

Advancements in Graph Neural Networks

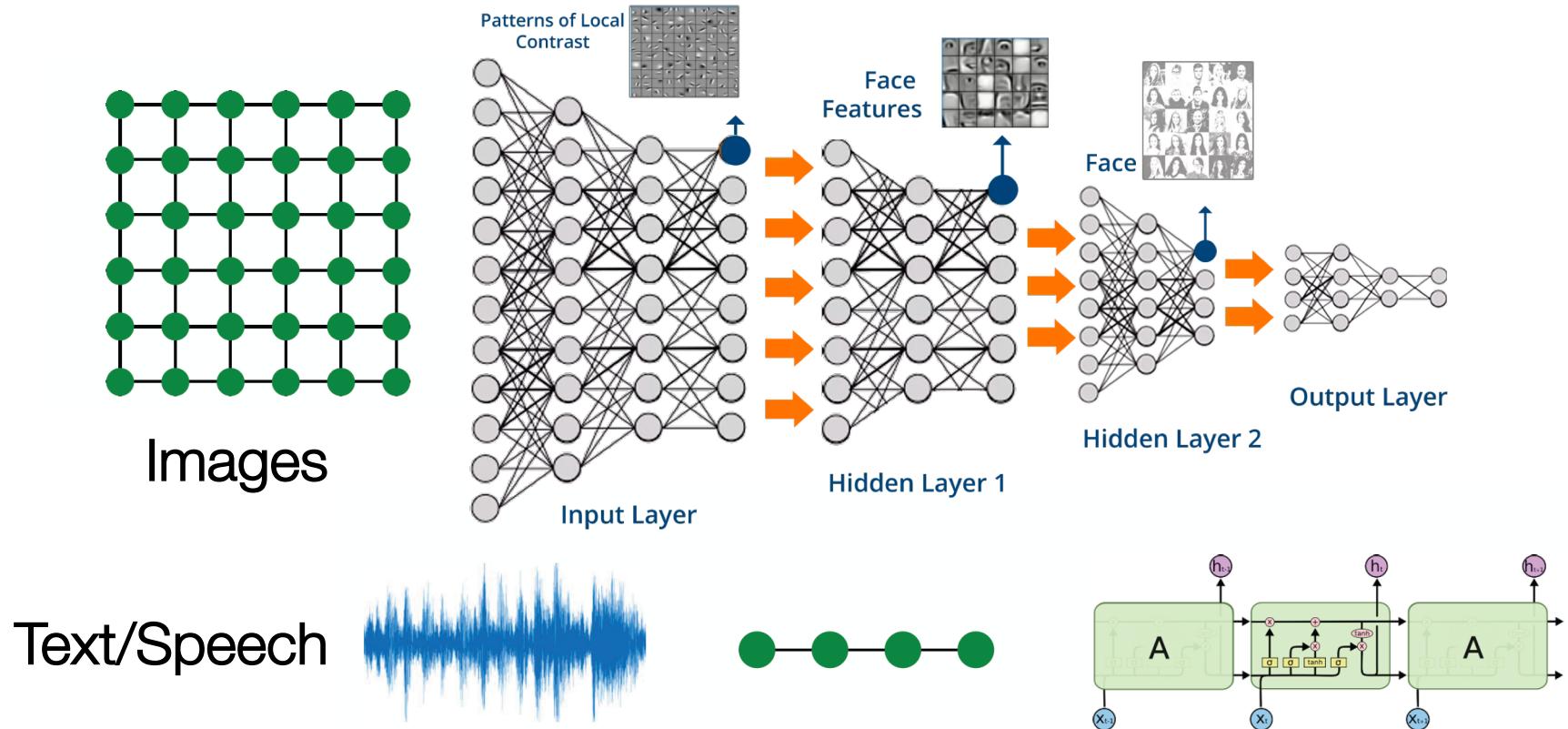
Jure Leskovec



CHAN ZUCKERBERG
BIOHUB

Includes joint work with H. Ren, W. Hamilton, R. Ying, J. You,
M. Zitnik, W. Hu, K. Xu, S. Jegelka

Modern ML Toolbox



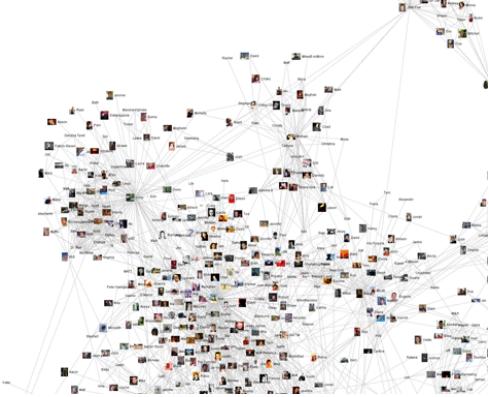
Modern deep learning toolbox is designed for simple sequences & grids

But not everything
can be represented as
a sequence or a grid

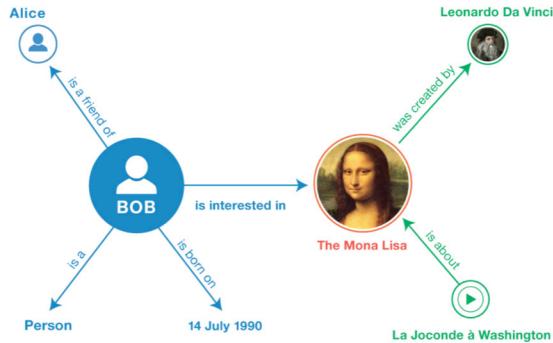
**How can we develop neural
networks that are much more
broadly applicable?**

New frontiers beyond classic neural
networks that learn on images and
sequences

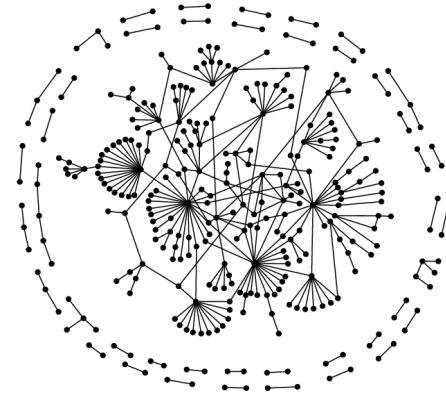
Networks of Interactions



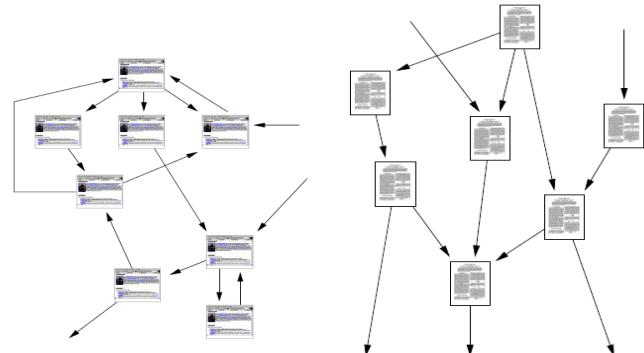
Social networks



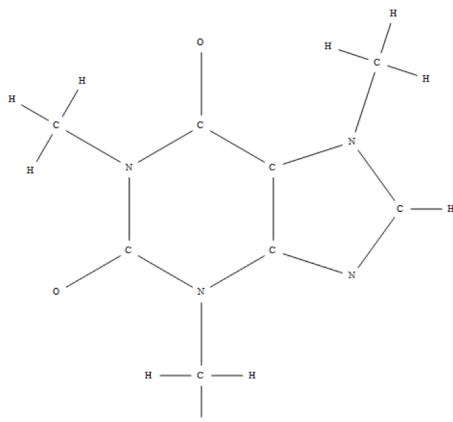
Knowledge graphs



Biological networks



Complex Systems

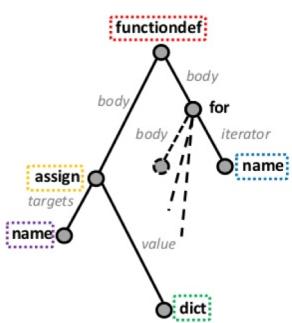


Molecules

```
def encode(obj):
    ...
    for key,value in obj.items():
        if isinstance(value,dict):
            e[key] = encode(value)
        elif isinstance(value,complex):
            e[key] = {'type': 'complex',
                      'r': value.real,
                      'i': value.imag}
    return e
```

```
import ast
tree = ast.parse(" ")
...

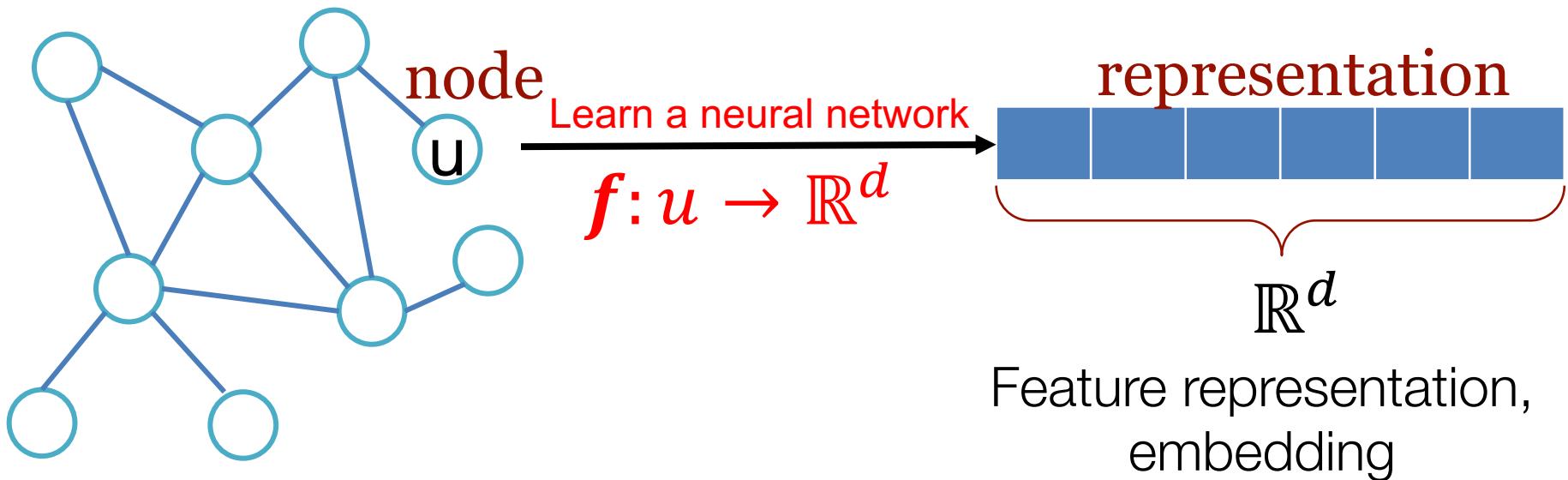
```



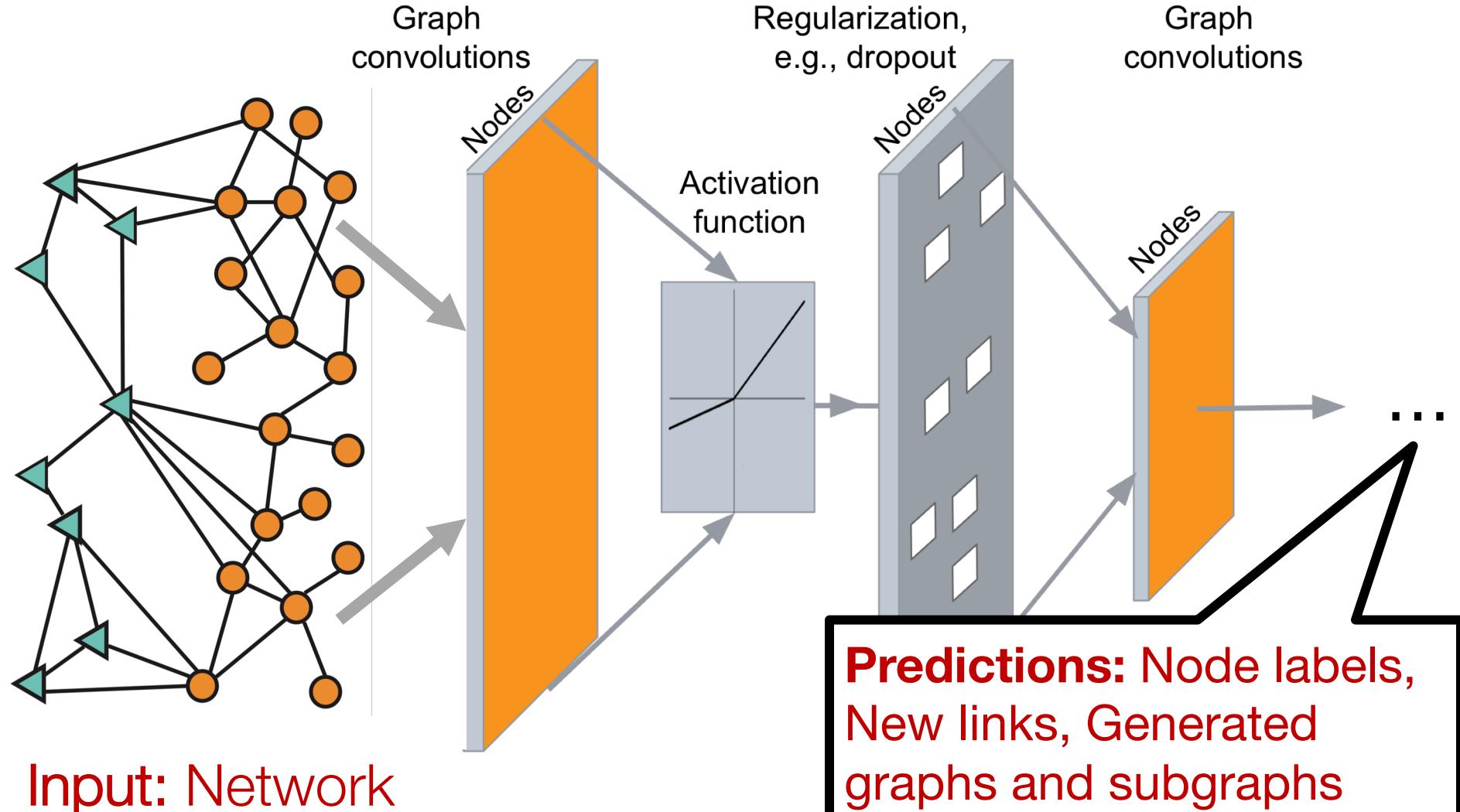
Code

Goal: Representation Learning

Map nodes to d-dimensional embeddings such that similar nodes in the network are embedded close together



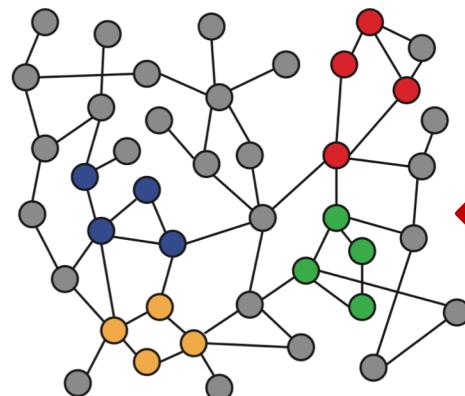
Deep Learning in Graphs



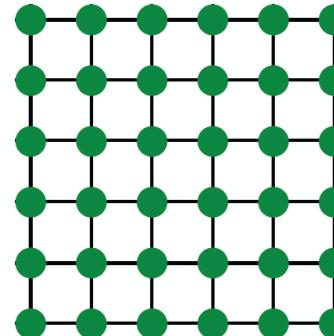
Why is it Hard?

Networks are complex!

- Arbitrary size and complex topological structure (i.e., no spatial locality like grids)



Networks



Images



Text

- No fixed node ordering or reference point
- Often dynamic and have multimodal features

GraphSAGE: Graph Neural Networks

[Inductive Representation Learning on Large Graphs.](#)

W. Hamilton, R. Ying, J. Leskovec. Neural Information Processing Systems (NIPS), 2017.

[Representation Learning on Graphs: Methods and Applications.](#)

W. Hamilton, R. Ying, J. Leskovec. IEEE Data Engineering Bulletin, 2017.

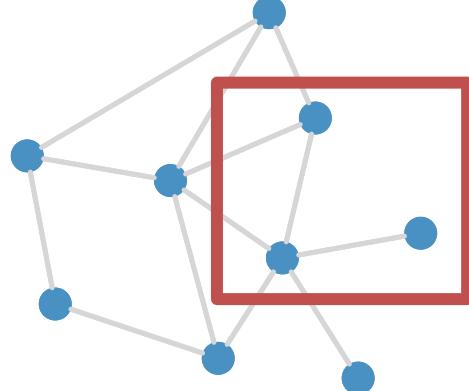
<http://snap.stanford.edu/graphsage>

Idea: Convolutional Networks

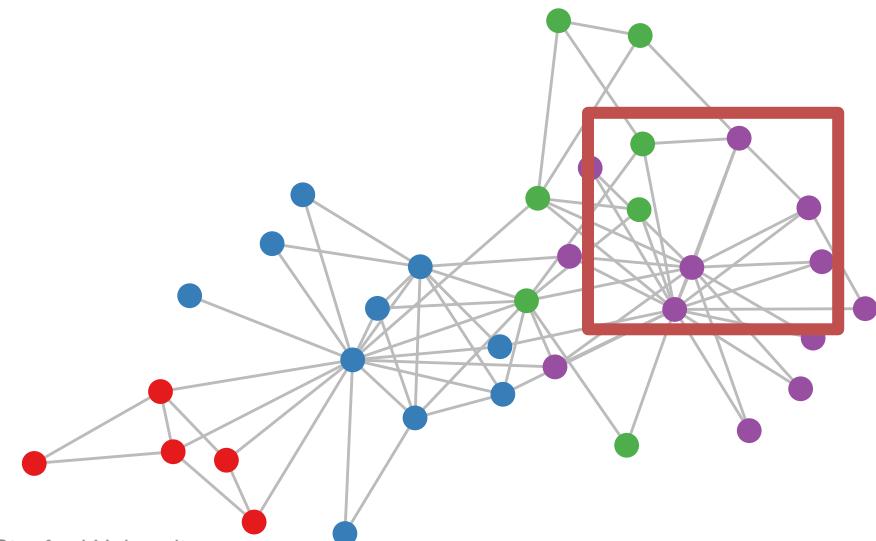
Goal is to generalize convolutions
beyond simple lattices

Leverage node features (text, images)

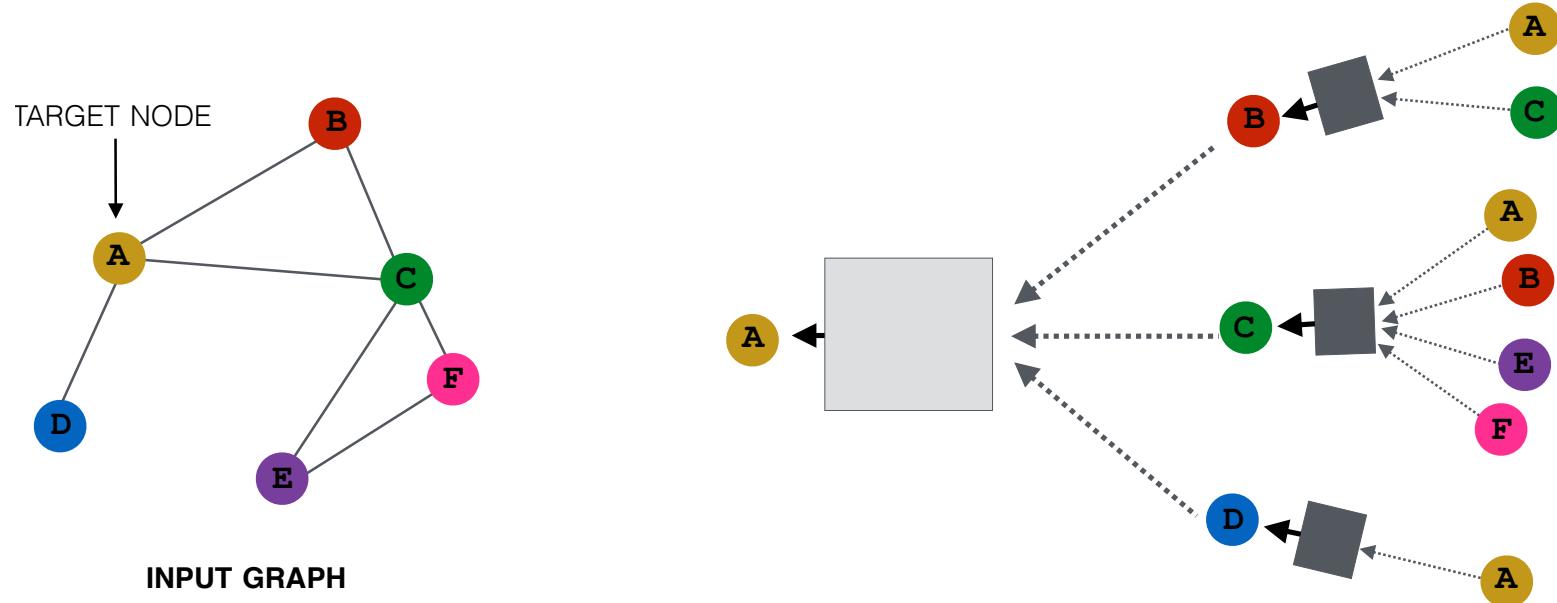
But real-world graphs look like this:



or this:



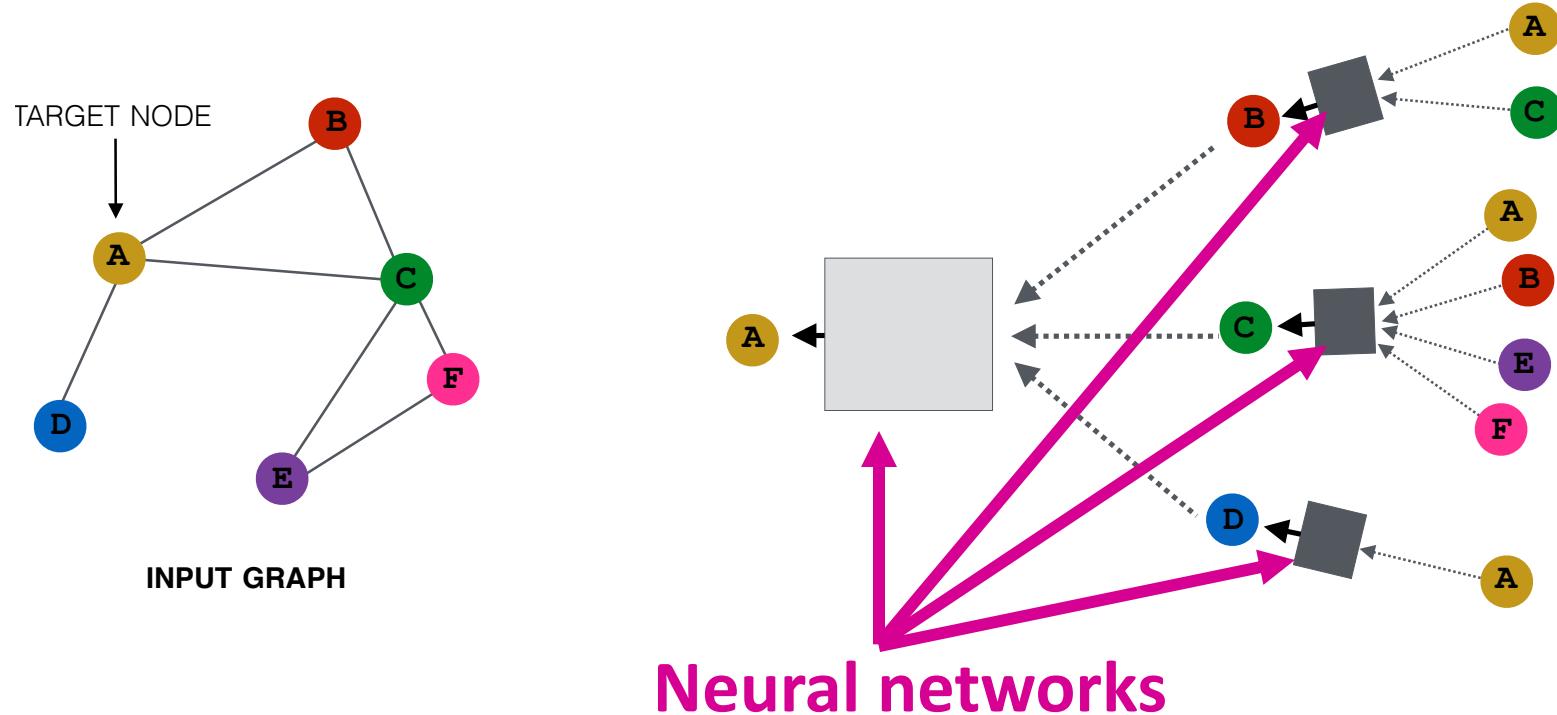
Graph Neural Networks



Each node defines a computation graph

- Each edge in this graph is a transformation/aggregation function

Graph Neural Networks

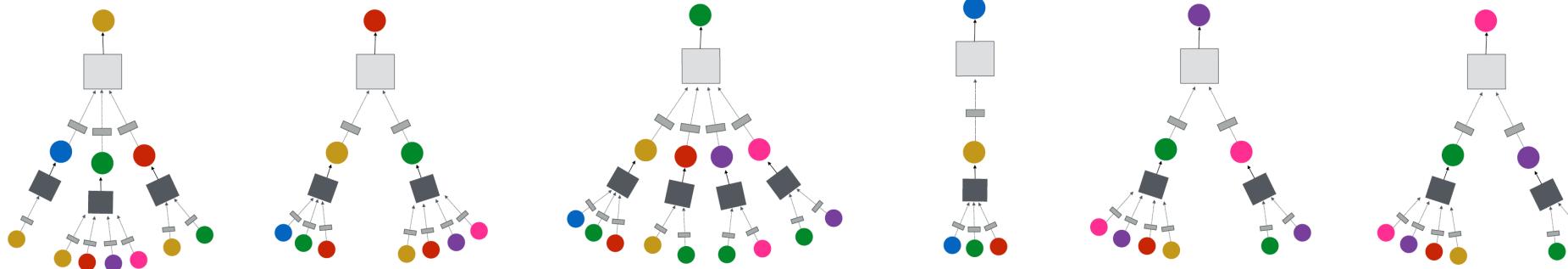
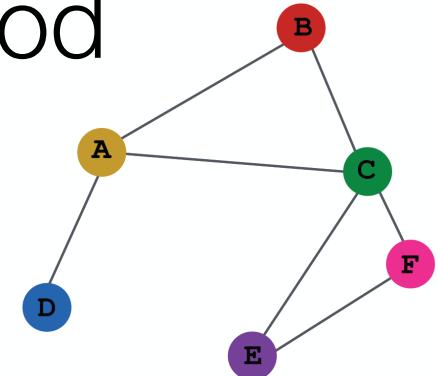


Intuition: Nodes aggregate information from their neighbors using neural networks

Idea: Aggregate Neighbors

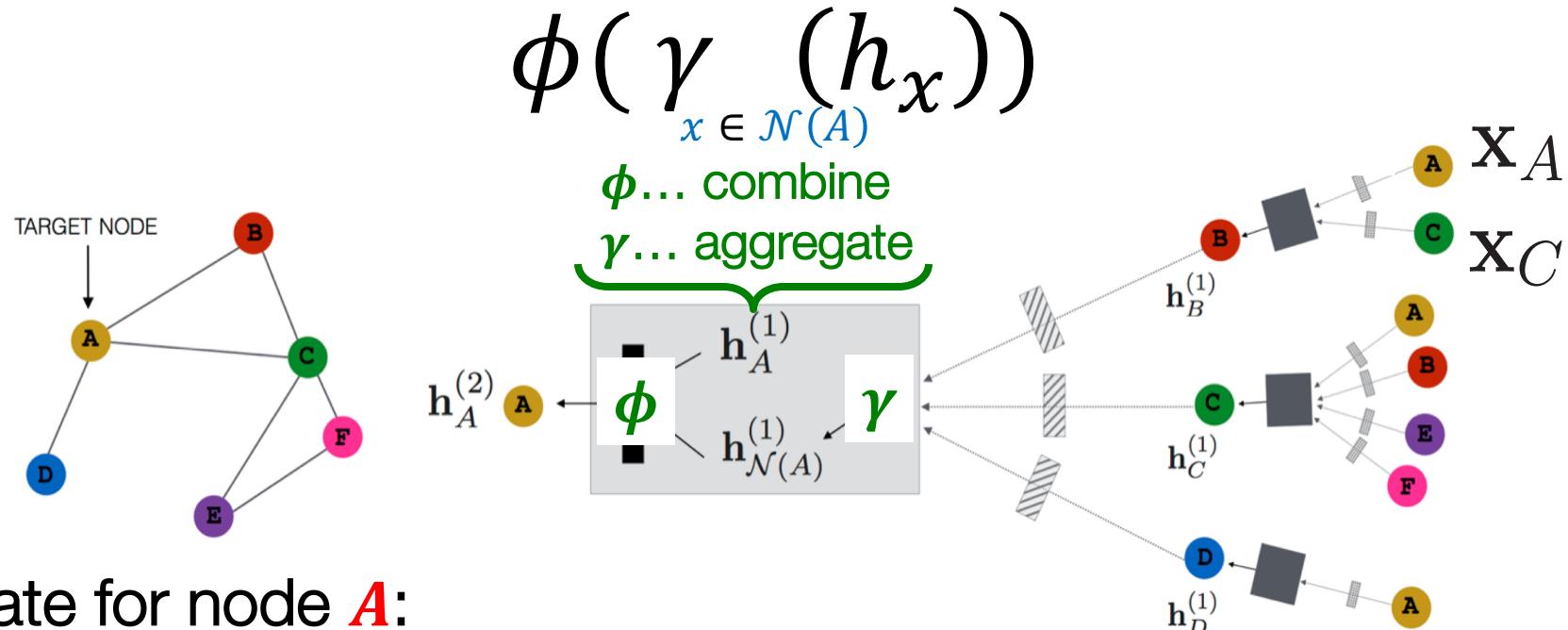
Intuition: Network neighborhood defines a computation graph

Every node defines a computation graph based on its neighborhood!



Can be viewed as learning a generic linear combination of graph low-pass and high-pass operators

Our Approach: GraphSAGE



Update for node A :

$$h_A^{(k+1)} = \sigma \left(W^{(k)} h_A^{(k)}, \gamma \left(\sigma(Q^{(k)} h_x^{(k)}) \right) \right)$$

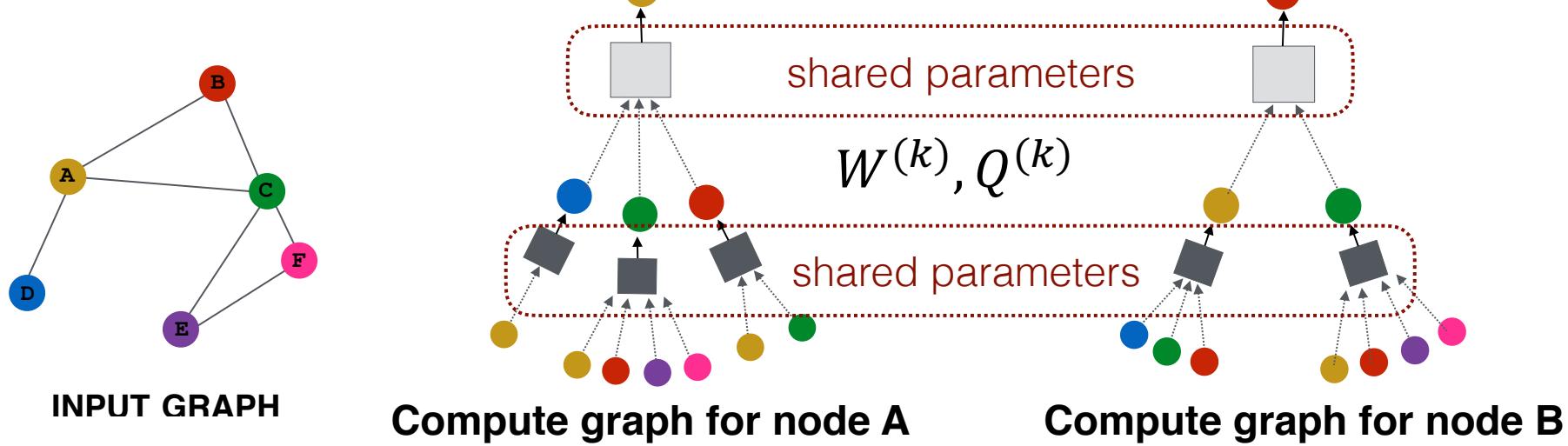
where

- $h_A^{(k+1)}$ is the $k + 1^{\text{st}}$ level embedding of node A .
- $h_A^{(k)}$ is Transform A 's own embedding from level k .
- $h_x^{(k)}$ is Transform and aggregate embeddings of neighbors n .

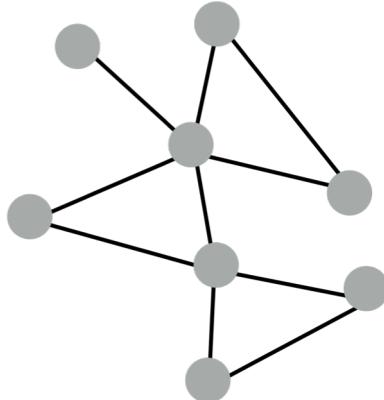
- $h_A^{(0)} = \text{attributes } X_A \text{ of node } A$, $\sigma(\cdot)$ is a sigmoid activation function

GraphSAGE: Training

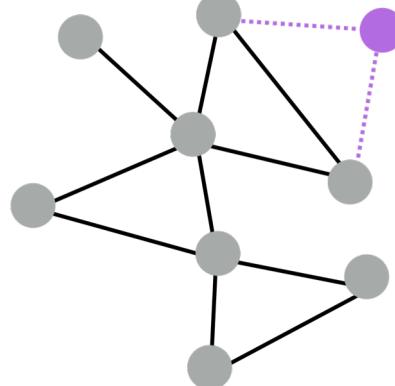
- Aggregation parameters are shared for all nodes
- Number of model parameters is independent of $|V|$
- Can use different loss functions:
 - Classification/Regression: $\mathcal{L}(h_A) = \|y_A - f(h_A)\|^2$
 - Pairwise Loss: $\mathcal{L}(h_A, h_B) = \max(0, 1 - dist(h_A, h_B))$



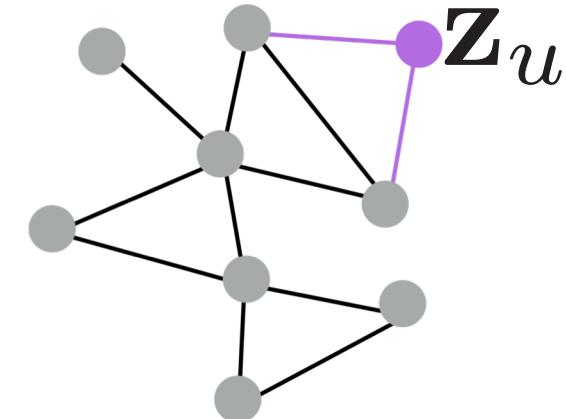
Inductive Capability



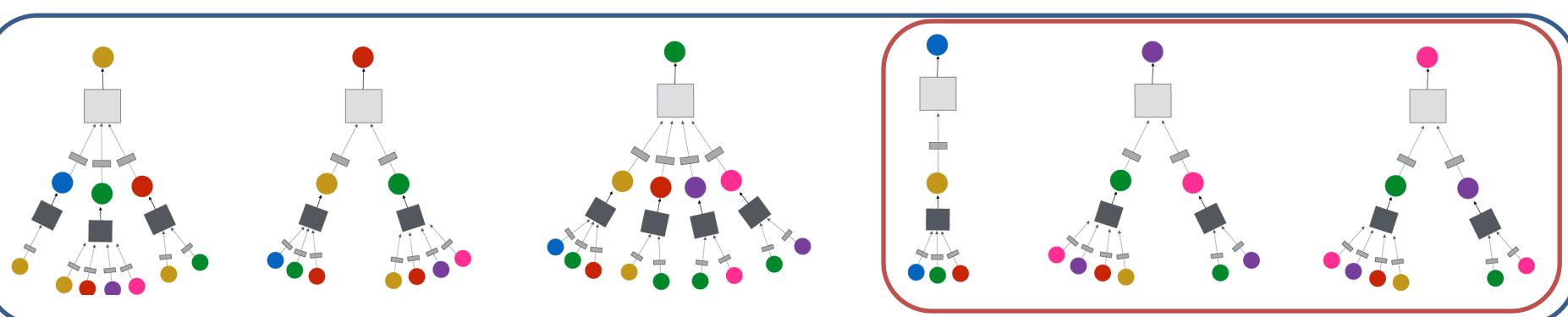
train with a snapshot



new node arrives

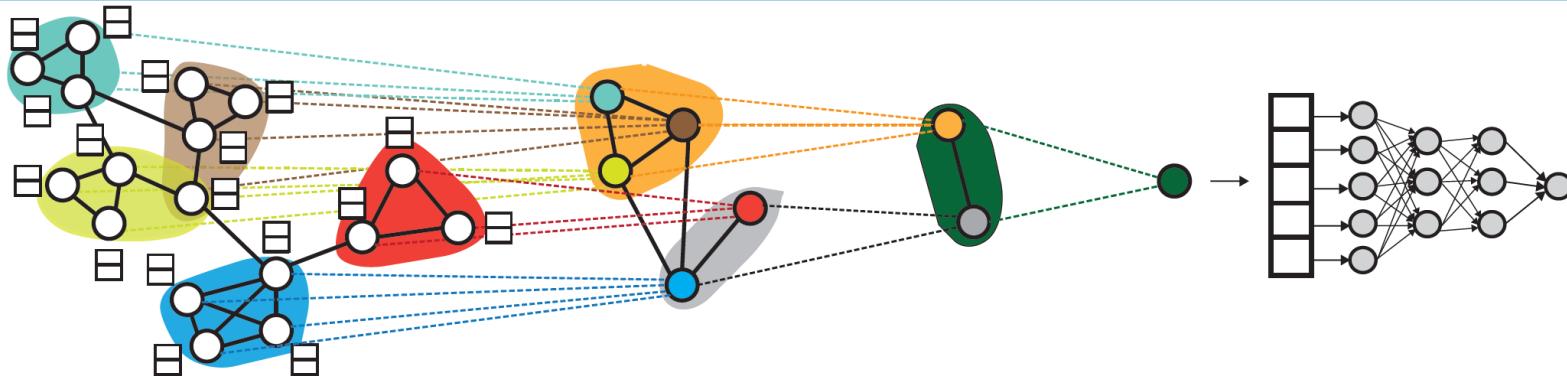


generate embedding
for new node



Even for nodes we
never trained on!

DIFFPOOL: Pooling for GNNs



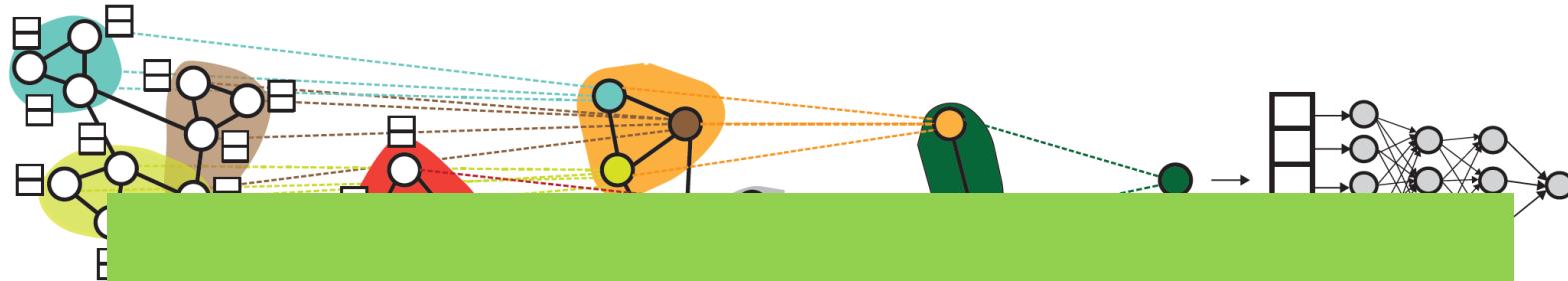
Don't just embed individual nodes. **Embed the entire graph.**

Problem: Learn how to hierarchical pool the nodes to embed the entire graph

Our solution: DIFFPOOL

- Learns hierarchical pooling strategy
- Sets of nodes are pooled hierarchically
- Soft assignment of nodes to next-level nodes

DIFFPOOL: Pooling for GNNs



Does the entire graph have to be processed? Can we learn the entire graph representation? What is the expressive power of Graph Neural Networks?

Problem: How expressive are Graph Neural Networks?

