

## Homework 10

Physics 5A

Due Sa 11 / 23 / 24 @ 11:59PM

The clearer your presentation is, the easier it is for us to give you points! "K.K." refers to the **2nd** edition of the textbook "An Introduction to Mechanics" authored by Kleppner & Kolenkow. Remember, you are encouraged to work together, but please make sure the work you turn in is your own.

### Problem 1. (15 pts)

A damped harmonic oscillator  $\ddot{x} + \gamma\dot{x} + \omega_0^2 x = 0$  with  $\omega_0 = 1$  radians/s begins with initial condition  $x(0) = 1$  m,  $v(0) = 0$ . Find and graph the analytic forms of the subsequent motion  $x(t)$  (you can either draw these graphs by hand, or use your favorite mathematical coding platform) for three cases:

- a)  $\gamma = 4/\text{s}$ .
- b)  $\gamma = 2/\text{s}$ .
- c)  $\gamma = 1/\text{s}$ .

### Problem 2. (15 pts)

A damped harmonic oscillator  $\ddot{x} + \gamma\dot{x} + \omega_0^2 x = 0$  is driven with an oscillating external force  $F_{\text{ext}} = m f_o \cos(\omega_D t)$ . Taking  $\omega_o = 10$  radians /s, and  $f_o = 1$  m/s<sup>2</sup>, find and graph the analytic forms of the amplitude of motion  $A(\omega_D)$  and relative phase between the drive and the steady state motion  $\phi(\omega_D)$  as a function of drive frequency  $\omega_D$  for three cases with different quality factors  $Q$  :

- a)  $Q = 1$ .
- b)  $Q = 2$ .
- c)  $Q = 10$ .

### Problem 3. (15 pts)

K.K. 11.7 (There is a typo in the problem: Part b) should ask for the time when the displacement will start to decrease, not the velocity.)

### Problem 4. (15 pts)

K.K. 11.9 (Note that here you are asked to find when the velocity, rather than the displacement, is in phase with the drive.)

**Problem 5.** (15 pts)

K.K. 11.11

**Problem 6.** (15 pts)

K.K. 11.14