

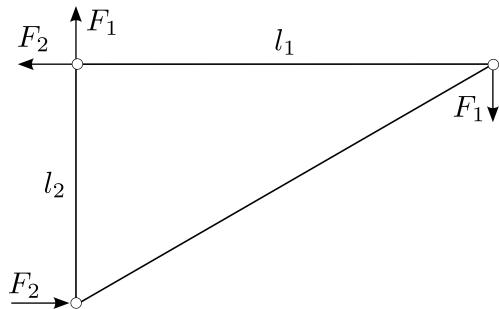
# Course of Aerospace Structures

Written test, September 2<sup>nd</sup>, 2019

## Exercise 1

A structure is made of three bars connected each other through hinge constraints. The bars are made of aluminum alloy with Young's modulus  $E$  and have area  $A$ . A set of loads is applied at the end of the bars, the concentrated loads being denoted as  $F_1$  and  $F_2$ , as shown in the figure.

By using a displacement-based approach, determine the internal stresses in the three bars.



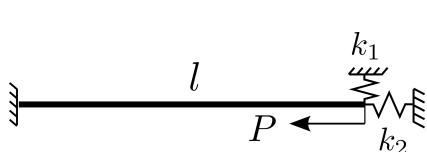
*Data*

$$\begin{aligned}l_1 &= 600 \text{ mm}; l_2 = 200 \text{ mm}; \\A &= 400 \text{ mm}^2; \\E &= 70 \text{ GPa}; \\F_1 &= 1.0 \times 10^4 \text{ N}; F_2 = 3.0 \times 10^4 \text{ N};\end{aligned}$$

## Exercise 2

Consider the elastically restrained column in the figure. Specifically, the column has length  $l$  and a square section of dimension  $a$ . The material is an aluminum alloy characterized by Young's moduli  $E$ . One end is fixed and the second one is grounded by means of two linear springs of stiffness  $k_1$  and  $k_2$ . A compressive load  $P$  is applied at one end.

Estimate the buckling load of the structure by resorting to a displacement-based approach along with an appropriate approximate solution strategy.



*Data*

$$\begin{aligned}l &= 1200 \text{ mm}; \\a &= 20 \text{ mm}; \\E &= 70 \text{ GPa}; \\k_1 &= 1 \text{ N/mm}; k_2 = 10 \text{ kN/mm};\end{aligned}$$

## Question 1

Illustrate how to estimate the torsional and transverse shear stiffnesses for a thin-walled beam in the context of the semi-monocoque approximation.