

Figure 1: *Temperature vs z plot. logarithmic y scale*

1a) In order to identify the layers I put conditions on temperature:

http://www.nasa.gov/mission_pages/iris/multimedia/layerzoo.html

Looking at the values from the file 'atmosphere.dat' ordered by height from top(of the atmosphere) to bottom I consider the corona while temperature ≥ 500000 K (T is decreasing), transition region until $T = 8000$ K, the chromosphere until T reaches the (only) minimum, afterwards the temperature starts to raise and I consider the layer before it reaches 6500 K the photosphere and the solar interior after

The exact values matching these conditions are:

corona between [39.802200, 2.535930] Mm temperatures: [1.080180e+06, 5.025160e+05] K

transition region between [2.516350, 0.991115] Mm temperatures: [4.991350e+05, 8.067640e+03] K

chromosphere between [0.971556, 0.305708] Mm temperatures: [7.306160e+03, 2.843670e+03] K

photosphere between [0.286093, -0.303487] Mm temperatures: [2.848470e+03, 6.297540e+03] K

solar interior between [-0.323184, -2.592960] Mm temperatures: [6.837750e+03, 2.068340e+04] K

1b) $\mu = \frac{n_H + 4n_{He}}{n_e + n_H + n_{He}}$
 $n_H = 10n_{He} \implies \mu = \frac{1.4n_H}{n_e + 1.1n_H}$

- totally ionized H and He $\implies n_e = n_H + 2n_{He} = 1.2n_H \implies \frac{n_H}{n_e} = \frac{5}{6}$ and $\mu = 0.6987$
- neutral H and He $\implies n_e = 0 \implies \mu = 1.2727$

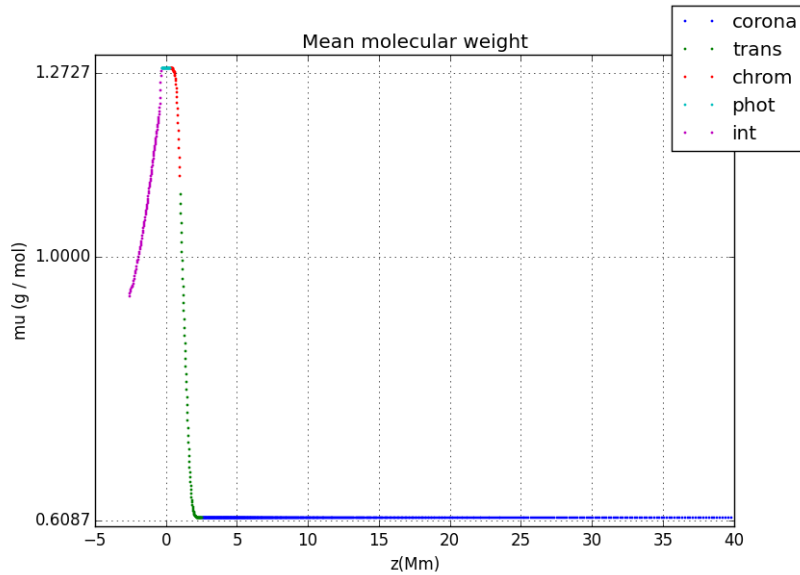


Figure 2: *Mean molecular weight(g/mol) vs z plot* Maximum close to $1.2727 = \mu$ in the case of neutral H and He and minimum close to $0.6087 = \mu$ calculated in the case of completely ionized H and He

$$\frac{n_H}{n_e} = \frac{\mu}{1.4 - 1.1\mu}$$

In the case of neutral H and He $n_e \rightarrow 0 \Rightarrow \frac{n_H}{n_e} \rightarrow \infty$

When plotting $\frac{n_H}{n_e}$ using μ from the file, as we can see in the graphic of μ there are some values of z for which $\mu > 1.2727 \Rightarrow 1.4 - 1.1\mu < 0 \Rightarrow \frac{n_H}{n_e} < 0$