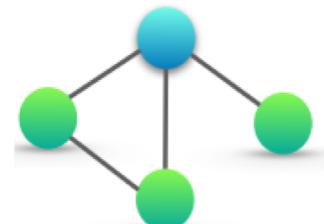
Our Solution:

- Learns hierarchical pooling strategy
- Sets of nodes are pooled hierarchically
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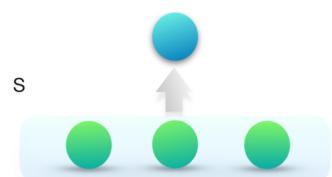
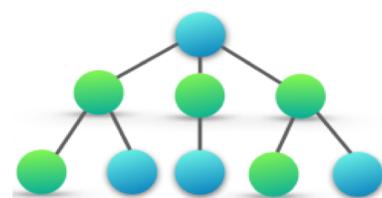
How expressive are GNNs?

Theoretical framework: Characterize GNN's discriminative power:

- Characterize upper bound of the discriminative power of GNNs
- Propose a maximally powerful GNN
- Characterize discriminative power of popular GNNs

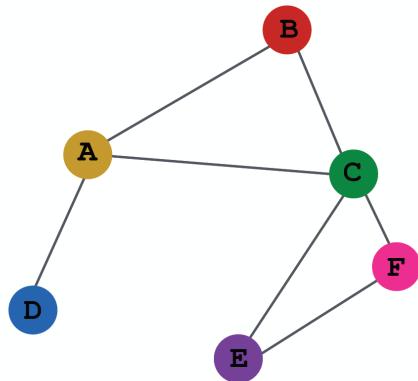


GNN tree:

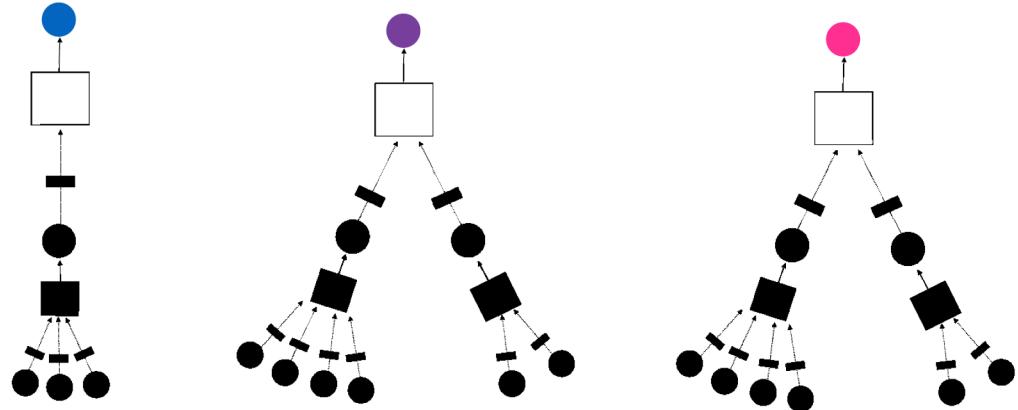


Key Insight: Rooted Subtrees

Graph:

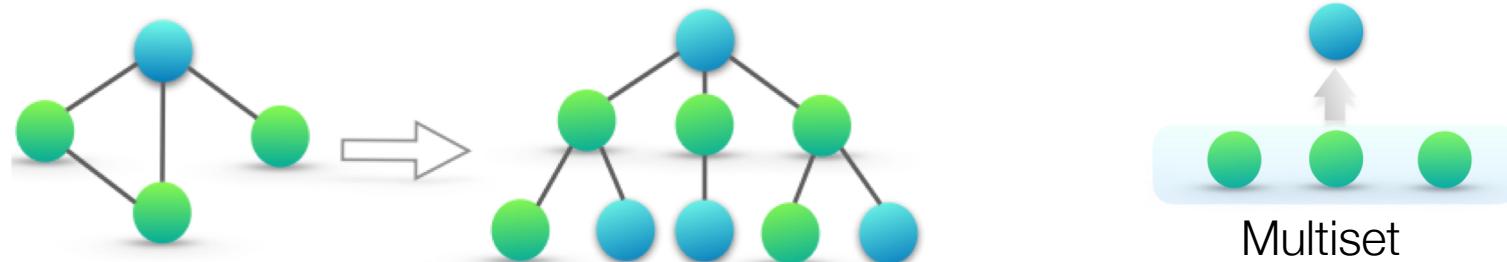


GNN distinguishes:



The most powerful GNN is able to distinguish rooted subtrees of different structure

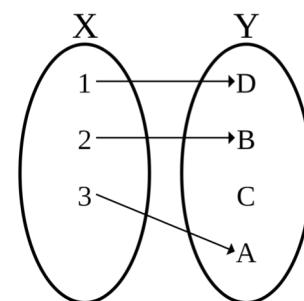
Discriminative Power of GNNs



Idea: If GNN functions are injective, GNN can capture/distinguish the rooted subtree structures

Theorem: The most discriminative GNN uses injective multiset function for neighbor aggregation

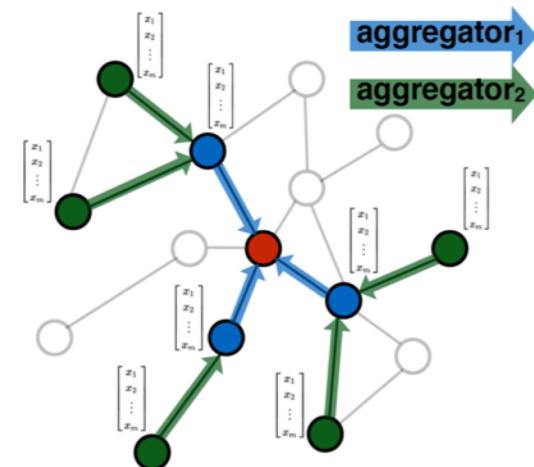
If the aggregation function is injective, GNN can fully capture/distinguish the rooted subtree structures



Three Consequences of GNNs

1) The GNN does two things:

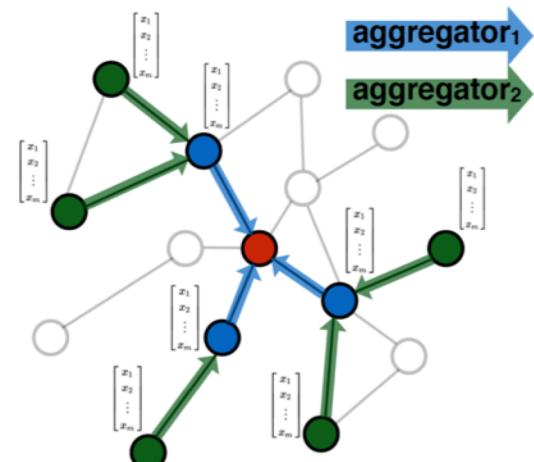
- Learns how to “borrow” feature information from nearby nodes to enrich the target node
- Each node can have a different computation graph and the network is also able to capture/learn its structure



Three Consequences of GNNs

2) Computation graphs can be chosen:

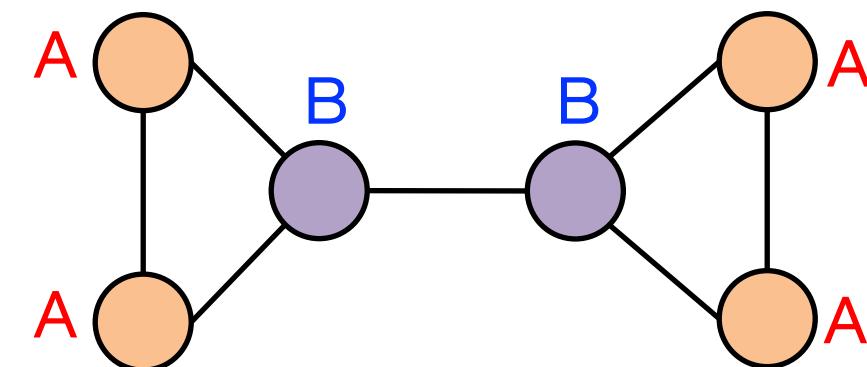
- Aggregation does not need to happen across all neighbors
- Neighbors can be strategically chosen/sampled
- Leads to big gains in practice



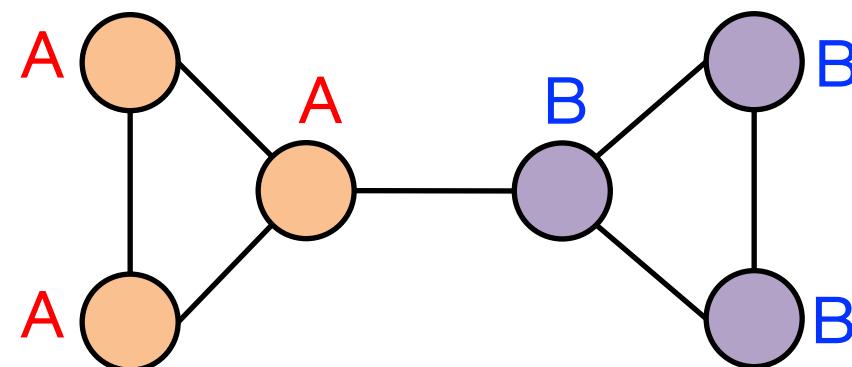
Three Consequences of GNNs

3) We understand GNN failure cases:

- GNNs fail to distinguish isomorphic nodes
- Structure-aware **Vs.** Position-aware

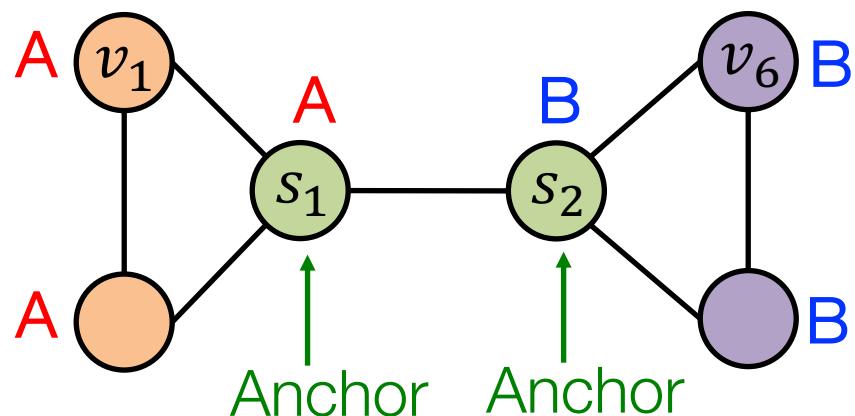


Vs.



PGNN: Position Aware GNNs

- Key idea: Anchors
 - Characterize node's position relative to a set of randomly selected anchor nodes and sets of nodes

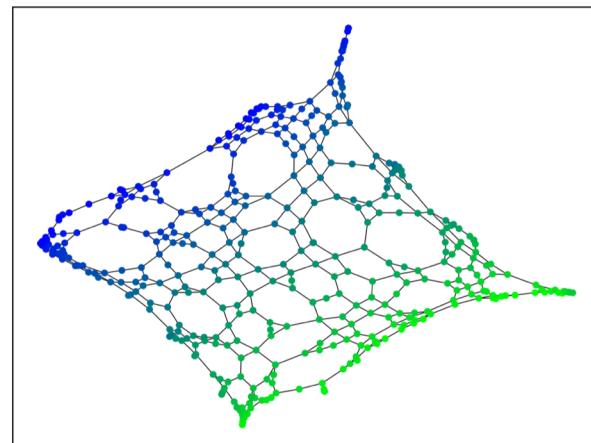


Distance to Anchor:

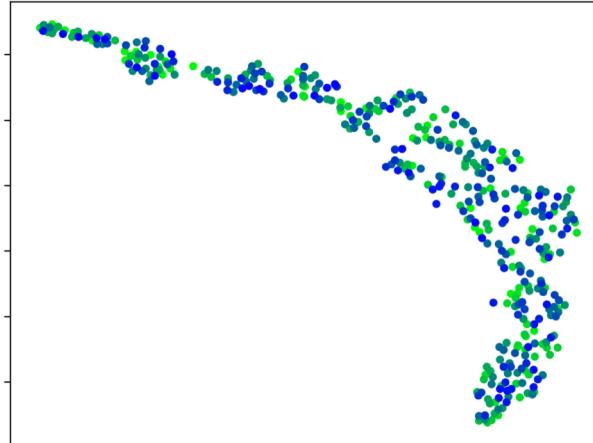
	s_1	s_2
v_1	1	2
v_6	2	1

PGNN: Visualizing Embeddings

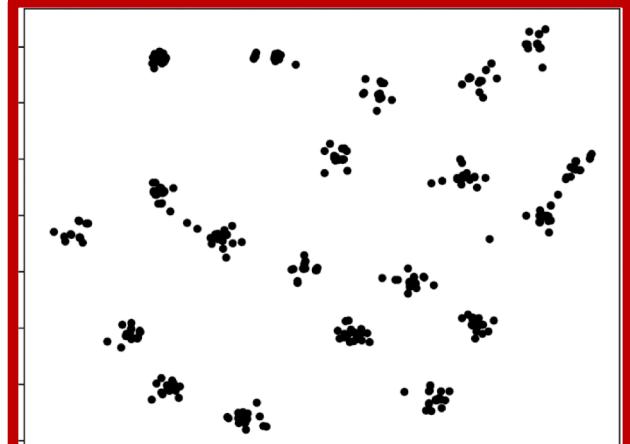
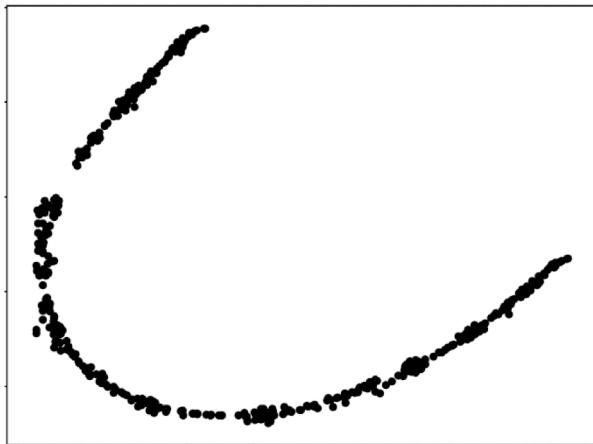
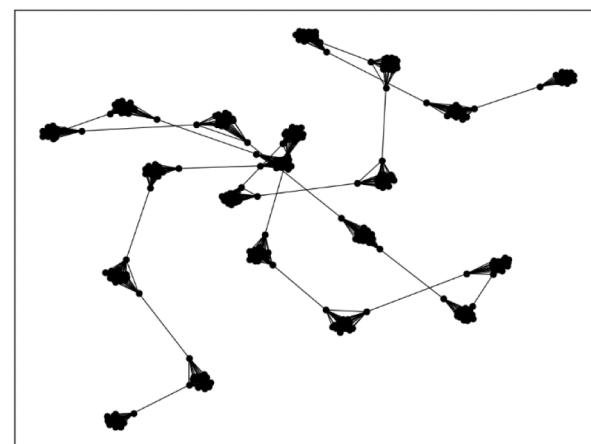
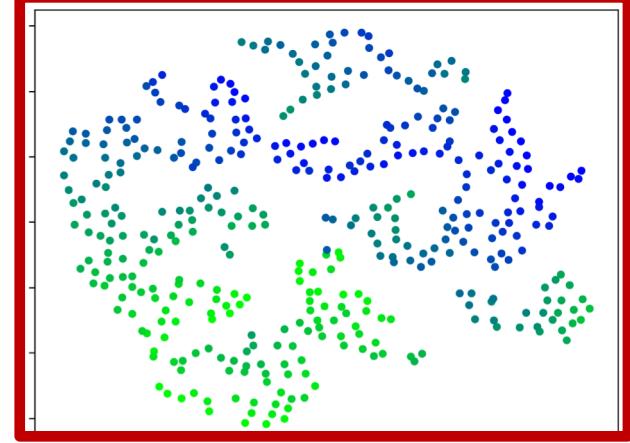
Input graph



GNN embedding



P-GNN embedding

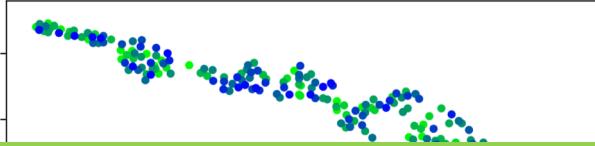


PGNN: Visualizing Embeddings

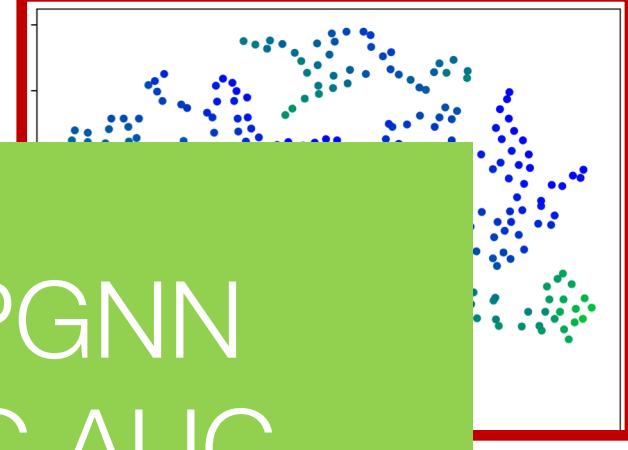
Input graph



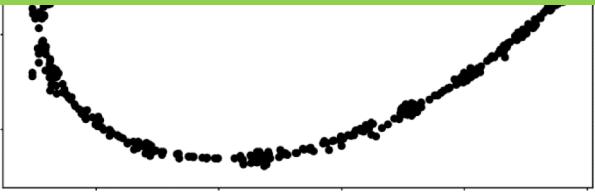
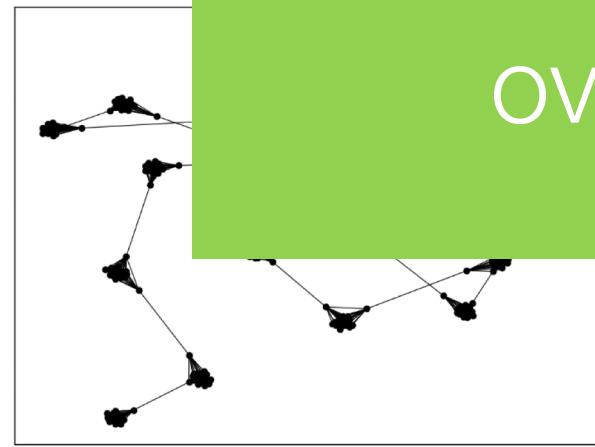
GNN embedding



P-GNN embedding



On real datasets PGNN
obtains +61% ROC AUC
over GCN, GAT, GIN

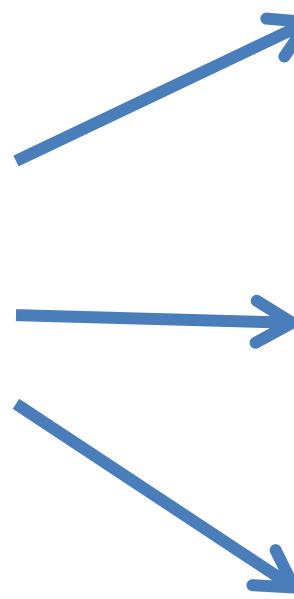
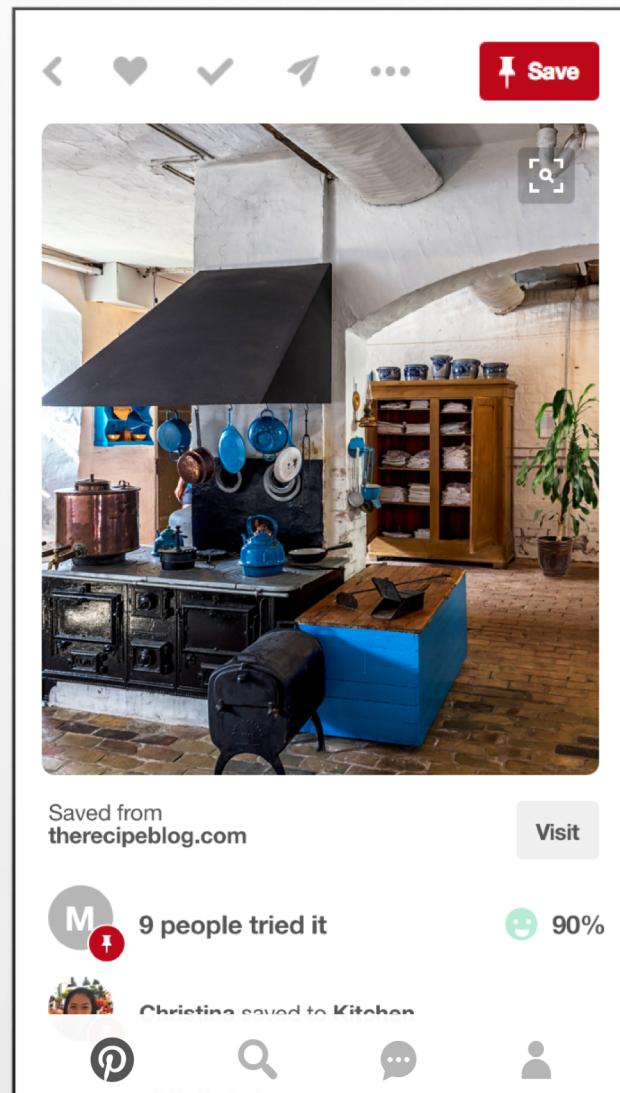


PinSAGE for Recommender Systems

[Graph Convolutional Neural Networks for Web-Scale Recommender Systems.](#) R. Ying, R. He, K. Chen, P. Eksombatchai, W. L. Hamilton, J. Leskovec. *KDD*, 2018.



