# Structural Analysis Toolbox Report

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#### 1 Overview

The investigated system has

- 15 constraints  $C = [c_1, c_2, c_3, c_4, c_5, c_6, d_7, d_8, d_9, d_10, d_11, d_12, m_13, m_14, m_15],$
- 4 known variables  $\mathcal{K} = [u, y_1, y_2, y_3]$  and
- 13 unknown variables  $\mathcal{X} = [\theta_1, \dot{\theta_1}, \omega_1, \dot{\omega_1}, \theta_2, \dot{\theta_2}, \omega_2, \dot{\omega_2}, \theta_3, \dot{\theta_3}, \omega_3, \dot{\omega_3}, d].$

The constraints of the system are as follows:

```
0 = dtheta_1 - w_1
c_1
        0 = d - u + J_1 dw_1 + b_1 w_1 + k_1 (\theta_1 - \theta_2)
c_2
        0 = dtheta_2 - w_2
c_3
        0 = J_2 dw_2 + b_2 w_2 - k_1 (\theta_1 - \theta_2) + k_2 (\theta_2 - \theta_3)
c_4
        0 = dtheta_3 - w_3
c_5
        0 = J_3 dw_3 + b_3 w_3 - k_2 (\theta_2 - \theta_3)
c_6
        0 = dtheta_1 - \theta_1'
d_7
        0 = dw_1 - w_1'
d_8
        0 = dtheta_2 - \theta_2'
        0 = dw_2 - w_2'
d_10
d_11
        0 = dtheta_3 - \theta_3'
        0 = dw_3 - w_3'
d_12
        0 = y_1 - \theta_1
m_13
m_14
        0 = y_2 - \theta_2
        0 = y_3 - \theta_3
m_15
```

The analysis obtained 1 matchings that yield in total 2 parity equations.

## 2 Canonical Decomposition

The system consists of

- the over-determined subsystem  $S^+$  with  $C^+ = [c_3, c_4, c_5, c_6, d_9, d_10, d_11, d_12, m_13, m_14, m_15]$  and  $\mathcal{X}^+ = [\theta_1, \theta_2, \dot{\theta_2}, \omega_2, \dot{\omega_2}, \theta_3, \dot{\theta_3}, \omega_3, \dot{\omega_3}],$
- the just-determined subsystem  $S^0$  with  $C^0 = [c_1, c_2, d_7, d_8]$  and  $\mathcal{X}^+ = [\dot{\theta_1}, \omega_1, \dot{\omega_1}, d]$  and
- the under-determined subsystem  $S^-$  with  $C^- = [\ ]$  and  $\mathcal{X}^+ = [\ ]$ .

#### 3 Incidence Matrix

Table 2 presents the incidence matrix of the investigated system.

		ŀ	C		$\mathcal{X}$												
#	n	$y_1$	$y_2$	$y_3$	$\theta_1$	$\dot{ heta_1}$	$\mathcal{E}_1$	$\dot{\beta}$	$\theta_2$	$\dot{\theta_2}$	$\mathcal{S}_2$	$\dot{\mathcal{S}}_2$	$\theta_3$	$\dot{\theta_3}$	$\mathcal{E}_3$	$\dot{\mathcal{S}}$	d
$c_1$	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0
$c_2$	1	0	0	0	1	0	1	1	1	0	0	0	0	0	0	0	1
$c_3$	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0
$c_4$	0	0	0	0	1	0	0	0	1	0	1	1	1	0	0	0	0
$c_5$	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0
$c_6$	0	0	0	0	0	0	0	0	1	0	0	0	1	0	1	1	0
$m_13$	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
$m_14$	0	0	1	0	0	0	0	0	1	0	0	0	0	0	0	0	0
$m_15$	0	0	0	1	0	0	0	0	0	0	0	0	1	0	0	0	0
$d_7$	0	0	0	0	X	1	0	0	0	0	0	0	0	0	0	0	0
$d_8$	0	0	0	0	0	0	X	1	0	0	0	0	0	0	0	0	0
$d_9$	0	0	0	0	0	0	0	0	X	1	0	0	0	0	0	0	0
$d_10$	0	0	0	0	0	0	0	0	0	0	X	1	0	0	0	0	0
$d_11$	0	0	0	0	0	0	0	0	0	0	0	0	X	1	0	0	0
$d_12$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	X	1	0

Table 2: Incidence matrix of the investigated system.

### 4 Matchings

Table 3 lists the obtained matchings. The fields either contain the matched unknown variables, zeros to indicate an unmatched constraints or nothing if constraints are not used in a matching.

	$c_1$	$c_2$										$d_12$	$m_13$	$m_14$	$m_15$
1	$\omega_1$	d	$\omega_2$	$\dot{\omega_2}$	$\omega_3$	$\dot{\omega_3}$	$\dot{ heta_1}$	$\dot{\omega_1}$	$\dot{ heta_2}$	0	$\dot{ heta_3}$	0	$\theta_1$	$\theta_2$	$\theta_3$

Table 3: Matchings of the investigated system.

## 5 Parity Equations

$$0 = -y_2'' - \frac{k_1 (y_2 - y_1) + k_2 (y_2 - y_3) + b_2 y_2'}{J_2}$$
$$0 = -y_3'' - \frac{k_2 (y_3 - y_2) + b_3 y_3'}{J_3}$$

### 6 Detectability and isolability analysis

Table 4 lists the detectability and isolability properties of the parity equations separately and over all combined. Detectable (d), isolable (i) and non-failable constraints (n) are marked accordingly.

	$c_1$	$c_2$	$c_3$	$c_4$	$c_5$	$c_6$	$d_7$	$d_8$	$d_9$	$d_10$	$d_11$	$d_12$	$m_13$	$m_14$	$m_15$
1			d	d	d	d	n	n	n	n	n	n	d	d	d
ALL			d	d	d	d	n	n	n	n	n	n	d	d	d

Table 4: Detectability and isolability of the investigated system.