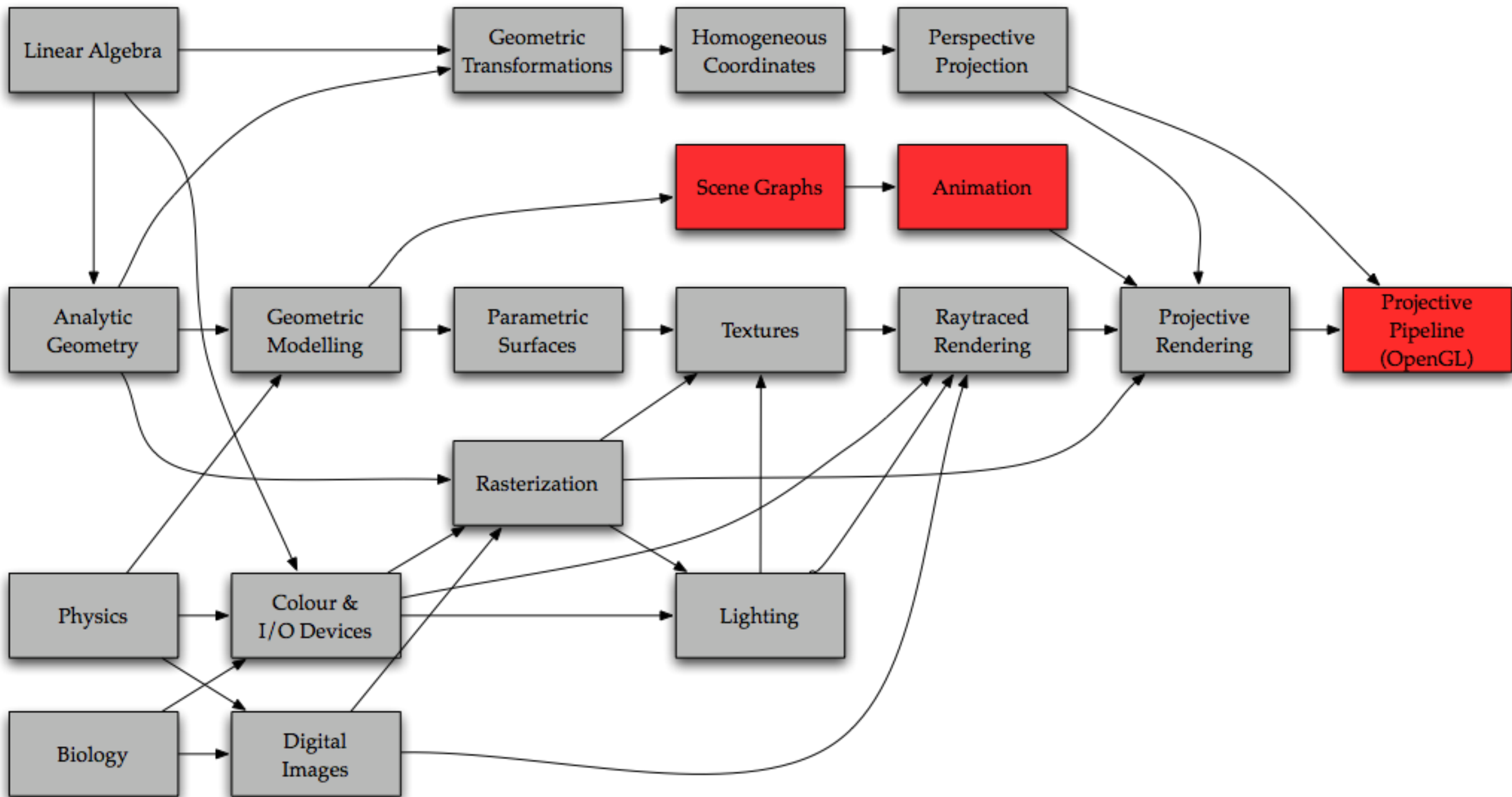


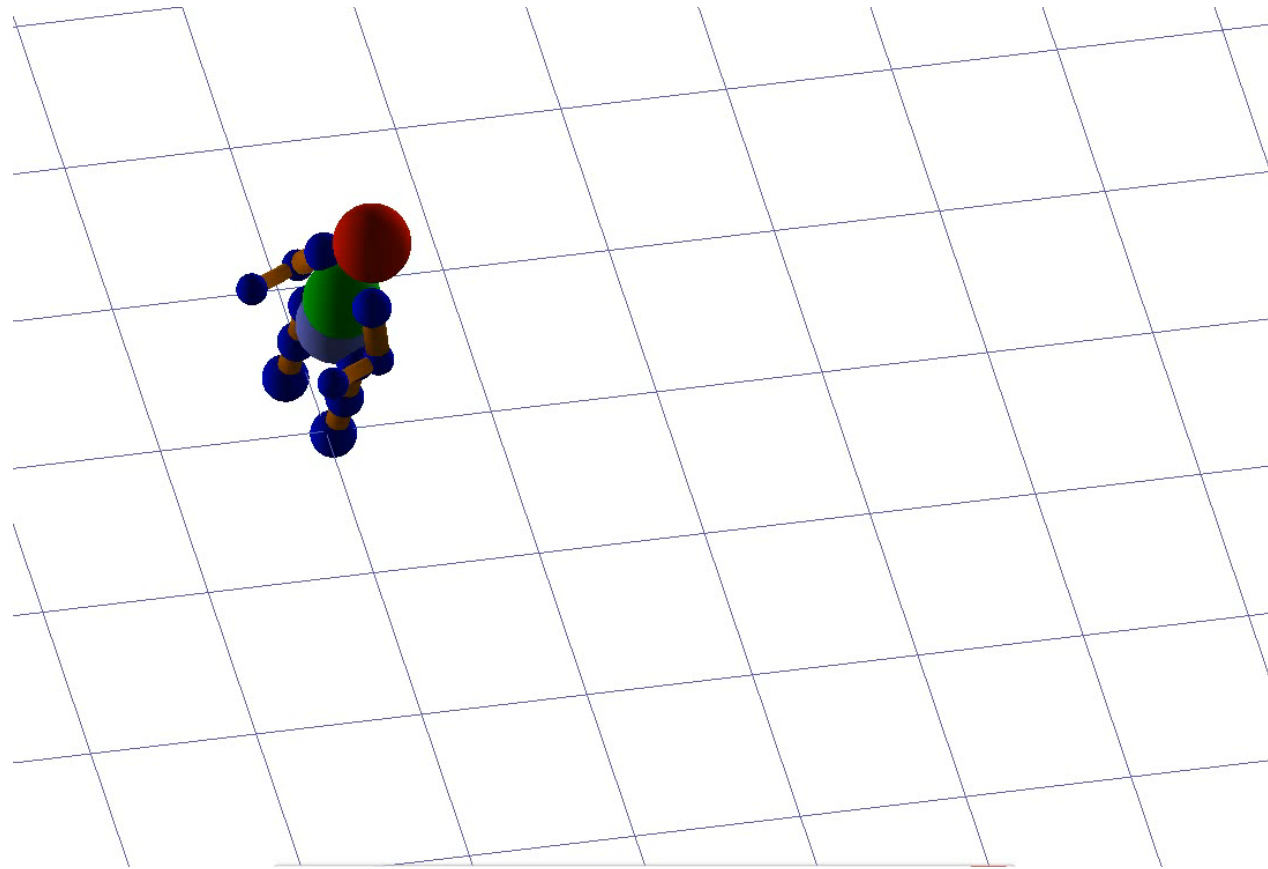
Hierarchical Animation



Where We Are



Animation Example:



What is Animation?