Pinterest



Blue accents
219 Pins



Vintage kitchen
377 Pins



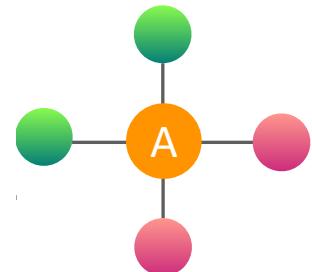
- 300M users
- 4+B pins, 2+B boards



Application: Pinterest

PinSage graph convolutional network:

- **Goal:** Generate embeddings for nodes in a large-scale Pinterest graph containing billions of objects
- **Key Idea:** Borrow information from nearby nodes
 - E.g., bed rail Pin might look like a garden fence, but gates and beds are rarely adjacent in the graph



- Pin embeddings are essential to various tasks like recommendation of Pins, classification, ranking
 - Services like “Related Pins”, “Search”, “Shopping”, “Ads”



Pinterest Graph

Human curated collection of pins



Very ape blue
structured coat

Nitty Gritty

Picked for you
Street style



Hans Wegner chair
Room and Board

Promoted by
Room & Board



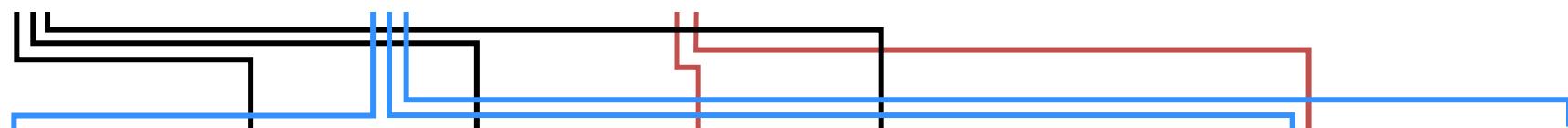
This is just a beautiful
image for thoughts.
Yay or nay, your choice.

14

Annie Teng
Plantation

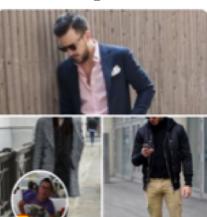
Pins: Visual bookmarks someone has saved from the internet to a board they've created.

Pin features: Image, text, links



mid century modern ...

MJL I -



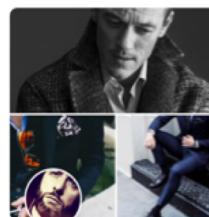
Man Style
Gavin Jones



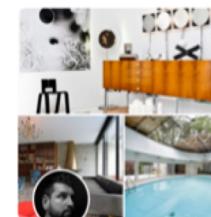
men + style I
FIG + SALT



Plants
HelloSandwich



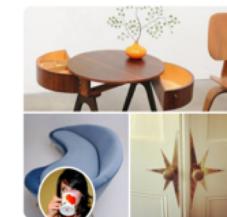
Men's Style
Andrea Sempi



Mid century modern
Tyler Goodro



Plants
Moorea Seal



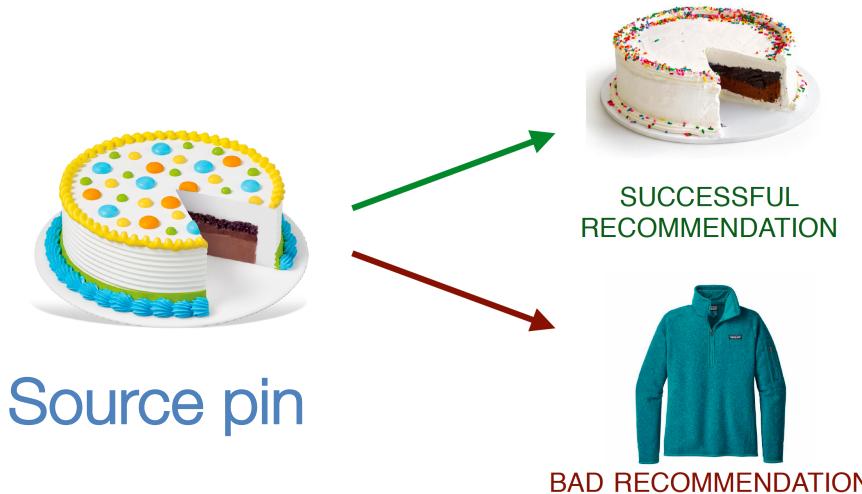
Mid century modern ...
Prettygreentea

Boards

Pin Recommendation



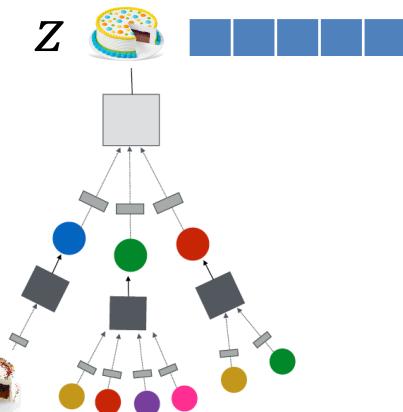
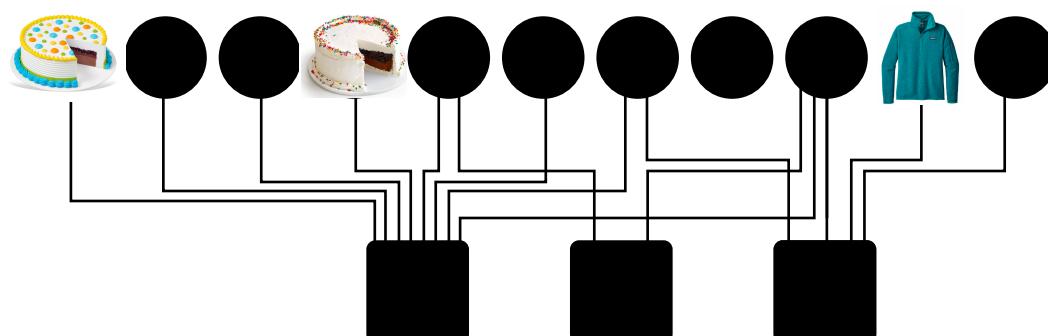
Task: Recommend related pins to users



Task: Learn node embeddings z_i such that

$$d(z_{cake1}, z_{cake2}) < d(z_{cake1}, z_{sweater})$$

Predict whether two nodes in a graph are related



PinSAGE Training



Goal: Identify target pin among 3B pins

- **Issue:** Need to learn with resolution of 100 vs. 3B
- **Massive size:** 3 billion nodes, 20 billion edges
- **Idea:** Use harder and harder negative samples



Source pin



Positive



Easy negative



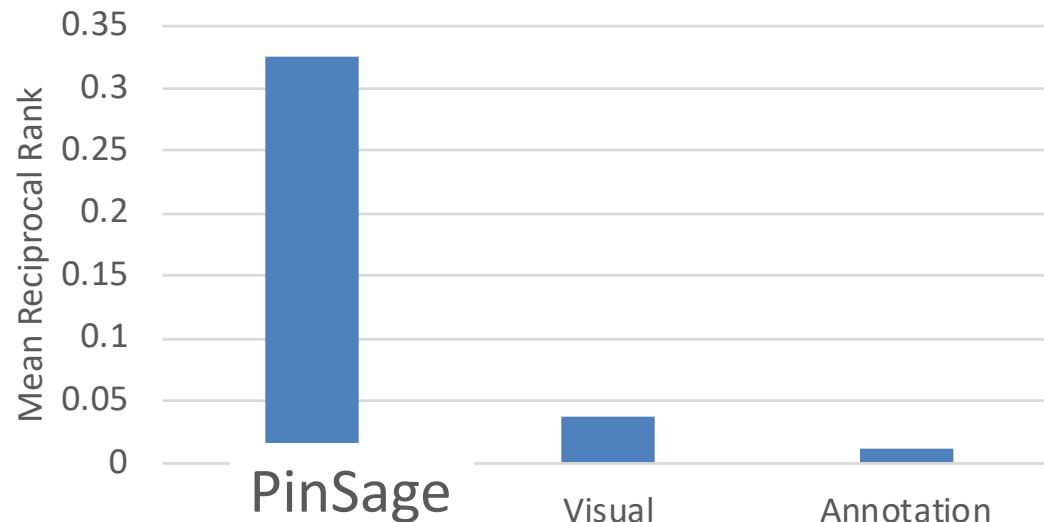
Hard negative

PinSAGE Performance



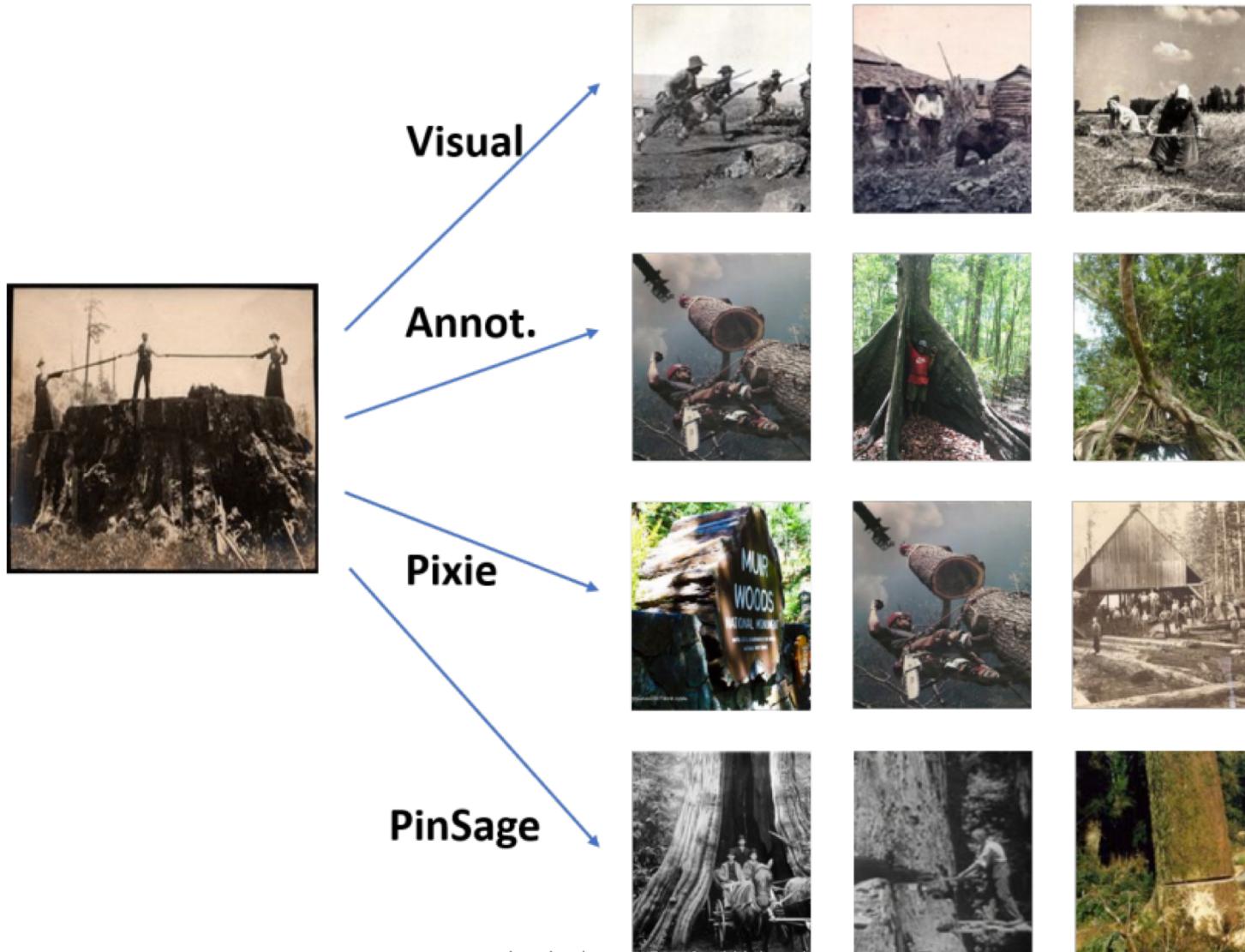
Related Pin recommendations

- Given a user is looking at pin Q, predict what pin X are they going to save next
- Setup: Embed 3B pins, perform nearest neighbor to generate recommendations





PinSAGE Example



Computational Drug Discovery: Drug Side Effect Prediction

[Modeling Polypharmacy Side Effects with Graph Convolutional Networks](#). M. Zitnik, M. Agrawal, J. Leskovec. Bioinformatics, 2018.

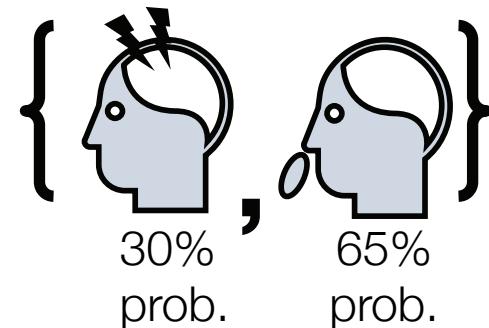
<http://snap.stanford.edu/decagon/>

Polypharmacy side effects

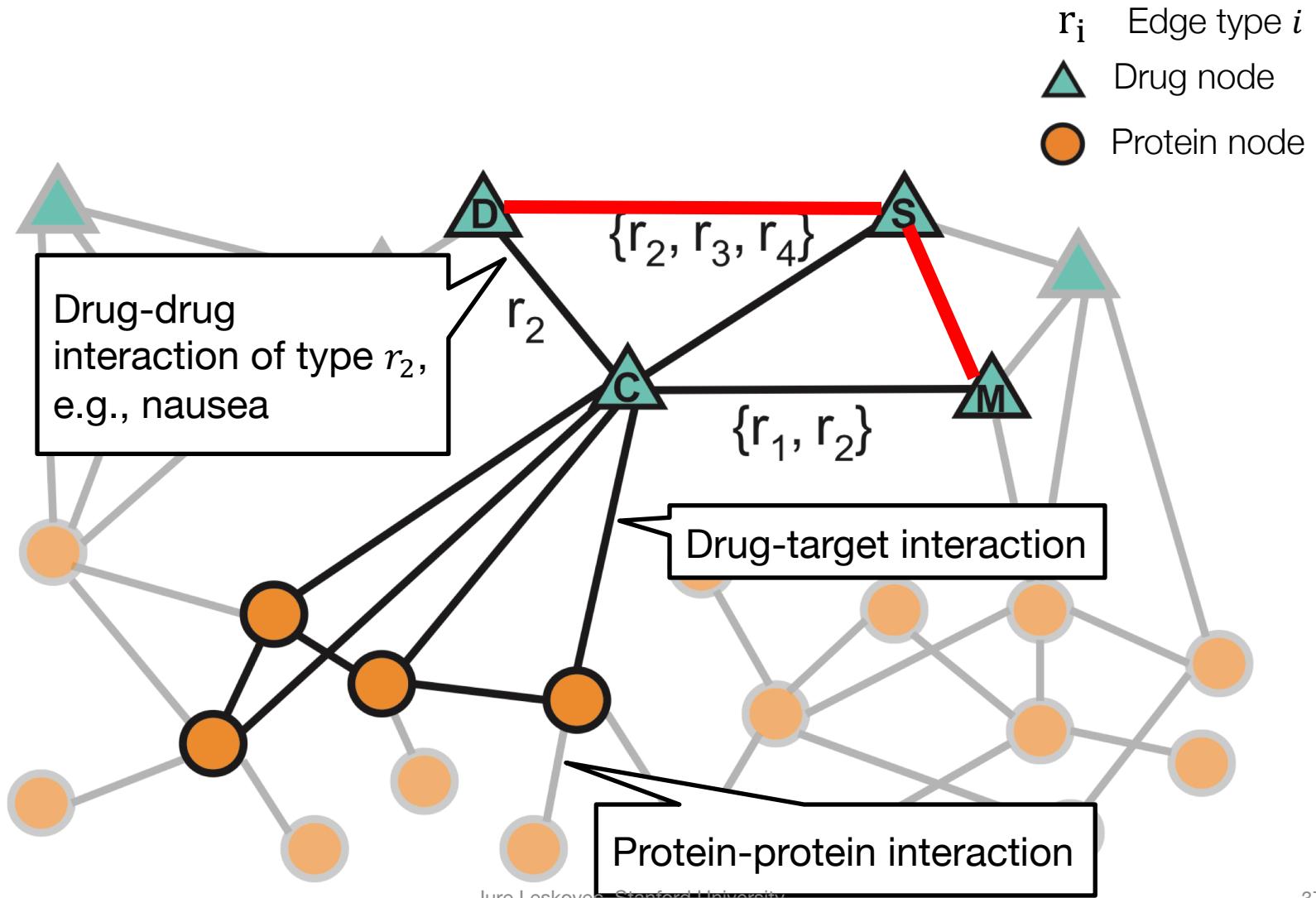
Many patients take multiple drugs to treat **complex** or co-existing diseases:

- 46% of people ages 70-79 take more than 5 drugs
- Many patients take more than 20 drugs to treat heart disease, depression, insomnia, etc.

Task: Given a pair of drugs predict adverse side effects



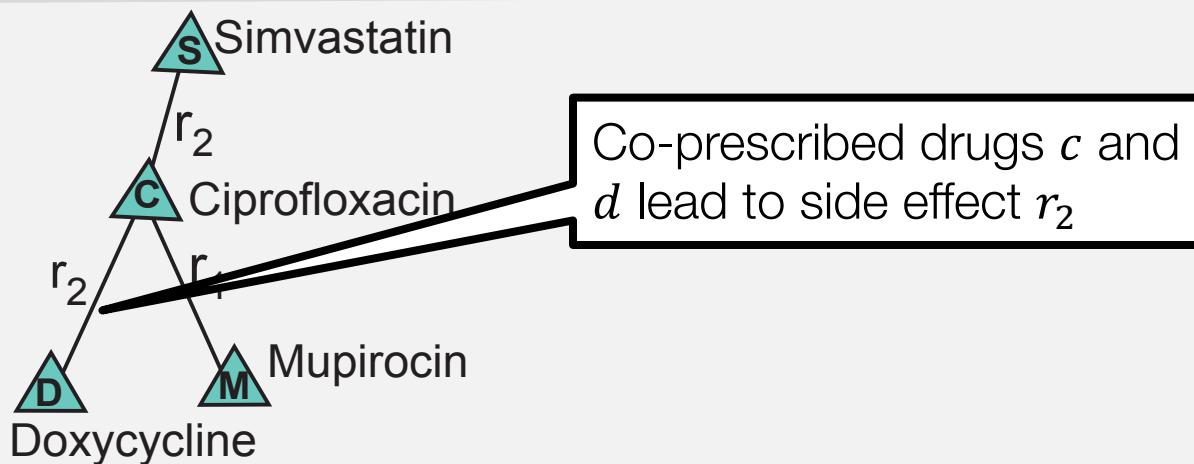
Approach: Build a Graph



Task: Link Prediction

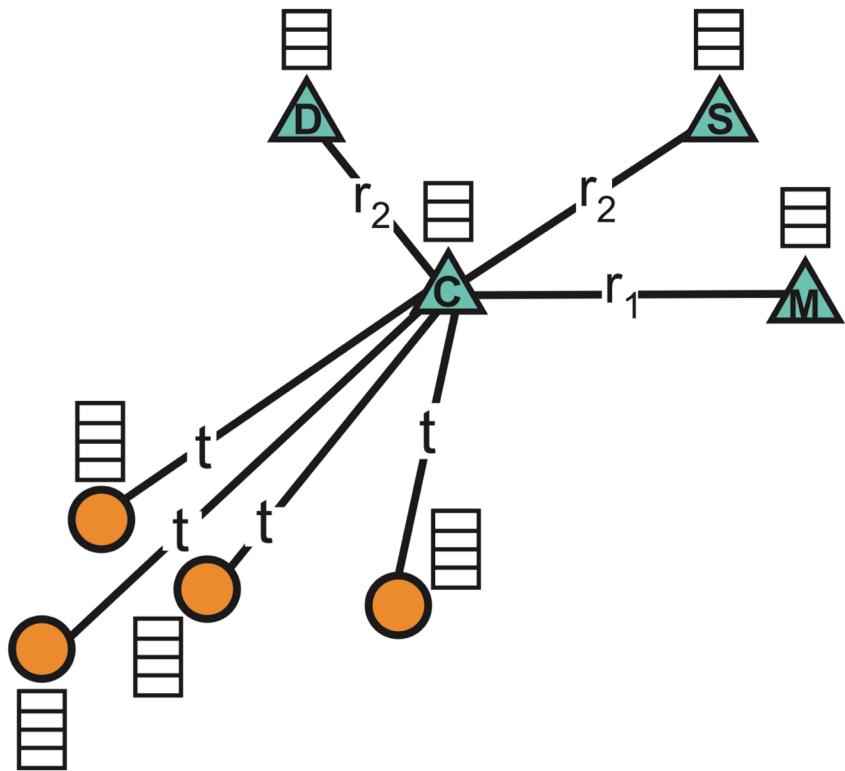
Task: Given a partially observed graph, predict labeled edges between drug nodes

Example query: Given drugs c, d , how likely is an edge (c, r_2, d) ?

