

Applying SPiCT to anchovy (*Engraulis encrasicolus*) in Division 9a South (Atlantic Iberian waters)

Presented at ICES WGHANSA, benchmark meeting 23-27 september 2024, Nantes, France.

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Introduction

Small and mid-size pelagic fish occupy intermediate levels in the marine trophic webs where they play an essential role (Cury *et al.*, 2000). These fish act as links between the upper and lower trophic levels, capturing energy from lower levels and making it available to higher trophic levels (Morello & Arneri, 2009). Global captures of finfish, the taxon where small and mid-size pelagic fish are included, account for the 85% of the marine captures, with small pelagics as the main group (FAO, 2024a).

According to the economic importance of *Engraulis encrasicolus*, the species under study, it accounted for approximately 4% of the total European countries fisheries in 2022 (FAO, 2024b). Concerning Spain and Portugal, *Engraulis encrasicolus* covers more than 5% and 2% of the total fisheries, respectively (FAO, 2024b). Therefore, the knowledge and correct management of the *Engraulis encrasicolus* fishery is of utmost importance for the fishing sector of both countries.

In this study we apply the Stochastic Surplus Production Model in Continuous Time (SPiCT) with 4 different model configurations to evaluate the *Engraulis encrasicolus* stock status in ICES Division 9a South. Model results allow us to establish reference points for Maximum Sustainable Yield, Biomass at Maximum Sustainable Yield and Fishing Mortality at Maximum Sustainable Yield as well as to determine how model configuration could affect the estimates and model robustness.

Material & Methods

Data

We used data from commercial landings as catch observations and independent scientific survey data as exploitable biomass indices. In this sense, we used quarterly commercial landings data comprised from 1989 to 2023 and yearly data from PELAGO (1999-2023), ECOCADIZ (2004-2023), ECOCADIZ-RECLUTAS (2012-2023) and BOCADEVA (2005-2023) surveys. We obtained the corresponding exploitable biomass index for each period and survey considering the minimum length observed in the landings during that period. In addition, we added as much uncertainty as possible, without compromising the stability of the model, to the 2012 estimate of the ECOCADIZ-RECLUTAS survey since it was only sampled in Spanish waters.

SPiCT

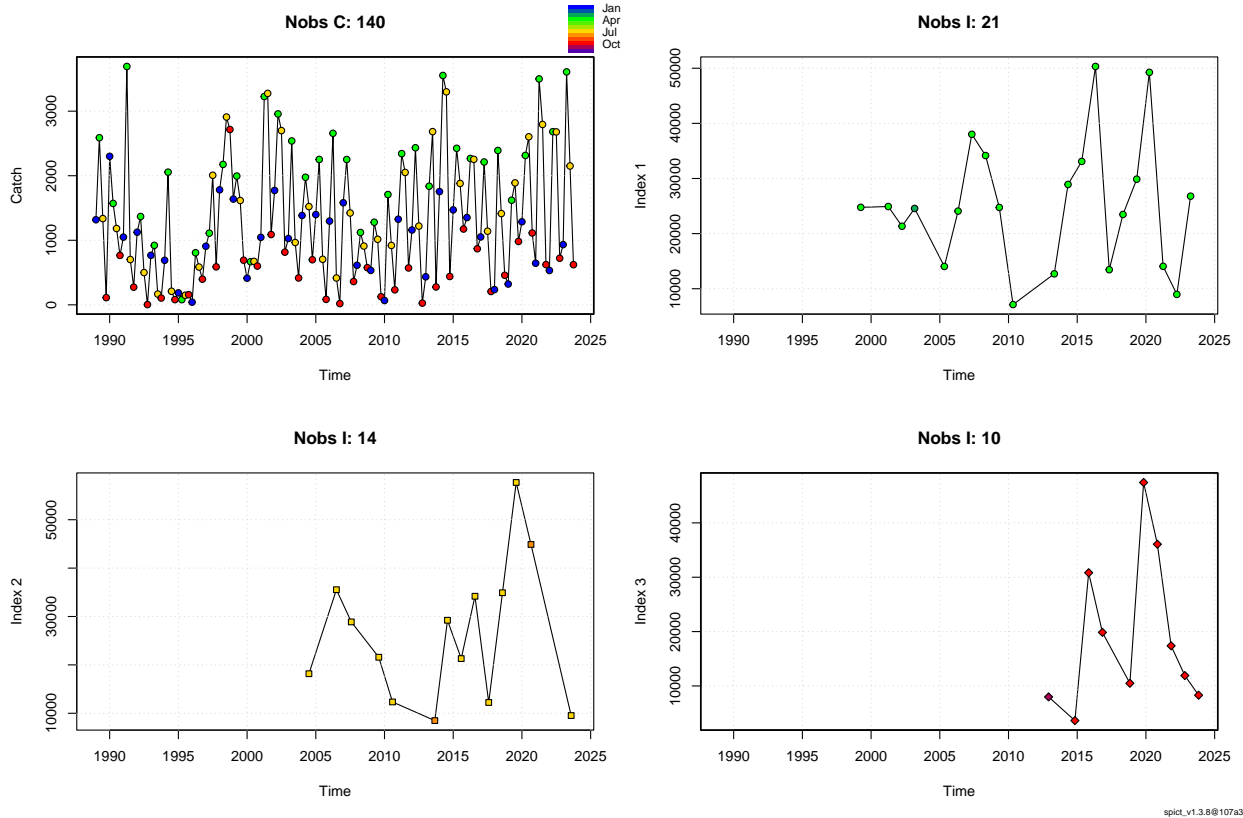
Stochastic Surplus Production Model in Continuous Time (Pedersen & Berg, 2017) is a model that has been widely used in data-limited situations (i.e. Bluemel *et al.*, 2021; González Herraiz *et al.*, 2023; Soto *et al.*, 2023). This stochastic state-space model aggregates biomass across size and age groups, using the equations reported by Pella and Tomlinson (1969), providing stock status estimates and reproducing population dynamics (Derhy *et al.*, 2022). By relaxing the common assumption that catches are known without error, SPiCT permits to assess fish stock status with a more realistic quantification of uncertainty (Pedersen & Berg, 2017), allowing for a broader perspective of the stock situation and a better understanding of the risks associated with management decisions.

Scenarios

We tested the SPiCT model with 4 different configurations of the input data:

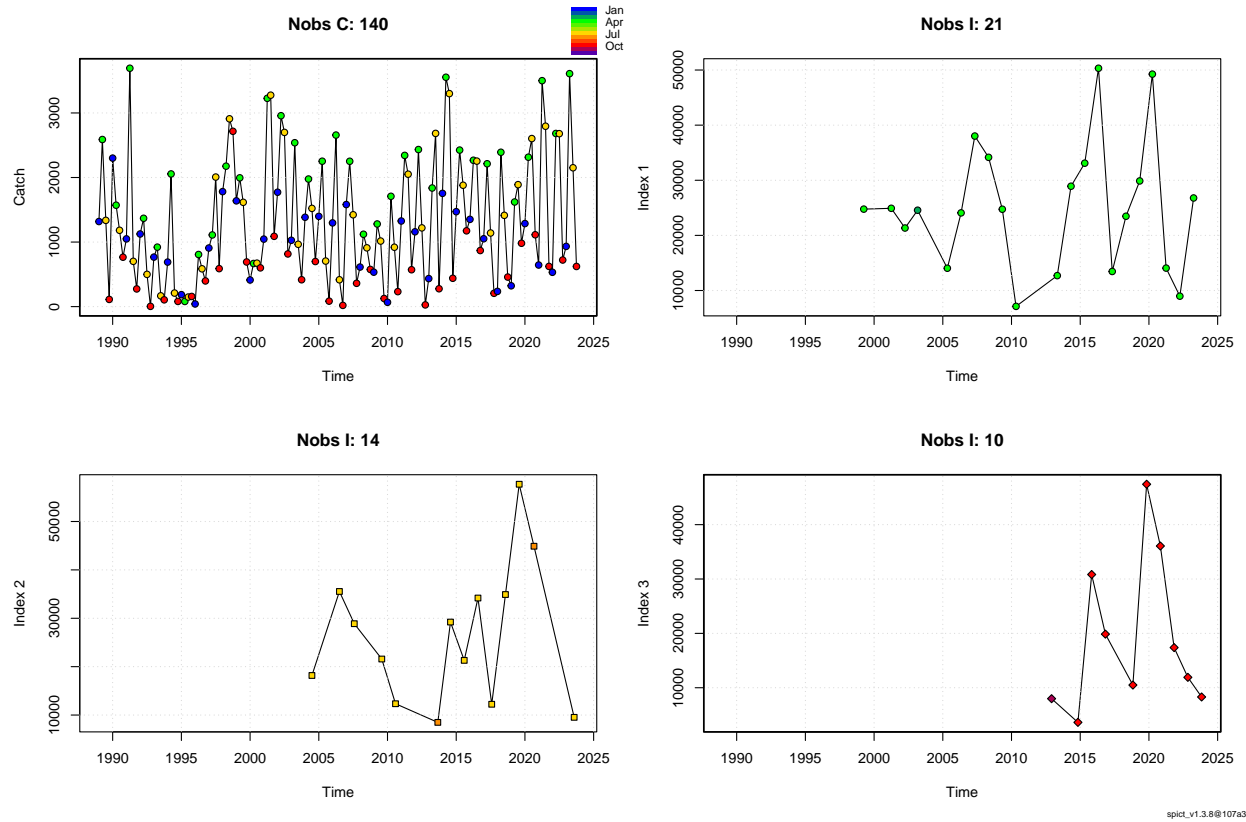
- Scenario 1: commercial landings data and exploitable biomass indices from PELAGO, ECOCADIZ and ECOCADIZ-RECLUTAS.

```
plotspict.data(sc_1_data, qlegend = TRUE)
```



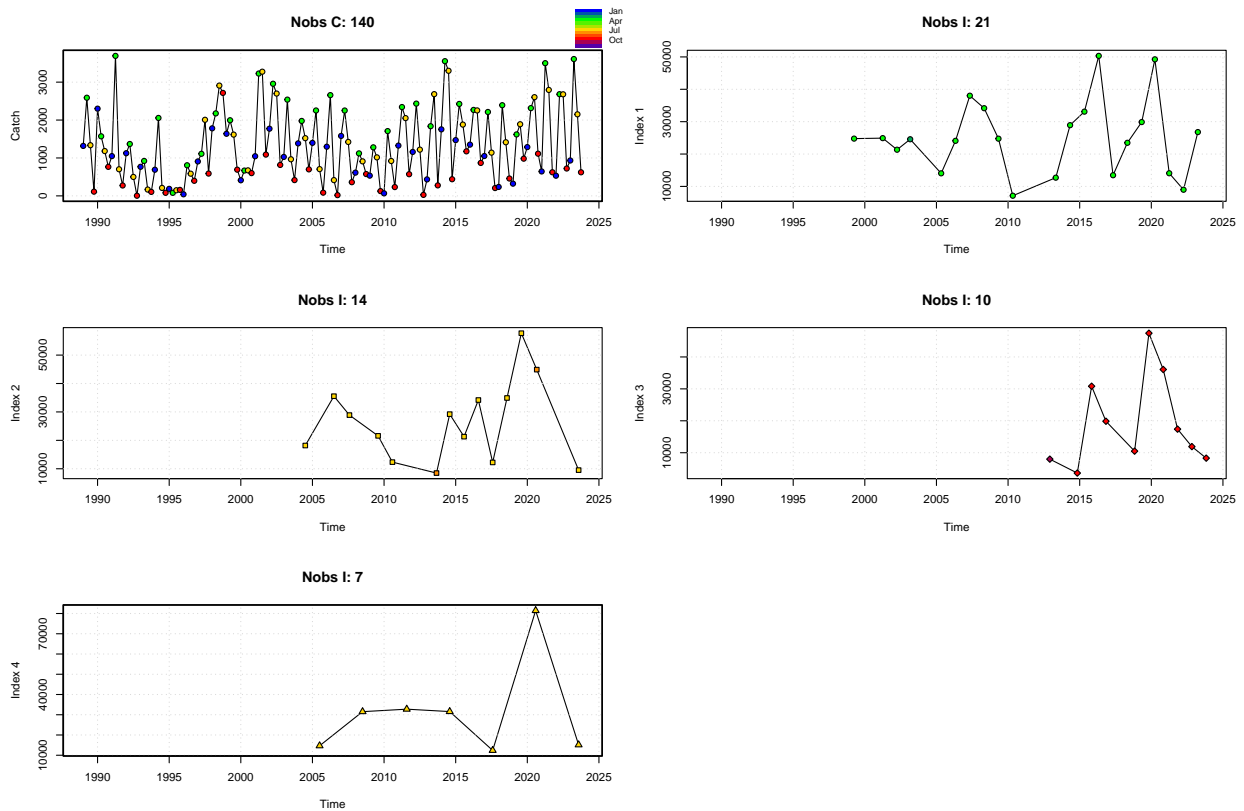
- Scenario 2: identical to Scenario 1 but adding uncertainty to the 2012 ECOCADIZ-RECLUTAS exploitable biomass estimate.

```
plotspict.data(sc_2_data, qlegend = TRUE)
```



- Scenario 3: commercial landings data and exploitable biomass indices from PELAGO, ECOCADIZ, ECOCADIZ-RECLUTAS and BOCADEVA.

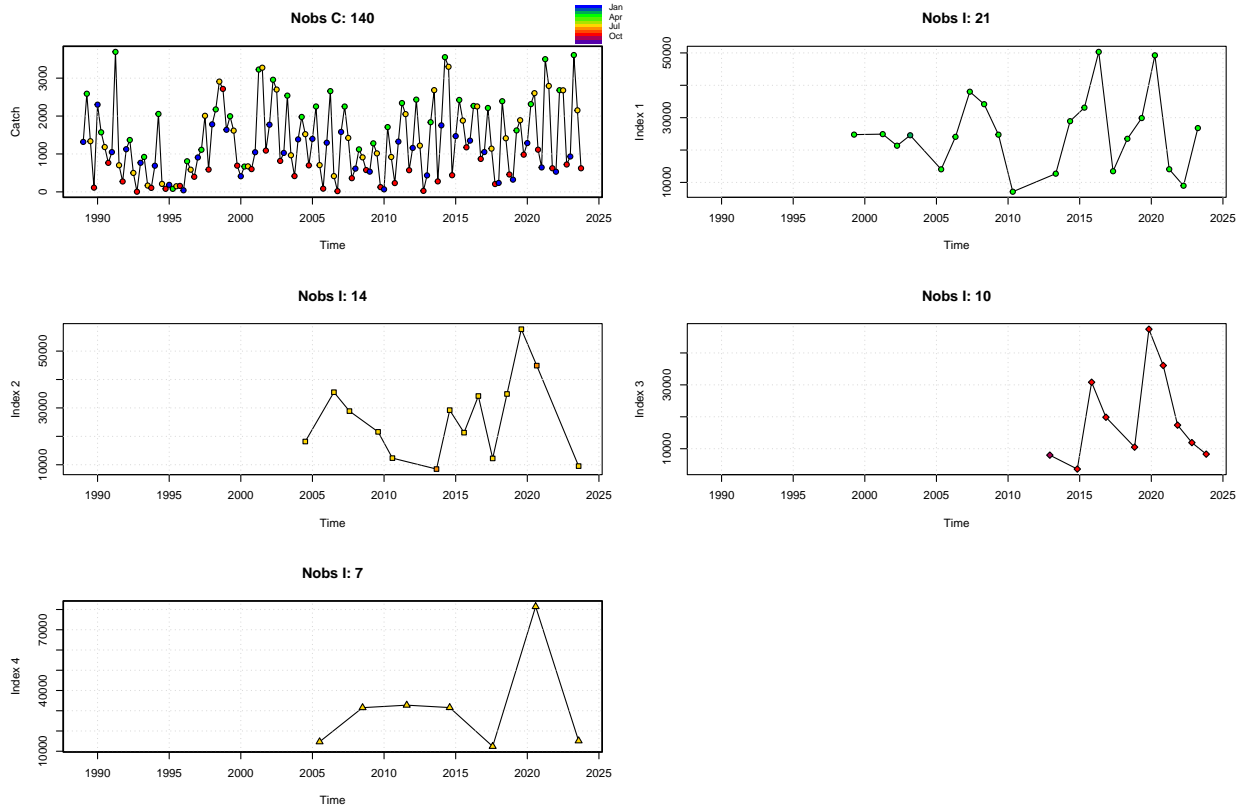
```
plotspict.data(sc_3_data, qlegend = TRUE)
```



spict_v1.3.8@107a32

- Scenario 4: identical to Scenario 3 but adding the uncertainty to the 2012 ECOCADIZ-RECLUTAS exploitable biomass estimate and to the BOCADEVA estimates.

```
plotspict.data(sc_4_data, qlegend = TRUE)
```



spict_v1.3.8@107a32

Implementation

We implemented the model and scenarios using the *SPiCT* package (Pedersen & Berg, 2017) from R (R Core Team, 2024) and the default priors.

