Pullback of $B \to P(A)$ is unique