

## Results

Without losing generality we can consider  $\rho_{\text{Left}}$  greater than  $\rho_{\text{Right}}$  otherwise the graphic will be reversed (the shock wave moving to the left, the rarefaction wave moving to the right, and the velocity with inversed sign)

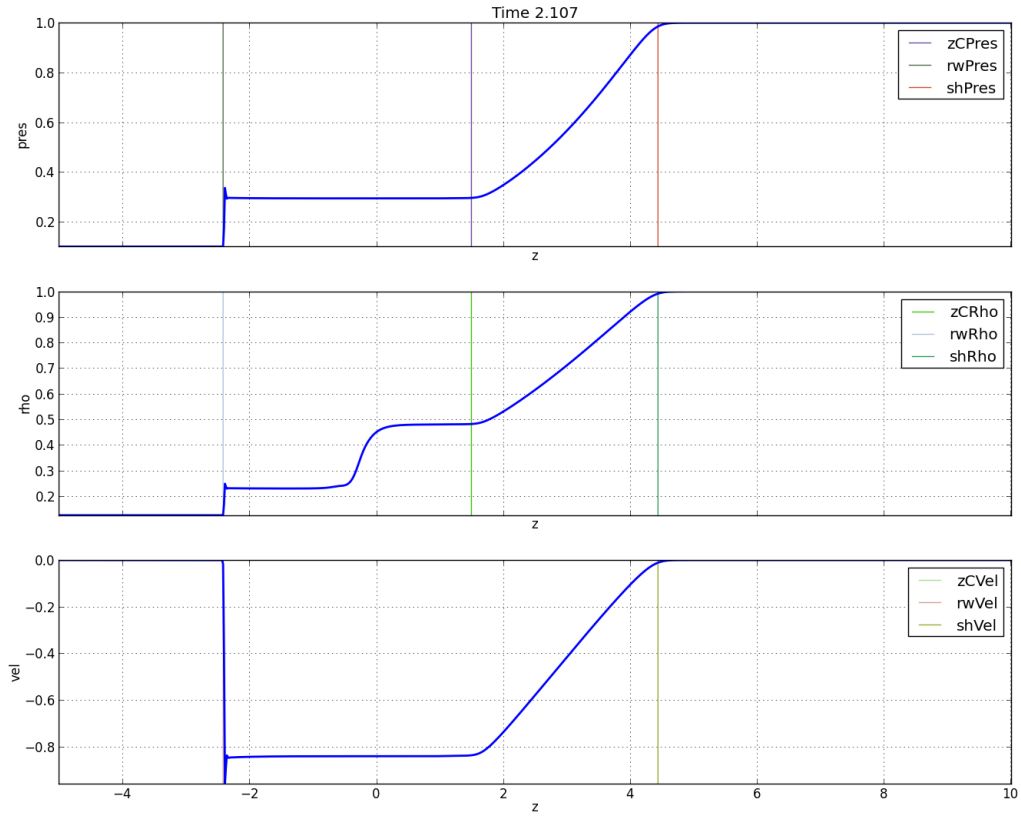


Figura 1: *shock tube reversed*

From now on we only consider cases when shock wave is moving left and rw left (it's checked in initcond.riemann for  $\rho_1 > \rho_2$ )

The points in the task file : p1, p2, p3, p4, p5, p6 Obs:

1.  $\text{pres1} = \text{presRight}$

2.  $\rho_1 = \rho_{\text{Right}}$
3.  $v_1 = v_{\text{Right}}$
4.  $v_2 = v_3$
5.  $p_2 = p_3$
6.  $p_6 = p_{\text{Left}}$
7.  $v_6 = v_{\text{Left}}$
8.  $\rho_6 = \rho_{\text{Left}}$
9. in the discontinuity part ( $p_2-p_3$ ) density is not constant, dcPoint will mark where it changes(it's discontinuous)  $\rho_2 < \rho_1$
1. rwPoint and shPoint are determined empirically(taking the points from left, right respective when the function pressure is not constant anymore) - analyze\_functions.py
2. The rarefaction wave is moving with speed( $cs_{\text{RW}}$ )  $v_{\text{Left}} - cs_{\text{Left}}$  and rwPoint is also plotted like this (rwPointAn in the graphic: Point is Rho, Pres and Vel). The point is initialized with the value of rwPoint after the time = timeAfterAnPoints (defined in riemann\_params.py)
3. When  $v_{\text{Left}} = v_{\text{Right}} = 0$ (not in the case of complete problem) the shock wave is moving with speed( $cs_{\text{Shock}}$ )  $v_2 * \rho_2 / (\rho_2 - \rho_{\text{Right}})$  in the graphic marked as shPointAn initialized in the same way as rwPointAn(after timeAfterAnPoints)
4. dcPoint is moving with speed  $v_2$  and it's initialized at the beginning = zC(it is analytically calculated. here analytically means that it was calculated and not empirically determined by observing the shapes of the functions )
5. the expressions from tasks file are evaluated after timeAfterAnPoints so we should redirect output

```
python main.py --timeEnd=10 > out
```