Results

We obtained two types of results: a) model parameter estimates, reference points & state estimations and b) model diagnostics for model acceptance.

Scenario 1

Model Fit

The model obtained acceptable uncertainty levels and an estimated exploitable biomass of 2219.43 tonnes and a fishing mortality of 3.25 in 2023. Predicted catchabilities were 6.29, 8.75 and 5.31 for PELAGO, ECOCADIZ and ECOCADIZ-RECLUTAS, respectively. Additionally, Kobe plot shows that the stock has suboptimal biomass estimates as well as lower fishing mortality than fishing mortality at Maximum Sustainable Yield (MSY).

```
res_sc_1 <- fit.spict(sc_1_data)
summary(res_sc_1)
```

Convergence: 0 MSG: relative convergence (4)
 Objective function at optimum: 217.9455143
 Euler time step (years): 1/16 or 0.0625
 Nobs C: 140, Nobs I1: 21, Nobs I2: 14, Nobs I3: 10

Priors

```
logn ~ dnorm[log(2), 2^2]
logalpha ~ dnorm[log(1), 2^2]
logbeta ~ dnorm[log(1), 2^2]
```

Model parameter estimates w 95% CI

| | estimate | cilow | ciupp | log.est |
|--------|--------------|--------------|--------------|------------|
| alpha1 | 0.1472304 | 0.0251668 | 8.613235e-01 | -1.9157567 |
| alpha2 | 0.1707301 | 0.0319501 | 9.123218e-01 | -1.7676714 |
| alpha3 | 0.3986602 | 0.1161241 | 1.368622e+00 | -0.9196458 |
| beta | 1.6935246 | 0.8889400 | 3.226343e+00 | 0.5268119 |
| r | 4.2377969 | 1.1869716 | 1.513004e+01 | 1.4440435 |
| rc | 5.9281435 | 2.5109657 | 1.399577e+01 | 1.7797111 |
| rold | 9.8617303 | 3.7699535 | 2.579706e+01 | 2.2886616 |
| m | 7830.0805345 | 5311.6801952 | 1.154252e+04 | 8.9657281 |
| K | 6069.6185357 | 2297.6358114 | 1.603399e+04 | 8.7110510 |
| q1 | 6.2913041 | 2.3604551 | 1.676817e+01 | 1.8391684 |
| q2 | 8.7530111 | 2.3391956 | 3.275280e+01 | 2.1693978 |
| q3 | 5.3056998 | 1.5223404 | 1.849156e+01 | 1.6687817 |
| n | 1.4297214 | 0.8350964 | 2.447745e+00 | 0.3574796 |
| sdb | 1.1780900 | 0.6023364 | 2.304188e+00 | 0.1638945 |
| sdf | 0.3449096 | 0.1755653 | 6.775977e-01 | -1.0644729 |
| sdi1 | 0.1734506 | 0.0387140 | 7.771132e-01 | -1.7518622 |
| sdi2 | 0.2011354 | 0.0431693 | 9.371339e-01 | -1.6037769 |
| sdi3 | 0.4696576 | 0.2032237 | 1.085397e+00 | -0.7557513 |
| sdc | 0.5841129 | 0.4477046 | 7.620825e-01 | -0.5376610 |
| phi1 | 3.8831595 | 1.8088397 | 8.336243e+00 | 1.3566491 |
| phi2 | 11.3419666 | 6.3157292 | 2.036823e+01 | 2.4285097 |
| phi3 | 11.4554653 | 5.8256527 | 2.252583e+01 | 2.4384669 |

Deterministic reference points (Drp)

| | estimate | cilow | ciupp | log.est |
|-------|-------------|-------------|--------------|----------|
| Bmsyd | 2641.663622 | 1134.936110 | 6148.704437 | 7.879164 |
| Fmsyd | 2.964072 | 1.255483 | 6.997883 | 1.086564 |
| MSYd | 7830.080534 | 5311.680195 | 11542.517419 | 8.965728 |

Stochastic reference points (Srp)

| | estimate | cilow | ciupp | log.est | rel.diff.Drp |
|-------|--------------|-------------|--------------|----------|--------------|
| Bmsys | 2435.613471 | 1380.317367 | 4297.716688 | 7.797954 | -0.08459887 |
| Fmsys | 4.224397 | 2.676875 | 6.666552 | 1.440876 | 0.29834440 |
| MSYs | 10548.688285 | 5533.814449 | 20108.159670 | 9.263757 | 0.25771998 |

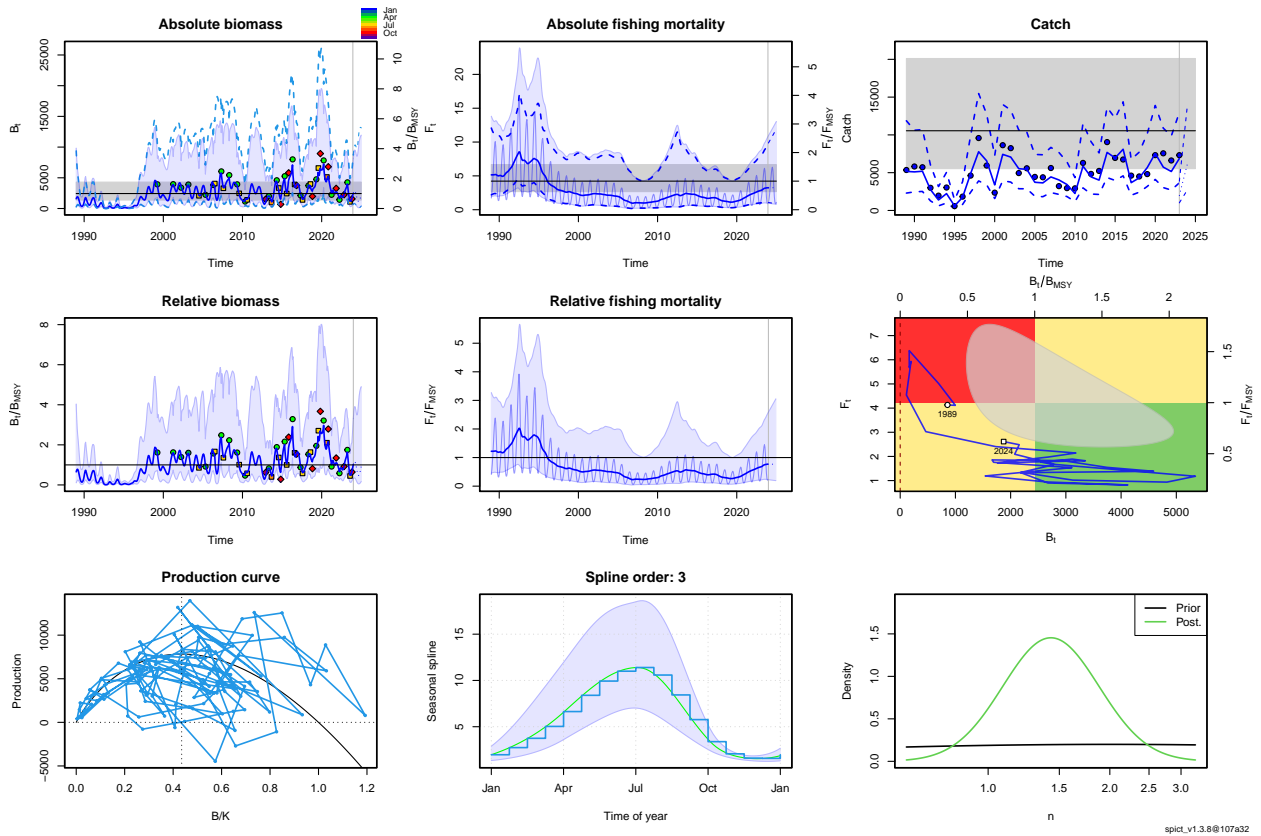
States w 95% CI (inp\$msytype: s)

| | estimate | cilow | ciupp | log.est |
|----------------|--------------|-------------|-------------|------------|
| B_2023.94 | 2219.4307185 | 623.5240116 | 7900.052961 | 7.7050060 |
| F_2023.94 | 3.2466487 | 1.0825588 | 9.736864 | 1.1776233 |
| B_2023.94/Bmsy | 0.9112409 | 0.2854531 | 2.908919 | -0.0929479 |
| F_2023.94/Fmsy | 0.7685473 | 0.2309132 | 2.557953 | -0.2632532 |

Predictions w 95% CI (inp\$msytype: s)

| | prediction | cilow | ciupp | log.est |
|----------------|--------------|--------------|--------------|------------|
| B_2025.00 | 2280.2387517 | 396.1363036 | 13125.504321 | 7.7320354 |
| F_2025.00 | 3.2466502 | 0.8842016 | 11.921192 | 1.1776238 |
| B_2025.00/Bmsy | 0.9362072 | 0.1787497 | 4.903415 | -0.0659185 |
| F_2025.00/Fmsy | 0.7685476 | 0.1914702 | 3.084895 | -0.2632528 |
| Catch_2024.00 | 6151.1230310 | 2718.4802992 | 13918.186037 | 8.7243900 |
| E(B_inf) | 3001.0968823 | NA | NA | 8.0067331 |

```
plot(res_sc_1)
```



Model Diagnostics

According to the diagnostic checklist for model acceptance, the model meets all requirements except normality of catch residuals.

- 1- The assessment converged:

```
# if 0 => OK
res_sc_1$opt$convergence
```

```
[1] 0
```

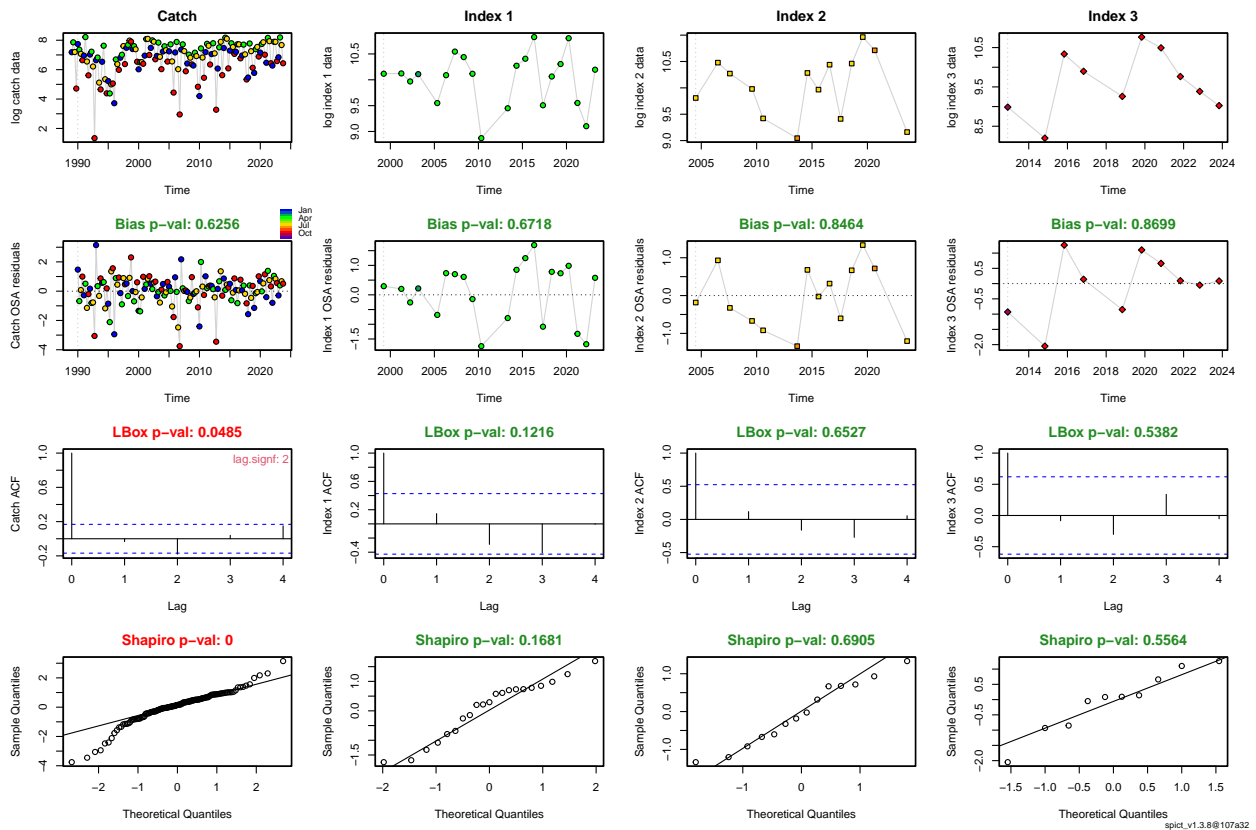
- 2- All variance parameters of the model parameters are finite:

```
# if TRUE => OK
all(is.finite(res_sc_1$sd))
```

```
[1] TRUE
```

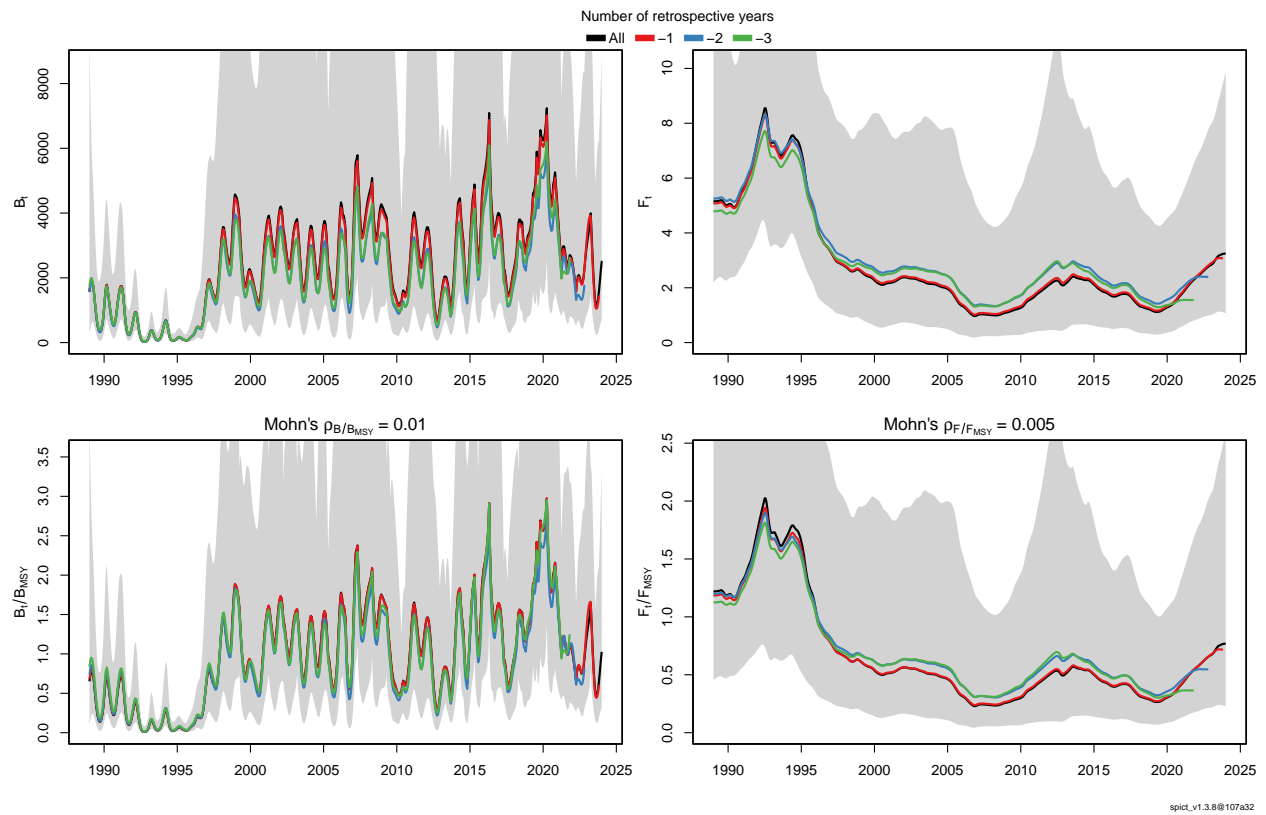
- 3- No violation of model assumptions:

```
res_sc_1 <- calc.osa.resid(res_sc_1)
plotspict.diagnostic(res_sc_1)
```



