

ESTIMATION OF THE SURFACE  
SHRINKAGE RATE BASED ON THE  
EFFECT OF DIFFERENT WASHING  
ALGORITHMS VIA MACHINE  
LEARNING APPROACH

## **SEN MÜHENDİSSİN BİZİMLESİN PROJECT**

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Gökhan SIR



# EXECUTIVE SUMMARY

The aim of the project is to analyze first input features with EDA (Exploratory Data Analysis) methodology by using Excel, Tableau and Python programs (such as descriptive analysis, correlation computation between inputs and also output, detecting outliers with statistic tests, OLS regression for backward selection to be able to analyze features' p-values,  $r^2$  score, feature importance scores after fitting the ML algorithms...) and then to install the model for estimation on surface area shrinkage rate of woolen textiles.

For the best model, bagging and boosting ensemble learning algorithms and linear regression will be used, also to avoid high variance and overfitting/underfitting, grid search method will be used to optimize algos' hyper params.

# INTRODUCTION

## Predictive Modeling

Generally used to feed predictive models:

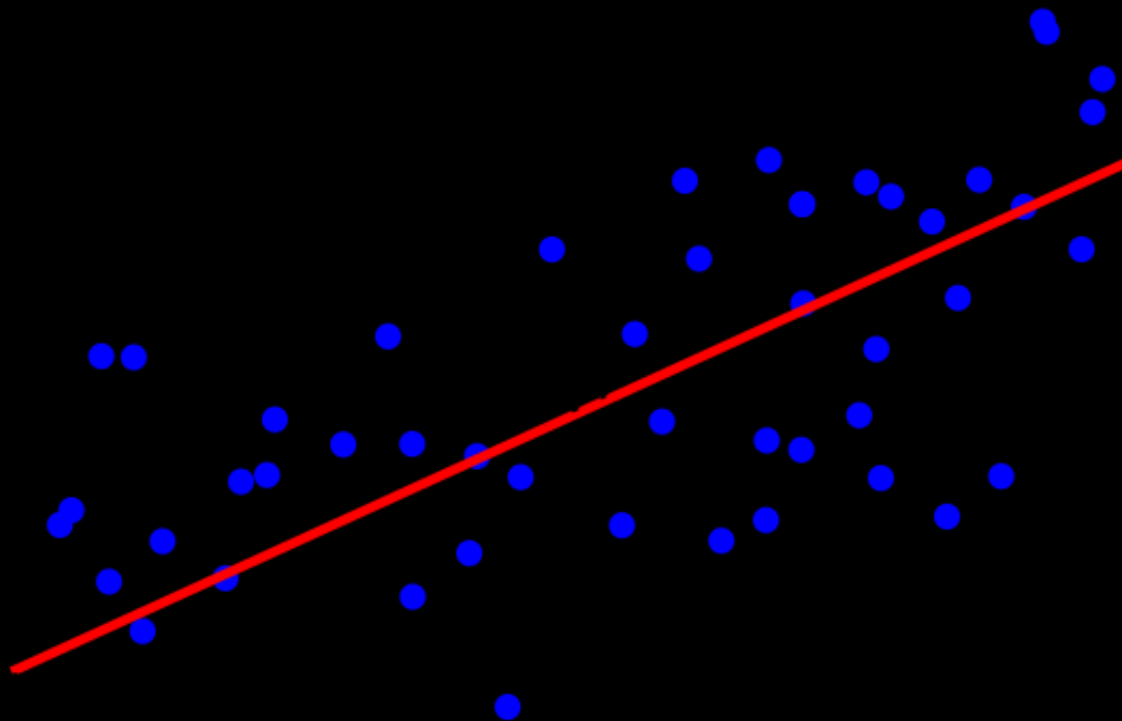
- Transaction data
- CRM data
- Customer service data
- Survey or polling data
- Digital marketing and advertising data
- Economic data
- Demographic data
- Machine-generated data (for example, telemetric data or data from sensors)
- Geographical data
- Web traffic data

Predictive  
Modeling

# INTRODUCTION

## Types of Predictive Models

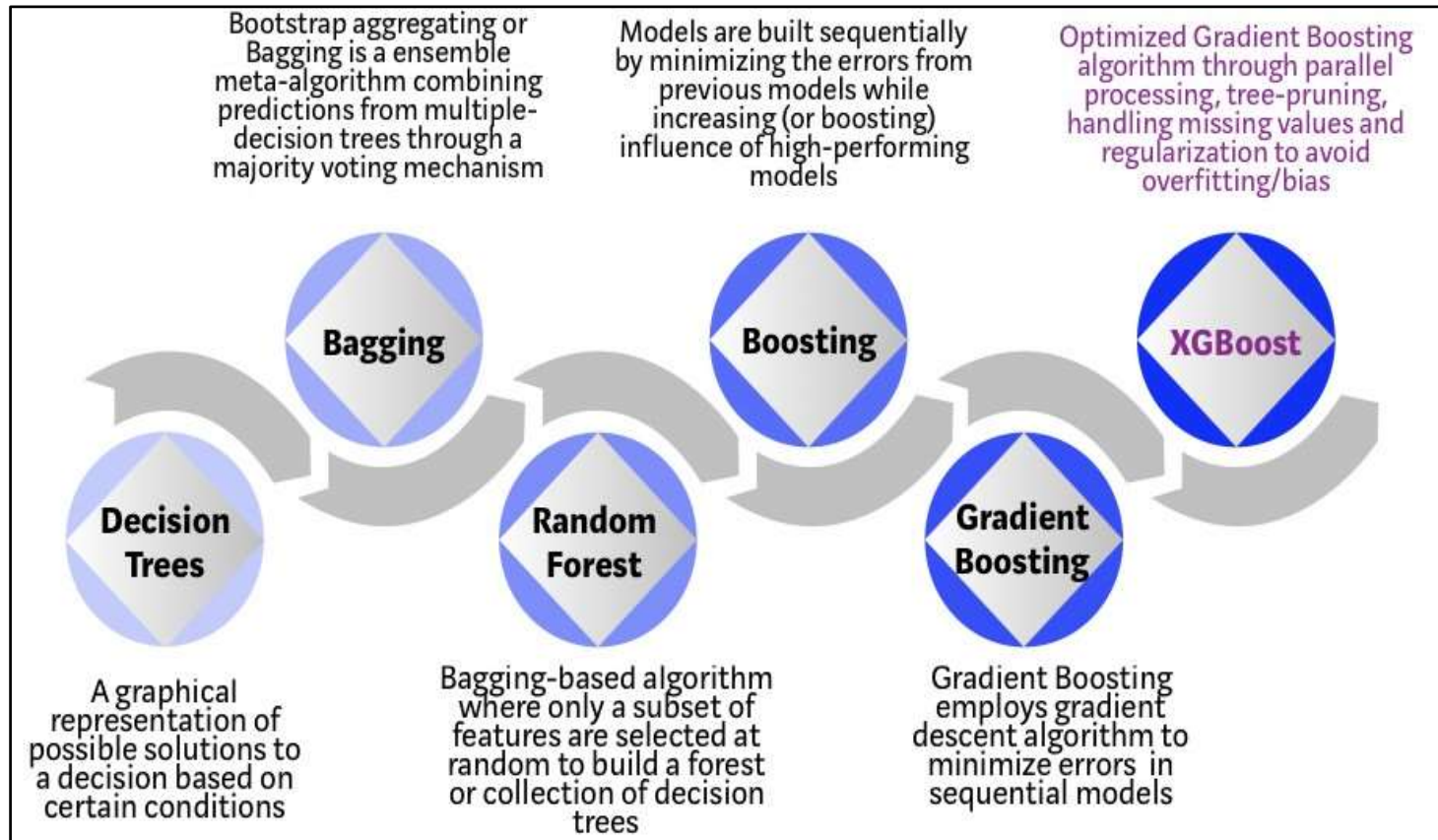
- Generalized Linear Models (GLM)
- Random Forests
- Decision Trees
- Neural Networks
  - ❑ In prediction problems involving unstructured data (images, text, etc.) artificial neural networks tend to **outperform** all other algorithms or frameworks.
- Gradient Boosting Models (GBM)
- Support vector machines (Support Vector Regression-SVR)
- Extended Gradient Boosting Models (XGBoost)
  - ❑ Small-to-medium structured /tabular data, decision tree-based algorithms are considered **best-in-class**.



# GENERALIZED LINEAR MODEL

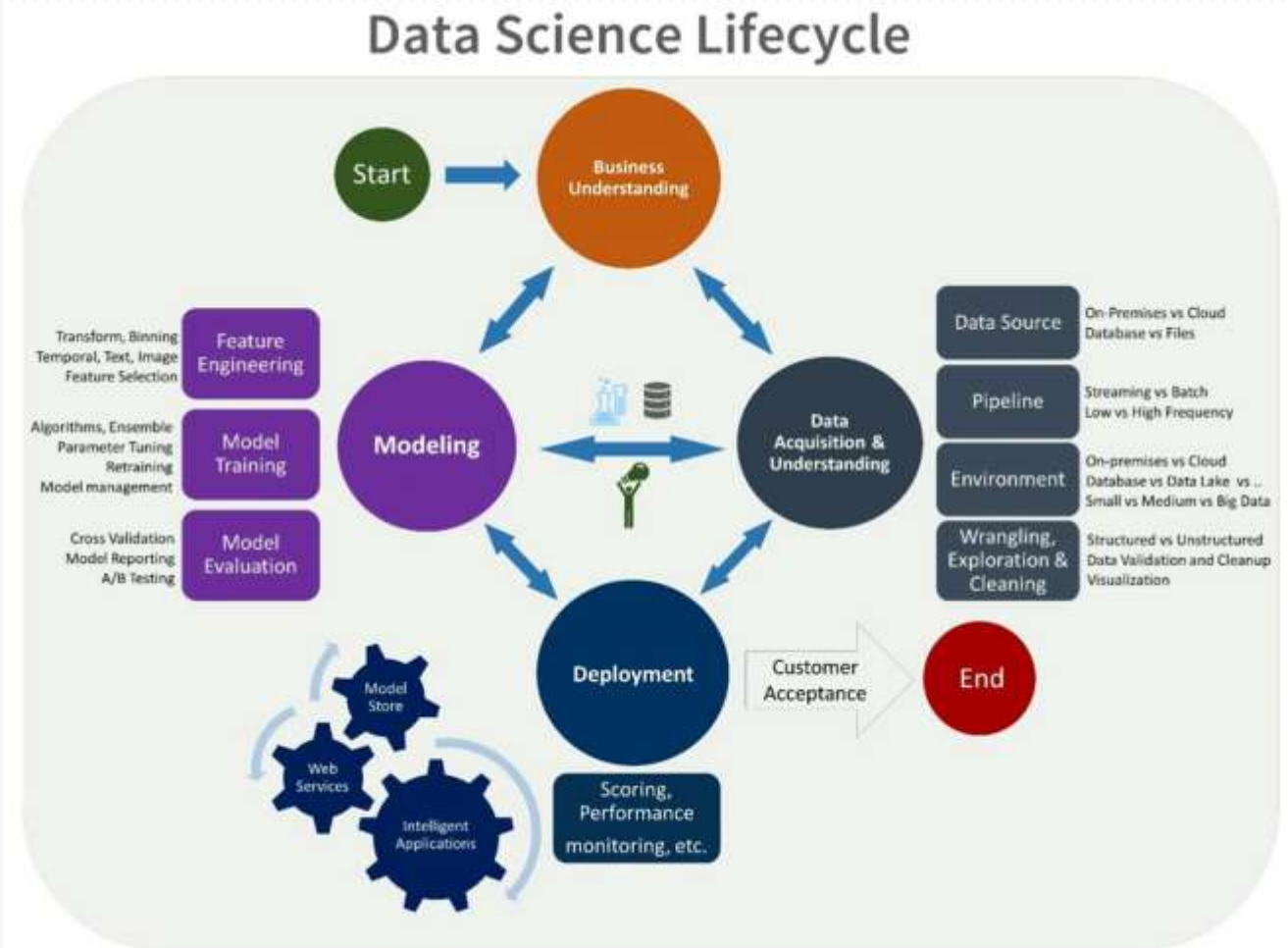
The GLM generalizes linear regression by allowing the linear model to be related to the response variable via a link function and by allowing the magnitude of the variance of each measurement to be a function of its predicted value.





# EVOLUTION OF TREE-BASED ALGOS

# METHODOLOGY



A grayscale photograph of an Arçelik front-loading washing machine. The top section shows the control panel with the Arçelik logo, a power button, a large circular dial, and several touch-sensitive buttons for various wash programs. Below the panel is the circular glass door, which is slightly ajar, revealing the internal drum and its paddles. The entire image is overlaid with a large, white, double-lined rectangular frame.

# DATA ACQUISITION & UNDERSTANDING



# DATA ACQUISITION & UNDERSTANDING

## Washing Machine algorithm flow:

- First, water is taken,
- The laundry is washed with this water for a certain period of time without heating,
- Then the heater turns on,
- After turning on the heater, water is heated,
- Again the laundry is washed with heated water,
- Then, dirty waters are drainaged,
- After the drainage, the 1st rinse water is taken. The laundry is cleaned with detergent and 1st rinse water. And same process is applied again for 2nd and 3rd rinse water,
- Then, after the drainage, process is finished by wring laundry.

|                                       |   |
|---------------------------------------|---|
| <b>Test_No</b>                        | # of test washings (1,2,3,4,5,6)              |
| <b>Numune_1_Relakse_Sonrasi_En_1</b>  | Measured width-1 value of the sample          |
| <b>Numune_1_Relakse_Sonrasi_En_2</b>  | Measured width-2 value of the sample          |
| <b>Numune_1_Relakse_Sonrasi_En_3</b>  | Measured width-3 value of the sample          |
| <b>Numune_1_Relakse_Sonrasi_Boy_1</b> | Measured length-1 value of the sample         |
| <b>Numune_1_Relakse_Sonrasi_Boy_2</b> | Measured length-2 value of the sample         |
| <b>Numune_1_Relakse_Sonrasi_Boy_3</b> | Measured length-3 value of the sample         |
| <b>Giris_Alan_Ortalama</b>            | Average inlet surface area of the sample      |
| <b>Deterjan_Miktari(gr)</b>           | The amount of detergent used in the algorithm |
| <b>Test_Kapasitesi(kg)</b>            | Weight of sample and filling load (kg)        |

|                          |   |
|--------------------------|---|
| <b>Su_Sertligi</b>       | Water hardness – German hardness (pH value)                                   |
| <b>Tambur_Hacmi_(lt)</b> | The volume of the washing machine   |
| <b>SY1_Sure_(sn)</b>     | Cold Washing Time (in seconds)  |
| <b>SY1_Devir_(rpm)</b>   | Cold Washing speed  |
| <b>SY1_ED</b>            | Total rotation rate of the engine in cold wash (in %)                         |
| <b>SG_Sic_(C)</b>        | Entry Temperature at which water enters first to washing machine in cold wash |
| <b>I_Bas_Sic (C)</b>     | Heater start Temperature at the end of the Cold Wash                          |
| <b>I_Sure_(sn)</b>       | Heating time of the heater (in mins)  |
| <b>I_Devir_(rpm)</b>     | Heater speed  |
| <b>I_MHY_ED</b>          | Total rotation rate of the engine in heater period (in %)                     |
| <b>I_Tset_(C)</b>        | Amount of temperature at the end of heating                                   |

