Echelon Form and Complex Numbers

(1) Find the equation of the quadratic

$$y = ax^2 + bx + c \tag{1}$$

which passes through (0,0),(1,2),(-1,3).

(2) Find the determinant for the following Hermitian matrix. What do you notice?

$$\begin{bmatrix} 4 & 3-2i & -3i \\ 3+2i & 1 & -5+2i \\ 3i & -5-2i & 2 \end{bmatrix}$$
 (2)

(3) Solve the following systems of linear equations.

$$3x - 4y + 7z = -23
5x - 10y + 11z = -47
5x - z = 7
x - 3y + 2z = -12$$
(3)

$$2u + v - 2w = 4
2u + 4v - 3w = 9
4 + 5v - 5w = -11$$
(4)

(4) Represent the following complex numbers in polar form $r(\cos \theta + i \sin \theta)$.

$$3 + 4i \tag{5}$$

$$-1.04 - 1.56i$$
 (6)

- (5) Solve the following problems in electrical engineering.
 - 1. The impedance Z (in Ω) in an alternating-current circuit is given by $Z=3560/-32.4^{\circ}$. Express this in rectangular form.
 - 2. The current in a microprocessor circuit is represented by $3.75/15.0^{\circ}\mu\text{A}$. Write this in rectangular form.
 - 3. The voltage of a generator is represented by 2.84-1.06ikV. Write this voltage in polar form.

(6) Use complex arithmetic to provide the following in rectangular form.

$$(8i - 5)(7 + 4i) \tag{7}$$

$$(\sqrt{-18}\sqrt{-4})\cdot 3i\tag{8}$$

$$(1+i)(1-i)^2 (9)$$

$$\frac{0.25}{3 - \sqrt{-1}}\tag{10}$$

$$\frac{6+5i}{3-4i} \tag{11}$$

$$\frac{(2-i^3)^4}{(i^8-i^6)^3} + i \tag{12}$$