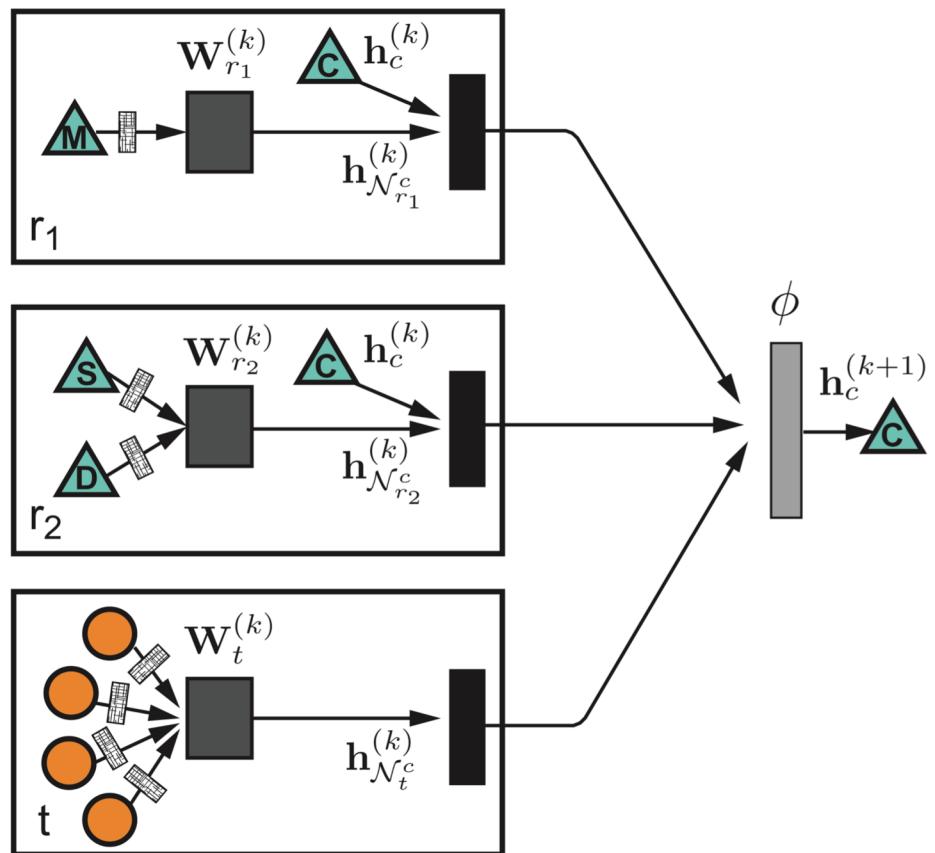


Decagon: Graph Neural Net

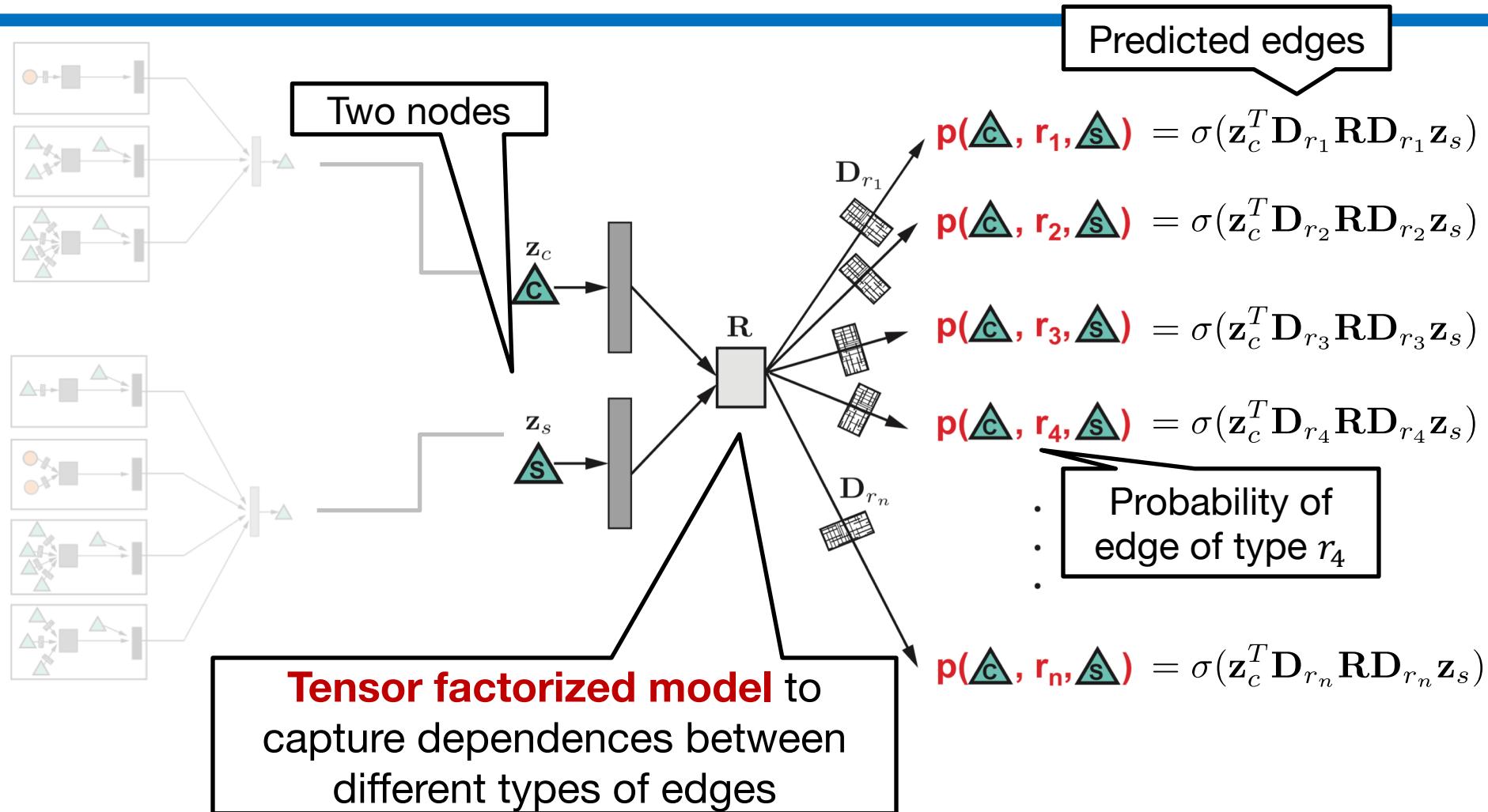
Network neighborhood of node C



Node C 's computation graph

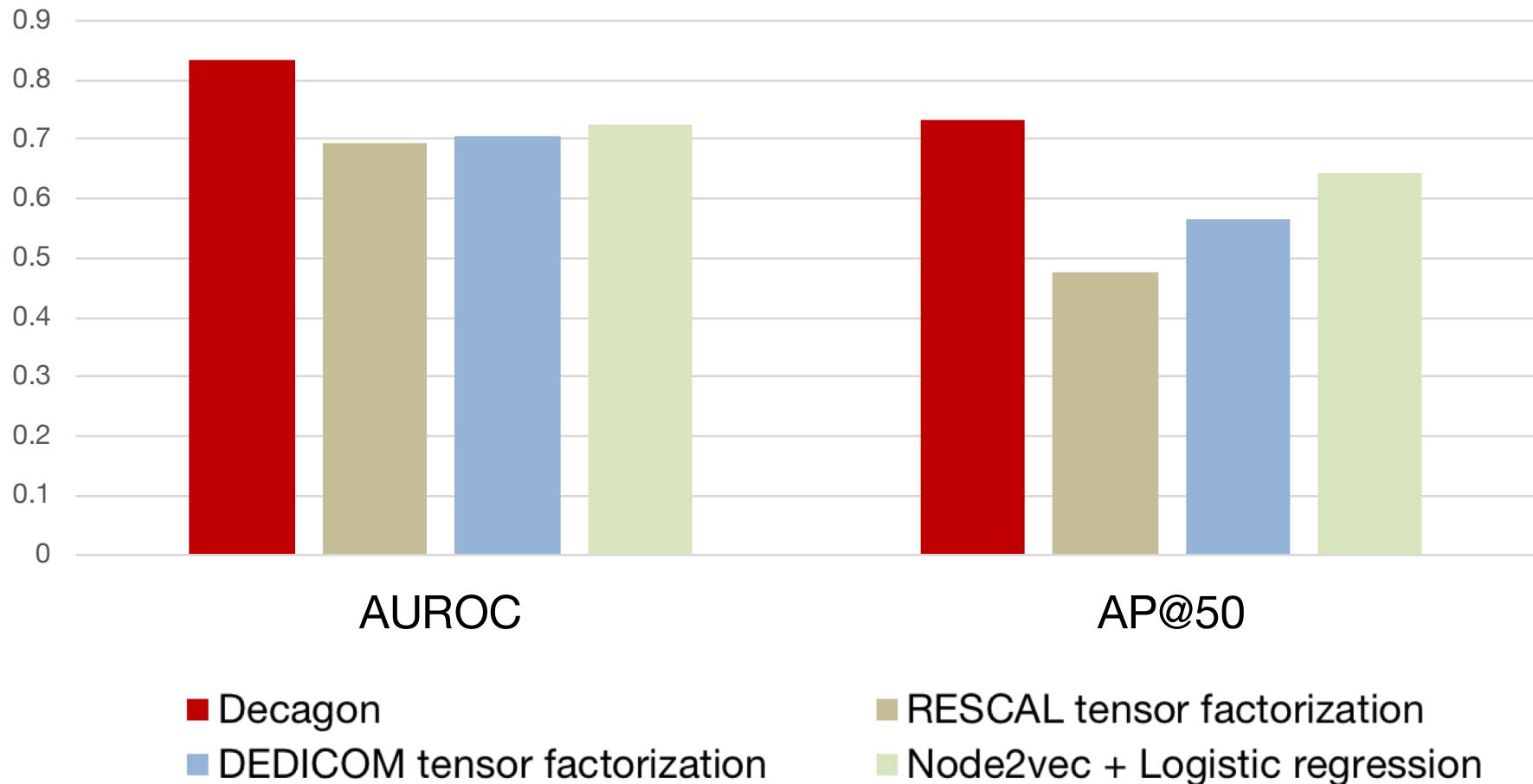


Decoder: Link Prediction



$\mathbf{R}, \mathbf{D}_{r_i}$ Parameter weight matrices

Results: Side Effect Prediction



36% average in AP@50 improvement over baselines

De novo Predictions

Rank	Drug c	Drug d	Side effect r
1	Pyrimethamine	Aliskiren	Sarcoma
2	Tigecycline	Bimatoprost	Autonomic neuropathy
3	Omeprazole	Dacarbazine	Telangiectases
4	Tolcapone	Pyrimethamine	Breast disorder
5	Minoxidil	Paricalcitol	Cluster headache
6	Omeprazole	Amoxicillin	Renal tubular acidosis
7	Anagrelide	Azelaic acid	Cerebral thrombosis
8	Atorvastatin	Amlodipine	Muscle inflammation
9	Aliskiren	Tioconazole	Breast inflammation
10	Estradiol	Nadolol	Endometriosis

De novo Predictions

Rank	Drug <i>c</i>	Drug <i>d</i>	Side effect <i>r</i>	Evidence found
1	Pyrimethamine	Aliskiren	Sarcoma	Stage <i>et al.</i> 2015
2	Tigecycline	Bimatoprost	Autonomic neuropathy	
3	Omeprazole	Dacarbazine	Telangiectases	
4	Tolcapone	Pyrimethamine	Breast disorder	Bicker <i>et al.</i> 2017
5	Minoxidil	Paricalcitol	Cluster headache	
6	Omeprazole	Amoxicillin	Renal tubular acidosis	Russo <i>et al.</i> 2016
7	Anagrelide	Azelaic acid	Cerebral thrombosis	
8	Atorvastatin	Amlodipine	Muscle inflammation	Banakh <i>et al.</i> 2017
9	Aliskiren	Tioconazole	Breast inflammation	Parving <i>et al.</i> 2012
10	Estradiol	Nadolol	Endometriosis	

Case Report

**Severe Rhabdomyolysis due to Presumed Drug Interactions
between Atorvastatin with Amlodipine and Ticagrelor**

Predictions in the Clinic

Clinical validation via drug-drug interaction markers, lab values, and

Medication List											Simple List	Timeline	Back to the Book	Feedback	Task List
Medication	Brand	Dose	Frequency	Quantity	Refills	Condition	Provider	Prescribed	2011	2012	2013	2014	Renew by		
beclomethasone HFA	QVAR HFA	2 puffs	bid	12	Asthma	Barnes	19 Feb 2011						19 Sep 2013		
chlorothalidone		25 mg	1 daily	90	3	Hypertension	Barnes	19 Sep 2006					19 Sep 2013		
insulin glargine	Lantus	28 u	daily	90	11	Diabetes	Ballard	19 Nov 2012					19 Sep 2013		
metformin		1000 mg	1 bid	180	3	Diabetes	Barnes	4 Mar 2008					19 Sep 2013		
naproxen	Aleve	500 mg	1 bid	90	0	Rheumatoid arthritis	Barnes	4 Mar 2008					19 Sep 2013		
prednisone		20 mg	2 d x5d prn	84	0	Asthma	Barnes	12 Sep 2010					19 Sep 2013		
zolpidem		5 mg	1 hs	90	0	Insomnia	Barnes	15 Mar 2012					22 Sep 2013		
simvastatin		40 mg	1 daily	84	0	High cholesterol	Belden	19 Mar 2010					30 Sep 2013		
terbinafine		250 mg	1 daily	84	0	Onychomycosis	Foote	30 Jul 2013					19 Oct 2013		



NEWTON-WELLESLEY
HOSPITAL



MASSACHUSETTS
GENERAL HOSPITAL



Stanford
MEDICINE



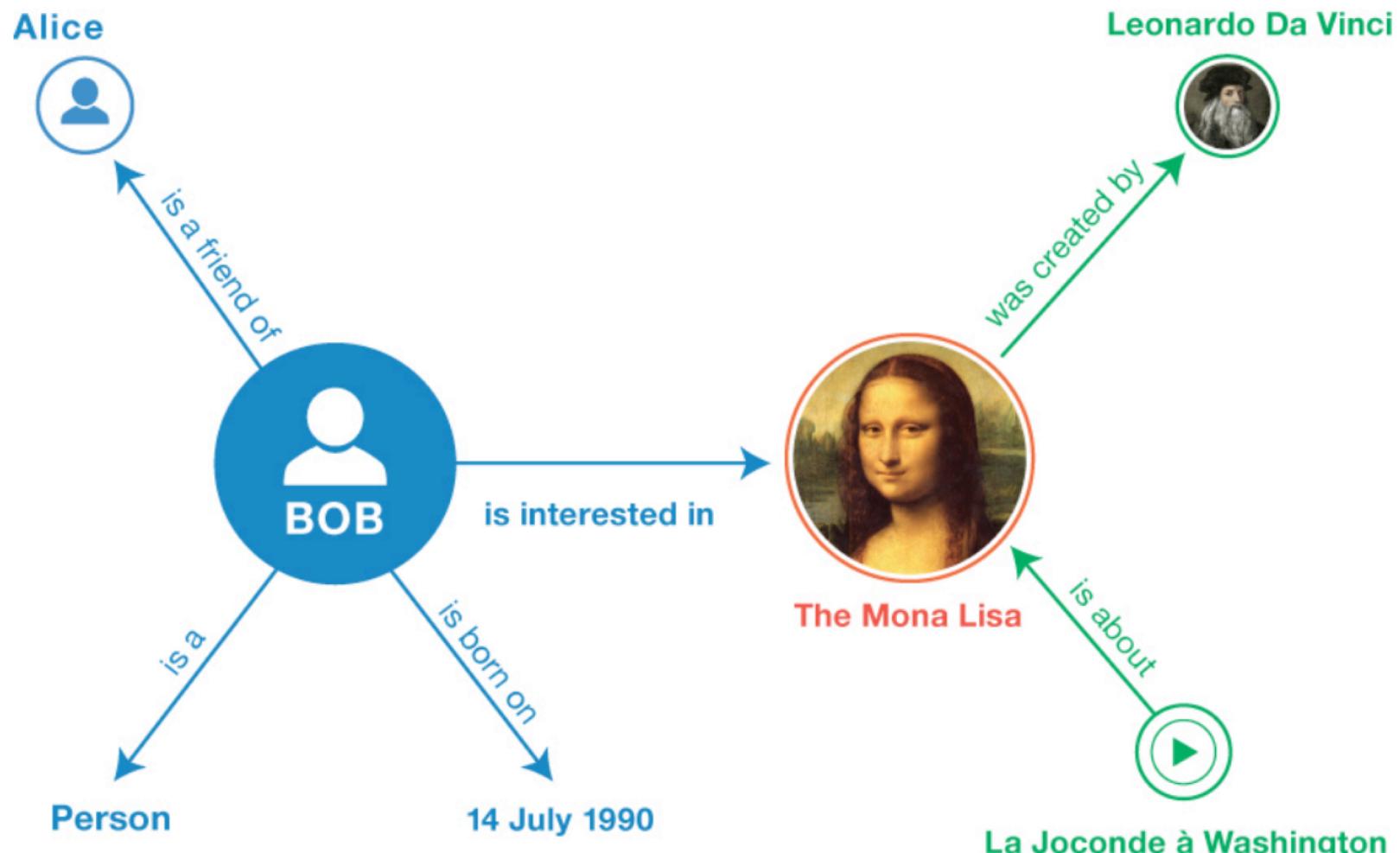
HARVARD
MEDICAL SCHOOL

First method to predict side effects of drug pairs, even for drug combinations not yet used in patients

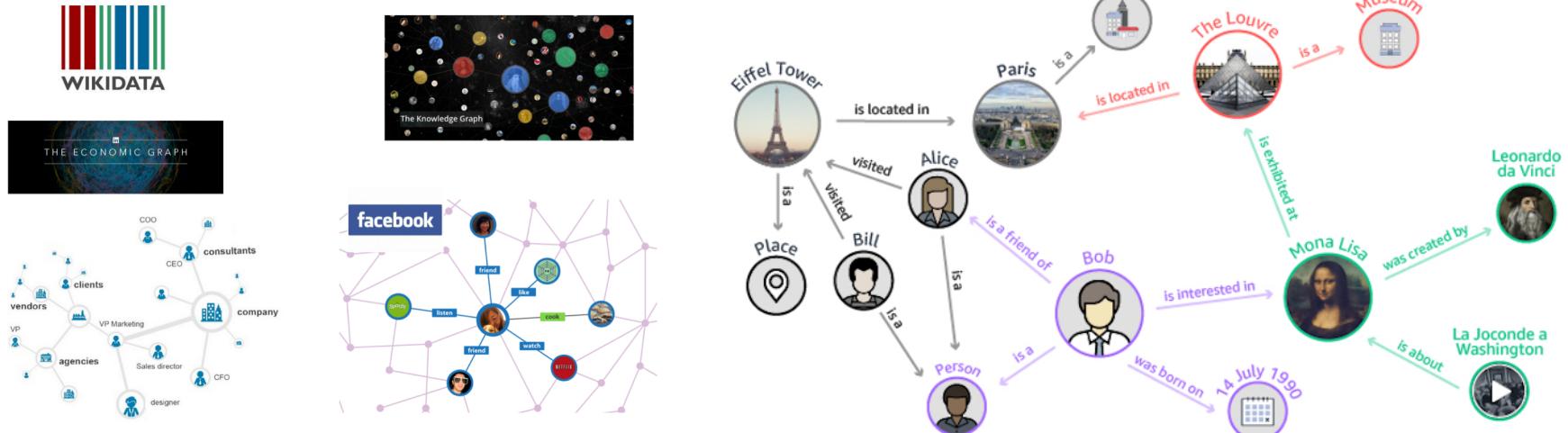
Reasoning in Knowledge Graphs

[Embedding Logical Queries on Knowledge Graphs](#). W. Hamilton, P. Bajaj, M. Zitnik, D. Jurafsky, J. Leskovec. *Neural Information Processing Systems (NeurIPS)*, 2018.