The output for the parameters in tasks file is in files out\_\*

6. We can mark point p1, p2, p3, p4, p5, p6 - (set mark6Points to True in model\_riemann.py) to see where actually the values are calculated - they are points right and left of shPoint, zC, and rwPoint respectively (we can change them moving them closer or farther - the distance from the points is equal) by changing delta in checkExpressions function in model\_riemann.py

## Shock tube

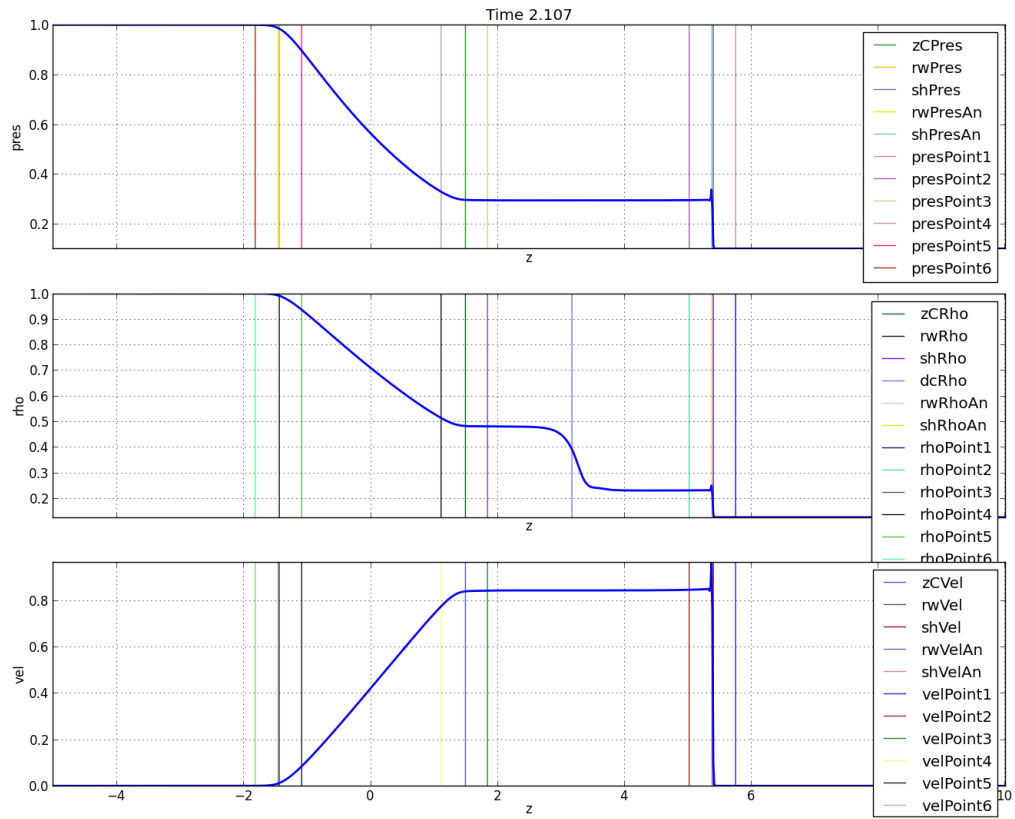


Figura 2: *shock tube*

Observations:

1.  $cs6 = -csRW$
2.  $csShock > cs1$  and  $csShock > cs2$
3. relations fulfilled see out\_shocktube file

## Complete

Observations:

1.  $csRW = cs6 - velLeft$  (this is true in all cases)
2. I don't know how to determine analytically  $csShock$  in this case when velocities are not 0 (but I think there is a way), that's why  $shPointAn$  is not shown in the graph in this case. I could calculate  $csShock$  from empirical determination of  $shPoint$  ( $csShock = (shPoint - shPointPrevious) / dt$ ), but this not done yet (to compare with  $cs1$  and  $cs2$ ). Calculating  $csShock$  as  $\sqrt{\gamma * pres / \rho}$  in  $shPoint$  is not practical because of the discontinuity and oscillations
3. relations fulfilled see out\_complete file
4. making  $velRight = -300$  (greater than  $csShock$ ) will make appear oscillations
5. But this was the case when  $velRight < 0$  and  $velLeft > 0$ , when changing signs (fluids not approaching each other) this oscillation does not appear

## Expansion into vacuum

Observations:

1. fluid from left is not filling instantly the right side
2. velocity grows slower in case b
3. density falls faster in case a - because of low density  $shPointAn$  is not very well calculated

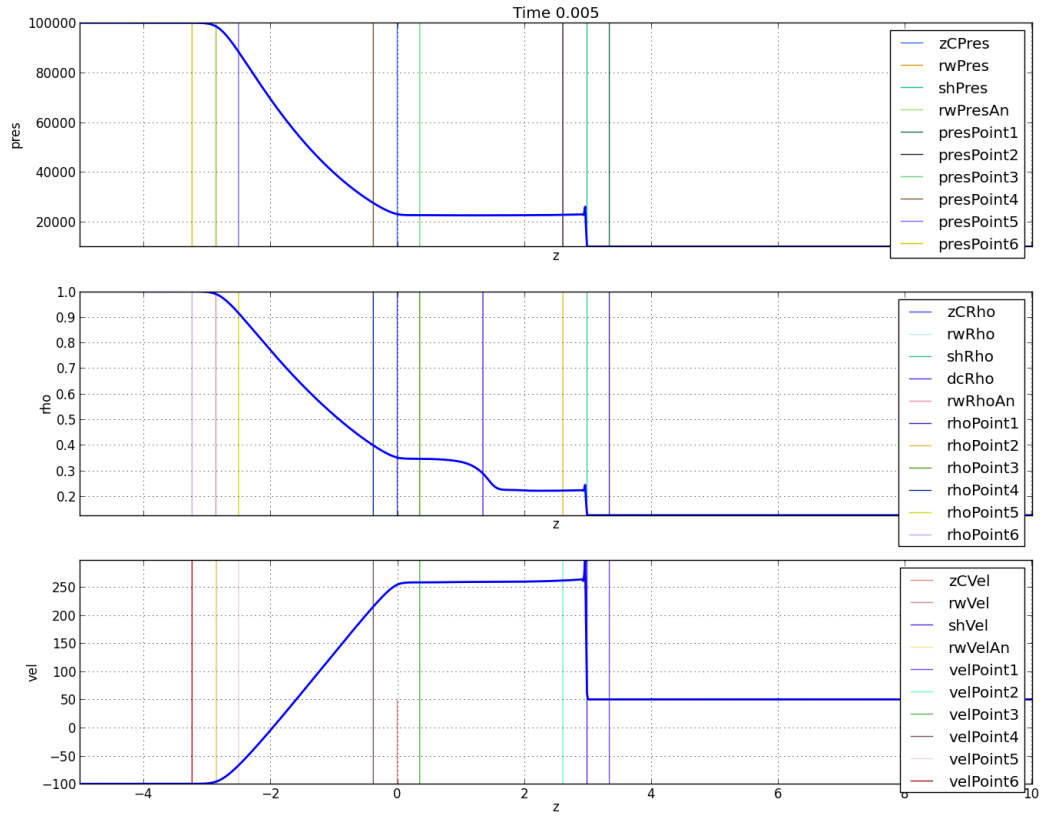


Figura 3: *complete*

## TODO

1. move legend out of the plot
2. calculate  $shPoint$  velocity ( $csShock$ ) in case of complete problem (I don't know the analytical solution in this case)

