CMPT 383 Comparative Programming Languages

Homework 7

This homework is due by 11:59pm PT on Tuesday Apr 1, 2025. No late submission is accepted. Please save your answers in a single file called H7_SFUID.pdf and submit it to Canvas. You may also write on paper and scan it (or take a picture) into a PDF. Please make sure the text is readable.

1. (20 points) Consider the FUN language with type annotations, prove the type of following expression is $Int \to Int$. In other words, show the derivation process using the type checking rules (with prefix T-).

lambda
$$x: \mathtt{Int.}\ 2+x$$

2. (30 points) Consider the FUN language with type annotations, prove the type of following expression is *Int* using the type checking rules (with prefix T-).

$$\mathtt{let}\ f: \mathtt{Int} \mathtt{-}\mathtt{>} \mathtt{Int} = \mathtt{lambda}\ x: \mathtt{Int}.\ x\ \mathtt{in}\ \mathtt{app}\ f\ 1$$

3. (10 points) Find a most general unifier of the following constraints. You do not need to show the steps.

$$\{X_1 = X_2 \to X_3, \ X_2 = X_3 \to X_4, \ X_3 = Int\}$$

4. (30 points) Consider the FUN language without type annotations, perform constraint-based type checking of the following expression using rules with CT- prefix (use CT-Ident1 and CT-Ident2 instead of CT-Ident). You need to show the derivation steps.

let
$$f = lambda x. x in app f 1$$

5. (10 points) Consider Question 4 again, find a most general unifier of the final constraints. You do not need to show the steps.