Knowledge as a Graph



Knowledge Graphs (KGs)



- Knowledge Graphs are **heterogenous** graphs
 - Multiple types of entities and relations exist
- Facts are represented as triples (h, r, t)
 - ('Alice', 'friend_with', 'Bob')
 - ('Paris', 'is_a', 'City')

Traditional Tasks

Knowledge Graph Competition/Link Prediction

- Predict the missing head or tail for a given triple (h, r, t)
- Example:

Barack Obama BornIn United States



Barack Obama Nationality American

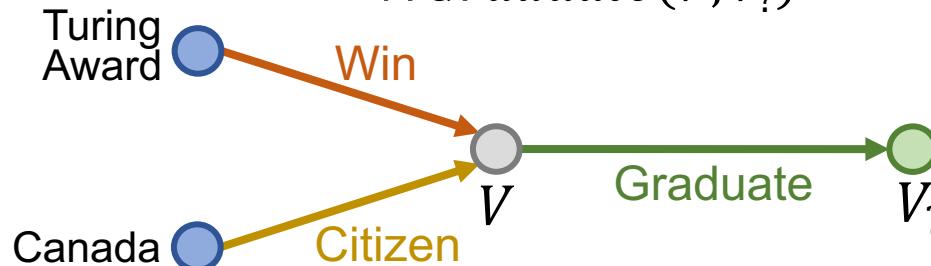
Our work: Beyond Link Prediction

Our goal: Reason over the knowledge graph using complex multi-hop queries

- Conjunctive queries: Subset of first-order logic with existential quantifier (\exists) and conjunction (\wedge)

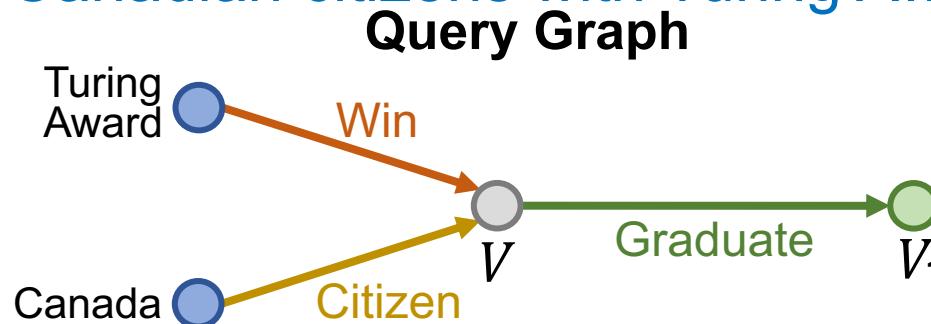
“Where did all Canadian citizens with Turing Award graduate?”

$$q = V_? . \exists V : Win(TuringAward, V) \wedge Citizen(Canada, V) \\ \wedge Graduate(V, V_?)$$

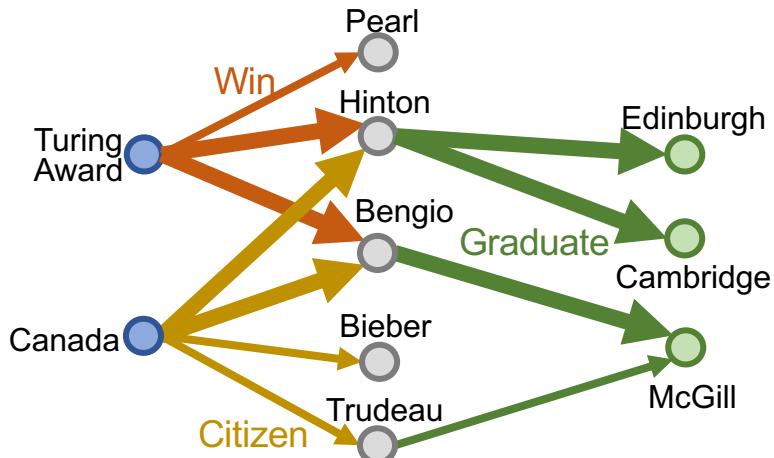


Answering Queries in KGs

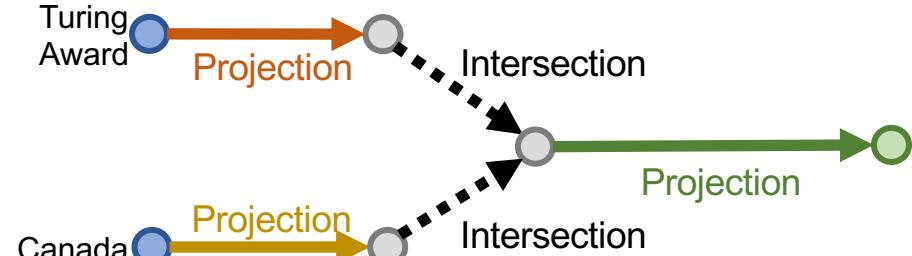
“Where did Canadian citizens with Turing Award graduate?”



Knowledge Graph



Computation Graph

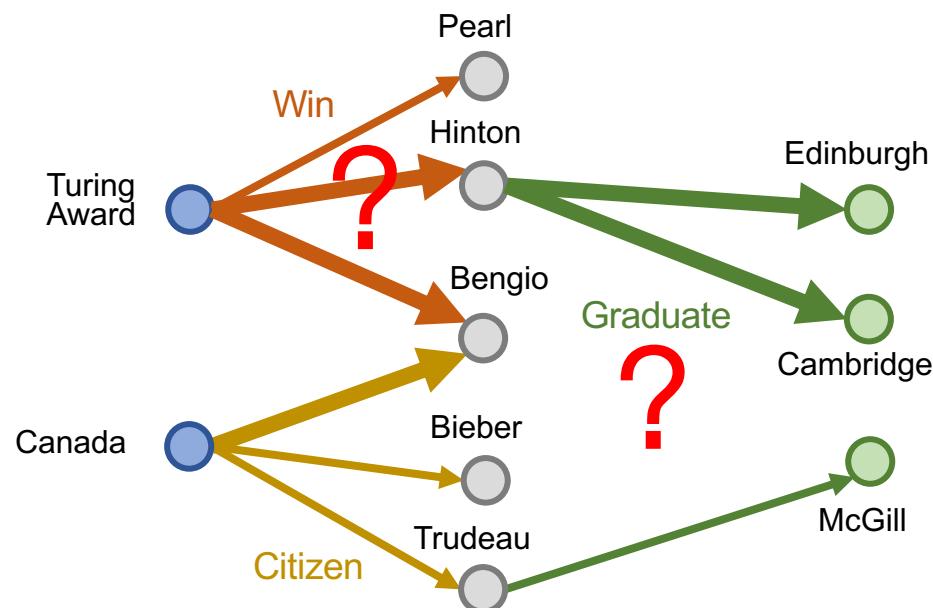


Each point corresponds to a set of entities

Why is it Hard?

Key challenge: Big graphs and queries can involve **noisy** and **unobserved** data!

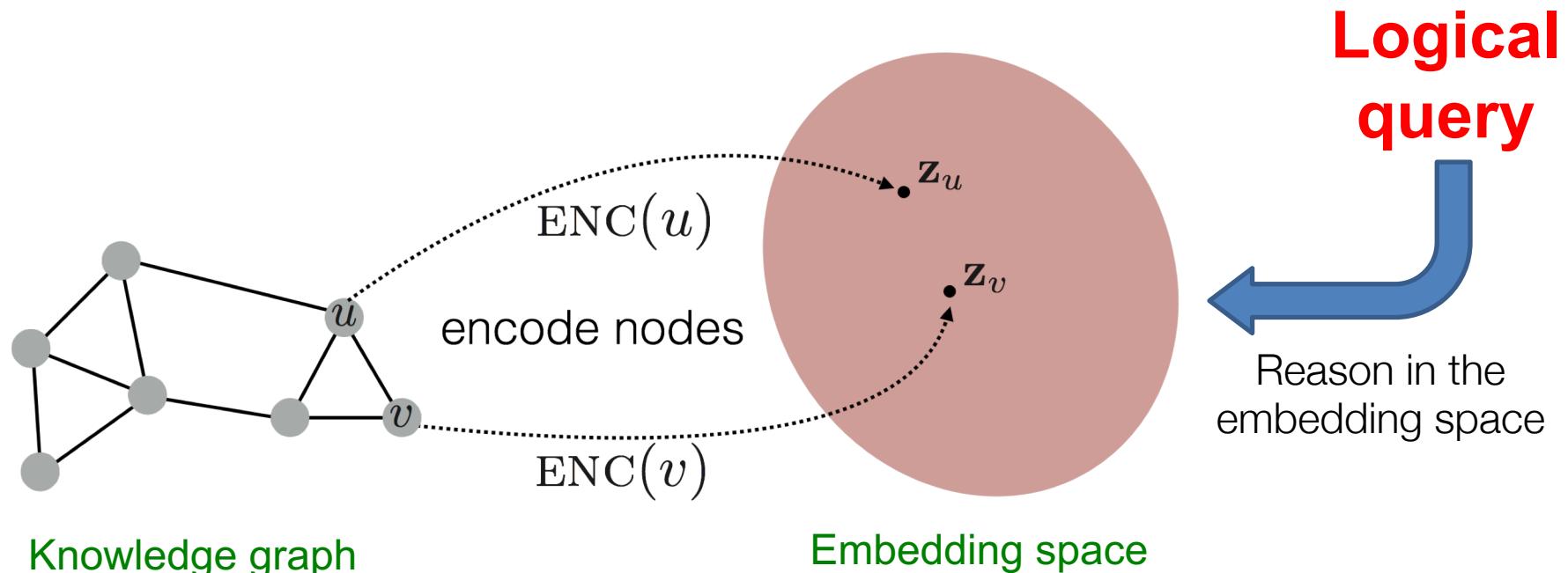
Some links might be noisy or missing



Problem: Naïve link prediction and graph template matching are too expensive

Our Idea: Query Embedding

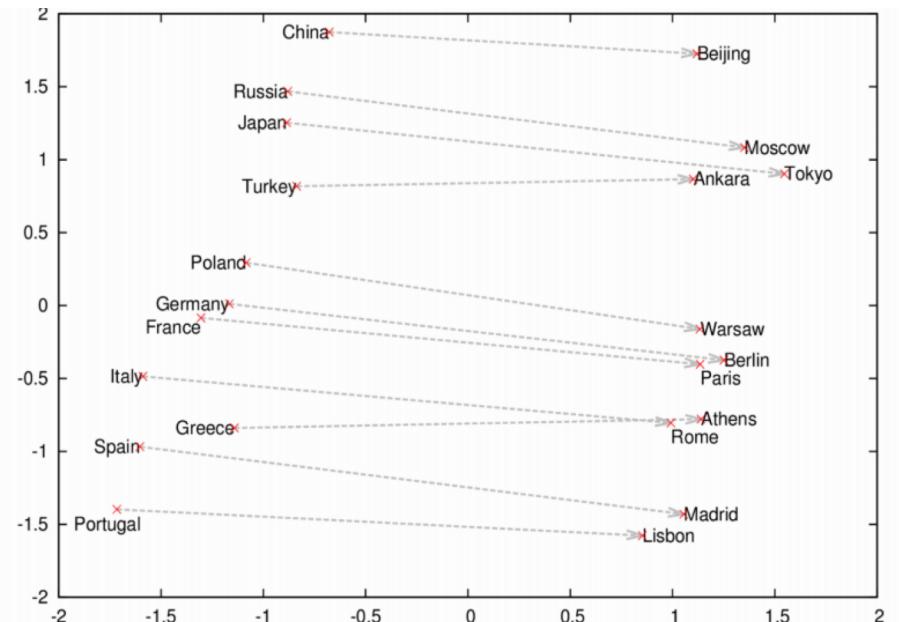
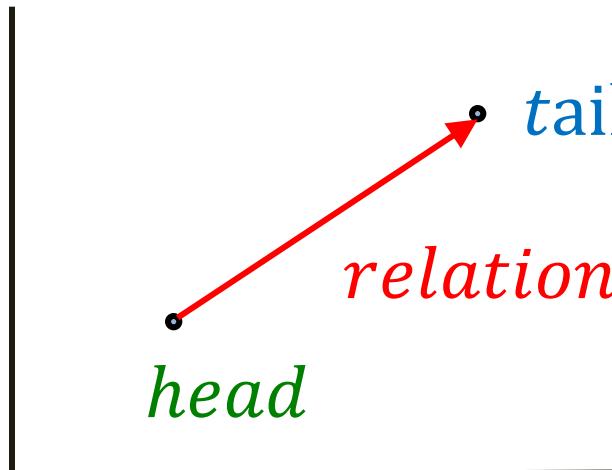
Use representation learning to map a graph into a Euclidean space and
learn to reason in that space



Semantic Embeddings

Remember Word2vec:

- TransE [Bordes et al., 2013]:
For a triple (h, r, t) : $\mathbf{h} + \mathbf{r} \approx \mathbf{t}$



Our Idea: **Query2Box**

Idea:

- **1)** Embed nodes of the graph
- **2)** For every logical operator learn a spatial operator

So that:

- **1)** Take an arbitrary logical query. Decompose it into a set of logical operators (\exists, \wedge, \vee)
- **2)** Apply a sequence of **spatial operators** to embed the query
- **3)** Answers to the query are entities close to the embedding of the query

Our Idea: **Query2Box**

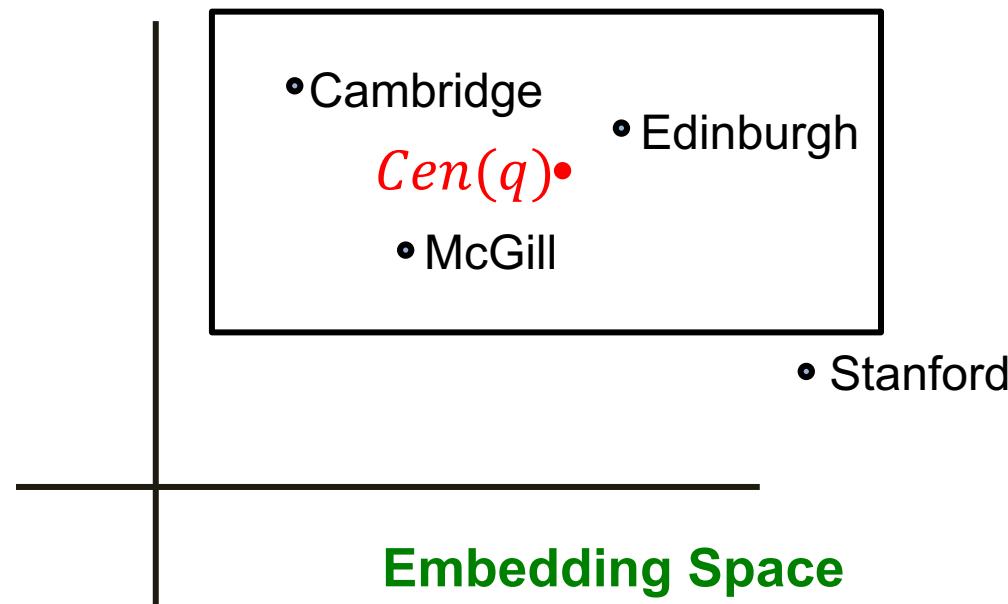
Idea:

- 1) Embed nodes of the graph
- 2) Represent query as a box.
- 3) Operations (union, intersection) are well defined over boxes.
- 4) Answers to the query are entities close to the embedding of the query

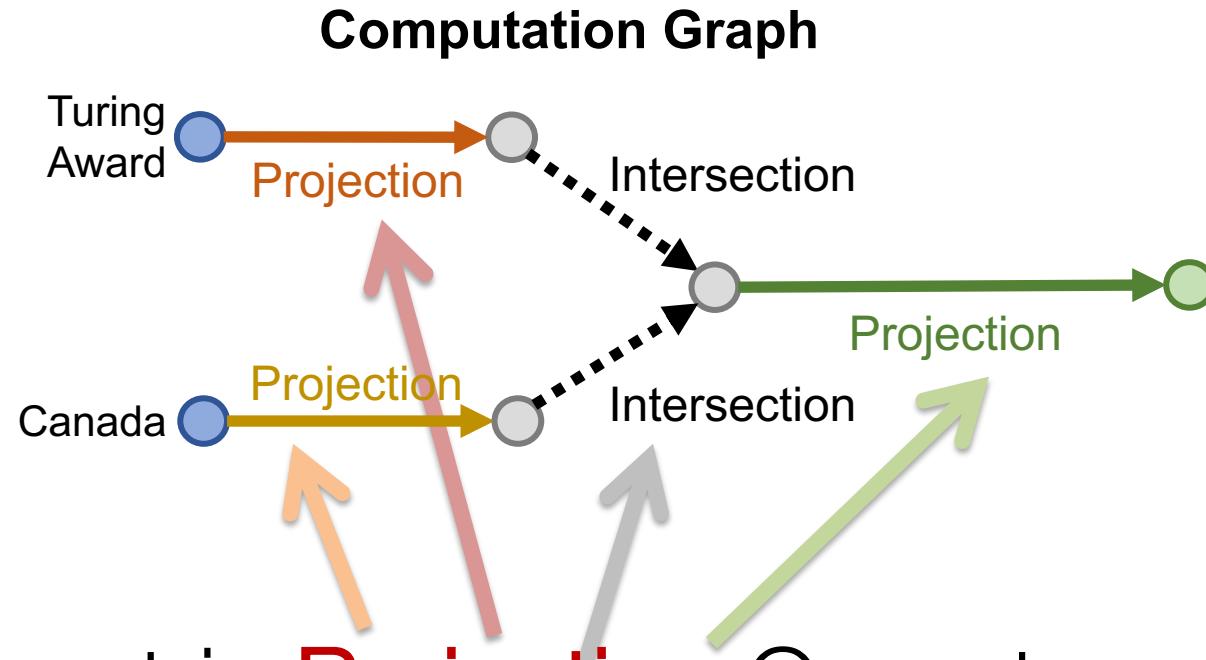
Embedding Queries

Query2Box embedding:

Embed queries with hyper-rectangles
(boxes): $\mathbf{q} = (Cen(q), Off(q))$.



