

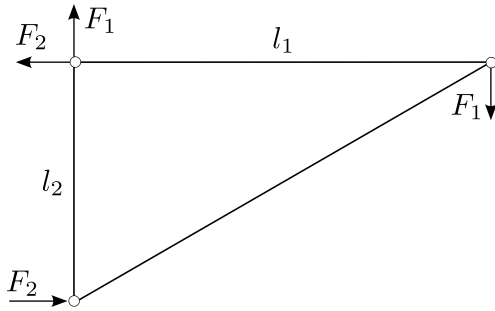
# Course of Aerospace Structures

Written test, September 2<sup>nd</sup>, 2019

## Exercise 1

A structure is made of three bars connected each other through hinge constraints. The bars are made of aluminum alloy with Young's modulus  $E$  and have area  $A$ . A set of loads is applied at the end of the bars, the concentrated loads being denoted as  $F_1$  and  $F_2$ , as shown in the figure.

By using a displacement-based approach, determine the internal stresses in the three bars.



*Data*

$$l_1 = 600 \text{ mm}; l_2 = 200 \text{ mm};$$

$$A = 400 \text{ mm}^2;$$

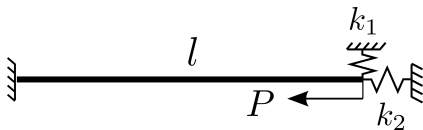
$$E = 70 \text{ GPa};$$

$$F_1 = 1.0 \times 10^4 \text{ N}; F_2 = 3.0 \times 10^4 \text{ N};$$

## Exercise 2

Consider the elastically restrained column in the figure. Specifically, the column has length  $l$  and a square section of dimension  $a$ . The material is an aluminum alloy characterized by Young's modulus  $E$ . One end is fixed and the second one is grounded by means of two linear springs of stiffness  $k_1$  and  $k_2$ . A compressive load  $P$  is applied at one end.

Estimate the buckling load of the structure by resorting to a displacement-based approach along with an appropriate approximate solution strategy.



*Data*

$$l = 1200 \text{ mm};$$

$$a = 20 \text{ mm};$$

$$E = 70 \text{ GPa};$$

$$k_1 = 1 \text{ N/mm}; k_2 = 10 \text{ kN/mm};$$

## Question 1

Illustrate how to estimate the torsional and transverse shear stiffnesses for a thin-walled beam in the context of the semi-monocoque approximation.