

## ML Interpretation

TOTAL POINTS: 8

1. You train the random forest pictured below and it gets a c-index of 0.90. After shuffling the values for x, your dataset is the following. What is the variable importance for x?

3/3 point

ID	x	y	death
1	2	3	1
2	4	5	0
3	1	2	1
4	5	2	0



- ☐ -0.05
- ☐ 0.1
- ☐ 0.5
- ☒ 0.85

✓ Correct

Explanation: We need to calculate the new C-index. The prediction for 1 is low risk, the prediction for 2 is low risk, the prediction for 3 is low risk, and the prediction for 4 is high risk. The permissible pairs are (1, 2), (1, 4), (3, 2), (3, 4). All of these are risk ties except for (3, 4) and (1, 4), which are not concordant. Therefore the c-index is  $0.5(2)/4 = 0.25$ . Therefore the difference between the original C-index and the new one is  $0.9 - 0.25 = 0.65$ , so the answer is D.

2. Say you have trained a decision tree which never splits on a variable X. What will be the variable importance for X using the permutation method?

3/3 point

- ☐ 0.5
- ☐ A random number between 0 and 1
- ☒ 0
- ☐ There is too little information to say

✓ Correct

Explanation: You might think that we don't have enough information to say since you don't even know the metric being used to compute the variable importance. However, since the tree never splits on X, we know that even if we permute the values of X in the dataset, this will never change any prediction. Therefore, no matter what metric we use the variable importance will be 0, since there will be no change in the model output. Therefore the answer is C.

3. We have the following table the output of a model f on an example using subsets of the variable. What is the Shapley value for  $x_{BP}$ ?

3/3 point

Feature Set	Output
$\emptyset$	0.5
$\{x_{BP}\}$	0.7
$\{d_{BP}\}$	0.6
$\{x_{BP}, d_{BP}\}$	0.65

- ☐ 0.3
- ☐ 0.2
- ☐ 0.85
- ☒ 0.125

✓ Correct

Refer to the lesson **Combining importances**.

We know that we compute our Shapley value by taking the prediction value of all features and subtracting it by the prediction value of the features that don't contain our desired value. We do this until we take the prediction value of the desired feature minus the prediction value of the empty set.

We compute the Shapley value for  $x_{BP}$  in the following way:

$$\{d_{BP}, x_{BP}\} - \{d_{BP}\} = (0.65) - (0.6) = \mathbf{0.05}$$

$$\{x_{BP}\} - \emptyset = (0.7) - (0.5) = \mathbf{0.2}$$

Once we have obtained all of our values, we sum them up altogether, then divide by the number of features we have. In this case, we have 2 total features, so we divide by 2.

Calculate the importance of  $x_{BP}$ :

$$((0.05) + (0.2)) / 2$$

$$(0.25) / 2$$

The shapley value for  $x_{BP}$  is: **0.125**

4. We have the following table the output of a model f on an example using subsets of the variable. What is the sum of the Shapley value for  $s_{BP}$  and  $d_{BP}$ ?

3/3 point

Feature Set	Output
$\emptyset$	0.5
$\{s_{BP}\}$	0.7
$\{d_{BP}\}$	0.6
$\{s_{BP}, d_{BP}\}$	0.65

- ☐ 0.3
- ☐ 0.2
- ☐ 0.85
- ☒ 0.15

✓ Correct

We already know the Shapley value of  $s_{BP}$  from Question 3 (0.125). Thus, all we need to calculate is the Shapley value from  $d_{BP}$ .

We compute the shapley value for  $d_{BP}$  in the following way:

$$\{s_{BP}, d_{BP}\} - \{s_{BP}\} = (0.65) - (0.7) = \mathbf{-0.05}$$

$$\{d_{BP}\} - \emptyset = (0.6) - (0.5) = \mathbf{0.1}$$

Once we have obtained all of our values, we sum them up altogether, then divide by the number of features we have. In this case, we have 2 total features, so we divide by 2.

Calculate the importance of  $d_{BP}$ :

$$(0.1 + (-0.05)) / 2$$

$$(0.05) / 2$$

The Shapley value for  $d_{BP}$  is: **0.025**

Since we want to calculate the sum of the Shapley value for  $s_{BP}$  and  $d_{BP}$ , and we already know the value of  $s_{BP}$  from the previous exercise we can sum:

$$\{s_{BP}\} + \{d_{BP}\} =$$

$$(0.125) + (0.025) =$$

$$\mathbf{0.15}$$

5. Could the following table of outputs be given by a linear model with no interactions (assume not including a feature means setting it to 0)?

3/3 point

Feature Set	Output
$\emptyset$	0.5
$\{s_{BP}\}$	0.7
$\{d_{BP}\}$	0.6
$\{s_{BP}, d_{BP}\}$	0.65

- ☐ Yes
- ☒ No

✓ Correct

Explanation: The answer is no. We see that when only adding  $d_{BP}$ , the output goes up, so the coefficient for it must be positive. We also see that when only adding  $s_{BP}$  the output increases, so the coefficient must be positive. However, when we add  $d_{BP}$  to the output with  $s_{BP}$ , the output goes down, a contradiction, since we already know the coefficient for  $d_{BP}$  is positive. This suggests that there must be at least an interaction between  $s_{BP}$  and  $d_{BP}$ .

6. Now assume we add Age as a variable. What is the new Shapley value for  $s_{BP}$ ?

3/3 point

Feature Set	Output
$\emptyset$	0.5
$\{s_{BP}\}$	0.7
$\{d_{BP}\}$	0.6
$\{Age\}$	0.7
$\{s_{BP}, d_{BP}\}$	0.65
$\{s_{BP}, Age\}$	0.7
$\{d_{BP}, Age\}$	0.8
$\{s_{BP}, d_{BP}, Age\}$	0.85

- ☐ 0.3
- ☒ 0.09
- ☐ 0.125
- ☐ 0.20

✓ Correct

Explanation: This computation will be a bit more involved. We see that if  $s_{BP}$  comes first, we get +0.2. If  $s_{BP}$  comes after  $d_{BP}$ , then we get +0.05, as before. If  $s_{BP}$  comes after Age, it gets +0.0. Finally, if it comes after both  $d_{BP}$  and Age, it gets +0.05. Now we have to take a weighted average. The probability  $s_{BP}$  comes first is 1/6, the probability it comes last is 1/6, and the probability it comes after  $d_{BP}$  is 1/6 and after Age is 1/6. Now, the weighted average is  $1/6(0.2) + 1/6(0.05) + 1/6(0.0) + 1/6(0.05) = 0.09$ , so the answer is B.