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|                        |  |
|------------------------|--|
| <b>AY_Su_Mik_(lt)</b>  | The amount of water used in the main wash  |
| <b>AY_Sure_(sn)</b>    | Main wash time   |
| <b>AY_Devir_(rpm)</b>  | Main wash speed  |
| <b>AY_MHY_ED</b>       | Total rotation rate of the engine in the main wash (in %)  |
| <b>AY_Tah_(C)</b>      | The temperature of the discharged water during the 1st rinse water removal after the main wash is finished |
| <b>Jet_Pompa</b>       | Jet pump system, 1 means machine has, 0 means does not have  |
| <b>Durulama_Sayisi</b> | # of rinses  |
| <b>1D_Su_Mik_(lt)</b>  | The amount of water taken in the 1st rinsing   |
| <b>1D_Sure_(sn)</b>    | 1st rinsing time   |
| <b>1D_Devir_(rpm)</b>  | 1st rinsing speed  |
| <b>1D_MHY_ED</b>       | Total rotation rate of the engine in the 1st rinsing (in %)  |

|                            |  |
|----------------------------|--|
| <b>2D_Su_Mik_(lt)</b>      | The amount of water taken in the 2nd rinsing                 |
| <b>2D_Sure_(sn)</b>        | 2nd rinsing time   |
| <b>2D_Devir_(rpm)</b>      | 2nd rinsing speed  |
| <b>2D_MHY_ED</b>           | Total rotation rate of the engine in the 2nd rinsing (in %)  |
| <b>2D_Sikma_(rpm)</b>      | 2nd rinsing spin amount                                      |
| <b>3D_Su_Mik_(lt)</b>      | The amount of water taken in the 3rd rinsing                 |
| <b>3D_Sure_(sn)</b>        | 3rd rinsing time   |
| <b>3D_Devir_(rpm)</b>      | 3rd rinsing speed  |
| <b>3D_MHY_ED</b>           | Total rotation rate of the engine in the 3rd rinsing (in %)  |
| <b>Cikis_Alan_Ortalama</b> | Average surface area of the sample at the end of the process |

**E** XPLORATORY

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**D** ATA

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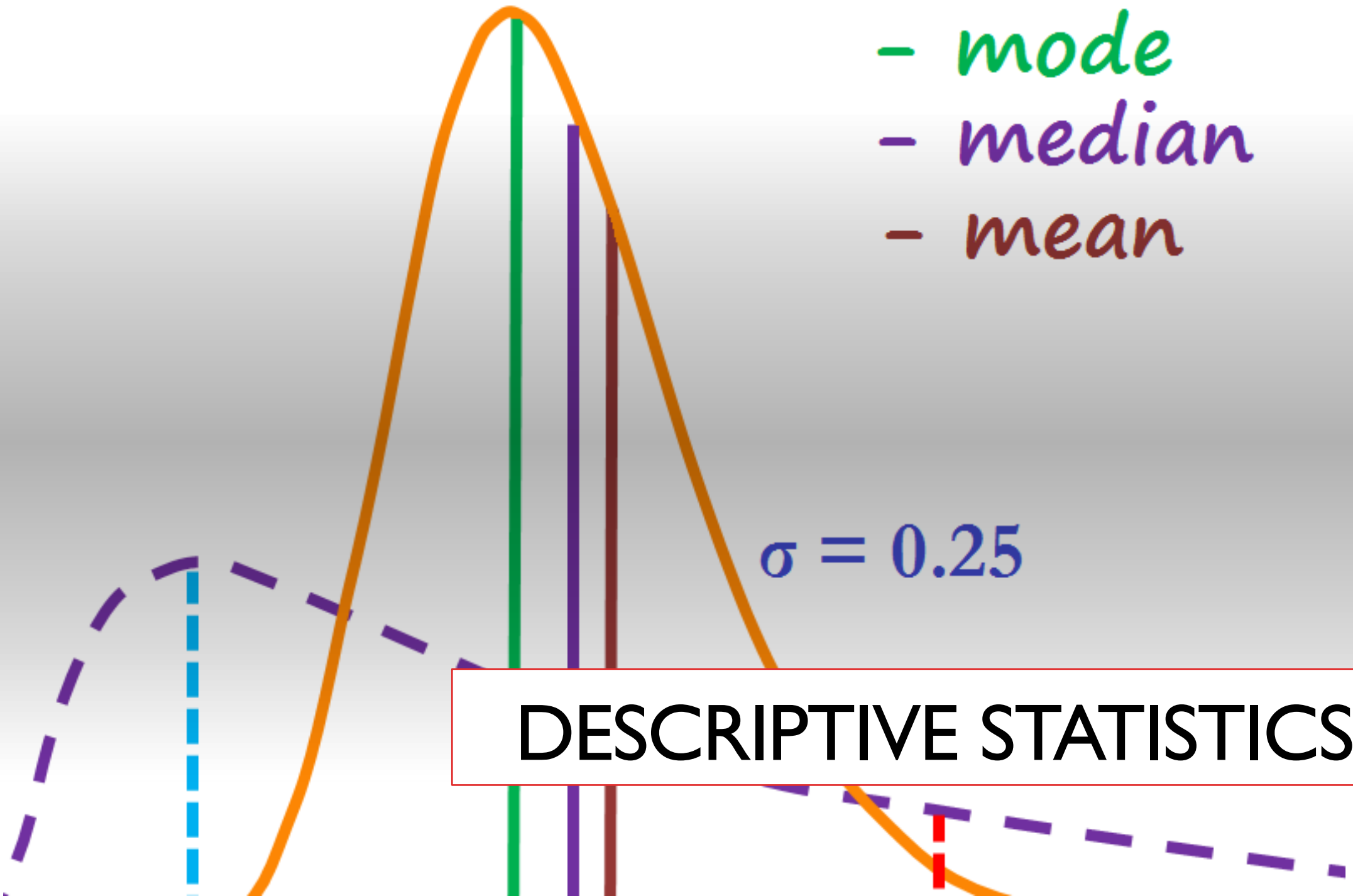
**A** NALYSIS



- mode
- median
- mean

$$\sigma = 0.25$$

DESCRIPTIVE STATISTICS



### df.dtypes

|                                |         |
|--------------------------------|---------|
| Test_No                        | float64 |
| Numune_I_Relakse_Sonrasi_En_1  | float64 |
| Numune_I_Relakse_Sonrasi_En_2  | float64 |
| Numune_I_Relakse_Sonrasi_En_3  | float64 |
| Numune_I_Relakse_Sonrasi_Boy_1 | float64 |
| Numune_I_Relakse_Sonrasi_Boy_2 | float64 |
| Numune_I_Relakse_Sonrasi_Boy_3 | float64 |
| Giris_Alan_Ortalama            | float64 |
| Deterjan_Miktari(gr)           | float64 |
| Test_Kapasitesi(kg)            | float64 |
| Su_Sertligi                    | float64 |
| Tambur_Hacmi_(lt)              | float64 |
| SYI_Sure_(sn)                  | float64 |
| SYI_Devir_(rpm)                | float64 |
| SYI_ED                         | float64 |
| SG_Sic_(C)                     | float64 |
| I_Bas_Sic (C)                  | float64 |
| I_Sure_(sn)                    | float64 |
| I_Devir_(rpm)                  | float64 |
| I_MHY_ED                       | float64 |
| I_Tset_(C)                     | float64 |

|                     |         |
|---------------------|---------|
| AY_Su_Mik_(lt)      | float64 |
| AY_Sure_(sn)        | float64 |
| AY_Devir_(rpm)      | float64 |
| AY_MHY_ED           | float64 |
| AY_Tah_(C)          | float64 |
| Jet_Pompa           | float64 |
| Durulama_Sayisi     | float64 |
| ID_Su_Mik_(lt)      | float64 |
| ID_Sure_(sn)        | float64 |
| ID_Devir_(rpm)      | float64 |
| ID_MHY_ED           | float64 |
| 2D_Su_Mik_(lt)      | float64 |
| 2D_Sure_(sn)        | float64 |
| 2D_Devir_(rpm)      | float64 |
| 2D_MHY_ED           | float64 |
| 2D_Sikma_(rpm)      | float64 |
| 3D_Su_Mik_(lt)      | float64 |
| 3D_Sure_(sn)        | float64 |
| 3D_Devir_(rpm)      | float64 |
| 3D_MHY_ED           | float64 |
| Cikis_Alan_Ortalama | float64 |

```
In [52]: df.isnull()
```

```
Out[52]:
```

|     | Test_No | Numune_1_ | Relakse_Sonrasi_ | En_1  | ... | 3D_MHY_ED | Cikis_Alan_Ortalama |
|-----|---------|-----------|------------------|-------|-----|-----------|---------------------|
| 0   | False   |           |                  | False | ... | False     | False               |
| 1   | False   |           |                  | False | ... | False     | False               |
| 2   | False   |           |                  | False | ... | False     | False               |
| 3   | False   |           |                  | False | ... | False     | False               |
| 4   | False   |           |                  | False | ... | False     | False               |
| ..  | ...     |           |                  | ...   | ... | ...       | ...                 |
| 175 | False   |           |                  | False | ... | False     | False               |
| 176 | False   |           |                  | False | ... | False     | False               |
| 177 | False   |           |                  | False | ... | False     | False               |
| 178 | False   |           |                  | False | ... | False     | False               |
| 179 | False   |           |                  | False | ... | False     | False               |

```
[180 rows x 42 columns]
```

NO MISSING VALUE

```
In [53]: duplicate_rows_df = df[df.duplicated()]
```

NO DUPLICATE  
ROW

```
In [54]: print('number of duplicate rows:', duplicate_rows_df.shape)
number of duplicate rows: (0, 42)
```

|             | Test_No      | En_1         | En_2         | En_3         | Boy_1        | Boy_2        | Boy_3        | GAO          | Deterjan_Mikt<br>arı(gr) | Test_Kapasitesi<br>(kg) | Su_Sertligi | Tambur_Hacmi<br>(lt) | SY1_Sure_(sn) | SY1_Devir_(rp<br>m) | SY1_ED       | SG_Sic_(C)   | I_Bas_Sic_(C) | I_Sure_(sn)  | I_Devir_(rpm) | I_MHY_ED     | I_Tset_(C)   | AY_Su_Mik_(lt) |
|-------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------------------|-------------------------|-------------|----------------------|---------------|---------------------|--------------|--------------|---------------|--------------|---------------|--------------|--------------|----------------|
| count       | 180          | 180          | 180          | 180          | 180          | 180          | 180          | 180          | 180                      | 180                     | 180         | 180                  | 180           | 180                 | 180          | 180          | 180           | 180          | 180           | 180          | 180          | 180            |
| mean        | 3,5          | 273,05       | 272,4166667  | 272,9        | 267,5        | 267,3666667  | 267,4833333  | 72953,2907   | 56,27333333              | 1,866666667             | 6,2         | 65,36                | 382,4111111   | 28,33333333         | 0,040266667  | 15,18066667  | 16,19766667   | 456,0111111  | 24,33333333   | 0,824666667  | 34,98666667  | 12,63722222    |
| std         | 1,712588945  | 1,694634978  | 2,018420756  | 1,814282258  | 5,000558628  | 4,722938201  | 4,688301142  | 1170,208449  | 3,647446493              | 0,34088285              | 3,496846145 | 0,681896796          | 327,8284991   | 7,695315269         | 0,018103859  | 0,500015195  | 6,437890811   | 232,9864644  | 12,26340334   | 1,607392017  | 8,339758581  | 0,55238038     |
| min         | 1            | 271          | 270          | 270,5        | 248,5        | 250          | 250          | 68986,75     | 47                       | 1                       | 3           | 64                   | 176,9         | 0                   | 0            | 12,98        | 0             | 0            | 0             | 0            | 15,98        | 11,48          |
| 25%         | 2            | 272          | 271          | 271,5        | 268          | 268          | 268          | 72807,778    | 57,7                     | 2                       | 5           | 65,7                 | 180           | 30                  | 0,029        | 14,83        | 17,57         | 300          | 30            | 0,011        | 30,94        | 12,32          |
| 50%         | 3,5          | 272,75       | 271,75       | 272,5        | 268,75       | 268,25       | 268,75       | 73144        | 57,7                     | 2                       | 5           | 65,7                 | 297           | 30                  | 0,036        | 15,23        | 18,265        | 477          | 30            | 0,058        | 37,47        | 12,685         |
| 75%         | 5            | 275          | 273,5        | 273,5        | 269,5        | 269          | 269          | 73485,833    | 57,7                     | 2                       | 5           | 65,7                 | 357           | 30                  | 0,058        | 15,51        | 19,32         | 636          | 30            | 0,058        | 41,77        | 12,8           |
| max         | 6            | 276,5        | 277          | 277          | 271          | 270          | 270,5        | 74292,167    | 57,7                     | 2                       | 15          | 65,7                 | 1480          | 35                  | 0,058        | 16,2         | 21            | 810          | 35            | 4,76         | 46,26        | 14,44          |
| max=min     | eşit değil   | eşit değil   | eşit değil   | eşit değil   | eşit değil   | eşit değil   | eşit değil   | eşit değil   | eşit değil               | eşit değil              | eşit değil  | eşit değil           | eşit değil    | eşit değil          | eşit değil   | eşit değil   | eşit değil    | eşit değil   | eşit değil    | eşit değil   | eşit değil   | eşit değil     |
| max-min     | 5            | 5,5          | 7            | 6,5          | 22,5         | 20           | 20,5         | 5305,417     | 10,7                     | 1                       | 12          | 1,7                  | 1303,1        | 35                  | 0,058        | 3,22         | 21            | 810          | 35            | 4,76         | 30,28        | 2,96           |
| median-mean | 0            | -0,3         | -0,666666667 | -0,4         | 1,25         | 0,883333333  | 1,266666667  | 190,7093     | 1,426666667              | 0,133333333             | -1,2        | 0,34                 | -85,41111111  | 1,666666667         | -0,004266667 | 0,049333333  | 2,067333333   | 20,98888889  | 5,666666667   | -0,766666667 | 2,483333333  | 0,047777778    |
| SKEWNESS    | 0            | 0,613060857  | 0,660676599  | 0,83572226   | -3,260261705 | -3,329913682 | -3,327572638 | -2,394629595 | -2,175448351             | -2,175448351            | 2,076044927 | -1,512634581         | 2,603931062   | -3,330688423        | -0,713845603 | -0,867887424 | -2,082686198  | -0,618799546 | -1,470632541  | 1,602676423  | -0,945102159 | 0,696366716    |
| KURTOSIS    | -1,270438828 | -0,783263545 | -0,712381127 | -0,230475788 | 9,401776493  | 9,642285988  | 9,641744814  | 6,035844615  | 2,763155003              | 2,763155003             | 2,570052941 | 0,291174697          | 5,886342993   | 9,73013713          | -0,439179542 | 2,635950529  | 2,54767411    | -0,392994428 | 0,247312818   | 0,739203732  | -0,045574969 | 2,56451849     |

