

# Linear Algebra

TOTAL POINTS 5

1. Let two matrices be

1 / 1 point

$$A = \begin{bmatrix} 1 & -4 \\ -2 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 0 & 3 \\ 5 & 8 \end{bmatrix}$$

What is  $A - B$ ?

- ☐  $\begin{bmatrix} 1 & 7 \\ 7 & 9 \end{bmatrix}$
- ☐  $\begin{bmatrix} 1 & 1 \\ -3 & -7 \end{bmatrix}$
- ☐  $\begin{bmatrix} 1 & -7 \\ -7 & 7 \end{bmatrix}$
- ☒  $\begin{bmatrix} 1 & -7 \\ -7 & -7 \end{bmatrix}$

✔ Correct

2.

1 / 1 point

Let  $x = \begin{bmatrix} 2 \\ 7 \\ 4 \\ 1 \end{bmatrix}$

What is  $3 * x$ ?

- ☒  $\begin{bmatrix} 6 \\ 21 \\ 12 \\ 3 \end{bmatrix}$
- ☐  $\begin{bmatrix} 6 & 21 & 12 & 3 \end{bmatrix}$
- ☐  $\begin{bmatrix} \frac{3}{2} & \frac{7}{4} & \frac{4}{3} & \frac{1}{2} \end{bmatrix}$
- ☐  $\begin{bmatrix} 2+4+7+1=14 \\ 3+7+4+1=15 \\ 2+7+4+1=14 \\ 3+7+4+1=15 \end{bmatrix}$

✔ Correct

To multiply the vector x by 3, take each element of x and multiply that element by 3.

3. Let u be a 3-dimensional vector, where specifically

1 / 1 point

$$u = \begin{bmatrix} 8 \\ 1 \\ 4 \end{bmatrix}$$

What is  $u^T$ ?

- ☐  $\begin{bmatrix} 4 & 1 & 8 \end{bmatrix}$
- ☐  $\begin{bmatrix} 8 \\ 1 \\ 4 \end{bmatrix}$
- ☐  $\begin{bmatrix} 4 \\ 1 \\ 8 \end{bmatrix}$
- ☒  $\begin{bmatrix} 8 & 1 & 4 \end{bmatrix}$

✔ Correct

4. Let u and v be 3-dimensional vectors, where specifically

1 / 1 point

$$u = \begin{bmatrix} -3 \\ 4 \\ 3 \end{bmatrix}$$

and

$$v = \begin{bmatrix} 3 \\ 1 \\ 5 \end{bmatrix}$$

What is  $u^T v$ ?

(Hint:  $u^T$  is a

1x3 dimensional matrix, and v can also be seen as a 3x1

matrix. The answer you want can be obtained by taking

the matrix product of  $u^T$  and v.) Do not add brackets to your answer.

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✔ Correct

5. Let A and B be 3x3 (square) matrices. Which of the following must necessarily hold true? Check all that apply.

1 / 1 point

- ☐ If  $C = A * B$ , then C is a 6x6 matrix.
- ☒ If A is the 3x3 identity matrix, then  $A * B = B * A$

✔ Correct

Even though matrix multiplication is not commutative in general ( $A * B \neq B * A$  for general matrices  $A, B$ ), for the special case where  $A = I$ , we have  $A * B = I * B = B$ , and also  $B * A = B * I = B$ . So,  $A * B = B * A$ .

- ☒  $A + B = B + A$

✔ Correct

We add matrices element-wise. So, this must be true.

- ☐  $A * B = B * A$