

Instance generation

We consider problem instances with $m = \{2, 3, 4\}$ technicians, each assigned to graphs with $|\mathcal{N}_0| = \{10, 15, 20\}$ nodes. Node coordinates are based on two instance types, corresponding to the R and C classes of Solomon’s dataset, with nodes selected and ordered as they appear in the original datasets. We vary the technician shift duration L , referred to as *short*, *medium*, and *long* to yield a total of 54 problem instances. Through all problem instances, we set α and ψ to 1 and β to 2. We consider three service categories, $\mathcal{P} = \{1, 2, 3\}$, where each category is characterized by a minimum and maximum amount of service time that a technician spends to repair the failure, denoted by Lb_{q_i} , Ub_{q_i} , respectively. Each customer’s service category, q_i , is uniformly drawn from \mathcal{P} . The service time for each customer is stochastic and follows a discrete triangular distribution $\Psi_{q_i}^i$. We develop the following procedure to determine $\Psi_{q_i}^i$. We assume that the support set for each customer consists of three points, including Lb_{q_i} , Ub_{q_i} . To determine the third point, we first divide the interval $[Lb_{q_i}, Ub_{q_i}]$ into three identical subintervals, and the third point is sampled uniformly from the middle subinterval. The discrete triangular distribution corresponding to customer i is characterized by three parameters: the minimum value e_i , the mode M_i , and the maximum value l_i . To prevent zero probabilities for support points, we set $e_i = Lb_{q_i} - \lambda$, and $l_i = Ub_{q_i} + \lambda$ where λ is given. To generate more skewed instances based on the values of the supports (probabilities), we construct three discrete triangular distribution families, including *symmetric*, *positive-skewed*, and *negative-skewed*. These families are distinguished by the position of the mode, M_i . Let $M_i = e_i + \sigma(l_i - e_i)$, where σ is a parameter that specifies the proportion by which the mode deviates from the minimum value e_i . For the symmetric, positive-skewed, and negative-skewed distributions, the value of σ must satisfy $\sigma = 0, 0 \leq \sigma \leq 0.5$, and $0.5 \leq \sigma \leq 1$, respectively. In our settings, we set λ to 40 for all families, and we set σ to 0.1 for positive-skewed and σ to 0.9 for negative-skewed distributions. The skew type of the triangular distribution for each customer is determined randomly. The expected service time \bar{d}^i is derived from the distribution $\Psi_{q_i}^i$. Table 1 presents the discrete triangular distribution function for customers. For problem instances with the same number of nodes $|\mathcal{N}_0|$, we randomly generate 50 realizations of service times according to the discrete triangular distributions (a total of $3 \times 50 = 150$ realizations). All distributions and realizations are generated using Python 3.13, with the random seed set to 12345 to ensure reproducibility.

To establish the shift duration L , we propose a model called LOPT. The LOPT is a multi-traveling salesman problem and consists of finding routes for all m technicians, who all start and end at the depot, such that each customer node is visited and served exactly once by one technician and the total travel and service times are minimized. For each problem instance with m and $|\mathcal{N}_0|$, the LOPT with expected customer service times is solved, then the average route duration per technician is multiplied by factors of 0.75, 1, and 1.25. The resulting shift duration limits are referred to as *short*, *medium*, and *long*, respectively.

The LOPT model is formulated as follows:

$$\min \sum_{v \in \mathcal{V}} \sum_{i \in \mathcal{N}_0} \sum_{j \in \mathcal{N}_0} \left(\frac{c_{ij}}{\psi} + d_j \right) x_{ijv} \quad (1)$$

subject to:

$$\sum_{i \in \mathcal{N}_0} \sum_{v \in \mathcal{V}} x_{ijv} = 1, \quad \forall j \in \mathcal{N} \quad (2)$$

$$\sum_{j \in \mathcal{N}} x_{0jv} = 1, \forall v \in \mathcal{V} \quad (3)$$

$$\sum_{i \in \mathcal{N}_0} x_{ilv} - \sum_{j \in \mathcal{N}_0} x_{ljev} = 0, \quad \forall l \in \mathcal{N}_0, \forall v \in \mathcal{V} \quad (4)$$

$$u_i - u_j + |\mathcal{N}_0| \sum_{v \in \mathcal{V}} x_{ijv} \leq |\mathcal{N}_0| - 1, \quad \forall i, j \in \mathcal{N}, i \neq j \quad (5)$$

$$u_i \geq 0, \quad \forall i \in \mathcal{N}_0 \quad (6)$$

$$x_{ijv} \in \{0, 1\}, \quad \forall i, j \in \mathcal{N}_0, \forall v \in \mathcal{V} \quad (7)$$

Table 1: Discrete triangular probability distributions of customers

Customer	Skewness	Mode	Expected	Support			Probability		
				1	2	3	1	2	3
1	Symmetric	105	116.6	30	126.5	180	0.23	0.54	0.23
2	Negative	111	85.1	30	69.5	120	0.18	0.36	0.45
3	Positive	51	92.3	30	112.9	240	0.42	0.47	0.11
4	Symmetric	75	70.7	30	66.1	120	0.26	0.49	0.26
5	Symmetric	105	107.0	30	108.4	180	0.21	0.58	0.21
6	Positive	39	64.1	30	77.9	120	0.45	0.37	0.18
7	Symmetric	105	117.4	30	128.2	180	0.23	0.53	0.23
8	Negative	111	88.4	30	79.6	120	0.18	0.39	0.43
9	Symmetric	75	78.7	30	82.5	120	0.25	0.49	0.25
10	Positive	45	84.2	30	112.7	180	0.46	0.39	0.15
11	Symmetric	105	112.0	30	117.4	180	0.22	0.56	0.22
12	Positive	39	67.1	30	88.8	120	0.47	0.34	0.19
13	Symmetric	105	92.0	30	80.4	180	0.23	0.53	0.23
14	Symmetric	105	94.3	30	85.3	180	0.23	0.54	0.23
15	Negative	219	165.3	30	120.9	240	0.12	0.41	0.47
16	Negative	111	88.4	30	79.7	120	0.18	0.39	0.43
17	Positive	51	106.6	30	156.7	240	0.48	0.39	0.13
18	Negative	165	135.0	30	123.6	180	0.13	0.44	0.42
19	Negative	165	136.9	30	128.2	180	0.13	0.45	0.42