



**Exercise
8**

DETERMINATION OF VISCOSITY OF FLUID BY STOKES' LAW

Measurement procedure

1. List of equipment

- Cylindrical tank with examined fluid
- Aerometer
- Set of balls
- Scales
- Micrometric screw
- Ruler with millimeter scale
- Stopwatch
- Höppler Viscometer

2. Goals

- Observation of bodies' falling motion in a continuous medium.
- Determination of fluid viscosity.

3. Measurement setup

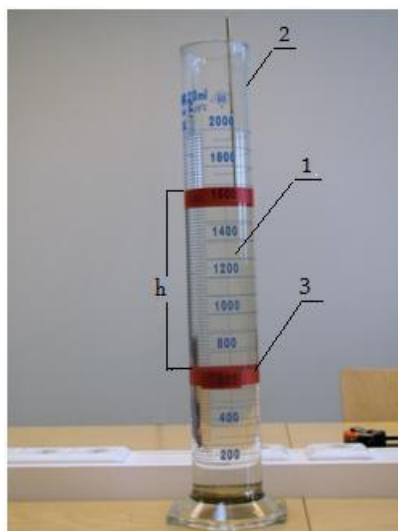


Fig.1. Device for measurement fluid viscosity by using Stokes' method:

- 1 – fluid
- 2 – glass cylinder
- 3 – rings
- h – distance between rings

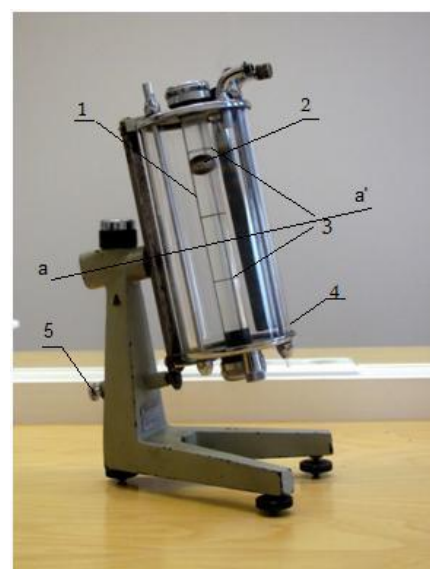


Fig.2. Höppler's viscometer:

- 1 – tube
- 2 – ball
- 3 – markers, between which the time of falling ball is measured
- 4 – thermostatic shield
- 5 – blocking device

4. Measurements

Wide cylindrical glass tank

- Perform measurements for a few balls, check first if they sink.
- Thoroughly clean every ball, then weigh each of them.
- Measure the diameter of each ball by a micrometric screw; the diameter ought to be measured at least 10 times in different directions.
- Use a ruler to measure the distance h between the rings on cylinder; upper ring should be at least 6 cm below fluid surface; the distance between rings is equal to path h travelled by balls with constant speed.
- Measure the time t of each ball falling over the distance h at least 10 times. Balls should be dropped right above the fluid surface, near to the cylinder axis.
- Measure the fluid density ρ_c by using an aerometer.

Höppler's viscometer

Do not dismantle the viscometer!!!

Do not insert anything into the viscometer!!!

- Level the viscometer.
- Assume the ball temperature as the ambient temperature; measure the time of the fall between markers for at least six times.
- Perform measurement by releasing the blocking device and rotating the tube with thermostatic shield by 180 degrees.

5. Results analysis

a) for a wide cylinder:

- Calculate the mean diameter \bar{d} of each ball and the measurement uncertainty $u(\bar{d})$.
- Calculate the mean falling time \bar{t} between rings for each ball and measurement uncertainties $u(\bar{t})$.
- Calculate each ball density ρ_k using formula (1) and their uncertainty $u_c(\rho_k)$.

$$\rho_k = \frac{6m}{\pi \cdot d^3} \quad (1)$$

- Calculate the fluid viscosity η using the formula below and its uncertainty $u_c(\eta)$.

$$\eta = \frac{d^2 \cdot g \cdot t \cdot (\rho_k - \rho_c)}{18h} \quad (2)$$

- Calculate the mean viscosity $\bar{\eta}$ for all measurements.
- Calculate the uncertainty of viscosity $u(\bar{\eta})$ (using standard deviation).

b) for Höppler viscometer

- Calculate the mean time of falling \bar{t} and its uncertainty $u(\bar{t})$.
- Calculate the fluid viscosity at room temperature and its uncertainty, using the formula:

$$\eta = k \cdot (\rho_k - \rho_c) \cdot t \quad (3)$$

Data required for calculations

- for the viscometer with **glass** ball
 $k = 0,7941 \cdot 10^{-6} \text{ m}^2/\text{s}^2$

- for the viscometer with **metal** ball:
 $k = 0,1216 \cdot 10^{-6} \text{ m}^2/\text{s}^2$

$$\rho_k = (2,41 \pm 0,01) \text{ g/cm}^3$$

$$\rho_c = (1,261 \pm 0,005) \text{ g/cm}^3$$

$$\rho_k = (8,12 \pm 0,01) \text{ g/cm}^3$$

$$\rho_c = (1,261 \pm 0,005) \text{ g/cm}^3$$

6. Additional information

The time of student reaction while turning the stopwatch on and off should be accounted for while calculating the time uncertainty $u(t)$.

7. Proposed tables (to be confirmed by teacher)

Table 1. Measurements of balls' parameters and times of falling with calculated viscosity.

| Ordinal | m 10 ⁻³ [kg] | d 10 ⁻³ [m] | h [m] | t [s] | ρ_k [kg/m ³] | ρ_c [kg/m ³] | η [Ns/m ²] |
|------------|------------------------------|-----------------------------|------------|------------|----------------------------------|----------------------------------|--------------------------------|
| 1 | | | | | | | |
| 2 | | | | | | | |
| 3 | | | | | | | |
| ⋮ | | | | | | | |
| n | | | | | | | |
| | | | | | | | |
| \bar{X} | | | | | | | |
| ΔX | | | | | | | |
| $u(X)$ | | | | | | | |
| $u_c(X)$ | | | | | | | |

$$\bar{\eta} = \quad u(\bar{\eta}) =$$

Table 2. Measurements of parameters and times of falling with calculated viscosity measured on Höppler viscometer.

| Ordinal | t [s] | k [m ² /s ²] | ρ_k [kg/m ³] | ρ_c [kg/m ³] | η [Ns/m ²] |
|------------|------------|--|----------------------------------|----------------------------------|--------------------------------|
| 1 | | | | | |
| 2 | | | | | |
| 3 | | | | | |
| ... | | | | | |
| n | | | | | |
| | | | | | |
| \bar{X} | | | | | |
| ΔX | | | | | |
| $u(X)$ | | | | | |
| $u_c(X)$ | | | | | |