPa (45 psi). If the diameter of the plunger in the cylinder of the pump is 2.5 cm, what is the range of the force that needs to be applied to the pump handle from beginning to end?
83. Estimate the pressure on the mountains underneath the Antarctic ice sheet, which is typically 2 km thick.
84. A simple model (Fig. 10–56) considers a continent as a block (density $\approx 2800 \text{ kg/m}^3$) floating in the mantle rock around it (density $\approx 3300 \text{ kg/m}^3$). Assuming the continent is 35 km thick (the average thickness of the Earth's continental crust), estimate the height of the continent above the surrounding mantle rock.

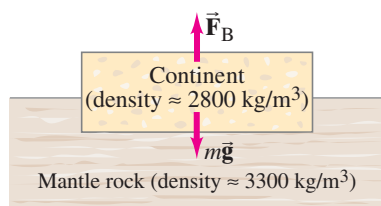


FIGURE 10–56 Problem 84.

85. A ship, carrying fresh water to a desert island in the Caribbean, has a horizontal cross-sectional area of 2240 m^2 at the waterline. When unloaded, the ship rises 8.25 m higher in the sea. How much water (m^3) was delivered?
86. A raft is made of 12 logs lashed together. Each is 45 cm in diameter and has a length of 6.5 m. How many people can the raft hold before they start getting their feet wet, assuming the average person has a mass of 68 kg? Do not neglect the weight of the logs. Assume the specific gravity of wood is 0.60.
87. Estimate the total mass of the Earth's atmosphere, using the known value of atmospheric pressure at sea level.

88. During each heartbeat, approximately 70 cm^3 of blood is pushed from the heart at an average pressure of 105 mm-Hg. Calculate the power output of the heart, in watts, assuming 70 beats per minute.
89. Four lawn sprinkler heads are fed by a 1.9-cm-diameter pipe. The water comes out of the heads at an angle of 35° above the horizontal and covers a radius of 6.0 m. (a) What is the velocity of the water coming out of each sprinkler head? (Assume zero air resistance.) (b) If the output diameter of each head is 3.0 mm, how many liters of water do the four heads deliver per second? (c) How fast is the water flowing inside the 1.9-cm-diameter pipe?
90. One arm of a U-shaped tube (open at both ends) contains water, and the other alcohol. If the two fluids meet at exactly the bottom of the U, and the alcohol is at a height of 16.0 cm, at what height will the water be?
91. The contraction of the left ventricle (chamber) of the heart pumps blood to the body. Assuming that the inner surface of the left ventricle has an area of 82 cm^2 and the maximum pressure in the blood is 120 mm-Hg, estimate the force exerted by that ventricle at maximum pressure.
92. An airplane has a mass of $1.7 \times 10^6 \text{ kg}$, and the air flows past the lower surface of the wings at 95 m/s. If the wings have a surface area of 1200 m^2 , how fast must the air flow over the upper surface of the wing if the plane is to stay in the air?
93. A drinking fountain shoots water about 12 cm up in the air from a nozzle of diameter 0.60 cm (Fig. 10–57). The pump at the base of the unit (1.1 m below the nozzle) pushes water into a 1.2-cm-diameter supply pipe that goes up to the nozzle. What gauge pressure does the pump have to provide? Ignore the viscosity; your answer will therefore be an underestimate.

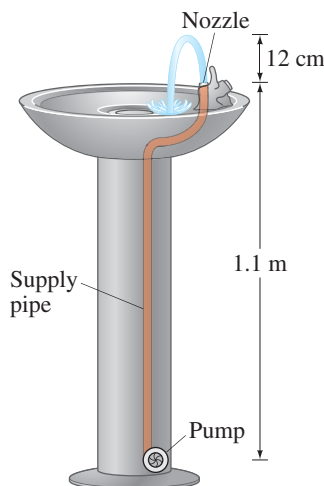


FIGURE 10–57
Problem 93.

94. A hurricane-force wind of 180 km/h blows across the face of a storefront window. Estimate the force on the $2.0 \text{ m} \times 3.0 \text{ m}$ window due to the difference in air pressure inside and outside the window. Assume the store is airtight so the inside pressure remains at 1.0 atm. (This is why you should not tightly seal a building in preparation for a hurricane.)

95. Blood is placed in a bottle 1.40 m above a 3.8-cm-long needle, of inside diameter 0.40 mm, from which it flows at a rate of $4.1 \text{ cm}^3/\text{min}$. What is the viscosity of this blood?
96. You are watering your lawn with a hose when you put your finger over the hose opening to increase the distance the water reaches. If you are holding the hose horizontally, and the distance the water reaches increases by a factor of 4, what fraction of the hose opening did you block?
97. A copper (Cu) weight is placed on top of a 0.40-kg block of wood (density $= 0.60 \times 10^3 \text{ kg/m}^3$) floating in water, as shown in Fig. 10–58. What is the mass of the copper if the top of the wood block is exactly at the water's surface?

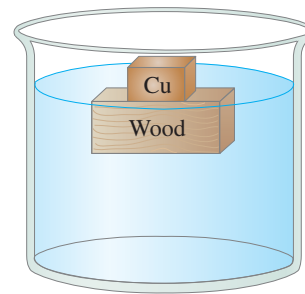


FIGURE 10–58 Problem 97.

98. You need to siphon water from a clogged sink. The sink has an area of 0.38 m^2 and is filled to a height of 4.0 cm. Your siphon tube rises 45 cm above the bottom of the sink and then descends 85 cm to a pail as shown in Fig. 10–59. The siphon tube has a diameter of 2.3 cm. (a) Assuming that the water level in the sink has almost zero velocity, use Bernoulli's equation to estimate the water velocity when it enters the pail. (b) Estimate how long it will take to empty the sink. Ignore viscosity.

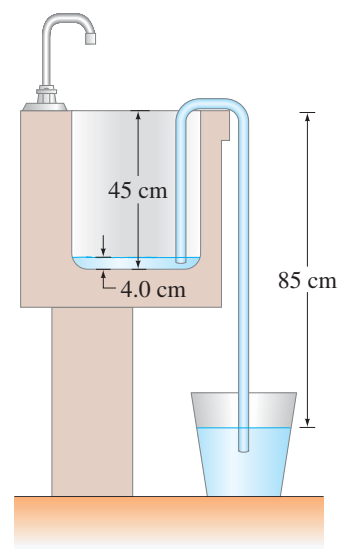


FIGURE 10–59
Problem 98.

- *99. If cholesterol buildup reduces the diameter of an artery by 25%, by what % will the blood flow rate be reduced, assuming the same pressure difference?

Search and Learn

1. A 5.0-kg block and 4.0 kg of water in a 0.50-kg container are placed symmetrically on a board that can balance at the center (Fig. 10–60). A solid aluminum cube of sides 10.0 cm is lowered into the water. How much of the aluminum must be under water to make this system balance? How would your answer change for a lead cube of the same size? Explain. (See Sections 10–7 and 9–1.)

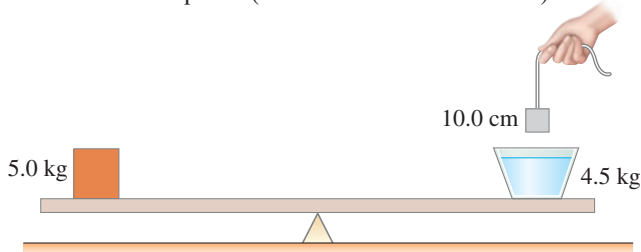


FIGURE 10–60 Search and Learn 1.

2. (a) Show that the buoyant force F_B on a partially submerged object such as a ship acts at the center of gravity of the fluid before it is displaced, Fig. 10–61. This point is called the **center of buoyancy**. (b) To ensure that a ship is in stable equilibrium, would it be better if its center of buoyancy was above, below, or at the same point as its center of gravity? Explain. (See Section 10–7 and Chapter 9.)

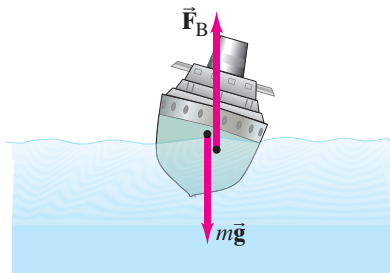


FIGURE 10–61
Search and Learn 2.

3. In working out his principle, Pascal showed dramatically how force can be multiplied with fluid pressure. He placed a long, thin tube of radius $r = 0.30$ cm vertically into a wine barrel of radius $R = 21$ cm, Fig. 10–62. He found that when the barrel was filled with water and the tube filled to a height of 12 m, the barrel burst. Calculate (a) the mass of water in the tube, and (b) the net force exerted by the water in the barrel on the lid just before rupture.

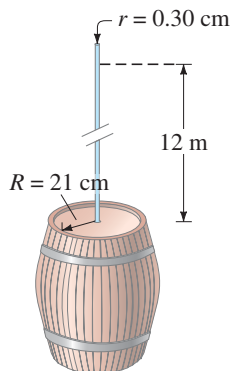


FIGURE 10–62 Search and Learn 3 (not to scale).

4. (a) When submerged in water, two objects with different volumes have the same *apparent* weight. When taken out of water, compare their weights in air. (b) Which object has the greater density?
5. A tub of water rests on a scale as shown in Fig. 10–63. The weight of the tub plus water is 100 N. A 50-N concrete brick is then lowered down from a fixed arm into the water but does not touch the tub. What does the scale read now? [Hint: Draw two free-body diagrams, one for the brick and a second one for the tub + water + brick.]

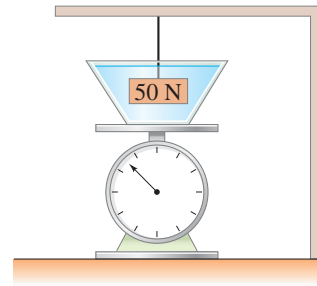


FIGURE 10–63 Search and Learn 5.

6. What approximations are made in the derivation of Bernoulli's equation? Qualitatively, how do you think Bernoulli's equation would change if each of these approximations was not made? (See Sections 10–8, 10–9, 10–11, and 10–12.)
- *7. Estimate the density of the water 5.4 km deep in the sea. (See Table 9–1 and Section 9–5 regarding bulk modulus.) By what fraction does it differ from the density at the surface?

ANSWERS TO EXERCISES

- A: (d).
B: The same. Pressure depends on depth, not on length.
C: (a).
D: (e).

- E: The rowboat is shaped to have a lot of empty, air-filled space, so its “average” density is much lower than that of water (unless the boat becomes full of water, in which case it sinks). Steel ships float for the same reason.
F: Increases.
G: (b).