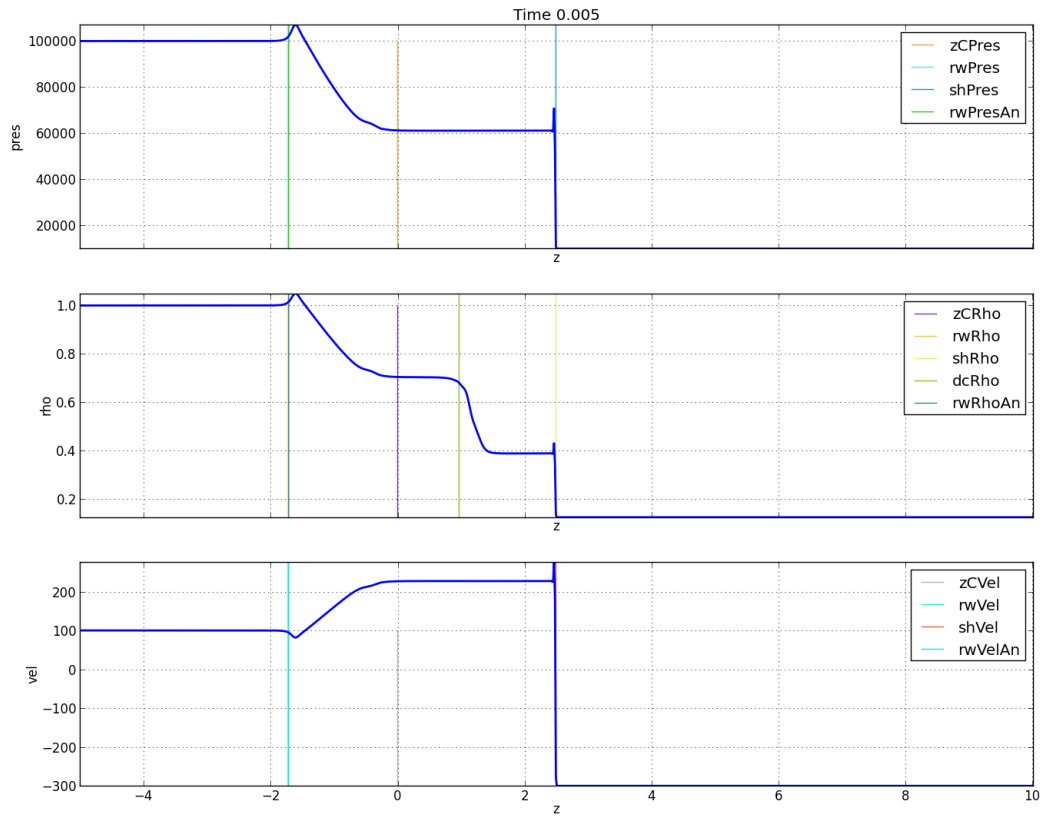


Figura 4: *complete abs(velRight) bigger*

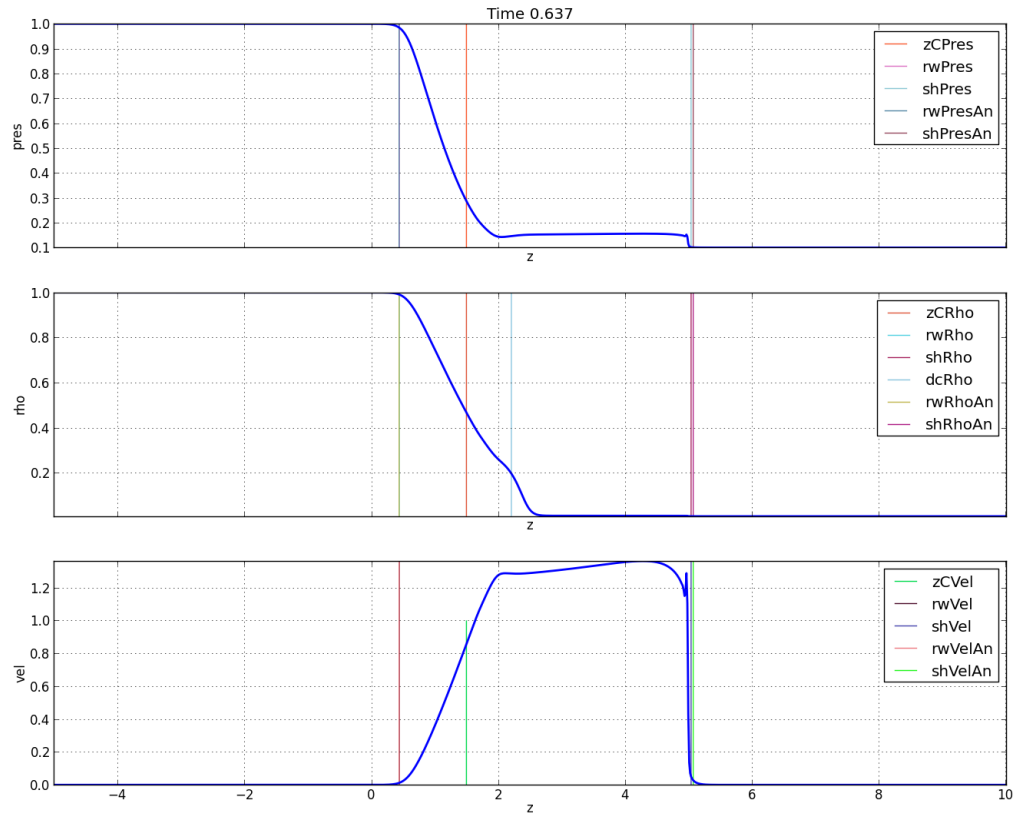


