



$$h \circ f = i \circ g$$

$$\forall X \in \text{Ob}(C), \forall \langle p, q \rangle \in B \rightarrow X \times C \rightarrow X$$

$$\exists! r \mid r \circ h = p \wedge r \circ i = q$$

$$\forall X \in \text{Ob}(C), \forall \langle p, q \rangle \in B \rightarrow X \times C \rightarrow X$$

$$pf_X!(p, q) := \text{unique } r \mid r \circ h = p \wedge r \circ i = q$$

$$\forall X \in \text{Ob}(C) \forall \{p, q\} \subseteq B \rightarrow X$$

$$p \circ f = q \circ f \implies p = q$$

$$x \in D \rightarrow X \mid x \circ i = y \circ i \wedge h \circ f = i \circ g \implies$$

$$(x \circ h) \circ f$$

$$= x \circ (h \circ f)$$

$$= x \circ (i \circ g)$$

$$= (x \circ i) \circ g$$

$$= (y \circ i) \circ g$$

$$= y \circ (i \circ g)$$

$$= y \circ (h \circ f)$$

$$= (y \circ h) \circ f \implies$$

$$x \circ h = y \circ h$$

$$x = pf_X!(x \circ h, x \circ i) = pf_X!(y \circ h, y \circ i) = y \implies$$

$$i \text{ is epic}$$

pushout of epic is epic ■