Term Test A version 2

(1) [5 points] Evaluate the limit

$$\lim_{x \to 4} \left(\frac{1}{x - 4} - \frac{8}{x^2 - 16} \right)$$

(2) [8 points] Find the equation of the tangent line to the curve

$$y = \frac{1}{5\cos x + 2\sin x}$$

at the point $(0, \frac{1}{2})$.

(3) [7 points] Find the domain and the derivative of

$$f(x) = \frac{\ln x}{2 + \ln x}$$

Make sure to simplify the derivative as much as possible.

(4) [5 points] Find the derivative of

$$g(t) = -7e^{t\sin t}$$

(5) [7 points] The half-life of Palladium-100 is 4 days. After 20 days a sample of Palladium-100 has been reduced to a mass of 1 mg. What was the initial mass (in mg) of the sample?

(6) [8 points] Provide the second derivative of the following two functions in their simplest form.

$$f(x) = 5x - \frac{3}{x-2}$$

$$g(x) = \frac{x^2 \ln x}{2} - \frac{3x^2}{4}$$

(7) [9 points] An aluminum beam was brought from the outside cold into a machine shop where the temperature was held at $70^{\circ}F$. After 10 minutes, the beam warmed to $30^{\circ}F$ and after another 10 minutes it was $45^{\circ}F$. Use Newton's law of cooling to estimate the beam's initial temperature.