I will limit my axis values to $[0, 4]$

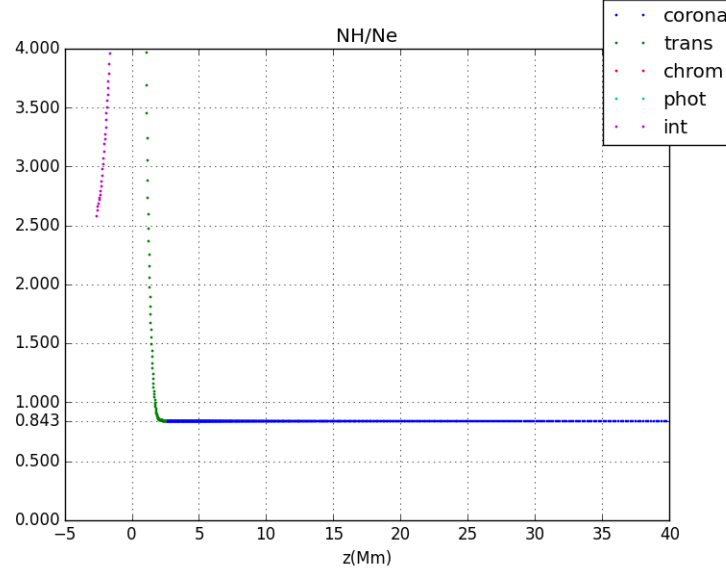


Figure 3: number of atoms of H / number of electrons

We can see a constant value of $\frac{n_H}{n_e}$ in the corona of $\frac{n_H}{n_e} = 0.843 \approx \frac{5}{6}$ which is the value we calculate in the case of totally ionized H and He and we expect this because of the high values of the temperature in the corona

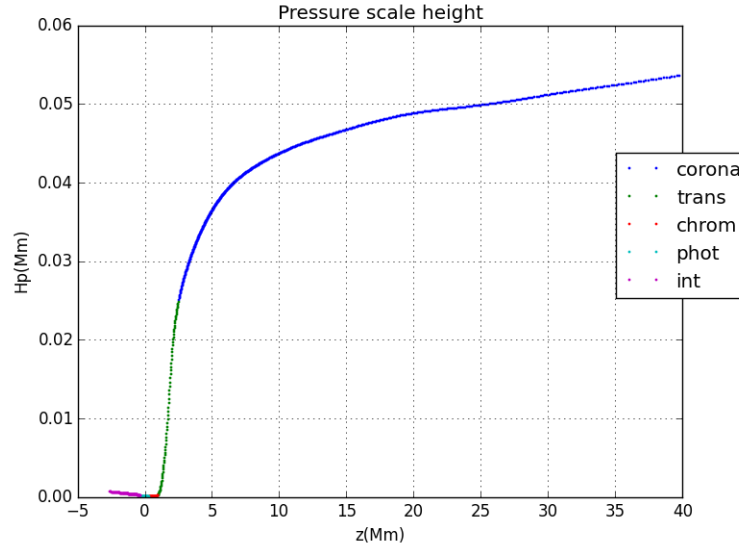


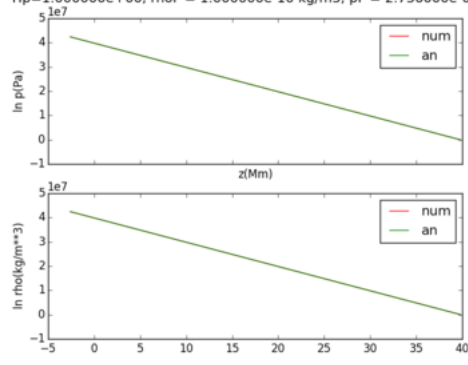
Figure 4: Pressure scale height

$$2) \quad \frac{d \ln p}{dz} = -\frac{1}{H_p}, H_p \text{ const} \Rightarrow \ln p(z) - \ln p(z_0) = -\frac{1}{H_p}(z - z_0) \Rightarrow p(z) = p(z_0) \exp\left(-\frac{z - z_0}{H_p}\right)$$