|             | AY_Sure_(sn) | AY_Devir_(rp<br>m) | AY_MHY_ED   | AY_Tah_(C)  | Jet_Pompa   | Durulama_Say<br>ısı | 1D_Su_Mik_(l<br>t) | 1D_Sure_(sn) | 1D_Devir_(rp<br>m) | 1D_MHY_ED   | 2D_Su_Mik_(l<br>t) | 2D_Sure_(sn) | 2D_Devir_(rp<br>m) | 2D_MHY_ED   | 2D_Sikma_(rp<br>m) | 3D_Su_Mik_(l<br>t) | 3D_Sure_(sn) | 3D_Devir_(rp<br>m) | 3D_MHY_ED   | CAO         |
|-------------|--------------|--------------------|-------------|-------------|-------------|---------------------|--------------------|--------------|--------------------|-------------|--------------------|--------------|--------------------|-------------|--------------------|--------------------|--------------|--------------------|-------------|-------------|
| count       | 180          | 180                | 180         | 180         | 180         | 180                 | 180                | 180          | 180                | 180         | 180                | 180          | 180                | 180         | 180                | 180                | 180          | 180                | 180         | 180         |
| mean        | 1187,833333  | 28,33333333        | 0,038666667 | 29,78288889 | 0,866666667 | 3                   | 11,24555556        | 264,4333333  | 28,33333333        | 0,039466667 | 11,29544444        | 255,9555556  | 28,33333333        | 1,426133333 | 81,57777778        | 13,99811111        | 222,85       | 28,33333333        | 0,039533333 | 67735,04257 |
| std         | 535,8431825  | 7,695315269        | 0,019429862 | 5,759223304 | 0,34088285  | 0                   | 0,635216254        | 68,39681295  | 7,695315269        | 0,018863343 | 0,675129056        | 58,98696213  | 7,695315269        | 1,78588724  | 208,5725884        | 0,53650617         | 40,8537636   | 7,695315269        | 0,018759995 | 3541,243852 |
| min         | 438          | 0                  | 0           | 17,85       | 0           | 3                   | 9,82               | 160          | 0                  | 0           | 9,82               | 160          | 0                  | 0           | 0                  | 13,26              | 160          | 0                  | 0           | 55492,5     |
| 25%         | 612          | 30                 | 0,024       | 26          | 1           | 3                   | 10,83              | 179          | 30                 | 0,024       | 10,87              | 180          | 30                 | 0,058       | 0                  | 13,66              | 180          | 30                 | 0,024       | 65556,12475 |
| 50%         | 955          | 30                 | 0,036       | 31,585      | 1           | 3                   | 11,595             | 295          | 30                 | 0,036       | 11,62              | 295          | 30                 | 0,058       | 0                  | 13,78              | 235          | 30                 | 0,036       | 68284       |
| 75%         | 1808         | 30                 | 0,058       | 33,58       | 1           | 3                   | 11,72              | 300          | 30                 | 0,058       | 11,74              | 299          | 30                 | 3,61        | 0                  | 14,58              | 240          | 30                 | 0,058       | 70600,49975 |
| max         | 1918         | 35                 | 0,058       | 41,28       | 1           | 3                   | 11,84              | 366          | 35                 | 0,058       | 12,71              | 304          | 35                 | 4,76        | 620                | 15,91              | 352          | 35                 | 0,058       | 73840,5     |
| max=min     | eşit değil   | eşit değil         | eşit değil  | eşit değil  | eşit değil  | eşit                | eşit değil         | eşit değil   | eşit değil         | eşit değil  | eşit değil         | eşit değil   | eşit değil         | eşit değil  | eşit değil         | eşit değil         | eşit değil   | eşit değil         | eşit değil  | eşit değil  |
| max-min     | 1480         | 35                 | 0,058       | 23,43       | 1           | 0                   | 2,02               | 206          | 35                 | 0,058       | 2,89               | 144          | 35                 | 4,76        | 620                | 2,65               | 192          | 35                 | 0,058       | 18348       |
| median-mean | -            | -                  | -           | -           | -           | -                   | -                  | -            | -                  | -           | -                  | -            | -                  | -           | -                  | -                  | -            | -                  | -           | -           |
|             | 232,8333333  | 1,666666667        | 0,002666667 | 1,802111111 | 0,133333333 | 0                   | 0,349444444        | 30,56666667  | 1,666666667        | 0,003466667 | 0,324555556        | 39,04444444  | 1,666666667        | 1,368133333 | 81,57777778        | 0,218111111        | 12,15        | 1,666666667        | 0,003533333 | 548,9574333 |
| SKEWNESS    | 0,102343503  | 3,330688423        | -0,53507349 | 0,588976304 | 2,175448351 | 0                   | 1,185669638        | 0,334065516  | 3,330688423        | 0,626218518 | 0,990964029        | 0,726616709  | 3,330688423        | 0,653548692 | 2,175836646        | 1,025273445        | 0,386394596  | 3,330688423        | 0,621556795 | 0,771024791 |
| KURTOSIS    | -            | -                  | -           | -           | -           | -                   | -                  | -            | -                  | -           | -                  | -            | -                  | -           | -                  | -                  | -            | -                  | -           | -           |
|             | 1,619877749  | 9,73013713         | 0,994405967 | 0,337445911 | 2,763155003 | 0                   | 0,142578778        | 1,263010795  | 9,73013713         | 0,771316786 | 0,078394437        | 1,453543148  | 9,73013713         | 1,363625826 | 2,76564041         | 0,354449722        | 0,266542043  | 9,73013713         | 0,766140788 | 0,308871767 |

# Interpretation for descriptive statistics

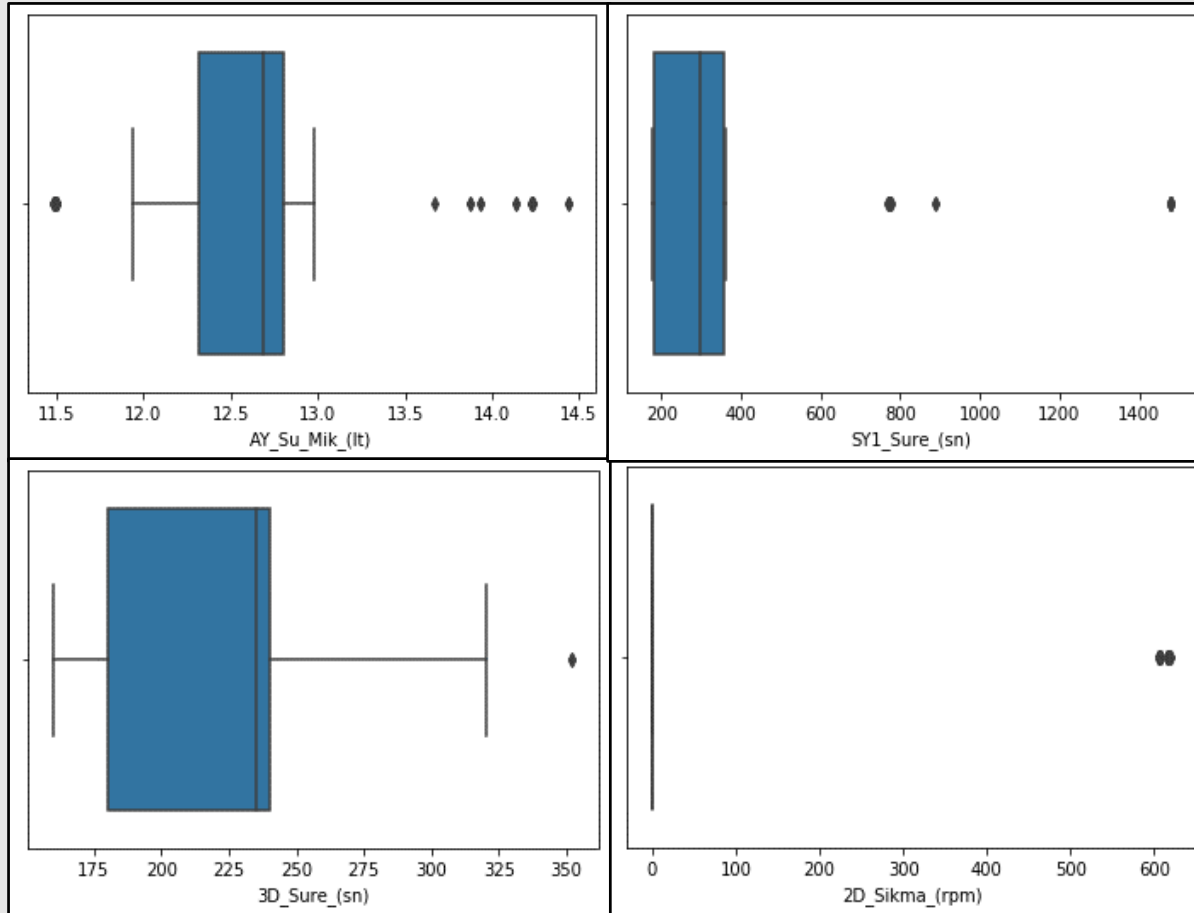
- **Count:** This is important for the first perception about the volume of «missing data».
  - Therefore, there are no missing values for all features.
- **Min and max values:** This can give an idea about the range of values and is helpful to detect outliers.
  - «Durulama Sayısı» has the same min and max values, which means this feature has to be dropped from the data frame. Bcz it causes error during the calculation of the standard deviation.
  - Furthermore, the other exception could eventually be the max values of «SYI\_Sure\_(sn)», «3D\_Sure\_(sn)» and «2D\_Sikma\_(rpm)».
- **Median and mean:** The proximity of the mean and median values indicate proximity to the normal distribution.

**!!! If median equals mean (or is very close), the distribution can be considered as normally distributed!!!**

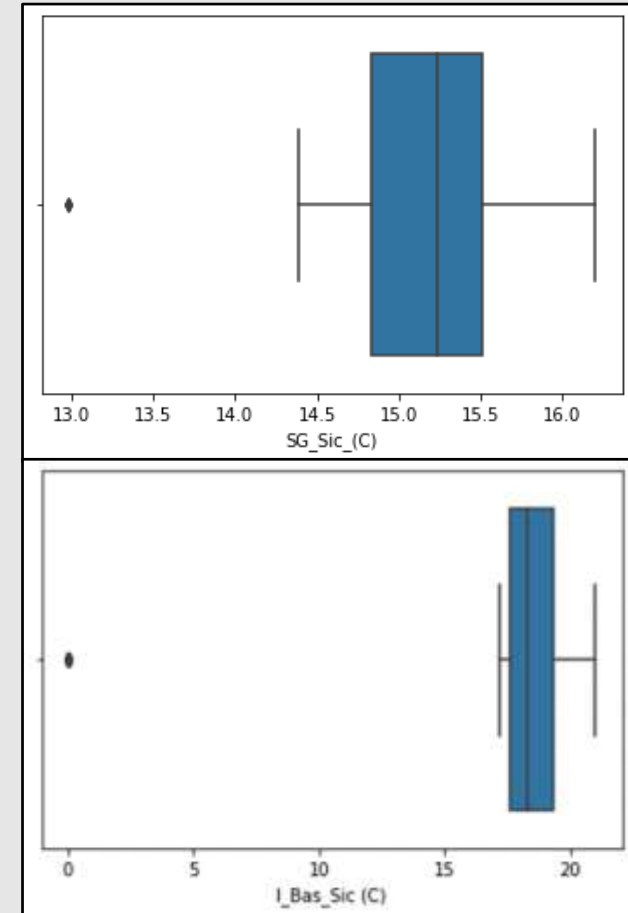
- **Mean and standard deviation:** «mean»; the central tendency of the distribution, «standard deviation», quantifies its amount of variation.

**!!! A low standard deviation suggests that data points tend to be close to the mean!!!**

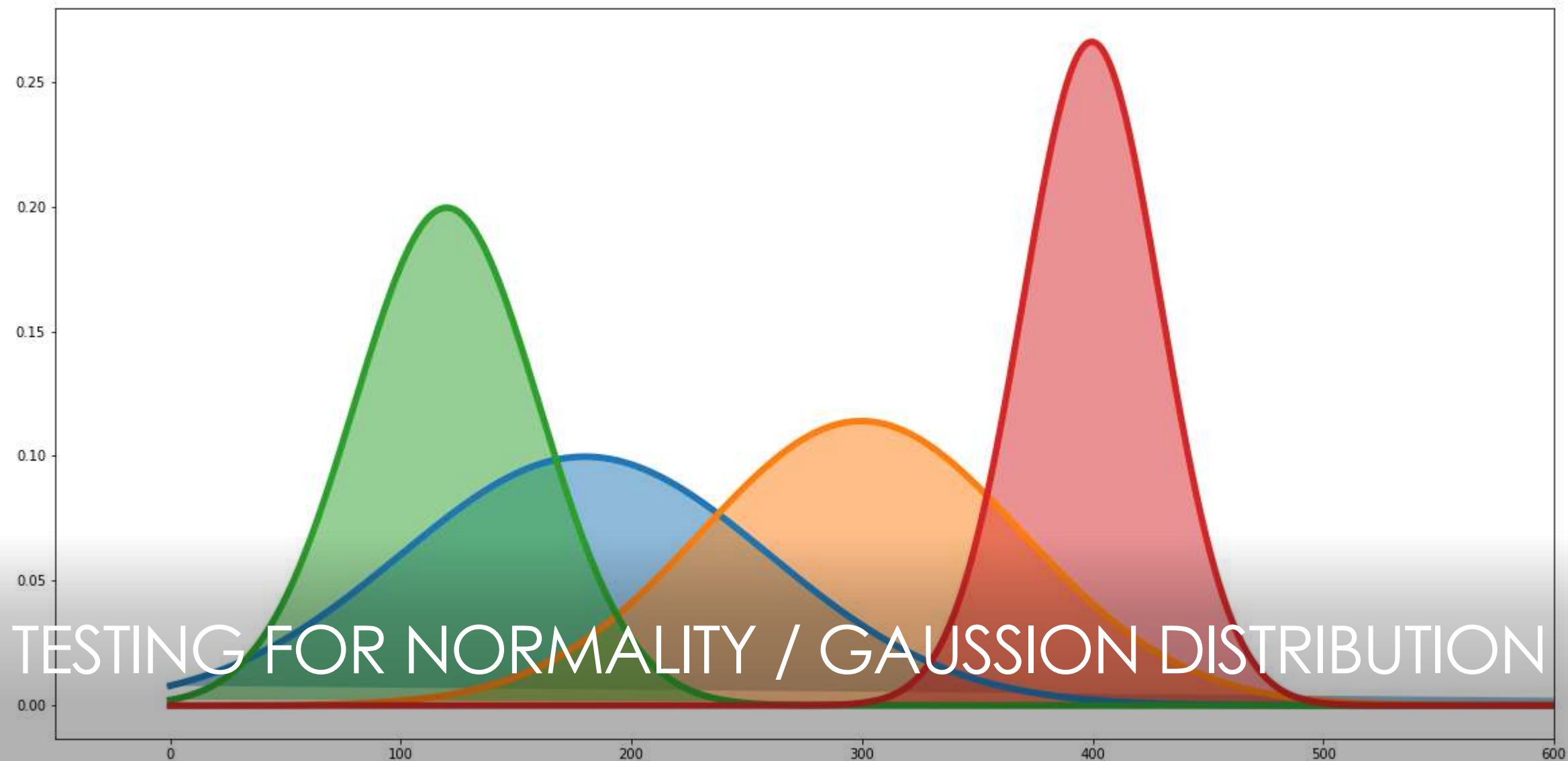
## Example of variables that have high max values