Embedding Queries

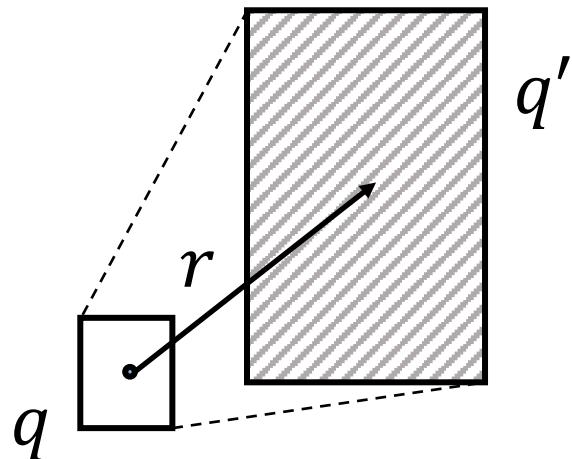


- Geometric **Projection** Operator
- Geometric **Intersection** Operator

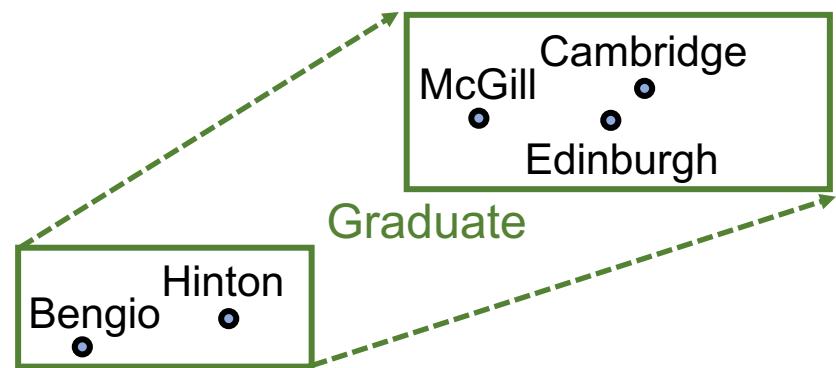
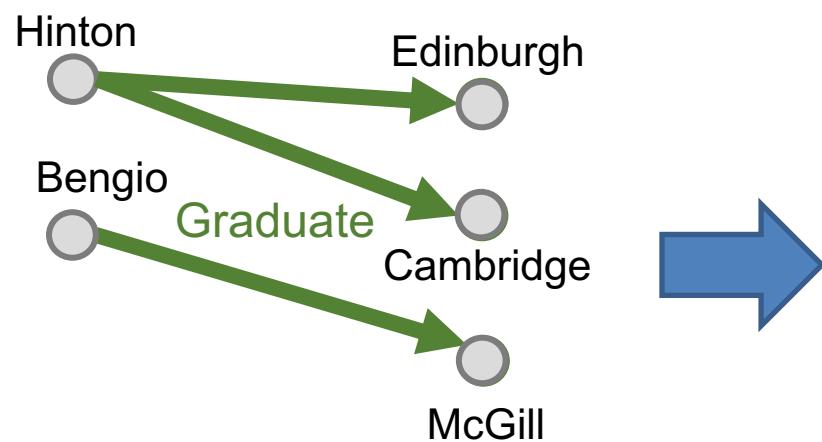
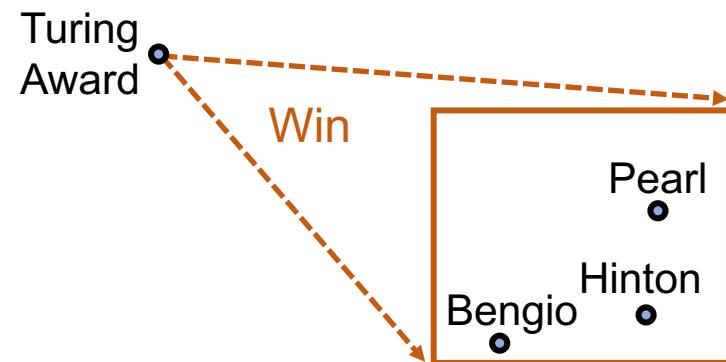
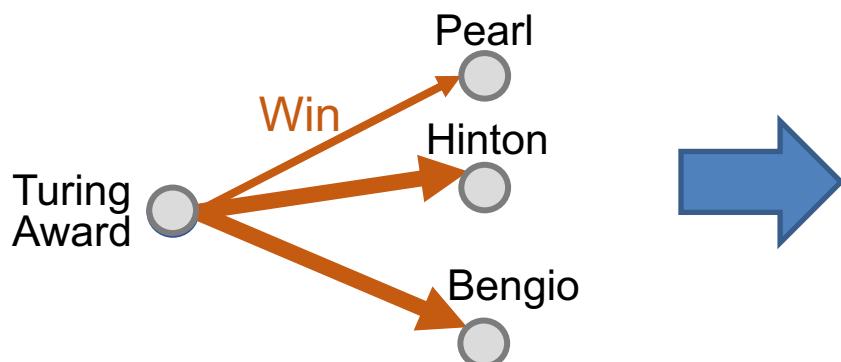
Projection Operator

Geometric Projection Operator \mathcal{P}

- $\mathcal{P} : \text{Box} \times \text{Relation} \rightarrow \text{Box}$



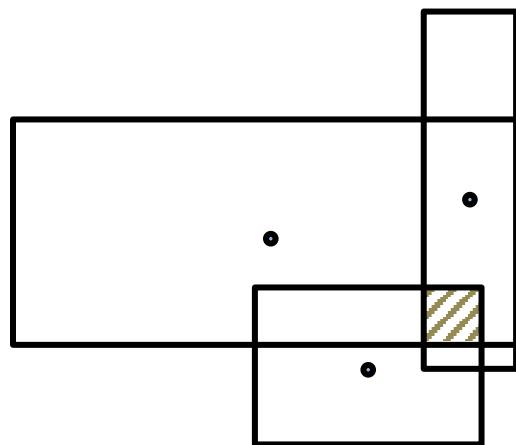
Projection Operator: Example



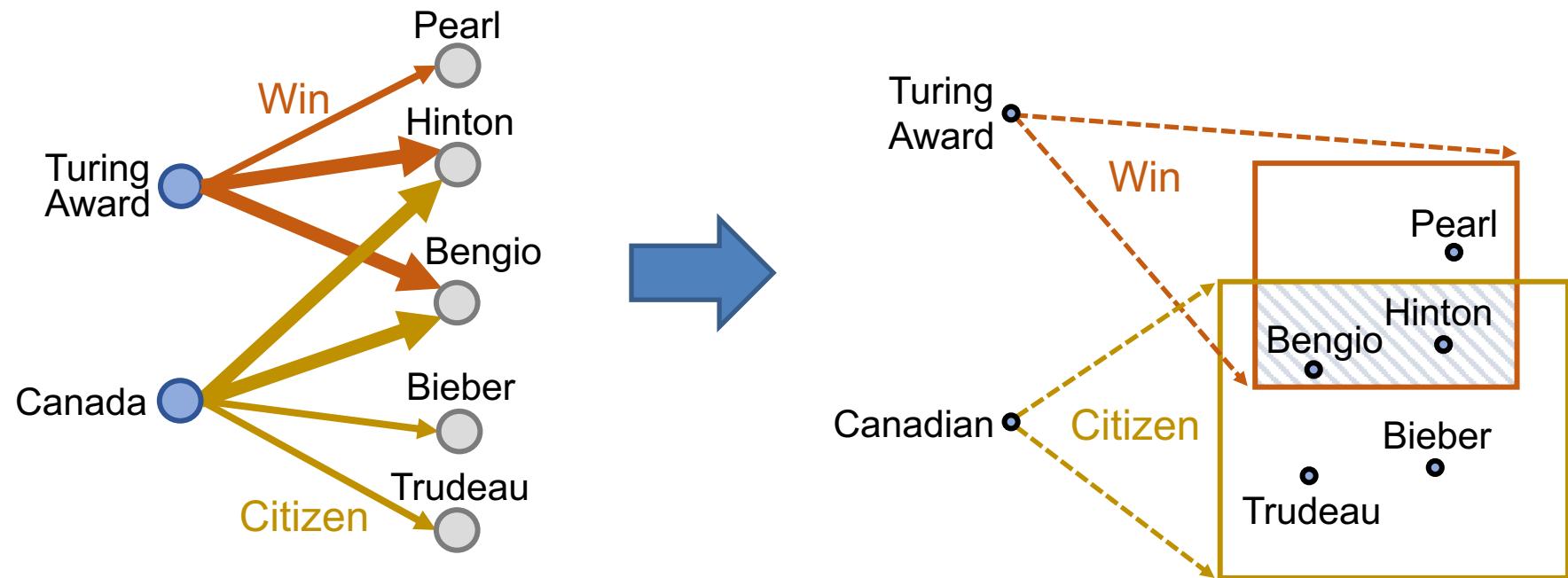
Intersection Operator

Geometric Intersection Operator \mathcal{J}

- $\mathcal{J} : \text{Box} \times \dots \times \text{Box} \rightarrow \text{Box}$
 - The new center is a weighted average
 - The new offset shrinks



Intersection Operator: Example



Benefits of Query2Box

Scalability and efficiency:

- Any query can be reduced to a couple of matrix operations and a single k-nearest neighbor search

Generality:

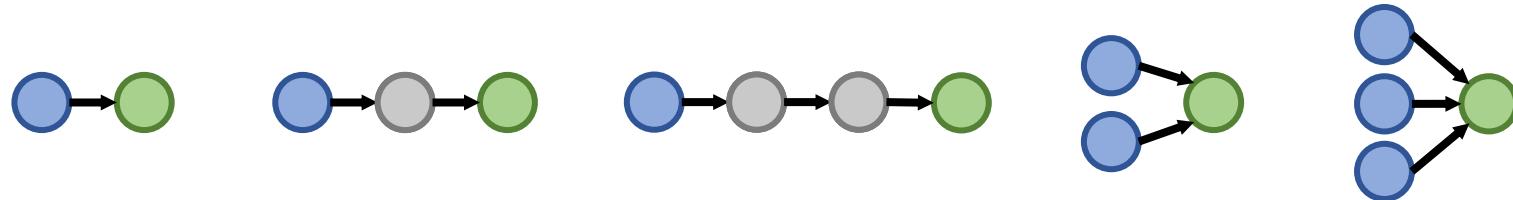
- We can answer any query (even those we have never seen before)

Robustness to noise:

- Graph can contain missing and noisy relationships

Query2Box : Model Training

Training examples: Queries on the graph



- **Positives:** Path with a known answer
- **Negatives:** Random nodes of the correct answer type
- **Goal:** Find embeddings and operators so that queries give correct answers

Experimental Setup

We essentially learn to “memorize” the answers to queries

- We embed entities so that our geometric operators give correct answers

Questions:

- Does our method generalize to new unseen queries?
- Does our method generalize to new query structures?
- Can method handle missing relations?

Experimental Setup

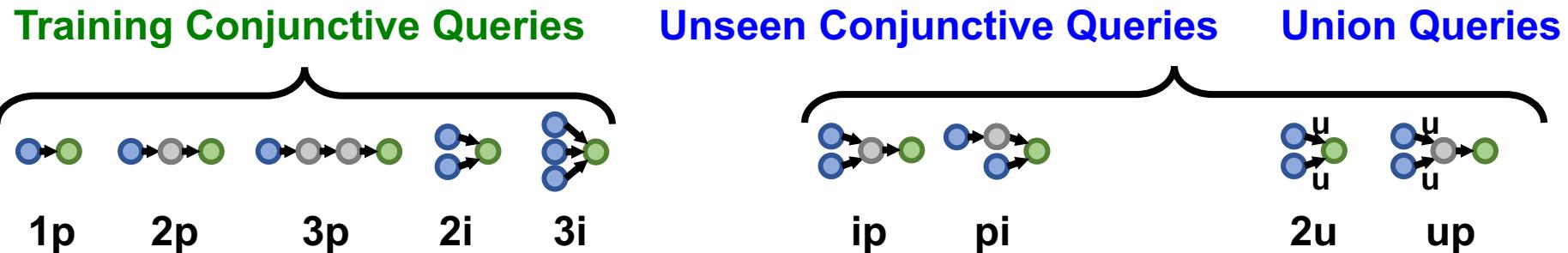
- **Training:**
 - Remove 10% of KG edges
 - Sample training queries and (non)answers
 - Train the model
- **Test set:**
 - Test queries/answers from the full graph
 - Ensure that the test queries are **not** directly answerable in the training graph
 - Every test query has at least one deleted edge
 - **Note:** Query template matching would have accuracy of random guessing

KG and Query Statistics

- Freebase: FB15K, FB15K-237

Dataset	Entities	Relations	Training Edges	Validation Edges	Test Edges	Total Edges
FB15k	14,951	1,345	483,142	50,000	59,071	592,213
FB15k-237	14,505	237	272,115	17,526	20,438	310,079

- Queries:



Queries	Training		Validation		Test	
	Dataset	1p	others	1p	others	1p
FB15k	273,710	273,710	59,097	8,000	67,016	8,000
FB15k-237	149,689	149,689	20,101	5,000	22,812	5,000

Experimental Results

Method	Avg	1p	2p	3p	2i	3i	ip	pi	2u	up
Q2B	0.268	0.467	0.24	0.186	0.324	0.453	0.108	0.205	0.239	0.193
GQE	0.228	0.402	0.213	0.155	0.292	0.406	0.083	0.170	0.169	0.163
GQE-DOUBLE	0.230	0.405	0.213	0.153	0.298	0.411	0.085	0.182	0.167	0.160

Table 3: H@3 on test set for QUERY2BOX vs. GQE on FB15k-237.

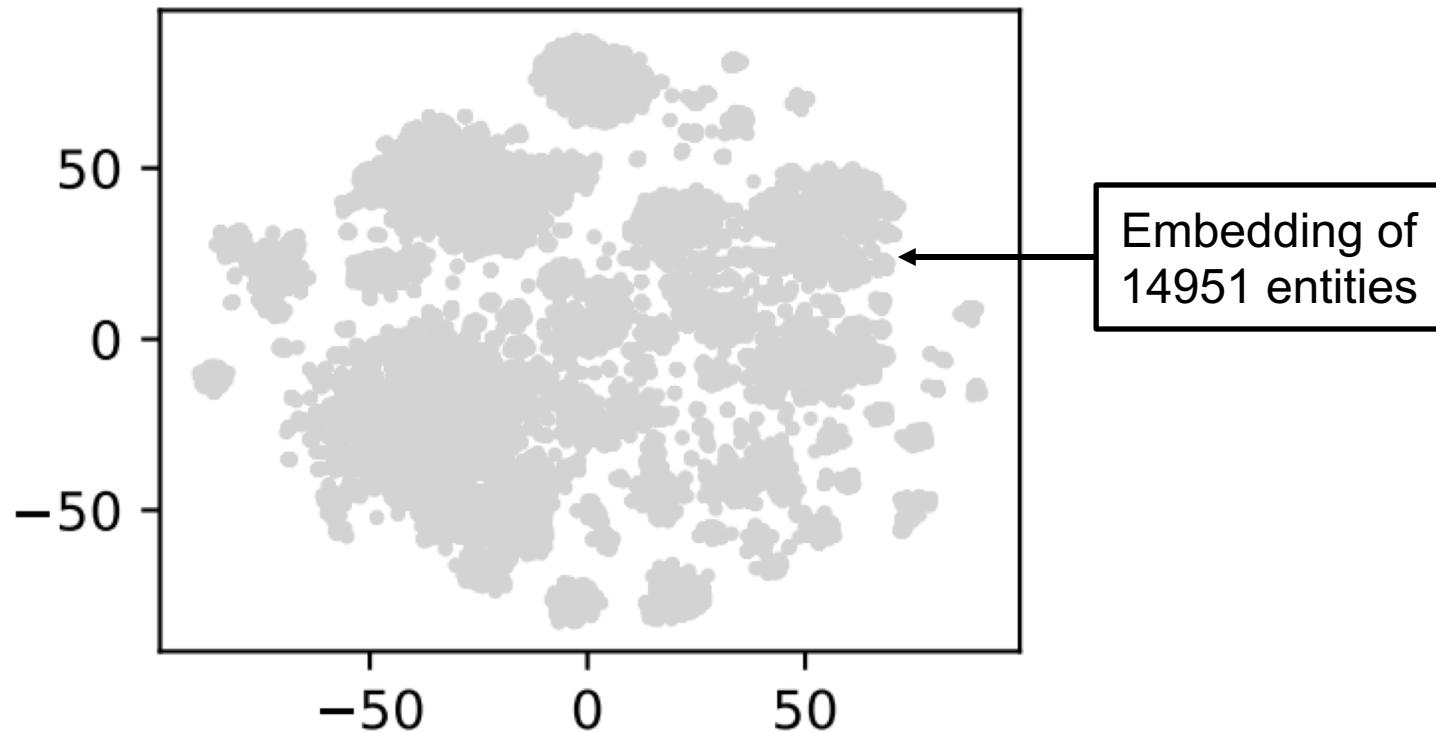
Method	Avg	1p	2p	3p	2i	3i	ip	pi	2u	up
Q2B	0.484	0.786	0.413	0.303	0.593	0.712	0.211	0.397	0.608	0.330
GQE	0.386	0.636	0.345	0.248	0.515	0.624	0.151	0.31	0.376	0.273
GQE-DOUBLE	0.384	0.63	0.346	0.250	0.515	0.611	0.153	0.32	0.362	0.271

Table 4: H@3 on test set for QUERY2BOX vs. GQE on FB15k.

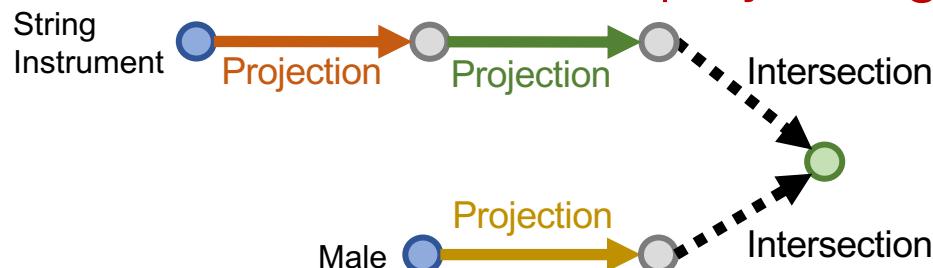
Observations:

- On “training” queries: +20% H@3
- On new conjunctive query structures: +15%
- On disjunctive queries: +36%

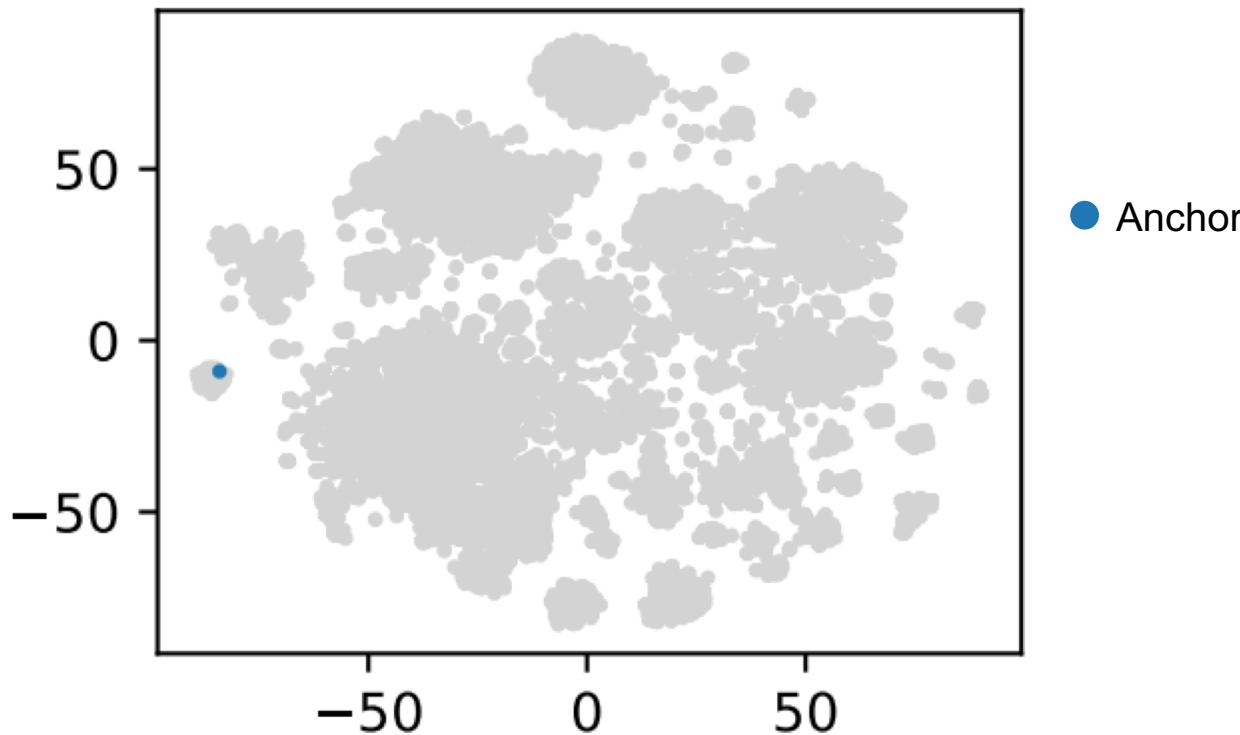
Embedding Space



“List male instrumentalists who play string instruments”



