

# ASSIGNMENT-9

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Download all python codes from

<https://github.com/behappy0604/Summer-Internship-IITH/tree/main/Assignment-9>

and latex-tikz codes from

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## 1 QUESTION No. 8.1

Let  $U$  and  $V$  be two independent zero mean Gaussian random variables of variances  $\frac{1}{4}$  and  $\frac{1}{9}$  respectively. The probability  $P(3V \geq 2U)$  is

- 1)  $\frac{4}{9}$       2)  $\frac{1}{2}$       3)  $\frac{2}{3}$       4)  $\frac{5}{9}$

## 2 SOLUTION

Since  $U$  and  $V$  are given to be normal random variables, therefore their difference will also be a normal random variable.

Here, let

$$X = 3V - 2U \quad (2.0.1)$$

where  $X$  is also a normal random variable with mean given as

$$X_M = 0 \quad (2.0.2)$$

and variance

$$X_{Vr} = \frac{1}{n} \sum_n^N (X_M - x_n)^2 = 2 \quad (2.0.3)$$

**Lemma 2.1.** *The area under the Gaussian PDF curve below and above the mean value is  $\frac{1}{2}$*

$$\Rightarrow P(X \geq X_M) = \frac{1}{2} \quad (2.0.4)$$

*The area under the curve and the x-axis is unity.*

So it will be symmetric about mean that is 0.

$$\therefore P(X \geq 0) = \boxed{\frac{1}{2}} \text{ (by symmetry property)} \quad (2.0.5)$$

Cumulative density function of the curve

$$CDF = \int_{-\infty}^x f(t) dt = \frac{1}{2} \quad (2.0.6)$$

Q-function

$$Q(X) = 1 - CDF = 1 - \frac{1}{2} = \frac{1}{2} \quad (2.0.7)$$

Hence option (b) is correct.