- The *illusion* of motion:
 - making things appear to move
 - by drawing things too fast for the eye
- So we go back to what the eye can do



The Illusion of Motion

- The eye sees events in about $1/24$ sec.
- Anything shorter, the eye mostly misses
- So, we show more than 24 *frames* / sec.
 - the eye *interprets* this as motion
 - but each image is static
- In practice, it's more complex



Movies

- Movies used to run at 16 *frames per second*
 - so they looked jerky
- Modern movies run at 24 fps or better
- Each frame is a single image
 - computed “off-line” & stored on film
 - projected one at a time at fixed speed



Computers

- Generate images on the fly
 - it takes most of the time just to draw
 - most of the $1/24$ sec you see nothing
 - you see some objects longer than others
 - last objects drawn look ghostly



Tearing

Tearing in computer graphics is a visual artifact that occurs when the display hardware shows information from multiple frames in a single screen draw. This results in a "tear" or horizontal split where parts of different frames are visible at once, leading to a disjointed appearance.

- **Tearing** results from a mismatch between the GPU's frame output and the monitor's refresh.
- **V-Sync** can eliminate tearing but might cause input lag.
- **Adaptive sync technologies** like **G-Sync** and **FreeSync** are the most effective modern solutions for eliminating tearing with minimal downsides.



Tearing

- Video output refreshes constantly
 - doesn't wait for frame to finish
 - so you get half a frame visible
- CRT's scan from top down
 - so you get a similar problem
 - we'll come back to this later



Double-buffering

- Use TWO copies of the framebuffer
- Draw one, show the other
- When finished drawing, swap them
 - `glutSwapBuffers()`

Triple Buffering

Uses three buffers instead of the usual two (front and back buffers). This allows the GPU to keep rendering new frames even if the previous one hasn't finished displaying.



Dropped Frames

- Show a new frame every 1 / 30 second
- What if we are late?
 - the eye sees the same frame twice
 - motion no longer looks smooth
- Solution: render faster & we won't notice
- Result: we want 60 fps or better



Simulating Motion

- For each frame, we compute:
 - new transformations for each object
 - new lighting (sometimes)
 - new colour / textures (occasionally)
 - new geometry (rarely)



Time & Motion

- We treat *position* p as a function of *time*
- We *compute* p given a particular t
- Usually in parametric form



Simple Example

```
void animateTrain()  
{ /* animateTrain() */  
  for (timeStep = 0; timeStep < 600; timeStep++)  
  { /* each frame */  
    computePosition(timeStep);  
    drawTrain();  
  } /* each frame */  
} /* animateTrain() */
```



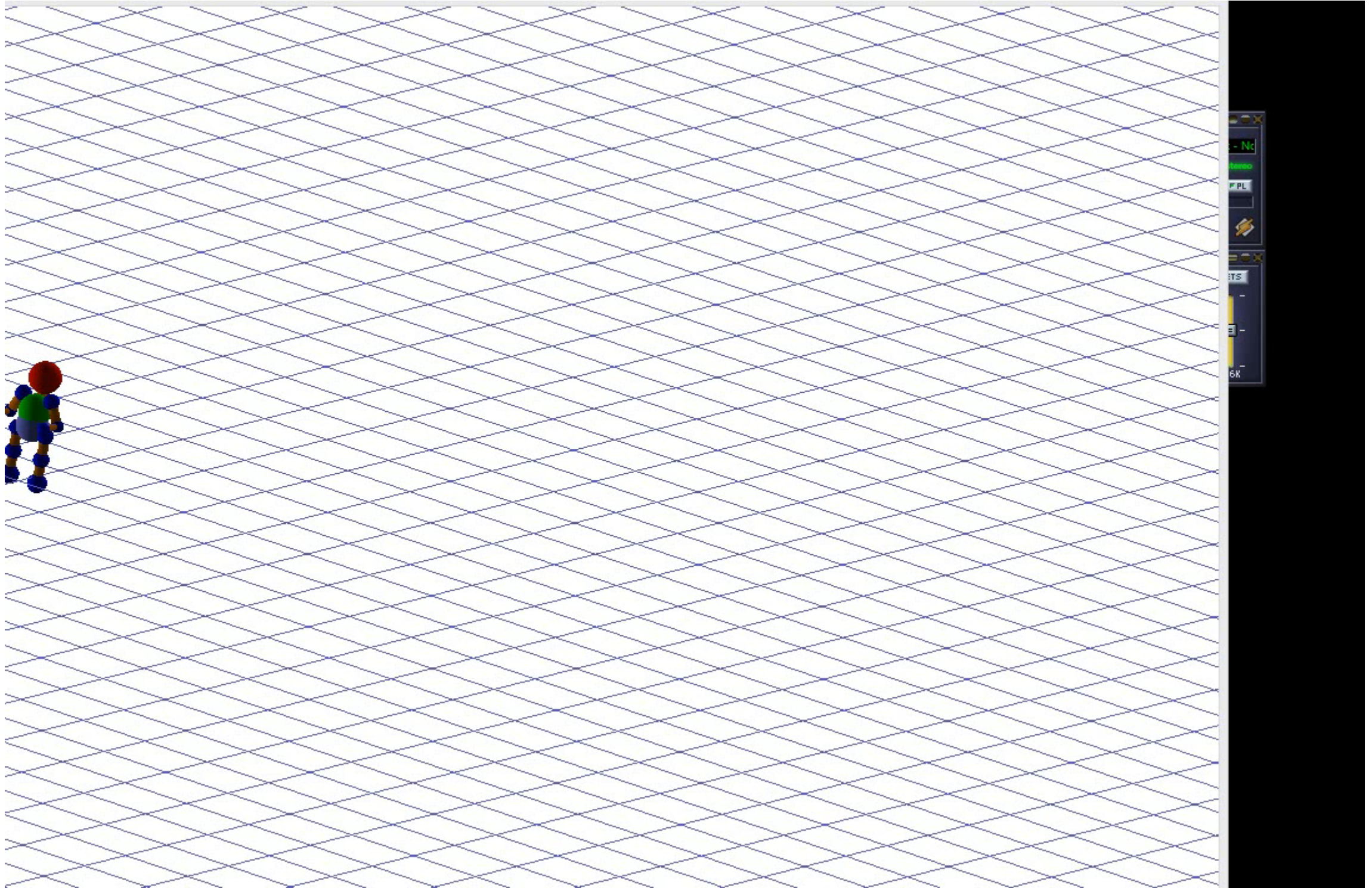
Computing Position

- Given the *time step*, compute position:

```
void computePosition(int time)
{ /* computePosition() */
  theta = (time / 600) * 2 * PI;
  posn_x = cos(theta);
  posn_y = sin(theta);
  glTranslatef(posn_x, posn_y, 0.0);
} /* computePosition() */
```



Oops ...

