Choco3 Documentation

Release 3.2.1

Charles Prud'homme, Jean-Guillaume Fages, Xavier Lorca

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Contents

Warning: This is a work-in-progress documentation. If you have any questions, suggestions or requests, please send an email to choco@mines-nantes.fr.

Part I

Preliminaries

CHAPTER 1

Main concepts

1.1 What is Constraint Programming?

Such a paradigm takes its features from various domains (Operational Research, Artificial Intelligence, etc). Constraint programming is now part of the portfolio of global solutions for processing real combinatorial problems. Actually, this technique provides tools to deal with a wide range of combinatorial problems. These tools are designed to allow non-specialists to address strategic as well as operational problems, which include problems in planning, scheduling, logistics, financial analysis or bio-informatics. Constraint programming differs from other methods of Operational Research by how it is implemented. Usually, the algorithms must be adapted to the specifications of the problem addressed. This is not the case in Constraint Programming where the problem addressed is described using the tools available in the library. The exercise consists in choosing carefully what constraints combine to properly express the problem, while taking advantage of the benefits they offer in terms of efficiency.

[wikipedia]

1.2 What is Choco ?

Choco is a Free and Open-Source Software [1] dedicated to Constraint Programming. It aims at describing real combinatorial problems in the form of Constraint Satisfaction Problems and to solve them with Constraint Programming techniques.

Choco is used for:

- teaching (a user-oriented constraint solver with open-source code)
- research (state-of-the-art algorithms and techniques, user-defined constraints, domains and variables)
- real-life applications (an efficient, reliable and free software with a support team)

Choco is easy to manipulate, that's why it is widely used for teaching. And Choco is also efficient, and we are proud to count industrial users too.

Choco is developed with Intellij IDEA and JProfiler.

Choco is one of the few Java libraries for constraint programming. The first version dates from the early 2000s, Choco is one of the forerunners among the free solvers - Choco written under BSD license. Maintenance and development tools are provided by the members of INRIA TASC team, especially by Charles Prud'homme and Jean-Guillaume Fages [2]. The latest version is Choco 3.2.

[1] Choco is distributed under BSD license (Copyright(c) 1999-2014, Ecole des Mines de Nantes).
[2] A complete list of contributors can be found on the website of Choco, team page.

Choco 3.2 is not the continuation of Choco2, but a completely rewritten version and there is no backward compatibility. The source code of choco-solver-3.2.1 is hosted on **GitHub** (https://github.com/chocoteam/choco3). Complementary information can be found on the webiste of Choco: http://www.choco-solver.org. Choco 3.2 comes with:

- various type of variables (integer, boolean, set and real),
- various state-of-the-art constraints (alldifferent, count, nvalues, etc.),
- various search strategies, from basic ones (first_fail, smallest, etc.) to most complex (impact-based and activity-based search),
- explanation-based engine, that enables conflict-based back jumping, dynamic backtracking and path repair,

But also, a FlatZinc parser, facilities to interact with the search loop, factories to help modeling, many samples, Choco-Ibex interface, etc.

An overview of the features of Choco 3.2 can be found in the presentation made in the "CP Solvers: Modeling, Applications, Integration, and Standardization" workshop of CP2013.

A forum is available on the website of Choco. A support mailing list is also available: choco3-support@mines-nantes.fr.

1.3 How to cite Choco ?

A reference to this manual, or more globally to Choco 3.2, is made like this:

```
@manual{
  author        = {Charles Prud'homme, Jean-Guillaume Fages, Xavier Lorca},
  title         = {Choco3 Documentation},
  year          = {2014},
  organization  = {TASC, INRIA Rennes, LINA CNRS UMR 6241},
  timestamp     = {Thu, 02 Oct 2014},
  url           = {http://www.choco-solver.org },
}
```

1.4 Who contribute to Choco ?

Core developers	Charles Prud'homme and Jean-Guillaume Fages.
Main contributors	Xavier Lorca, Narendra Jussien, Fabien Hermenier, Jimmy Liang.
Previous versions contributors	François Laburthe, Hadrien Cambazard, Guillaume Rochart, Arnaud Malapert, Sophie Demassey, Nicolas Beldiceanu, Julien Menana, Guillaume Richaud, Thierry Petit, Julien Vion, Stéphane Zampelli.

If you want to contribute, let us know.

CHAPTER 2

Getting started

2.1 Installing Choco 3.2

Choco 3.2 is a java library based on Java 7. The main library is named `choco-solver` and can be seen as the core library. Some extensions are also provided, such as `choco-parsers` or `choco-cpviz`, and rely on but not include `choco-solver`.

2.1.1 Which jar to select ?

We provide a zip file which contains the following files:

- choco-solver-3.2.1.jar

An ready-to-use jar file ; it provides tools to declare a Solver, the variables, the constraints, the search strategies, etc. In a few words, it enables modeling and solving CP problems.

- choco-solver-3.2.1-sources.jar

The source of the core library.

- choco-samples-3.2.1-sources.jar

The source of the artifact *choco-samples* made of problems modeled with Choco. It is a good start point to see what it is possible to do with Choco.

- apidocs-3.2.1.zip

Javadoc of Choco-3.2.1

Extensions

There are also official extensions, thus maintained by the Choco team. They are provided apart from the zip file. The available extensions are: *choco-parsers*, *choco-gui*, *choco-cpviz*, *choco-graph*, *choco-geost*, *choco-exppar*, *choco-eps*.

Note: Each of those extensions include all dependencies but choco-solver classes, which ease their usage.

To start using Choco 3.2, you need to be make sure that the right version of java is installed. Then you can simply add the `choco-solver` jar file (and extension libraries) to your classpath or declare them as dependency of a Maven-based project.

2.1.2 Update the classpath

Simply add the jar file to the classpath of your project (in a terminal or in your favorite IDE).

```
java -cp .:choco-solver-3.2.1.jar my.project.Main
```

2.1.3 As a Maven Dependency

Choco is build and managed using Maven3. To declare Choco as a dependency of your project, simply update the `pom.xml` of your project by adding the following instruction:

```
<dependency>
 <groupId>choco</groupId>
 <artifactId>choco-solver</artifactId>
 <version>X.Y.Z</version>
</dependency>
```

where `X.Y.Z` is replaced by 3.2.1.

You need to add a new repository to the list of declared ones in the `pom.xml` of your project:

```
<repository>
  <id>choco.repos</id>
  <url>http://www.emn.fr/z-info/choco-repo/mvn/repository/</url>
</repository>
```

2.1.4 Compiling sources

As a Maven-based project, Choco can be installed in a few instructions. Once you have downloaded the source (from the zip file or GitHub, simply run the following command:

```
mvn clean install -DskipTests
```

This instruction downloads the dependencies required for Choco3 (such as the trove4j and logback) then compiles the sources. The instruction `-DskipTests` avoids running the tests after compilation (and saves you a couple of hours). Regression tests are run on a private continuous integration server.

Maven provides commands to generate files needed for an IDE project setup. For example, to create the project files for your favorite IDE:

IntelliJ Idea

```
mvn idea:idea
```

Eclipse

```
mvn eclipse:eclipse
```

2.1.5 Note about logging

Choco 3.2 is not a stand-alone application but a library likely to be embedded in an application. In order to avoid imposing a logging framework on end-user, Choco 3.2 relies on SLF4J for the logging system.

> "SLF4J is a simple facade for logging systems allowing the end-user to plug-in the desired logging system at deployment time." – http://www.slf4j.org/faq.html

SLF4J is only a facade, meaning that it does not provide a complete logging solution, and a logging framework must be bound. Otherwise, you'll get the following error:

```
SLF4J: Failed to load class "org.slf4j.impl.StaticLoggerBinder".
SLF4J: Defaulting to no-operation (NOP) logger implementation
SLF4J: See http://www.slf4j.org/codes.html#StaticLoggerBinder for further details.
```

Choco is developed using Logback, but other framework are available such as log4j (a exhaustive list is given on SL4J). Declaring a logging framework is as simple as adding jar files to the classpath of your application:

Command-line

For logback:

```
java \
-cp .:choco-solver-3.2.1.jar:logback-core-1.0.13.jar:logback-classic-1.0.13.jar \
my.project.Main
```

Note: Logback relies on property file, namely *logback.xml*, provided in the zip file. Where should the configuration files such as logback.groovy, logback-test.xml or logback.xml be located on the classpath?

For log4j:

```
java -cp .:choco-solver-3.2.1.jar:slf4j-log4j12-1.7.7.jar my.project.Main
```

Maven

For logback:

```
<dependency>
  <groupId>ch.qos.logback</groupId>
  <artifactId>logback-classic</artifactId>
  <version>1.0.13</version>
</dependency>
```

For log4j:

```
<dependency>
  <groupId>org.slf4j</groupId>
  <artifactId>slf4j-log4j12</artifactId>
  <version>1.7.7</version>
</dependency>
```

More details can be found on http://www.slf4j.org/manual.html.

2.2 Overview of Choco 3.2

The following steps should be enough to start using Choco 3.2. The minimal problem should at least contains a solver, some variables and constraints to linked them together.

To facilitate the modeling, Choco 3.2 provides factories for almost every required component of CSP and its resolution:

Factory	Shortcut	Enables to create
`VariableFactory`	VF	Variables and views (integer, boolean, set and real)
`IntConstraintFactory`	ICF	Constraints over integer variables
`SetConstraintFactory`	SCF	Constraints over set variables
`LogicalConstraintFactory`	LCF	(Manages constraint reification)
`IntStrategyFactory`	ISF	Custom or black-box search strategies
`SetStrategyFactory`	SSF	
`SearchMonitorFactory`	SMF	log, resolution limits, restarts etc.

Note that, in order to have a concise and readable model, factories have shortcut names. Furthermore, they can be imported in a static way:

```
import static solver.search.strategy.ISF.*;
```

Let say we want to model and solve the following equation: $x + y < 5$, where the $x \in [\![0, 5]\!]$ and $y \in [\![0, 5]\!]$. Here is a short example which illustrates the main steps of a CSP modeling and resolution with Choco 3.2 to treat this equation.

```
1         // 1. Create a Solver
2         Solver solver = new Solver("my first problem");
3         // 2. Create variables through the variable factory
4         IntVar x = VariableFactory.bounded("X", 0, 5, solver);
5         IntVar y = VariableFactory.bounded("Y", 0, 5, solver);
6         // 3. Create and post constraints by using constraint factories
7         solver.post(IntConstraintFactory.arithm(x, "+", y, "<", 5));
8         // 4. Define the search strategy
9         solver.set(IntStrategyFactory.lexico_LB(new IntVar[]{x, y}));
10        // 5. Launch the resolution process
11        solver.findSolution();
```

One may notice that there is no distinction between model objects and solver objects. This makes easier for beginners to model and solve problems (reduction of concepts and terms to know) and for developers to implement their own constraints and strategies (short cutting process).

Don't be afraid to take a look at the sources, we think it is a good start point.

2.3 Choco 3.2 quick documentation

2.3.1 Solver

The `Solver` is a central object and must be created first: `Solver solver = new Solver();`.

[Solver]

2.3.2 Variables

The `VariableFactory` (`VF` for short) eases the creation of variables. Available variables are: `BoolVar`, `IntVar`, `SetVar`, `GraphVar` and `RealVar`. Note, that an `IntVar` domain can be bounded (only bounds are stored) or enumerated (all values are stored); a boolean variable is a 0-1 IntVar.

[Variables]

2.3.3 Views

A view is a variable whose domain is defined by a function over another variable domain. Available views are: `not`, `offset`, `eq`, `minus`, `scale` and `real`.

[Views]

2.3.4 Constants

Fixed-value integer variables should be created with the specific `VF.fixed(int, Solver)` function.

[Constants]

2.3.5 Constraints

Several constraint factories ease the creation of constraints: `LogicalConstraintFactory` (`LCF`), `IntConstraintFactory` (`ICF`), `SetConstraintsFactory` (`SCF`) and `GraphConstraintFactory` (`GCF`). `RealConstraint` is created with a call to new and to `addFunction` method. It requires the Ibex solver. Constraints hold once posted: `solver.post(c);`. Reified constraints should not be posted.

[Constraints]

2.3.6 Search

Defining a specific way to traverse the search space is made thanks to: `solver.set(AbstractStrategy)`. Predefined strategies are available in `IntStrategyFactory` (`ISF`), `SetStrategyFactory` and `GraphStrategyFactory`.

2.3.7 Large Neighborhood Search (LNS)

Various LNS (random, propagation-guided, etc.) can be created from the LNSFactory to improve performance on optimization problems.

2.3.8 Monitors

An `ISearchMonitor` is a callback which enables to react on some resolution events (failure, branching, restarts, solutions, etc.). `SearchMonitorFactory` (`SMF`) lists most useful monitors. User-defined monitors can be added with `solver.plugSearchMonitor(...)`.

2.3.9 Limits

A limit may be imposed on the search. The search stops once a limit is reached. Available limits are `SMF.limitTime(solver, 5000)`, `SMF.limitFail(solver, 100)`, etc.

2.3.10 Restarts

Restart policies may also be applied `SMF.geometrical(...)` and `SMF.luby(...)` are available.

2.3.11 Logging

Logging the search is possible. There are variants but the main way to do it is made through the `SMF.log(Solver, boolean, boolean)`. The first boolean indicates whether or not logging solutions, the second indicates whether or not logging search decisions. It also print, by default, main statistics of the search (time, nodes, fails, etc.)

2.3.12 Solving

Finding if a problem has a solution is made through a call to: `solver.findSolution()`. Looking for the next solution is made thanks to `nextSolution()`. `findAllSolutions()` enables to enumerate all solutions of a problem. To optimize an objective function, call `findOptimalSolution(...)`. Resolutions perform a Depth First Search.

2.3.13 Solutions

By default, the last solution is restored at the end of the search. Solutions can be accessed as they are discovered by using an `IMonitorSolution`.

2.3.14 Explanations

Choco natively supports explained constraints to reduce the search space and to give feedback to the user. Explanations are disabled by default.

Part II

Modelling problems

CHAPTER 3

The solver

The object `Solver` is the key component. It is built as following:

```
Solver solver = new Solver();
```

or:

```
Solver solver = new Solver("my problem");
```

This should be the first instruction, prior to any other modelling instructions. Indeed, a solver is needed to declare variables, and thus constraints.

Here is a list of the commonly used Solver API.

Note: The API related to resolution are not described here but detailed in *Solving*. Similarly, API provided to add a constraint to the solver are detailed in *Constraints*. The other missing methods are only useful for internal behavior.

3.1 Getters

3.1.1 Variables

Method	Definition
`Variable[] getVars()`	Return the array of variables declared in the solver. It includes all type of variables declared, integer, boolean, etc. but also *fixed* variables such as `Solver.ONE`.
`int getNbVars()`	Return the number of variables involved in the solver.
`Variable getVar(int i)`	Return the i^th variable declared in the solver.
`IntVar[] retrieveIntVars()`	Extract from the solver variables those which are integer (ie whose *KIND* is set to *INT*, that is, including *fixed* integer variables and boolean variables).
`retrieveBoolVars()`	Extract from the solver variables those which are boolean (ie whose *KIND* is set to *BOOL*, that is, including `Solver.ZERO` and `Solver.ONE`).
`SetVar[] retrieveSetVars()`	Extract from the solver variables those which are set (ie whose *KIND* is set to *SET*)
`RealVar[] retrieveRealVars()`	Extract from the solver variables those which are set (ie whose *KIND* is set to *REAL*)

3.1.2 Constraints

Method	Definition
`Constraint[] getCstrs()`	Return the array of constraints posted in the solver.
`getNbCstrs()`	Return the number of constraints posted in the solver.

3.1.3 Other

Method	Definition
`String getName()`	Return the name of the solver.
`IMeasures getMeasures()`	Return a reference to the measure recorder which stores resolution statistics.
`AbstractStrategy getStrategy()`	Return a reference to the declared search strategy.
`ISolutionRecorder getSolutionRecorder()`	Return the solution recorder.
`IEnvironment getEnvironment()`	Return the internal *environment* of the solver, essential to manage backtracking.
`ObjectiveManager getObjectiveManager()`	Return the objective manager of the solver, needed when an objective has to be optimized.
`ExplanationEngine getExplainer()`	Return the explanation engine declared, (default is *NONE*).
`IPropagationEngine getEngine()`	Return the propagation engine of the solver, which *orchestrate* the propagation of constraints.
`ISearchLoop getSearchLoop()`	Return the search loop of the solver, which guide the search process.

3.2 Setters

Method	Definition
`set(AbstractStrategy... strategies)`	Set a strategy to explore the search space. In case many strategies are given, they will be called in sequence.
`set(ISolutionRecorder sr)`	Set a solution recorder, and erase the previous declared one (by default, `LastSolutionRecorder` is declared, it only stores the last solution found.
`set(ISearchLoop searchLoop)`	Set the search loop to use during resolution. The default one is a binary search loop.
`set(IPropagationEngine propagationEngine)`	Set the propagation engine to use during resolution. The default one is `TwoBucketPropagationEngine`.
`set(ExplanationEngine explainer)`	Set the explanation engine to use during resolution. The default one is `ExplanationEngine` which does nothing.
`set(ObjectiveManager om)`	Set the objective manager to use during the resolution. *For advanced usage only*.

3.3 Others

Method	Definition
`void plugMonitor(ISearchMonitor sm)`	Put a *search monitor* to react on search events (solutions, decisions, fails, ...).
`Solver duplicateModel()`	Duplicate the model associates with a solver, ie only variables and constraints, and return a new solver.

CHAPTER 4

Declaring variables

4.1 Principle

A variable is an *unknown*, mathematically speaking. The goal of a resolution is to *assign* a *value* to each declared variable. In Constraint Programming, the *domain* –set of values that a variable can initially take– must be defined.

Choco 3.2 includes five types of variables: `IntVar`, `BoolVar`, `SetVar` and `RealVar`. A factory is available to ease the declaration of variables: `VariableFactory` (or `VF` for short). At least, a variable requires a name and a solver to be declared in. The name is only helpful for the user, to read the results computed.

4.2 Integer variable

An integer variable is based on domain made with integer values. There exists under three different forms: **bounded**, **enumerated** or **boolean**. An alternative is to declare variable-based views.

4.2.1 Bounded variable

Bounded (integer) variables take their value in $[\![a, b]\!]$ where a and b are integers such that $a < b$ (the case where $a = b$ is handled through views). Those variables are pretty light in memory (the domain requires two integers) but cannot represent holes in the domain.

To create a bounded variable, the `VariableFactory` should be used:

```
IntVar v = VariableFactory.bounded("v", 1, 12, solver);
```

To create an array of 5 bounded variables of initial domain $[\![-2, 8]\!]$:

```
IntVar[] vs = VariableFactory.boundedArray("vs", 5, -2, 8, solver);
```

To create a matrix of 5x6 bounded variables of initial domain $[\![0, 5]\!]$:

```
IntVar[][] vs = VariableFactory.boundedMatrix("vs", 5, 6, 0, 5, solver);
```

Note: When using bounded variables, branching decisions must either be domain splits or bound assignments/removals. Indeed, assigning a bounded variable to a value strictly comprised between its bounds may results in disastrous performances, because such branching decisions will not be refutable.

4.2.2 Enumerated variable

Integer variables with enumerated domains, or shortly, enumerated variables, take their value in $[\![a, b]\!]$ where a and b are integers such that $a < b$ (the case where $a = b$ is handled through views) or in an array of ordered values $a, b, c, .., z$, where $a < b < c... < z$. Enumerated variables provide more information than bounded variables but are heavier in memory (usually the domain requires a bitset).

To create an enumerated variable, the `VariableFactory` should be used:

```
IntVar v = VariableFactory.enumerated("v", 1, 12, solver);
```

which is equivalent to :

```
IntVar v = VariableFactory.enumerated("v", new int[]{1,2,3,4,5,6,7,8,9,10,11,12}, solver);
```

To create a variable with holes in its initial domain:

```
IntVar v = VariableFactory.enumerated("v", new int[]{1,7,8}, solver);
```

To create an array of 5 enumerated variables with same domains:

```
IntVar[] vs = VariableFactory.enumeratedArray("vs", 5, -2, 8, solver);
```

```
IntVar[] vs = VariableFactory.enumeratedArray("vs", 5, new int[]{-10, 0, 10}, solver);
```

To create a matrix of 5x6 enumerated variables with same domains:

```
IntVar[][] vs = VariableFactory.enumeratedMatrix("vs", 5, 6, 0, 5, solver);
```

```
IntVar[][] vs = VariableFactory.enumeratedMatrix("vs", 5, 6, new int[]{1,2,3,5,6,99}, solver);
```

Modelling: Bounded or Enumerated?

The choice of representation of the domain variables should not be done lightly. Not only the memory consumption should be considered but also the type of constraints used. Indeed, some constraints only update bounds of integer variables, using them with bounded variables is enough. Others make holes in variables' domain, using them with enumerated variables takes advantage of the *power* of the filtering algorithm. Most of the time, variables are associated with propagators of various *power*. The choice of domain representation must then be done on a case by case basis.

4.2.3 Boolean variable

Boolean variables, BoolVar, are specific `IntVar` which take their value in $[\![0, 1]\!]$.

To create a new boolean variable:

```
BoolVar b = VariableFactory.bool("b", solver);
```

To create an array of 5 boolean variables:

```
BoolVar[] bs = VariableFactory.boolArray("bs", 5, solver);
```

To create a matrix of 5x6 boolean variables:

```
BoolVar[] bs = VariableFactory.boolMatrix("bs", 5, 6, solver);
```

4.3 Constants

Fixed-value integer variables should be created with a call to the following functions:

```
VariableFactory.fixed("seven", 7, solver);
```

Or:

```
VariableFactory.fixed(8, Solver)
```

where 7 and 8 are the constant values. Not specifying a name to a constant enables the solver to use *cache* and avoid multiple occurrence of the same object in memory.

4.4 Variable views

Views are particular integer variables, they can be used inside constraints. Their domains are implicitly defined by a function and implied variables.

`x` is a constant :

```
IntVar x = VariableFactory.fixed(1, solver);
```

`x = y + 2`:

```
IntVar x = VariableFactory.offset(y, 2);
```

`x = -y`:

```
IntVar x = VariableFactory.minus(y);
```

`x = 3*y`:

```
IntVar x = VariableFactory.scale(y, 3);
```

Views can be combined together:

```
IntVar x = VariableFactory.offset(VariableFactory.scale(y,2),5);
```

4.5 Set variable

A set variable `SV` represents a set of integers. Its domain is defined by a set interval: `[S_E,S_K]`

- the envelope `S_E` is an `ISet` object which contains integers that potentially figure in at least one solution,
- the kernel `S_K` is an `ISet` object which contains integers that figure in every solutions.

Initial values for both `S_K` and `S_E` can be specified. If no initial value is given for `S_K`, it is empty by default. Then, decisions and filtering algorithms will remove integers from `S_E` and add some others to `S_K`. A set variable is instantiated if and only if `S_E = S_K`.

A set variable can be created as follows:

```
// z initial domain
int[] z_envelope = new int[]{2,1,3,5,7,12};
int[] z_kernel = new int[]{2};
z = VariableFactory.set("z", z_envelope, z_kernel, solver);
```

4.6 Real variable

Real variables have a specific status in Choco 3.2. Indeed, continuous variables and constraints are managed with Ibex solver.

A real variable is declared with two doubles which defined its bound:

```
RealVar x = VariableFactory.real("y", 0.2d, 1.0e8d, 0.001d, solver);
```

Or a real variable can be declared on the basis of on integer variable:

```
IntVar ivar = VariableFactory.bounded("i", 0, 4, solver);
RealVar x = VariableFactory.real(ivar, 0.01d);
```

CHAPTER 5

Constraints and propagators

5.1 Principle

A constraint is a logic formula that defines allowed combinations of values for its variables, that is, restrictions over variables that must be respected in order to get a feasible solution. A constraint is equipped with a (set of) filtering algorithm(s), named *propagator(s)*. A propagator **removes**, from the domains of the targeted variables, values that cannot correspond to a valid combination of values. A solution of a problem is an assignment of all its variables simultaneously verifying all the constraints.

Constraint can be declared in *extension*, by defining the valid/invalid tuples, or in *intension*, by defining a relation between the variables. Choco 3.2 provides various factories to declare constraints (see *Overview* to have a list of available factories). A list of constraints available through factories is given in *List of available constraints*.

Modelling: Selecting the right constraints

Constraints, through propagators, suppress forbidden values of the domain of the variables. For a given paradigm, there can be several propagators available. A widely used example is the *AllDifferent* constraints which holds that all its variables should take a distinct value in a solution. Such a rule can be formulated :

- using a clique of inequality constraints,
- using a global constraint: either analysing bounds of variable (*Bound consistency*) or analysing all values of the variables (*Arc consistency*),
- or using a table constraint –an extension constraint which list the valid tuples.

The choice must be made by not only considering the gain in expressiveness of stress compared to others. Indeed, the effective yield of each option can be radically different as the efficiency in terms of computation time.

Many global constraints are used to model problems that are inherently NP-complete. And only a partial domain filtering variables can be done through a polynomial algorithm. This is for example the case of *NValue* constraint that one aspect relates to the problem of "minimum hitting set." Finally, the *global* nature of this type of constraint also simplifies the work of the solver in that it provides all or part of the structure of the problem.

If we want an integer variable `sum` to be equal to the sum of values of variables in the set `atLeast`, we can use the `IntConstraintFactory.sum` constraint:

```
solver.post(IntConstraintFactory.sum(atLeast, sum));
```

A constraint may define its specific checker through the method `isSatisfied()`, but most of the time the checker is given by checking the entailment of each of its propagators. The satisfaction of the constraints' solver is done on each solution if assertions are enabled.

Note: One can enable assertions by adding the `-ea` instruction in the JVM arguments.

It can thus be slower if the checker is often called (which is not the case in general). The advantage of this framework is the economy of code (less constraints need to be implemented), the avoidance of useless redundancy when several constraints use the same propagators (for instance `IntegerChanneling` constraint involves `AllDifferent constraint`), which leads to better performances and an easier maintenance.

Note: To ease modelling, it is not required to manipulate propagators, but only constraints. However, one can define specific constraints by defining combinations of propagators and/or its own propagators. More detailed are given in *Defining its own constraint*.

Choco 3.2 provides various types of constraints.

5.1.1 Available constraints

FALSE, *TRUE*

On one integer variable

arithm, *member*, *not_member*.

On two integer variables

absolute, *arithm*, *distance*, *square*, *table*, *times*.

On three integer variables

arithm, *distance*, *eucl_div*, *maximum*, *minimum*, *mod*, *times*.

On an undefined number of integer variables

element, *sort*, *table*.

alldifferent, *alldifferent_conditionnal*, *alldifferent_except_0*, *global_cardinality*,

among, *atleast_nvalues*, *atmost_nvalues*, *count*, *nvalues*,

boolean_channeling, *inverse_channeling*.

cumulative, *diffn*.

lex_chain_less, *lex_chain_less_eq*, *lex_less*, *lex_less_eq*.

maximum, *minimum*,

scalar, *sum*.

cost_regular, *multicost_regular*, *regular*.

circuit, *path*, *subcircuit*, *subpath*, *tree*.

bin_packing, *knapsack*, *tsp*.

On one set variable

notEmpty.

On two set variables

disjoint, *offSet*.

On an undefined number of set variables

all_different, *all_disjoint*, *all_equal*, *bool_channel*, *intersection*, *inverse_set*, *member*, *nbEmpty*, *partition*, *subsetEq*, *symmetric*, *union*.

On integer and set variables

cardinality, *element*, *int_channel*, *max*, *member*, *min*, *sum*.

On real variables

Constraints over real variables.

5.2 Posting constraints

To be effective, a constraint must be posted to the solver. This is achieved using the method:

```
solver.post(Constraint cstr);
```

Otherwise, if the `solver.post(Constraint cstr)` method is not called, the constraint will not be taken into account during the resolution process : it may not be satisfied in all solutions.

Method	Definition
`void post(Constraint c)`	Post **permanently** a constraint in the constraint network defined by the solver. The constraint is not propagated on posting, but is added to the propagation engine.
`void post(Constraint... cs)`	Post **permanently** the constraints in the constraint network defined by the solver.
`void postTemp(Constraint c)`	Post a constraint **temporary** in the constraint network. The constraint will active on the current sub-tree and be removed upon backtrack.
`void unpost(Constraint c)`	Remove permanently the constraint from the constraint network

5.3 Reifying constraints

In Choco 3.2, it is possible to reify any constraint. Reifying a constraint means associating it with a `BoolVar` to represent whether the constraint holds or not:

```
BoolVar b = constraint.reify();
```

Or:

```
BoolVar b = VF.bool("b", solver);
constraint.reifyWith(b);
```

The first API `constraint.reify()` creates the variable, if it does not already exists, and reify the constraint. The second API `constraint.reifyWith(b)` reify the constraint with the given variable.

Note: A constraint is reified with only one boolean variable. If multiple reification are required, equality constraints will be created.

Reifying a constraint means that we allow the constraint not to be satisfied. Therefore, the constraint **should not** be posted.

The `LogicalConstraintFactory` enables to manipulate constraints through their reification. For instance, we can represent the constraint "either `x<0` or `y>42`" as the following:

```
Constraint a = IntConstraintFactory.arithm(x,"<",0);
Constraint b = IntConstraintFactory.arithm(y,">",42);
Constraint c = LogicalConstraintFactory.or(a,b);
solver.post(c);
```

This will actually reify both constraints `a` and `b` and say that at least one of the corresponding boolean variables must be true. Note that only the constraint `c` is posted.

5.4 SAT constraints

A SAT solver is embedded in Choco. It is not designed to be accessed directly. The SAT solver is internally managed as a constraint (and a propagator), that's why it is referred as SAT constraint in the following.

Important: The SAT solver is directly inspired by MiniSat[EenSorensson03]. However, it only propagates clauses, no learning or search is implemented.

On a call to any methods of `solver.constraints.SatFactory`, the SAT constraint (and propagator) is created and automatically posted to the solver.

5.4.1 How to add clauses

Clauses can be added with calls to the `solver.constraints.SatFactory`.

On one boolean variable

addTrue, *addFalse*.

On two boolean variables

addBoolEq, *addBoolLe*, *addBoolLt*, *addBoolNot*.

Reification on two boolean variables

addBoolIsEqVar, *addBoolIsLeVar*, *addBoolIsLtVar*, *addBoolIsNeqVar*, *addBoolOrEqVar*, *addBoolXorEqVar*, *addBoolAndEqVar*.

On undefined number of boolean variables

addBoolOrArrayEqualTrue, *addAtMostNMinusOne*, *addAtMostOne*, *addBoolAndArrayEqualFalse*, *addBoolAndArrayEqVar*, *addBoolOrArrayEqVar*, *addClauses*, *addMaxBoolArrayLessEqVar*, *addSumBoolArrayGreaterEqVar*, *addSumBoolArrayLessEqVar*.

Part III

Solving problems

CHAPTER 6

Finding solutions

Choco 3.2 provides different API, offered by `Solver`, to launch the problem resolution. Before everything, there are two methods which help interpreting the results.

Feasibility: Once the resolution ends, a call to the `solver.isFeasible()` method will return a boolean which indicates whether or not the problem is feasible.

- `true`: at least one solution has been found, the problem is proven to be feasible,
- `false`: in principle, the problem has no solution. More precisely, if the search space is guaranteed to be explored entirely, it is proven that the problem has no solution.

Limitation: When the resolution is limited (See *Limiting the resolution* for details and examples), one may guess if a limit has been reached. The `solver.hasReachedLimit()` method returns `true` if a limit has bypassed the search process, `false` if it has ended *naturally*.

Warning: In some cases, the search may not be complete. For instance, if one enables restart on each failure with a static search strategy, there is a possibility that the same sub-tree is explored permanently. In those cases, the search may never stop or the two above methods may not be sufficient to confirm the lack of solution.

6.1 Satisfaction problems

6.1.1 Finding a solution

A call to `solver.findSolution()` launches a resolution which stops on the first solution found, if any.

```
1         // 1. Create a Solver
2         Solver solver = new Solver("my first problem");
3         // 2. Create variables through the variable factory
4         IntVar x = VariableFactory.bounded("X", 0, 5, solver);
5         IntVar y = VariableFactory.bounded("Y", 0, 5, solver);
6         // 3. Create and post constraints by using constraint factories
7         solver.post(IntConstraintFactory.arithm(x, "+", y, "<", 5));
8         // 4. Define the search strategy
9         solver.set(IntStrategyFactory.lexico_LB(new IntVar[]{x, y}));
10        // 5. Launch the resolution process
11        solver.findSolution();
```

If a solution has been found, the resolution process stops on that solution, thus each variable is instantiated to a value, and the method returns `true`.

If the method returns `false`, two cases must be considered:

- A limit has been reached. There may be a solution, but the solver has not been able to find it in the given limit or there is no solution but the solver has not been able to prove it (i.e., to close to search tree) in the given limit. The resolution process stops in no particular place in the search tree and the resolution can be run again.
- No limit has been declared. The problem has no solution, the complete exploration of the search tree proved it.

To ensure the problem has no solution, one may call `solver.hasReachedLimit()`. It returns `true` if a limit has been reached, `false` otherwise.

6.1.2 Enumerating solutions

Once the resolution has been started by a call to `solver.findSolution()` and if the problem is feasible, the resolution can be resumed using `solver.nextSolution()` from the last solution found. The method returns `true` if a new solution is found, `false` otherwise (a call to `solver.hasReachedLimit()` must confirm the lack of new solution). If a solution has been found, alike `solver.findSolution()`, the resolution stops on this solution, each variable is instantiated, and the resolution can be resumed again until there is no more new solution.

One may enumerate all solution like this:

```
if(solver.findSolution()){
   do{
       // do something, e.g. print out variables' value
   }while(solver.nextSolution());
}
```

`solver.findSolution()` and `solver.nextSolution()` are the only ways to resume a resolution process which has already began.

Tip: On a solution, one can get the value assigned to each variable by calling

```
ivar.getValue(); // instantiation value of an IntVar, return a int
svar.getValues(); // instantiation values of a SerVar, return a int[]
rvar.getLB(); // lower bound of a RealVar, return a double
rvar.getUB(); // upper bound of a RealVar, return a double
```

An alternative is to call `solver.findAllSolutions()`. It attempts to find all solutions of the problem. It returns the number of solutions found (in the given limit if any).

6.2 Optimization problems

Choco 3.2 enables to solve optimization problems, that is, in which a variable must be optimized.

Tip: For functions, one should declare an objective variable and declare it as the result of the function:

```
// Function to maximize: 3X + 4Y
IntVar OBJ = VF.bounded("objective", 0, 999, solver);
solver.post(ICF.scalar(new IntVar[]{X,Y}, new int[]{3,4}, OBJ));
solver.findOptimalSolution(ResolutionPolicy.MAXIMIZE, OBJ);
```

6.2.1 Finding one optimal solution

Finding one optimal solution is made through a call to the `solver.findOptimalSolution(ResolutionPolicy, IntVar)` method. The first argument defines the kind of optimization required: minimization

(`ResolutionPolicy.MINIMIZE`) or maximization (`ResolutionPolicy.MAXIMIZE`). The second argument indicates the variable to optimize.

For instance:

```
solver.findOptimalSolution(ResolutionPolicy.MAXIMIZE, OBJ);
```

states that the variable `OBJ` must be maximized.

The method does not return any value. However, the best solution found so far is restored.

Important: Because the best solution is restored, all variables are instantiated after a call to `solver.findOptimalSolution(...)`.

The best solution found is the optimal one if the entire search space has been explored.

The process is the following: anytime a solution is found, the value of the objective variable is stored and a *cut* is posted. The cut is an additional constraint which states that the next solution must be strictly better than the current one, ie in minimization, strictly smaller.

6.2.2 Finding all optimal solutions

There could be more than one optimal solutions. To find them all, one can call `findAllOptimalSolutions(ResolutionPolicy, IntVar, boolean)`. The two first arguments defines the optimisation policy and the variable to optimize. The last argument states the way the solutions are computed. Set to `true` the resolution will be achieved in two steps: first finding and proving an optimal solution, then enumerating all solutions of optimal cost. Set to `false`, the posted cuts are *soft*. When an equivalent solution is found, it is stored and the resolution goes on. When a strictly better solution is found, previous solutions are removed. Setting the boolean to `false` allow finding non-optimal intermediary solutions, which may be time consuming.

6.3 Multi-objective optimization problems

6.3.1 Finding the pareto front

It is possible to solve a multi-objective optimization problems with Choco 3.2, using `solver.findParetoFront(ResolutionPolicy policy, IntVar... objectives)`.
The first argument define the resolution policy, which can be `Resolution.MINIMIZE` or `ResolutionPolicy.MAXIMIZE`. Then, the second argument defines the list of variables to optimize.

Note: All variables should respect the same resolution policy.

The underlying approach is naive, but it simplifies the process. Anytime a solution is found, a cut is posted which states that at least one of the objective variables must be better. Such as $(X_0 < b_0 \vee X_1 < b_1 \vee \ldots \vee X_n < b_n$ where X_i is the ith objective variable and b_i its best known value.

The method ends by restoring the last solution found so far, if any.

Here is a simple illustration:

```
1                a = VF.enumerated("a", 0, 2, solver);
2                b = VF.enumerated("b", 0, 2, solver);
3                c = VF.enumerated("c", 0, 2, solver);
4                solver.post(ICF.arithm(a, "+", b, "<", 3));
5                solver.findParetoFront(ResolutionPolicy.MAXIMIZE,a,b);
6                List<Solution> paretoFront = solver.getSolutionRecorder().getSolutions();
```

```
7                   System.out.println("The pareto front has "+paretoFront.size()+" solutions : ");
8                   for(Solution s:paretoFront){
9                           System.out.println("a = "+s.getIntVal(a)+" and b = "+s.getIntVal(b));
10                  }
```

6.4 Propagation

One may want to propagate each constraint manually. This can be achieved by calling `solver.propagate()`. This method runs, in turn, the domain reduction algorithms of the constraints until it reaches a fix point. It may throw a `ContradictionException` if a contradiction occurs. In that case, the propagation engine must be flushed calling `solver.getEngine().flush()` to ensure there is no pending events.

Warning: If there are still pending events in the propagation engine, the propagation may results in unexpected results.

CHAPTER 7

Recording solutions

Choco 3.2 requires each solution to be fully instantiated, i.e. every variable must be fixed. Otherwise, an exception will be thrown if assertions are turned on (when `-ea` is added to the JVM parameters). Choco 3.2 includes several ways to record solutions.

7.1 Solution storage

A solution is usually stored through a `Solution` object which maps every variable with its current value. Such an object can be erased to store new solutions.

7.2 Solution recording

7.2.1 Built-in solution recorders

A solution recorder (`ISolutionRecorder`) is an object in charge of recording variable values in solutions. There exists many built-in solution recorders:

`LastSolutionRecorder` only keeps variable values of the last solution found. It is the default solution recorder. Furthermore, it is possible to restore that solution after the search process ends. This is used by default when seeking an optimal solution.

`AllSolutionsRecorder` records all solutions that are found. As this may result in a memory explosion, it is not used by default.

`BestSolutionsRecorder` records all solutions but removes from the solution set each solution that is worse than the best solution value found so far. This may be used to enumerate all optimal (or at least, best) solutions of a problem.

`ParetoSolutionsRecorder` records all solutions of the pareto front of the multi-objective problem.

7.2.2 Custom recorder

You can build you own way of manipulating and recording solutions by either implementing your own `ISolutionRecorder` object or by simply using an `ISolutionMonitor`, as follows:

```
1                 solver.plugMonitor(new IMonitorSolution() {
2                         @Override
3                         public void onSolution() {
4                                 bestObj = nbValues.getValue();
```

```
5                                       System.out.println("Solution found! Objective = "+bestObj);
6                                   }
7                       });
```

7.3 Solution restoration

A `Solution` object can be restored, i.e. variables are fixed back to their values in that solution. For this purpose, we recommend to restore initial domains and then restore the solution, with the following code:

```
try{
   solver.getSearchLoop().restoreRootNode();
   solver.getEnvironment().worldPush();
   solution.restore();
}catch (ContradictionException e){
   throw new UnsupportedOperationException("restoring the solution ended in a failure");
}
solver.getEngine().flush();
```

Note that if initial domains are not restored, then the solution restoration may lead to a failure. This would happen when trying to restore out of the current domain.

CHAPTER 8

Search Strategies

8.1 Principle

The search space induces by variables' domain is equal to $S = |d_1| * |d_2| * ... * |d_n|$ where d_i is the domain of the i^{th} variable. Most of the time (not to say always), constraint propagation is not sufficient to build a solution, that is, to remove all values but one from (integer) variables' domain. Thus, the search space needs to be explored using one or more *search strategies*. A search strategy performs a performs a Depth First Search and reduces the search space by making *decisions*. A decision involves a variables, a value and an operator, for instance $x = 5$. Decisions are computed and applied until all the variables are instantiated, that is, a solution is found, or a failure has been detected.

> Choco|release| build a binary search tree: each decision can be refuted. When a decision has to be computed, the search strategy is called to provide one, for instance $x = 5$. The decision is then applied, the variable, the domain of `x` is reduced to `5`, and the decision is validated thanks to the propagation. If the application of the decision leads to a failure, the search backtracks and the decision is refuted ($x \neq 5$) and validated through propagation. Otherwise, if there is no more free variables then a solution has been found, else a new decision is computed.

Note: There are many ways to explore the search space and this steps should not be overlooked. Search strategies or heuristics have a strong impact on resolution performances. Thus, it is strongly recommended to adapt the search space exploration to the problem treated.

8.2 Zoom on IntStrategy

A search strategy `IntStrategy` is dedicated to `IntVar` only. It is based on a list of variables `scope`, a selector of variable `varSelector`, a value selector `valSelector` and an optional `decOperator`.

1. `scope`: array of variables to branch on.
2. `varSelector`: a variable selector, defines how to select the next variable to branch on.
3. `valSelector`: a value selector, defines how to select a value in the domain of the selected variable.
4. `decOperator`: a decision operator, defines how to modify the domain of the selected variable with the selected value.

On a call to `IntStrategy.getDecision()`, `varSelector` try to find, among `scope`, a variable not yet instantiated. If such a variable does not exist, the method returns `null`, saying that it can not compute decision anymore. Otherwise, `valSelector` selects a value, within the domain of the selected variable. A decision can then be computed with the selected variable and the selected value, and is returned to the caller.

By default, the decision built is an assignment: its application leads to an instantiation, its refutation, to a value removal. It is possible create other types of decision by defining a decision operator `DecisionOperator`.

API

IntStrategyFactory.custom(VariableSelector<IntVar> VAR_SELECTOR, IntValueSelector VAL_SELECTOR, DecisionOperator<IntVar> DEC_OPERATOR, IntVar... VARS)

IntStrategyFactory.custom(VariableSelector<IntVar> VAR_SELECTOR, IntValueSelector VAL_SELECTOR, IntVar... VARS)

new IntStrategy(IntVar[] scope, VariableSelector<IntVar> varSelector, IntValueSelector valSelector) new IntStrategy(IntVar[] scope, VariableSelector<IntVar> varSelector, IntValueSelector valSelector,

DecisionOperator<IntVar> decOperator)

Sometimes, on a call to the variable selector, several variables could be selected. In that case, the order induced by `VARS` is used to break tie: the variable with the smallest index is selected. However, it is possible to break tie with other `VAR_SELECTOR``s. They should be declared as parameters of ``VariablesSelectorWithTies`.

```
solver.set(ISF.custom(
    new VariableSelectorWithTies(new FirstFail(), new Random(123L)),
    new IntDomainMin(), vars);
```

The variable with the smallest domain is selected first. If there are more than one variable whose domain size is the smallest, ties are randomly broken.

Note: Only variable selectors which implement `VariableEvaluator` can be used to break ties.

Very similar operations are achieved in `SetStrategy` and `RealStrategy`.

See `solver.search.strategy.IntStrategyFactory` and `solver.search.strategy.SetStrategyFactory` for built-in strategies and selectors.

8.2.1 Available variable selectors

For integer variables

lexico_var_selector, *random_var_selector*, *minDomainSize_var_selector*, *maxDomainSize_var_selector*, *maxRegret_var_selector*.

For set variables

See `solver.search.strategy.selectors.variables.MaxDelta`, `solver.search.strategy.selectors.var`

For real variables

See `solver.search.strategy.selectors.variables.Cyclic`.

8.2.2 Available value selectors

For integer variables

min_value_selector, *mid_value_selector*, *max_value_selector*, *randomBound_value_selector*, *random_value_selector*.

For set variables

See `solver.search.strategy.selectors.values.SetDomainMin`.

For real variables

See `solver.search.strategy.selectors.values.RealDomainMiddle`.

8.2.3 Available decision operators

assign, *remove*, *split*, *reverse_split*.

8.2.4 Available strategies

For integer variables

custom, *sequencer*.

lexico_LB, *lexico_Neq_LB*, *lexico_Split*, *lexico_UB*, *minDom_LB*, *minDom_MidValue*, *maxDom_Split*, *minDom_UB*, *maxReg_LB*, *random_bound*, *random_value*.

domOverWDeg, *activity*, *impact*.

lastConflict.

generateAndTest.

For set variables

custom, *sequencer*.

force_first, *force_maxDelta_first*, *force_minDelta_first*, *remove_first*.

lastConflict.

Important: Black-box search strategies

There are many ways of choosing a variable and computing a decision on it. Designing specific search strategies can be a very tough task to do. The concept of *Black-box search heuristic* (or adaptive search strategy) has naturally emerged from this statement. Most common black-box search strategies observe aspects of the CSP resolution in order to drive the variable selection, and eventually the decision computation (presumably, a value assignment). Three main families of heuristic, stemming from the concepts of variable impact, conflict and variable activity, can be found in Chocolrelease|. Black-box strategies can be augmented with restarts.

8.3 Default search strategies

If no search strategy is specified in the model, Choco 3.2 will generate a default one. In many cases, this strategy will not be sufficient to produce satisfying performances and it will be necessary to specify a dedicated strategy, using `solver.set(...)`. The default search strategy distincts variables per types and defines a specific search strategy per each type:

1. integer variables (but boolean variables: `IntStrategyFactory.minDom_LB(ivars)`
2. boolean variables: `IntStrategyFactory.lexico_UB(bvars)`
3. set variables: `SetStrategyFactory.force_minDelta_first(svars)`
4. real variables `new RealStrategy(rvars, new Cyclic(), new RealDomainMiddle())`

Constants are excluded from search strategies' variable scope.

`IntStrategyFactory`, `SetStrategyFactory` and `GraphStrategyFactory` offer several built-in search strategies and a simple framework to build custom searches.

8.4 Composition of strategies

Most of the time, it is necessary to combine various strategies. A `StrategiesSequencer` enables to compose various `AbstractStrategy`. It is created on the basis of a list of `AbstractStrategy`. The current active strategy is called to compute a decision through its `getDecision()` method. When no more decision can be computed for the current strategy, the following one becomes active. The intersection of variables from each strategy does not have to be empty. When a variable appears in various strategy, it is ignored as soon as it is instantiated.

When no environment is given in parameter, the last active strategy is not stored, and strategies are evaluated in lexicographical order to find the first active one, based on its capacity to return a decision.

When an environment is given in parameter, the last active strategy is stored.

API

> IntStrategyFactory.sequencer(AbstractStrategy... strategies)
>
> new StrategiesSequencer(AbstractStrategy... strategies) new StrategiesSequencer(IEnvironment environment, AbstractStrategy... strategies)

Finally, one can create its own strategy, see *Defining its own search* for more details.

8.5 Restarts

Restart means stopping the current tree search, then starting a new tree search from the root node. Restarting makes sense only when coupled with randomized dynamic branching strategies ensuring that the same enumeration tree is not constructed twice. The branching strategies based on the past experience of the search, such as adaptive search strategies, are more accurate in combination with a restart approach.

Unless the number of allowed restarts is limited, a tree search with restarts is not complete anymore. It is a good strategy, though, when optimizing an NP-hard problem in a limited time.

Some adaptive search strategies resolutions are improved by sometimes restarting the search exploration from the root node. Thus, the statistics computed on the bottom of the tree search can be applied on the top of it.

There a two restart strategies available in `SearchMonitorFactory`:

```
geometrical(Solver solver, int base, double grow, ICounter counter, int limit)
```

It performs a search with restarts controlled by the resolution event [1] `counter` which counts events occurring during the search. Parameter `base` indicates the maximal number of events allowed in the first search tree. Once this limit is reached, a restart occurs and the search continues until `base ``*``grow` events are done, and so on. After each restart, the limit number of events is increased by the geometric factor `grow`. `limit` states the maximum number of restarts.

and:

```
luby(Solver solver, int base, int grow, ICounter counter, int limit)
```

The Luby 's restart policy is an alternative to the geometric restart policy. It performs a search with restarts controlled by the number of resolution events [1] counted by `counter`. The maximum number of events allowed at a given restart iteration is given by base multiplied by the Las Vegas coefficient at this iteration. The sequence of these coefficients is defined recursively on its prefix subsequences: starting from the first prefix 1, the $(k+1)^t h$ prefix is the $k^t h$ prefix repeated `grow` times and immediately followed by coefficient `grow`^{k}.

- the first coefficients for `grow` =2: [1,1,2,1,1,2,4,1,1,2,1,1,2,4,8,1,...]

[1] Resolution events are: backtracks, fails, nodes, solutions, time or user-defined ones.

- the first coefficients for `grow` =3 : [1, 1, 1, 3, 1, 1, 1, 3, 1, 1, 1, 3, 9,...]

8.6 Limiting the resolution

8.6.1 Built-in search limits

The exploration of the search tree can be limited in various ways. Some usual limits are provided in `SearchMonitorFactory`, or `SMF` for short:

- `limitTime` stops the search when the given time limit has been reached. This is the most common limit, as many applications have a limited available runtime.

Note: The potential search interruption occurs at the end of a propagation, i.e. it will not interrupt a propagation algorithm, so the overall runtime of the solver might exceed the time limit.

- `limitSolution` stops the search when the given solution limit has been reached.
- `limitNode` stops the search when the given search node limit has been reached.
- `limitFail` stops the search when the given fail limit has been reached.
- `limitBacktrack` stops the search when the given backtrack limit has been reached.

8.6.2 Custom search limits

You can decide to interrupt the search process whenever you want with one of the following instructions:

```
solver.getSearchLoop().reachLimit();
solver.getSearchLoop().interrupt(String message);
```

Both options will interrupt the search process but only the first one will inform the solver that the search stops because of a limit. In other words, calling

```
solver.hasReachedLimit()
```

will return false if the second option is used.

Going further

Large Neighborhood Search, *Explanations*.

CHAPTER 9

Logging

Choco 3.2 has a simple logger which can be used by calling

```
SearchMonitorFactory.log(Solver solver, boolean solution, boolean choices);
```

The first argument is the solver. The second indicates whether or not each solution (and associated resolution statistics) should be printed. The third argument indicates whether or not each branching decision should be printed. This may be useful for debugging.

In general, in order to have a reasonable amount of information, we set the first boolean to true and the second to false.

If the two booleans are set to false, the trace would start with a welcome message:

```
** Choco 3.2.0 (2014-05) : Constraint Programming Solver, Copyleft (c) 2010-2014
** Solve : myProblem
```

Then, when the resolution process ends, a complementary message is printed, based on the measures recorded.

```
- Search complete - [ No solution. ]
   Solutions: {0}
[  Maximize = {1}  ]
[  Minimize = {2}  ]
   Building time : {3}s
   Initialisation : {4}s
   Initial propagation : {5}s
   Resolution : {6}s
   Nodes: {7}
   Backtracks: {8}
   Fails: {9}
   Restarts: {10}
   Max depth: {11}
   Propagations: {12} + {13}
   Memory: {14}mb
   Variables: {15}
   Constraints: {16}
```

Brackets *[instruction]* indicate an optional instruction. If no solution has been found, the message "No solution." appears on the first line. `Maximize` –resp. `Minimize`– indicates the best known value before exiting of the objective value using a `ResolutionPolicy.MAXIMIZE` –resp. ResolutionPolicy.MINIMIZE- policy.

Curly braces *{value}* indicate search statistics:

0. number of solutions found
1. objective value in maximization
2. objective value in minimization

3. building time in second (from `new Solver()` to `findSolution()` or equivalent)
4. initialisation time in second (before initial propagation)
5. initial propagation time in second
6. resolution time in second (from `new Solver()` till now)
7. number of decision created, that is, nodes in the binary tree search
8. number of backtracks achieved
9. number of failures that occurred
10. number of restarts operated
11. maximum depth reached in the binary tree search
12. number of *fine* propagations
13. number of *coarse* propagations
14. estimation of the memory used
15. number of variables in the model
16. number of constraints in the model

If the resolution process reached a limit before ending *naturally*, the title of the message is set to :

```
- Incomplete search - Limit reached.
```

The body of the message remains the same. The message is formated thanks to the `IMeasureRecorder` which is a *search monitor*.

When the first boolean of `SearchMonitorFactory.log(Solver, boolean, boolean);` is set to true, on each solution the following message will be printed:

```
{0} Solutions, [Maximize = {1}][Minimize = {2}], Resolution {6}s, {7} Nodes, \\
                                    {8} Backtracks, {9} Fails, {10} Restarts
```

followed by one line exposing the value of each decision variables (those involved in the search strategy).

When the second boolean of `SearchMonitorFactory.log(Solver, boolean, boolean);` is set to true, on each node a message will be printed indicating which decision is applied. The message is prefixed by as many "." as nodes in the current branch of the search tree. A decision is prefixed with `[R]` and a refutation is prefixed by `[L]`.

Warning: Printing the choices slows down the search process.

Part IV

Advanced usage

CHAPTER 10

Large Neighborhood Search (LNS)

Local search techniques are very effective to solve hard optimization problems. Most of them are, by nature, incomplete. In the context of constraint programming (CP) for optimization problems, one of the most well-known and widely used local search techniques is the Large Neighborhood Search (LNS) algorithm [1]. The basic idea is to iteratively relax a part of the problem, then to use constraint programming to evaluate and bound the new solution.

10.1 Principle

LNS is a two-phase algorithm which partially relaxes a given solution and repairs it. Given a solution as input, the relaxation phase builds a partial solution (or neighborhood) by choosing a set of variables to reset to their initial domain; The remaining ones are assigned to their value in the solution. This phase is directly inspired from the classical Local Search techniques. Even though there are various ways to repair the partial solution, we focus on the technique in which Constraint Programming is used to bound the objective variable and to assign a value to variables not yet instantiated. These two phases are repeated until the search stops (optimality proven or limit reached).

The `LNSFactory` provides pre-defined configurations. Here is the way to declare LNS to solve a problem:

```
LNSFactory.rlns(solver, ivars, 30, 20140909L, new FailCounter(100));
solver.findOptimalSolution(ResolutionPolicy.MINIMIZE, objective);
```

It declares a *random* LNS which, on a solution, computes a partial solution based on `ivars`. If no solution are found within 100 fails (`FailCounter(100)`), a restart is forced. Then, every `30` calls to this neighborhood, the number of fixed is randomly picked. `20140909L` is the seed for the `java.util.Random`.

The instruction `LNSFactory.rlns(solver, vars, level, seed, frcounter)` runs:

```
1         LargeNeighborhoodSearch lns = new LargeNeighborhoodSearch(solver, neighbor, true);
2         solver.getSearchLoop().plugSearchMonitor(lns);
3         return lns;
```

The factory provides other LNS configurations together with built-in neighbors.

10.2 Neighbors

While the implementation of LNS is straightforward, the main difficulty lies in the design of neighborhoods able to move the search further. Indeed, the balance between diversification (i.e., evaluating unexplored sub-tree) and intensification (i.e., exploring them exhaustively) should be well-distributed.

[1] Paul Shaw. Using constraint programming and local search methods to solve vehicle routing problems. In Michael Maher and Jean-Francois Puget, editors, *Principles and Practice of Constraint Programming, CP98*, volume 1520 of *Lecture Notes in Computer Science*, pages 417–431. Springer Berlin Heidelberg, 1998.

10.2.1 Generic neighbors

One drawback of LNS is that the relaxation process is quite often problem dependent. Some works have been dedicated to the selection of variables to relax through general concept not related to the class of the problem treated [5,24]. However, in conjunction with CP, only one generic approach, namely Propagation-Guided LNS [24], has been shown to be very competitive with dedicated ones on a variation of the Car Sequencing Problem. Nevertheless, such generic approaches have been evaluated on a single class of problem and need to be thoroughly parametrized at the instance level, which may be a tedious task to do. It must, in a way, automatically detect the problem structure in order to be efficient.

10.2.2 Combining neighborhoods

There are two ways to combine neighbors.

Sequential

Declare an instance of `SequenceNeighborhood(n1, n2, ..., nm)`. Each neighbor ni is applied in a sequence until one of them leads to a solution. At step k, the $(k \mod m)^{th}$ neighbor is selected. The sequence stops if at least one of the neighbor is complete.

Adaptive

Declare an instance of `AdaptiveNeighborhood(1L, n1, n2, ..., nm)`. At the beginning a weight of 1 at assigned to each neighbor ni. Then, if a neighbor leads to solution, its weight w_i is increased by 1. Any time a partial solution has to be computed, a value `W` between 1 and $w_1 + w_2 + ... + w_n$ is randomly picked (`1L` is the seed). Then the weight of each neighbor is subtracted from `W`, as soon as `W`≤ 0, the corresponding neighbor is selected. For instance, let's consider three neighbors n1, n2 and n3, their respective weights w1=2, w2=4, w3=1. `W` = 3 is randomly picked between 1 and 7. Then, the weight of n1 is subtracted, `W``2-=1; the weight of n2 is subtracted, ``W`-4 = -3, `W` is less than 0 and n2 is selected.

10.2.3 Defining its own neighborhoods

One can define its own neighbor by extending the abstract class `ANeighbor`. It forces to implements the following methods:

Method	Definition
`void recordSolution()`	Action to perform on a solution (typicallu, storing the current variables' value).
`void fixSomeVariables(ICause cause) throws ContradictionException`	Fix some variables to their value in the last solution, computing a partial solution.
`void restrictLess()`	Relax the number of variables fixed. Called when no solution was found during a LNS run (trapped into a local optimum).
`boolean isSearchComplete()`	Indicates whether the neighbor is complete, that is, can end.

10.3 Restarts

A generic and common way to reinforce diversification of LNS is to introduce restart during the search process. This technique has proven to be very flexible and to be easily integrated within standard backtracking procedures [2].

10.4 Walking

A complementary technique that appear to be efficient in practice is named *Walking* and consists in accepting equivalent intermediate solutions in a search iteration instead of requiring a strictly better one. This can be achieved by defining an `ObjectiveManager` like this:

```
solver.set(new ObjectiveManager(objective, ResolutionPolicy.MAXIMIZE, false));
```

Where the last parameter, named `strict` must be set to false to accept equivalent intermediate solutions.

[2] Laurent Perron. Fast restart policies and large neighborhood search. In Francesca Rossi, editor, *Principles and Practice of Constraint Programming at CP 2003*, volume 2833 of *Lecture Notes in Computer Science*. Springer Berlin Heidelberg, 2003.

CHAPTER 11

Explanations

Choco 3.2 natively support explanations [1]. However, no explanation engine is plugged-in by default.

11.1 Principle

Nogoods and explanations have long been used in various paradigms for improving search. An explanation records some sufficient information to justify an inference made by the solver (domain reduction, contradiction, etc.). It is made of a subset of the original propagators of the problem and a subset of decisions applied during search. Explanations represent the logical chain of inferences made by the solver during propagation in an efficient and usable manner. In a way, they provide some kind of a trace of the behavior of the solver as any operation needs to be explained.

Explanations have been successfully used for improving constraint programming search process. Both complete (as the mac-dbt algorithm) and incomplete (as the decision-repair algorithm) techniques have been proposed. Those techniques follow a similar pattern: learning from failures by recording each domain modification with its associated explanation (provided by the solver) and taking advantage of the information gathered to be able to react upon failure by directly pointing to relevant decisions to be undone. Complete techniques follow a most-recent based pattern while incomplete technique design heuristics to be used to focus on decisions more prone to allow a fast recovery upon failure.

11.1.1 Key components of an explanation system

Adding explanations capabilities to a constraint solver requires addressing several aspects:

Computing explanations: domain reductions are usually associated with a cause: the propagator that actually performed the modification. This information can be used to compute an explanation. This can be done synchronously during propagation (by intrusive modification of the propagation algorithm) or asynchronously post propagation (by accessing an explanation service provided by propagators).

Storing explanations: a data structure needs to be defined to be able to store decisions made by the solver, domain reductions and their associated explanations. There exist several ways for storing explanations: a flattened storage of the domain modifications and their explanations composed of propagators and previously made decisions, or a un-flattened storage of the domain modifications and their explanations expressed through previous domain modifications. The data structure is referred to as explanation store.

Accessing explanations: the data structure used to store explanations needs to provide access not only to domain modification explanations but also to current upper and lower bounds of the domains, current domain as a whole, etc.

Despite being possibly very efficient, explanations suffer from several drawbacks:

[1] Narendra Jussien. The versatility of using explanations within constraint programming. Technical Report 03-04-INFO, 2003.

Memory: storing explanations requires storing a way or another, variable modifications;

CPU: computing explanations usually comes with a cost even though the propagation algorithm can be partially used for that;

Software engineering: implementing explanations can be quite intrusive within a constraint solver.

11.2 In practice

Consider the following example:

```
1          Solver solver = new Solver();
2          BoolVar[] bvars = VF.boolArray("B", 4, solver);
3          solver.post(ICF.arithm(bvars[2], "=", bvars[3]));
4          solver.post(ICF.arithm(bvars[2], "!=", bvars[3]));
5          solver.set(ISF.lexico_LB(bvars));
6          solver.findAllSolutions();
```

The problem has no solution since the two constraints cannot be satisfied together. A naive strategy such as `ISF.lexico_LB(bvars)` (which selects the variables in lexicographical order) will detect lately and many times the failure. By plugging-in an explanation engine, on each failure, the reasons of the conflict will be explained.

```
1          ExplanationFactory.CBJ.plugin(solver, true);
```

The explanation engine records *deductions* and *causes* in order to compute explanations. In that small example, when an explanation engine is plugged-in, the two first failures will enable to conclude that the problem has no solution. Only three nodes are created to close the search, seven are required without explanations.

Note: Only unary, binary, ternary and sum propagators over integer variables have a dedicated explanation algorithm. Although global constraints over integer variables are compatible with explanations, they should be either accurately explained or reformulated to fully benefit from explanations.

11.2.1 Deduction

There are five types of deductions: value removal, decision application, decision refutation, propagator activation and explanation.

Value removal and branching decision They are specific deductions; they store the touched couple variable-value. They are triggered by, respectively, propagation and search process. The relation expressed can be value deletion or assignment.

Propagator activation It stores the touched propagator; it is mainly triggered through reification.

Explanation A specific deduction made of a set of deductions and a set of propagators.

11.2.2 Cause

A cause implements `ICause` and must defined a `explain(Deduction d, Explanation e)` method. Such a method completes the explanation `e` with the help of the deduction `d`. Every time a variable is modified, the cause needs to be specified in order to compute explanations. For instance, when a propagator updates the bound of an integer variable, the cause is the propagator itself. So do decisions, objective manager, etc.

11.2.3 Computing explanations

When a contradiction occurs during propagation, it can only be thrown by:

- a propagator which detects unsatisfiability, based on the current domain of its variables;
- or a variable whom domain is emptied.

Consequently, in addition to causes, variables can also explain the current state of their domain. And, computing an explanation of a failure consists in recursive calls to `explain` methods from causes and variables. The entry point is either a the unsatisfiabable propagator or the empty variable.

Note: Explanations can be computed without failure. The entry point is a variable, and only removed values can be explained.

Variables explain themselves by iterating over removed values and calling the explanation engine to explain each of them. Each propagator embeds its own explanation algorithm which relies on the relation it defines over variables. By default, if no explanation algorithm is defined, a default algorithm is applied: the current deduction is due to the current domain of the involved variables and the application of the propagator. But, this is a weak explanation and providing specific explanations betters the overall process.

For instance, here is the algorithm of `PropGreaterOrEqualX_YC` ($x \geq y + c$, `x` and `y` are integer variables, `c` is a constant):

```
1     public void explain(Deduction d, Explanation e) {
2         e.add(solver.getExplainer().getPropagatorActivation(this));
3         e.add(aCause);
4         Variable var = d.getVar();
5         if (var.equals(x)) {
6             y.explain(VariableState.LB, e);
7         } else if (var.equals(y)) {
8             x.explain(VariableState.UB, e);
9         } else {
10            super.explain(d, e);
11        }
12    }
```

The two first lines indicate that the deduction is due to the application of the propagator (l.3), maybe through reification (l.2). Then, depending on the variable touched by the deduction, either the lower bound of `y` (l.5) or the upper bound of `x` (l.7) explains the deduction. Indeed, such a propagator only updates lower bound of `y` based on the upper bound of `x` and *vice versa*.

Let consider that the deduction involves `x` and is explained by the lower bound of `y`. The lower bound `y` needs to be explained. The value below the current lower bound of `y` are iterated and each deduction are explained, thanks to the causes previously stored. This is repeated until all deductions are explained. The results is a set of deductions, including branching decisions, and a set a propagators, which applied altogether explained the conflict.

11.3 Explanations for the system

Explanations for the system, which try to reduce the search space, differ from the ones giving feedback to a user about the insatisfiability of its model. Both rely on the capacity of the explanation engine to motivate a failure, during the search form system explanations and once the search is complete for user ones.

Important: Most of the time, explanations are raw and need to be processed to be easily interpreted by users.

11.3.1 Conflict-based backjumping

When Conflict-based Backjumping (CBJ) is plugged-in, the search is hacked in the following way. On a failure, explanations are retrieved. From all left branch decisions explaining the failure, the last taken, *return decision*, is stored to jump back to it. Decisions from the current one to the return decision (excluded) are erased. Then, the return decision is refuted and the search goes on. If the explanation is made of no left branch decision, the problem is proven to have no solution and search stops.

Factory: `solver.explanations.ExplanationFactory`

API:

```
CBJ.plugin(Solver solver, boolean flattened)
```

11.3.2 Dynamic backtracking

This strategy, Dynamic backtracking (DBT) corrects a lack of deduction of Conflict-based backjumping. On a failure, explanations are retrieved. From all left branch decisions explaining the failure, the last taken, *return decision*, is stored to jump back to it. Decisions from the current one to the return decision (excluded) are maintained, only the return decision is refuted and the search goes on. If the explanation is made of no left branch decision, the problem is proven to have no solution and search stops.

Factory: `solver.explanations.ExplanationFactory`

API:

```
DBT.plugin(Solver solver, boolean flattened)
```

11.4 Explanations for the end-user

Explaining the last failure of a complete search without solution provides information about the reasons why a problem has no solution. For the moment, there is no simplified way to get such explanations. CBJ and DBT enable retrieving an explanation of the last conflict. It requires to enable propagators in explanation (set to *false* by default in *configuration.properties*). And then to activate the storing of the last explanation computed:

```
// .. problem definition ..
// First manually plug CBJ, or DBT
solver.set(new RecorderExplanationEngine(solver));
ConflictBasedBackjumping cbj = new ConflictBasedBackjumping(solver.getExplainer());
// Then active end-user explanation
cbj.activeUserExplanation(true);
if(!solver.findSolution()){
    // If the problem has no solution, the end-user explanation can be retrieved
    System.out.println(cbj.getUserExplanation());
}
```

Incomplete search leads to incomplete explanations: as far as at least one decision is part of the explanation, there is no guarantee the failure does not come from that decision. On the other hand, when there is no decision, the explanation is complete.

CHAPTER 12

Search monitor

12.1 Principle

A search monitor is an observer of the search loop. It gives user access before and after executing each main step of the search loop:

- *initialize*: when the search loop starts,
- *initial propagator*: when the initial propagation is run,
- *open node*: when a decision is computed,
- *down left branch*: on going down in the tree search applying a decision,
- *down right branch*: on going down in the tree search refuting a decision,
- *up branch*: on going up in the tree search to reconsider a decision,
- *solution*: when a solution is got,
- *restart search*: when the search is restarted to a previous node, commonly the root node,
- *close*: when the search loop ends,
- *contradiction*: on a failure,
- *interruption*: on the interruption of the search loop.

With the accurate search monitor, one can easily interact with the search loop, from pretty printing of a solution to forcing a restart, or many other actions.

The interfaces to implement are:

- `IMonitorInitialize`,
- `IMonitorInitPropagation`,
- `IMonitorOpenNode`,
- `IMonitorDownBranch`,
- `IMonitorUpBranch`,
- `IMonitorSolution`,
- `IMonitorRestart`,
- `IMonitorContradiction`,
- `IMonitorInterruption`,

- `IMonitorClose`.

Most of them gives the opportunity to do something before and after a step. The other ones are called after a step.

For instance, `NogoodStoreFromRestarts` monitors restarts. Before a restart is done, the nogoods are extracted from the current decision path; after the restart has been done, the newly created nogoods are added and the nogoods are propagated. Thus, the framework is almost not intrusive.

```
1  public class NogoodStoreFromRestarts extends Constraint implements IMonitorRestart {
2      public void beforeRestart() {
3          extractNogoodFromPath();
4      }
5      public void afterRestart() {
6          try {
7                          // add newly created no goods
8              while (!nogoods.isEmpty()) {
9                  INogood ng = nogoods.pollFirst();
10                                 png.addNogood(ng);
11             }
12                         // initial propagation of no goods
13                         png.unitPropagation();
14                         // forces to reach the fix-point of constraints
15                         png.getSolver().getEngine().propagate();
16         } catch (ContradictionException e) {
17                         png.getSolver().getSearchLoop().interrupt(MSG_NGOOD);
18         }
19     }
```

CHAPTER 13

Defining its own search strategy

One key component of the resolution is the exploration of the search space induced by the domains and constraints. It happens that built-in search strategies are not enough to tackle the problem. Or one may want to define its own strategy. This can be done in three steps: selecting the variable, selecting the value, then making a decision.

The following instructions are based on IntVar, but can be easily adapted to other types of variables.

13.1 Selecting the variable

An implementation of the `VariableSelector<V extends Variable>` interface is needed. A variable selector specifies which variable should be selected at a fix point. It is based specifications (ex: smallest domain, most constrained, etc.). Although it is not required, the selected variable should not be already instantiated to a singleton. This interface forces to define only one method:

```
V getVariable(V[] variables)
```

One variable has to be selected from `variables` to create a decision on. If no valid variable exists, the method is expected to return `null`.

An implementation of the `VariableEvaluator<V extends Variable>` is strongly recommended. It enables breaking ties. It forces to define only one method:

```
double evaluate(V variable)
```

An evaluation of the given variable is done wrt the evaluator. The variable with the **smallest** value will then be selected.

Here is the code of the `FirstFail` variable selector which selects first the variable with the smallest domain.

```
1  public class FirstFail implements VariableSelector<IntVar>, VariableEvaluator<IntVar> {
2
3
4      @Override
5      public IntVar getVariable(IntVar[] variables) {
6          int small_idx = -1;
7          int small_dsize = Integer.MAX_VALUE;
8          for (int idx = 0; idx < variables.length; idx++) {
9              int dsize = variables[idx].getDomainSize();
10             if (dsize > 1 && dsize < small_dsize) {
11                 small_dsize = dsize;
12                 small_idx = idx;
13             }
14         }
```

```
15            return small_idx > -1 ? variables[small_idx] : null;
16        }
17
18        @Override
19        public double evaluate(IntVar variable) {
20            return variable.getDomainSize();
21        }
22    }
```

13.2 Selecting the variable

The value to be selected must belong to the variable domain.

For `IntVar` the interface `IntValueSelector` is required. It imposes one method:

`int selectValue(IntVar var)`

Return the value to constrain `var` with.

13.3 Making a decision

A decision is made of a variable, an decision operator and a value. The decision operator should be selected in `DecisionOperator` among:

`int_eq`

For `IntVar`, represents an instantiation, $X = 3$. The refutation of the decision will be a value removal.

`int_neq`

For `IntVar`, represents a value removal, $X \neq 3$. The refutation of the decision will be an instantiation.

`int_split`

For `IntVar`, represents an upper bound modification, $X \leq 3$. The refutation of the decision will be a lower bound modification.

`int_reverse_split`

For `IntVar`, represents a lower bound modification, $X \geq 3$. The refutation of the decision will be an upper bound modification.

`set_force`

For `SetVar`, represents a kernel addition, $3 \in S$. The refutation of the decision will be an envelop removal.

`set_remove`

For `SetVar`, represents an envelop removal, $3 \notin S$. The refutation of the decision will be a kernel addition.

Attention: A particular attention should be made while using ‘‘IntVar‘‘s and their type of domain. Indeed, bounded variables does not support making holes in their domain. Thus, removing a value which is not a current bound will be missed, and can lead to an infinite loop.

One can define its own operator by extending `DecisionOperator`.

`void apply(V var, int value, ICause cause)`

Operations to execute when the decision is applied (left branch). It can throw an `ContradictionException` if the application is not possible.

`void unapply(V var, int value, ICause cause)`

Operations to execute when the decision is refuted (right branch). It can throw an `ContradictionException` if the application is not possible.

`DecisionOperator opposite()`

Opposite of the decision operator. *Currently useless*.

`String toString()`

A pretty print of the decision, for logging.

Most of the time, extending `AbstractStrategy` is not necessary. Using specific strategy dedicated to a type of variable, such as `IntStrategy` is enough. The one above has an alternate constructor:

```
public IntStrategy(IntVar[] scope,
                   VariableSelector<IntVar> varSelector,
                   IntValueSelector valSelector,
                   DecisionOperator<IntVar> decOperator) {...}
```

And defining your own strategy is really crucial, start by copying/pasting an existing one. Indeed, decisions are stored in pool managers to avoid creating too many decision objects, and thus garbage collecting too often.

Defining its own constraint

Important: The array of variables given in parameter of a `Propagator` constructor is not cloned but referenced. That is, if a permutation occurs in the array of variables, all propagators referencing the array will be incorrect.

CHAPTER 15

Ibex

> "IBEX is a C++ library for constraint processing over real numbers.
>
> It provides reliable algorithms for handling non-linear constraints. In particular, roundoff errors are also taken into account. It is based on interval arithmetic and affine arithmetic." – http://www.ibex-lib.org/

To manage continuous constraints with Choco, an interface with Ibex has been done. It needs Ibex to be installed on your system. Then, simply declare the following VM options:

```
-Djava.library.path=/path/to/Ibex/lib
```

The path */path/to/Ibex/lib* points to the *lib* directory of the Ibex installation directory.

15.1 Installing Ibex

See the installation instructions of Ibex to complied Ibex on your system. More specially, take a look at Installation as a dynamic library and do not forget to add the `--with-java-package=solver.constraints.real` configuration option.

Once the installation is completed, the JVM needs to know where Ibex is installed to fully benefit from the Choco-Ibex bridge and declare real variables and constraints.

Part V

Elements of Choco

CHAPTER 16

Constraints over integer variables

16.1 absolute

The `absolute` constraint involves two variables *VAR1* and *VAR2*. It ensures that *VAR1* = | *VAR2* | .

API:

```
Constraint absolute(IntVar VAR1, IntVar VAR2)
```

Example

```
        Solver solver = new Solver();
        IntVar X = VF.enumerated("X", 0, 2, solver);
        IntVar Y = VF.enumerated("X", -6, 1, solver);
        solver.post(ICF.absolute(X, Y));
        solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 0, Y = 0*
- *X = 1, Y = -1*
- *X = 1, Y = 1*
- *X = 2, Y = -2*

16.2 alldifferent

The *alldifferent* constraints involves two or more integer variables *VARS* and holds that all variables from *VARS* take a different value. A signature offers the possibility to specify the filtering algorithm to use:

- `"BC"`: filters on bounds only, based on: "A Fast and Simple Algorithm for Bounds Consistency of the AllDifferent Constraint", A. Lopez-Ortiz, CG. Quimper, J. Tromp, P.van Beek.
- `"AC"`: filters on the entire domain of the variables. It uses Regin algorithm; it runs in *O(m.n)* worst case time for the initial propagation and then in *O(n+m)* time per arc removed from the support.
- `"DEFAULT"`: uses `"BC"` plus a probabilistic `"AC"` propagator to get a compromise between `"BC"` and `"AC"`.

See also: alldifferent in the Global Constraint Catalog.

Implementation based on: [Regin94], [LopezOrtizQTvB03].

API:

```
Constraint alldifferent(IntVar[] VARS)
Constraint alldifferent(IntVar[] VARS, String CONSISTENCY)
```

Example

```
        Solver solver = new Solver();
        IntVar W = VF.enumerated("W", 0, 1, solver);
        IntVar X = VF.enumerated("X", -1, 2, solver);
        IntVar Y = VF.enumerated("Y", 2, 4, solver);
        IntVar Z = VF.enumerated("Z", 5, 7, solver);
        SMF.log(solver, true, false);
```

Some solutions of the problem are :

- *X = -1, Y = 2, Z = 5, W = 1*
- *X = 1, Y = 2, Z = 7, W = 0*
- *X = 2, Y = 3, Z = 5, W = 0*
- *X = 2, Y = 4, Z = 7, W = 1*

16.3 alldifferent_conditionnal

The *alldifferent_conditionnal* constraint is a variation of the *alldifferent* constraint. It holds the *alldifferent* constraint on the subset of variables *VARS* which satisfies the given condition *CONDITION*.

A simple example is the *alldifferent_except_0* variation of the *alldifferent* constraint.

API:

```
Constraint alldifferent_conditionnal(IntVar[] VARS, Condition CONDITION)
Constraint alldifferent_conditionnal(IntVar[] VARS, Condition CONDITION, boolean AC)
```

One can force the *AC* algorithm to be used by calling the second signature.

Example

```
        Solver solver = new Solver();
        IntVar[] XS = VF.enumeratedArray("XS", 5, 0, 3, solver);
        solver.post(ICF.alldifferent_conditionnal(XS,
                new Condition() {
                    @Override
                    public boolean holdOnVar(IntVar x) {
                        return !x.contains(1) && !x.contains(3);
                    }
                }));
        solver.findAllSolutions();
```

The condition in the example states that the values *1* and *3* can appear more than once, unlike other values.

Some solutions of the problem are :

- *XS[0] = 0, XS[1] = 1, XS[2] = 1, XS[3] = 1, XS[4] = 1*
- *XS[0] = 0, XS[1] = 1, XS[2] = 2, XS[3] = 1, XS[4] = 1*
- *XS[0] = 1, XS[1] = 2, XS[2] = 1, XS[3] = 1, XS[4] = 1*

- *XS[0] = 0, XS[1] = 1, XS[2] = 2, XS[3] = 3, XS[4] = 3*

16.4 alldifferent_except_0

The *alldifferent_except_0* involves an array of variables *VARS*. It ensures that all variables from *VAR* take a distinct value or 0, that is, all values but 0 can't appear more than once.

See also: alldifferent_except_0 in the Global Constraint Catalog.

API:

```
Constraint alldifferent_except_0(IntVar[] VARS)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] XS = VF.enumeratedArray("XS", 4, 0, 2, solver);
3         solver.post(ICF.alldifferent_except_0(XS));
4         solver.findAllSolutions();
```

Some solutions of the problem are :

- *XS[0] = 0, XS[1] = 0, XS[2] = 0, XS[3] = 0*
- *XS[0] = 0, XS[1] = 1, XS[2] = 2, XS[3] = 0*
- *XS[0] = 0, XS[1] = 2, XS[2] = 0, XS[3] = 0*
- *XS[0] = 2, XS[1] = 1, XS[2] = 0, XS[3] = 0*

16.5 among

The *among* constraint involves:

- an integer variable *NVAR*,
- an array of integer variables *VARIABLES* and
- an array of integers.

It holds that *NVAR* is the number of variables of the collection *VARIABLES* that take their value in *VALUES*.

See also: among in the Global Constraint Catalog.

Implementation based on: [BessiereHH+05].

API:

```
Constraint among(IntVar NVAR, IntVar[] VARS, int[] VALUES)
```

Example

```
1         Solver solver = new Solver();
2         IntVar N = VF.enumerated("N", 2, 3, solver);
3         IntVar[] XS = VF.enumeratedArray("XS", 4, 0, 6, solver);
4         solver.post(ICF.among(N, XS, new int[]{1, 2, 3}));
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *N = 2, XS[0] = 0, XS[1] = 0, XS[2] = 1, XS[3] = 1*
- *N = 2, XS[0] = 0, XS[1] = 1, XS[2] = 3, XS[3] = 6*
- *N = 3, XS[0] = 1, XS[1] = 1, XS[2] = 2, XS[3] = 4*
- *N = 3, XS[0] = 3, XS[1] = 2, XS[2] = 1, XS[3] = 0*

16.6 arithm

The constraint *arithm* involves either:

- a integer variable *VAR*, an operator *OP* and a constant *CST*. It holds *VAR OP CSTE*, where *CSTE* must be chosen in {"=", "!=", ">","<",">=","<="}.
- or two variables *VAR1* and *VAR2* and an operator *OP*. It ensures that *VAR1 OP VAR2*, where *OP* must be chosen in {"=", "!=", ">","<",">=","<="} .
- or two variables *VAR1* and *VAR2*, two operators *OP1* and *OP2* and an constant *CSTE*. The operators must be different, taken from {"=", "!=", ">","<",">=","<="} or {"+", "-"}, the constarint ensures that *VAR1 OP1 VAR2 OP2 CSTE*.

API:

```
Constraint arithm(IntVar VAR, String OP, int CSTE)
Constraint arithm(IntVar VAR1, String OP, IntVar VAR2)
Constraint arithm(IntVar VAR1, String OP1, IntVar VAR2, String OP2, int CSTE)
```

Example 1

```
1         Solver solver = new Solver();
2         IntVar X = VF.enumerated("X", 1, 4, solver);
3         solver.post(ICF.arithm(X, ">", 2));
4         solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 3*
- *X = 4*

Example 2

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 0, 2, solver);
3          IntVar Y = VF.enumerated("X", -6, 1, solver);
4          solver.post(ICF.arithm(X, "<=", Y, "+", 1));
5          solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 0, Y = -1*
- *X = 0, Y = 0*
- *X = 0, Y = 1*
- *X = 1, Y = 0*

- *X = 1, Y = 1*
- *X = 2, Y = 1*

16.7 atleast_nvalues

The *atleast_nvalues* constraint involves:

- an array of integer variables *VARS*,
- an integer variable *NVALUES* and
- a boolean *AC*.

Let *N* be the number of distinct values assigned to the variables of the *VARS* collection. The constraint enforces the condition $N \geq NVALUES$ to hold. The boolean *AC* set to true enforces arc-consistency.

See also: atleast_nvalues in the Global Constraint Catalog.

Implementation based on: [Regin95].

API:

```
Constraint atleast_nvalues(IntVar[] VARS, IntVar NVALUES, boolean AC)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] XS = VF.enumeratedArray("XS", 4, 0, 2, solver);
3          IntVar N = VF.enumerated("N", 2, 3, solver);
4          solver.post(ICF.atleast_nvalues(XS, N, true));
5          solver.findAllSolutions();
```

Some solutions of the problem are :

- *XS[0] = 0 XS[1] = 0 XS[2] = 0 XS[3] = 1 N = 2*
- *XS[0] = 0 XS[1] = 1 XS[2] = 0 XS[3] = 1 N = 2*
- *XS[0] = 0 XS[1] = 1 XS[2] = 2 XS[3] = 1 N = 2*
- *XS[0] = 2 XS[1] = 0 XS[2] = 2 XS[3] = 1 N = 3*
- *XS[0] = 2 XS[1] = 2 XS[2] = 1 XS[3] = 0 N = 3*

16.8 atmost_nvalues

The *atmost_nvalues* constraint involves:

- an array of integer variables *VARS*,
- an integer variable *NVALUES* and
- a boolean *GREEDY*.

Let *N* be the number of distinct values assigned to the variables of the *VARS* collection. The constraint enforces the condition $N \leq NVALUES$ to hold. The boolean *GREEDY* set to true filters the conjunction of *atmost_nvalues* and disequalities (see Fages and Lapègue, CP'13 or Artificial Intelligence journal). It automatically detects disequalities and *alldifferent* constraints. Presumably useful when *NVALUES* must be minimized

See also: atmost_nvalues in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint atmost_nvalues(IntVar[] VARS, IntVar NVALUES, boolean GREEDY)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] XS = VF.enumeratedArray("XS", 4, 0, 2, solver);
3          IntVar N = VF.enumerated("N", 1, 3, solver);
4          solver.post(ICF.atmost_nvalues(XS, N, false));
5          solver.findAllSolutions();
```

Some solutions of the problem are :

- *XS[0] = 0, XS[1] = 0, XS[2] = 0, XS[3] = 0, N = 1*
- *XS[0] = 0, XS[1] = 0, XS[2] = 0, XS[3] = 0, N = 2*
- *XS[0] = 0, XS[1] = 0, XS[2] = 0, XS[3] = 0, N = 3*
- *XS[0] = 0, XS[1] = 0, XS[2] = 0, XS[3] = 1, N = 2*
- *XS[0] = 0, XS[1] = 1, XS[2] = 1, XS[3] = 0, N = 2*
- *XS[0] = 2, XS[1] = 2, XS[2] = 1, XS[3] = 0, N = 3*

16.9 bin_packing

The *bin_packing* constraint involves:

- an array of integer variables *ITEM_BIN*,
- an array of integers *ITEM_SIZE*,
- an array of integer variables *BIN_LOAD* and
- an integer *OFFSET*.

It holds the Bin Packing Problem rules: a set of items with various to pack into bins with respect to the capacity of each bin.

- *ITEM_BIN* represents the bin of each item, that is, *ITEM_BIN[i] = j* states that the i th is put in the j th bin.
- *ITEM_SIZE* represents the size of each size.
- *BIN_LOAD* represents the load of each bin, that is, the sum of size of the items in it.

This constraint is not a built-in constraint and is based on various propagators.

See also: bin_packing in the Global Constraint Catalog.

API:

```
Constraint[] bin_packing(IntVar[] ITEM_BIN, int[] ITEM_SIZE, IntVar[] BIN_LOAD, int OFFSET)
```

Example

```
Solver solver = new Solver();
IntVar[] IBIN = VF.enumeratedArray("IBIN", 5, 1, 3, solver);
int[] sizes = new int[]{2, 3, 1, 4, 2};
IntVar[] BLOADS = VF.enumeratedArray("BLOADS", 3, 0, 5, solver);
solver.post(ICF.bin_packing(IBIN, sizes, BLOADS, 1));
solver.findAllSolutions();
```

Some solutions of the problem are :

- *IBIN[0] = 1, IBIN[1] = 1, IBIN[2] = 2, IBIN[3] = 2, IBIN[4] = 3, BLOADS[0] = 5, BLOADS[1] = 5, BLOADS[2] = 2*
- *IBIN[0] = 1, IBIN[1] = 3, IBIN[2] = 1, IBIN[3] = 2, IBIN[4] = 1, BLOADS[0] = 5, BLOADS[1] = 4, BLOADS[2] = 3*
- *IBIN[0] = 2, IBIN[1] = 3, IBIN[2] = 1, IBIN[3] = 1, IBIN[4] = 3, BLOADS[0] = 5, BLOADS[1] = 2, BLOADS[2] = 5*

16.10 bit_channeling

The *bit_channeling* constraint involves:

- an array of boolean variables *BVARS* and
- an integer variable *VAR*.

It ensures that: *VAR* = $2^0 \times$ *BITS[0]* $2^1 \times$ *BITS[1]* + ... +:math:*2^{n} times BITS[n]. BIT[0] is related to the first bit of 'VAR* (2^0), *BIT[1] is related to the second bit of 'VAR* (2^1), etc. The upper bound of *VAR* is given by $2^{|BITS|+1}$.

API:

```
Constraint bit_channeling(BoolVar[] BITS, IntVar VAR)
```

Example

```
Solver solver = new Solver();
BoolVar[] BVARS = VF.boolArray("BVARS", 4, solver);
IntVar VAR = VF.enumerated("VAR", 0, 15, solver);
solver.post(ICF.bit_channeling(BVARS, VAR));
solver.findAllSolutions();
```

The solutions of the problem are :

- *VAR = 0, BVARS[0] = 0, BVARS[1] = 0, BVARS[2] = 0, BVARS[3] = 0*
- *VAR = 1, BVARS[0] = 1, BVARS[1] = 0, BVARS[2] = 0, BVARS[3] = 0*
- *VAR = 2, BVARS[0] = 0, BVARS[1] = 1, BVARS[2] = 0, BVARS[3] = 0*
- *VAR = 11, BVARS[0] = 1, BVARS[1] = 1, BVARS[2] = 0, BVARS[3] = 1*
- *VAR = 15, BVARS[0] = 1, BVARS[1] = 1, BVARS[2] = 1, BVARS[3] = 1*

16.11 boolean_channeling

The *boolean_channeling* constraint involves:

- an array of boolean variables *BVARS*,
- an integer variable *VAR* and
- an integer *OFFSET*.

It ensures that: *VAR* = *i* ⇔ *BVARS* [*i-OFFSET*] = *1*. The *OFFSET* is typically set to 0.

API:

```
Constraint boolean_channeling(BoolVar[] BVARS, IntVar VAR, int OFFSET)
```

Example

```
1          Solver solver = new Solver();
2          BoolVar[] BVARS = VF.boolArray("BVARS", 5, solver);
3          IntVar VAR = VF.enumerated("VAR", 1, 5, solver);
4          solver.post(ICF.boolean_channeling(BVARS, VAR, 1));
5          solver.findAllSolutions();
```

The solutions of the problem are :

- *VAR = 1, BVARS[0] = 1, BVARS[1] = 0, BVARS[2] = 0, BVARS[3] = 0, BVARS[4] = 0*
- ‘VAR = 2, BVARS[0] = 0, BVARS[1] = 1, BVARS[2] = 0, BVARS[3] = 0, BVARS[4] = 0 ‘
- *VAR = 3, BVARS[0] = 0, BVARS[1] = 0, BVARS[2] = 1, BVARS[3] = 0, BVARS[4] = 0*
- *VAR = 4, BVARS[0] = 0, BVARS[1] = 0, BVARS[2] = 0, BVARS[3] = 1, BVARS[4] = 0*
- *VAR = 5, BVARS[0] = 0, BVARS[1] = 0, BVARS[2] = 0, BVARS[3] = 0, BVARS[4] = 1*

16.12 circuit

The *circuit* constraint involves:

- an array of integer variables *VARS*,
- an integer *OFFSET* and
- a configuration *CONF*.

It ensures that the elements of *VARS* define a covering circuit where *VARS* [i] = *OFFSET* + *j* means that *j* is the successor of *i*. The filtering algorithms are:

- subtour elimination,
- *alldifferent*,
- dominator-based,
- and strongly connected components based filtering.

The *CONF* is a defined by an `enum`:

- `CircuitConf.LIGHT`:
- `CircuitConf.FIRST`:
- `CircuitConf.RD`:
- `CircuitConf.ALL`:

See also: circuit in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint circuit(IntVar[] VARS, int OFFSET, CircuitConf CONF)
Constraint circuit(IntVar[] VARS, int OFFSET) // with CircuitConf.RD
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] NODES = VF.enumeratedArray("NODES", 5, 0, 4, solver);
3          solver.post(ICF.circuit(NODES, 0, CircuitConf.LIGHT));
4          solver.findAllSolutions();
```

Some solutions of the problem are :

- *NODES[0] = 1, NODES[1] = 2, NODES[2] = 3, NODES[3] = 4, NODES[4] = 0*
- *NODES[0] = 3, NODES[1] = 4, NODES[2] = 0, NODES[3] = 1, NODES[4] = 2*
- *NODES[0] = 4, NODES[1] = 2, NODES[2] = 3, NODES[3] = 0, NODES[4] = 1*
- *NODES[0] = 4, NODES[1] = 3, NODES[2] = 1, NODES[3] = 0, NODES[4] = 2*

16.13 cost_regular

The *cost_regular* constraint involves:

- an array of integer variables *VARS*,
- an integer variable *COST* and
- a cost automaton *CAUTOMATON*.

It ensures that the assignment of a sequence of variables *VARS* is recognized by *CAUTOMATON*, a deterministic finite automaton, and that the sum of the costs associated to each assignment is bounded by the cost variable. This version allows to specify different costs according to the automaton state at which the assignment occurs (i.e. the transition starts).

The *CAUOTMATON* can be defined using the ‘‘solver.constraints.nary.automata.FA.CostAutomaton‘ either:

- by creating a `CostAutomaton`: once created, states should be added, then initial and final states are defined and finally, transitions are declared.
- or by first creating a `FiniteAutomaton` and then creating a matrix of costs and finally calling one of the following API from `CostAutomaton`:
  - `ICostAutomaton makeSingleResource(IAutomaton pi, int[][][] costs, int inf, int sup)`
  - `ICostAutomaton makeSingleResource(IAutomaton pi, int[][] costs, int inf, int sup)`

  The other API of `CostAutomaton` (`makeMultiResources(...)`) are dedicated to the *multi-cost_regular* constraint.

Implementation based on: [DPR06].

API:

```
Constraint cost_regular(IntVar[] VARS, IntVar COST, ICostAutomaton CAUTOMATON)
```

Example

```
1           Solver solver = new Solver();
2           IntVar[] VARS = VF.enumeratedArray("VARS", 5, 0, 2, solver);
3           IntVar COST = VF.enumerated("COST", 0, 10, solver);
4           FiniteAutomaton fauto = new FiniteAutomaton();
5           int start = fauto.addState();
6           int end = fauto.addState();
7           fauto.setInitialState(start);
8           fauto.setFinal(start, end);
9
10          fauto.addTransition(start, start, 0, 1);
11          fauto.addTransition(start, end, 2);
12
13          fauto.addTransition(end, end, 1);
14          fauto.addTransition(end, start, 0, 2);
15
16          int[][] costs = new int[5][3];
17          costs[0] = new int[]{1, 2, 3};
18          costs[1] = new int[]{2, 3, 1};
19          costs[2] = new int[]{3, 1, 2};
20          costs[3] = new int[]{3, 2, 1};
21          costs[4] = new int[]{2, 1, 3};
22
23          solver.post(ICF.cost_regular(VARS, COST, CostAutomaton.makeSingleResource(fauto, costs,
24          solver.findAllSolutions();
```

Some solutions of the problem are :

- *VARS[0] = 0, VARS[1] = 0, VARS[2] = 0, VARS[3] = 0, VARS[4] = 1, COST = 10*
- *VARS[0] = 0, VARS[1] = 0, VARS[2] = 0, VARS[3] = 1, VARS[4] = 1, COST = 9*
- *VARS[0] = 0, VARS[1] = 0, VARS[2] = 1, VARS[3] = 2, VARS[4] = 1, COST = 6*
- *VARS[0] = 1, VARS[1] = 2, VARS[2] = 1, VARS[3] = 0, VARS[4] = 1, COST = 8*

16.14 count

The *count* constraint involves:

- an integer *VALUE*,
- an array of integer variables *VARS* and
- an integer variable *LIMIT*.

The constraint holds that *LIMIT* is equal to the number of variables from *VARS* assigned to the value *VALUE*. An alternate signature enables *VALUE* to be an integer variable.

See also: count in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint count(int VALUE, IntVar[] VARS, IntVar LIMIT)
Constraint count(IntVar VALUE, IntVar[] VARS, IntVar LIMIT)
```

Example

```
1           Solver solver = new Solver();
2           IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 3, solver);
3           IntVar VA = VF.enumerated("VA", new int[]{1, 3}, solver);
4           IntVar CO = VF.enumerated("CO", new int[]{0, 2, 4}, solver);
5           solver.post(ICF.count(VA, VS, CO));
6           solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 0, VS[1] = 0, VS[2] = 0, VS[3] = 0, VA = 1, CO = 0*
- *VS[0] = 0, VS[1] = 1, VS[2] = 1, VS[3] = 0, VA = 1, CO = 2*
- *VS[0] = 0, VS[1] = 2, VS[2] = 2, VS[3] = 1, VA = 3, CO = 0*
- *VS[0] = 3, VS[1] = 3, VS[2] = 3, VS[3] = 3, VA = 3, CO = 4*

16.15 cumulative

The *cumulative* constraints involves:

- an array of task object *TASKS*,
- an array of integer variable *HEIGHTS*,
- an integer variable *CAPACITY* and
- a boolean *INCREMENTAL*.

It ensures that at each point of the time the cumulated height of the set of tasks that overlap that point does not exceed the given capacity.

See also: cumulative in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint cumulative(Task[] TASKS, IntVar[] HEIGHTS, IntVar CAPACITY)
Constraint cumulative(Task[] TASKS, IntVar[] HEIGHTS, IntVar CAPACITY, boolean INCREMENTAL)
```

The first API relies on the second, and set *INCREMENTAL* to `TASKS.length > 500`.

Example 1

```
1           Solver solver = new Solver();
2           Task[] TS = new Task[5];
3           IntVar[] HE = new IntVar[5];
4           for (int i = 0; i < TS.length; i++) {
5               IntVar S = VF.bounded("S_" + i, 0, 4, solver);
6               TS[i] = VF.task(
7                       S,
8                       VF.fixed("D_" + i, i + 1, solver),
9                       VF.offset(S, i + 1)
10              );
```

```
            HE[i] = VF.bounded("HE_" + i, i - 1, i + 1, solver);
        }
        IntVar CA = VF.enumerated("CA", 1, 3, solver);
        solver.post(ICF.cumulative(TS, HE, CA, true));
        solver.findAllSolutions();
```

Some solutions of the problem are :

- *S_0 = 0, HE_0 = 0, S_1 = 0, HE_1 = 0, S_2 = 0, HE_2 = 1, S_3 = 0, HE_3 = 2 S_4 = 4, HE_4 = 3, CA = 3*
- *S_0 = 4, HE_0 = 0, S_1 = 4, HE_1 = 0, S_2 = 1, HE_2 = 1, S_3 = 0, HE_3 = 2 S_4 = 4, HE_4 = 3, CA = 3*
- *S_0 = 0, HE_0 = 1, S_1 = 0, HE_1 = 0, S_2 = 1, HE_2 = 1, S_3 = 0, HE_3 = 2 S_4 = 4, HE_4 = 3, CA = 3*

16.16 diffn

The *diffn* constraint involves:

- four arrays of integer variables *X*, *Y*, *WIDTH* and *HEIGHT* and
- a boolean *USE_CUMUL*.

It ensures that each rectangle *i* defined by its coordinates (*X[i]*, *Y[i]*) and its dimensions (*WIDTH[i]*, *HEIGHT[i]*) does not overlap each other. The option *USE_CUMUL*, recommended, indicates whether or not redundant *cumulative* constraints should be added on each dimension.

See also: diffn in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint[] diffn(IntVar[] X, IntVar[] Y, IntVar[] WIDTH, IntVar[] HEIGHT, boolean USE_CUMUL)
```

Example 1

```
        Solver solver = new Solver();
        IntVar[] X = VF.boundedArray("X", 4, 0, 1, solver);
        IntVar[] Y = VF.boundedArray("Y", 4, 0, 2, solver);
        IntVar[] D = new IntVar[4];
        IntVar[] W = new IntVar[4];
        for (int i = 0; i < 4; i++) {
            D[i] = VF.fixed("D_" + i, 1, solver);
            W[i] = VF.fixed("W_" + i, i + 1, solver);
        }
        solver.post(ICF.diffn(X, Y, D, W, true));
        solver.findAllSolutions();
```

Some solutions of the problem are :

- *X[0] = 0 X[1] = 1, X[2] = 0, X[3] = 1, Y[0] = 0, Y[1] = 0, Y[2] = 1, Y[3]*
- *X[0] = 1 X[1] = 0, X[2] = 1, X[3] = 0, Y[0] = 0, Y[1] = 0, Y[2] = 2, Y[3]*
- *X[0] = 0 X[1] = 1, X[2] = 0, X[3] = 1, Y[0] = 1, Y[1] = 0, Y[2] = 2, Y[3]*

16.17 distance

The `distance` constraint involves either:

- two variables *VAR1* and *VAR2*, an operator *OP* and a constant *CSTE*. It ensures that | *VAR1* - *VAR2* | *OP CSTE*, where *OP* must be chosen in `{"=", "!=", ">","<"}` .
- or three variables *VAR1*, *VAR2* and *VAR3* and an operator *OP*. It ensures that | *VAR1* - *VAR2* | *OP VAR3*, where *OP* must be chosen in `{"=",">","<"}` .

See also: distance in the Global Constraint Catalog.

API:

```
Constraint distance(IntVar VAR1, IntVar VAR2, String OP, int CSTE)
Constraint distance(IntVar VAR1, IntVar VAR2, String OP, IntVar VAR3)
```

Example 1

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 0, 2, solver);
3          IntVar Y = VF.enumerated("X", -3, 1, solver);
4          solver.post(ICF.distance(X, Y, "=", 1));
5          solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 0, Y = -1*
- *X = 0, Y = 1*
- *X = 1, Y = 0*
- *X = 2, Y = 1*

Example 2

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 1, 3, solver);
3          IntVar Y = VF.enumerated("Y", -1, 1, solver);
4          IntVar Z = VF.enumerated("Z", 2, 3, solver);
5          solver.post(ICF.distance(X, Y, "<", Z));
6          solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 1, Y = 0, Z = 2*
- *X = 1, Y = 1, Z = 2*
- *X = 2, Y = 1, Z = 2*
- *X = 1, Y = -1, Z = 3*
- *X = 1, Y = 0, Z = 3*
- *X = 1, Y = 1, Z = 3*
- *X = 2, Y = 0, Z = 3*
- *X = 2, Y = 1, Z = 3*
- *X = 3, Y = 1, Z = 3*

16.18 element

The *element* constraint involves either:

- two variables *VALUE* and *INDEX*, an array of values *TABLE*, an offset *OFFSET* and an ordering property *SORT*. *SORT* must be chosen among:
  - `"none"`: if values in *TABLE* are not sorted,
  - `"asc"`: if values in *TABLE* are sorted in increasing order,
  - `"desc"`: if values in *TABLE* are sorted in decreasing order,
  - `"detect"`: let the constraint detects the ordering of values in *TABLE*, if any (default value).
- or an integer variable *VALUE*, an array of integer variables *TABLE*, an integer variable *INDEX* and an integer *OFFSET*.

The *element* constraint ensures that *VALUE* = *TABLE* [*INDEX* - *OFFSET*]. *OFFSET* matches *INDEX.LB* and *TABLE[0]* (0 by default).

See also: element in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint element(IntVar VALUE, int[] TABLE, IntVar INDEX)
Constraint element(IntVar VALUE, int[] TABLE, IntVar INDEX, int OFFSET, String SORT)
Constraint element(IntVar VALUE, IntVar[] TABLE, IntVar INDEX, int OFFSET)
```

Example

```
1          Solver solver = new Solver();
2          IntVar V = VF.enumerated("V", -2, 2, solver);
3          IntVar I = VF.enumerated("I", 0, 5, solver);
4          solver.post(ICF.element(V, new int[]{2, -2, 1, -1, 0}, I, 0, "none"));
5          solver.findAllSolutions();
```

The solutions of the problem are :

- *V = -2, I = 1*
- *V = -1, I = 3*
- *V = 0, I = 4*
- *V = 1, I = 2*
- *V = 2, I = 0*

16.19 eucl_div

The *eucl_div* constraints involves three variables *DIVIDEND*, *DIVISOR* and *RESULT*. It ensures that *DIVIDEND* / *DIVISOR* = *RESULT*, rounding towards 0.

The API is :

```
Constraint eucl_div(IntVar DIVIDEND, IntVar DIVISOR, IntVar RESULT)
```

Example

```
Solver solver = new Solver();
IntVar X = VF.enumerated("X", 1, 3, solver);
IntVar Y = VF.enumerated("Y", -1, 1, solver);
IntVar Z = VF.enumerated("Z", 2, 3, solver);
solver.post(ICF.eucl_div(X, Y, Z));
solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 2, Y = 1, Z = 2*
- *X = 3, Y = 1, Z = 3*

16.20 FALSE

The *FALSE* constraint is always unsatisfied. It should only be used with `LogicalFactory`.

16.21 global_cardinality

The *global_cardinality* constraint involves:

- an array of integer variables *VARS*,
- an array of integer *VALUES*,
- an array of integer variables *OCCURRENCES* and
- a boolean *CLOSED*.

It ensures that each value *VALUES[i]* is taken by exactly *OCCURRENCES[i]* variables in *VARS*. The boolean *CLOSED* set to *true* restricts the domain of *VARS* to the values defined in *VALUES*.

The underlying propagator does not ensure a well-defined level of consistency, yet.

See also: global_cardinality in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint global_cardinality(IntVar[] VARS, int[] VALUES, IntVar[] OCCURRENCES, boolean CLOSED)
```

Example

```
Solver solver = new Solver();
IntVar[] VS = VF.boundedArray("VS", 4, 0, 4, solver);
int[] values = new int[]{-1, 1, 2};
IntVar[] OCC = VF.boundedArray("OCC", 3, 0, 2, solver);
solver.post(ICF.global_cardinality(VS, values, OCC, true));
solver.findAllSolutions();
```

The solutions of the problem are :

- *VS[0] = 1, VS[1] = 1, VS[2] = 2, VS[3] = 2, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*
- *VS[0] = 1, VS[1] = 2, VS[2] = 1, VS[3] = 2, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*

- *VS[0] = 1, VS[1] = 2, VS[2] = 2, VS[3] = 1, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*
- *VS[0] = 2, VS[1] = 1, VS[2] = 1, VS[3] = 2, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*
- *VS[0] = 2, VS[1] = 1, VS[2] = 2, VS[3] = 1, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*
- *VS[0] = 2, VS[1] = 2, VS[2] = 1, VS[3] = 1, OCC[0] = 0, OCC[1] = 2, OCC[2] = 2*

16.22 inverse_channeling

The *inverse_channeling* constraint involves:

- two arrays of integer variables *VARS1* and *VARS2* and
- two integers *OFFSET1* and *OFFSET2*.

It ensures that *VARS1[i - OFFSET2] = j* $\Leftrightarrow$ *VARS2[j - OFFSET1] = i*. It performs AC if the domains are enumerated. Otherwise, BC is not guaranteed. It also automatically imposes one *alldifferent* constraints on each array of variables.

API:

```
Constraint inverse_channeling(IntVar[] VARS1, IntVar[] VARS2, int OFFSET1, int OFFSET2)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] X = VF.enumeratedArray("X", 3, 0, 3, solver);
3          IntVar[] Y = VF.enumeratedArray("Y", 3, 1, 4, solver);
4          solver.post(ICF.inverse_channeling(X, Y, 0, 1));
5          solver.findAllSolutions();
```

The solutions of the problems are:

- *X[0] = 0, X[1] = 1, X[2] = 2, Y[0] = 1, Y[1] = 2, Y[2] = 3*
- *X[0] = 0, X[1] = 2, X[2] = 1, Y[0] = 1, Y[1] = 3, Y[2] = 2*
- *X[0] = 1, X[1] = 0, X[2] = 2, Y[0] = 2, Y[1] = 1, Y[2] = 3*
- *X[0] = 1, X[1] = 2, X[2] = 0, Y[0] = 3, Y[1] = 1, Y[2] = 2*
- *X[0] = 2, X[1] = 0, X[2] = 1, Y[0] = 2, Y[1] = 3, Y[2] = 1*
- *X[0] = 2, X[1] = 1, X[2] = 0, Y[0] = 3, Y[1] = 2, Y[2] = 1*

16.23 knapsack

The *knapsack* constraint involves: - an array of integer variables *OCCURRENCES*, - an integer variable *TOTAL_WEIGHT*, - an integer variable *TOTAL_ENERGY*, - an array of integers *WEIGHT* and - an an array of integers *ENERGY*.

It formulates the Knapsack Problem: to determine the count of each item to include in a collection so that the total weight is less than or equal to a given limit and the total value is as large as possible.

- *OCCURRENCES[i]* $\times$ *WEIGHT[i]* $\leq$ *TOTAL_WEIGHT* and
- *OCCURRENCES[i]* $\times$ *ENERGY[i] = TOTAL_ENERGY*.

API:

```
Constraint knapsack(IntVar[] OCCURRENCES, IntVar TOTAL_WEIGHT, IntVar TOTAL_ENERGY,
                                    int[] WEIGHT, int[] ENERGY)
```

Example

```
1           Solver solver = new Solver();
2           IntVar[] IT = new IntVar[3]; // 3 items
3           IT[0] = VF.bounded("IT_0", 0, 3, solver);
4           IT[1] = VF.bounded("IT_1", 0, 2, solver);
5           IT[2] = VF.bounded("IT_2", 0, 1, solver);
6           IntVar WE = VF.bounded("WE", 0, 8, solver);
7           IntVar EN = VF.bounded("EN", 0, 6, solver);
8           int[] weights = new int[]{1, 3, 4};
9           int[] energies = new int[]{1, 4, 6};
10          solver.post(ICF.knapsack(IT, WE, EN, weights, energies));
11          solver.findAllSolutions();
```

Some solutions of the problems are:

- *IT_0 = 0, IT_1 = 0, IT_2 = 0, WE = 0, EN = 0*
- *IT_0 = 3, IT_1 = 0, IT_2 = 0, WE = 3, EN = 3*
- *IT_0 = 1, IT_1 = 1, IT_2 = 0, WE = 4, EN = 5*
- *IT_0 = 2, IT_1 = 1, IT_2 = 0, WE = 5, EN = 6*

16.24 lex_chain_less

The *lex_chain_less* constraint involves a matrix of integer variables *VARS*. It ensures that, for each pair of consecutive arrays *VARS[i]* and *VARS[i+1]*, *VARS[i]* is lexicographically strictly less than *VARS[i+1]*.

See also: lex_chain_less in the Global Constraint Catalog.

Implementation based on: [CB02].

API:

```
Constraint lex_chain_less(IntVar[]... VARS)
```

Example

```
1           Solver solver = new Solver();
2           IntVar[] X = VF.enumeratedArray("X", 3, -1, 1, solver);
3           IntVar[] Y = VF.enumeratedArray("Y", 3, 1, 2, solver);
4           IntVar[] Z = VF.enumeratedArray("Z", 3, 0, 2, solver);
5           solver.post(ICF.lex_chain_less(X, Y, Z));
6           solver.findAllSolutions();
```

Some solutions of the problems are:

- *X[0] = -1, X[1] = -1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 1, Z[1] = 1, Z[2] = 2*
- *X[0] = 0, X[1] = 1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 1, Z[1] = 2, Z[2] = 0*
- *X[0] = 1, X[1] = 0, X[2] = 1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 1, Z[1] = 2, Z[2] = 0*
- *X[0] = -1, X[1] = 1, X[2] = 1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 2, Z[1] = 2, Z[2] = 1*

16.25 lex_chain_less_eq

The *lex_chain_less_eq* constraint involves a matrix of integer variables *VARS*. It ensures that, for each pair of consecutive arrays *VARS[i]* and *VARS[i+1]*, *VARS[i]* is lexicographically strictly less or equal than *VARS[i+1]*.

See also: lex_chain_less_eq in the Global Constraint Catalog.

Implementation based on: [CB02].

API:

```
Constraint lex_chain_less_eq(IntVar[]... VARS)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] X = VF.enumeratedArray("X", 3, -1, 1, solver);
3          IntVar[] Y = VF.enumeratedArray("Y", 3, 1, 2, solver);
4          IntVar[] Z = VF.enumeratedArray("Z", 3, 0, 2, solver);
5          solver.post(ICF.lex_chain_less_eq(X, Y, Z));
6          solver.findAllSolutions();
```

Some solutions of the problems are:

- *X[0] = -1, X[1] = -1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 1, Z[1] = 1, Z[2] = 1*
- *X[0] = -1, X[1] = 1, X[2] = 1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 1, Z[1] = 1, Z[2] = 1*
- *X[0] = 0, X[1] = 1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1, Z[0] = 2, Z[1] = 1, Z[2] = 2*
- *X[0] = -1, X[1] = -1, X[2] = 0, Y[0] = 1, Y[1] = 1, Y[2] = 2, Z[0] = 2, Z[1] = 2, Z[2] = 2*

16.26 lex_less

The *lex_less* constraint involves two arrays of integer variables *VARS1* and *VARS2*. It ensures that *VARS1* is lexicographically strictly less than *VARS2*.

See also: lex_less in the Global Constraint Catalog.

Implementation based on: [FHK+02].

API:

```
Constraint lex_less(IntVar[] VARS1, IntVar[] VARS2)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] X = VF.enumeratedArray("X", 3, -1, 1, solver);
3          IntVar[] Y = VF.enumeratedArray("Y", 3, 1, 2, solver);
4          solver.post(ICF.lex_less(X, Y));
5          solver.findAllSolutions();
```

Some solutions of the problems are:

- *X[0] = -1, X[1] = -1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1*

- *X[0] = -1, X[1] = 0, X[2] = 0, Y[0] = 1, Y[1] = 2, Y[2] = 1*
- *X[0] = -1, X[1] = 0, X[2] = -1, Y[0] = 2, Y[1] = 1, Y[2] = 1*
- *X[0] = -1, X[1] = -1, X[2] = 0, Y[0] = 2, Y[1] = 2, Y[2] = 2*

16.27 lex_less_eq

The *lex_less_eq* constraint involves two arrays of integer variables *VARS1* and *VARS2*. It ensures that *VARS1* is lexicographically strictly less or equal than *VARS2*.

See also: lex_less_eq in the Global Constraint Catalog.

Implementation based on: [FHK+02].

API:

```
Constraint lex_less_eq(IntVar[] VARS1, IntVar[] VARS2)
```

Example

```
Solver solver = new Solver();
IntVar[] X = VF.enumeratedArray("X", 3, -1, 1, solver);
IntVar[] Y = VF.enumeratedArray("Y", 3, 1, 2, solver);
solver.post(ICF.lex_less_eq(X, Y));
solver.findAllSolutions();
```

Some solutions of the problems are:

- *X[0] = -1, X[1] = -1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1*
- *X[0] = 1, X[1] = -1, X[2] = -1, Y[0] = 1, Y[1] = 1, Y[2] = 1*
- *X[0] = 0, X[1] = 0, X[2] = 0, Y[0] = 2, Y[1] = 1, Y[2] = 2*
- *X[0] = 1, X[1] = 1, X[2] = 1, Y[0] = 2, Y[1] = 2, Y[2] = 2*

16.28 maximum

The *maximum* constraints involves a set of integer variables and a third party integer variable, either:

- two integer variables *VAR1* and *VAR2* and an integer variable *MAX*, it ensures that *MAX*‘= *maximum(*‘*VAR1*, *VAR2*).
- or an array of integer variables *VARS* and an integer variable *MAX*, it ensures that *MAX* is the maximum value of the collection of domain variables *VARS*.
- or an array of boolean variables *BVARS* and a booean variable *MAX*, it ensures that *MAX* is the maximum value of the collection of boolean variables *BVARS*.

See also: maximum in the Global Constraint Catalog.

API: :: Constraint maximum(IntVar MAX, IntVar VAR1, IntVar VAR2) Constraint maximum(IntVar MAX, IntVar[] VARS) Constraint maximum(BoolVar MAX, BoolVar[] VARS)

Example

```
Solver solver = new Solver();
IntVar MAX = VF.enumerated("MAX", 1, 3, solver);
IntVar Y = VF.enumerated("Y", -1, 1, solver);
IntVar Z = VF.enumerated("Z", 2, 3, solver);
solver.post(ICF.maximum(MAX, Y, Z));
solver.findAllSolutions();
```

The solutions of the problem are :

- *MAX = 2, Y = -1, Z = 2*
- *MAX = 2, Y = 0, Z = 2*
- *MAX = 2, Y = 1, Z = 2*
- *MAX = 3, Y = -1, Z = 3*
- *MAX = 3, Y = 0, Z = 3*
- *MAX = 3, Y = 1, Z = 3*

16.29 member

A constraint which restricts the values a variable can be assigned to with respect to either:

- a given list of values, it involves a integer variable *VAR* and an array of distinct values *TABLE*. It ensures that *VAR* takes its values in *TABLE*.
- or two bounds (included), it involves a integer variable *VAR* and two integer *LB* and *UB*. It ensures that *VAR* takes its values in [*LB*, *UB*].

API:

```
Constraint member(IntVar VAR, int[] TABLE)
Constraint member(IntVar VAR, int LB, int UB)
```

Example 1

```
Solver solver = new Solver();
IntVar X = VF.enumerated("X", 1, 4, solver);
solver.post(ICF.member(X, new int[]{-2, -1, 0, 1, 2}));
solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 1*
- *X = 2*

Example 2

```
Solver solver = new Solver();
IntVar X = VF.enumerated("X", 1, 4, solver);
solver.post(ICF.member(X, 2, 5));
solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 2*

- *X = 3*
- *X = 4*

16.30 minimum

The *minimum* constraints involves a set of integer variables and a third party integer variable, either:

- two integer variables *VAR1* and *VAR2* and an integer variable *MIN*, it ensures that *MIN*‘= *minimum(*‘*VAR1*, *VAR2*).
- or an array of integer variables *VARS* and an integer variable *MIN*, it ensures that *MIN* is the minimum value of the collection of domain variables *VARS*.
- or an array of boolean variables *BVARS* and a booean variable *MIN*, it ensures that *MIN* is the minimum value of the collection of boolean variables *BVARS*.

See also: minimum in the Global Constraint Catalog.

API: :: Constraint minimum(IntVar MIN, IntVar VAR1, IntVar VAR2) Constraint minimum(IntVar MIN, IntVar[] VARS) Constraint minimum(BoolVar MIN, BoolVar[] VARS)

Example

```
1         Solver solver = new Solver();
2         IntVar MIN = VF.enumerated("MIN", 1, 3, solver);
3         IntVar Y = VF.enumerated("Y", -1, 1, solver);
4         IntVar Z = VF.enumerated("Z", 2, 3, solver);
5         solver.post(ICF.minimum(MIN, Y, Z));
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *MIN = 2, Y = -1, Z = 2*
- *MIN = 2, Y = 0, Z = 2*
- *MIN = 2, Y = 1, Z = 2*
- *MIN = 3, Y = -1, Z = 3*
- *MIN = 3, Y = 0, Z = 3*
- *MIN = 3, Y = 1, Z = 3*

16.31 mod

The *mod* constraints involves three variables *X*, *Y* and *Z*. It ensures that $X \mod Y = Z$. There is no native constraint for *mod*, so this is reformulated with the help of additional variables.

The API is :

```
Constraint mod(IntVar X, IntVar Y, IntVar Z)
```

Example

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 2, 4, solver);
3          IntVar Y = VF.enumerated("Y", -1, 4, solver);
4          IntVar Z = VF.enumerated("Z", 1, 3, solver);
5          solver.post(ICF.mod(X, Y, Z));
6          solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 2, Y = 3, Z = 2*
- *X = 2, Y = 4, Z = 2*
- *X = 3, Y = 2, Z = 1*
- *X = 3, Y = 4, Z = 3*
- *X = 4, Y = 3, Z = 1*

16.32 multicost_regular

The *multicost_regular* constraint involves:

- an array of integer variables *VARS*,
- an array of integer variables *CVARS* and
- a cost automaton *CAUTOMATON*.

It ensures that the assignment of a sequence of variables *VARS* is recognized by *CAUTOMATON*, a deterministic finite automaton, and that the sum of the cost array associated to each assignment is bounded by the *CVARS*. This version allows to specify different costs according to the automaton state at which the assignment occurs (i.e. the transition starts).

The *CAUOTMATON* can be defined using the ‘‘solver.constraints.nary.automata.FA.CostAutomaton‘ either:

- by creating a `CostAutomaton`: once created, states should be added, then initial and final states are defined and finally, transitions are declared.
- or by first creating a `FiniteAutomaton` and then creating a matrix of costs and finally calling one of the following API from `CostAutomaton`:
  - `ICostAutomaton makeMultiResources(IAutomaton pi, int[][][] layer_value_resource, int[] infs, int[] sups)`
  - `ICostAutomaton makeMultiResources(IAutomaton pi, int[][][][] layer_value_resource_state, int[] infs, int[] sups)`
  - `ICostAutomaton makeMultiResources(IAutomaton auto, int[][][][] c, IntVar[] z)`
  - `ICostAutomaton makeMultiResources(IAutomaton auto, int[][][] c, IntVar[] z)`

  The other API of `CostAutomaton` (`makeSingleResource(...)`) are dedicated to the *cost_regular* constraint.

Implementation based on: [MD09].

API:

```
Constraint multicost_regular(IntVar[] VARS, IntVar[] CVARS, ICostAutomaton CAUTOMATON)
```

Example

TBD

16.33 not_member

A constraint which prevents a variable to be assigned to some values defined by either:

- a list of values, it involves a integer variable *VAR* and an array of distinct values *TABLE*. It ensures that *VAR* does not take its values in *TABLE*.
- two bounds (included), it involves a integer variable *VAR* and two integer *LB* and *UB*. It ensures that *VAR* does not take its values in [*LB*, *UB*].

The constraint

API:

```
Constraint not_member(IntVar VAR, int[] TABLE)
Constraint not_member(IntVar VAR, int LB, int UB)
```

Example 1

```
1         Solver solver = new Solver();
2         IntVar X = VF.enumerated("X", 1, 4, solver);
3         solver.post(ICF.not_member(X, new int[]{-2, -1, 0, 1, 2}));
4         solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 3*
- *X = 4*

Example

```
1         Solver solver = new Solver();
2         IntVar X = VF.enumerated("X", 1, 4, solver);
3         solver.post(ICF.not_member(X, 2, 5));
4         solver.findAllSolutions();
```

The solution of the problem is :

- *X = 1*

16.34 nvalues

The *nvalues* constraint involves:

- an array of integer variables *VARS* and
- an integer variable *NVALUES*.

The constraint ensures that *NVALUES* is the number of distinct values assigned to the variables of the *VARS* array. This constraint is a combination of the *atleast_nvalues* and *atmost_nvalues* constraints.

This constraint is not a built-in constraint and is based on various propagators.

See also: nvalues in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint[] nvalues(IntVar[] VARS, IntVar NVALUES)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 2, solver);
3         IntVar N = VF.enumerated("N", 0, 3, solver);
4         solver.post(ICF.nvalues(VS, N));
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 0 VS[1] = 0 VS[2] = 0 VS[3] = 0 N = 1*
- *VS[0] = 0 VS[1] = 0 VS[2] = 0 VS[3] = 1 N = 2*
- *VS[0] = 0 VS[1] = 1 VS[2] = 2 VS[3] = 2 N = 3*

16.35 path

The *path* constraint involves:

- an array of integer variables *VARS*,
- an integer variable *START*,
- an integer variable *END* and
- an integer *OFFSET*.

It ensures that the elements of *VARS* define a covering path from *START* to *END*, where *VARS[i] = OFFSET + j* means that *j* is the successor of *i*. Moreover, *VARS[END-OFFSET] =* |‘VARS‘ |+ *OFFSET*. The constraint relies on the *circuit* propagators.

See also: path in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint[] path(IntVar[] VARS, IntVar START, IntVar END, int OFFSET)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 4, solver);
3         IntVar S = VF.enumerated("S", 0, 3, solver);
4         IntVar E = VF.enumerated("E", 0, 3, solver);
5         solver.post(ICF.path(VS, S, E, 0));
6         solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 1, VS[1] = 2, VS[2] = 3, VS[3] = 4, S = 0, E = 3*
- *VS[0] = 1, VS[1] = 3, VS[2] = 0, VS[3] = 4, S = 2, E = 3*
- *VS[0] = 3, VS[1] = 4, VS[2] = 0, VS[3] = 1, S = 2, E = 1*
- *VS[0] = 4, VS[1] = 3, VS[2] = 1, VS[3] = 0, S = 2, E = 0*

16.36 regular

The *regular* constraint involves:

- an array of integer variables *VARS* and
- a deterministic finite automaton *AUTOMATON*.

It enforces the sequences of *VARS* to be a word recognized by *AUTOMATON*.

There are various ways to declare the automaton:

- create a `FiniteAutomaton` and add states, initial and final ones and transitions (see `FiniteAutomaton` API for more details),
- create a `FiniteAutomaton` with a regexp as argument.

Implementation based on: [Pes04]. **API**:

```
Constraint regular(IntVar[] VARS, IAutomaton AUTOMATON)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] CS = VF.enumeratedArray("CS", 4, 1, 5, solver);
3         solver.post(ICF.regular(CS,
4                 new FiniteAutomaton("(1|2)(3*)(4|5)")));
5         solver.findAllSolutions();
```

The solutions of the problem are :

- *CS[0] = 1, CS[1] = 3, CS[2] = 3, CS[3] = 4*
- *CS[0] = 1, CS[1] = 3, CS[2] = 3, CS[3] = 5*
- *CS[0] = 2, CS[1] = 3, CS[2] = 3, CS[3] = 4*
- *CS[0] = 2, CS[1] = 3, CS[2] = 3, CS[3] = 5*

16.37 scalar

The *scalar* constraint involves:

- an array of integer variables *VARS*,
- an array of integer *COEFFS*,
- an optional operator *OPERATOR* and
- an integer variable *SCALAR*.

It ensures that *sum(VARS[i]*COEFFS[i]) OPERATOR SCALAR*; where *OPERATOR* must be chosen from {"=", "!=", ">","<",">=","<="}. The *scalar* constraint filters on bounds only. The constraint suppress variables with coefficients set to 0, recognizes *sum* (when all coefficients are equal to *-1*, or all equal to *-1*), and enables, under certain conditions, to reformulate the constraint with a *table* constraint providint AC filtering algorithm.

See also: scalar_product in the Global Constraint Catalog.

Implementation based on: [HS02].

API:

```
Constraint scalar(IntVar[] VARS, int[] COEFFS, IntVar SCALAR)
Constraint scalar(IntVar[] VARS, int[] COEFFS, String OPERATOR, IntVar SCALAR)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] CS = VF.enumeratedArray("CS", 4, 1, 4, solver);
3         int[] coeffs = new int[]{1, 2, 3, 4};
4         IntVar R = VF.bounded("R", 0, 20, solver);
5         solver.post(ICF.scalar(CS, coeffs, R));
6         solver.findAllSolutions();
```

Some solutions of the problem are :

- *CS[0] = 1, CS[1] = 1, CS[2] = 1, CS[3] = 1, R = 10*
- *CS[0] = 1, CS[1] = 2, CS[2] = 3, CS[3] = 1, R = 18*
- *CS[0] = 1, CS[1] = 4, CS[2] = 2, CS[3] = 1, R = 19*
- *CS[0] = 1, CS[1] = 2, CS[2] = 1, CS[3] = 3, R = 20*

16.38 sort

The *sort* constraint involves two arrays of integer variables *VARS* and *SORTEDVARS*. It ensures that the variables of *SORTEDVARS* correspond to the variables of *VARS* according to a permutation. Moreover, the variable of *SORTEDVARS* are sorted in increasing order.

See also: sort in the Global Constraint Catalog.

Implementation based on: [MT00].

API:

```
Constraint sort(IntVar[] VARS, IntVar[] SORTEDVARS)
```

Example

```
1         Solver solver = new Solver();
2         IntVar[] X = VF.enumeratedArray("X", 3, 0, 2, solver);
3         IntVar[] Y = VF.enumeratedArray("Y", 3, 0, 2, solver);
4         solver.post(ICF.sort(X, Y));
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *X[0] = 0, X[1] = 0, X[2] = 0, Y[0] = 0, Y[1] = 0, Y[2] = 0*
- *X[0] = 1, X[1] = 0, X[2] = 2, Y[0] = 0, Y[1] = 1, Y[2] = 2*

- *X[0] = 2, X[1] = 1, X[2] = 0, Y[0] = 0, Y[1] = 1, Y[2] = 2*
- *X[0] = 2, X[1] = 1, X[2] = 2, Y[0] = 1, Y[1] = 2, Y[2] = 2*

16.39 square

The `square` constraint involves two variables *VAR1* and *VAR2*. It ensures that *VAR1* = *VAR2*^{2}.

API:

```
Constraint square(IntVar VAR1, IntVar VAR2)
```

Example

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 0, 5, solver);
3          IntVar Y = VF.enumerated("Y", -1, 3, solver);
4          solver.post(ICF.square(X, Y));
5          solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 1, Y = -1*
- *X = 0, Y = 0*
- *X = 1, Y = 1*
- *X = 4, Y = 2*

16.40 subcircuit

The *subcircuit* constraint involves:

- an array of integer variables *VARS*,
- an integer *OFFSET* and
- an integer variable *SUBCIRCUIT_SIZE*.

It ensures that the elements of *VARS* define a single circuit of *SUBCIRCUIT_SIZE* nodes where:

- *VARS[i] = OFFSET+j* means that *j* is the successor of *i*,
- *VARS[i] = OFFSET+i* means that *i* is not part of the circuit.

It also ensures that $|\{VARS[i] \neq OFFSET+i\}| = SUBCIRCUIT\_SIZE$.

API:

```
Constraint subcircuit(IntVar[] VARS, int OFFSET, IntVar SUBCIRCUIT_SIZE)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] NODES = VF.enumeratedArray("NS", 5, 0, 4, solver);
3          IntVar SI = VF.enumerated("SI", 2, 3, solver);
```

```
4           solver.post(ICF.subcircuit(NODES, 0, SI));
5           solver.findAllSolutions();
```

Some solutions of the problem are :

- *NS[0] = 0, NS[1] = 1, NS[2] = 2, NS[3] = 4, NS[4] = 3, SI = 2*
- *NS[0] = 4, NS[1] = 1, NS[2] = 2, NS[3] = 3, NS[4] = 0, SI = 2*
- *NS[0] = 1, NS[1] = 2, NS[2] = 0, NS[3] = 3, NS[4] = 4, SI = 3*
- *NS[0] = 3, NS[1] = 1, NS[2] = 2, NS[3] = 4, NS[4] = 0, SI = 3*

16.41 subpath

The *subpath* constraint involves:

- an array of integer variables *VARS*,
- an integer variable *START*,
- an integer variable *END*,
- an integer *OFFSET* and
- an integer variable *SIZE*.

It ensures that the elements of *VARS* define a path of *SIZE* vertices, leading from *START* to *END* where:

- *VARS[i] = OFFSET+j* means that *j* is the successor of *i*,
- *VARS[i] = OFFSET+i* means that vertex *i* is excluded from the path.

Moreover, *VARS[END-OFFSET]* = | *VARS* | +'OFFSET'.

See also: subpath in the Global Constraint Catalog.

Implementation based on: [tbd].

API:

```
Constraint[] subpath(IntVar[] VARS, IntVar START, IntVar END, int OFFSET, IntVar SIZE)
```

Example

```
1           Solver solver = new Solver();
2           IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 4, solver);
3           IntVar S = VF.enumerated("S", 0, 3, solver);
4           IntVar E = VF.enumerated("E", 0, 3, solver);
5           IntVar SI = VF.enumerated("SI", 2, 3, solver);
6           solver.post(ICF.subpath(VS, S, E, 0, SI));
7           solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 1, VS[1] = 4, VS[2] = 2, VS[3] = 3, S = 0, E = 1, SI = 2*
- *VS[0] = 4, VS[1] = 1, VS[2] = 2, VS[3] = 0, S = 3, E = 0, SI = 2*
- *VS[0] = 3, VS[1] = 1, VS[2] = 4, VS[3] = 2, S = 0, E = 2, SI = 3*
- *VS[0] = 0, VS[1] = 2, VS[2] = 4, VS[3] = 1, S = 3, E = 2, SI = 3*

16.42 sum

The *sum* constraint involves:

- an array of integer (or boolean) variables *VARS*,
- an optional operator *OPERATOR* and
- an integer variable *SUM*.

It ensures that *sum(VARS[i]) OPERATOR SUM*; where operator must be chosen among `{"=", "!=", ">","<",">=","<="}`. If no operator is defined, `"="` is set by default. Note that when the operator differs from `"="`, an intermediate variable is declared and an *arithm* constraint is returned. For performance reasons, a specialization for boolean variables is provided.

See also: scalar_product in the Global Constraint Catalog.

Implementation based on: [HS02].

API:

```
Constraint sum(IntVar[] VARS, IntVar SUM)
Constraint sum(IntVar[] VARS, String OPERATOR, IntVar SUM)
Constraint sum(BoolVar[] VARS, IntVar SUM)
Constraint sum(BoolVar[] VARS, String OPERATOR, IntVar SUM)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 4, solver);
3          IntVar SU = VF.enumerated("SU", 2, 3, solver);
4          solver.post(ICF.sum(VS, "<=", SU));
5          solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 0 VS[1] = 0 VS[2] = 0 VS[3] = 0 SU = 2*
- *VS[0] = 0 VS[1] = 0 VS[2] = 0 VS[3] = 2 SU = 2*
- *VS[0] = 0 VS[1] = 0 VS[2] = 0 VS[3] = 3 SU = 3*
- *VS[0] = 1 VS[1] = 1 VS[2] = 0 VS[3] = 0 SU = 3*

16.43 table

The `table` constraint involves either:

- two variables *VAR1* and *VAR2*, a list of pair of values, named *TUPLES* and an algorithm *ALGORITHM*.
- or an array of variables *VARS*, a list of tuples of values, named *TUPLES* and an algorithm *ALGORITHM*.

It is an extensional constraint enforcing, most of the time, arc-consistency.

When only two variables are involved, the available algorithms are:

- `"AC2001"`: applies the AC2001 algorithm,
- `"AC3"`: applies the AC3 algorithm,
- `"AC3rm"`: applies the AC3rm algorithm,

- "AC3bit+rm": (default) applies the AC3bit+rm algorithm,
- "FC": applies the forward checking algorithm.

When more than two variables are involved, the available algorithms are:

- "GAC2001": applies the GAC2001 algorithm,
- "GAC2001+": applies the GAC2001 algorithm for allowed tuples only,
- "GAC3rm": applies the GAC3 algorithm,
- "GAC3rm+": (default) applies the GAC3rm algorithm for allowed tuples only,
- "GACSTR+": applies the GAC version STR for allowed tuples only,
- "STR2+": applies the GAC STR2 algorithm for allowed tuples only,
- "FC": applies the forward checking algorithm.

Implementation based on: [tbd].

API:

```
Constraint table(IntVar VAR1, IntVar VAR2, Tuples TUPLES, String ALGORITHM)
Constraint table(IntVar[] VARS, Tuples TUPLES, String ALGORITHM)
```

Example

```
1          Solver solver = new Solver();
2          IntVar X = VF.enumerated("X", 0, 5, solver);
3          IntVar Y = VF.enumerated("Y", -1, 3, solver);
4          Tuples tuples = new Tuples(true);
5          tuples.add(1, -2);
6          tuples.add(1, 1);
7          tuples.add(4, 2);
8          tuples.add(1, 4);
9          solver.post(ICF.table(X, Y, tuples, "AC2001"));
10         solver.findAllSolutions();
```

The solutions of the problem are :

- *X = 1, Y = 1*
- *X = 4, Y = 2*

16.44 times

The *times* constraints involves either:

- three variables X, Y and Z. It ensures that $X \times Y = Z$.
- or two variables X and Z and a constant y. It ensures that $X \times y = Z$.

The propagator of the *times* constraint filters on bounds only. If the option is enabled and under certain condition, the *times* constraint may be redefined with a *table* constraint, providing a better filtering algorithm.

The API are :

```
Constraint times(IntVar X, IntVar Y, IntVar Z)
Constraint times(IntVar X, int Y, IntVar Z)
```

Example

```
Solver solver = new Solver();
IntVar X = VF.enumerated("X", -1, 2, solver);
IntVar Y = VF.enumerated("Y", 2, 4, solver);
IntVar Z = VF.enumerated("Z", 5, 7, solver);
solver.post(ICF.times(X, Y, Z));
solver.findAllSolutions();
```

The solution of the problem is :

- *X = 2 Y = 3 Z = 6*

16.45 tree

The *tree* constraint involves:

- an array of integer variables *SUCCS*,
- an integer variable *NBTREES* and
- an integer *OFFSET*.

It partitions the *SUCCS* variables into *NBTREES* (anti) arborescences:

- *SUCCS[i] = OFFSET+j* means that *j* is the successor of *i*,
- *SUCCS[i] = OFFSET+i* means that *i* is a root.

See also: tree in the Global Constraint Catalog.

Implementation based on: [FL11].

API:

```
Constraint tree(IntVar[] SUCCS, IntVar NBTREES, int OFFSET)
```

Example

```
Solver solver = new Solver();
IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 4, solver);
IntVar NT = VF.enumerated("NT", 2, 3, solver);
solver.post(ICF.tree(VS, NT, 0));
solver.findAllSolutions();
```

Some solutions of the problem are :

- *VS[0] = 0, VS[1] = 1, VS[2] = 1, VS[3] = 1, NT = 2*
- *VS[0] = 1, VS[1] = 1, VS[2] = 2, VS[3] = 1, NT = 2*
- *VS[0] = 2, VS[1] = 0, VS[2] = 2, VS[3] = 3, NT = 2*
- *VS[0] = 0, VS[1] = 3, VS[2] = 2, VS[3] = 3, NT = 3*
- *VS[0] = 3, VS[1] = 1, VS[2] = 2, VS[3] = 3, NT = 3*

16.46 TRUE

The *TRUE* constraint is always satisfied. It should only be used with `LogicalFactory`.

16.47 tsp

The *tsp* constraint involves:

- an array of integer variables *SUCCS*,
- an integer variable *COST* and
- a matrix of integers *COST_MATRIX*.

It formulates the Travelling Salesman Problem: the variables *SUCCS* form a hamiltonian circuit of value *COST*. Going from *i* to *j*, *SUCCS[i] = j*, costs *COST_MATRIX[i][j]*.

This constraint is not a built-in constraint and is based on various propagators.

API:

```
Constraint[] tsp(IntVar[] SUCCS, IntVar COST, int[][] COST_MATRIX)
```

Example

```
1          Solver solver = new Solver();
2          IntVar[] VS = VF.enumeratedArray("VS", 4, 0, 4, solver);
3          IntVar CO = VF.enumerated("CO", 0, 15, solver);
4          int[][] costs = new int[][]{{0, 1, 3, 7}, {1, 0, 1, 3}, {3, 1, 0, 1}, {7, 3, 1, 0}};
5          solver.post(ICF.tsp(VS, CO, costs));
6          solver.findAllSolutions();
```

The solutions of the problem are :

- *VS[0] = 2, VS[1] = 0, VS[2] = 3, VS[3] = 1, CO = 8*
- *VS[0] = 3, VS[1] = 0, VS[2] = 1, VS[3] = 2, CO = 10*
- *VS[0] = 1, VS[1] = 2, VS[2] = 3, VS[3] = 0, CO = 10*
- *VS[0] = 3, VS[1] = 2, VS[2] = 0, VS[3] = 1, CO = 14*
- *VS[0] = 1, VS[1] = 3, VS[2] = 0, VS[3] = 2, CO = 8*
- *VS[0] = 2, VS[1] = 3, VS[2] = 1, VS[3] = 0, CO = 14*

CHAPTER 17

Constraints over set variables

17.1 all_different

The *all_different* constraint involves an array of set variables *SETS*. It ensures that sets in *SETS* are all different (not necessarily disjoint). Note that there cannot be more than two empty sets.

API:

```
Constraint all_different(SetVar[] SETS)
```

17.2 all_disjoint

The *all_disjoint* constraint involves an array of set variables *SETS*. It ensures that all sets from *SETS* are disjoint. Note that there can be multiple empty sets.

API:

```
Constraint all_disjoint(SetVar[] SETS)
```

17.3 all_equal

The *all_equal* constraint involves an array of set variables *SETS*. It ensures that sets in *SETS* are all equal.

API:

```
Constraint all_equal(SetVar[] SETS)
```

17.4 bool_channel

The *bool_channel* constraint involves:

- an array of boolean variables *BOOLEANS*,
- a set variable *SET* and
- an integer *OFFSET*.

It channels *BOOLEANS* and *SET* such that : $i \in$ SET $\Leftrightarrow$ *BOOLEANS[i-OFFSET] = 1*.

API:

```
Constraint bool_channel(BoolVar[] BOOLEANS, SetVar SET, int OFFSET)
```

17.5 cardinality

The *cardinality* constraint involves:

- a set variable *SET* and
- an integer variable *CARD*.

It ensures that | *SET_VAR* | = *CARD*.

The API is :

```
Constraint cardinality(SetVar SET, IntVar CARD)
```

17.6 disjoint

The *disjoint* constraint involves two set variables *SET_1* and *SET_2*. It ensures that *SET_1* and *SET_2* are disjoint, that is, they cannot contain the same element. Note that they can be both empty.

API:

```
Constraint disjoint(SetVar SET_1, SetVar SET_2)
```

17.7 element

The *element* constraint involves:

- an integer variable *INDEX*,
- and array of set variables *SETS*,
- an integer *OFFSET* and
- a set variable *SET*.

It ensures that *SETS[INDEX-OFFSET] = SET*.

API:

```
Constraint element(IntVar INDEX, SetVar[] SETS, int OFFSET, SetVar SET)
```

17.8 int_channel

The *int_channel* constraint involves:

- an array of set variables *SETS*,
- an array of integer variables *INTEGERS*,

- two integers *OFFSET_1* and *OFFSET_2*.

It ensures that: *x* ∈ *SETS[y-OFFSET_1]* ⇔ *INTEGERS[x-OFFSET_2]* = *y*.

The API is :

```
Constraint int_channel(SetVar[] SETS, IntVar[] INTEGERS, int OFFSET_1, int OFFSET_2)
```

17.9 int_values_union

The *int_values_union* constraint involves:

- an array of integer variables *VARS* and
- a set variable *VALUES*

It ensures that: $\text{VALUES} = \text{VARS}_1 \cup \text{VARS}_2 \cup \ldots \cup \text{VARS}_n$.

The API is :

```
Constraint int_values_union(IntVar[] VARS, SetVar VALUES)
```

17.10 intersection

The *intersection* constraint involves:

- an array of set variables *SETS* and
- a set variable *INTERSECTION*.

It ensures that *INTERSECTION* is the intersection of the sets *SETS*.

The API is :

```
Constraint intersection(SetVar[] SETS, SetVar INTERSECTION)
```

17.11 inverse_set

The *inverse_set* constraint involves:

- an array of set variables *SETS*,
- an array of set variable *INVERSE_SETS* and
- two integers *OFFSET_1* and *OFFSET_2*.

It ensures that *x :math:*in‘ *SETS[y-OFFSET_1]* ⇔ y ∈ *INVERSE_SETS[x-OFFSET_2]*.

API:

```
Constraint inverse_set(SetVar[] SETS, SetVar[] INVERSE_SETS, int OFFSET_1, int OFFSET_2)
```

17.12 max

The *max* constraint involves:

- either:
  - a set variable *SET*,
  - an integer variable *MAX_ELEMENT_VALUE* and
  - a boolean *NOT_EMPTY*.

  It ensures that *MIN_ELEMENT_VALUE* is equal to the maximum element of *SET*.
- or:
  - a set variable *SET*,
  - an array of integer *WEIGHTS*,
  - an integer *OFFSET*,
  - an integer variable *MAX_ELEMENT_VALUE* and
  - a boolean *NOT_EMPTY*.

  It ensures that *max(WEIGHTS[i-OFFSET] | i in INDEXES) = MAX_ELEMENT_VALUE*.

The boolean *NOT_EMPTY* set to *true* states that *INDEXES* cannot be empty.

API:

```
Constraint max(SetVar SET, IntVar MAX_ELEMENT_VALUE, boolean NOT_EMPTY)
Constraint max(SetVar INDEXES, int[] WEIGHTS, int OFFSET, IntVar MAX_ELEMENT_VALUE, boolean NOT_EMPTY
```

17.13 member

The *member* constraint involves:

- either:
  - an array of set variables *SETS* and
  - a set variable *SET*.

  It ensures that *SET* belongs to *SETS*.
- or:
  - an integer variable *INTEGER* and
  - a set variable *SET*.

  It ensures that *INTEGER* is included in *SET*.

API:

```
Constraint member(SetVar[] SETS, SetVar SET)
Constraint member(IntVar INTEGER, SetVar SET)
```

17.14 min

The *min* constraint involves:

- either:
  - a set variable *SET*,
  - an integer variable *MIN_ELEMENT_VALUE* and
  - a boolean *NOT_EMPTY*.

  It ensures that *MIN_ELEMENT_VALUE* is equal to the minimum element of *SET*.
- or:
  - a set variable *SET*,
  - an array of integer *WEIGHTS*,
  - an integer *OFFSET*,
  - an integer variable *MAX_ELEMENT_VALUE* and
  - a boolean *NOT_EMPTY*.

  It ensures that *min(WEIGHTS[i-OFFSET] | i in INDEXES) = MIN_ELEMENT_VALUE*.

The boolean *NOT_EMPTY* set to *true* states that *INDEXES* cannot be empty.

API:

```
Constraint min(SetVar SET, IntVar MIN_ELEMENT_VALUE, boolean NOT_EMPTY)
Constraint min(SetVar INDEXES, int[] WEIGHTS, int OFFSET, IntVar MIN_ELEMENT_VALUE, boolean NOT_EMPTY
```

17.15 nbEmpty

The *nbEmpty* constraint involves:

- an array of set variables *SETS* and
- an integer variable *NB_EMPTY_SETS*.

It restricts the number of empty sets in *SETS* to be equal *NB_EMPTY_SET*.

API:

```
Constraint nbEmpty(SetVar[] SETS, IntVar NB_EMPTY_SETS)
```

17.16 notEmpty

The *notEmpty* constraint involves a set variable *SET*.

It prevents *SET* to be empty.

API:

```
Constraint notEmpty(SetVar SET)
```

17.17 offSet

The *offset* constraint involves:

- two set variables *SET_1* and *SET_2* and
- an integer *OFFSET*.

It ensures that to any value *x* in *SET_1*, the value *x+OFFSET* is in *SET_2* (and reciprocally).

API:

```
Constraint offSet(SetVar SET_1, SetVar SET_2, int OFFSET)
```

17.18 partition

The *partition* constraint involves:

- an array of set variables *SETS* and
- a set variable *UNIVERSE*.

It ensures that *UNVIVERSE* is partitioned in disjoint sets *SETS*.

API:

```
Constraint partition(SetVar[] SETS, SetVar UNIVERSE)
```

17.19 subsetEq

The *subsetEq* constraint involves an array of set variables *SETS*. It ensures that $i<j \Leftrightarrow SET\_VARS[i] \subseteq SET\_VARS[j]$.

The API is :

```
Constraint subsetEq(SetVar[] SETS)
```

17.20 sum

The *sum* constraint involves:

- a set variables *INDEXES*,
- an array of integer *WEIGHTS*,
- an integer *OFFSET*,
- an integer variable *SUM* and
- a boolean *NOT_EMPTY*.

The constraint ensures that *sum(WEIGHTS[i-OFFSET] | i in INDEXES) = SUM*. The boolean *NOT_EMPTY* set to *true* states that *INDEXES* cannot be empty.

API:

```
Constraint sum(SetVar INDEXES, int[] WEIGHTS, int OFFSET, IntVar SUM, boolean NOT_EMPTY)
```

17.21 symmetric

The *symmetric* constraint involves:

- an array of set variables *SETS* and
- an integer *OFFSET*.

It ensures that: $x \in SETS[y\text{-}OFFSET] \Leftrightarrow y \in SETS[x\text{-}OFFSET]$.

API:

```
Constraint symmetric(SetVar[] SETS, int OFFSET)
```

17.22 union

The *union* constraint involves:

- an array of set variables *SETS* and
- a set variable *UNION*.

It ensures that *SET_UNION* is equal to the union if the sets in *SET_VARS*.

The API is :

```
Constraint union(SetVar[] SETS, SetVar UNION)
```

CHAPTER 18

Constraints over real variables

Real constraints are managed externally with *Ibex*. Due to the limited number of declaration possibilities, there is no factory for real constraints. Indeed, posting a `RealConstraint` is enough.

The available constructors are:

```
RealConstraint(String name, String functions, int option, RealVar... rvars)
RealConstraint(String name, String functions, RealVar... rvars)
RealConstraint(String functions, RealVar... rvars)
```

- `name` enables to set a name to the constraint.
- `functions` is a `String` which defines the list of functions to hold, separated with semi-colon ";".

A function is a declared using the following format:

- the '{i}' tag defines a variable, where 'i' is an explicit index the array of variables `rvars`,
- one or more operators :'+,-,*,/,=,<,>,<=,>=,exp( ),ln( ),max( ),min( ),abs( ),cos( ), sin( ),...'

A complete list is available in the documentation of IBEX. - `rvars` is the list of involved real variables. - `option` is enable to state the propagation option (default is `Ibex.COMPO`).

Example

```
1         Solver solver = new Solver();
2         double PREC = 0.01d; // precision
3         RealVar x = VariableFactory.real("x", -1.0d, 1.0d, PREC, solver);
4         RealVar y = VariableFactory.real("y", -1.0d, 1.0d, PREC, solver);
5         RealConstraint rc = new RealConstraint(
6                 "my fct",
7                 "({0}*{1})+sin({0})=1.0;ln({0}+[-0.1,0.1])>=2.6",
8                 Ibex.HC4,
9                 x, y);
10        solver.post(rc);
11        solver.findSolution();
```

CHAPTER 19

Logical constraints

CHAPTER 20

Sat solver

20.1 addAtMostNMinusOne

Add a clause to the SAT constraint whic states that: $BOOLVARS_1 + BOOLVARS_2 + ... + BOOLVARS_n < |BOOLVARS|$.

API:

```
boolean addAtMostNMinusOne(BoolVar[] BOOLVARS)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
3         SatFactory.addAtMostNMinusOne(BVARS);
4         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, BS[3] = 0*
- *BS[0] = 1, BS[1] = 0, BS[2] = 1, BS[3] = 0*
- *BS[0] = 0, BS[1] = 1, BS[2] = 1, BS[3] = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 0*

20.2 addAtMostOne

Add a clause to the SAT constraint whic states that: $BOOLVARS_1 + BOOLVARS_2 + ... + BOOLVARS_n \leq 1$.

API:

```
boolean addAtMostOne(BoolVar[] BOOLVARS)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
3         SatFactory.addAtMostOne(BVARS);
4         solver.findAllSolutions();
```

The solutions of the problem are :

- *BS[0] = 1, BS[1] = 0, BS[2] = 0, BS[3] = 0*
- *BS[0] = 0, BS[1] = 1, BS[2] = 0, BS[3] = 0*
- *BS[0] = 0, BS[1] = 0, BS[2] = 1, BS[3] = 0*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 0*

20.3 addBoolAndArrayEqualFalse

Add a clause to the SAT constraint whic states that: $|not`(`BOOLVARS_1 \wedge BOOLVARS_2 \wedge ... \wedge BOOLVARS_n)$.

API:

boolean addBoolAndArrayEqualFalse(BoolVar[] BOOLVARS)

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
3         SatFactory.addBoolAndArrayEqualFalse(BVARS);
4         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, BS[3] = 0*
- *BS[0] = 1, BS[1] = 0, BS[2] = 1, BS[3] = 1*
- *BS[0] = 1, BS[1] = 0, BS[2] = 0, BS[3] = 0*
- *BS[0] = 0, BS[1] = 1, BS[2] = 0, BS[3] = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 0*

20.4 addBoolAndArrayEqVar

Add a clause to the SAT constraint which states that: $(BOOLVARS_1 \wedge BOOLVARS_2 \wedge ... \wedge BOOLVARS_n) \Leftrightarrow TARGET$.

API:

```
boolean addBoolAndArrayEqVar(BoolVar[] BOOLVARS, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
3         BoolVar T = VF.bool("T", solver);
4         SatFactory.addBoolAndArrayEqVar(BVARS, T);
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, BS[3] = 1 T = 1*

- *BS[0] = 1, BS[1] = 1, BS[2] = 0, BS[3] = 1, T = 0*
- *BS[0] = 0, BS[1] = 1, BS[2] = 0, BS[3] = 0, T = 0*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 0, T = 0*

20.5 addBoolAndEqVar

Add a clause to the SAT constraint which states that: $(LEFT \wedge RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolAndEqVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolAndEqVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1, T = 1*
- *L = 1, R = 0, T = 0*
- *L = 0, R = 1, T = 0*
- *L = 0, R = 0, T = 0*

20.6 addBoolEq

Add a clause to the SAT constraint which states that the two boolean variables *LEFT* and *RIGHT* are equal.

API:

```
boolean addBoolEq(BoolVar LEFT, BoolVar RIGHT)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         SatFactory.addBoolEq(L, R);
5         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1*
- *L = 0, R = 0*

20.7 addBoolIsEqVar

Add a clause to the SAT constraint which states that: $(LEFT = RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolIsEqVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolIsEqVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1, T = 1*
- *L = 1, R = 0, T = 0*
- *L = 0, R = 1, T = 0*
- *L = 0, R = 0, T = 1*

20.8 addBoolIsLeVar

Add a clause to the SAT constraint which states that: $(LEFT \leq RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolIsLeVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolIsLeVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1, T = 1*
- *L = 1, R = 0, T = 0*
- *L = 0, R = 1, T = 1*
- *L = 0, R = 0, T = 1*

20.9 addBoolIsLtVar

Add a clause to the SAT constraint which states that: $(LEFT < RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolIsLtVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolIsLtVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- $L = 1, R = 1, T = 0$
- $L = 1, R = 0, T = 0$
- $L = 0, R = 1, T = 1$
- $L = 0, R = 0, T = 0$

20.10 addBoolIsNeqVar

Add a clause to the SAT constraint which states that: $(LEFT \neq RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolIsNeqVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolIsNeqVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- $L = 1, R = 1, T = 0$
- $L = 1, R = 0, T = 1$
- $L = 0, R = 1, T = 1$
- $L = 0, R = 0, T = 0$

20.11 addBoolLe

Add a clause to the SAT constraint which states that the boolean variable *LEFT* is less or equal than the boolean variable *RIGHT*.

