### Results

Without losing generality we can consider rhoLeft greater than rhoRight otherwise the graphic will be reversed (the shock wave moving to the left, the rarefaction wave moving to the right, and the velocity with inversed sign)

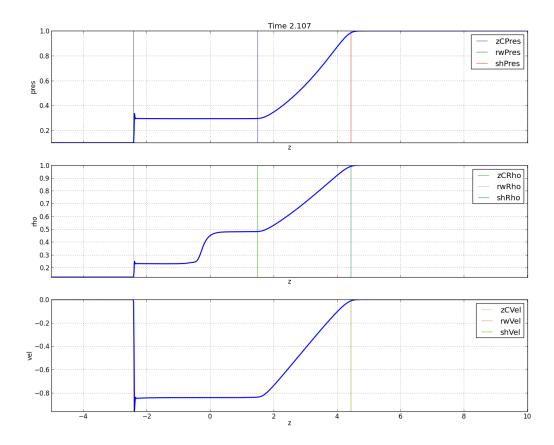


Figura 1: shock tube reversed

From now on we olly consider cases when shock wave is moving left and rw left(it's checked in initcond\_riemann for rho1 >rho2)

The points in the task file: p1, p2, p3, p4, p5, p6 Obs:

1. pres1 = pLeft

- 2. rho1 = rhoLeft
- 3. vel 1 = velLeft
- 4. vel 2 = vel 3
- 5. pres2 = pres3
- 6. pres6 = presLeft
- 7. vel6 = velLeft
- 8. rho6 = rhoLeft
- 9. in the discontinuity part (p2-p3) density is not constant, dcPoint will mark where it changes(it's discontinuous) rho2 <rho1
- 1. rwPoint and shPoint are determined empirically(taking the points from left, right respective when the function pressure is not constant anymore)
- 2. The rarefaction wave is moving with speed(csRW) velLeft csLeft and rwPoint is also plotted like this (rwPointAn in the graphic: Point is Rho, Pres and Vel). The point is initialized with the value of rwPoint after the time = timeAfterAnPoints (defined in riemann\_params.py)
- 3. When velLeft = velRight = 0 the shock wave is moving with speed(csShock) vel2 \* rho2 / (rho2 rhoRight) in the graphic marked as shPointAn initialized in the same way as rwPointAn
- 4. dcPoint is moving with speed vel2 and it's initialized at the beginning = zC

We can mark point p1, p2, p3, p4, p5, p6 - (set mark6Points to True in model\_riemann.py) to see where actually the values are calculated (we can change them (moving them closer or farther) by changing delta in checkExpressions function in model\_riemann.py

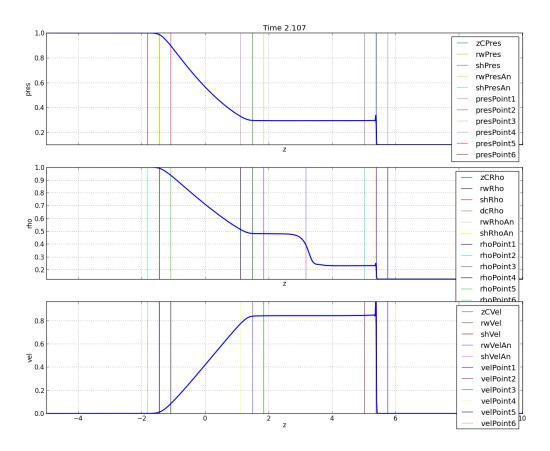


Figura 2: shock tube

### Shock tube

Observations:

- 1. cs6 = -csRW
- 2. csShock >cs1 and csShock >cs2
- 3. relations fulfilled see out\_shocktube file

