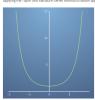
1/1 point

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## Applying the Taylor series

he two previous videos, we have shown the short mathematical proofs for the Taylor series, and for special is when the starting point is x=0, the Maklaurin series. In these set of questions, we will begin to work on hying the Taylor and MacLaurin series formula to obtain approximations of functions.

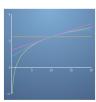


- ①  $f(x) = 1 + x^2 + \frac{x^4}{2} + \dots$ ①  $f(x) = x^2 + \frac{x^4}{2} + \frac{x^4}{6} + \dots$
- $f(x) = 1 + 2x + \frac{x^2}{2} + ...$   $f(x) = 1 x^2 \frac{x^4}{2} ...$



- $f(x) = \frac{(e-4)}{34} + \frac{(e-4)^2}{64} \frac{(e-4)^3}{266} ...$
- $\int f(x) = \frac{1}{4} \frac{(x+4)}{16} + \frac{(x+4)^2}{64} + \dots$   $\bullet f(x) = \frac{1}{4} \frac{(x+4)}{16} + \frac{(x+4)^2}{64} + \dots$   $\bullet f(x) = \frac{1}{4} \frac{(x+4)}{16} \frac{(x+4)^2}{64} + \dots$   $\bullet f(x) = -\frac{1}{4} \frac{(x+4)}{16} \frac{(x+4)^2}{64} + \dots$





- $\triangle f(2) = 0$   $\triangle f(2) = 0.5$
- $\triangle f(2) = 1.0$

## ✓ Correct The second order Taylor approxin

ation about the point x=10 is  $f(x)=\ln(10)+rac{(x-10)}{10}-rac{(x-10)^2}{300}\dots$ 

 $g_1 = \ln(10) + \frac{(s-10)}{10}$ 

and the second order approxima

 $g_2 = \ln(10) + \frac{(x-10)}{10} - \frac{(x-10)^2}{200}$ .

 $|g_2(2)-g_1(2)|=|-rac{(x-10)^2}{200}|$  and substituting in x=2 gives t

 $|g_2(2)-g_1(2)|=|-\tfrac{(2-10)^2}{200}|=0.32$ 

In some case, a Taylor series can be supressed in a general equation that allows us to find a particular  $r^{th}$  term of our series. For example the function  $f(x) = e^{x}$  has the general equation  $f(x) = \sum_{n=0}^{\infty} \frac{1}{n^n}$ . Therefore if we want to find the  $S^{th}$  eterm in our Taylor series, substituting m = 2 into the general equation gives us the term  $\frac{d^2}{2}$ . We know the Taylor series of the function  $e^{x}$  is  $f(x) = 1 + x + \frac{x^2}{n} + \frac{x^2}{n} + \dots$ . Now let us try a further confirming example quality into greater equations with Taylor series.





By evaluating the function  $f(x) = \frac{1}{(1-x)^2}$  order term correctly represents f(x).

- order term correctly represents f  $\int f(x) = \sum_{n=0}^{\infty} (1+n)(-x)^n$   $\int f(x) = \sum_{n=0}^{\infty} (2+n)(x)^n$   $\int f(x) = \sum_{n=0}^{\infty} (1+2n)(x)^n$   $\bullet f(x) = \sum_{n=0}^{\infty} (1+n)x^n$

 $\checkmark$  Correct By doing a Matleurin series approximation, we obtain  $f(x)=1+2x+3x^2+4x^3+5x^4+\dots$  which satisfies the general equation shown.



- ⓐ  $f(x) = 2 \frac{x}{4} \frac{x^2}{64}$ ...  $f(x) = \frac{x}{4} \frac{x^2}{64}$ ...  $f(x) = 2 x \frac{x^2}{64}$ ...  $f(x) = 2 + x + x^2$ ...