

Term Test B version 1

(1) [5 points] How long will it take the world population to double at an exponential growth rate of 1.37% per year?

$$\frac{\ln 2}{\ln 1.0137} =$$

$$0.013607$$

$$50.9405$$

(2) [5 points] Suppose we are preparing a lovely *Canard à l'Orange* (roast duck with orange sauce). We first take our duck out of a 36°F refrigerator and place it in a 350°F oven to roast. After 10 minutes the internal temperature is 53°F. If we want to roast the duck until just under well-done (about 170°F internally), when will it be ready?

$$99.969 \text{ min}$$

(3) [5 points] Rewrite the expression as a single logarithm,

$$2(\log_5 x + 2\log_5 y - 3\log_5 z)$$

$$\log \frac{x^2 y^4}{z^6}$$

① (4) [5 points] Solve the following equation,

$$3^{x^2} = 175^{x-1}$$

$$0 = x^2 \ln 3 - x \ln 175 + \ln 175$$

(5) [5 points] Solve the following equation,

$$\ln 2x - \ln 4 + \ln(x-2) = 1$$

$$S = \{3.537\}$$

$$\text{not: } -1.537$$

(6) [5 points] Suppose that you plan to need \$10,000 in thirty-six months' time when your child starts attending university. You want to invest in an instrument yielding 3.5% interest per year, compounded monthly. How much should you invest? Use the formula

$$A = P \left(1 + \frac{r}{m}\right)^{mt}$$

$$\$9003.54$$

$$9004.62$$

(7) [5 points] Rewrite so that there is no logarithm of a product, quotient, root, or power,

$$\ln \frac{x^3 \sqrt{x-1}}{3x+4}$$

$$3 \ln x + \frac{1}{2} \ln(x-1) -$$

$$\ln(3x+4)$$

(8) [5 points] Evaluate without a calculator. Show all of your work.

$$\log_4 (2 \cdot \sqrt{32}) + \log_{27} \sqrt{3}$$

$$\log 4^{\frac{7}{4}} + \log 27^{\frac{1}{6}} = \frac{7}{4} + \frac{1}{6} = \frac{23}{12}$$