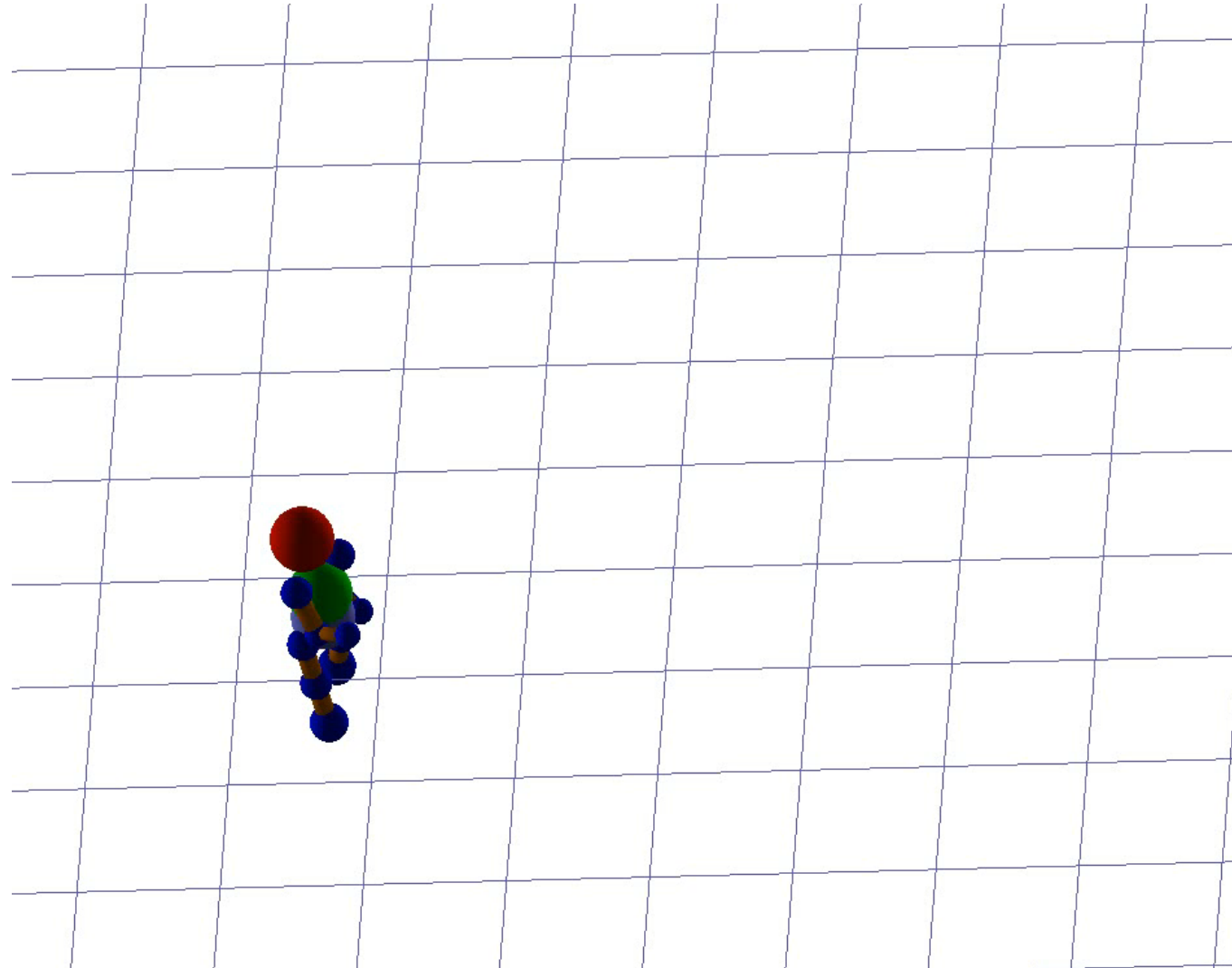


Position & Orientation

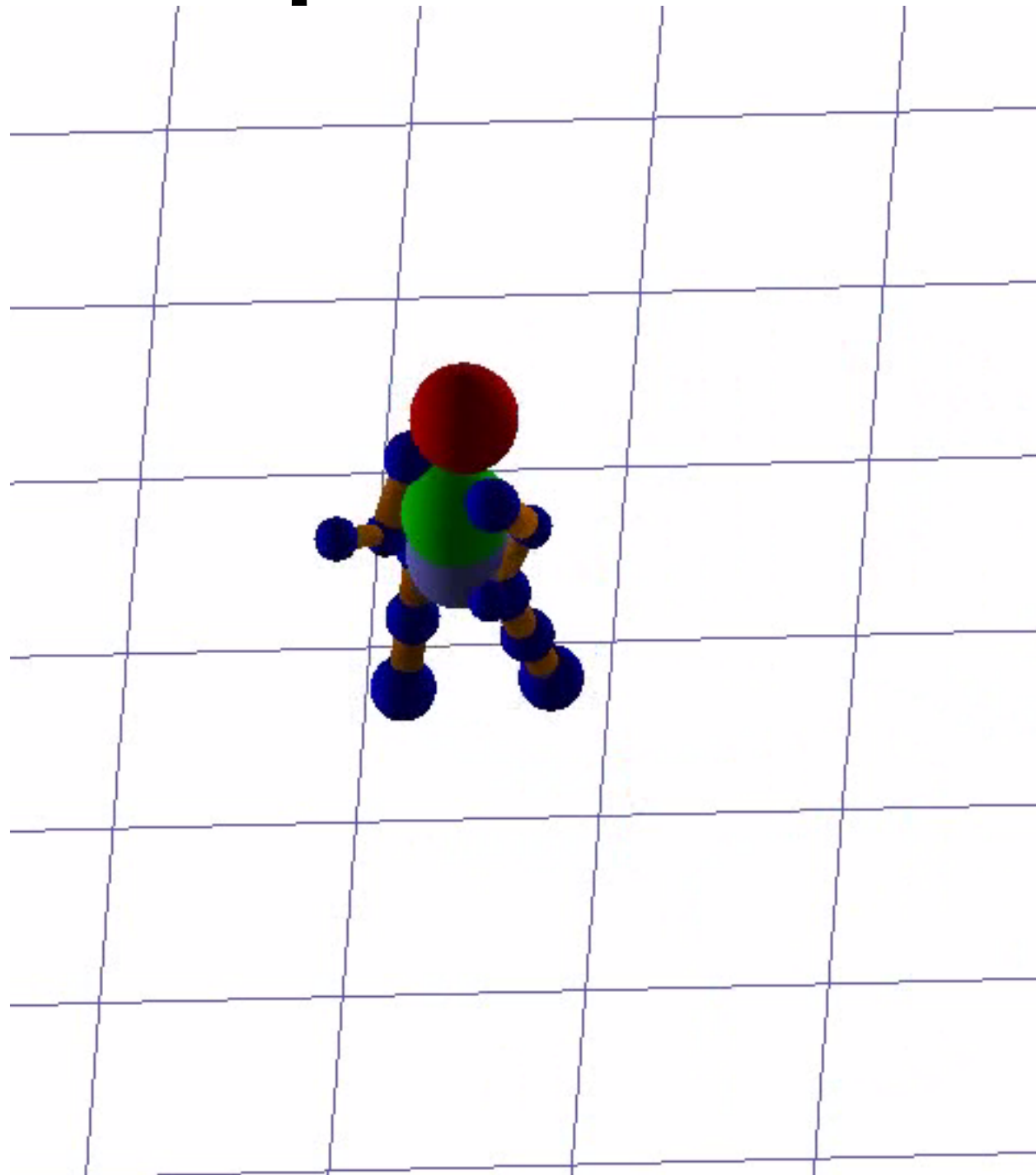
```
void computePosition(int time)
{ /* computePosition() */
  thetaDeg = (time / 600) * 360;
  thetaRad = (time / 600) * 2 * PI;
  posn_x = cos(thetaRad);
  posn_y = sin(thetaRad);
  glTranslatef(posn_x, posn_y, 0.0);
  glRotatef(thetaDeg, 0.0, 0.0, 1.0);
} /* computePosition() */
```