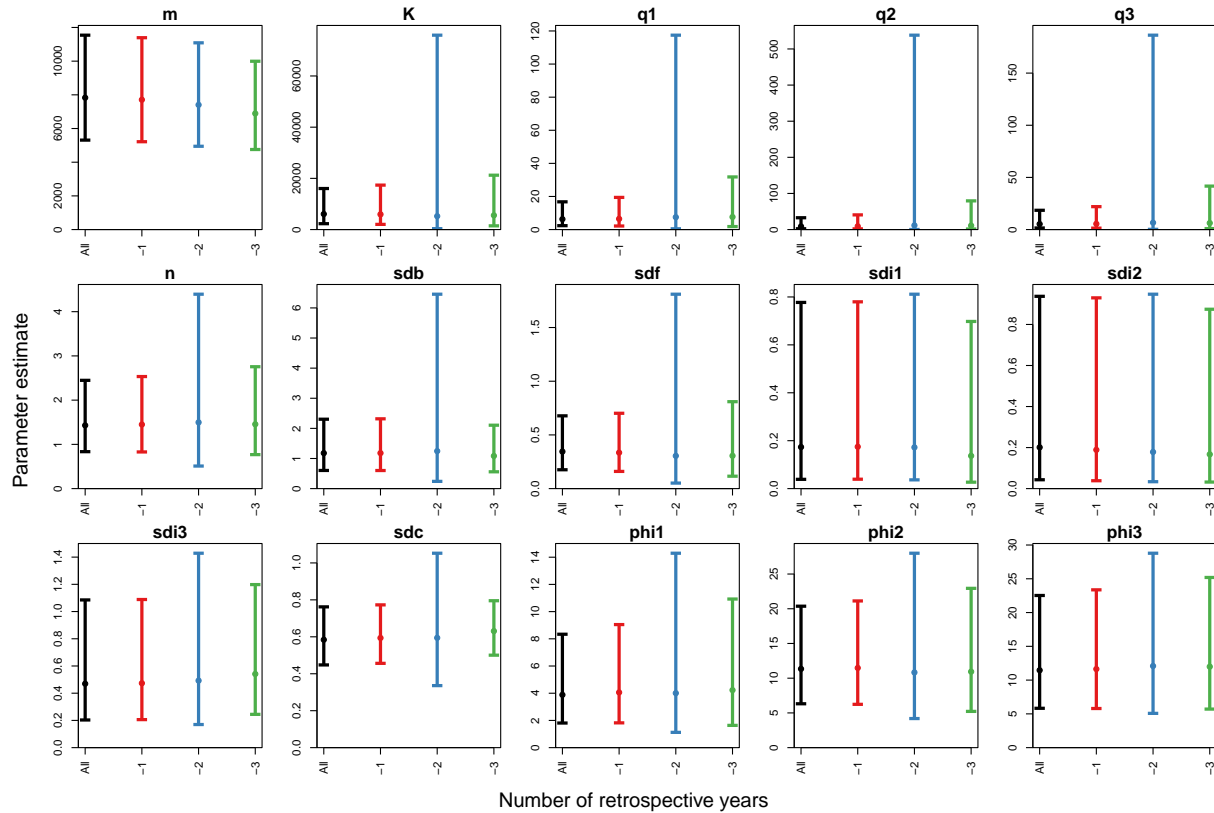
- 4- Consistent patterns in the retrospective analysis:

```
# if -0.2 < mohns_rho < 0.2 => OK
retro_sc_1 <- retro(res_sc_1, nretroyear = 3)
plotspict.retro(retro_sc_1)
```

FFmsy BBmsy
0.004889144 0.010451340

```
plotspict.retro.fixed(retro_sc_1)
```

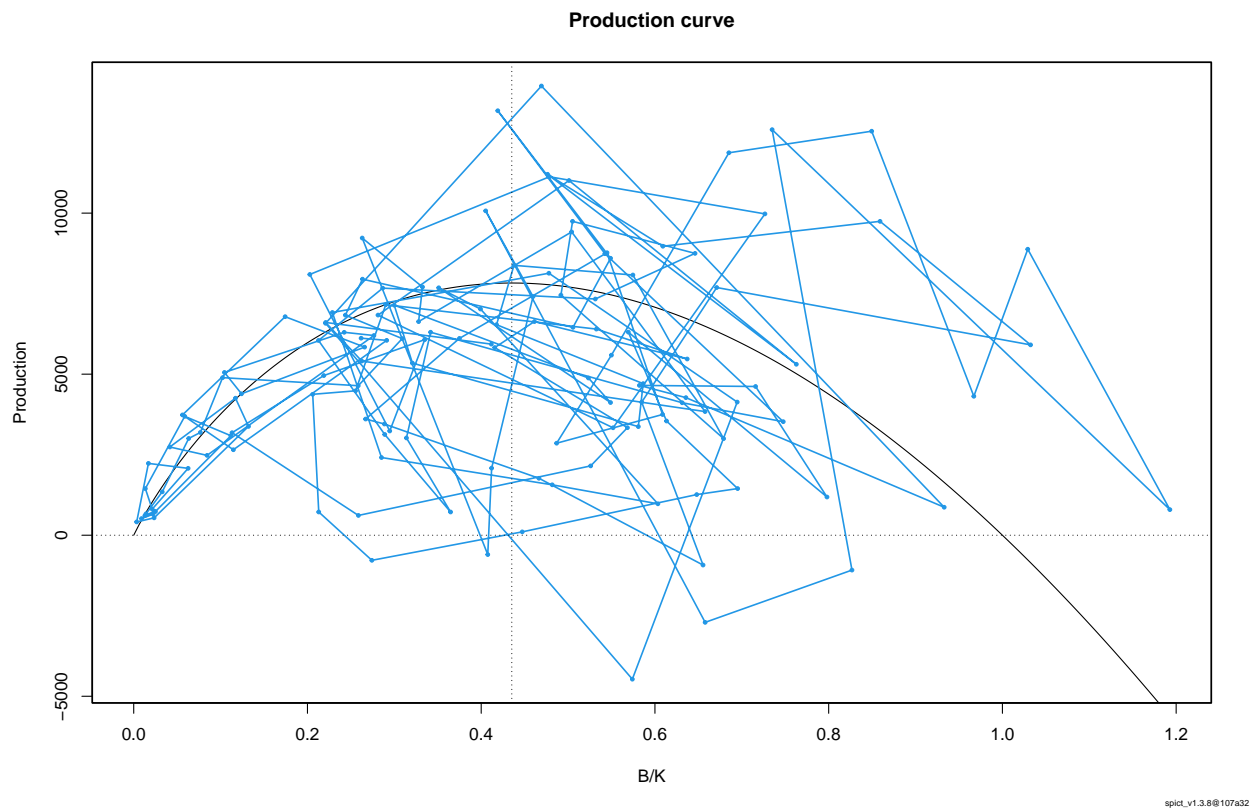


- 5- Realistic production curve:

```
# if between 0.1 and 0.9 => OK
calc.bmsyk(res_sc_1)
```

```
[1] 0.4352273
```

```
plotspict.production(res_sc_1)
```



- 6- High assessment uncertainty:

Main variance parameteres (logsdB, logsdC, logsdI, logsdF) should not be unreallistically high:
`get.par("logsdB", res_sc_1)`

| | ll | est | ul | sd | cv |
|--------|------------|-----------|-----------|-----------|----------|
| logsdB | -0.5069392 | 0.1638945 | 0.8347282 | 0.3422684 | 2.088346 |

`get.par("logsdC", res_sc_1)`

| | ll | est | ul | sd | cv |
|--------|------------|-----------|------------|-----------|------------|
| logsdC | -0.8036216 | -0.537661 | -0.2717005 | 0.1356966 | -0.2523832 |

`get.par("logsdI", res_sc_1)`

| | ll | est | ul | sd | cv |
|--------|-----------|------------|-------------|-----------|------------|
| logsdI | -3.251555 | -1.7518622 | -0.25216928 | 0.7651635 | -0.4367715 |
| logsdI | -3.142625 | -1.6037769 | -0.06492909 | 0.7851409 | -0.4895574 |
| logsdI | -1.593448 | -0.7557513 | 0.08194539 | 0.4274041 | -0.5655354 |

`get.par("logsdF", res_sc_1)`

| | ll | est | ul | sd | cv |
|--------|-----------|-----------|------------|-----------|------------|
| logsdF | -1.739744 | -1.064473 | -0.3892015 | 0.3445326 | -0.3236649 |

```
calc.om(res_sc_1) # if order of magnitude < 2 => OK)
```

| | lower | est | upper | CI range | order | magnitude |
|--------|-------|------|-------|----------|-------|-----------|
| B/Bmsy | 0.29 | 0.91 | 2.91 | 2.62 | | 1 |
| F/Fmsy | 0.06 | 0.21 | 0.73 | 0.67 | | 1 |

- 7- Initial values do not influence the parameter estimates:

```
check_sc_1$check.ini$resmat # Trials that converged should have same or similar estimates.
```

| | Distance | m | K | q | q | q | n | sdb | sdf | sdi | sdi | sdi |
|----------|----------|---------|---------|------|------|------|------|------|------|------|-----|------|
| Basevec | 0.00 | 7830.08 | 6069.62 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 1 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 2 | 0.05 | 7830.08 | 6069.67 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 3 | 0.02 | 7830.08 | 6069.64 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 4 | 0.13 | 7830.07 | 6069.75 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 5 | 0.02 | 7830.08 | 6069.64 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 6 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 7 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 8 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 9 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 10 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 11 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 12 | 0.11 | 7830.09 | 6069.51 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 13 | 0.08 | 7830.11 | 6069.69 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 14 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 15 | 0.03 | 7830.08 | 6069.65 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 16 | 0.01 | 7830.08 | 6069.63 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 17 | 0.05 | 7830.06 | 6069.66 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 18 | 0.02 | 7830.10 | 6069.61 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 19 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 20 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 21 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 22 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 23 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 24 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 25 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 26 | 0.03 | 7830.08 | 6069.64 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 27 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 28 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 29 | 0.01 | 7830.08 | 6069.63 | 6.29 | 8.75 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 30 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |

| | sdc | phi | phi | phi |
|---------|------|------|-------|-------|
| Basevec | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 1 | NA | NA | NA | NA |
| Trial 2 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 3 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 4 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 5 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 6 | NA | NA | NA | NA |
| Trial 7 | NA | NA | NA | NA |
| Trial 8 | NA | NA | NA | NA |

| | | | | |
|----------|------|------|-------|-------|
| Trial 9 | NA | NA | NA | NA |
| Trial 10 | NA | NA | NA | NA |
| Trial 11 | NA | NA | NA | NA |
| Trial 12 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 13 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 14 | NA | NA | NA | NA |
| Trial 15 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 16 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 17 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 18 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 19 | NA | NA | NA | NA |
| Trial 20 | NA | NA | NA | NA |
| Trial 21 | NA | NA | NA | NA |
| Trial 22 | NA | NA | NA | NA |
| Trial 23 | NA | NA | NA | NA |
| Trial 24 | NA | NA | NA | NA |
| Trial 25 | NA | NA | NA | NA |
| Trial 26 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 27 | NA | NA | NA | NA |
| Trial 28 | NA | NA | NA | NA |
| Trial 29 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 30 | NA | NA | NA | NA |

Scenario 2

Model Fit

In this second configuration of the model, the uncertainty levels were also acceptable and the estimated exploitable biomass was 2217.19 tonnes and the fishing mortality was 3.25 for 2023. Predicted catchabilities were estimated at 6.30, 8.77 and 5.31 for PELAGO, ECOCADIZ and ECOCADIZ-RECLUTAS, respectively. Additionally, Kobe plot also shows that the stock has suboptimal biomass estimates as well as lower fishing mortality than fishing mortality at MSY.

```
res_sc_2 <- fit.spict(sc_2_data)
summary(res_sc_2)
```

```
Convergence: 0 MSG: relative convergence (4)
Objective function at optimum: 217.9459292
Euler time step (years): 1/16 or 0.0625
Nobs C: 140, Nobs I1: 21, Nobs I2: 14, Nobs I3: 10
```

Priors

```
logn ~ dnorm[log(2), 2^2]
logalpha ~ dnorm[log(1), 2^2]
logbeta ~ dnorm[log(1), 2^2]
```

Model parameter estimates w 95% CI

| | estimate | ci_low | ciupp | log.est |
|--------|-----------|-----------|--------------|------------|
| alpha1 | 0.1469549 | 0.0250799 | 8.610786e-01 | -1.9176298 |
| alpha2 | 0.1704595 | 0.0318803 | 9.114243e-01 | -1.7692575 |
| alpha3 | 0.3977649 | 0.1155602 | 1.369130e+00 | -0.9218942 |
| beta | 1.6934230 | 0.8885506 | 3.227370e+00 | 0.5267520 |
| r | 4.2466456 | 1.1853627 | 1.521391e+01 | 1.4461294 |

| | | | | |
|------|--------------|--------------|--------------|------------|
| rc | 5.9369191 | 2.5087730 | 1.404950e+01 | 1.7811903 |
| rold | 9.8624104 | 3.7767789 | 2.575399e+01 | 2.2887306 |
| m | 7831.8636127 | 5312.1014581 | 1.154686e+04 | 8.9659558 |
| K | 6060.4068303 | 2290.4188151 | 1.603573e+04 | 8.7095322 |
| q1 | 6.3010912 | 2.3609741 | 1.681668e+01 | 1.8407228 |
| q2 | 8.7714196 | 2.3392162 | 3.289042e+01 | 2.1714987 |
| q3 | 5.3134927 | 1.5229434 | 1.853858e+01 | 1.6702494 |
| n | 1.4305890 | 0.8348883 | 2.451328e+00 | 0.3580863 |
| sdb | 1.1795620 | 0.6017959 | 2.312024e+00 | 0.1651432 |
| sdf | 0.3447639 | 0.1752830 | 6.781157e-01 | -1.0648955 |
| sdi1 | 0.1733424 | 0.0386606 | 7.772137e-01 | -1.7524866 |
| sdi2 | 0.2010675 | 0.0431220 | 9.375297e-01 | -1.6041144 |
| sdi3 | 0.4691883 | 0.2028282 | 1.085341e+00 | -0.7567511 |
| sdc | 0.5838311 | 0.4469616 | 7.626130e-01 | -0.5381435 |
| phi1 | 3.8811312 | 1.8075853 | 8.333316e+00 | 1.3561267 |
| phi2 | 11.3374494 | 6.3114390 | 2.036584e+01 | 2.4281114 |
| phi3 | 11.4590398 | 5.8278906 | 2.253124e+01 | 2.4387789 |

Deterministic reference points (Drp)

| | estimate | cilow | ciupp | log.est |
|-------|-------------|-------------|-------------|----------|
| Bmsyd | 2638.359567 | 1132.275821 | 6147.74340 | 7.877913 |
| Fmsyd | 2.968459 | 1.254387 | 7.02475 | 1.088043 |
| MSYd | 7831.863613 | 5312.101458 | 11546.85921 | 8.965956 |

Stochastic reference points (Srp)

| | estimate | cilow | ciupp | log.est | rel.diff.Drp |
|-------|--------------|-------------|--------------|----------|--------------|
| Bmsys | 2434.171731 | 1376.685553 | 4303.954524 | 7.797362 | -0.08388391 |
| Fmsys | 4.225844 | 2.677389 | 6.669839 | 1.441219 | 0.29754632 |
| MSYs | 10543.172099 | 5544.367419 | 20048.901799 | 9.263234 | 0.25716250 |

