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1  (*PROBLEM 3*)
2  (*Problem 3.1: A datatype declaration that can be used to represent
3   logical expressions *)
4
5  datatype expr = var of string | AND of expr * expr
6   | OR of expr * expr | NOT of expr;
7
8  (*Problem 3.2:
9   The assignment of truth values for propositional variables within a logical
10  expression can be represented as a list of tuples containing the name of the
11  variable and the truth assignment for it. Thus, this representation would have
12  type (string*bool) list. As an example, [("p", true), ("q", true)] is an
13  assignment list whereby the propositional variables p and q within some given
14  expression both have the value true.*)
15
16  (*Problem 3.3 A function that returns the truth value of a logical Expression E
17  and an assignment L of truth values for propositional variables. This function
18  makes use of a helper function truthValue that identifies the boolean value of
19  a specific propositional variable.*)
20
21  fun truthValue [] prop = false
22    | truthValue ((name, value)::rest) prop =
23      if name = prop then value else truthValue rest prop
24  ;
25
26  fun eval (List, (var x)) = truthValue List x
27    | eval (List, (AND(left, right))) =
28      if (eval (List, left)) = true then
29        if (eval (List, right)) = true then
30          true
31        else false
32      else false
33    | eval (List, (OR(left, right))) =
34      if (eval (List, left)) = false then
35        if (eval (List, right)) = false then
36          false
37        else true
38      else true
39    | eval (List, (NOT(value))) =
40      if (eval (List, value)) = true then
41        false
42      else true
43  ;
44
45  (*Problem 3.4 A function that takes a logical expression and returns a list of
46  all the propositional variables appearing in that list. *)
47
48  fun removeDups [] str = str::[]
49    | removeDups (head::rest) str =
50      if head = str then removeDups rest str else head::(removeDups rest str)
51  ;
52
53  fun varsInExp (expr) =

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54 let
55   fun helper (List, (var x)) = removeDups List x
56   | helper (List, (AND(left, right))) =
57     let val x = (helper (List, left))
58     in
59       (helper (x, right))
60     end
61   | helper (List, (OR(left, right))) =
62     let val x = (helper (List, left))
63     in
64       (helper (x, right))
65     end
66   | helper (List, (NOT(value))) =
67     (helper (List, value))
68 in
69   helper([], expr)
70 end;
71
72
73
74 (*Problem 3.5 A function that takes a logical expression as argument and
75 returns true if the expression is a tautology and false otherwise. Uses 2
76 helper functions: combine creates an assignment list from a list of propositional
77 variables, while flipValue changes the truth assignments for the variables in
78 the assignment list. Raises an END exception if no new truth assignments can
79 occur*)
80
81 exception END
82
83 fun flipValue [] = raise END
84   | flipValue ((name, value)::rest) =
85     if value = false then (name, true)::rest else (name, value)::(flipValue rest)
86   ;
87
88 (*Function initially sets all assignments to false*)
89 fun combine [] value = []
90   | combine (head::rest) value =
91     (head, value)::(combine rest value)
92   ;
93
94 fun isTaut (expr) =
95   let
96     fun flipValue2 assign = (flipValue assign) handle END => [("END", false)]
97     fun checker L E =
98       if eval(L, E) = true then
99         let val newL = flipValue2 L
100         in
101           if newL = [("END", false)] then true else checker newL E
102         end
103       else false
104     val varList = varsInExp(expr)
105     val inititalAssignemnt = combine varList false
106   in
107     checker inititalAssignemnt expr
108   end
109   ;

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110
111
112 Control.Print.printDepth := 10;
113 Control.Print.printLength := 10;
114
115 (*TESTS*)
116 val expression1 = AND(OR(var("p"), var("q")), NOT(var("p")));
117 val assignment1 = [("p", false), ("q", true)];
118
119 (*Testing eval function - should return true*)
120 val expression1Eval = eval(assignment1, expression1);
121
122 (*Testing varsInExp function - should return true*)
123 val allVars = varsInExp(expression1);
124
125 (*Testing isTaut function*)
126 val expression2 = OR(var("p"), NOT(var("p")));
127 val isExprTaut = isTaut(expression2);
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