And the result



A Complex Example



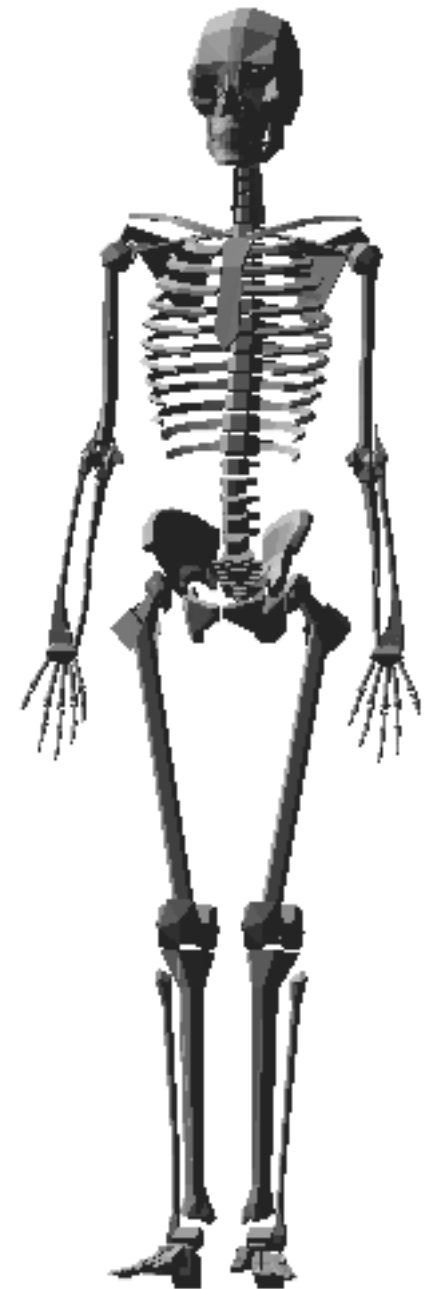
Articulation

- Humans are different from toy trains
 - they are *articulated*
 - composed of *bones* (i.e. limbs)
 - connected by *joints*
- so we will model them this way