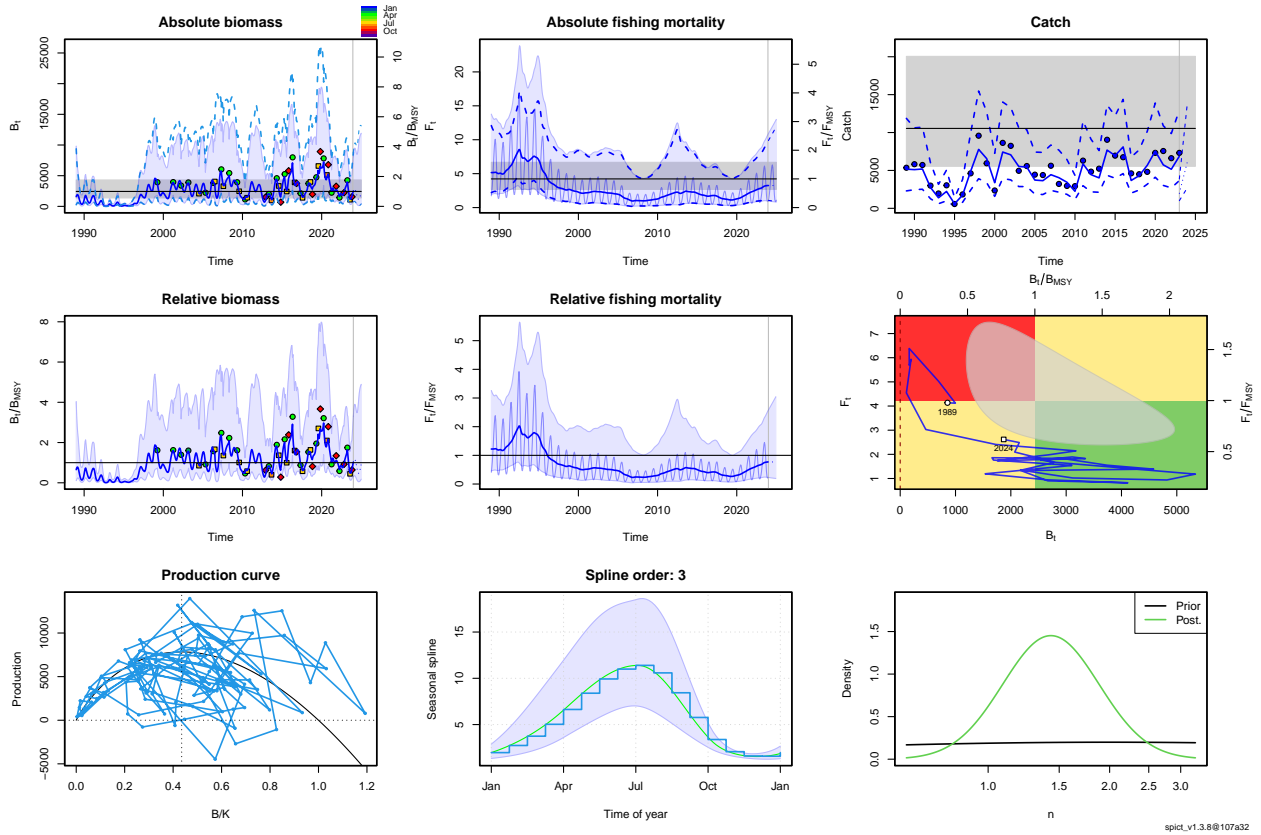
States w 95% CI (inp\$msytype: s)

| | estimate | cilow | ciupp | log.est |
|----------------|--------------|-------------|-------------|------------|
| B_2023.94 | 2217.1929789 | 622.8802453 | 7892.279043 | 7.7039973 |
| F_2023.94 | 3.2509177 | 1.0836816 | 9.752372 | 1.1789373 |
| B_2023.94/Bmsy | 0.9108614 | 0.2860864 | 2.900063 | -0.0933646 |
| F_2023.94/Fmsy | 0.7692943 | 0.2321613 | 2.549149 | -0.2622816 |

Predictions w 95% CI (inp\$msytype: s)

| | prediction | cilow | ciupp | log.est |
|----------------|--------------|--------------|--------------|------------|
| B_2025.00 | 2277.6312923 | 395.5390189 | 13115.278281 | 7.7308913 |
| F_2025.00 | 3.2509192 | 0.8852964 | 11.937782 | 1.1789378 |
| B_2025.00/Bmsy | 0.9356905 | 0.1789278 | 4.893129 | -0.0664706 |
| F_2025.00/Fmsy | 0.7692947 | 0.1924187 | 3.075660 | -0.2622812 |
| Catch_2024.00 | 6150.3446013 | 2717.8426494 | 13917.928149 | 8.7242634 |
| E(B_inf) | 2993.6033459 | NA | NA | 8.0042331 |

```
plot(res_sc_2)
```



Model Diagnostics

According to the diagnostic checklist, the model meets all requirements except normality of catch residuals, as in Scenario 1.

- 1- The assessment converged:

```
# if 0 => OK
res_sc_2$opt$convergence
```

```
[1] 0
```

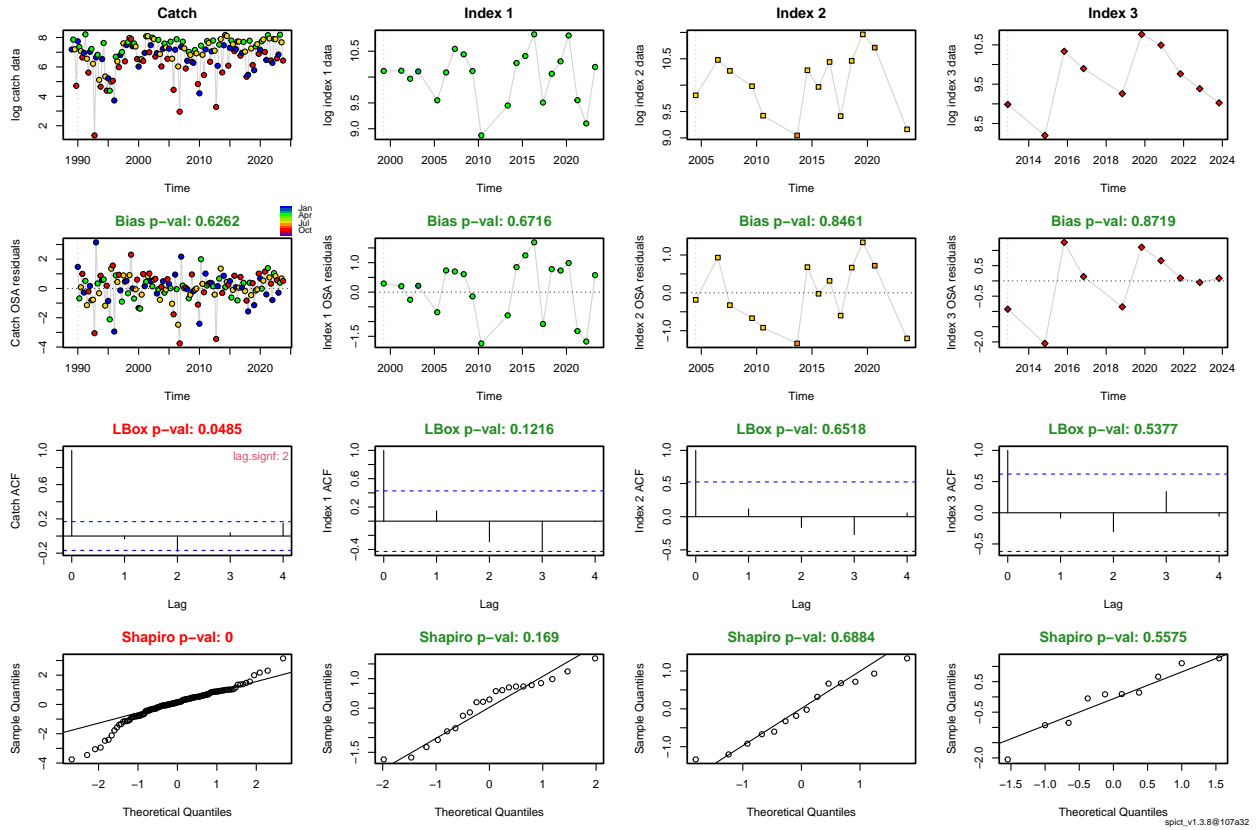
- 2- All variance parameters of the model parameters are finite:

```
# if TRUE => OK
all(is.finite(res_sc_2$sd))
```

```
[1] TRUE
```

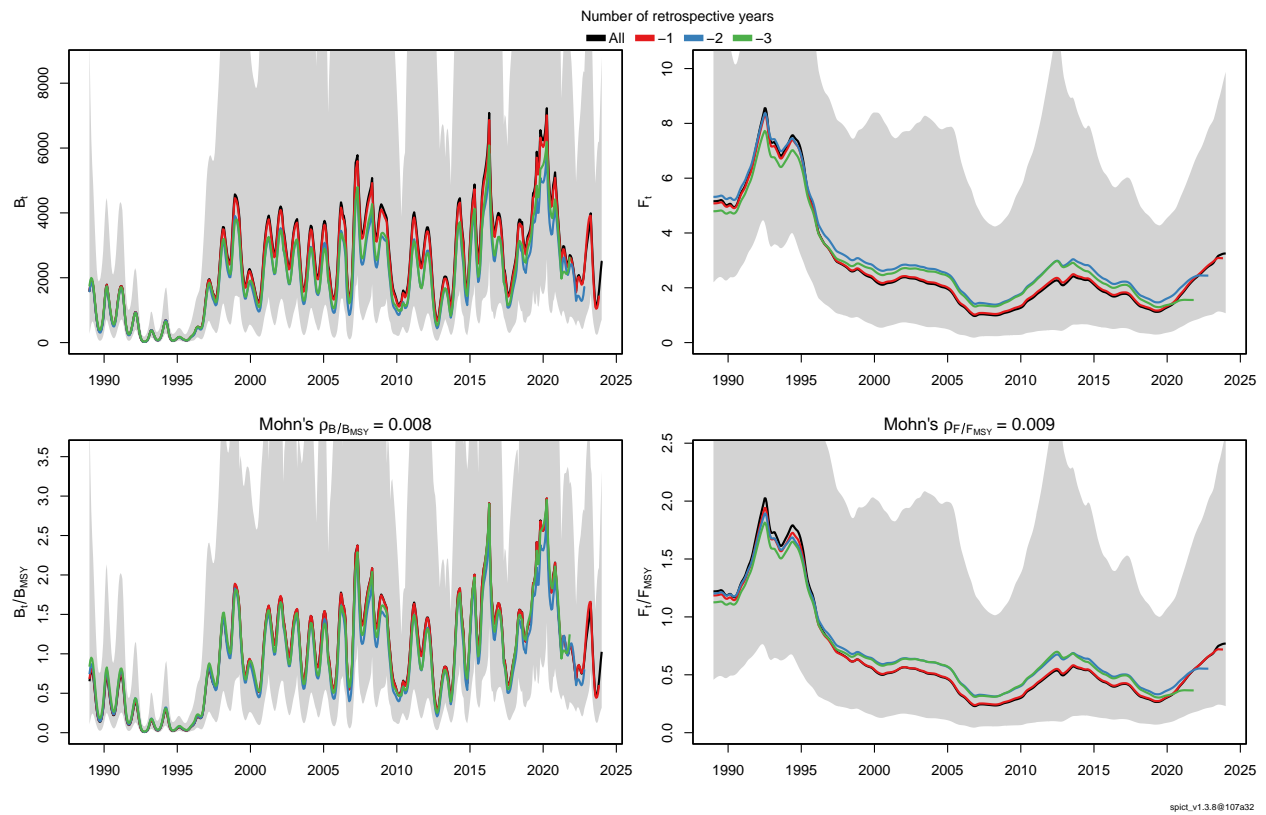
- 3- No violation of model assumptions:

```
res_sc_2 <- calc.osa.resid(res_sc_2)
plotspict.diagnostic(res_sc_2)
```



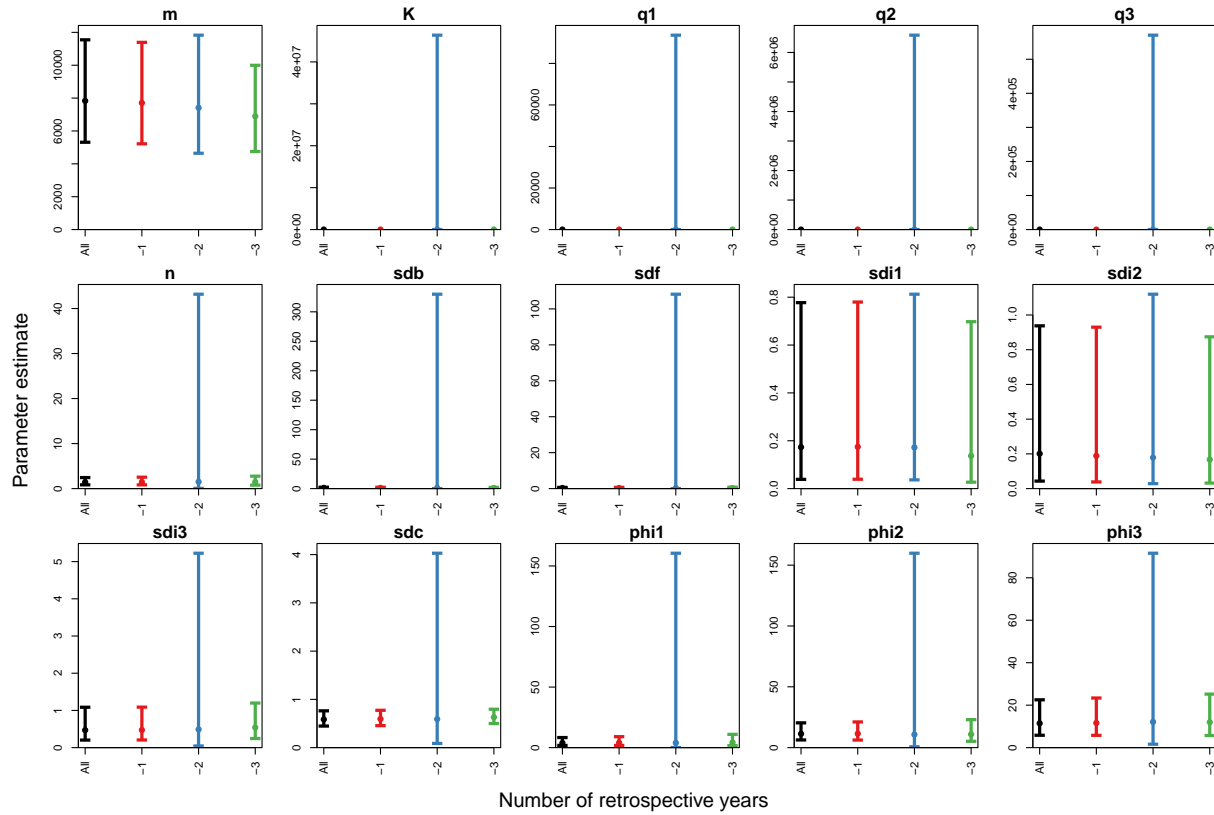
- 4- Consistent patterns in the retrospective analysis:

```
# if -0.2 < mohns_rho < 0.2 => OK
retro_sc_2 <- retro(res_sc_2, nretroyear = 3)
plotspict.retro(retro_sc_2)
```

