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16 14

Term Test B

6

- (1) [6 points] Solve the following three equations. Remember that the logarithm of a non-positive number is not defined.

$$3^{2x-1} = 27$$

$$(2x-1)\ln 3 = 3\ln 3$$

$$2x-1=3$$

$$x=2$$

$$S=923$$

$$\log_2 x + \log_2(x-2) = 3$$

$$\log_2(x^2-2x) = \log_2 8$$

$$x^2-2x-8=0$$

$$(x-4)(x+2)=0$$

$$\ln(x+1)^2 = 2$$

$$2\ln(x+1) = 2$$

$$x+1=e$$

$$x=e-1$$

$$S=9e-13$$

$$S=343$$

5

- (2) [5 points] How long will it take the world population to double at an exponential growth rate of 1.64% per year?

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- (3) [5 points] Suppose we are preparing a lovely *Canard à l'Orange* (roast duck with orange sauce). We first take our duck out of a 36°F refrigerator and place it in a 350°F oven to roast. After 10 minutes the internal temperature is 53°F. If we want to roast the duck until just under well-done (about 170°F internally), when will it be ready?

$$U_0 \leftrightarrow T? \quad (2)$$

3

- (4) [5 points] Evaluate

$$\log_4(2 \cdot \sqrt{32}) + \log_{27} \sqrt{3}$$

$$\log_4(4^{\frac{1}{2}} \cdot 2^{\frac{5}{2}}) + \log_{27}(27^{\frac{1}{3}})^{\frac{1}{2}} =$$

$$\log_4(4^{\frac{1}{2}} \cdot 4^{\frac{5}{4}}) + \log_{27} 27^{\frac{1}{6}} =$$

6

- (5) [6 points] Solve the following three equations.

$$7^{x-5} = 2$$

$$\ln(5-2x) = -2$$

$$6 - 5e^x = -e^{2x}$$

$$\frac{7}{4} + \frac{1}{6} = \frac{21}{12} + \frac{2}{12} = \frac{23}{12}$$

$$1.91667$$

5

- (6) [5 points] Suppose that you plan to need \$10,000 in thirty-six months' time when your child starts attending university. You want to invest in an instrument yielding 3.5% interest, compounded monthly. How much should you invest? Use the formula

$$A = P \left(1 + \frac{r}{m}\right)^{mt}$$

$$\boxed{\$ 9004.62}$$

(1)

$$t=3, \text{ not } 36$$

$$\rightarrow \$ 2841.74$$

$$\boxed{3.5}$$