## Complete

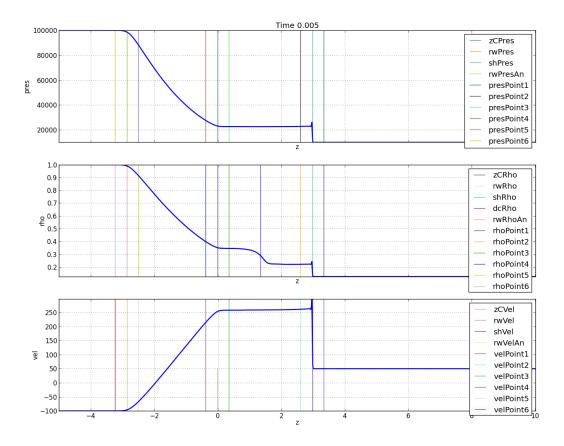


Figura 3: complete

#### Observations:

- 1. csRW = cs6 velLeft (this should always be true)
- 2. I don't know how to determine analytically csShock in this case when velocities are not 0(but I think there is a way), that's why shPointAn is not shown in the graph in this case. I could calculate

csShock from empirical determination of shPoint (csShock = (shPoint - shPointPrevious) / dt) , but this not done yet(to compare with cs1 and cs2). Calculating csShock as sqrt(gamma \* pres / rho) in shPoint is not practical because of the discontinuity and oscillations

- 3. relations fulfilled see out\_complete file
- 4. making velRight = -300 (greater than csShock) will make appear oscillations

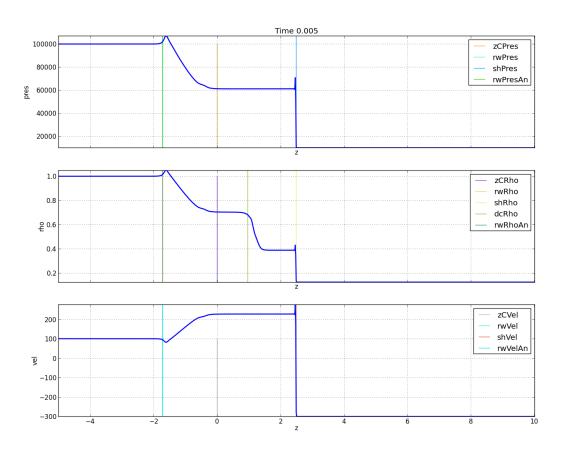


Figura 4: complete velRight bigger

# Expansion into vacuum

#### Case a

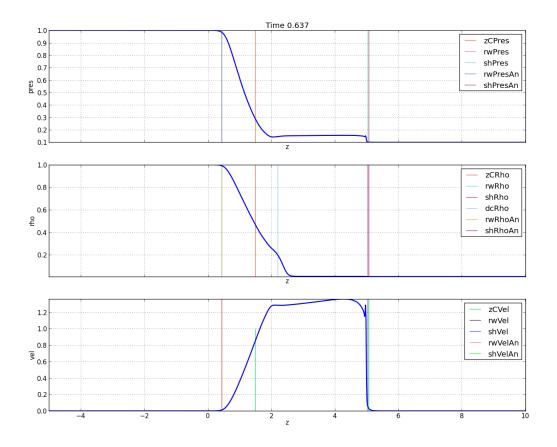


Figura 5: exp vacuum case a

#### Case b Observations:

- 1. velocity grows slower in case b
- 2. density falls faster in case a because of low density shPointAn is not very well calculated

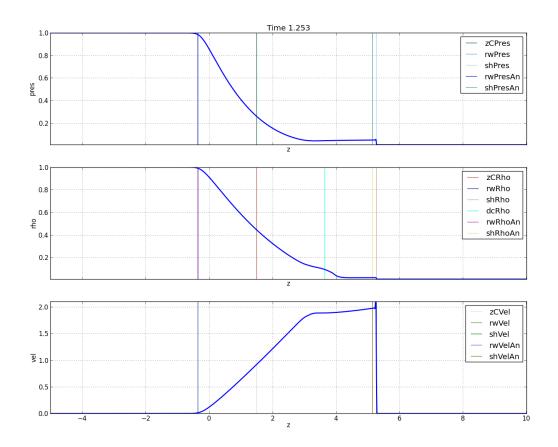


Figura 6:  $exp\ vacuum\ case\ b$ 

## TODO

- 1. move legend out of the plot
- 2. calculate shPoint velocity (csShock) in case of complete problem (I don't know the analytical solution in this case)