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1  (*Problem 3.1: A datatype declaration that can be used to represent
2  logical expressions *)
3
4  datatype expr = var of string | AND of expr * expr
5  | OR of expr * expr | NOT of expr;
6
7  (*Problem 3.2:
8  The assignment of truth values for propositional variables within a logical
9  expression can be represented as a list of tuples containing the name of the
10 variable and the truth assignment for it. Thus, this representation would have
11 type (string*bool) list. As an example, [("p", true), ("q", true)] is an
12 assignment list whereby the propositional variables p and q within some given
13 expression both have the value true.*)
14
15 (*Problem 3.3 A function that returns the truth value of a logical Expression E
16 and an assignment L of truth values for propositional variables. This function
17 makes use of a helper function truthValue that identifies the boolean value of
18 a specific propositional variable.*)
19
20 fun truthValue [] prop = false
21 | truthValue ((name, value)::rest) prop =
22   if name = prop then value else truthValue rest prop
23 ;
24
25 fun eval (List, (var x)) = truthValue List x
26 | eval (List, (AND(left, right))) =
27   if (eval (List, left)) = true then
28     if (eval (List, right)) = true then
29       true
30     else false
31   else false
32 | eval (List, (OR(left, right))) =
33   if (eval (List, left)) = false then
34     if (eval (List, right)) = false then
35       false
36     else true
37   else true
38 | eval (List, (NOT(value))) =
39   if (eval (List, value)) = true then
40     false
41   else true
42 ;
43
44 (*Problem 3.4 A function that takes a logical expression and returns a list of
45 all the propositional variables appearing in that list. *)
46
47 fun removeDups [] str = str::[]
48 | removeDups (head::rest) str =
49   if head = str then removeDups rest str else head::(removeDups rest str)
50 ;
51
52 fun varsInExp (expr) =
53   let

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54 fun helper (List, (var x)) = removeDups List x
55 | helper (List, (AND(left, right))) =
56   let val x = (helper (List, left))
57   in
58     (helper (x, right))
59   end
60 | helper (List, (OR(left, right))) =
61   let val x = (helper (List, left))
62   in
63     (helper (x, right))
64   end
65 | helper (List, (NOT(value))) =
66   (helper (List, value))
67 in
68   helper([], expr)
69 end;
70
71
72
73 (*Problem 3.5 A function that takes a logical expression as argument and
74 returns true if the expression is a tautology and false otherwise. Uses 2
75 helper functions: combine creates an assignment list from a list of propositional
76 variables, while flipValue changes the truth assignments for the variables in
77 the assignment list. Raises an END exception if no new truth assignments can
78 occur*)
79
80 exception END
81
82 fun flipValue [] = raise END
83 | flipValue ((name, value)::rest) =
84   if value = false then (name, true)::rest else (name, value)::(flipValue rest)
85 ;
86
87 (*Function initially sets all assignments to false*)
88 fun combine [] value = []
89 | combine (head::rest) value =
90   (head, value)::(combine rest value)
91 ;
92
93 fun isTaut (expr) =
94   let
95     fun flipValue2 assign = (flipValue assign) handle END => [("END", false)]
96     fun checker L E =
97       if eval(L, E) = true then
98         let val newL = flipValue2 L
99         in
100           if newL = [("END", false)] then true else checker newL E
101         end
102       else false
103     val varList = varsInExp(expr)
104     val inititalAssignemnt = combine varList false
105   in
106     checker inititalAssignemnt expr
107   end
108 ;
109

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110
111 Control.Print.printDepth := 10;
112 Control.Print.printLength := 10;
113
114 (*TESTS*)
115 val expression1 = AND(OR(var("p"), var("q")),NOT(var("p")));
116 val assignment1 = [("p", false), ("q", true)];
117
118 (*Testing eval function - should return true*)
119 val expression1Eval = eval(assignment1, expression1);
120
121 (*Testing varsInExp function - should return true*)
122 val allVars = varsInExp(expression1);
123
124 (*Testing isTaut function*)
125 val expression2 = OR(var("p"), NOT(var("p")));
126 val isExprTaut = isTaut(expression2);
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