Integration

Technical Mathematics for Geomatics, MATH 2511

(1) Find the length of the following curve:

$$y = \frac{1}{3} (x^2 + 2)^{\frac{3}{2}}$$
 from $x = 0$ to $x = 3$

(2) Find the length of the following curve:

$$x = \frac{y^3}{3} + \frac{1}{4y}$$
 from $y = 1$ to $y = 3$

(3) Find the length of the following curve:

$$y = \frac{x^2}{2} - \frac{\ln x}{4}$$
 from $x = 1$ to $x = 3$

(4) Find the area of a surface of revolution for the following curve:

$$y = 2\sqrt{x}, 1 \le x \le 2$$

(5) Evaluate the following indefinite integral:

$$\int_{1}^{\infty} \frac{\ln x}{x^2} \, dx$$

(6) Evaluate the following indefinite integral:

$$\int_0^\infty e^{-\frac{x}{2}} \, dx$$

(7) Use integration by parts to find the following integral:

$$\int (\ln x)^2 \ dx$$

(8) Use integration by parts to find the following integral:

$$\int_0^{0.5\pi^2} \cos\sqrt{2x} \, dx$$

(9) Use integration by parts or trigonometric integration to find the following integral:

$$\int_{\frac{\pi}{2}}^{\pi} \sin^4 x \, dx$$

(10) Evaluate the following definite integral:

$$\int_{1}^{3} x\sqrt{3x^2 - 2} \, dx$$

(11) Evaluate the following definite integral:

$$\int_0^2 \frac{x}{\sqrt{x^2 + 5}} \, dx$$

(12) Evaluate the following definite integral:

$$\int_0^2 x e^{x^2} dx$$

(13) Evaluate the following definite integral:

$$\int_{1}^{2} \frac{\ln x}{x} \, dx$$

(14) Evaluate the following integral.

$$\int_0^{\frac{\pi}{6}} 3\cos^5 3x \, dx$$