Figura 5: *exp vacuum case a*

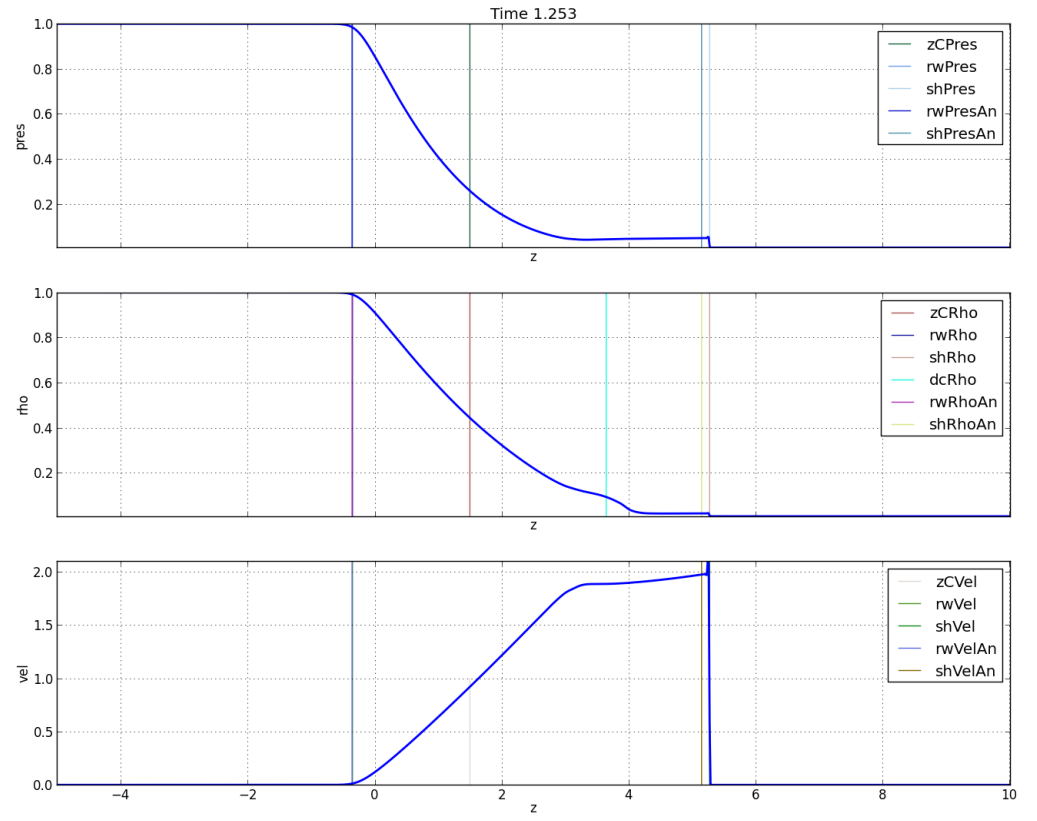


Figura 6: *exp vacuum case b*