## Matching functions and approximations



Below are three graphs highlighting the zeroth, second and fourth order approximations of a common trigonometric function. Observe how increasing the number of approximations in the power series begins to build a better approximation, and determine which function these approximations represent.

 $f_0(x) = 1$ 



$$f_4(x) = 1 - \frac{x^2}{2} + \frac{x^4}{24}$$





The function  $f(x)=\cos(x)$  is symmetric about the line x=0. Furthermore our approximation of this function is when x=0, from an a Maclaurin series. At the point x=0, f(0)=1 which is shown in the zeroth order approximation.

Below are three graphs highlighting the first, third and fifth order approximations of a common trigonometric function. Observe how the power series begins to build the function, and determine which function these approximations represent.





 $f_5(x) = 2x - \frac{4x^3}{12} + \frac{4x^5}{12}$ 





✓ Correct

The function f(x) = sin(2x) has rotational symmetry about the origin. Furthermore, we can see that the period is much shorter, also evident from the three approximations shown.



 $f(x) = -\frac{x^2}{3} + \frac{x^2}{3}$ .





 $\checkmark$  Correct
We can see this approximation goes through the origin and also books as if it fits the function well between  $\delta < x < 0.5$ .





The sinusoidal function  $f(x)=\sin(x)$  (green line) centered at x=0 is shown in the graph below. The approximation for this function is shown through the series  $f(x)=x-\frac{x^2}{6}\dots$  (orange line). Determine what polynomial order is represented by the orange line.







- First Order
  Second Order
  Third Order

  Not a correct a