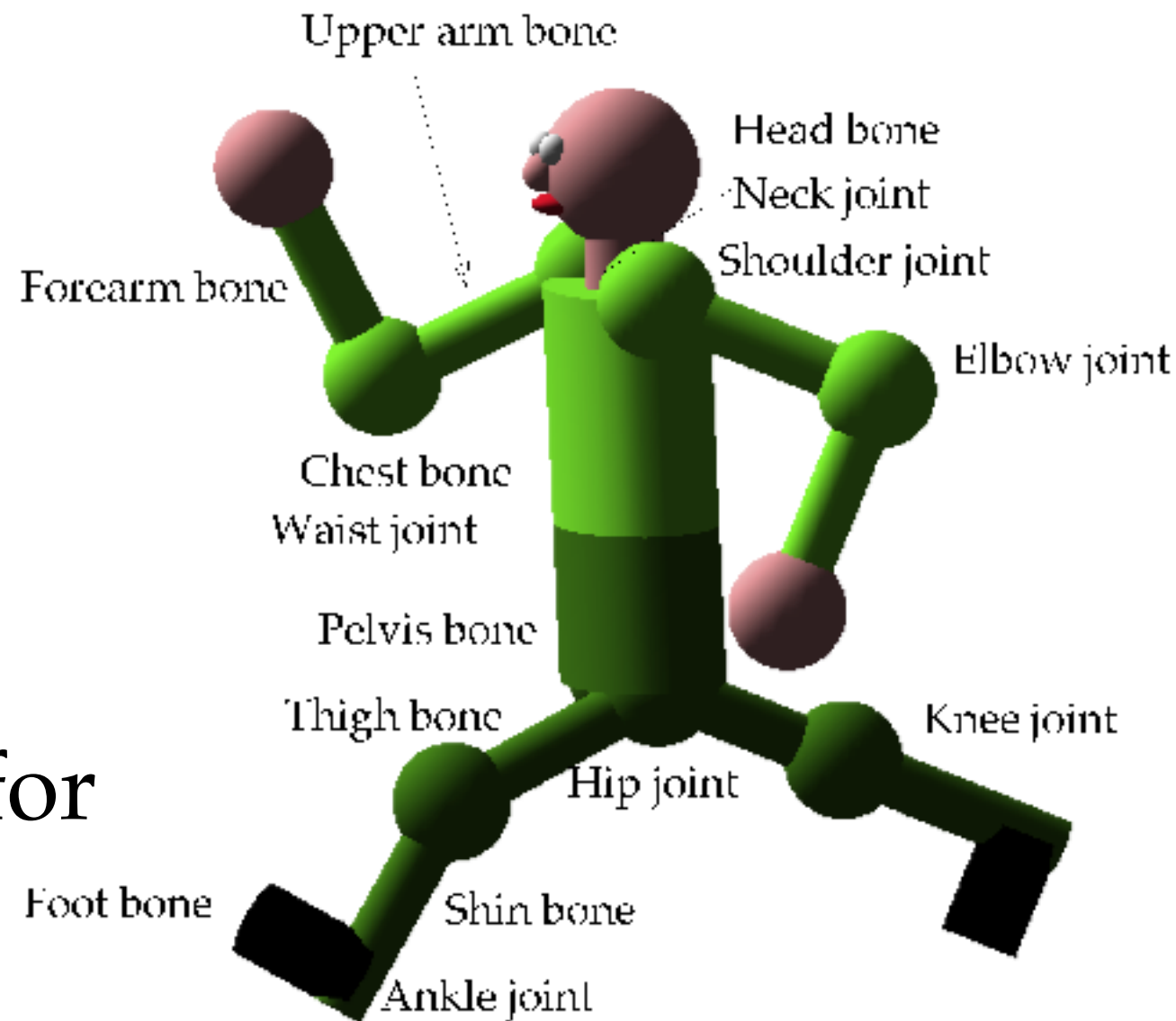
Bones

- How many bones do we have?
 - 208 (approximately)
 - but many don't matter
- A *bone* is a separately transformed piece of the object - often a limb
- Even trains have *bones* - wheels, &c.



How many Bones?

- Number of bones depends on detail
- Sometimes need fingers, toes, &c.
- Even need “bones” for facial expressions



Bone Coordinates

- Each bone has its own coordinates
 - i.e. *local coordinate systems*
- But we know how to deal with these
- Bones are connected by *joints*
 - points where two bones meet



Joints

- *Joints* are points at which bones meet
 - one bone rotates around the joint
- Joint is fixed in stationary bone's coords
- Joint is *origin* of other bone's coords
 - to move the bone, rotate around joint
 - “simple” rotation matrix



Degrees of Freedom

- Not all rotations are possible at joints:
- *degrees of freedom* = number of rotations
- Elbow & knee: 1 *d.o.f.*, 135° *range*
- Shoulder / hip:
- Wrist / ankle:
- Waist / neck:



Direction of Axes

- Axes for bone are up to you
 - convenient if rotations are simple
 - e.g. elbow y-axis sticks out sideways
 - so all elbow rotations are y-rotations
- I like putting z-axis down centre of bone



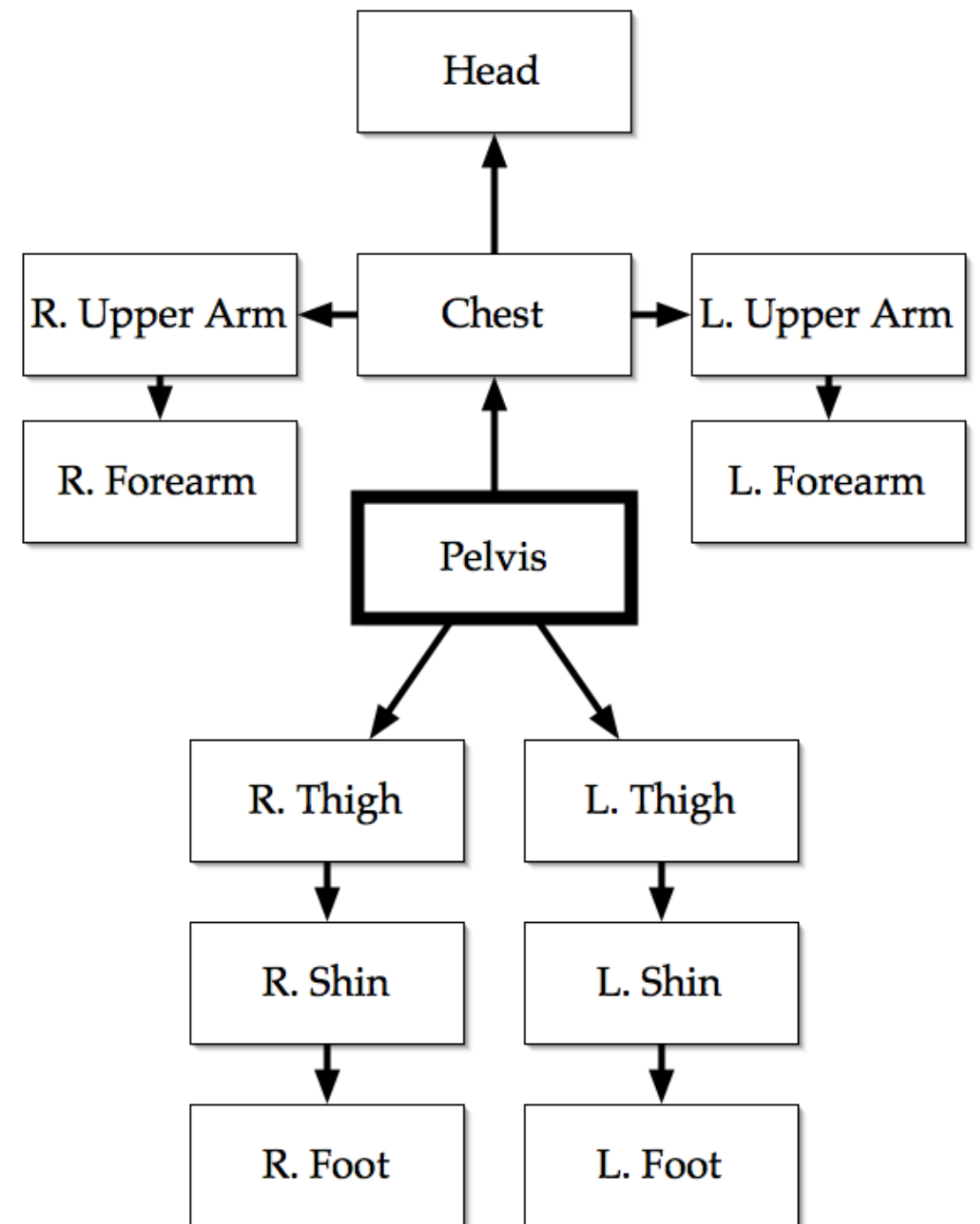
Which Bone Rotates?