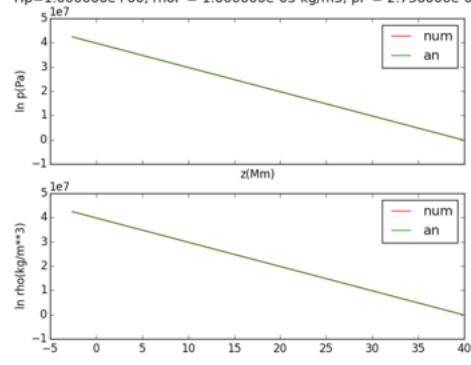
$$\rho(z) = \frac{1}{g H_p} p(z) = \frac{p(z_0)}{g H_p} \exp\left(-\frac{z - z_0}{H_p}\right) = \rho(z_0) \exp\left(-\frac{z - z_0}{H_p}\right)$$

Analytic test for H_p constant (with values 1 and 1e10) with $\rho(z_{max})$ taking values: $1e-10, 1e-5, 1e-2, 1, 1e2, 1e3, 1e7, 1e10$
Integrating downward or forward in height makes no difference (using $\ln p$)

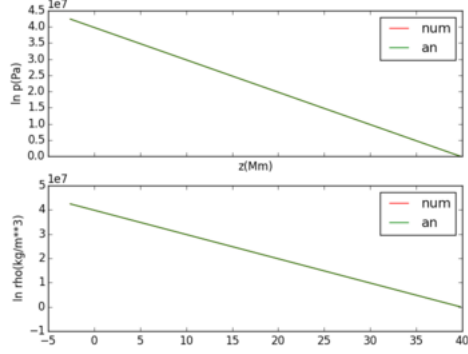
Hp=1.000000e+00, rhoF = 1.000000e-10 kg/m3, pF = 2.736000e-08 Pa



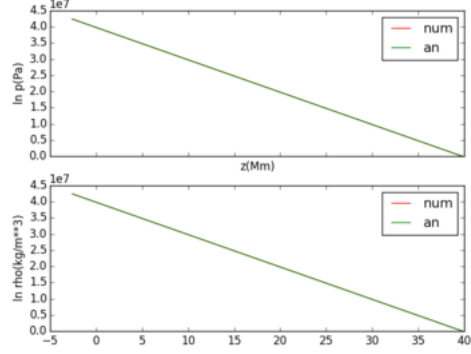
Hp=1.000000e+00, rhoF = 1.000000e-05 kg/m3, pF = 2.736000e-03 Pa



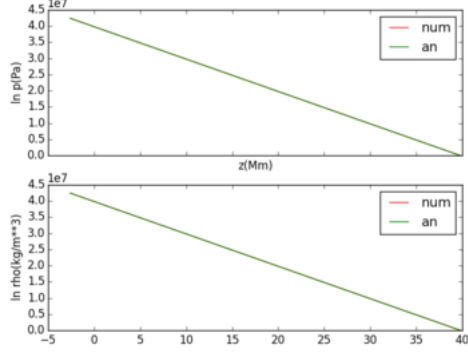
Hp=1.000000e+00, rhoF = 1.000000e-02 kg/m3, pF = 2.736000e+00 Pa



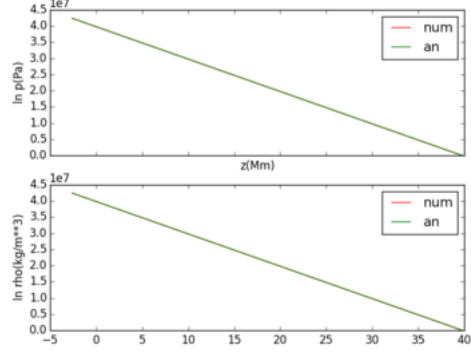
Hp=1.000000e+00, rhoF = 1.000000e+00 kg/m3, pF = 2.736000e+02 Pa



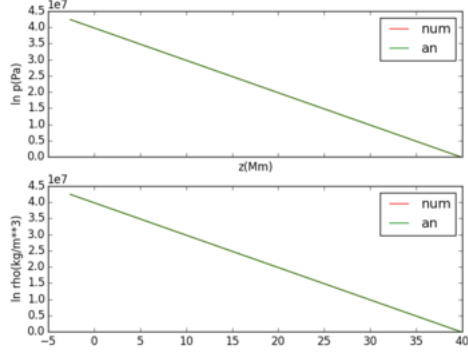
Hp=1.000000e+00, rhoF = 1.000000e+02 kg/m3, pF = 2.736000e+04 Pa



