

## CS2040S: Data Structures and Algorithms

### Discussion Group Problems for Week 3

*For: January 24–January 28*

#### Problem 1. Java Review

At this point, most of you should be comfortable enough to work with Java. Let's take some time to review a few concepts in Java so that we can limit our Java-related issues and, hence, focus on the algorithms when solving future Problem Sets.

- (a) What is the difference between a class and an object? Illustrate with an example.
- (b) Why does the `main` method come with a `static` modifier?
- (c) Give an example class (or classes) that uses the modifier `private` incorrectly (i.e., the program will not compile as it is, but would compile if `private` was changed to `public`).
- (d) The following question is about Interfaces.
  - (d)(i) Why do we use interfaces?
  - (d)(ii) Give an example of using an interface.
  - (d)(iii) Can a method return an interface?
- (e) Refer to `IntegerExamination.java`, which can be found in the same folder as this PDF. Without running the code, predict the output of the `main` method. Can you explain the outputs?
- (f) Can a variable in a parameter list for a method have the same name as a member (or static) variable in the class? If yes, how is the conflict of names resolved?

#### Problem 2. Asymptotic Analysis

This is a good time for a quick review of asymptotic big-O notation. For each of the expressions below, what is the best (i.e. tightest) asymptotic upper bound (in terms of  $n$ )?

- (a)  $f_1(n) = 7.2 + 34n^3 + 3254n$
- (b)  $f_2(n) = n^2 \log n + 25n \log^2 n$
- (c)  $f_3(n) = 2^{4 \log n} + 5n^5$
- (d)  $f_4(n) = 2^{2n^2+4n+7}$

**Problem 3. More Asymptotic Analysis!**

Let  $f$  and  $g$  be functions of  $n$  where  $f(n) = O(n)$  and  $g(n) = O(\log n)$ . Find the best asymptotic bound (if possible) of the following functions.

- (a)  $h_1(n) = f(n) + g(n)$
- (b)  $h_2(n) = f(n) \times g(n)$
- (c)  $h_3(n) = \max(f(n), g(n))$
- (d)  $h_4(n) = f(g(n))$
- (e)  $h_5(n) = f(n)^{g(n)}$

**Problem 4. Time Complexity Analysis**

Analyse the following code snippets and find the best asymptotic bound for the time complexity of the following functions with respect to  $n$ .

- (a) 

```
public int niceFunction(int n) {
    for (int i = 0; i < n; i++) {
        System.out.println("I am nice!");
    }
    return 42;
}
```
- (b) 

```
public int meanFunction(int n) {
    if (n == 0) return 0;
    return 2 * meanFunction(n / 2) + niceFunction(n);
}
```
- (c) 

```
public int strangerFunction(int n) {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < i; j++) {
            System.out.println("Execute order?");
        }
    }
    return 66;
}
```
- (d) 

```
public int suspiciousFunction(int n) {
    if (n == 0) return 2040;

    int a = suspiciousFunction(n / 2);
    int b = suspiciousFunction(n / 2);
    return a + b + niceFunction(n);
}
```

```

(e) public int badFunction(int n) {
    if (n <= 0) return 2040;
    if (n == 1) return 2040;
    return badFunction(n - 1) + badFunction(n - 2) + 0;
}

(f) public int metalGearFunction(int n) {
    for (int i = 0; i < n; i++) {
        for (int j = 1; j < i; j *= 2) {
            System.out.println("!");
        }
    }
    return 0;
}

(g) public String simpleFunction(int n) {
    String s = "";
    for (int i = 0; i < n; i++) {
        s += "?";
    }
    return s;
}

```

### Problem 5. Another Application of Binary Search

Given a sorted array of  $n-1$  unique elements in the range  $[1, n]$ , how would you find the missing element? Discuss possible naive solutions and possibly faster solutions.

### Problem 6. Yet Another Application of Binary Search

(Optional) Given an array of  $n$   $x$  and  $y$ -coordinates of an  $n$ -sided convex polygon in clockwise order, find a bounding box around the polygon. Discuss possible naive solutions and possibly faster solutions. A convex polygon is a polygon where all interior angles are less than 180 degrees.

An example of such an array is shown below:

