

①

$$\frac{\begin{array}{l} E \vdash e_1 : c_1 \\ E \vdash e_2 : c_2 \\ c_1 \leq c_2 \end{array}}{E \vdash e_1 \leq e_2 : \text{true}}$$

$$\frac{\begin{array}{l} E \vdash e_1 : c_1 \\ E \vdash e_2 : c_2 \\ c_1 > c_2 \end{array}}{E \vdash e_1 \leq e_2 : \text{false}}$$

②

$$\frac{\begin{array}{c} \text{Ident } x \quad E[x+2](x)=2 \\ E[x+2] \vdash 1 : 1 \end{array}}{E[x+2] \vdash x+1 : 3}$$

$$\frac{E \vdash 2 : 2 \quad E[x+2] \vdash x+1 : 3}{E \vdash \text{let } x = 2 \text{ in } x+1 : 3}$$

③

negative Number

$$\frac{\begin{array}{l} E \vdash e_1 : c \quad c < 0 \\ E \vdash e_2 : \checkmark \end{array}}{E \vdash \text{testSign } e_1 e_2 e_3 e_4 : \checkmark}$$

zero

$$\frac{\begin{array}{l} E \vdash e_1 : 0 \\ E \vdash e_3 : \checkmark \end{array}}{E \vdash \text{testSign } e_1 e_2 e_3 e_4 : \checkmark}$$

positive num

$$\frac{\begin{array}{l} E \vdash e_1 : c \quad c > 0 \\ E \vdash e_4 : \checkmark \end{array}}{E \vdash \text{testSign } e_1 e_2 e_3 e_4 : \checkmark}$$

$$\langle e_1, E \rangle \longrightarrow \langle e'_1, E' \rangle$$

④

$$\langle \text{testSign } e_1 e_2 e_3 e_4, E \rangle \longrightarrow \langle \text{testSign } e'_1 e_2 e_3 e_4, E' \rangle$$

 $c < 0$

$$\langle \text{testSign } c \ e_2 e_3 e_4, E \rangle \longrightarrow \langle e_2, E \rangle$$

$$\langle \text{testSign } 0 \ e_2 e_3 e_4, E \rangle \longrightarrow \langle e_3, E \rangle$$

 $c > 0$

$$\langle \text{testSign } c \ e_2 e_3 e_4, E \rangle \longrightarrow \langle e_4, E \rangle$$