Hp=1.000000e+00, rhoF = 1.000000e+03 kg/m3, pF = 2.736000e+05 Pa



Hp=1.000000e+00, rhoF = 1.000000e+07 kg/m3, pF = 2.736000e+09 Pa



Hp=1.000000e+00, rhoF = 1.000000e+10 kg/m3, pF = 2.736000e+12 Pa

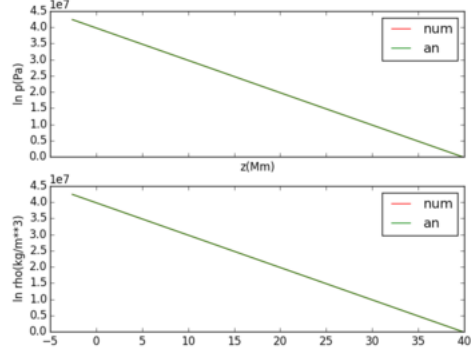


Figura 5: Analytic test Hp=1

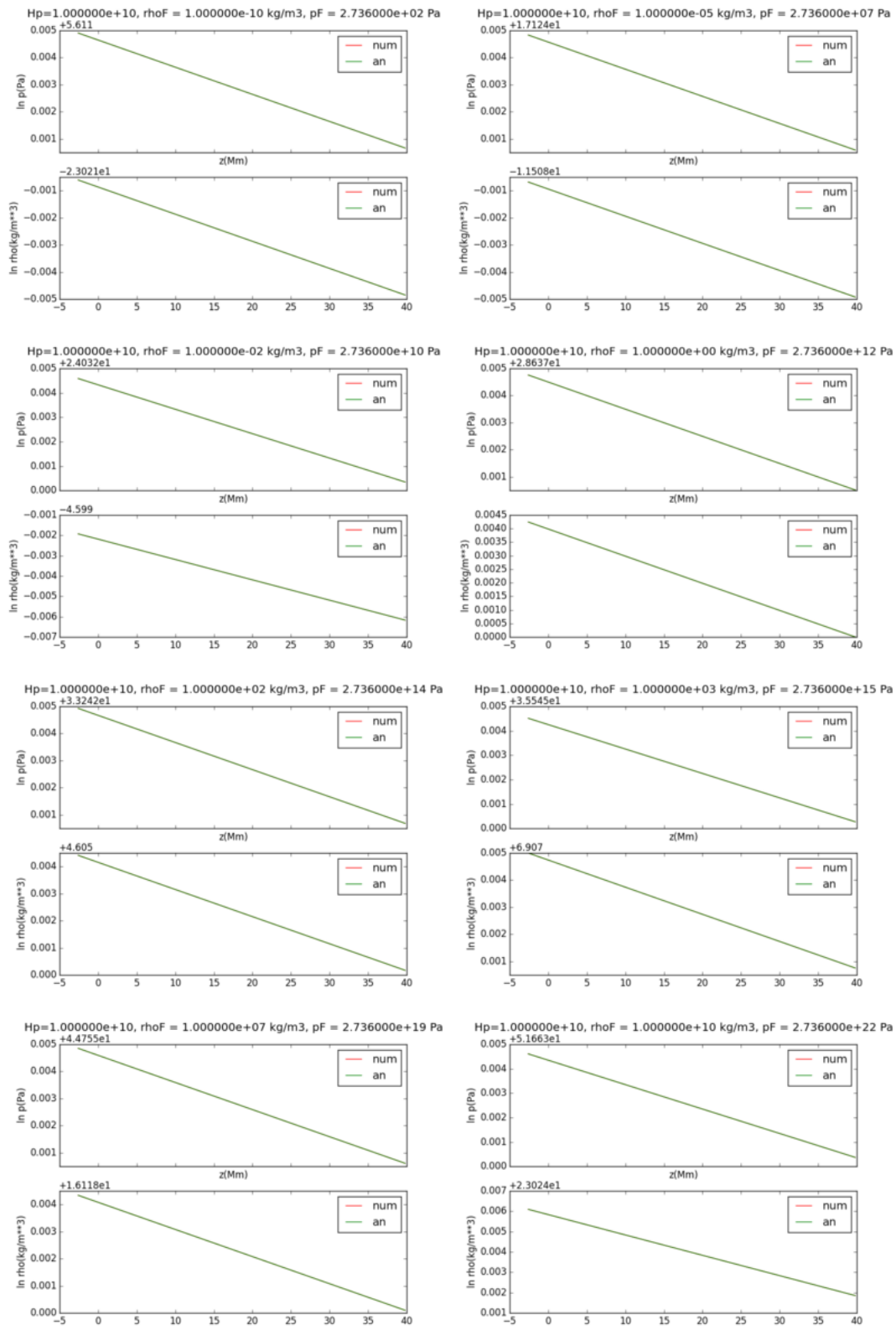


Figura 6: Analytic test $H_p=1e10$

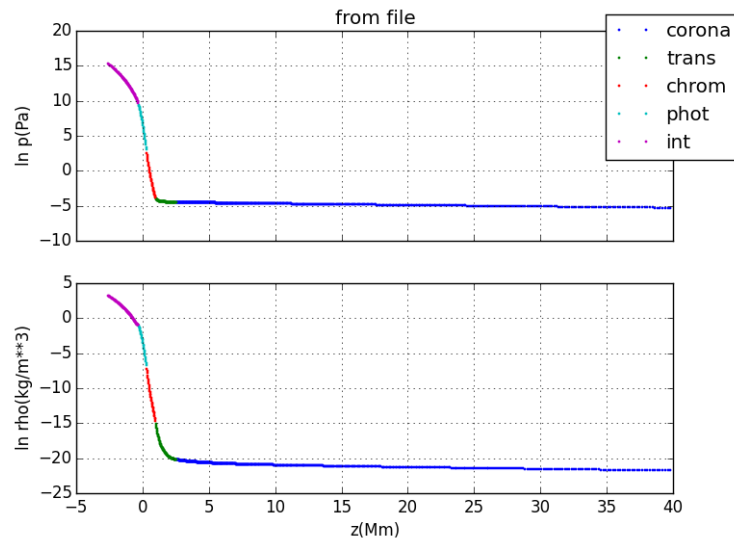


Figure 7: logarithmic (base e: ln) of pres, rho

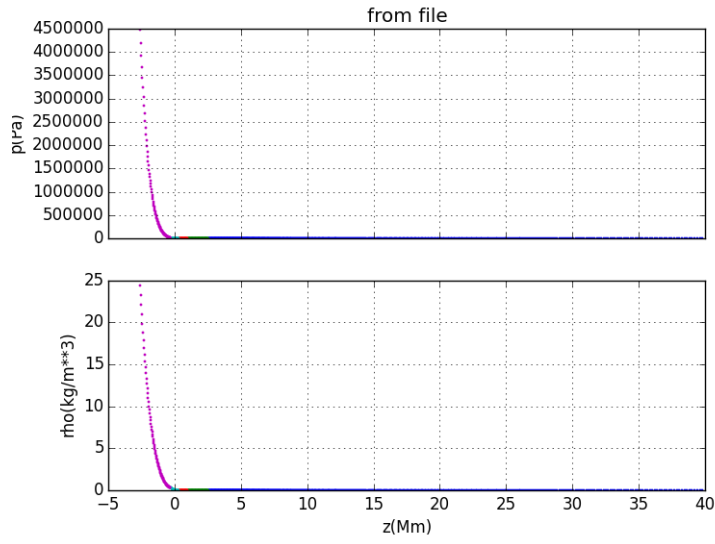


Figure 8: pres, rho

Notation: μ_0 = magnetic permeability

$$\beta = \frac{p}{p_{mag}} \text{ where } p_{mag} = \frac{B^2}{2\mu_0}$$

$$v_A = \frac{B^2}{\mu_0 \rho}$$

$$c_s = \sqrt{\frac{\gamma p}{\rho}}$$

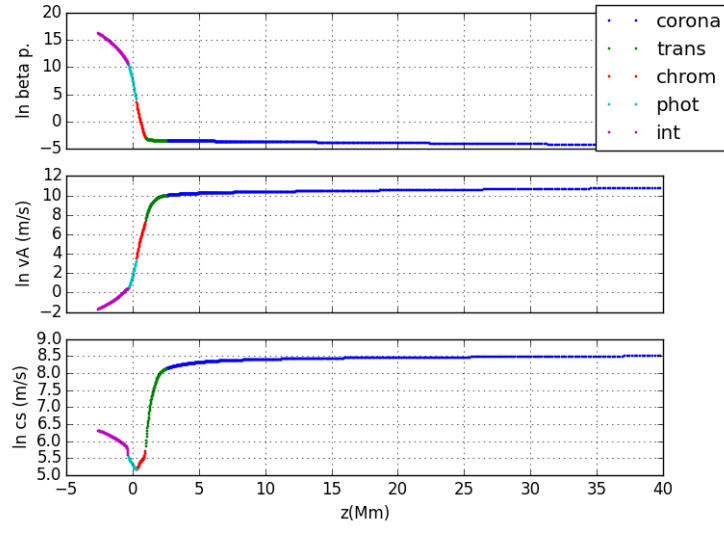


