Echelon Form and Complex Numbers

(1) Find the equation of the quadratic

$$y = ax^2 + bx + c \tag{1}$$

which passes through (0,0),(1,2),(-1,3).

(2) Find the determinant for the following Hermitian matrix. What do you notice?

$$\begin{bmatrix} 4 & 3-2i & -3i \\ 3+2i & 1 & -5+2i \\ 3i & -5-2i & 2 \end{bmatrix}$$
 (2)

(3) Solve the following systems of linear equations.

$$3x - 4y + 7z = -23$$

$$5x - 10y + 11z = -47$$

$$5x - z = 7$$

$$x - 3y + 2z = -12$$
(3)

$$2u + v - 2w = 4
2u + 4v - 3w = 9
4 + 5v - 5w = -11$$
(4)

- (4) Represent the following complex numbers in polar form $r(\cos \theta + i \sin \theta)$.
 - 1. 3 + 4i
 - 2. -1.04 1.56i
- (5) Solve the following problems in electrical engineering.
 - 1. The impedance Z (in Ω) in an alternating-current circuit is given by $Z=3560/-32.4^{\circ}$. Express this in rectangular form.
 - 2. The current in a microprocessor circuit is represented by $3.75/15.0^{\circ}\mu A$. Write this in rectangular form.
 - 3. The voltage of a generator is represented by 2.84 1.06ikV. Write this voltage in polar form.

(6) Solve the following problems in complex arithmetic.

$$(8i - 5)(7 + 4i) (5)$$

$$(\sqrt{-18}\sqrt{-4})\cdot 3i\tag{6}$$

$$(1+i)(1-i)^2 (7)$$

$$\frac{0.25}{3 - \sqrt{-1}}\tag{8}$$

$$\frac{6+5i}{3-4i} \tag{9}$$

$$\frac{(2-i^3)^4}{(i^8-i^6)^3} + i \tag{10}$$