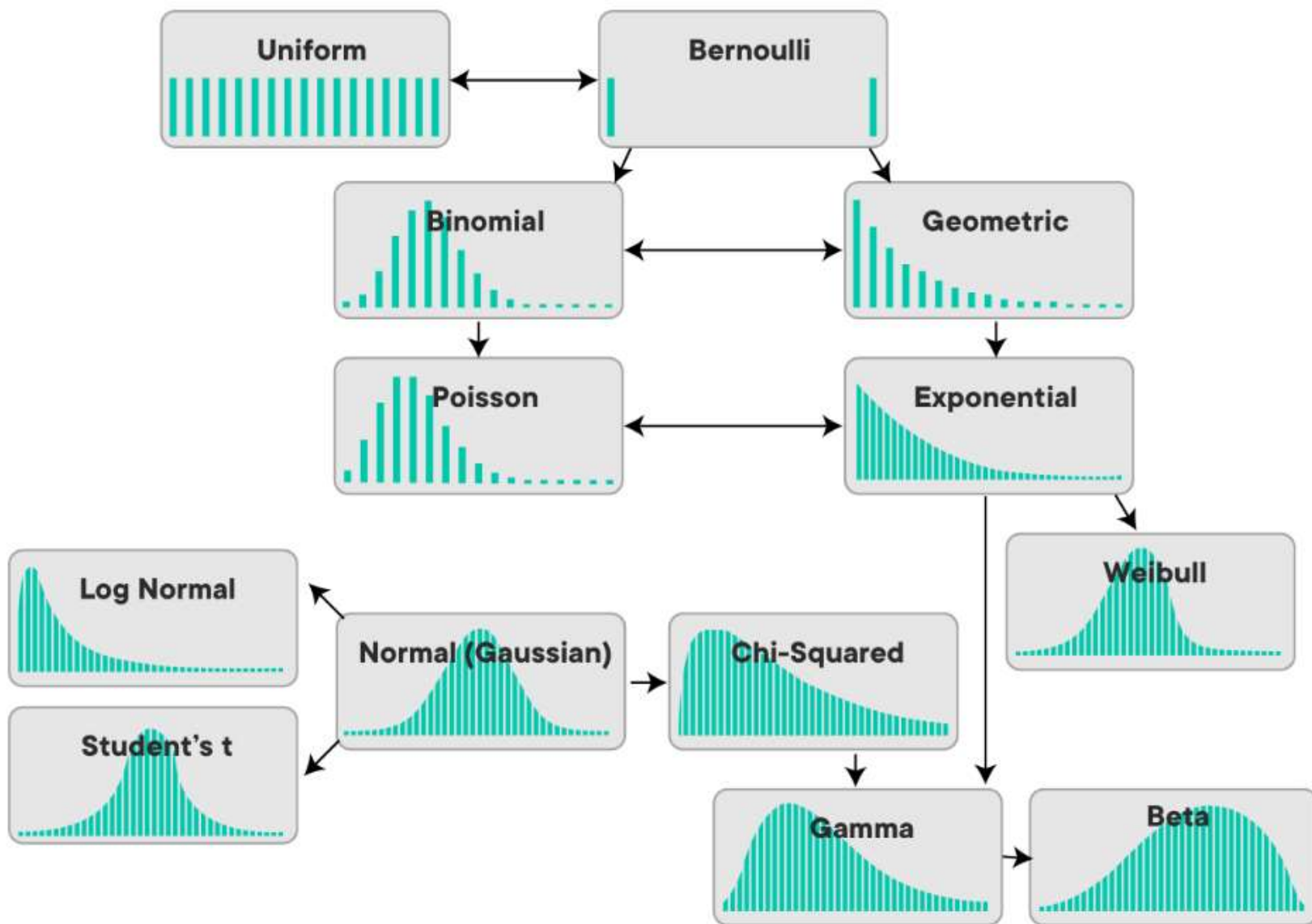


## Example of min outlier value and zero outlier that caused by non-measurable value

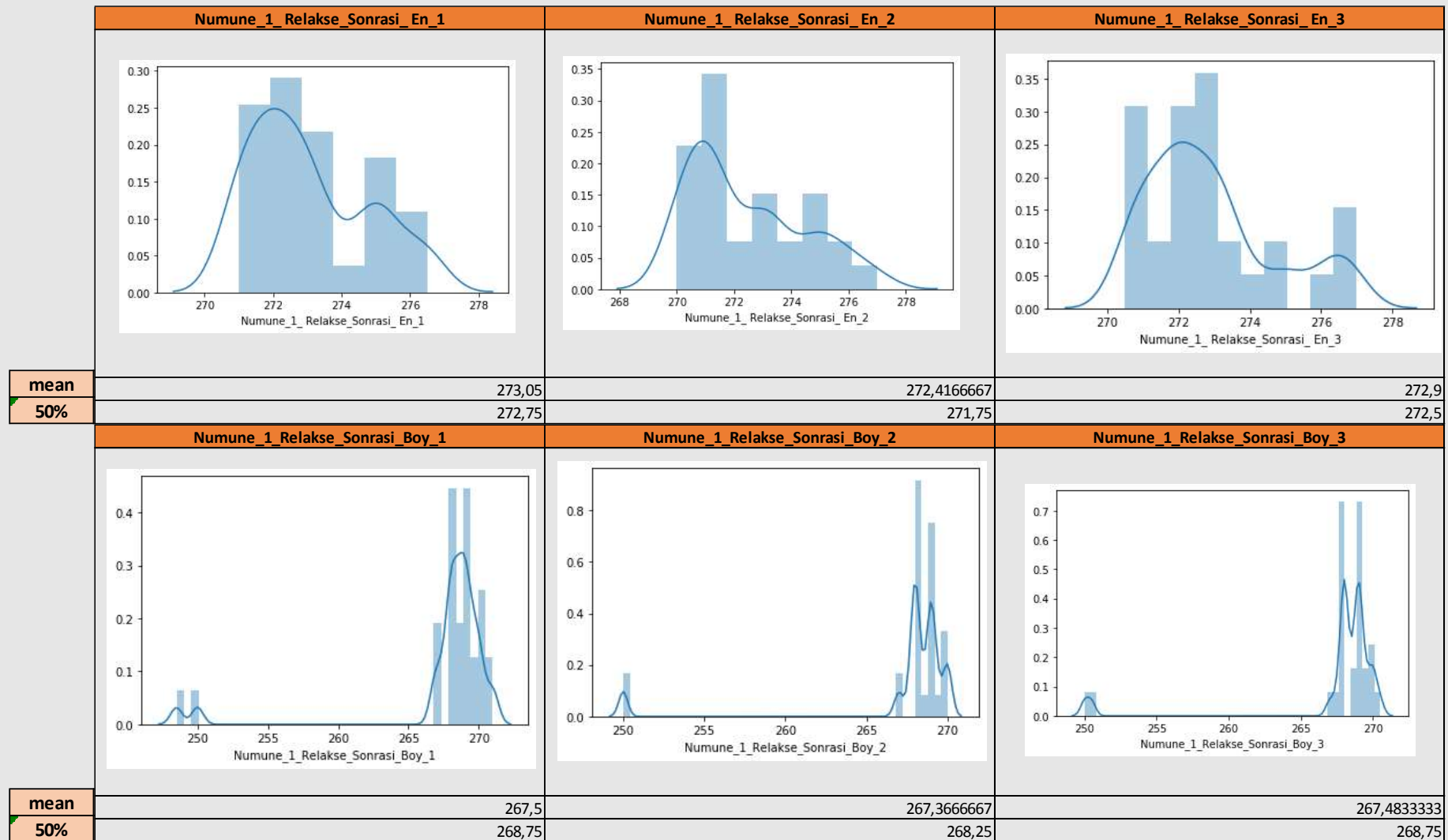




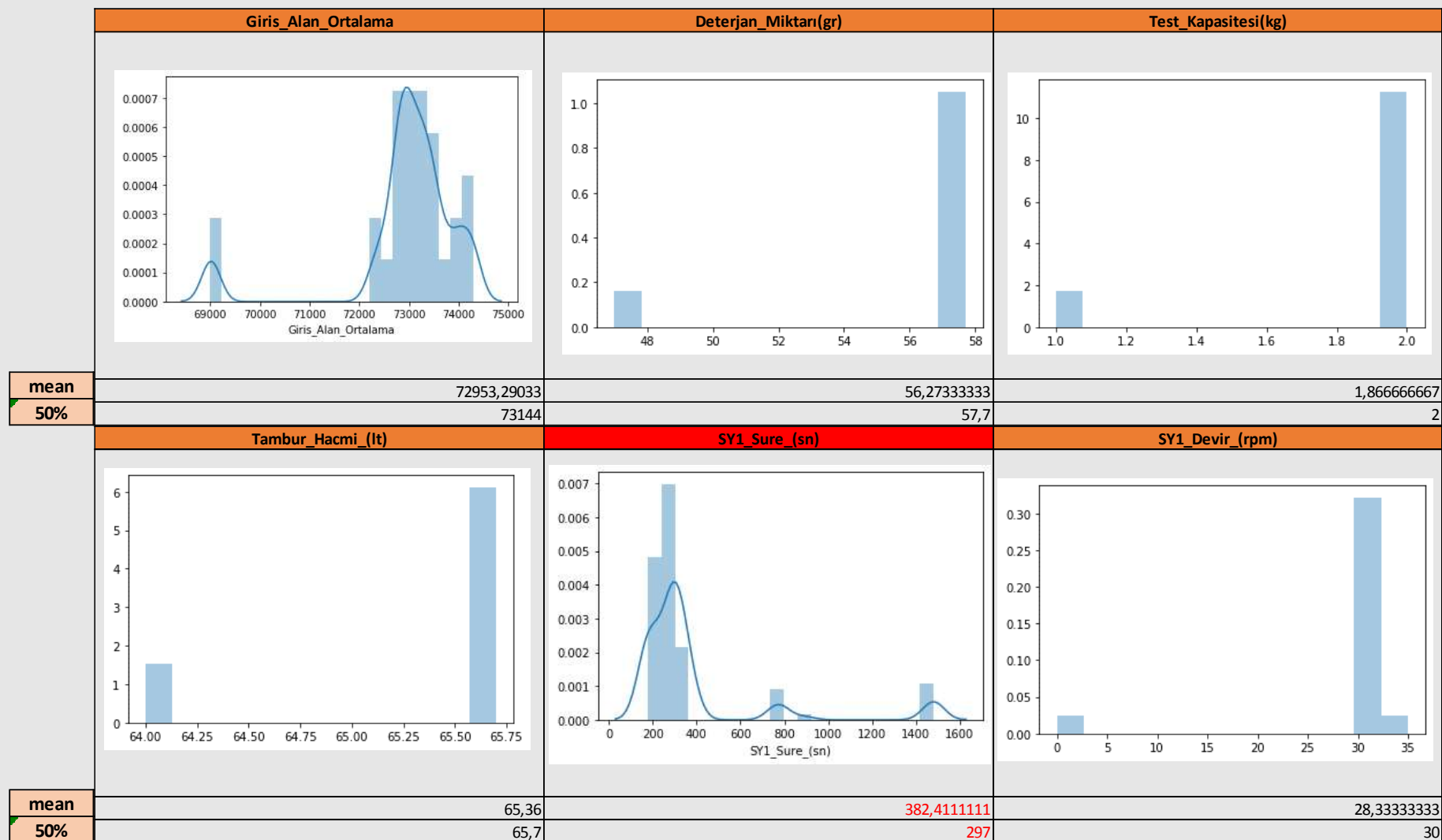




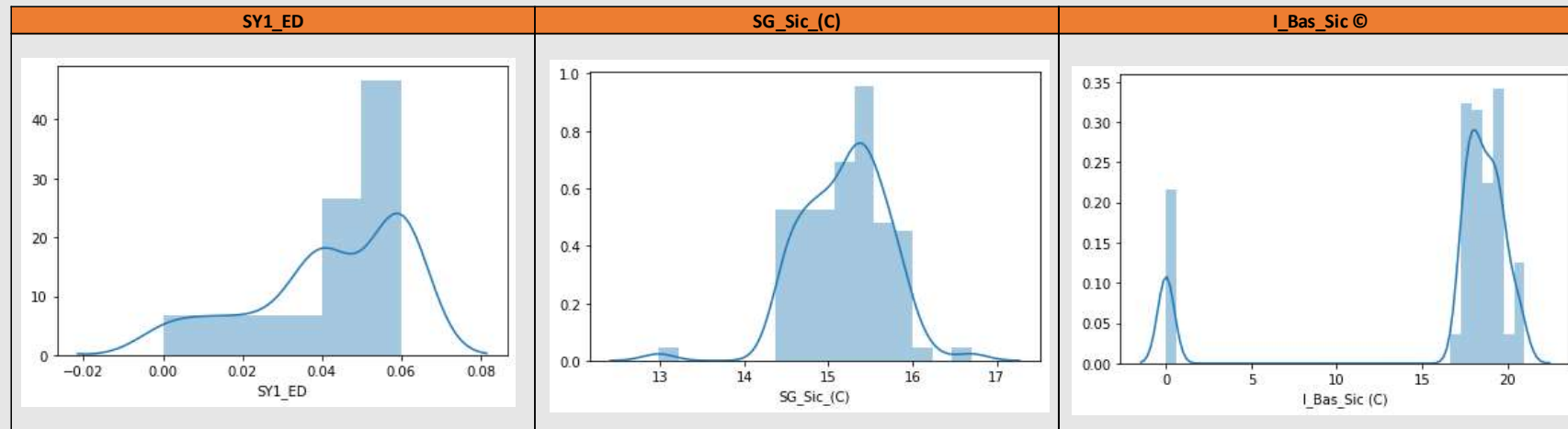
# Visualization data with Histogram whether model variables are normal distributed or not



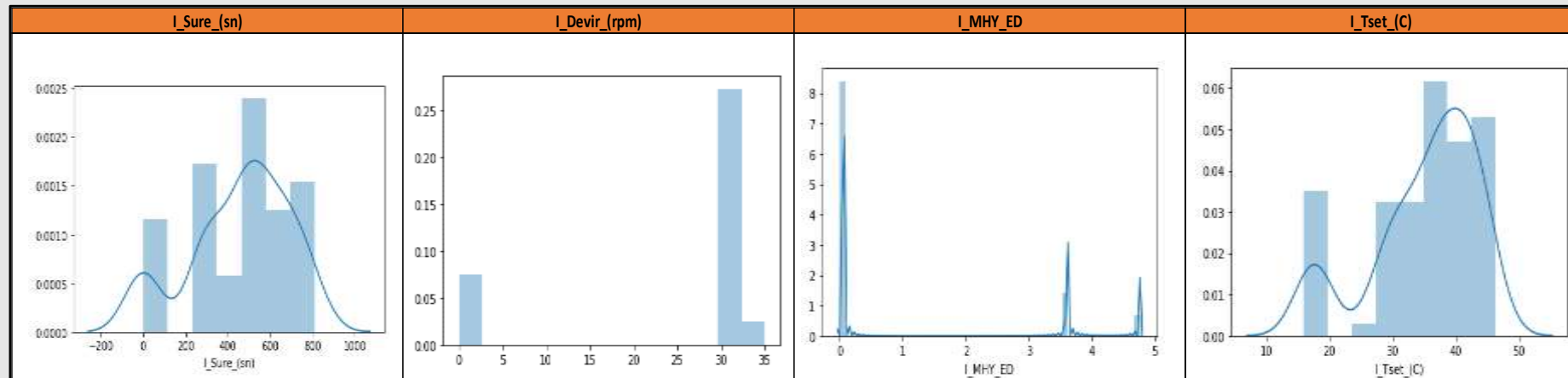
# Visualization data with Histogram whether model variables are normal distributed or not



# Visualization data with Histogram whether model variables are normal distributed or not

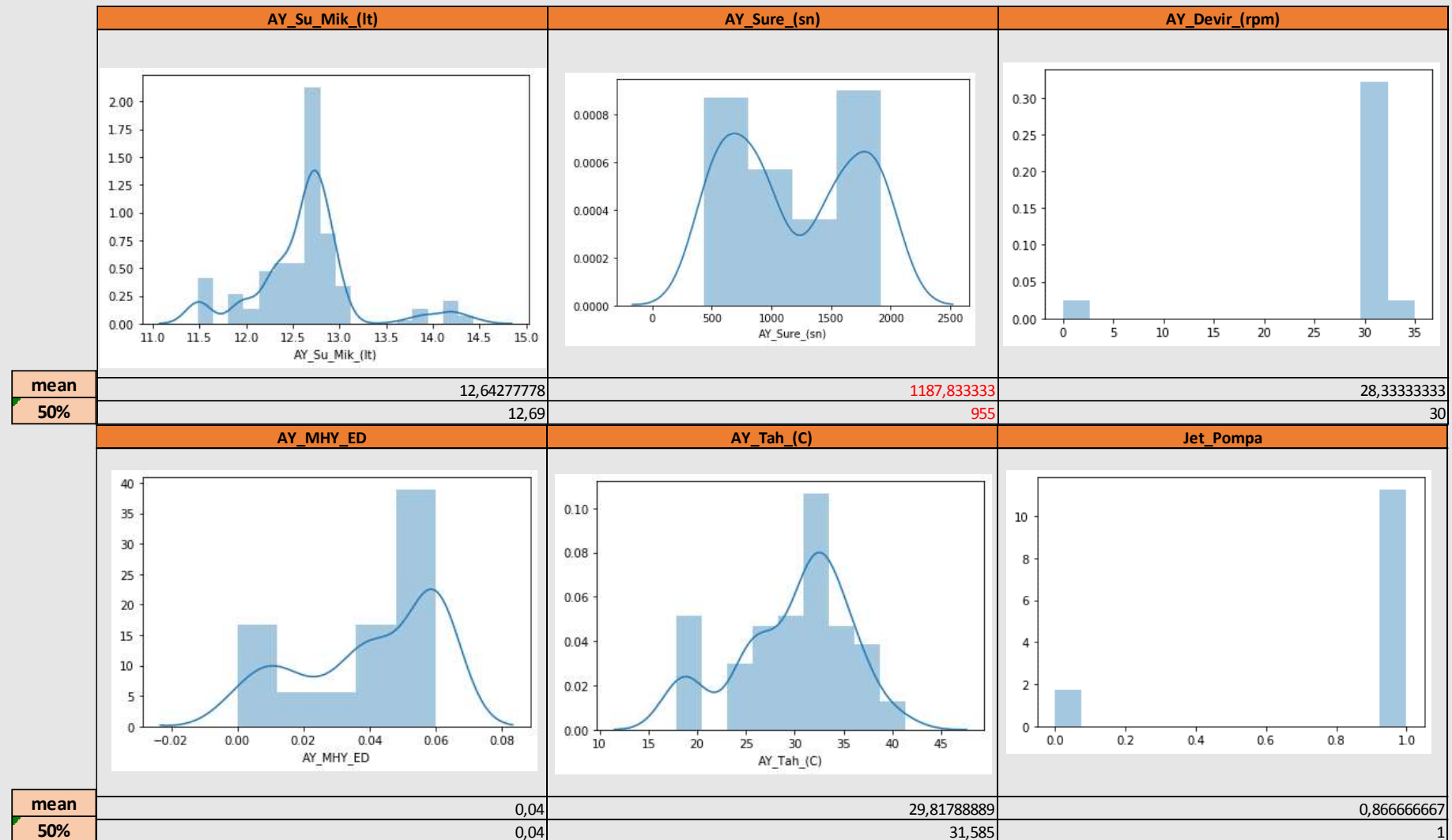


|      |       |             |             |
|------|-------|-------------|-------------|
| mean | 0,042 | 15,19066667 | 16,22316667 |
| 50%  | 0,04  | 15,24       | 18,3        |



