Term Test Bb version 2

(1) [5 points] Linearize the following function around $x = \pi, y = 2$.

$$f\left(\left[\begin{array}{c} x\\y \end{array}\right]\right) = \left[\begin{array}{c} y\cos(xy)\\2x^2 + y^2 \end{array}\right] \tag{1}$$

(2) [5 points] There is a linear relationship between the latitude of the centre of a US state and that state's skin cancer mortality rate (deaths per ten million in one year). Ideally, you would use the data from all fifty states, but that's a large matrix and impractical for a term test. Find the best estimate for a linear regression line from the following data:

State	Alabama	California	Nebraska	Wisconsin
Mortality Rate	219	182	122	110
Centre Latitude	33.0	37.5	41.5	44.5

(3) [5 points] Find the distance between the point T=(7,-2,12) and the plane containing P=(8,-8,-1), Q=(1,-1,-1), R=(8,-22,11). (Hint: find the displacement vectors $\vec{PT}, \vec{PQ}, \vec{PR}$ and project \vec{PT} onto the plane spanned by \vec{PQ} and \vec{PR} ; then find the difference between \vec{PT} and its projection.)