Figure 9: logarithmic (base e: \ln) of beta plasma, vA, cs

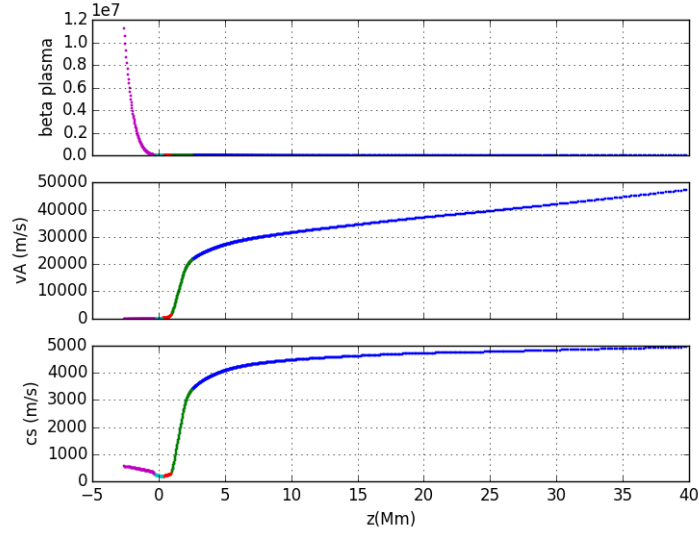


Figure 10: beta plasma, vA, cs

$$\beta = \frac{2p\mu_0}{B^2} = \frac{2p}{\rho v_A^2} = \frac{2}{\gamma} \left(\frac{c_s}{v_A} \right)^2 \implies \beta \left(\frac{v_A}{c_s} \right)^2 \frac{\gamma}{2} = 1$$

We call this function $\text{func}(\beta, \frac{v_A}{c_s})$ in the graphic below and expect it to be 1