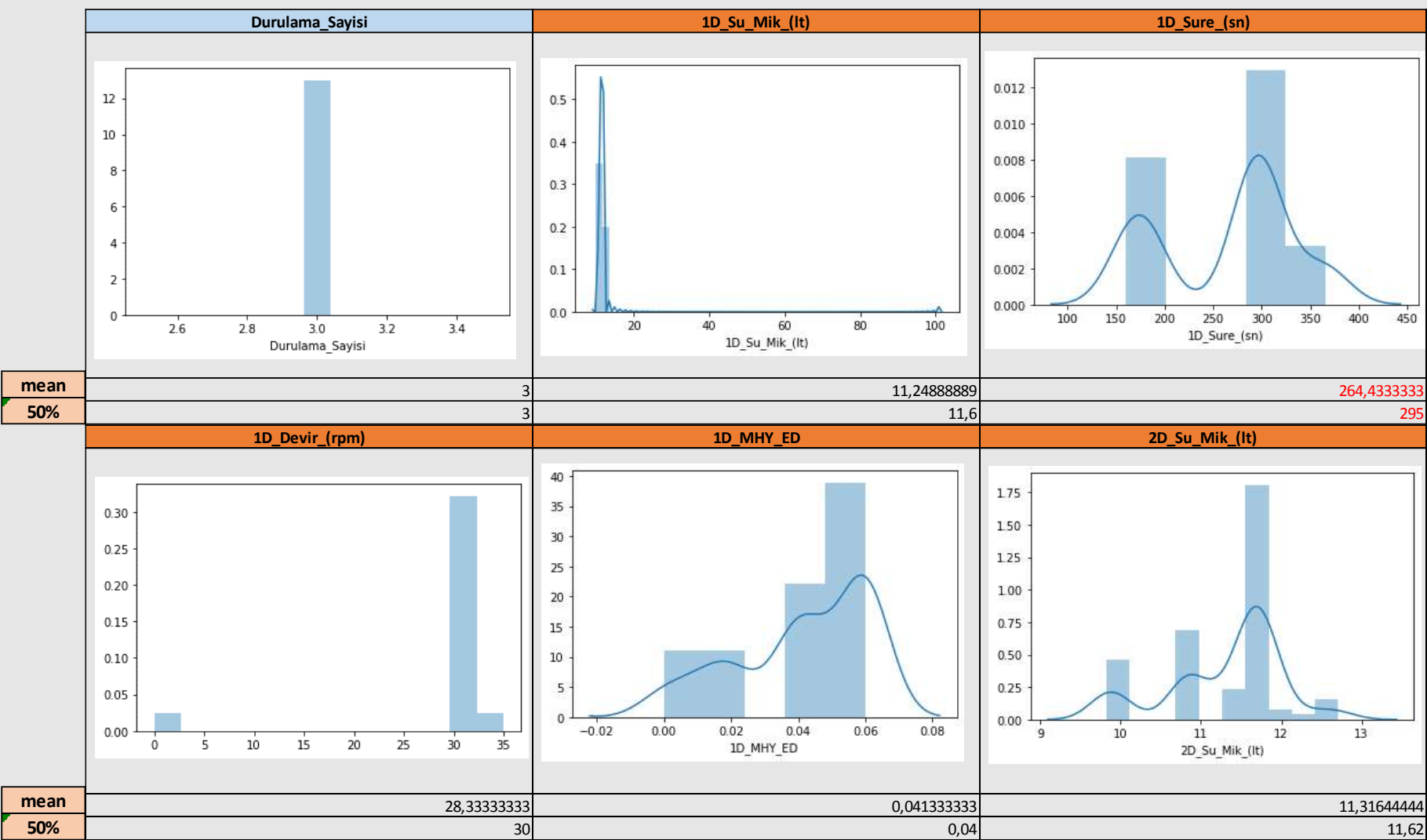
|      |             |             |             |             |
|------|-------------|-------------|-------------|-------------|
| mean | 456,0111111 | 24,33333333 | 0,825333333 | 35,04066667 |
| 50%  | 477         | 30          | 0,06        | 37,71       |

# Visualization data with Histogram whether model variables are normal distributed or not

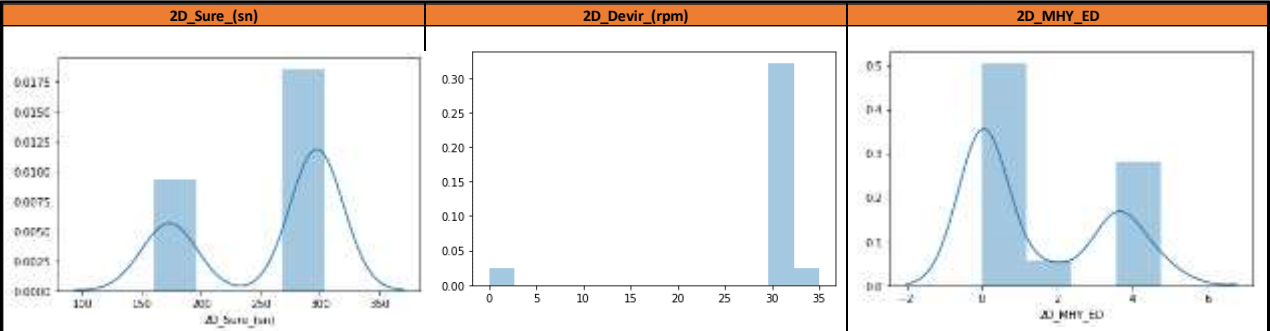




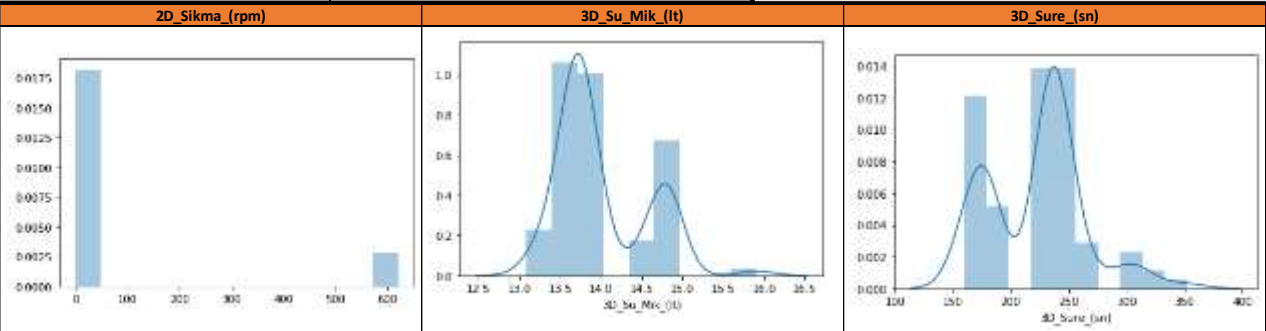
# Visualization data with Histogram whether model variables are normal distributed or not



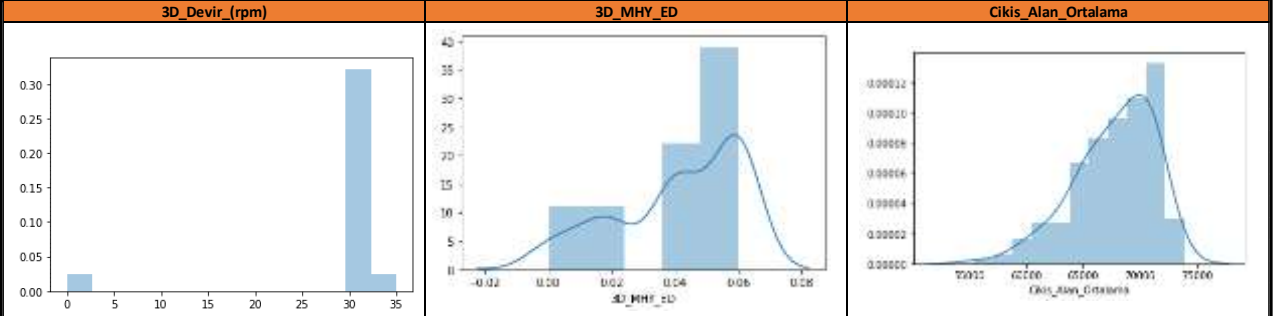
# Visualization data with Histogram whether model variables are normal distributed or not



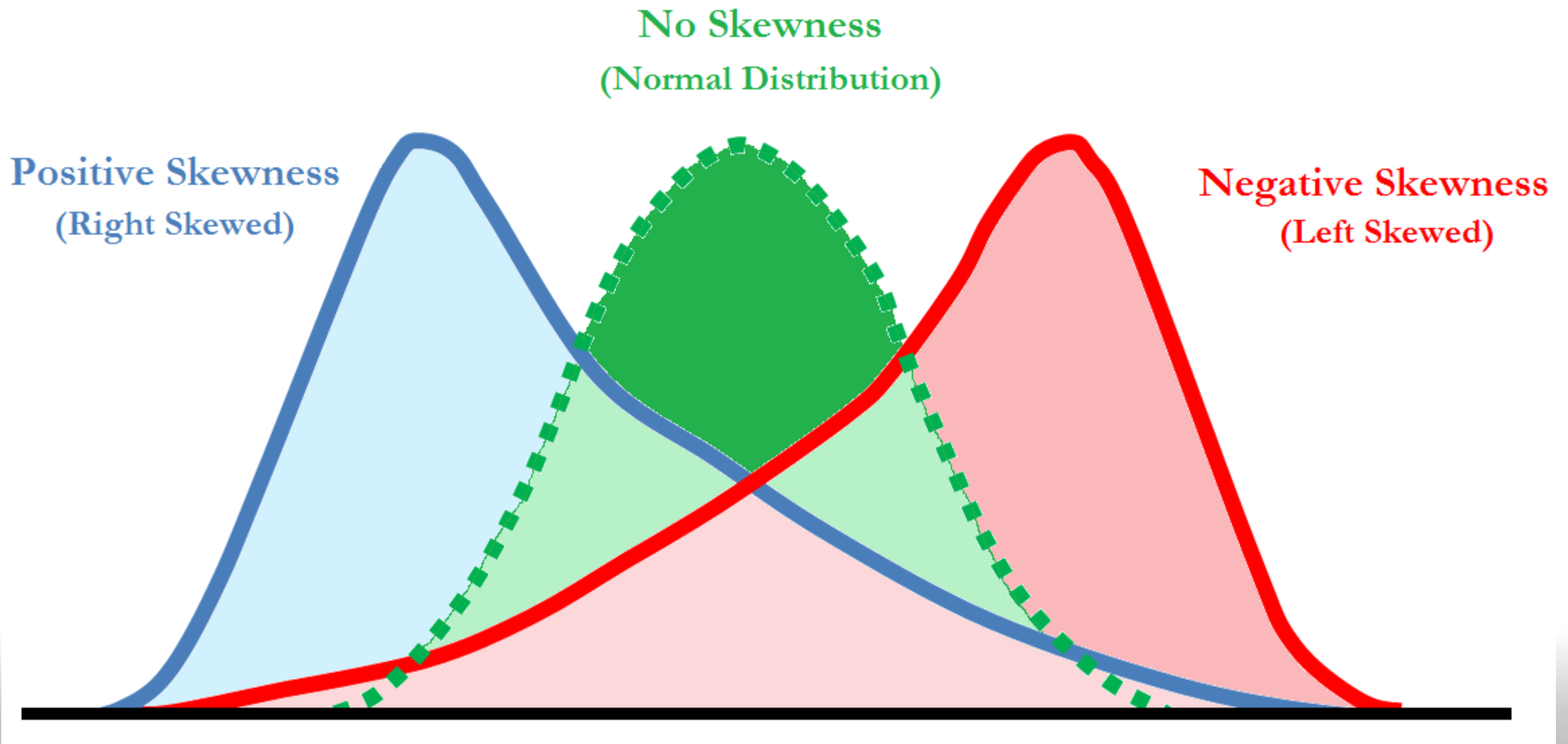
|      |             |             |             |
|------|-------------|-------------|-------------|
| mean | 255,9555556 | 28,33333333 | 1,426666667 |
| 50%  | 295         | 30          | 0,06        |



|      |             |             |        |
|------|-------------|-------------|--------|
| mean | 81,57777778 | 13,99411111 | 222,85 |
| 50%  | 0           | 13,78       | 235    |



|      |             |             |             |
|------|-------------|-------------|-------------|
| mean | 28,33333333 | 0,041333333 | 67735,04272 |
| 50%  | 30          | 0,04        | 68284       |