FFmsy BBmsy
0.009121556 0.008218423

```
plotspict.retro.fixed(retro_sc_2)
```

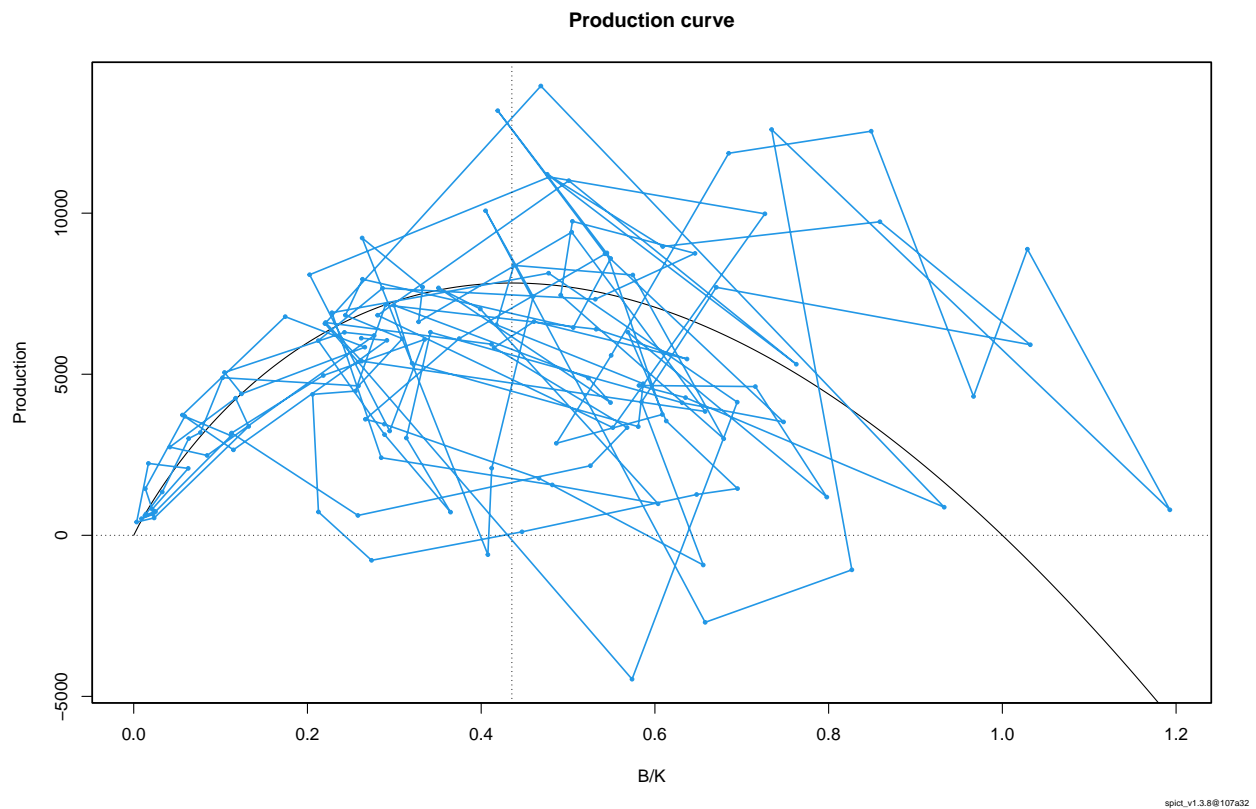


- 5- Realistic production curve:

```
# if between 0.1 and 0.9 => OK
calc.bmsyk(res_sc_2)
```

```
[1] 0.4353436
```

```
plotspict.production(res_sc_2)
```



- 6- High assessment uncertainty:

Main variance parameteres (logsdB, logsdC, logsdI, logsdF) should not be unreallistically high:
`get.par("logsdB", res_sc_2)`

| | ll | est | ul | sd | cv |
|--------|------------|-----------|-----------|-----------|----------|
| logsdB | -0.5078369 | 0.1651432 | 0.8381233 | 0.3433635 | 2.079187 |

`get.par("logsdC", res_sc_2)`

| | ll | est | ul | sd | cv |
|--------|------------|------------|------------|-----------|------------|
| logsdC | -0.8052825 | -0.5381435 | -0.2710046 | 0.1362979 | -0.2532742 |

`get.par("logsdI", res_sc_2)`

| | ll | est | ul | sd | cv |
|--------|-----------|------------|-------------|-----------|------------|
| logsdI | -3.252933 | -1.7524866 | -0.25203991 | 0.7655481 | -0.4368353 |
| logsdI | -3.143722 | -1.6041144 | -0.06450683 | 0.7855285 | -0.4896961 |
| logsdI | -1.595396 | -0.7567511 | 0.08189393 | 0.4278880 | -0.5654276 |

`get.par("logsdF", res_sc_2)`

| | ll | est | ul | sd | cv |
|--------|-----------|-----------|------------|----------|------------|
| logsdF | -1.741354 | -1.064895 | -0.3884374 | 0.345138 | -0.3241051 |

```
calc.om(res_sc_2) # if order of magnitude < 2 => OK)
```

| | lower | est | upper | CI range | order | magnitude |
|--------|-------|------|-------|----------|-------|-----------|
| B/Bmsy | 0.29 | 0.91 | 2.90 | 2.61 | | 1 |
| F/Fmsy | 0.06 | 0.21 | 0.73 | 0.67 | | 1 |

- 7- Initial values do not influence the parameter estimates:

```
check_sc_2$check.ini$resmat # Trials that converged should have same or similar estimates.
```

| | Distance | m | K | q | q | q | n | sdb | sdf | sdi | sdi | sdi |
|----------|----------|---------|---------|-----|------|------|------|------|------|------|-----|------|
| Basevec | 0.00 | 7831.86 | 6060.41 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 1 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 2 | 0.13 | 7831.78 | 6060.50 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 3 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 4 | 0.15 | 7831.77 | 6060.52 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 5 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 6 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 7 | 0.13 | 7831.77 | 6060.51 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 8 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 9 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 10 | 0.16 | 7831.76 | 6060.53 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 11 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 12 | 0.32 | 7831.73 | 6060.70 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 13 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 14 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 15 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 16 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 17 | 0.14 | 7831.77 | 6060.50 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 18 | 0.13 | 7831.77 | 6060.49 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 19 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 20 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 21 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 22 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 23 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 24 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 25 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 26 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 27 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 28 | 0.14 | 7831.77 | 6060.50 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 29 | 0.14 | 7831.77 | 6060.52 | 6.3 | 8.77 | 5.31 | 1.43 | 1.18 | 0.34 | 0.17 | 0.2 | 0.47 |
| Trial 30 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |

| | sdc | phi | phi | phi |
|---------|------|------|-------|-------|
| Basevec | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 1 | NA | NA | NA | NA |
| Trial 2 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 3 | NA | NA | NA | NA |
| Trial 4 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 5 | NA | NA | NA | NA |
| Trial 6 | NA | NA | NA | NA |
| Trial 7 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 8 | NA | NA | NA | NA |

| | | | | |
|----------|------|------|-------|-------|
| Trial 9 | NA | NA | NA | NA |
| Trial 10 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 11 | NA | NA | NA | NA |
| Trial 12 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 13 | NA | NA | NA | NA |
| Trial 14 | NA | NA | NA | NA |
| Trial 15 | NA | NA | NA | NA |
| Trial 16 | NA | NA | NA | NA |
| Trial 17 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 18 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 19 | NA | NA | NA | NA |
| Trial 20 | NA | NA | NA | NA |
| Trial 21 | NA | NA | NA | NA |
| Trial 22 | NA | NA | NA | NA |
| Trial 23 | NA | NA | NA | NA |
| Trial 24 | NA | NA | NA | NA |
| Trial 25 | NA | NA | NA | NA |
| Trial 26 | NA | NA | NA | NA |
| Trial 27 | NA | NA | NA | NA |
| Trial 28 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 29 | 0.58 | 3.88 | 11.34 | 11.46 |
| Trial 30 | NA | NA | NA | NA |

Scenario 3

Model Fit

Results when BOCADEVA data is included in the model indicate that uncertainty levels are higher. According to the estimated exploitable biomass, the model estimated an exploitable biomass of 2513.81 tonnes and a fishing mortality of 2.75. Predicted catchabilities were 5.52, 7.33, 4.45 and 8.86 for PELAGO, ECOCADIZ, ECOCADIZ-RECLUTAS and BOCADEVA, respectively. Moreover, as in the two previous scenarios, Kobe plot determines that the stock biomass is in suboptimal levels and the fishing mortality is lower than fishing mortality at MSY.

```
res_sc_3 <- fit.spict(sc_3_data)
summary(res_sc_3)
```

```
Convergence: 0 MSG: relative convergence (4)
Objective function at optimum: 220.8719401
Euler time step (years): 1/16 or 0.0625
Nobs C: 140, Nobs I1: 21, Nobs I2: 14, Nobs I3: 10, Nobs I4: 7
```

Priors

```
logn ~ dnorm[log(2), 2^2]
logalpha ~ dnorm[log(1), 2^2]
logbeta ~ dnorm[log(1), 2^2]
```

Model parameter estimates w 95% CI

| | estimate | cilow | ciupp | log.est |
|--------|-----------|-----------|--------------|------------|
| alpha1 | 0.1492717 | 0.0284465 | 7.832967e-01 | -1.9019871 |
| alpha2 | 0.1587590 | 0.0458762 | 5.494010e-01 | -1.8403677 |
| alpha3 | 0.4369255 | 0.1556105 | 1.226806e+00 | -0.8279926 |
| alpha4 | 0.1322751 | 0.0261861 | 6.681678e-01 | -2.0228717 |

| | | | | |
|------|--------------|--------------|--------------|------------|
| beta | 1.6438885 | 0.9015020 | 2.997630e+00 | 0.4970645 |
| r | 3.2607914 | 1.2203602 | 8.712805e+00 | 1.1819699 |
| rc | 5.0159124 | 2.5258119 | 9.960907e+00 | 1.6126153 |
| rold | 10.8628311 | 3.2319933 | 3.651032e+01 | 2.3853470 |
| m | 7589.0191643 | 5237.2155476 | 1.099691e+04 | 8.9344576 |
| K | 7255.2039430 | 3033.3622138 | 1.735302e+04 | 8.8894743 |
| q1 | 5.5171546 | 2.1782544 | 1.397403e+01 | 1.7078623 |
| q2 | 7.3343738 | 2.1296352 | 2.525927e+01 | 1.9925720 |
| q3 | 4.4537980 | 1.3198273 | 1.502948e+01 | 1.4937572 |
| q4 | 8.8623509 | 2.5640604 | 3.063160e+01 | 2.1818121 |
| n | 1.3001788 | 0.8470871 | 1.995621e+00 | 0.2625018 |
| sdb | 1.0674449 | 0.6589232 | 1.729243e+00 | 0.0652678 |
| sdf | 0.3632356 | 0.2025167 | 6.515024e-01 | -1.0127036 |
| sdi1 | 0.1593393 | 0.0352388 | 7.204843e-01 | -1.8367192 |
| sdi2 | 0.1694665 | 0.0549095 | 5.230222e-01 | -1.7750998 |
| sdi3 | 0.4663939 | 0.2135365 | 1.018670e+00 | -0.7627247 |
| sdi4 | 0.1411963 | 0.0300516 | 6.634054e-01 | -1.9576039 |
| sdc | 0.5971188 | 0.4864066 | 7.330305e-01 | -0.5156391 |
| phi1 | 4.0426228 | 1.9031506 | 8.587234e+00 | 1.3968937 |
| phi2 | 11.4571298 | 6.4915431 | 2.022105e+01 | 2.4386122 |
| phi3 | 11.2542578 | 5.7112408 | 2.217702e+01 | 2.4207465 |

Deterministic reference points (Drp)

| | estimate | cilow | ciupp | log.est |
|-------|-------------|-------------|--------------|-----------|
| Bmsyd | 3025.977578 | 1375.735821 | 6655.740271 | 8.0149895 |
| Fmsyd | 2.507956 | 1.262906 | 4.980453 | 0.9194682 |
| MSYd | 7589.019164 | 5237.215548 | 10996.914554 | 8.9344576 |

Stochastic reference points (Srp)

| | estimate | cilow | ciupp | log.est | rel.diff.Drp |
|-------|-------------|--------------|-------------|----------|--------------|
| Bmsys | 2373.58976 | 298.3070405 | 18886.34053 | 7.772159 | -0.2748528 |
| Fmsys | 4.50693 | 0.9803418 | 20.71973 | 1.505616 | 0.4435334 |
| MSYs | 12001.70964 | 3424.8397796 | 42057.74390 | 9.392804 | 0.3676718 |

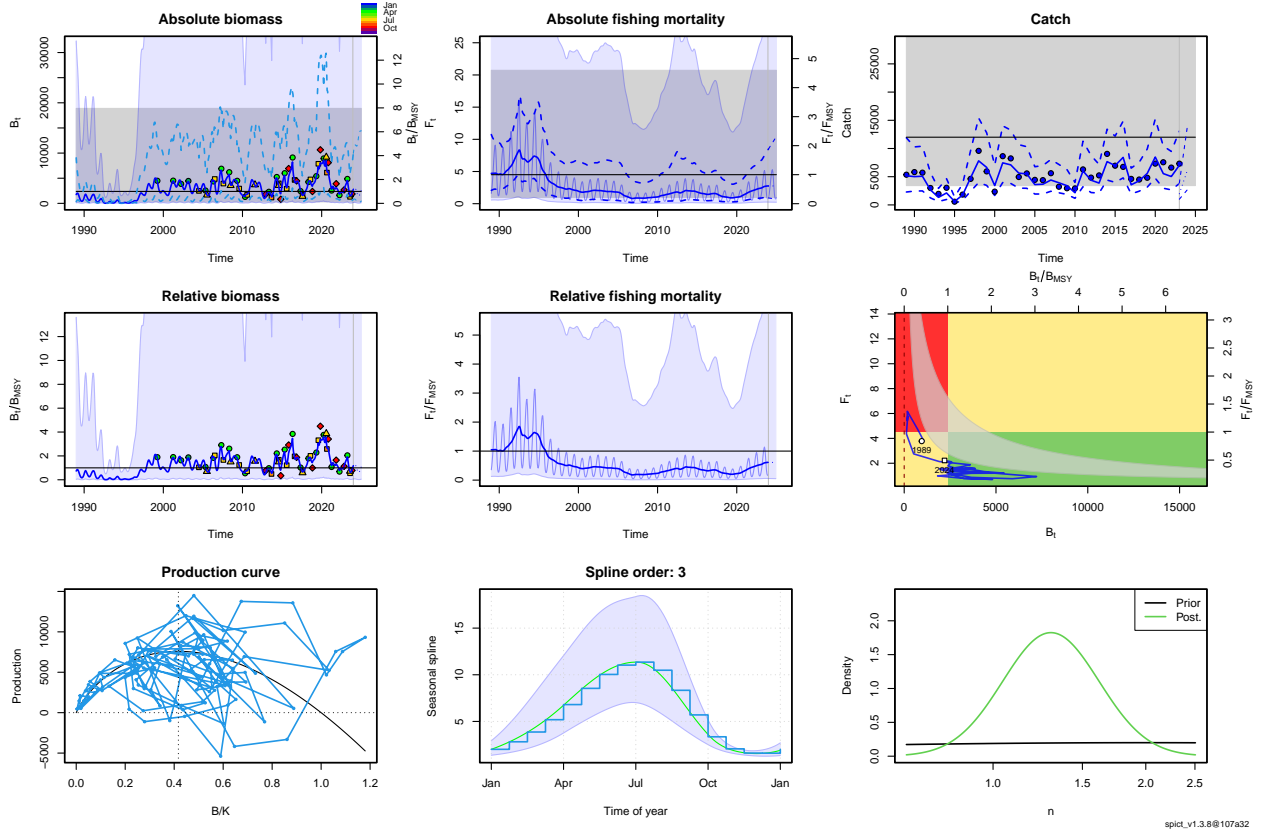
States w 95% CI (inp\$msytype: s)

| | estimate | cilow | ciupp | log.est |
|----------------|--------------|-------------|-------------|------------|
| B_2023.94 | 2513.8097970 | 695.7095338 | 9083.158112 | 7.8295547 |
| F_2023.94 | 2.7535907 | 0.9059081 | 8.369791 | 1.0129058 |
| B_2023.94/Bmsy | 1.0590751 | 0.0597899 | 18.759704 | 0.0573960 |
| F_2023.94/Fmsy | 0.6109681 | 0.0562845 | 6.632060 | -0.4927105 |

Predictions w 95% CI (inp\$msytype: s)

| | prediction | cilow | ciupp | log.est |
|----------------|--------------|--------------|--------------|------------|
| B_2025.00 | 2568.9390262 | 457.4582694 | 14426.338228 | 7.8512483 |
| F_2025.00 | 2.7535921 | 0.7267465 | 10.433170 | 1.0129063 |
| B_2025.00/Bmsy | 1.0823012 | 0.0492211 | 23.798247 | 0.0790895 |
| F_2025.00/Fmsy | 0.6109684 | 0.0504034 | 7.405899 | -0.4927100 |
| Catch_2024.00 | 6120.2249729 | 2689.7488405 | 13925.892691 | 8.7193541 |
| E(B_inf) | 4158.0545086 | NA | NA | 8.3328026 |

```
plot(res_sc_3)
```



Model Diagnostics

In relation to the diagnostic checklist, the model meets all requirements except normality of catch residuals and order of magnitudes of $B/BMSY$ and $F/FMSY$. In this sense, $B/BMSY$ and $F/FMSY$ orders of magnitude were 3 and 2, respectively. Moreover, the retrospective analysis could not converge with peel -3.

