

Term Test Ba version 1

(1) [5 points]

(2) [5 points]

(3) [5 points] Consider the following three vectors in \mathbb{R}^3 : $(-7, -2, 3)^\top$, $(-6, -10, -2)^\top$, $(10, -3, 7)^\top$. Determine the three lengths of these vectors and the three angles between them. If they replace the origin to the points P, Q, R , determine the plane equation for the plane containing the three points, using the cross product.

(4) [5 points] Solve the following system of linear equations.

$$\begin{array}{rcccccccl} 2a & - & 6b & - & 3c & = & 13 \\ -5a & - & 3b & + & c & = & 15 \\ 19a & - & 3b & - & 9c & = & -19 \end{array}$$

If the system is consistent and dependent, provide your answer in the form

$$S = \{u \in \mathbb{R}^3 \mid u \text{ corresponds to } \vec{u} = \vec{v}_0 + s_1\vec{v}_1 + \dots + s_n\vec{v}_n\}$$

where n is the dimension of the solution space and $s_i \in \mathbb{R}$ for $i = 1, \dots, n$. Note that $(-1, -3, 1)^\top$ solves the system.