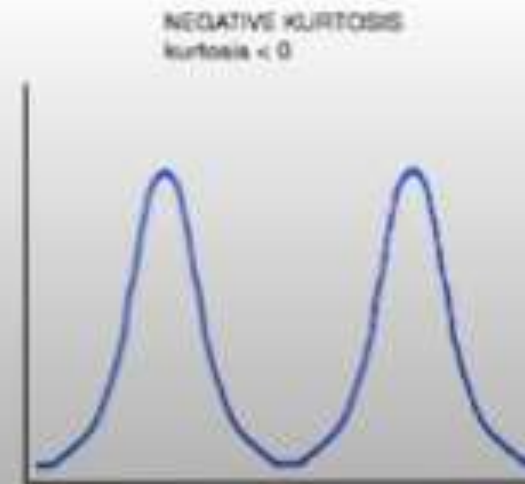
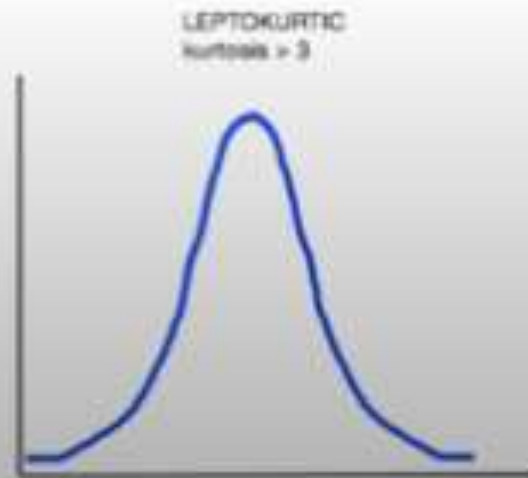
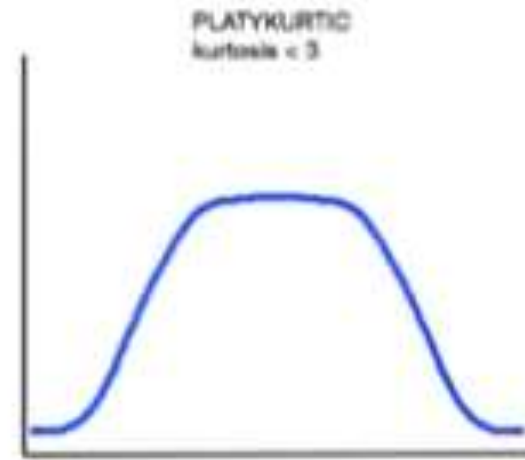
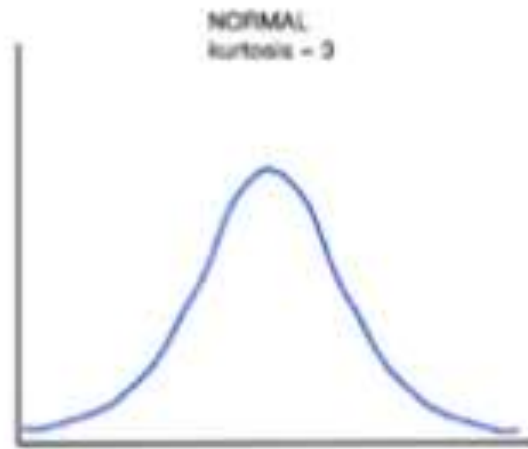
## SKEWNESS ANALYSIS

```
Skewness_values = df.skew()
```

|                                |              |
|--------------------------------|--------------|
| Test_No                        | 0            |
| Numune_1_Relakse_Sonrasi_En_1  | 0,613060857  |
| Numune_1_Relakse_Sonrasi_En_2  | 0,660676599  |
| Numune_1_Relakse_Sonrasi_En_3  | 0,83572226   |
| Numune_1_Relakse_Sonrasi_Boy_1 | -3,260261705 |
| Numune_1_Relakse_Sonrasi_Boy_2 | -3,329913682 |
| Numune_1_Relakse_Sonrasi_Boy_3 | -3,327572638 |
| Giris_Alan_Ortalama            | -2,394629595 |
| Deterjan_Miktari(gr)           | -2,175448351 |
| Test_Kapasitesi(kg)            | -2,175448351 |
| Su_Sertligi                    | 2,076044927  |
| Tambur_Hacmi_(lt)              | -1,512634581 |
| SY1_Sure_(sn)                  | 2,603931062  |
| SY1_Devir_(rpm)                | -3,330688423 |
| SY1_ED                         | -0,713845603 |
| SG_Sic_(C)                     | -0,867887424 |
| I_Bas_Sic (C)                  | -2,082686198 |
| I_Sure_(sn)                    | -0,618799546 |
| I_Devir_(rpm)                  | -1,470632541 |
| I_MHY_ED                       | 1,602676423  |
| I_Tset_(C)                     | -0,945102159 |

|                     |              |
|---------------------|--------------|
| AY_Su_Mik_(lt)      | 0,696366716  |
| AY_Sure_(sn)        | 0,102343503  |
| AY_Devir_(rpm)      | -3,330688423 |
| AY_MHY_ED           | -0,53507349  |
| AY_Tah_(C)          | -0,588976304 |
| Jet_Pompa           | -2,175448351 |
| Durulama_Sayisi     | 0            |
| 1D_Su_Mik_(lt)      | -1,185669638 |
| 1D_Sure_(sn)        | -0,334065516 |
| 1D_Devir_(rpm)      | -3,330688423 |
| 1D_MHY_ED           | -0,626218518 |
| 2D_Su_Mik_(lt)      | -0,990964029 |
| 2D_Sure_(sn)        | -0,726616709 |
| 2D_Devir_(rpm)      | -3,330688423 |
| 2D_MHY_ED           | 0,653548692  |
| 2D_Sikma_(rpm)      | 2,175836646  |
| 3D_Su_Mik_(lt)      | 1,025273445  |
| 3D_Sure_(sn)        | 0,386394596  |
| 3D_Devir_(rpm)      | -3,330688423 |
| 3D_MHY_ED           | -0,621556795 |
| Cikis_Alan_Ortalama | -0,771024791 |

Skewness is 0 in a normal distribution, so the farther away from 0, the more non-normal the distribution



# KURTOSIS ANALYSIS

```
Kurtosisi_values = df.kurtosis()
```

|                                |              |
|--------------------------------|--------------|
| Test_No                        | -1,270438828 |
| Numune_1_Relakse_Sonrasi_En_1  | -0,783263545 |
| Numune_1_Relakse_Sonrasi_En_2  | -0,712381127 |
| Numune_1_Relakse_Sonrasi_En_3  | -0,230475788 |
| Numune_1_Relakse_Sonrasi_Boy_1 | 9,401776493  |
| Numune_1_Relakse_Sonrasi_Boy_2 | 9,642285988  |
| Numune_1_Relakse_Sonrasi_Boy_3 | 9,641744814  |
| Giris_Alan_Ortalama            | 6,035844615  |
| Deterjan_Miktari(gr)           | 2,763155003  |
| Test_Kapasitesi(kg)            | 2,763155003  |
| Su_Sertligi                    | 2,570052941  |
| Tambur_Hacmi(It)               | 0,291174697  |
| SY1_Sure_(sn)                  | 5,886342993  |
| SY1_Devir_(rpm)                | 9,73013713   |
| SY1_ED                         | -0,439179542 |
| SG_Sic_(C)                     | 2,635950529  |
| I_Bas_Sic_(C)                  | 2,54767411   |
| I_Sure_(sn)                    | -0,392994428 |
| I_Devir_(rpm)                  | 0,247312818  |
| I_MHY_ED                       | 0,739203732  |
| I_Tset_(C)                     | -0,045574969 |

|                     |              |
|---------------------|--------------|
| AY_Su_Mik_(It)      | 2,56451849   |
| AY_Sure_(sn)        | -1,619877749 |
| AY_Devir_(rpm)      | 9,73013713   |
| AY_MHY_ED           | -0,994405967 |
| AY_Tah_(C)          | -0,337445911 |
| Jet_Pompa           | 2,763155003  |
| Durulama_Sayisi     | 0            |
| 1D_Su_Mik_(It)      | 0,142578778  |
| 1D_Sure_(sn)        | -1,263010795 |
| 1D_Devir_(rpm)      | 9,73013713   |
| 1D_MHY_ED           | -0,771316786 |
| 2D_Su_Mik_(It)      | 0,078394437  |
| 2D_Sure_(sn)        | -1,453543148 |
| 2D_Devir_(rpm)      | 9,73013713   |
| 2D_MHY_ED           | -1,363625826 |
| 2D_Sikma_(rpm)      | 2,76564041   |
| 3D_Su_Mik_(It)      | 0,354449722  |
| 3D_Sure_(sn)        | 0,266542043  |
| 3D_Devir_(rpm)      | 9,73013713   |
| 3D_MHY_ED           | -0,766140788 |
| Cikis_Alan_Ortalama | 0,308871767  |

The value is often compared to the kurtosis of the normal distribution, which is equal to 3. If the kurtosis is greater than 3, then the dataset has heavier tails than a normal distribution (more in the tails). If the kurtosis is less than 3, then the dataset has lighter tails than a normal distribution (less in the tails).



# Detecting Outliers

“Sometimes outliers are bad data, and should be excluded, such as typos. Sometimes they are Wayne Gretzky or Michael Jordan, and should be kept.”

◦ According to **IQR**, (not considering zero (0) values)

- ❖ Numune\_I\_Relakse\_Sonrasi\_En\_3
- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_1
- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_2
- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_3
- ❖ Giris\_Alan\_Ortalama
- ❖ Deterjan\_Miktari(gr)
- ❖ Test\_Kapasitesi(kg)
- ❖ Su\_Sertligi
- ❖ Tambur\_Hacmi(It)
- ❖ SYI\_Sure(sn)
- ❖ SYI\_Devir(rpm)
- ❖ SG\_Sic(C)
- ❖ I\_Bas\_Sic(C) ( bcz of zero values)
- ❖ I\_Sure(sn)
- ❖ AY\_Su\_Mik(It)
- ❖ AY\_Devir(rpm)
- ❖ Jet\_Pompa ( bcz of zero values)
- ❖ ID\_Devir(rpm)
- ❖ 2D\_Devir(rpm)
- ❖ 2D\_Sikma(rpm)\*
- ❖ 3D\_Sure(sn) -> (2 outliers)
- ❖ 3D\_Devir(rpm)
- ❖ 3D\_MHY\_ED
- ❖ Cikis\_Alan\_Ortalama -> (2 outliers)

An outlier is a point which falls more than 1.5 times the interquartile range above the third (75%) quartile or below the first quartile (25%).

◦ According to **Z score**,

- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_1
- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_2
- ❖ Numune\_I\_Relakse\_Sonrasi\_Boy\_3
- ❖ Giris\_Alan\_Ortalama
- ❖ SYI\_Sure(sn)
- ❖ SYI\_Devir(rpm)
- ❖ SG\_Sic(C)
- ❖ AY\_Su\_Mik(It)
- ❖ AY\_Devir(rpm)
- ❖ ID\_Devir(rpm)
- ❖ 2D\_Devir(rpm)
- ❖ 3D\_Su\_Mik(It)
- ❖ 3D\_Sure(sn)
- ❖ 3D\_Devir(rpm)
- ❖ Cikis\_Alan\_Ortalama

variables have values more than threshold which is 3.