- 1- The assessment converged:

```
# if 0 => OK
res_sc_3$opt$convergence
```

```
[1] 0
```

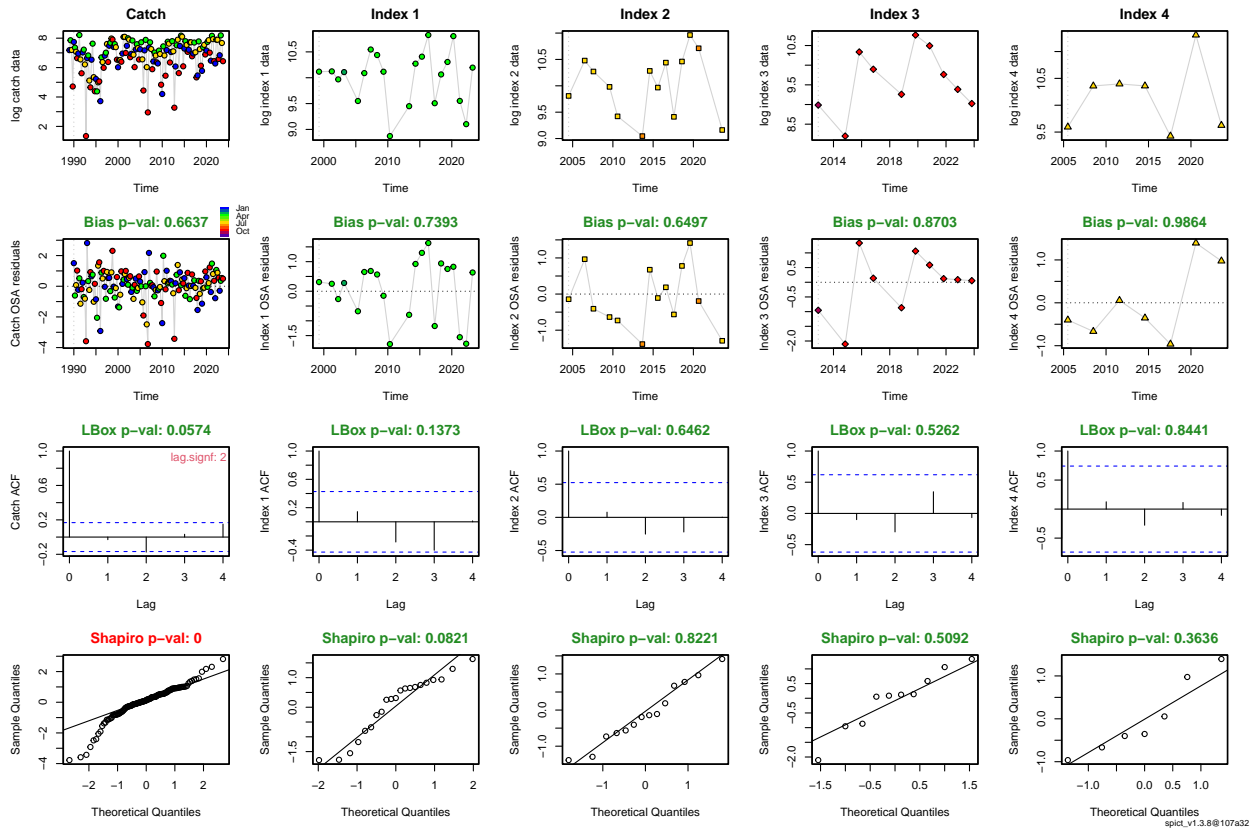
- 2- All variance parameters of the model parameters are finite:

```
# if TRUE => OK
all(is.finite(res_sc_3$sd))
```

```
[1] TRUE
```

- 3- No violation of model assumptions:

```
res_sc_3 <- calc.osa.resid(res_sc_3)
plotspict.diagnostic(res_sc_3)
```



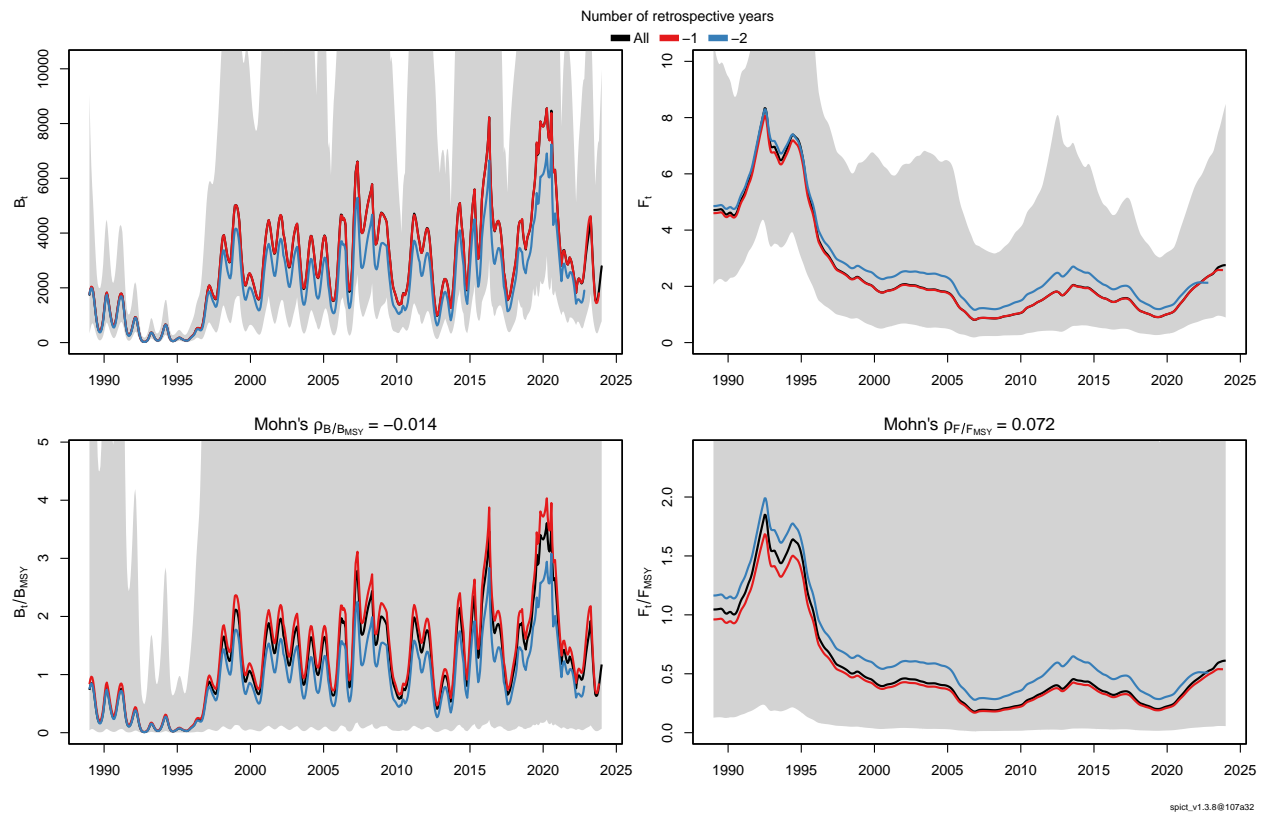
- 4- Consistent patterns in the retrospective analysis:

```
# if -0.2 < mohns_rho < 0.2 => OK
retro_sc_3 <- retro(res_sc_3, nretroyear = 3)
```

```
Error in calc.osa.resid(rep) :
  Could not calculate OSA residuals because estimation did not converge.
```

```
plotspict.retro(retro_sc_3)
```

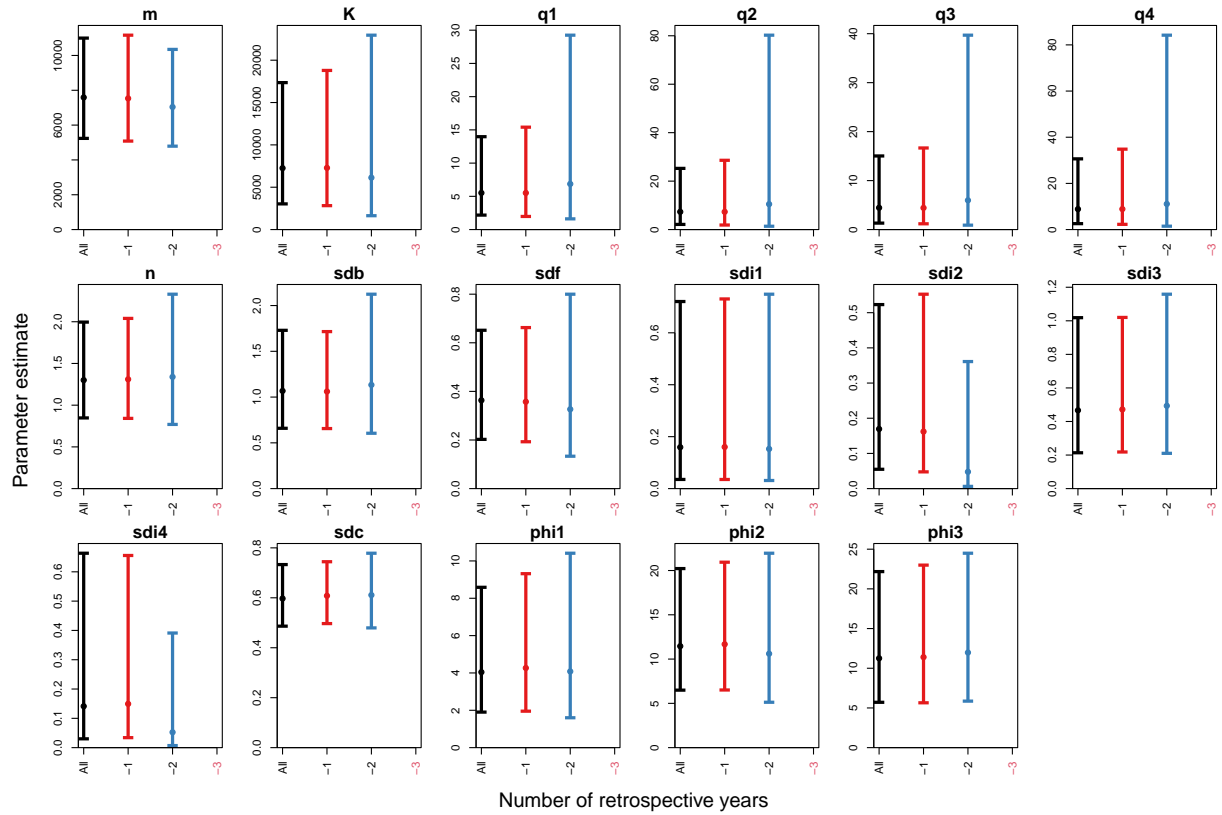
Excluded 1 retrospective runs that was not converged: 3



FFmsy BBmsy
0.07179524 -0.01381742

```
plotspict.retro.fixed(retro_sc_3)
```

Excluded 1 retrospective run that was not converged: 3

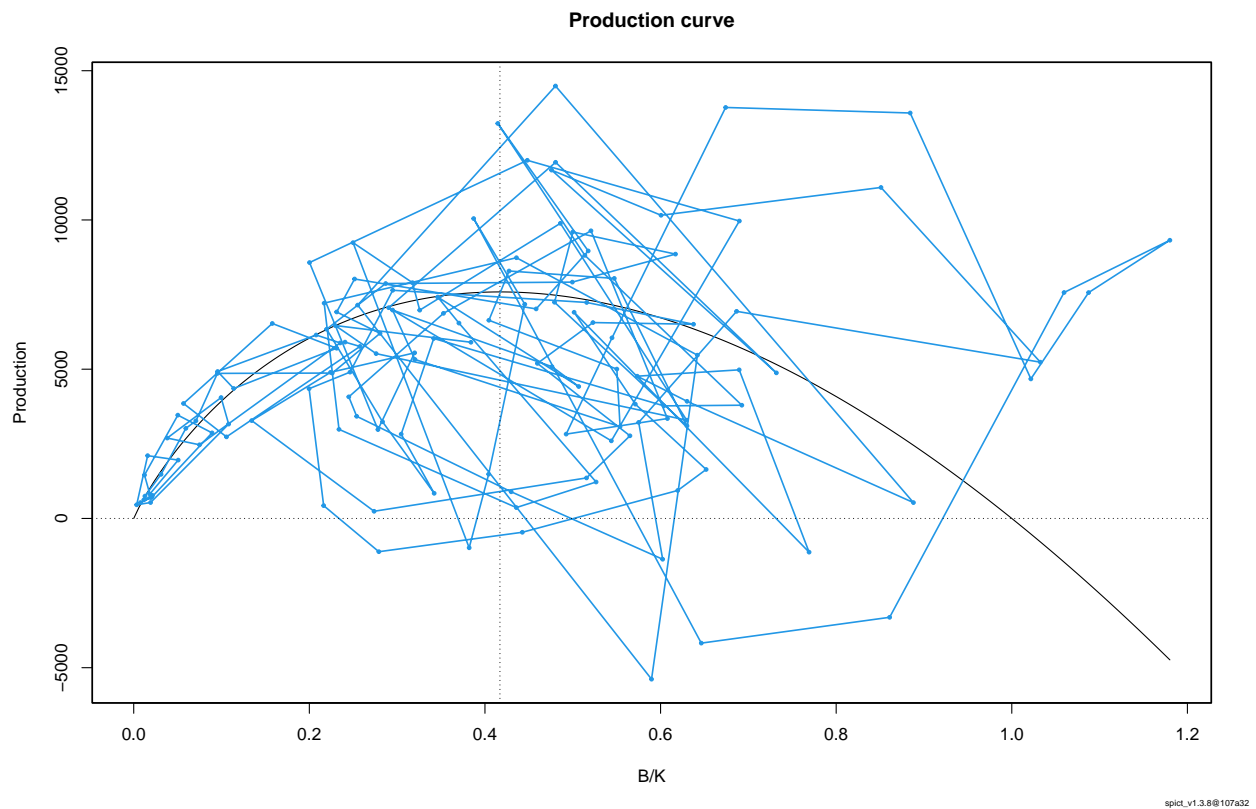


- 5- Realistic production curve:

```
# if between 0.1 and 0.9 => OK
calc.bmsyk(res_sc_3)
```

```
[1] 0.4170768
```

```
plotspict.production(res_sc_3)
```



- 6- High assessment uncertainty:

Main variance parameteres (logsdB, logsdC, logsdI, logsdF) should not be unreallistically high:
`get.par("logsdB", res_sc_3)`

| | ll | est | ul | sd | cv |
|--------|------------|------------|----------|-----------|----------|
| logsdB | -0.4171483 | 0.06526784 | 0.547684 | 0.2461352 | 3.771156 |

`get.par("logsdC", res_sc_3)`

| | ll | est | ul | sd | cv |
|--------|------------|------------|------------|-----------|------------|
| logsdC | -0.7207103 | -0.5156391 | -0.3105679 | 0.1046301 | -0.2029134 |

`get.par("logsdI", res_sc_3)`

| | ll | est | ul | sd | cv |
|--------|-----------|------------|-------------|-----------|------------|
| logsdI | -3.345607 | -1.8367192 | -0.32783169 | 0.7698547 | -0.4191467 |
| logsdI | -2.902068 | -1.7750998 | -0.64813136 | 0.5749945 | -0.3239223 |
| logsdI | -1.543948 | -0.7627247 | 0.01849811 | 0.3985904 | -0.5225875 |
| logsdI | -3.504839 | -1.9576039 | -0.41036897 | 0.7894201 | -0.4032583 |

`get.par("logsdF", res_sc_3)`

| | ll | est | ul | sd | cv |
|--------|-----------|-----------|------------|-----------|------------|
| logsdF | -1.596933 | -1.012704 | -0.4284742 | 0.2980817 | -0.2943425 |

```
calc.om(res_sc_3) # if order of magnitude < 2 => OK)
```

| | lower | est | upper | CI range | order | magnitude |
|--------|-------|------|-------|----------|-------|-----------|
| B/Bmsy | 0.06 | 1.06 | 18.76 | 18.70 | | 3 |
| F/Fmsy | 0.01 | 0.16 | 1.87 | 1.85 | | 2 |