API:

```
boolean addBoolLe(BoolVar LEFT, BoolVar RIGHT)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         SatFactory.addBoolLe(L, R);
5         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1*
- *L = 0, R = 1*
- *L = 0, R = 0*

20.12 addBoolLt

Add a clause to the SAT constraint which states that the boolean variable *LEFT* is less than the boolean variable *RIGHT*.

API:

```
boolean addBoolLt(BoolVar LEFT, BoolVar RIGHT)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         SatFactory.addBoolLt(L, R);
5         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 0, R = 1*

20.13 addBoolNot

Add a clause to the SAT constraint which states that the two boolean variables *LEFT* and *RIGHT* are not equal.

API:

```
boolean addBoolNot(BoolVar LEFT, BoolVar RIGHT)
```

Example

```
        Solver solver = new Solver();
        BoolVar L = VF.bool("L", solver);
        BoolVar R = VF.bool("R", solver);
        SatFactory.addBoolLe(L, R);
        solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 0*
- *L = 0, R = 1*

20.14 addBoolOrArrayEqualTrue

Add a clause to the SAT constraint which states that: $BOOLVARS_1 \vee BOOLVARS_2 \vee ... \vee BOOLVARS_n$.

API:

```
boolean addBoolOrArrayEqualTrue(BoolVar[] BOOLVARS)
```

Example

```
        Solver solver = new Solver();
        BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
        SatFactory.addBoolOrArrayEqualTrue(BVARS);
        solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, BS[3] = 1*
- *BS[0] = 1, BS[1] = 1, BS[2] = 0, BS[3] = 0*
- *BS[0] = 1, BS[1] = 0, BS[2] = 0, BS[3] = 0*
- *BS[0] = 0, BS[1] = 1, BS[2] = 0, BS[3] = 0*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 1*

20.15 addBoolOrArrayEqVar

Add a clause to the SAT constraint which states that: $(BOOLVARS_1 \vee BOOLVARS_2 \vee ... \vee BOOLVARS_n) \Leftrightarrow TARGET$.

API:

```
boolean addBoolOrArrayEqVar(BoolVar[] BOOLVARS, BoolVar TARGET)
```

Example

```
        Solver solver = new Solver();
        BoolVar[] BVARS = VF.boolArray("BS", 4, solver);
        BoolVar T = VF.bool("T", solver);
        SatFactory.addBoolOrArrayEqVar(BVARS, T);
        solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, BS[3] = 1, T = 1*
- *BS[0] = 1, BS[1] = 1, BS[2] = 0, BS[3] = 1, T = 1*
- *BS[0] = 0, BS[1] = 1, BS[2] = 0, BS[3] = 0, T = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, BS[3] = 0, T = 0*

20.16 addBoolOrEqVar

Add a clause to the SAT constraint which states that: $(LEFT \vee RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolOrEqVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolOrEqVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1, T = 1*
- *L = 1, R = 0, T = 1*
- *L = 0, R = 1, T = 1*
- *L = 0, R = 0, T = 0*

20.17 addBoolXorEqVar

Add a clause to the SAT constraint which states that: $(LEFT \oplus RIGTH) \Leftrightarrow TARGET$.

API:

```
boolean addBoolXorEqVar(BoolVar LEFT, BoolVar RIGHT, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar L = VF.bool("L", solver);
3         BoolVar R = VF.bool("R", solver);
4         BoolVar T = VF.bool("T", solver);
5         SatFactory.addBoolXorEqVar(L, R, T);
6         solver.findAllSolutions();
```

The solutions of the problem are :

- *L = 1, R = 1, T = 0*

- *L = 1, R = 0, T = 1*
- *L = 0, R = 1, T = 1*
- *L = 0, R = 0, T = 0*

20.18 addClauses

Adding a clause involved either:

- a logical operator *TREE* and an instance of the solver,
- or, two arrays of boolean variables.

The two methods add a clause to the SAT constraint.

- The first method adds one or more clauses defined by a `LogOp`.

`LopOp` aims at simplifying the declaration of clauses by providing some static methods. However, it should be considered as a last resort, due to the verbosity it comes with.

- The second API add one or more clauses defined by two arrays *POSLITS* and *NEGLITS*.

The first array declares positive boolean variables, those who should be satisfied; the second array declares negative boolean variables, those who should not be satisfied.

API:

```
boolean addClauses(LogOp TREE, Solver SOLVER)
boolean addClauses(BoolVar[] POSLITS, BoolVar[] NEGLITS)
```

Example 1

```
1         Solver solver = new Solver();
2         BoolVar C1 = VF.bool("C1", solver);
3         BoolVar C2 = VF.bool("C2", solver);
4         BoolVar R = VF.bool("R", solver);
5         BoolVar AR = VF.bool("AR", solver);
6         SatFactory.addClauses(
7                 LogOp.ifThenElse(LogOp.nand(C1, C2), R, AR),
8                 solver);
9         solver.findAllSolutions();
```

Some solutions of the problem are :

- *C1 = 1, C2 = 0, R = 1, AR = 1*
- *C1 = 1, C2 = 0, R = 0, AR = 1*
- *C1 = 0, C2 = 1, R = 1, AR = 0*
- *C1 = 0, C2 = 0, R = 0, AR = 1*

Example 2

```
1         Solver solver = new Solver();
2         BoolVar P1 = VF.bool("P1", solver);
3         BoolVar P2 = VF.bool("P2", solver);
4         BoolVar P3 = VF.bool("P3", solver);
5         BoolVar N = VF.bool("N", solver);
```

```
6         SatFactory.addClauses(new BoolVar[]{P1, P2, P3}, new BoolVar[]{N});
7         solver.findAllSolutions();
```

Some solutions of the problem are :

- *P1 = 1, P2 = 1, P3 = 1, N = 1*
- *P1 = 1, P2 = 1, P3 = 1, N = 0*
- *P1 = 1, P2 = 0, P3 = 1, N = 0*
- *P1 = 0, P2 = 0, P3 = 1, N = 1*

20.19 addFalse

Add a unit clause to the SAT constraint which states that the boolean variable *BOOLVAR* must be false (equal to 0).

API:

```
boolean addFalse(BoolVar BOOLVAR)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar B = VF.bool("B", solver);
3         SatFactory.addFalse(B);
4         solver.findAllSolutions();
```

The solution of the problem is :

- *B = 0*

20.20 addMaxBoolArrayLessEqVar

Add a clause to the SAT constraint which states that: maximum($BOOLVARS_i$) $\leq$ *TARGET*.

API:

```
boolean addMaxBoolArrayLessEqVar(BoolVar[] BOOLVARS, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 3, solver);
3         BoolVar T = VF.bool("T", solver);
4         SatFactory.addMaxBoolArrayLessEqVar(BVARS, T);
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, T = 1*
- *BS[0] = 1, BS[1] = 0, BS[2] = 1, T = 1*
- *BS[0] = 0, BS[1] = 1, BS[2] = 1, T = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, T = 0*

20.21 addSumBoolArrayGreaterEqVar

Add a clause to the SAT constraint which states that: sum($BOOLVARS_i$) $\geq$ $TARGET$.

API:

```
boolean addSumBoolArrayGreaterEqVar(BoolVar[] BOOLVARS, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 3, solver);
3         BoolVar T = VF.bool("T", solver);
4         SatFactory.addSumBoolArrayGreaterEqVar(BVARS, T);
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1, BS[1] = 1, BS[2] = 1, T = 1*
- *BS[0] = 1, BS[1] = 0, BS[2] = 1, T = 1*
- *BS[0] = 0, BS[1] = 1, BS[2] = 1, T = 1*
- *BS[0] = 0, BS[1] = 0, BS[2] = 0, T = 0*

20.22 addSumBoolArrayLessEqVar

Add a clause to the SAT constraint which states that: sum($BOOLVARS_i$) $\leq$ $TARGET$.

API:

```
boolean addSumBoolArrayLessEqVar(BoolVar[] BOOLVARS, BoolVar TARGET)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar[] BVARS = VF.boolArray("BS", 3, solver);
3         BoolVar T = VF.bool("T", solver);
4         SatFactory.addSumBoolArrayLessEqVar(BVARS, T);
5         solver.findAllSolutions();
```

Some solutions of the problem are :

- *BS[0] = 1 BS[1] = 1 BS[2] = 1 T = 1*
- *BS[0] = 1 BS[1] = 0 BS[2] = 1 T = 1*
- *BS[0] = 0 BS[1] = 1 BS[2] = 1 T = 1*
- *BS[0] = 0 BS[1] = 0 BS[2] = 0 T = 1*

20.23 addTrue

Add a unit clause to the SAT constraint which states that the boolean variable *BOOLVAR* must be true (equal to 1).

API:

```
boolean addTrue(BoolVar BOOLVAR)
```

Example

```
1         Solver solver = new Solver();
2         BoolVar B = VF.bool("B", solver);
3         SatFactory.addTrue(B);
4         solver.findAllSolutions();
```

The solution of the problem is :

- *B = 1*

CHAPTER 21

Variable selectors

Important: By default, in case of equalities, the variable with the smallest index in the input array is returned. Otherwise, consider using a `VariableSelectorWithTies` (See *Zoom on IntStrategy*).

21.1 lexico_var_selector

A built-in variable selector which chooses the first non-instantiated integer variable to branch on, regarding the lexicographic order.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
VariableSelector<IntVar> lexico_var_selector()
```

21.2 random_var_selector

A built-in variable selector which randomly chooses an integer variable, among non-instantiated ones, to branch on.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
VariableSelector<IntVar> random_var_selector(long SEED)
```

21.3 minDomainSize_var_selector

A built-in variable selector which chooses the non-instantiated integer variable with the smallest domain to branch on.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
VariableSelector<IntVar> minDomainSize_var_selector()
```

21.4 maxDomainSize_var_selector

A built-in variable selector which chooses the non-instantiated integer variable with the largest domain to branch on.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
VariableSelector<IntVar> maxDomainSize_var_selector()
```

21.5 maxRegret_var_selector

A built-in variable selector which chooses the non-instantiated integer variable with the largest difference between the two smallest values in its domain to branch on .

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
VariableSelector<IntVar> maxRegret_var_selector()
```

CHAPTER 22

Value selectors

22.1 min_value_selector

A built-in value selector which selects the variable lower bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntValueSelector min_value_selector()
```

22.2 mid_value_selector

A built-in value selector which selects the value in the variable domain closest to the mean of its current bounds. It computes the middle value of the domain. Then checks if the mean is contained in the domain. If not, the closest value to the middle is chosen. Rounding policy is floor. It could be override by creating a new instance of `IntDomainMiddle` with `false` as parameter.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntValueSelector mid_value_selector()
```

22.3 max_value_selector

A built-in value selector which selects the variable upper bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntValueSelector max_value_selector()
```

22.4 randomBound_value_selector

A built-in value selector which randomly selects either the lower bound or the upper bound of the variable.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntValueSelector randomBound_value_selector(long SEED)
```

22.5 random_value_selector

Selects randomly a value in the variable domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntValueSelector random_value_selector(long SEED)
```

CHAPTER 23

Decision operators

23.1 assign

A built-in decision operator which assigns the selected variable to the selected value. Its negation is *remove*.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
DecisionOperator<IntVar> assign()
```

23.2 remove

A built-in decision operator which removes the selected value from the selected variable domain. Its negation is *assign*.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
DecisionOperator<IntVar> remove()
```

23.3 split

A built-in decision operator which splits the selected variable domain at the selected value, that is, it updates the upper bound of the variable to the selected value. Its negation is *reverse_split* on *value + 1*.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
DecisionOperator<IntVar> split()
```

23.4 reverse_split

A built-in decision operator which splits the selected variable domain at the selected value, that is, it updates the lower bound of the variable to the selected value. Its negation is *split* on *value - 1*.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
DecisionOperator<IntVar> reverse_split()
```

CHAPTER 24

Built-in strategies

24.1 custom

To build a specific strategy based on `IntVar` or `SetVar`. A strategy is based on a variable selector, a value selector and an optional decision operator.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy custom(VariableSelector<IntVar> VAR_SELECTOR,
                                            IntValueSelector VAL_SELECTOR,
                                            DecisionOperator<IntVar> DEC_OPERATOR,
                                            IntVar... VARS)

IntStrategy custom(VariableSelector<IntVar> VAR_SELECTOR,
                                           IntValueSelector VAL_SELECTOR,
                                           IntVar... VARS)

SetStrategy custom(VariableSelector<SetVar> varS, SetValueSelector valS, boolean enforceFirst,
                   SetVar... sets)
```

24.2 force_first

A built-in strategy which chooses the first non-instantiated variable, regarding the lexicographic order, and forces its first smallest unfixed value to be part of the kernel.

Scope: `SetVar`

Factory: `solver.search.strategy.SetStrategyFactory`

API:

```
SetStrategy force_first(SetVar... sets)
```

24.3 force_maxDelta_first

A built-in strategy which chooses the first non-instantiated variable of maximum delta (envelope's cardinality minus kernel's cardinality) and forces its smallest unfixed value to be part of the kernel.

Scope: `SetVar`

Factory: `solver.search.strategy.SetStrategyFactory`

API:

```
SetStrategy force_maxDelta_first(SetVar... sets)
```

24.4 force_minDelta_first

A built-in strategy which chooses the first non-instantiated variable of minimum delta (envelope's cardinality minus kernel's cardinality) and forces its smallest first unfixed value to be part of the kernel.

Scope: `SetVar`

Factory: `solver.search.strategy.SetStrategyFactory`

API:

```
SetStrategy force_minDelta_first(SetVar... sets)
```

24.5 lexico_LB

A built-in strategy which chooses the first non-instantiated variable, regarding the lexicographic order, and assigns it to its lower bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy lexico_LB(IntVar... VARS)
```

24.6 lexico_Neq_LB

A built-in strategy which chooses the first non-instantiated variable, regarding the lexicographic order, and removes its lower bound from its domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy lexico_Neq_LB(IntVar... VARS)
```

24.7 lexico_Split

A built-in strategy which chooses the first non-instantiated variable, regarding the lexicographic order, and removes the second half of its domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy lexico_Split(IntVar... VARS)
```

24.8 lexico_UB

A built-in strategy which chooses the first non-instantiated variable, regarding the lexicographic order, and assigns it to its upper bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy lexico_UB(IntVar... VARS)
```

24.9 minDom_LB

A built-in strategy which chooses the first non-instantiated variable with the smallest domain size, and assigns it to its lower bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy minDom_LB(IntVar... VARS)
```

24.10 minDom_MidValue

A built-in strategy which chooses the first non-instantiated variable with the smallest domain size, and assigns it to the value closest to its middle of its domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy minDom_MidValue(IntVar... VARS)
```

24.11 maxDom_Split

A built-in strategy which chooses the first non-instantiated variable with largest domain size, and removes the second half of its domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy maxDom_Split(IntVar... VARS)
```

24.12 minDom_UB

A built-in strategy which chooses the first non-instantiated variable with the smallest domain size, and assigns it to its upper bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy minDom_UB(IntVar... VARS)
```

24.13 maxReg_LB

A built-in strategy which chooses the first non-instantiated variable with the largest difference between the two smallest values of its domain, and assigns it to its lower bound.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy maxReg_LB(IntVar... VARS)
```

24.14 random_bound

A built-in strategy which randomly chooses a non-instantiated variable, and assigns it to one of its bounds, randomly selected.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy random_bound(IntVar[] VARS)
IntStrategy random_bound(IntVar[] VARS, long SEED)
```

24.15 random_value

A built-in strategy which randomly chooses a non-instantiated variable, and assigns it to a randomly selected value from its domain.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
IntStrategy random_value(IntVar[] VARS)
IntStrategy random_value(IntVar[] VARS, long SEED)
```

24.16 remove_first

A built-in strategy which chooses the first unfixed variable and removes its smallest unfixed value from the envelope.

Scope: `SetVar`

Factory: `solver.search.strategy.SetStrategyFactory`

API:

```
SetStrategy remove_first(SetVar... sets)
```

24.17 sequencer

A meta strategy which applies sequentially the strategies in its scope.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy sequencer(AbstractStrategy... strategies)
```

24.18 domOverWDeg

A black-box strategy for `IntVar` which selects the non-instantiated variable with the smallest ratio $\frac{|d(x)|}{w(x)}$, where $|d(x)|$ denotes the domain size of a variable x and $w(x)$ its weighted degree. The weighted degree of a variable sums the weight of each of the constraint it is involved in where at least 2 variables remains uninstantiated. The weight of a constraint is initialized to *1* and increased by one each time a constraint propagation fails during the search.

Implementation based on: [BHLS04].

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy<IntVar> domOverWDeg(IntVar[] VARS, long SEED, IntValueSelector VAL_SELECTOR)
AbstractStrategy<IntVar> domOverWDeg(IntVar[] VARS, long SEED) // default: min_value_selector
```

24.19 activity

A black-box strategy for `IntVar` which selects the non-instantiated variable with the largest ratio $\frac{a(x)}{|d(x)|}$, where $|d(x)|$ denotes the domain size of a variable x and $a(x)$ its activity. The activity of a variable measures how often the domain of the variable is reducing during the search. Then, the value with the least activity is selected from the domain of the variable.

Implementation based on: [MH12].

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy<IntVar> activity(IntVar[] VARS, double GAMMA, double DELTA, int ALPHA,
                                  double RESTART, int FORCE_SAMPLING, long SEED)
AbstractStrategy<IntVar> activity(IntVar[] VARS, long SEED) // default: 0.999d, 0.2d, 8, 1.1d, 1
```

24.20 impact

A black-box strategy for `IntVar` which selects the non-instantiated variable with the largest impact $\sum_{a in d(x)} 1 - I(x = a)$, $I(x = a)$ denotes the impact of assigning the variable x to a value a from its domain $d(x)$. The impact of an assignment measures the search space reduction induced by a decision, by evaluating the size of the search before and after the application of a decision. The higher the impact, the greater the search space reduction. Then, the value with the least impact is selected from the domain of the variable. An approximation of the impacts is preprocessed.

Implementation based on: [Ref04].

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy<IntVar> impact(IntVar[] VARS, int ALPHA, int SPLIT, int NODEIMPACT,
                                long SEED, boolean INITONLY)
AbstractStrategy<IntVar> impact(IntVar[] VARS, long SEED) // default: 2, 3, 10, true
```

24.21 lastConflict

A composite heuristic which override the defined strategy by forcing some decisions to branch on variables involved in recent conflicts. After each conflict, the last assigned variable is selected in priority, so long as a failure occurs.

Implementation based on: [LSTV09].

Scope: `Variable`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy lastConflict(Solver SOLVER)
AbstractStrategy lastConflict(Solver SOLVER, AbstractStrategy STRAT)
AbstractStrategy lastKConflicts(Solver SOLVER, int K, AbstractStrategy STRAT)
```

24.22 generateAndTest

A strategy that simulate a *Generate and Test* behavior through a specific internal decision. The main idea is, from all the variables of a problem, to generate and test the satisfiability of a complete instantiation. The process does not rely on propagation anymore, but on satisfaction only.

Such strategy can be triggered when the search space reached a given limit.

Scope: `IntVar`

Factory: `solver.search.strategy.IntStrategyFactory`

API:

```
AbstractStrategy<IntVar> generateAndTest(Solver SOLVER)
AbstractStrategy<IntVar> generateAndTest(Solver SOLVER, AbstractStrategy<IntVar> mainStrategy,
                                         int searchSpaceLimit)
```

Part VI

Extensions of Choco

CHAPTER 25

IO extensions

25.1 choco-parsers

choco-parsers is an extension of Choco 3.2. It provides a parser for the FlatZinc language, a low-level solver input language that is the target language for MiniZinc. This module follows the flatzinc standards that are used for the annual MiniZinc challenge. It only supports integer variables. You will find it at https://github.com/chocoteam/choco-parsers

25.2 choco-gui

choco-gui is an extension of Choco 3.2. It provides a Graphical User Interface with various views which can be simply plugged on any Choco Solver object. You will find it at https://github.com/chocoteam/choco-gui

25.3 choco-cpviz

choco-cpviz is an extension of Choco 3.2 to deal with cpviz library. You will find it at https://github.com/chocoteam/choco-cpviz

CHAPTER 26

Modeling extensions

26.1 choco-graph

choco-graph is a Choco 3.2 module which allows to search for a graph, which may be subject to graph constraints. The domain of a graph variable G is a graph interval in the form [G_lb,G_ub]. G_lb is the graph representing vertices and edges which must belong to any single solution whereas G_ub is the graph representing vertices and edges which may belong to one solution. Therefore, any value G_v must satisfy the graph inclusion "G_lb subgraph of G_v subgraph of G_ub". One may see a strong connection with set variables. A graph variable can be subject to graph constraints to ensure global graph properties (e.g. connectedness, acyclicity) and channeling constraints to link the graph variable with some other binary, integer or set variables. The solving process consists of removing nodes and edges from G_ub and adding some others to G_lb until having G_lb = G_ub, i.e. until G gets instantiated. These operations stem from both constraint propagation and search. The benefits of graph variables stem from modeling convenience and performance.

This extension has documentation. You will find it at https://github.com/chocoteam/choco-graph

26.2 choco-geost

choco-geost is a Choco 3.2 module which provides the GEOST global constraint. This constraint is designed for geometrical and packing applications (see http://www.emn.fr/z-info/sdemasse/gccat/Cgeost.html). You will find it at https://github.com/chocoteam/choco-geost

26.3 choco-exppar

choco-exppar is a Choco 3.2 module which provides an expression parser. This enables to simplify the modeling step. You will find it at https://github.com/chocoteam/choco-exppar

26.4 choco-eps

Embarrassingly Parallel Search for Choco 3.2 enables to speed up search on multi-core systems. This extension is currently under development. You will find it at https://github.com/chocoteam/choco-eps

Part VII

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