**Formula for Z score =**  
(Observation -  
Mean)/Standard Deviation

```
##### Detecting Outliers- Uç noktalarrrrr #####
df.shape
(180, 42)

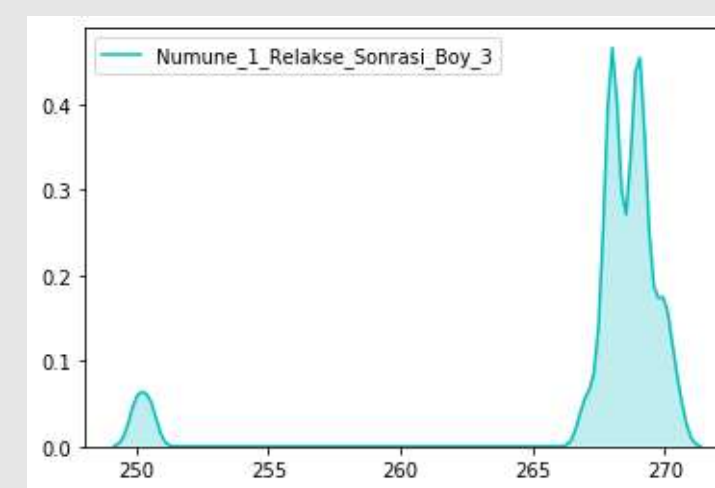
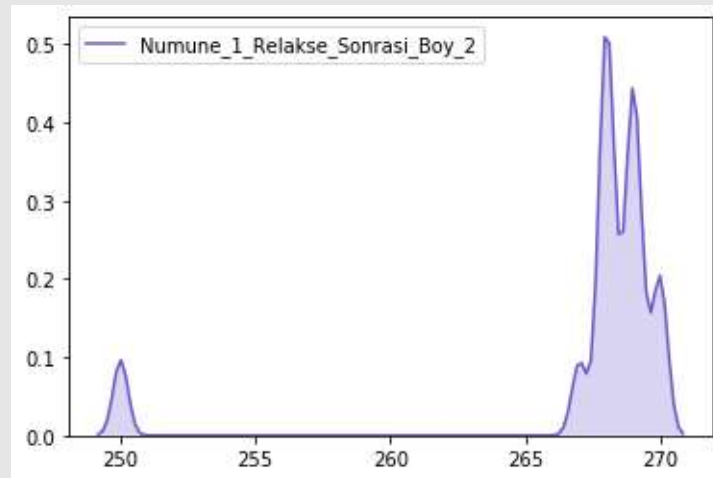
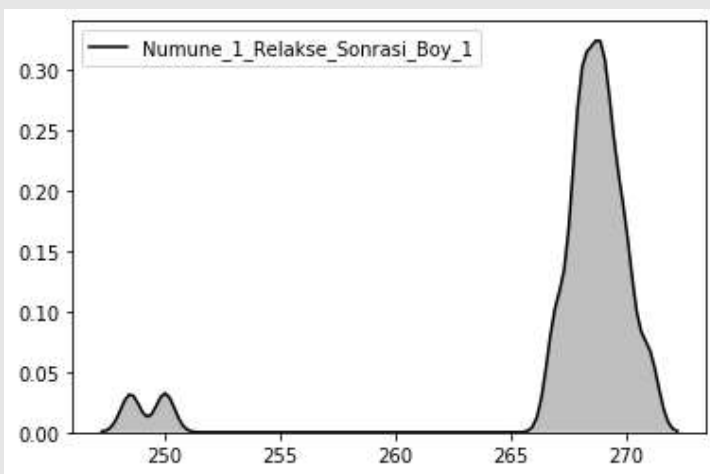
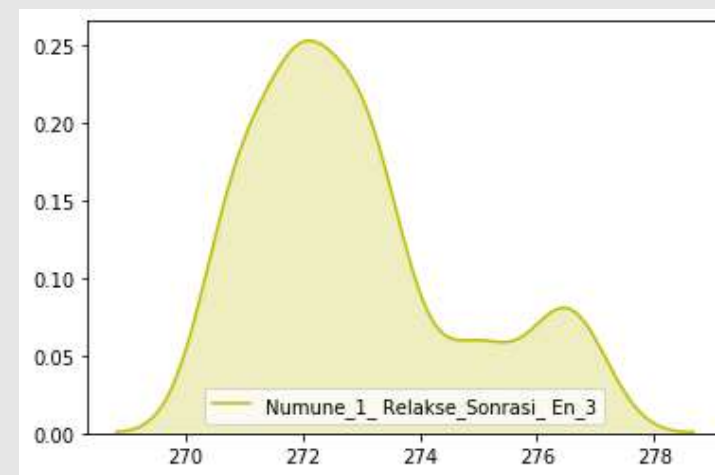
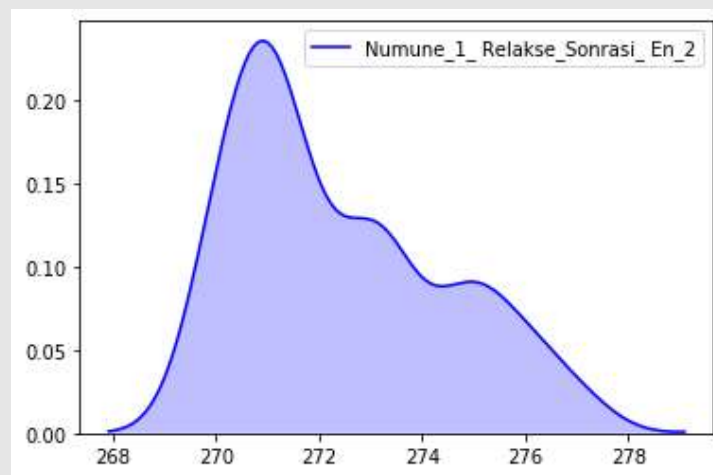
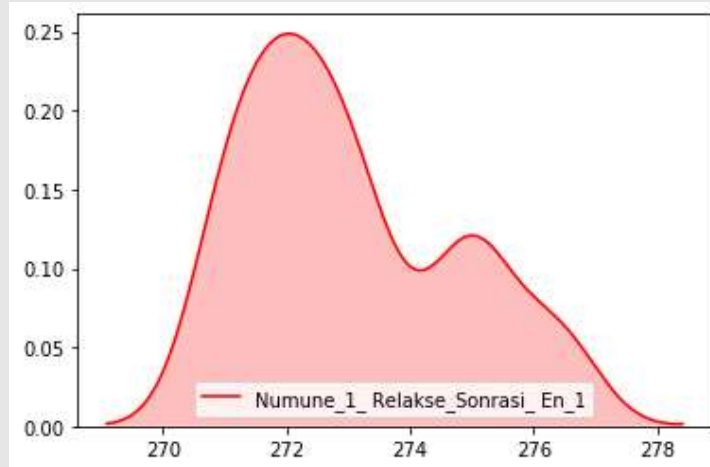
Q1 = df.quantile(0.25)
Q3 = df.quantile(0.75)
IQR = Q3-Q1
print(IQR)

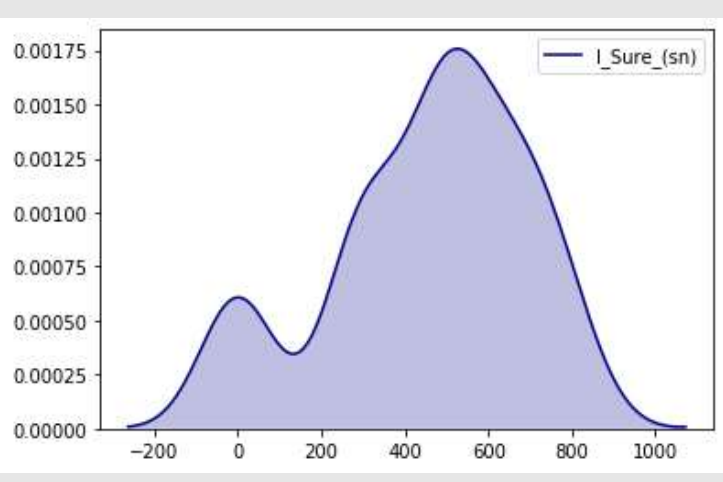
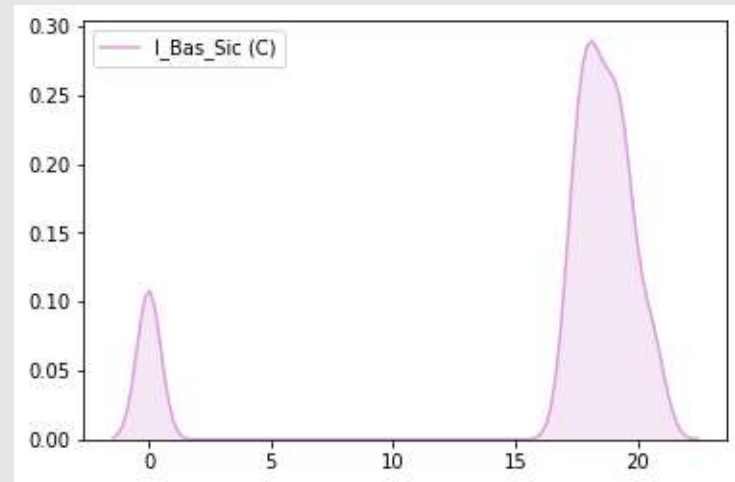
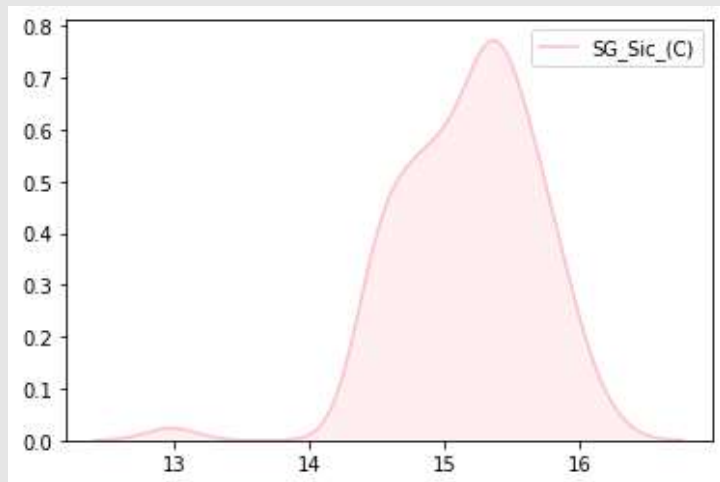
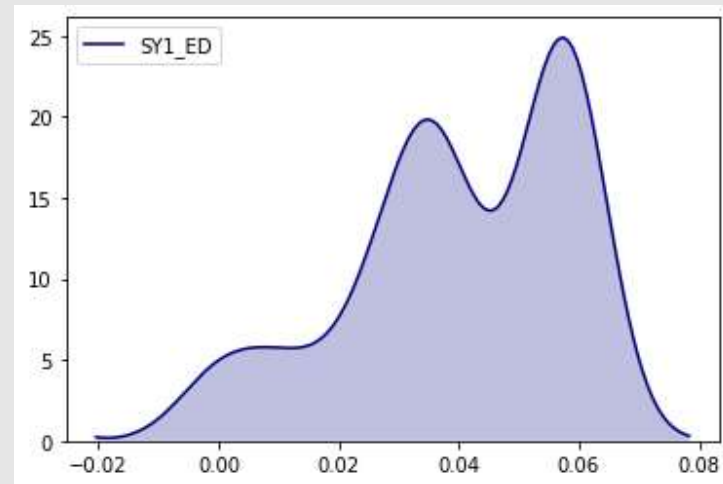
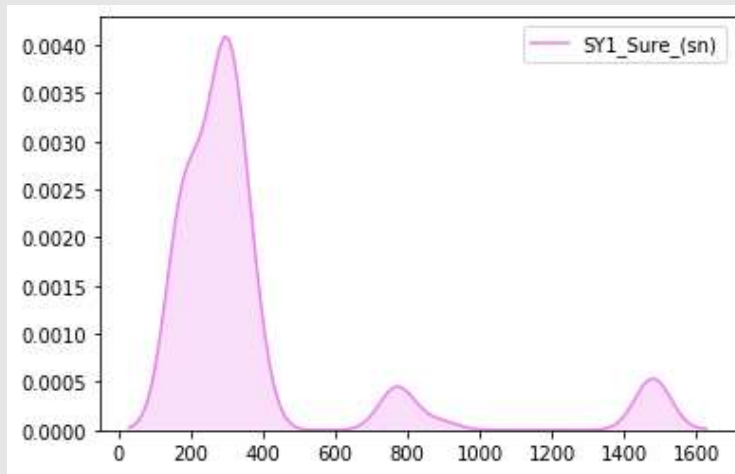
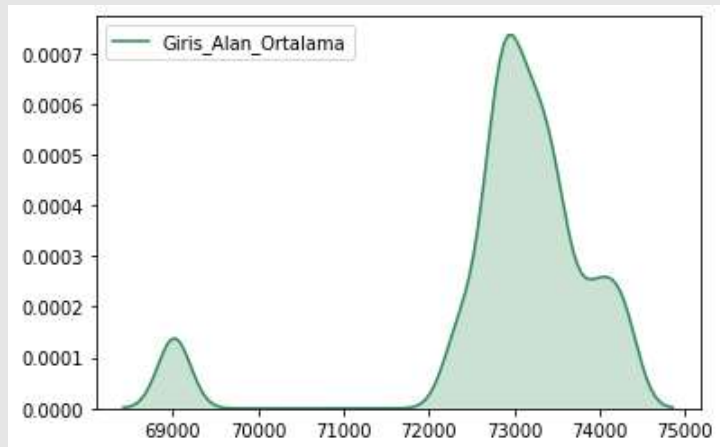
df = df[~((df < (Q1-1.5*IQR)) |(df > (Q3+1.5*IQR))).any(axis=1)]
df.shape
(48, 42) #132 rows are outliers.....

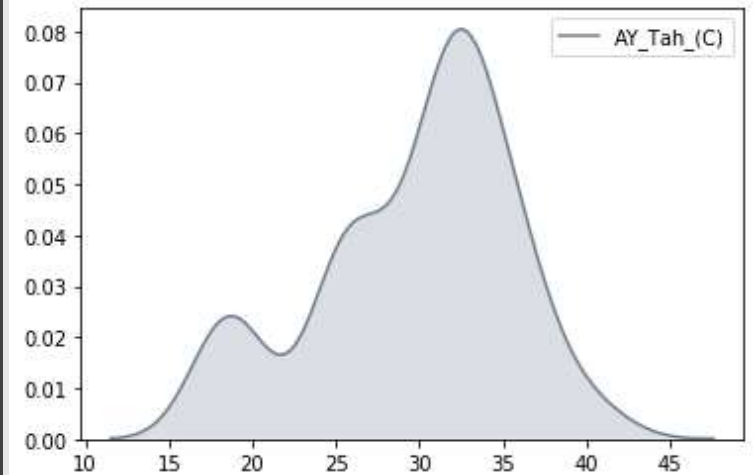
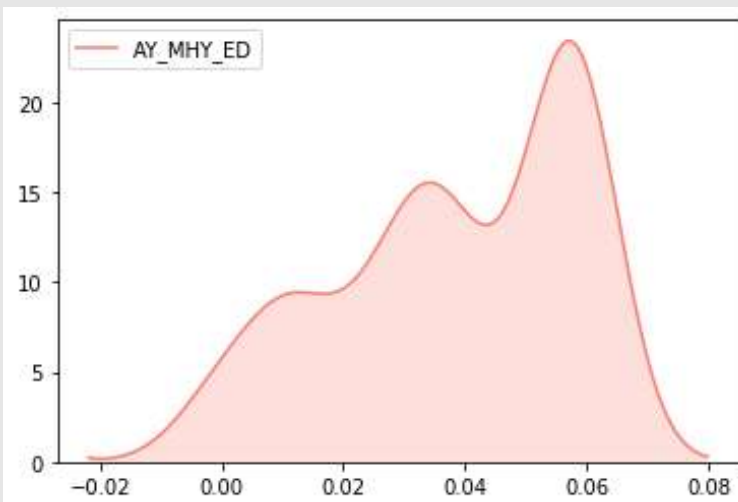
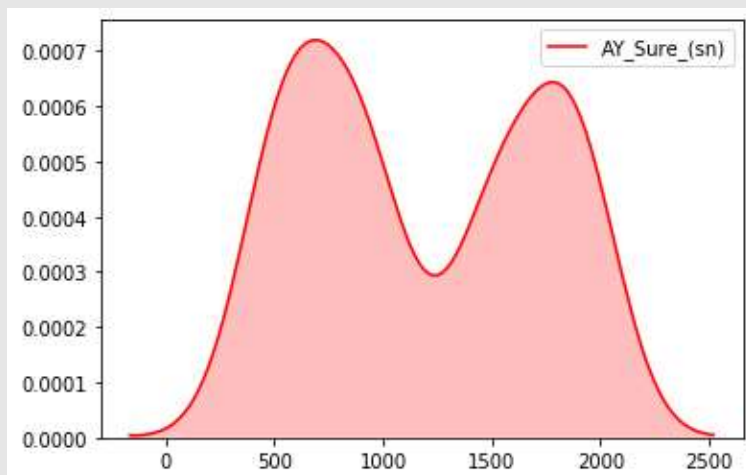
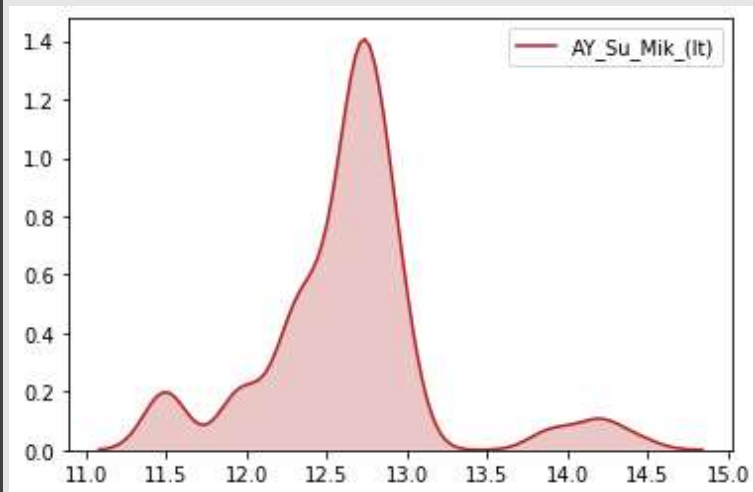
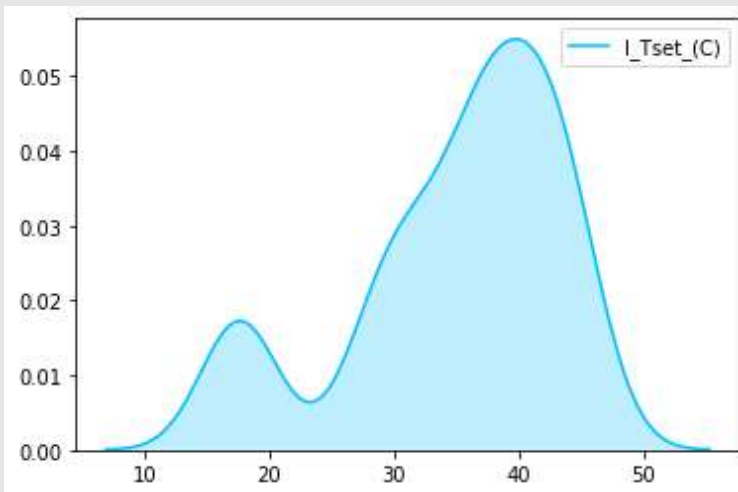
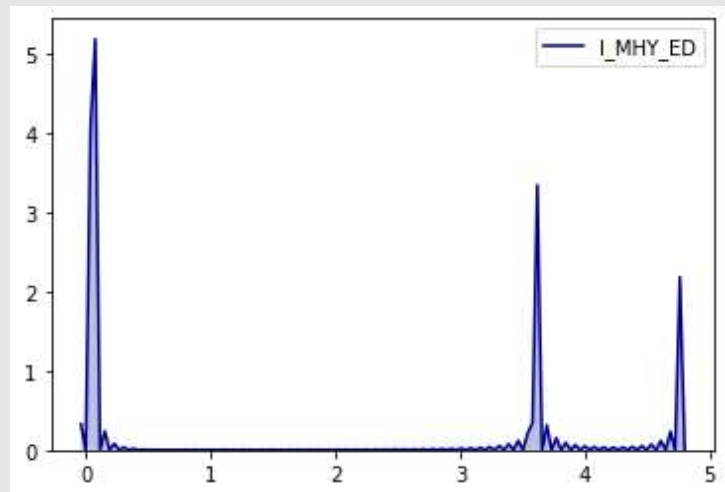
#z-score-outliers

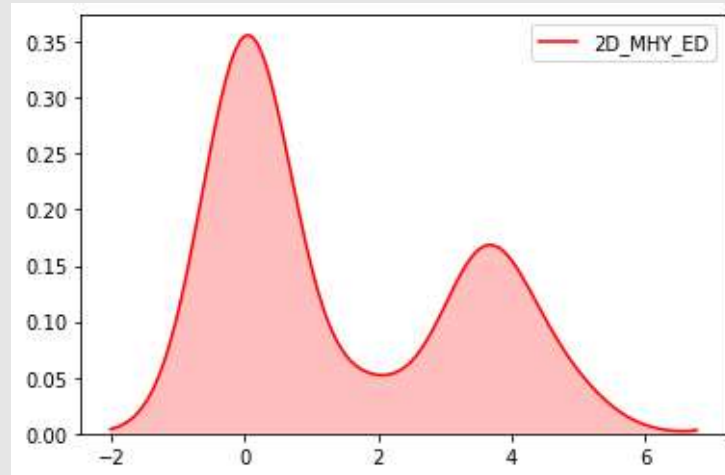
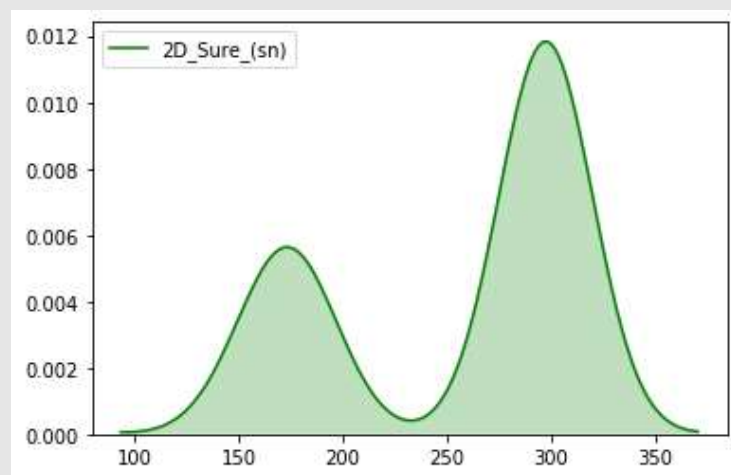
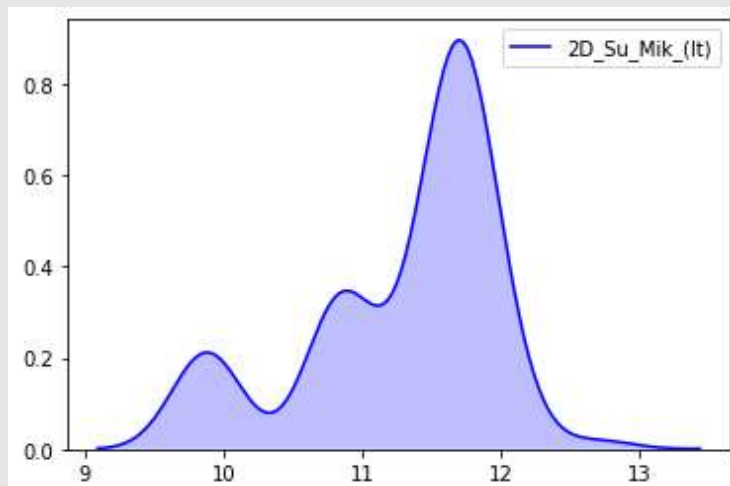
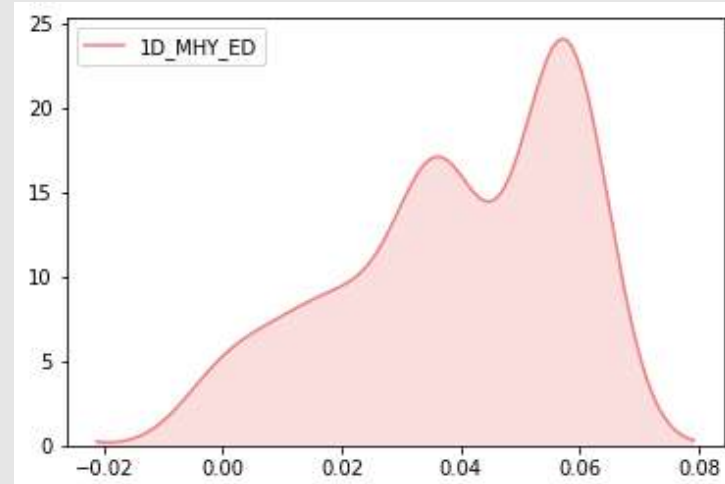
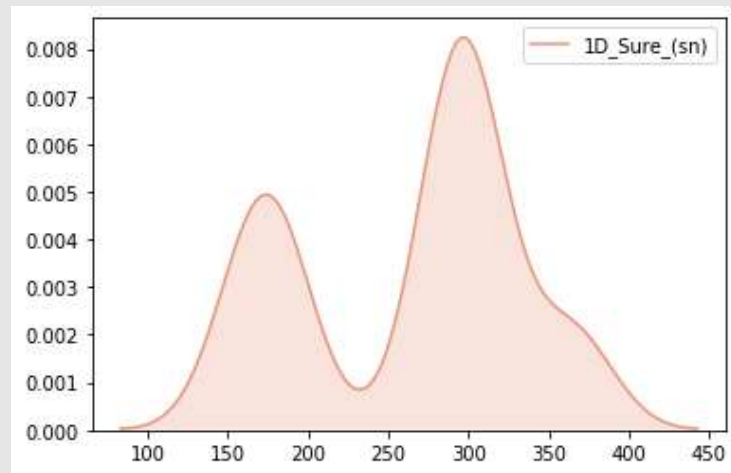
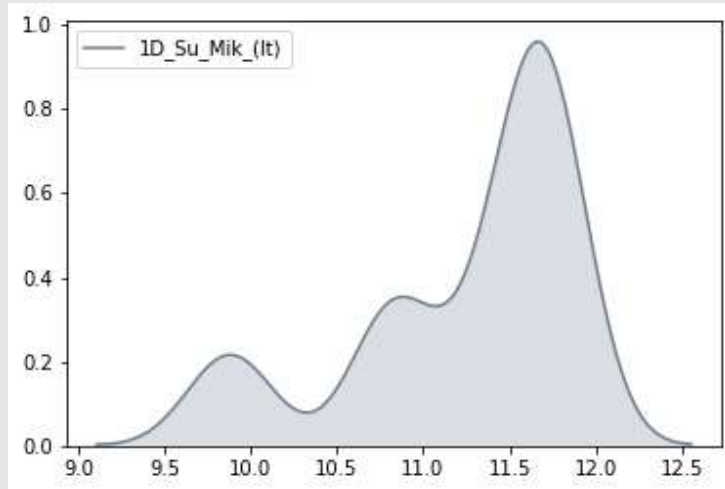
from scipy import stats
import numpy as np
z = np.abs(stats.zscore(df))
print(z)
z_score = pd.DataFrame(data = z, index= range(180), columns = df.columns)

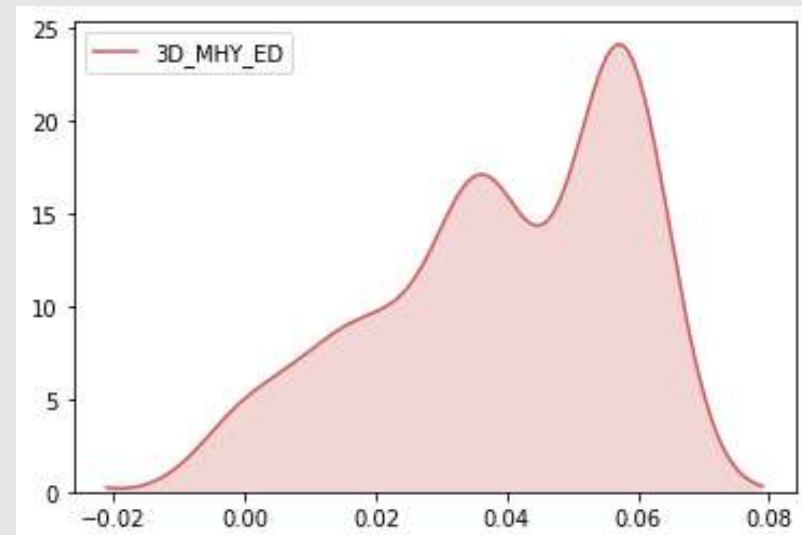
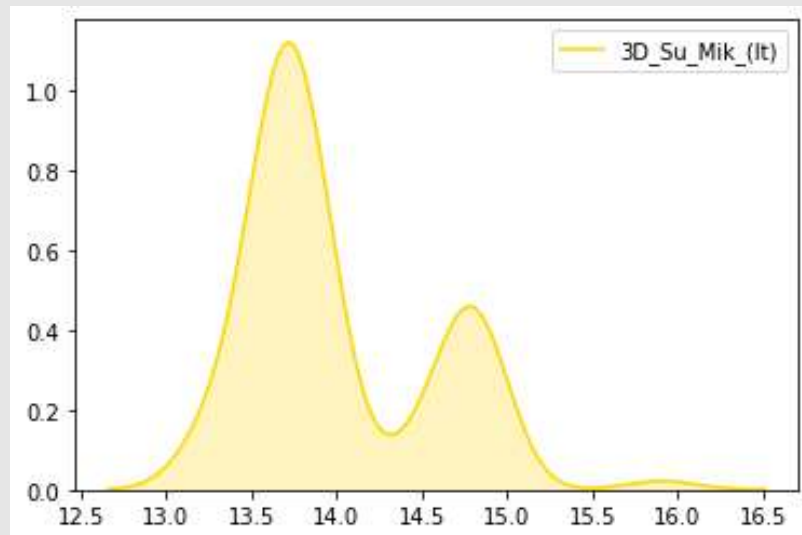
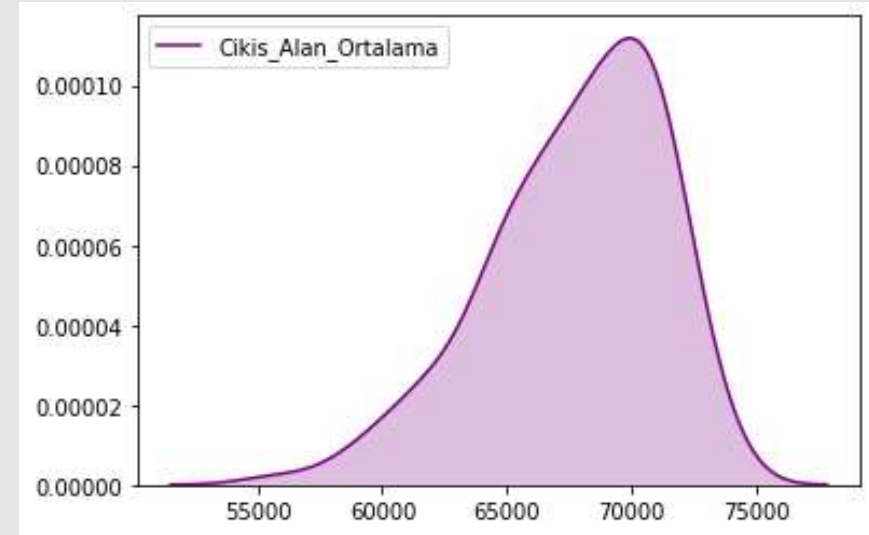
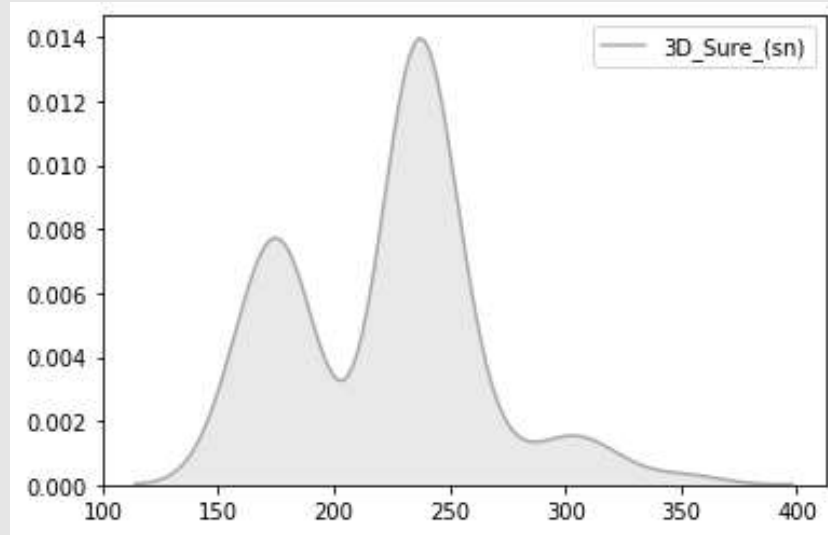
z_score.to_excel('C:\\Users\\DSI\\Desktop\\Z_score_outliers.xlsx')
threshold = 3
print(np.where(z > 3))
# print(z[18][21])
```