- 7- Initial values do not influence the parameter estimates:

```
check_sc_3$check.ini$resmat # Trials that converged should have same or similar estimates.
```

| | Distance | m | K | q | q | q | q | n | sdb | sdf |
|----------|----------|----------|---------|--------|--------|--------|--------|------|------|------|
| Basevec | 0.00 | 7589.02 | 7255.20 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 1 | 0.01 | 7589.02 | 7255.21 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 2 | 0.01 | 7589.03 | 7255.21 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 3 | 0.02 | 7589.01 | 7255.22 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 4 | 0.00 | 7589.02 | 7255.20 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 5 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 6 | 0.06 | 7588.97 | 7255.24 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 7 | 0.04 | 7589.02 | 7255.24 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 8 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 9 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 10 | 6747.17 | 10001.28 | 989.54 | 119.93 | 223.10 | 584.88 | 232.28 | 1.12 | 0.15 | 0.52 |
| Trial 11 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 12 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 13 | 0.02 | 7589.01 | 7255.23 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 14 | 0.02 | 7589.00 | 7255.20 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 15 | 0.05 | 7588.98 | 7255.18 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 16 | 0.17 | 7589.02 | 7255.03 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 17 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 18 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 19 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 20 | 0.06 | 7589.04 | 7255.15 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 21 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 22 | 0.01 | 7589.03 | 7255.20 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 23 | 0.01 | 7589.03 | 7255.20 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 24 | 0.10 | 7589.04 | 7255.11 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 25 | 0.03 | 7589.01 | 7255.23 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 26 | 0.01 | 7589.02 | 7255.19 | 5.52 | 7.33 | 4.45 | 8.86 | 1.30 | 1.07 | 0.36 |
| Trial 27 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 28 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 29 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 30 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA |

| | sdi | sdi | sdi | sdi | sdc | phi | phi | phi |
|---------|------|------|------|------|------|------|-------|-------|
| Basevec | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 1 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 2 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 3 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 4 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 5 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 6 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 7 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 8 | NA | NA | NA | NA | NA | NA | NA | NA |

| | | | | | | | | |
|----------|------|------|------|------|------|------|-------|-------|
| Trial 9 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 10 | 0.08 | 0.28 | 0.60 | 0.06 | 0.35 | 0.62 | 0.37 | 0.96 |
| Trial 11 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 12 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 13 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 14 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 15 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 16 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 17 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 18 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 19 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 20 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 21 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 22 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 23 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 24 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 25 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 26 | 0.16 | 0.17 | 0.47 | 0.14 | 0.60 | 4.04 | 11.46 | 11.25 |
| Trial 27 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 28 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 29 | NA | NA | NA | NA | NA | NA | NA | NA |
| Trial 30 | NA | NA | NA | NA | NA | NA | NA | NA |

Scenario 4

Model Fit

Results when BOCADEVA data and its uncertainty levels were included in the model also show high uncertainty levels of model estimations. According to the estimated exploitable biomass, the model estimated an exploitable biomass of 2440.36 tonnes and a fishing mortality of 2.84. Predicted catchabilities were 5.62, 7.55, 4.58 and 9.08 for PELAGO, ECOCADIZ, ECOCADIZ-RECLUTAS and BOCADEVA, respectively. Kobe plot again defines stock biomass in suboptimal levels and the fishing mortality in lower levels than fishing mortality at MSY.

```
res_sc_4 <- fit.spict(sc_4_data)
summary(res_sc_4)
```

```
Convergence: 0 MSG: relative convergence (4)
Objective function at optimum: 220.42738
Euler time step (years): 1/16 or 0.0625
Nobs C: 140, Nobs I1: 21, Nobs I2: 14, Nobs I3: 10, Nobs I4: 7
```

Priors

```
logn ~ dnorm[log(2), 2^2]
logalpha ~ dnorm[log(1), 2^2]
logbeta ~ dnorm[log(1), 2^2]
```

Model parameter estimates w 95% CI

| | estimate | cilow | ciupp | log.est |
|--------|-----------|-----------|--------------|------------|
| alpha1 | 0.1475009 | 0.0280514 | 7.755940e-01 | -1.9139211 |
| alpha2 | 0.1420530 | 0.0348073 | 5.797358e-01 | -1.9515554 |
| alpha3 | 0.4267707 | 0.1500109 | 1.214133e+00 | -0.8515084 |
| alpha4 | 0.2502797 | 0.0532823 | 1.175625e+00 | -1.3851760 |

| | | | | |
|------|--------------|--------------|--------------|------------|
| beta | 1.6429756 | 0.9033329 | 2.988233e+00 | 0.4965090 |
| r | 3.3269404 | 1.2402004 | 8.924794e+00 | 1.2020531 |
| rc | 5.1036921 | 2.5632432 | 1.016200e+01 | 1.6299642 |
| rold | 10.9532980 | 3.3277610 | 3.605269e+01 | 2.3936406 |
| m | 7587.9997108 | 5250.7683247 | 1.096558e+04 | 8.9343233 |
| K | 7120.5758661 | 2979.0337578 | 1.701981e+04 | 8.8707439 |
| q1 | 5.6240096 | 2.2269346 | 1.420315e+01 | 1.7270449 |
| q2 | 7.5484102 | 2.1855796 | 2.607020e+01 | 2.0213370 |
| q3 | 4.5753142 | 1.3554758 | 1.544365e+01 | 1.5206754 |
| q4 | 9.0768836 | 2.6402405 | 3.120542e+01 | 2.2057309 |
| n | 1.3037387 | 0.8497476 | 2.000282e+00 | 0.2652361 |
| sdb | 1.0813576 | 0.6654948 | 1.757090e+00 | 0.0782173 |
| sdf | 0.3624569 | 0.2023657 | 6.491961e-01 | -1.0148497 |
| sdi1 | 0.1595012 | 0.0352494 | 7.217332e-01 | -1.8357038 |
| sdi2 | 0.1536100 | 0.0420065 | 5.617230e-01 | -1.8733381 |
| sdi3 | 0.4614917 | 0.2089301 | 1.019358e+00 | -0.7732912 |
| sdi4 | 0.2706419 | 0.0617029 | 1.187093e+00 | -1.3069587 |
| sdc | 0.5955078 | 0.4836252 | 7.332735e-01 | -0.5183407 |
| phi1 | 4.0102790 | 1.8849893 | 8.531793e+00 | 1.3888608 |
| phi2 | 11.3755379 | 6.4251603 | 2.014002e+01 | 2.4314653 |
| phi3 | 11.3034089 | 5.7492505 | 2.222325e+01 | 2.4251043 |

Deterministic reference points (Drp)

| | estimate | cilow | ciupp | log.est |
|-------|-------------|-------------|--------------|----------|
| Bmsyd | 2973.533507 | 1354.117240 | 6529.642530 | 7.997506 |
| Fmsyd | 2.551846 | 1.281622 | 5.080999 | 0.936817 |
| MSYd | 7587.999711 | 5250.768325 | 10965.583711 | 8.934323 |

Stochastic reference points (Srp)

| | estimate | cilow | ciupp | log.est | rel.diff.Drp |
|-------|--------------|-------------|-------------|----------|--------------|
| Bmsys | 2474.098015 | 603.346879 | 10145.34292 | 7.813631 | -0.2018657 |
| Fmsys | 4.361733 | 1.263216 | 15.06054 | 1.472870 | 0.4149468 |
| MSYs | 11695.277848 | 3760.353370 | 36374.11447 | 9.366940 | 0.3511912 |

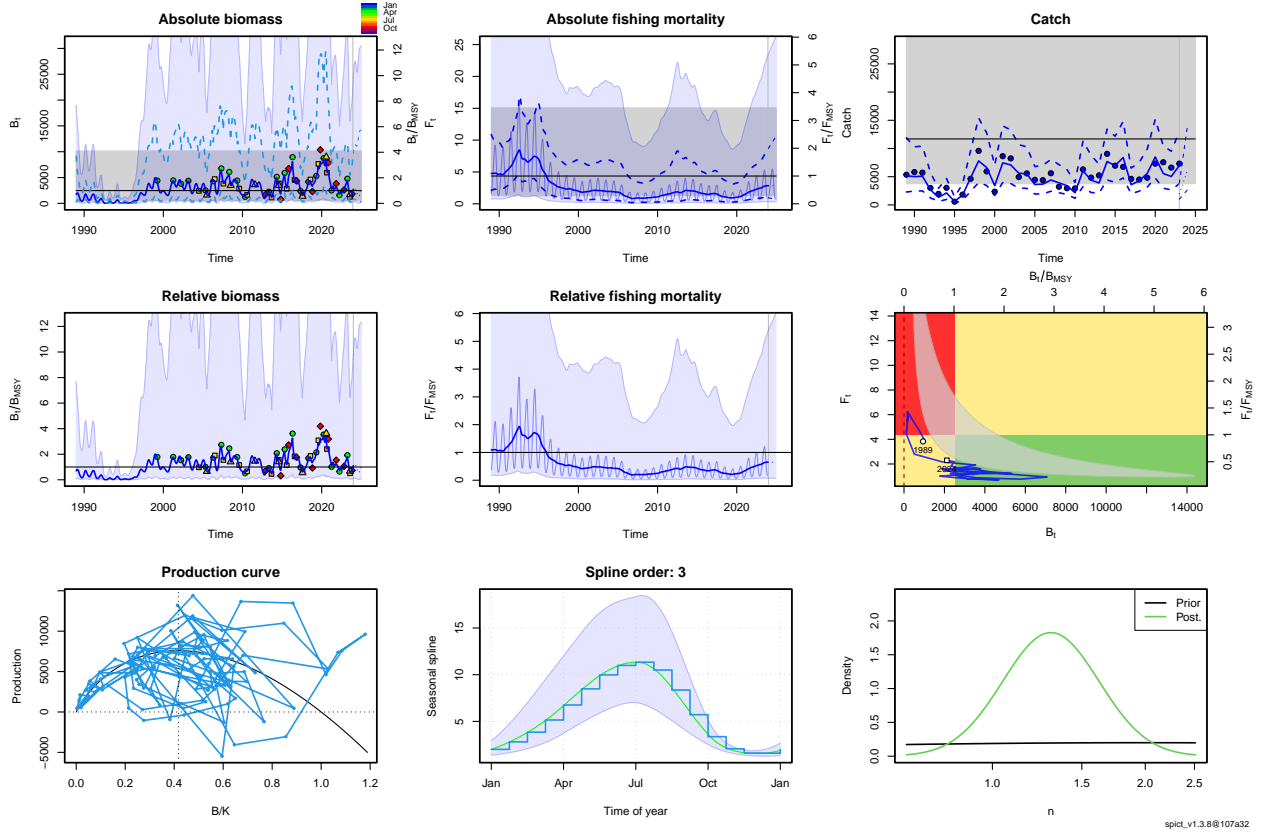
States w 95% CI (inp\$msytype: s)

| | estimate | cilow | ciupp | log.est |
|----------------|--------------|-------------|-------------|------------|
| B_2023.94 | 2440.3596567 | 676.2632860 | 8806.267289 | 7.7999007 |
| F_2023.94 | 2.8432254 | 0.9420090 | 8.581585 | 1.0449391 |
| B_2023.94/Bmsy | 0.9863634 | 0.1067080 | 9.117520 | -0.0137305 |
| F_2023.94/Fmsy | 0.6518568 | 0.0793537 | 5.354723 | -0.4279304 |

Predictions w 95% CI (inp\$msytype: s)

| | prediction | cilow | ciupp | log.est |
|----------------|--------------|--------------|--------------|------------|
| B_2025.00 | 2485.4785739 | 436.3576031 | 14157.204316 | 7.8182205 |
| F_2025.00 | 2.8432268 | 0.7554802 | 10.700397 | 1.0449396 |
| B_2025.00/Bmsy | 1.0045999 | 0.0818640 | 12.328024 | 0.0045893 |
| F_2025.00/Fmsy | 0.6518571 | 0.0701220 | 6.059692 | -0.4279299 |
| Catch_2024.00 | 6097.2496810 | 2672.7504817 | 13909.436712 | 8.7155931 |
| E(B_inf) | 3921.6866360 | NA | NA | 8.2742771 |

```
plot(res_sc_4)
```



Model Diagnostics

Diagnostic checklist determined that model met all requirements except normality of catch residuals and order of magnitude of F/F_{MSY} . In this sense, F/F_{MSY} order of magnitude was 2. Additionally, the retrospective analysis could not converge with peel -3.

- 1- The assessment converged:

```
# if 0 => OK
res_sc_4$opt$convergence
```

[1] 0

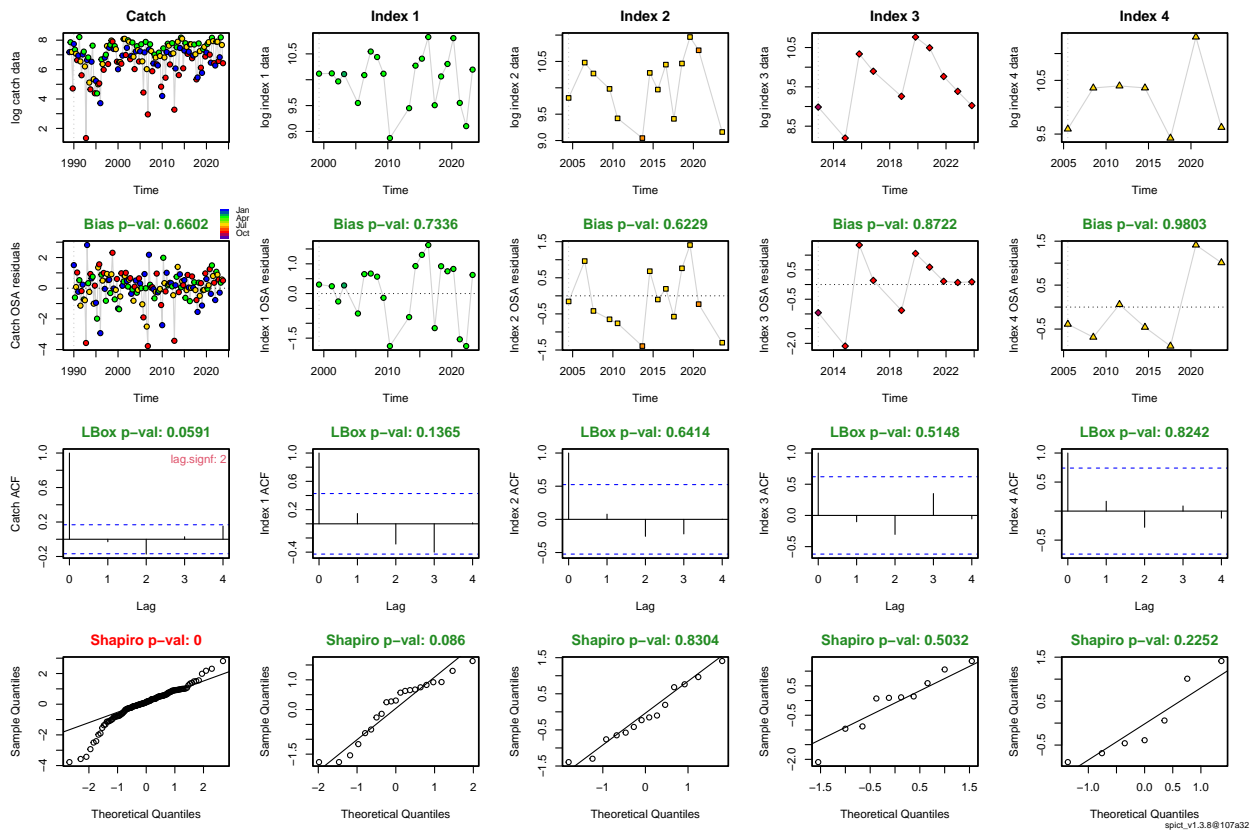
- 2- All variance parameters of the model parameters are finite:

```
# if TRUE => OK
all(is.finite(res_sc_4$sd))
```

[1] TRUE

- 3- No violation of model assumptions:

```
res_sc_4 <- calc.osa.resid(res_sc_4)
plotspict.diagnostic(res_sc_4)
```



