1/1 point

1/1 point

## Newton-Raphson in one dimension

Consider the following graph of a function



There are two planear x=1.

Then, if we assume that the function goes to zero somewhere nearby, we can re-arrange to file, e. assume  $f(x_0+\delta x)=0$  and solve for  $\delta x$ . This becomes,

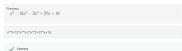
$$\delta x = -\frac{f(x_0)}{f'(x_0)}$$

Since the function, f(x) is not a line, this formula will (try) to get closer to the root, but won't exactly hit it. But this is OK, because we can repeat the process from the new starting point to get even closer,

 $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$ 

For the graph we showed above, the equation of the function is

$$f(x) = \frac{x^6}{6} - 3x^4 - \frac{2x^3}{3} + \frac{27x^2}{2} + 18x - 30.$$



By using  $x_0=1$  as a starting point and calculating -f(1)/f'(1) by Raphson method, i.e., find  $x_1$  .

```
Give your answer to 3 decimal places.

1.063
```

Let's use code to find the other root, near x=-4.

Complete the d\_f function in the code block with you perform iterations of the Newton-Raphson method.



-3.760

Since the step size is given by  $\delta x=-f(x)/f'(x)$ , this can get big we exactly zero at turning points of f(x). This is where Newton-Raphson

None of the other stat

lacksquare The method converges to the root nearest z=-4



Some starting points on the curve do not co  $3.1\,\mathrm{as}$  a starting point; it does just this.

Again, this is behaviour that happens in areas where the curve is not well descri our initial linearisation assumption was not a good one for such a starting point



(a) Yes, to the root nearest x = 1.

 $\bigcap$  Yes, to the root nearest x=-4.

✓ Correct Eventually this tricky starting point s