



$$\forall T \in Ob(C) \exists! 1^T \in T \rightarrow 1$$

let $(t_1, t_2) \in (T \rightarrow B \times T \rightarrow C) := (p_1 \circ T^1, p_2 \circ T^1)$ then

$$\forall (t'_1, t'_2) \in (T \rightarrow B \times T \rightarrow C)$$

$$\exists! x \in (T \rightarrow 1) \mid t'_1 = p_1 \circ x \wedge t'_2 = p_2 \circ x$$

but

$$(T \rightarrow 1) = \{T^1\} \text{ so } (t'_1, t'_2) = (p_1 \circ T^1, p_2 \circ T^1)$$

$$\forall (t'_1, t'_2) \in (T \rightarrow B \times T \rightarrow C);$$

$$(T \rightarrow B) = \{p_1 \circ T^1\} \forall T \in Ob(C) \implies$$

$$B \text{ terminal} \implies$$

$$B \simeq 1 \implies$$

$$1 = B \times C = B \blacksquare$$

$$1 = B \times C \implies B = B \times C$$