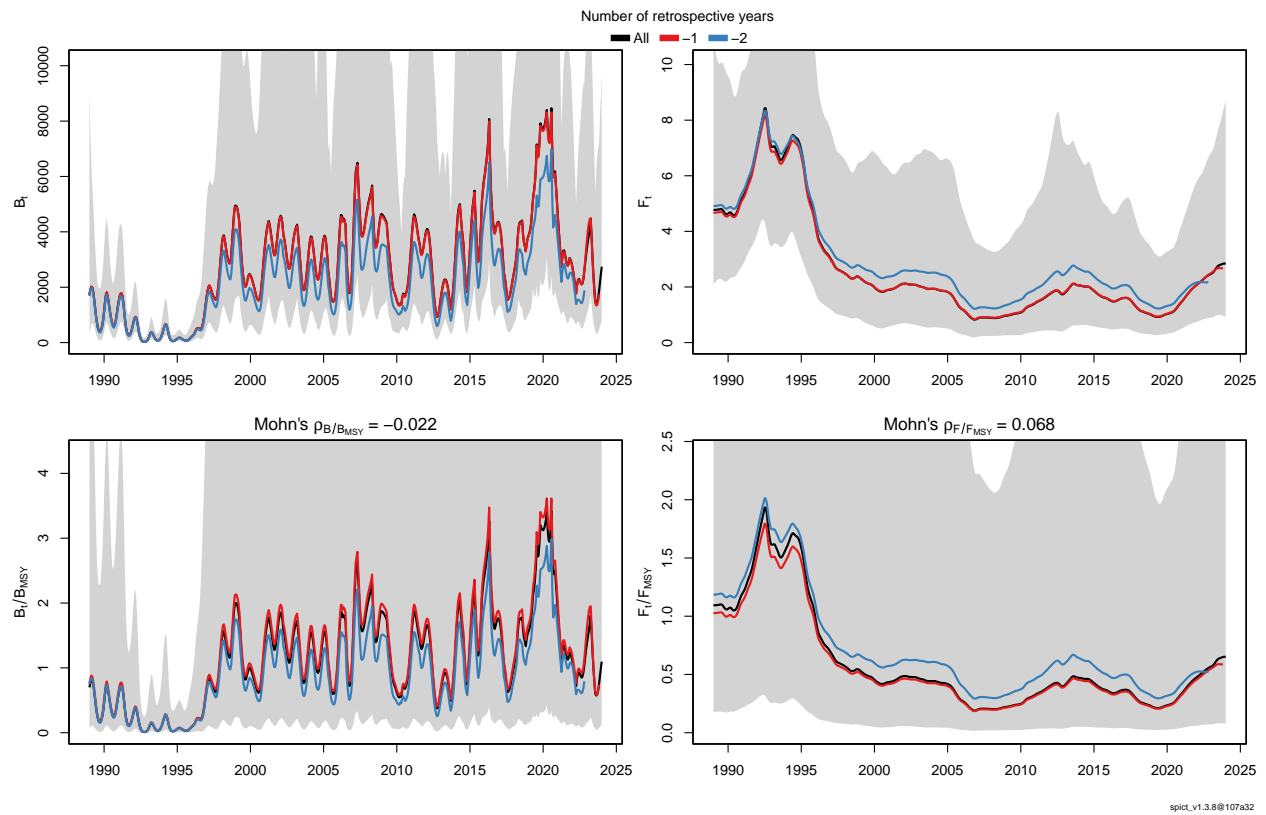
- 4- Consistent patterns in the retrospective analysis:

```
# if -0.2 < mohns_rho < 0.2 => OK
retro_sc_4 <- retro(res_sc_4, nretroyear = 3)
```

```
Error in calc.osa.resid(rep) :
  Could not calculate OSA residuals because estimation did not converge.
```

```
plotspict.retro(retro_sc_4)
```

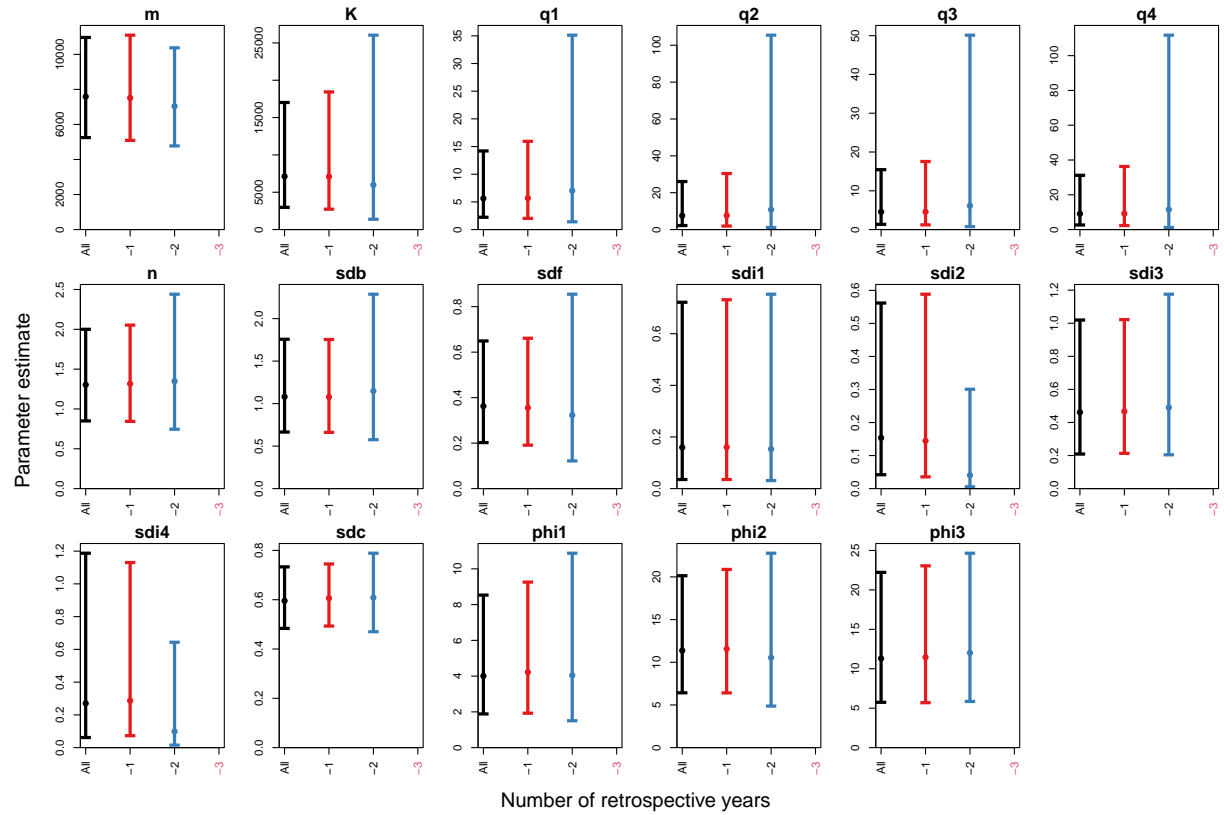
Excluded 1 retrospective runs that was not converged: 3



FFmsy BBmsy
0.06803314 -0.02170606

```
plotspict.retro.fixed(retro_sc_4)
```

Excluded 1 retrospective run that was not converged: 3

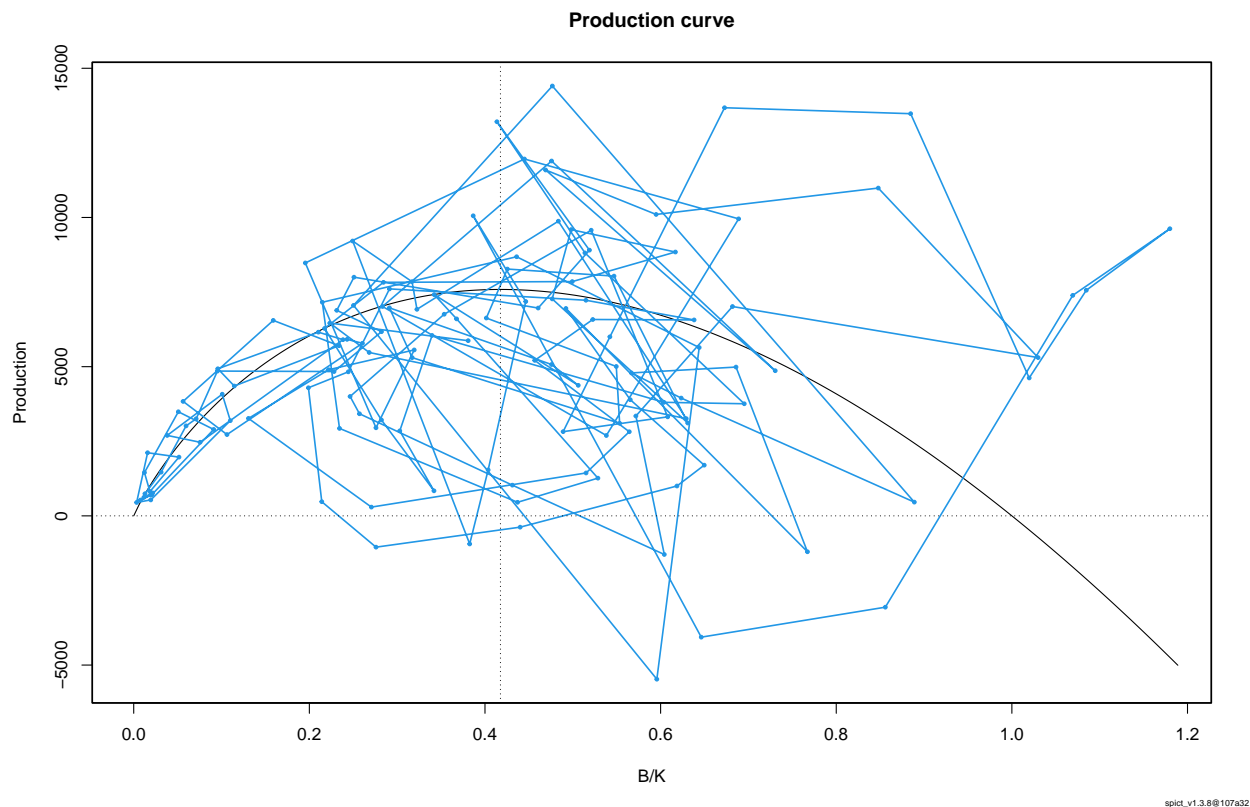


- 5- Realistic production curve:

```
# if between 0.1 and 0.9 => OK
calc.bmsyk(res_sc_4)
```

```
[1] 0.4175973
```

```
plotspict.production(res_sc_4)
```



- 6- High assessment uncertainty:

Main variance parameteres (logsdB, logsdC, logsdI, logsdF) should not be unreallistically high:
`get.par("logsdB", res_sc_4)`

| | ll | est | ul | sd | cv |
|--------|------------|------------|----------|-----------|----------|
| logsdB | -0.4072245 | 0.07821726 | 0.563659 | 0.2476789 | 3.166551 |

`get.par("logsdC", res_sc_4)`

| | ll | est | ul | sd | cv |
|--------|-----------|------------|------------|-----------|------------|
| logsdC | -0.726445 | -0.5183407 | -0.3102365 | 0.1061776 | -0.2048413 |

`get.par("logsdI", res_sc_4)`

| | ll | est | ul | sd | cv |
|--------|-----------|------------|-------------|-----------|------------|
| logsdI | -3.345308 | -1.8357038 | -0.32609972 | 0.7702203 | -0.4195777 |
| logsdI | -3.169930 | -1.8733381 | -0.57674647 | 0.6615385 | -0.3531335 |
| logsdI | -1.565755 | -0.7732912 | 0.01917312 | 0.4043259 | -0.5228638 |
| logsdI | -2.785425 | -1.3069587 | 0.17150763 | 0.7543334 | -0.5771670 |

`get.par("logsdF", res_sc_4)`

| | ll | est | ul | sd | cv |
|--------|-----------|----------|------------|-----------|------------|
| logsdF | -1.597679 | -1.01485 | -0.4320205 | 0.2973673 | -0.2930161 |

```
calc.om(res_sc_4) # if order of magnitude < 2 => OK)
```

| | lower | est | upper | CI range | order | magnitude |
|--------|-------|------|-------|----------|-------|-----------|
| B/Bmsy | 0.11 | 0.99 | 9.12 | 9.01 | | 1 |
| F/Fmsy | 0.02 | 0.18 | 1.52 | 1.50 | | 2 |

- 7- Initial values do not influence the parameter estimates:

```
check_sc_4$check.ini$resmat # Trials that converged should have same or similar estimates.
```

| | Distance | m | K | q | q | q | q | q | n | sdb | sdf | sdi |
|----------|----------|----------|----------|------|------|-------|-------|------|------|------|------|-----|
| Basevec | 0.00 | 7588.00 | 7120.58 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 1 | 0.08 | 7588.02 | 7120.66 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 2 | 0.10 | 7588.01 | 7120.67 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 3 | 0.07 | 7588.01 | 7120.64 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 4 | 0.12 | 7588.00 | 7120.70 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 5 | 0.10 | 7588.03 | 7120.67 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 6 | 0.10 | 7588.02 | 7120.67 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 7 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 8 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 9 | 0.18 | 7588.04 | 7120.75 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 10 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 11 | 0.12 | 7588.01 | 7120.70 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 12 | 0.02 | 7588.02 | 7120.58 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 13 | 0.10 | 7588.02 | 7120.68 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 14 | 0.08 | 7588.01 | 7120.66 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 15 | 0.12 | 7588.03 | 7120.69 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 16 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 17 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 18 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 19 | 0.10 | 7588.02 | 7120.67 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 20 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 21 | 0.01 | 7587.99 | 7120.57 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 22 | 11314.52 | 12366.37 | 17376.57 | 2.00 | 2.14 | 1.34 | 2.58 | 1.68 | 0.99 | 0.41 | 0.15 | |
| Trial 23 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 24 | 0.13 | 7588.04 | 7120.70 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 25 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 26 | 0.13 | 7588.02 | 7120.71 | 5.62 | 7.55 | 4.58 | 9.08 | 1.30 | 1.08 | 0.36 | 0.16 | |
| Trial 27 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 28 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 29 | 0.00 | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | |
| Trial 30 | 11314.42 | 12366.25 | 17376.52 | 2.00 | 2.14 | 1.34 | 2.58 | 1.68 | 0.99 | 0.41 | 0.15 | |
| | sdi | sdi | sdi | sdc | phi | phi | phi | | | | | |
| Basevec | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 1 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 2 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 3 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 4 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 5 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 6 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 | | | | | |
| Trial 7 | NA | NA | NA | NA | NA | NA | NA | | | | | |
| Trial 8 | NA | NA | NA | NA | NA | NA | NA | | | | | |

| | | | | | | | |
|----------|------|------|------|------|------|-------|-------|
| Trial 9 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 10 | NA | NA | NA | NA | NA | NA | NA |
| Trial 11 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 12 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 13 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 14 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 15 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 16 | NA | NA | NA | NA | NA | NA | NA |
| Trial 17 | NA | NA | NA | NA | NA | NA | NA |
| Trial 18 | NA | NA | NA | NA | NA | NA | NA |
| Trial 19 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 20 | NA | NA | NA | NA | NA | NA | NA |
| Trial 21 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 22 | 0.17 | 0.50 | 0.25 | 0.65 | 5.90 | 15.00 | 8.43 |
| Trial 23 | NA | NA | NA | NA | NA | NA | NA |
| Trial 24 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 25 | NA | NA | NA | NA | NA | NA | NA |
| Trial 26 | 0.15 | 0.46 | 0.27 | 0.60 | 4.01 | 11.38 | 11.30 |
| Trial 27 | NA | NA | NA | NA | NA | NA | NA |
| Trial 28 | NA | NA | NA | NA | NA | NA | NA |
| Trial 29 | NA | NA | NA | NA | NA | NA | NA |
| Trial 30 | 0.17 | 0.50 | 0.25 | 0.65 | 5.90 | 15.00 | 8.43 |

Conclusions

Results indicate that the most robust scenario was Scenario 2. This scenario obtained better results than Scenario 3 and 4 in the diagnostic checklist and included an uncertainty level in ECOCADIZ-RECLUTAS 2012 estimate, making it more realistic than Scenario 1. The greater robustness shown by Scenario 2 compared to Scenarios 3 and 4 could be due to the number of estimates from the BOCADEVA campaign (7 estimates). The low number of estimates from BOCADEVA index may have negatively affected the model fit introducing some noise or additional uncertainty. Thus, we recommend using the scenario 2 estimates over the other scenarios. Finally, a larger number of estimates in the BOCADEVA survey could improve the model obtained in both scenario 3 and scenario 4. Therefore, in order to define the influence of BOCADEVA estimates in the model, we recommend repeating the same exercise in a few years when more BOCADEVA campaigns have been carried out.

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