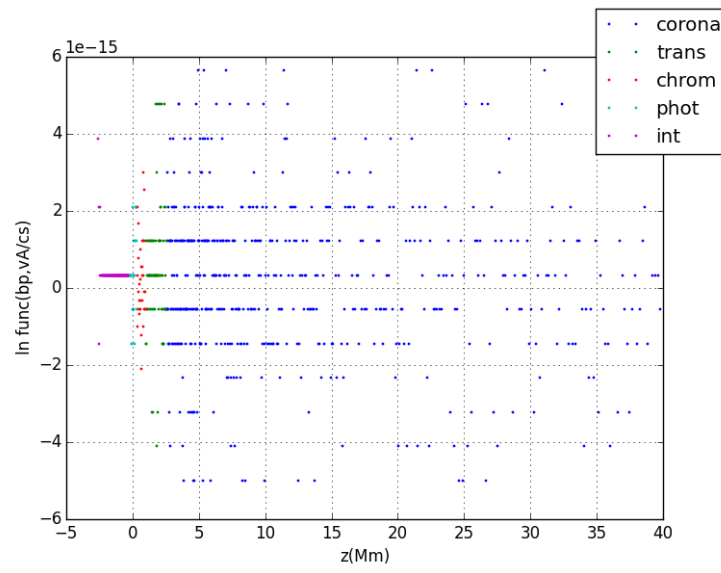


Figura 11: $\ln \text{func}(\text{bp}, \text{vA}/\text{cs}) \approx 0$

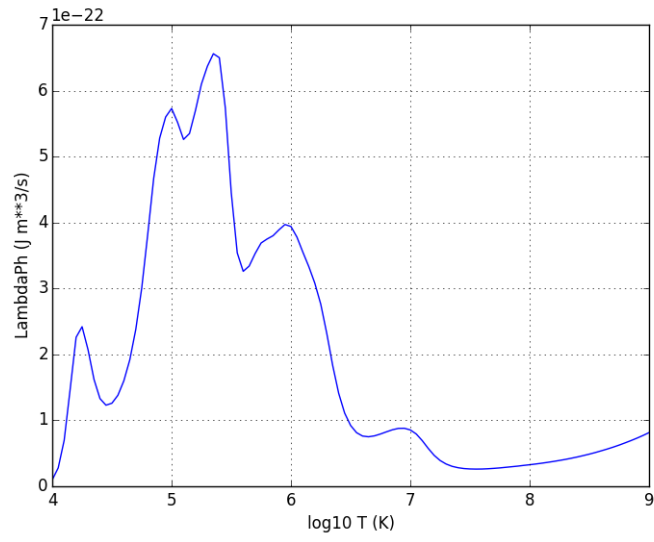


Figura 12: Λ_{phot}

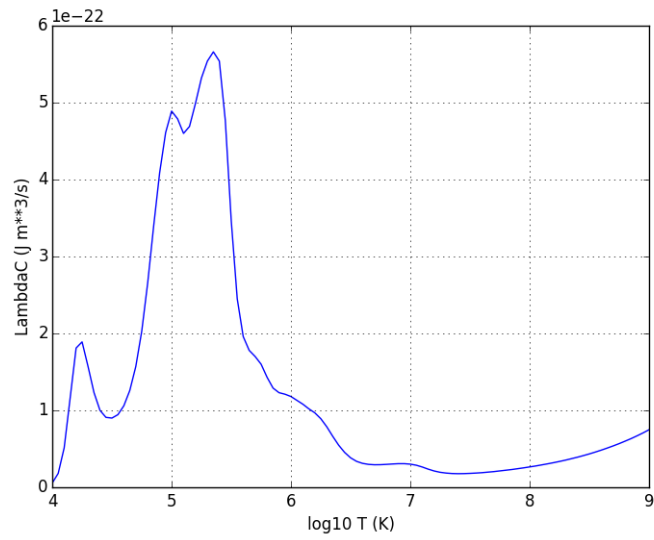


Figura 13: Λ_{corona}

3a) Both functions have the maximum for $T = 2.238721 \times 10^5 \text{ K}$

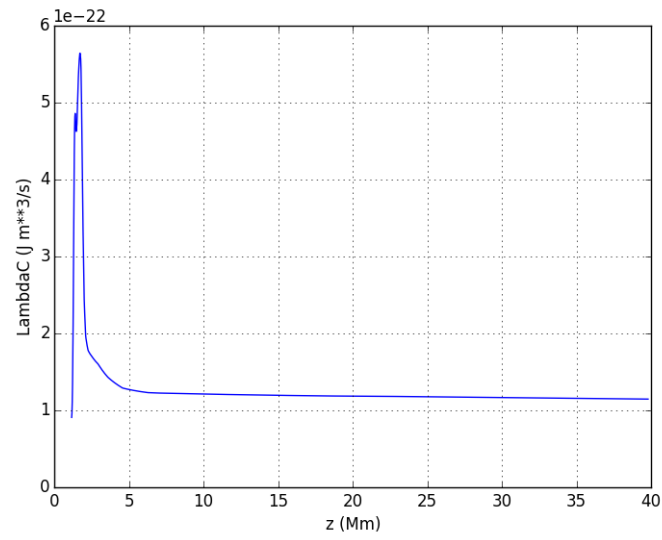


Figura 14: Lambda corona interpolated for atm. temperatures $> 3 \times 10^4$ K in 'atmosphere.dat' plotted vs z

