

1 Kinematics

$$\vec{v}(t) = \vec{v}_0 + \vec{a}t \quad (1.0.1)$$

$$\vec{r}(t) = \vec{r}_0 + \vec{v}_0 t + \frac{1}{2} \vec{a} t^2 \quad (1.0.2)$$

$$\vec{v}^2(t) = \vec{v}_0^2 + 2\vec{a} \cdot (\vec{r}_1 - \vec{r}_0) \quad (1.0.3)$$

$$\vec{r} = \frac{\vec{v}_0 + \vec{v}_1}{2} t \quad (1.0.4)$$

2 Polar Coordinates

$$\hat{r} = \cos(\theta)\hat{x} + \sin(\theta)\hat{y} \quad (2.0.1)$$

$$\hat{\theta} = -\sin(\theta)\hat{x} + \cos(\theta)\hat{y} \quad (2.0.2)$$

$$\frac{d}{dt}\hat{r} = \dot{\theta}\hat{\theta} \quad (2.0.3)$$

$$\vec{r} = r(t) \cdot \hat{r}(t) \quad (2.0.4)$$

$$\vec{v} = \dot{r}\hat{r} + r\dot{\theta}\hat{\theta} \quad (2.0.5)$$

$$\vec{a} = (\ddot{r} - r\dot{\theta}^2)\hat{r} + (r\ddot{\theta} + 2\dot{r}\dot{\theta})\hat{\theta} \quad (2.0.6)$$

2.1 Uniform Circular Motion

θ is constant in time

$$\vec{v} = \omega r \hat{\theta} \quad (2.1.1)$$

$$\vec{a} = -\omega r^2 \hat{r} \quad (2.1.2)$$