

Final Exam

Show all of your work. Correct answers without showing how to get them does not earn you points.

There are TWO pages and NINE questions. The maximum number of points is 100.

(1) Solve the logarithmic equation. Do not use a calculator for your calculation. It's OK to use a calculator to check your answer. [9]

$$\log_2 x - \log_2 \frac{1}{4} = 3 \quad (1)$$

(2) Solve the trigonometric equation in $\{x \in \mathbb{R} | 0^\circ \leq x < 360^\circ\}$. [12]

$$5 \cos^2 x = 4 \sin x + 4 \quad (2)$$

(3) Solve the following system of equations by any method. [9]

$$\begin{array}{rcl} x & + & \frac{1}{5}y = \frac{4}{3} \\ 3x & - & 2y = -9 \end{array} \quad (3)$$

(4) A surveyor measures an angle at $53^\circ 16' 26''$. She knows from long experience that the true angle (as opposed to her measurement) is a normally distributed random variable with a mean of $53^\circ 16' 26''$ and a standard deviation of $1' 13''$. What is the probability that the true angle is between $53^\circ 16'$ and $15^\circ 17'$? [12]

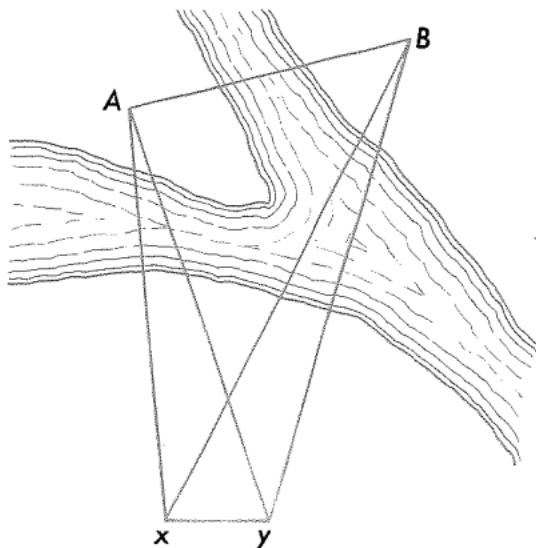
(5) Vancouver is at $49^\circ 15' N, 123^\circ 6' E$. Osaka in Japan is at $34^\circ 42' N, 135^\circ 30' E$. Honolulu on Hawaii is at $21^\circ 18' N, 157^\circ 49' W$. Two airplanes leave from Vancouver to go to their respective destinations, Osaka and Honolulu, along a great circle. What is the angle between the routes of the two airplanes as they leave Vancouver? [12]

(6) Solve the exponential equation. Do not use a calculator for your calculation. It's OK to use a calculator to check your answer. [10]

$$3^{x-1} = e^{3x} \quad (4)$$

- (7) The points A and B in the figure are on opposite sides of the river and inaccessible from points x and y . Find the distance AB from the survey notes. [12]

distance from x to y	450ft
angle at x for triangle Axy	129°
angle at y for triangle Ayx	32°
angle at x for triangle Bxy	43°
angle at y for triangle Byx	113°



- (8) Solve the following right spherical triangle with a right angle at A . [12]

$$b = 56^\circ 21' 30'', B = 59^\circ 15' 32'' \quad (5)$$

- (9) According to 2010 census data, the ratio of men to women among centenarians is 1 : 4 (i.e. 20% of centenarians are men). Use normal approximation of the binomial distribution to calculate the probability that out of 50 centenarians 12 or more are male. [12]