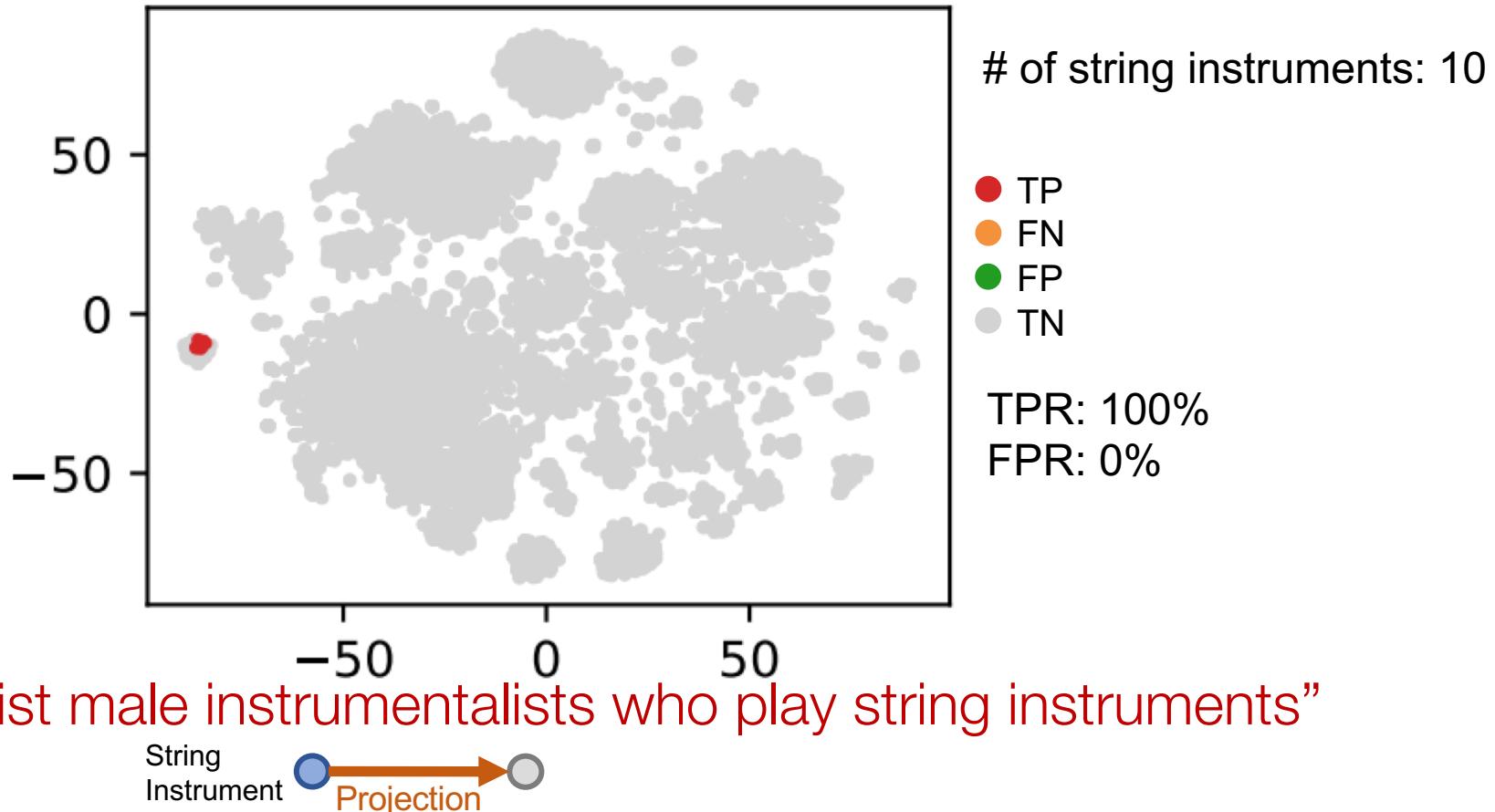
Embedding Space



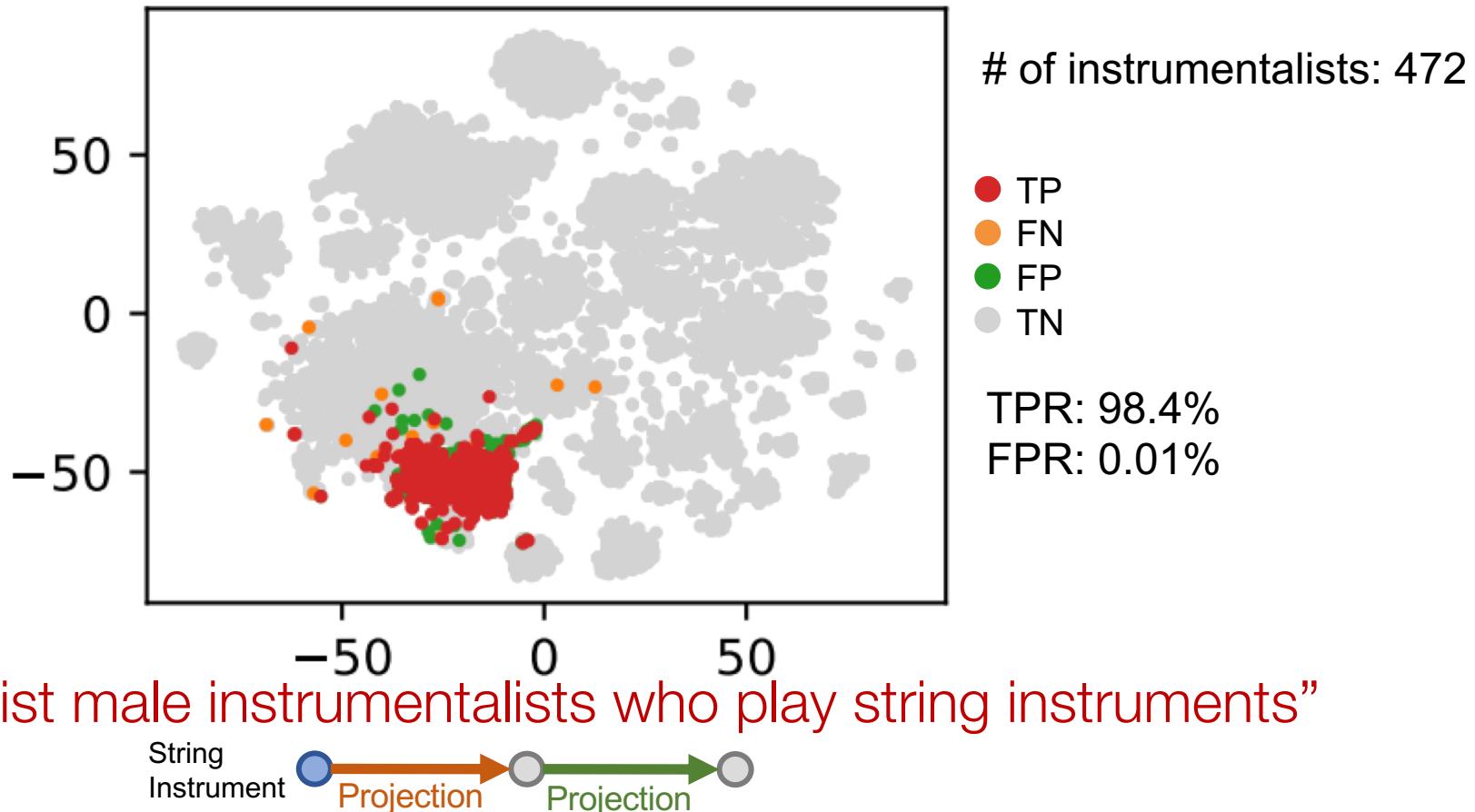
“List male instrumentalists who play string instruments”

String
Instrument

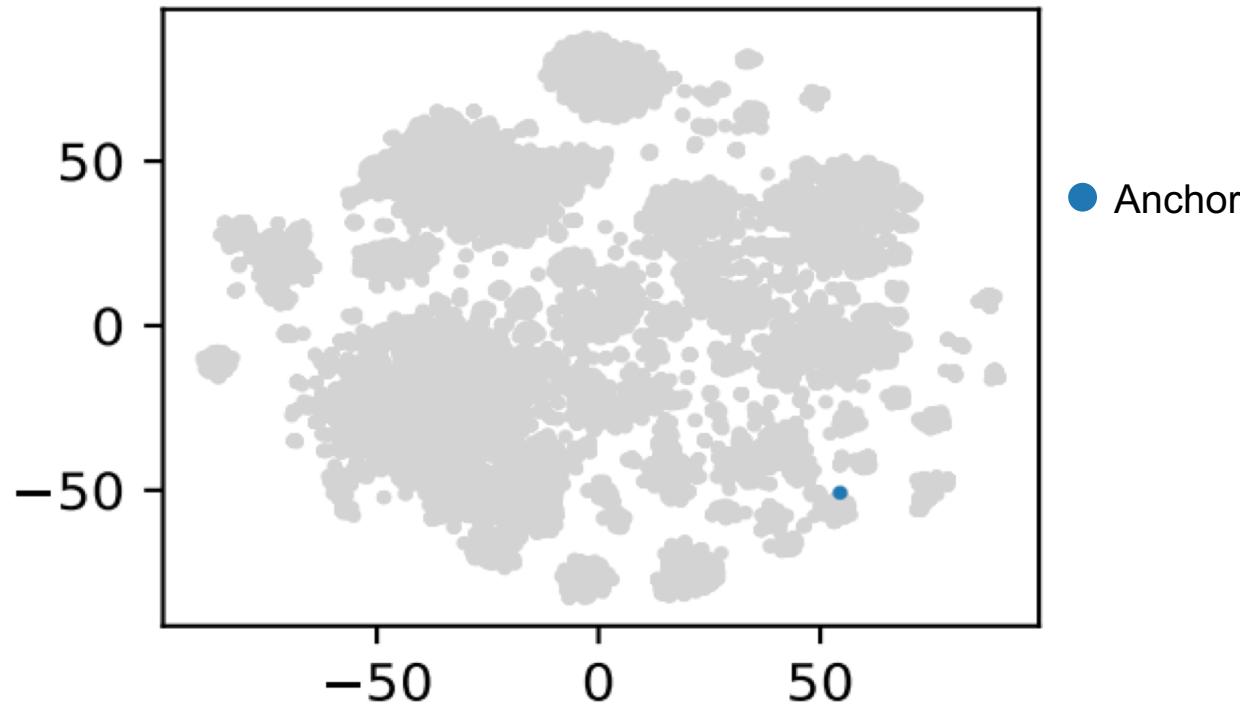
Embedding Space



Embedding Space



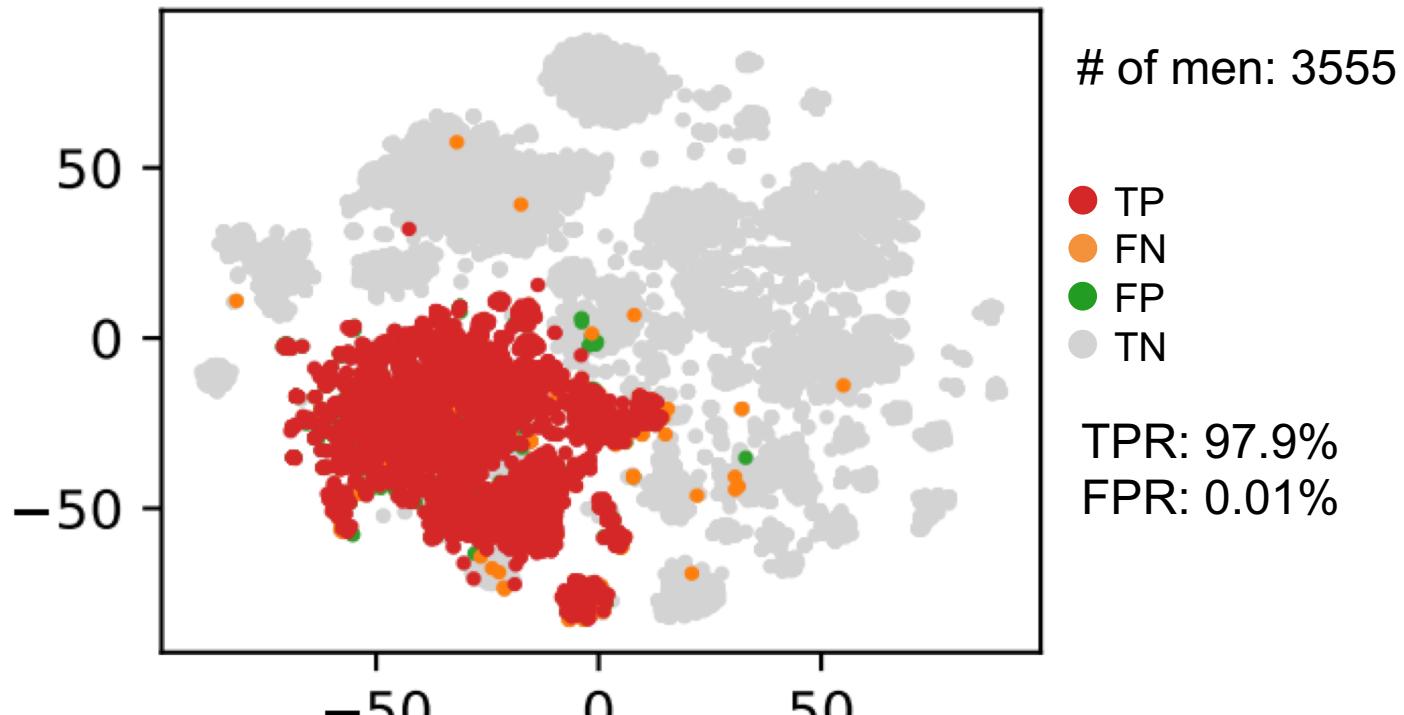
Embedding Space



“List male instrumentalists who play string instruments”

Male

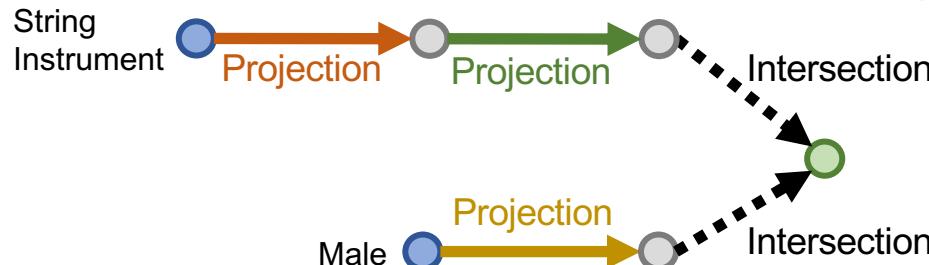
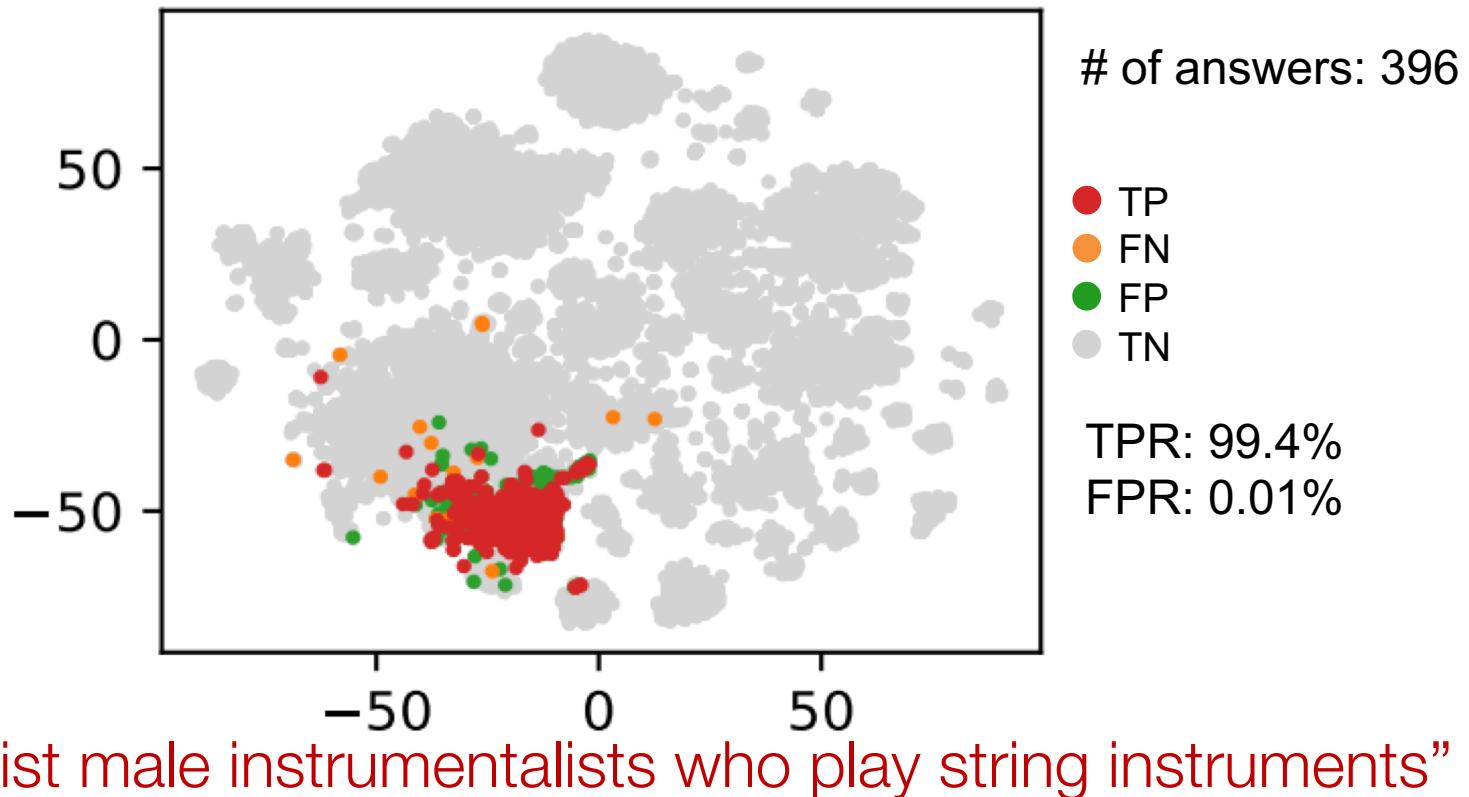
Embedding Space



“List male instrumentalists who play string instruments”



Embedding Space



Query2Box: Summary

- **Query2Box:**
 - Embed the query as a box
 - Logical operations become spatial operations
- **Composability of queries:**
 - Generalize well to unseen, extrapolated queries
 - Explicitly training for composability is important
- Instance vs. multi-hop generalization

How can this technology be used for other problems?

**We can now apply neural networks
much more broadly**

New frontiers beyond classic neural networks
that learn on images and sequences

Many other applications:

- **Nodes:** Predict tissue-specific protein functions
- **Subgraphs:** Predict which drug treats what disease
- **Graph generation:** Generate molecules/drugs

Summary

- Graph Convolutional Neural Networks
 - Generalize beyond simple convolutions
- Fuses node features & graph info
 - State-of-the-art accuracy for node classification and link prediction
- Model size independent of graph size; can scale to billions of nodes
 - Largest embedding to date (3B nodes, 20B edges)
- Leads to significant performance gains

Conclusion

Results from the past 2-3 years have shown:

- Representation learning paradigm can be extended to graphs
- No feature engineering necessary
- Can effectively combine node attribute data with the network information
- State-of-the-art results in a number of domains/tasks
- Use end-to-end training instead of multi-stage approaches for better performance

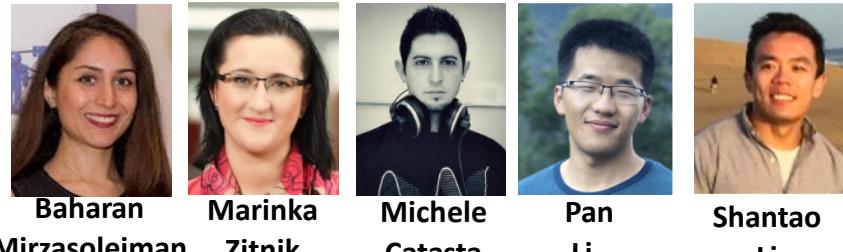
Industry Partnerships



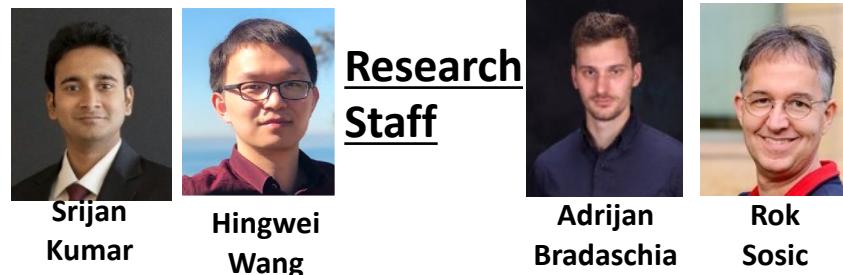
PhD Students



Post-Doctoral Fellows



Research Staff



azumio



Viaduct

Funding



Collaborators

Dan Jurafsky, Linguistics, Stanford University

David Grusky, Sociology, Stanford University

Stephen Boyd, Electrical Engineering, Stanford University

David Gleich, Computer Science, Purdue University

VS Subrahmanian, Computer Science, University of Maryland

Sarah Kunz, Medicine, Harvard University

Russ Altman, Medicine, Stanford University

Jochen Profit, Medicine, Stanford University

Eric Horvitz, Microsoft Research

Jon Kleinberg, Computer Science, Cornell University

Sendhill Mullainathan, Economics, Harvard University

Scott Delp, Bioengineering, Stanford University

James Zou, Medicine, Stanford University



WE'RE HIRING!

Postdoc positions in 3 topics:

- (1) Core ML on Graphs
- (2) Biomedical, Common Sense Reasoning
- (3) Societal Applications of ML

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 - <http://snap.stanford.edu/decagon/>
 - https://github.com/bowenliu16/r_graph_generation
 - <https://github.com/williamleif/graphgembird>
 - <https://github.com/snap-stanford/GraphRNN>