- Both, unless there is another force acting
- Ultimately, motion pushes against ground
- But the feet move a lot!
- Human motion keeps body / head stable
- So pelvis is treated as stationary
 - if it moves or rotates, the body does too

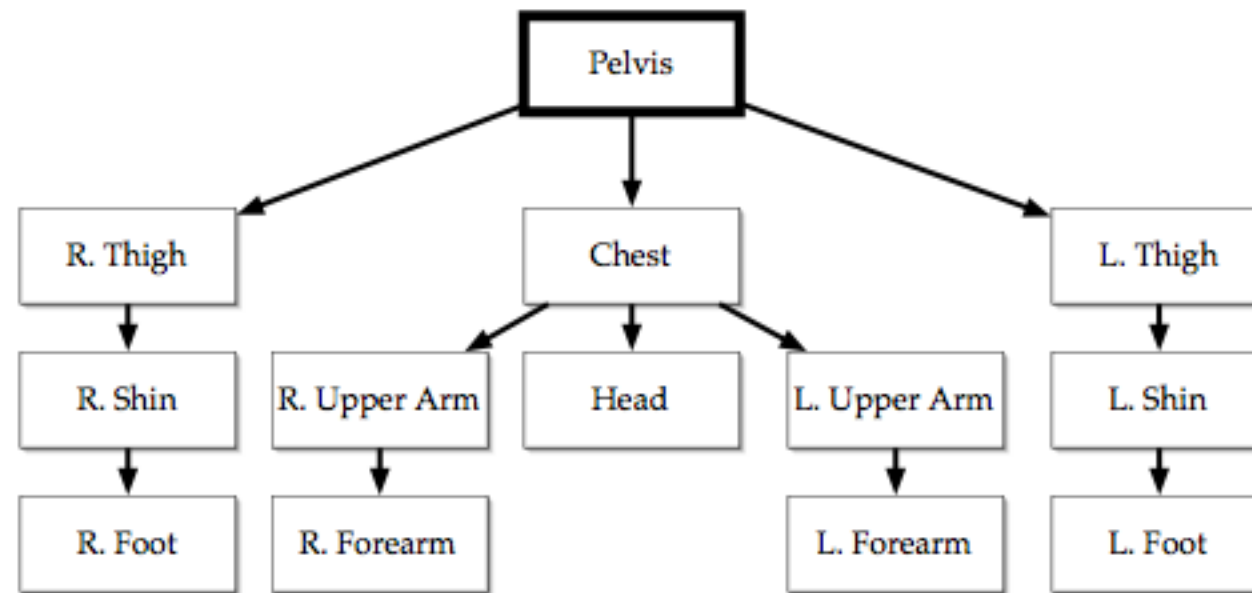


Bone Diagram

- Pelvis is master bone
- all others hang off it
- So let's redraw this diagram:



Bone Hierarchy



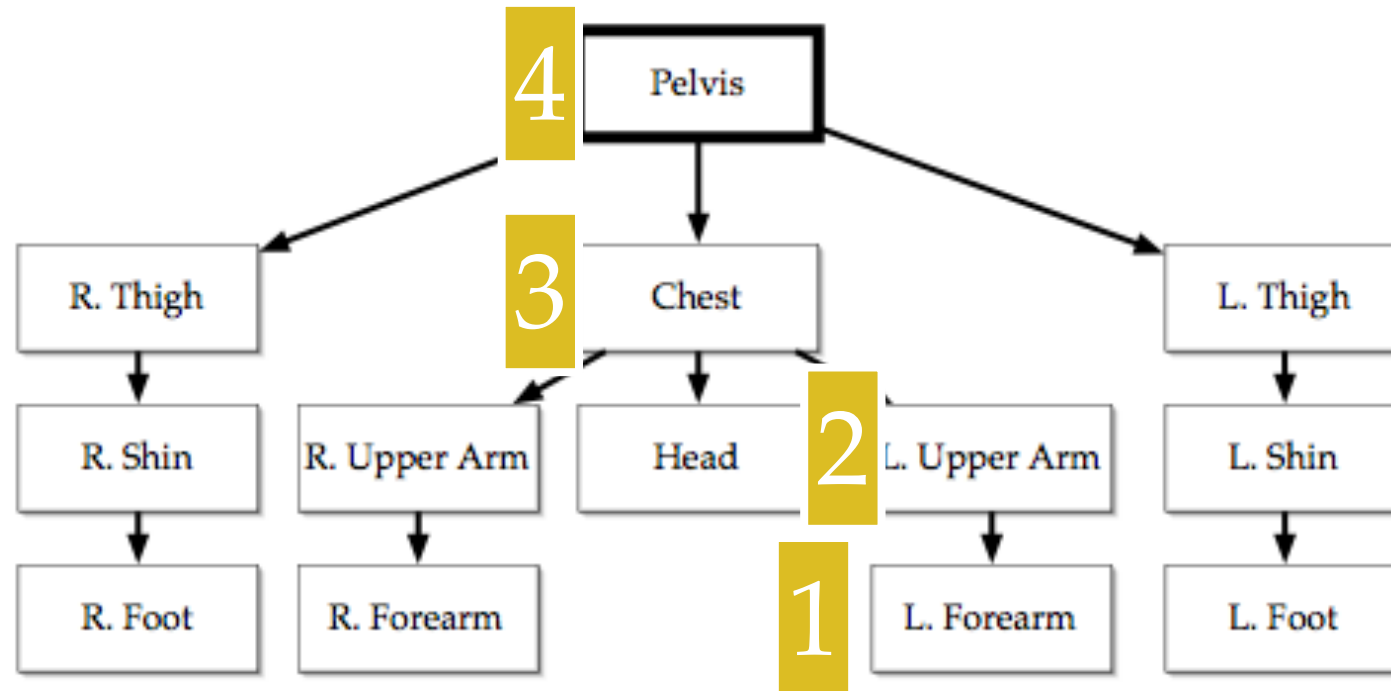
- This hierarchy makes drawing easier
- Let's look at drawing the left hand

Drawing Left Hand

- Left hand is part of forearm
 - defined in forearm's *local coordinates*
 - transform to upper arm's *LCS*
 - then transform to chest's *LCS*
 - then to pelvis' *LCS*
 - finally to *WCS*