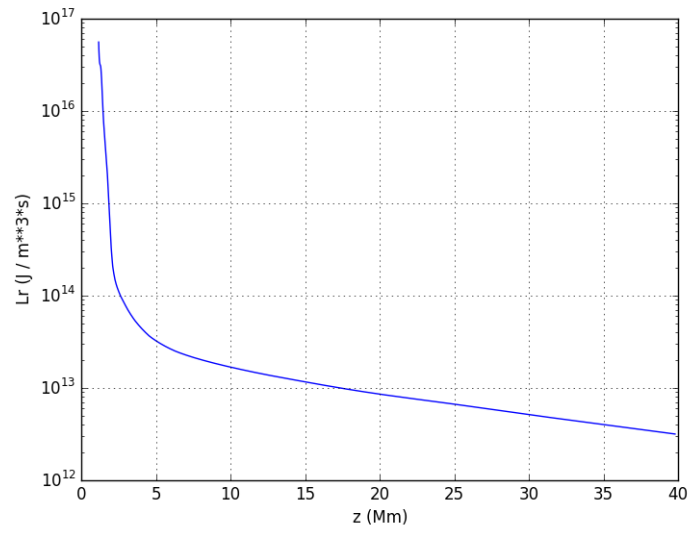


Figura 15: Lr logarithmic y scale

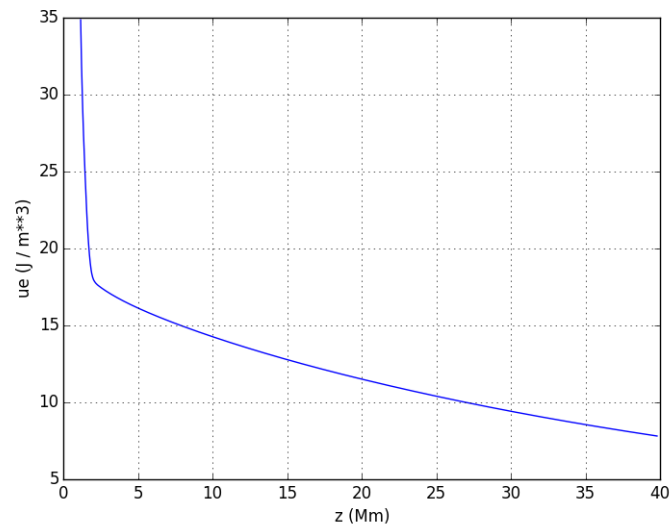


Figura 16: Internal energy

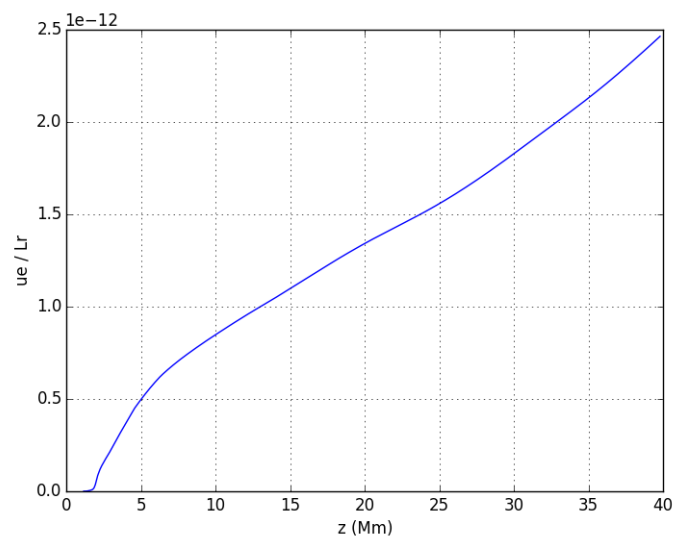


Figura 17: Internal energy / Lr