

$$f(x) = \frac{x^{\frac{3}{4}} \sqrt{x^2+1}}{(3x+2)^5} \quad g(x) = \ln \frac{x^{\frac{3}{4}} \sqrt{x^2+1}}{(3x+2)^5}$$

$$g'(x) = \frac{(3x+2)^5}{x^{\frac{3}{4}} \sqrt{x^2+1}} \cdot \frac{d}{dx} f(x)$$

$$g(x) = \frac{3}{4} \ln x + \frac{1}{2} \ln(x^2+1) - 5 \ln(3x+2)$$

$$g'(x) = \frac{3}{4x} + \frac{1}{2(x^2+1)} \cdot 2x - 5 \cdot \frac{1}{3x+2} \cdot 3$$

$$= \frac{3}{4x} + \frac{2x}{2(x^2+1)} - \frac{15}{3x+2}$$

$$\Rightarrow f'(x) = \frac{x^{\frac{3}{4}} \sqrt{x^2+1}}{(3x+2)^5} \cdot \left[ \frac{3}{4x} + \frac{2x}{2(x^2+1)} - \frac{15}{3x+2} \right]$$