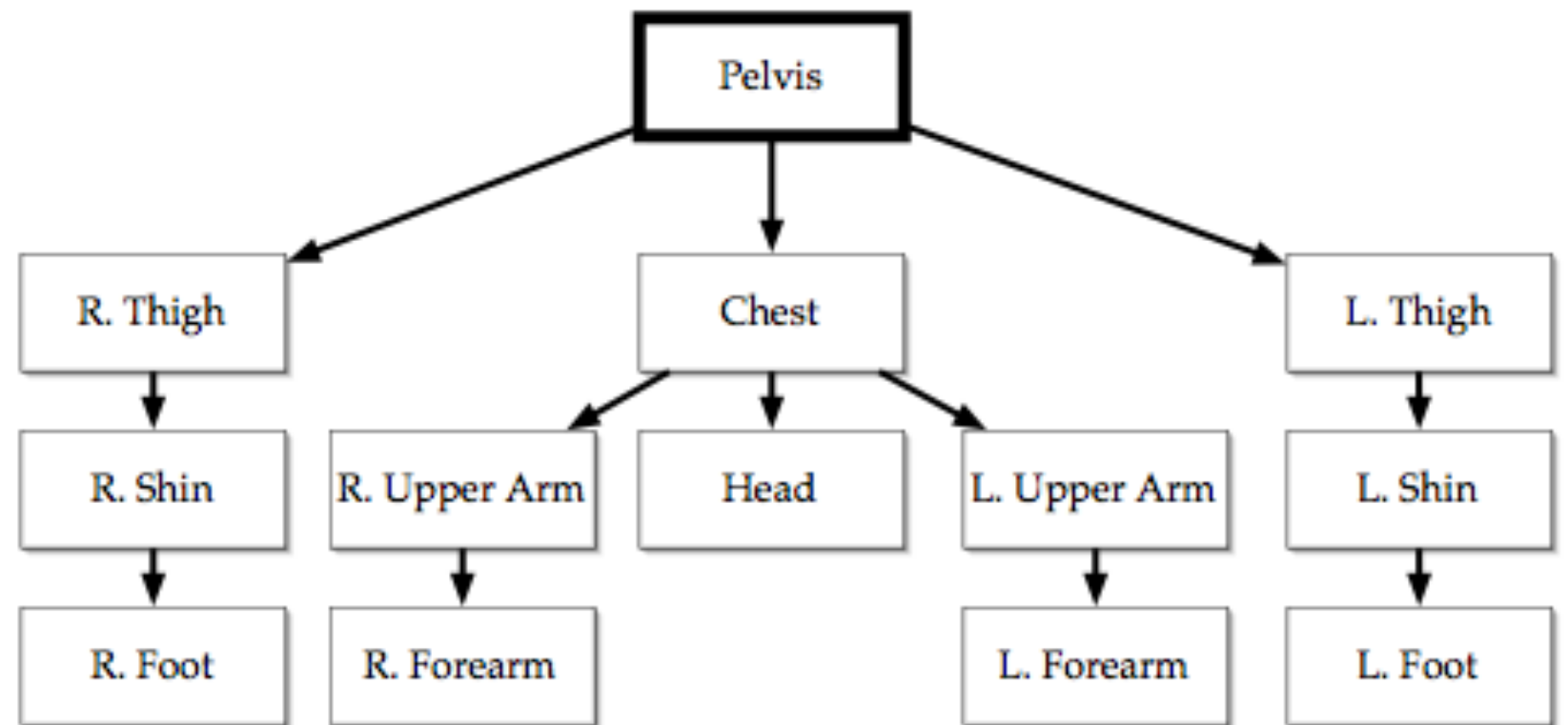
Left Hand Transformations



- Transformations inherited from hierarchy
 - we call them *hierarchical transformations*
 - diagram is the *transformation hierarchy*
- Right hand shares some of these

Drawing the Man

```
Apply T_pelvis
Draw Pelvis
Apply T_chest
Draw Chest
Apply T_L_arm
Draw L Upper Arm
Apply T_L_forearm
Draw L Forearm
Remove T_L_forearm
Remove T_L_arm
Apply T_head
Draw head
Remove T_head
Apply T_R_arm
Draw R Upper Arm
```



Traverse the hierarchy:
going down, apply matrix
going up, remove it

Matrix Stacks

- Since this is Computer Science
 - we can represent this with *stacks*
 - *push* another matrix going down
 - *pop* a matrix going up
 - and OpenGL has this built in



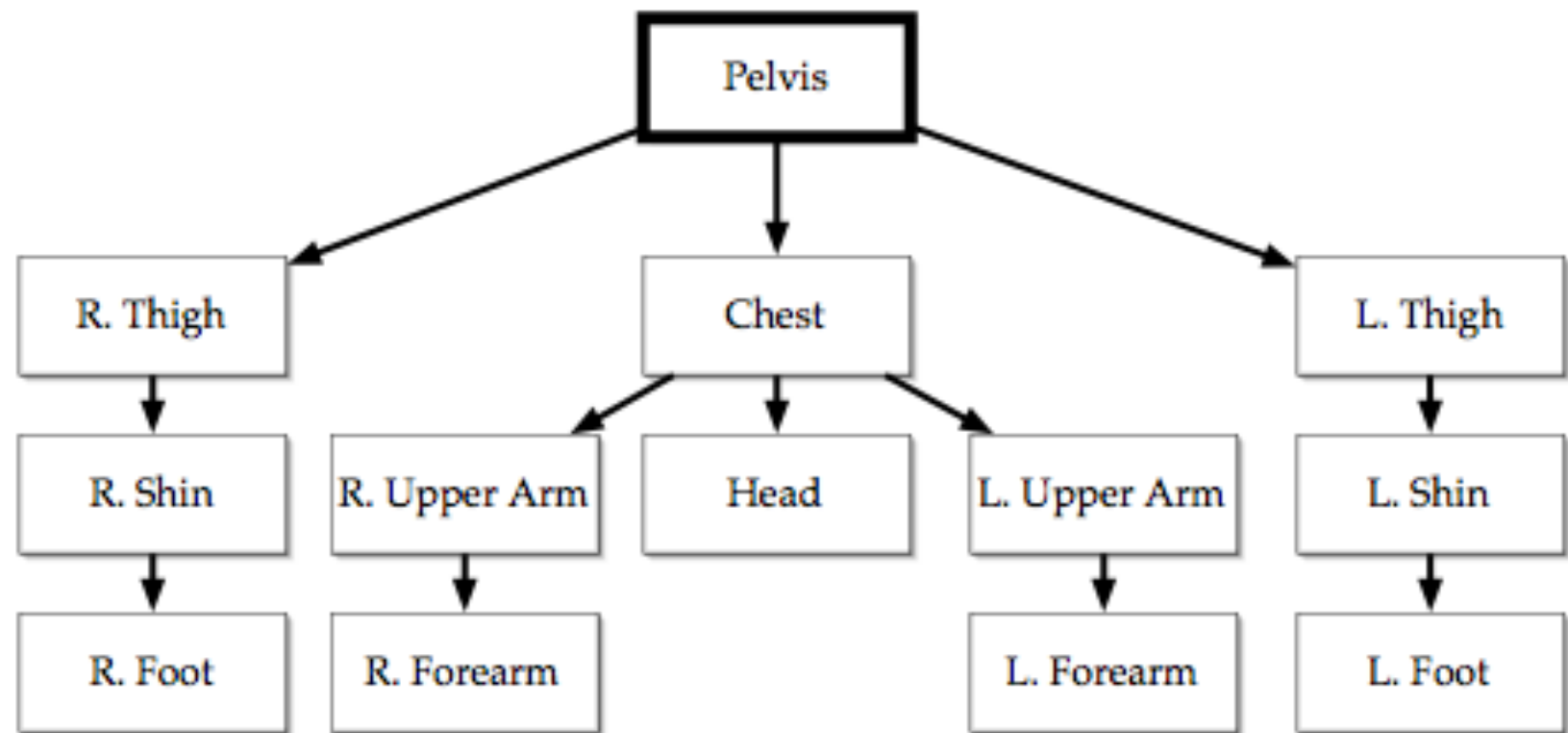
glPushMatrix()

- glPushMatrix() pushes current matrix
 - and gives you a copy to work with
- glPopMatrix() gets rid of copy
 - and reverts to last version on stack
- Like glBegin(), OpenGL doesn't balance them
 - make sure you do



Drawing the Man

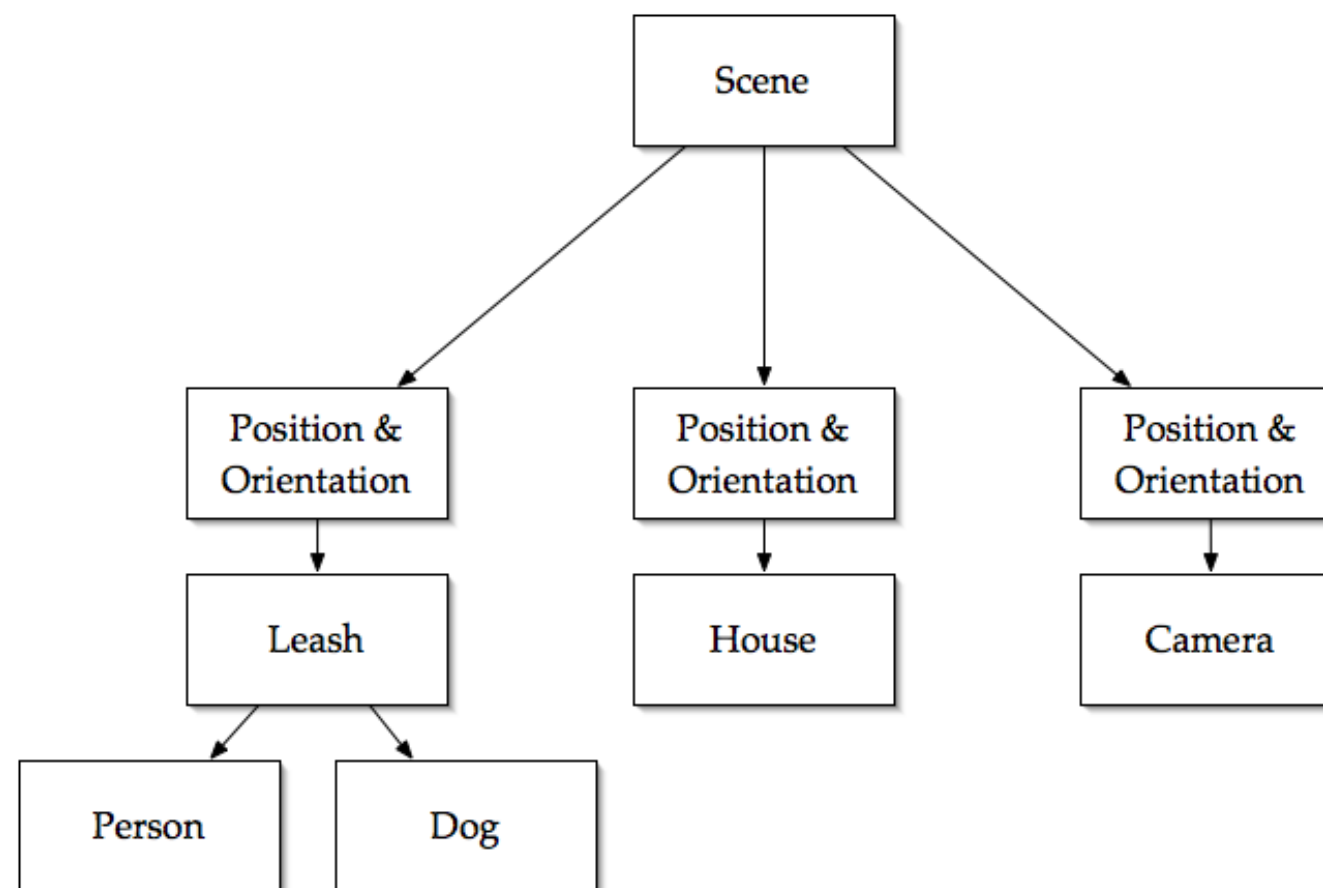
```
glPushMatrix()  
Apply T_pelvis  
Draw Pelvis  
glPushMatrix()  
Apply T_chest  
Draw Chest  
glPushMatrix()  
Apply T_L_arm  
Draw L Upper Arm  
glPushMatrix()  
Apply T_L_forearm  
Draw L Forearm  
glPopMatrix()  
glPopMatrix()  
glPushMatrix()  
Apply T_head  
Draw head  
glPopMatrix(), &c. &c.
```



Traverse the hierarchy:
going down, apply matrix
going up, remove it

Scene Graphs

- General form of animation hierarchy
- Hierarchical description of a *scene*



Terminology

- A *frame* is a single image in a sequence
- A *bone* is a piece of an articulated object
- A *joint* is where two bones meet
- A *pose* is the set of rotations for a frame

Generating Poses

- How *do* we determine the poses?
 - motion capture
 - keyframe interpolation
 - physical simulation
 - inverse kinematics



Motion Capture

- Measure the joint angles of a person
 - then build a model of the person
- Commonly used in
 - movies (Planet of the Apes)
 - sports games (FIFA)
 - Starting to become a potential VR interface



Mocap Problems

- Motion only works for one character
 - looks wrong on smaller / larger
- Hard to measure joint angles
 - surface occlusion, markers off-centre
- Requires expensive hardware & people
- Only works for real animals / humans



Mocap – New inexpensive Methods

- **Using Time of Flight methods**
 - Leap Motion
 - Microsoft's KINECT
- **Using just inertia sensors -**
 - Perception Neuron
 - Developed here in Beijing
 - No need for external optical tracking
 - No large setup area as directly attached to the body
- **Measuring muscle movement using EMG's**
 - **Myo Gesture Control Armband**
 - Advantage that the movement is sensed before your hand actual moves, thus a perfect tool for tele-presence as you can synchronise interactions in real time across the world.
- **Using Camera and DL computer vision models**



Keyframe Interpolation

- Some frames are important (i.e. *key*)
 - artist specifies joint angles at keyframes
 - compute angles for frames in between
 - simple interpolation
- Requires well-trained artists



Physics Simulation

- Simulate Newtonian mechanics
- Much more complex than it sounds
 - and doesn't give humans control
- Best for inanimate objects
 - we must detect collisions
 - even for human motions



Inverse Kinematics

It is primarily used for creating realistic and efficient character movement by calculating the required joint angles to place a part of a character (like a hand or foot) in a specific position in space.

- 1. End Effector:** The target point, typically a hand, foot, or other part of the character you want to position. The animator sets a goal for where the end effector should be located.
- 2. Joint Chains:** A series of connected joints (like shoulder, elbow, and wrist) form a **kinematic chain**. IK calculations are performed on these joint chains to determine how to position each joint so that the end effector reaches its target.
- 3. IK Solvers:** Algorithms (like Jacobian Inverse or CCD - Cyclic Coordinate Descent) are used to solve the IK problem. The solvers calculate the necessary joint rotations to position the end effector accurately.



Animation Challenges

- Collision detection & response
- Smooth interpolation (*blending*) of poses
- Smooth *skinning* between joints
- Mapping to different characters