# Variables that do not have a density

- |                        |                     |
|------------------------|---------------------|
| ◦ Deterjan_Miktari(gr) | Test_Kapasitesi(kg) |
| ◦ Su_Sertligi          | Tambur_Hacmi_(lt)   |
| ◦ SYI_Devir_(rpm)      | I_Devir_(rpm)       |
| ◦ AY_Devir_(rpm)       | Jet_Pompa           |
| ◦ ID_Devir_(rpm)       | 2D_Devir_(rpm)      |
| ◦ 2D_Sikma_(rpm)       | 3D_Devir_(rpm)      |









# PEARSON VS. SPEARMAN'S RANK CORRELATION ANALYSIS

Pearson  $r$  correlation is a parametric correlation statistic to measure the degree of the relationship between linearly related variables.

The Spearman's rank coefficient of correlation is a nonparametric measure of rank correlation.



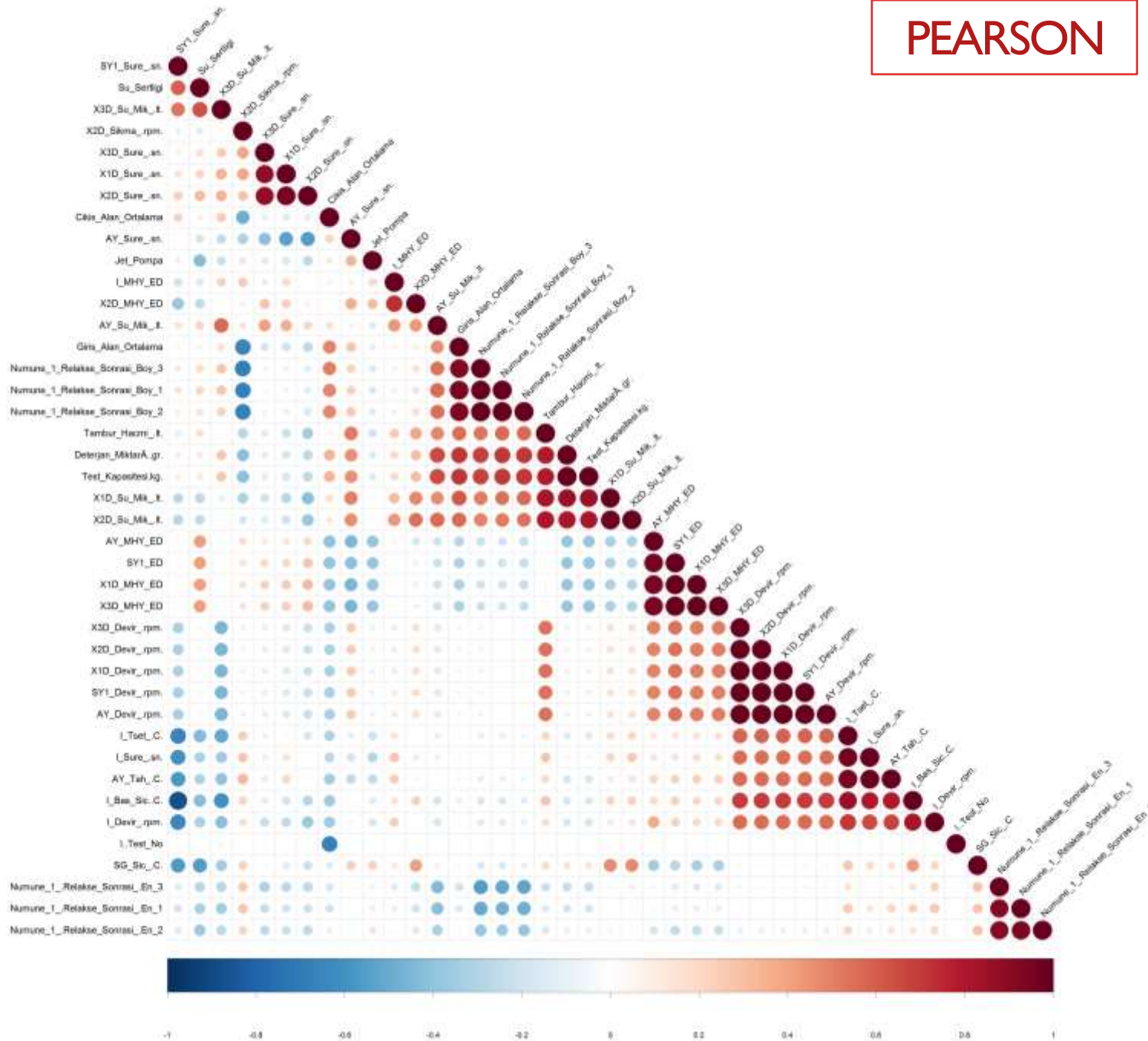
| Size of Correlation         | Interpretation                            |
|-----------------------------|---|
| .90 to 1.00 (–.90 to –1.00) | Very high positive (negative) correlation |
| .70 to .90 (–.70 to –.90)   | High positive (negative) correlation      |
| .50 to .70 (–.50 to –.70)   | Moderate positive (negative) correlation  |
| .30 to .50 (–.30 to –.50)   | Low positive (negative) correlation       |
| .00 to .30 (.00 to –.30)    | negligible correlation                    |

| Feature\Response | Continuous            | Categorical |
|------------------|-----------------------|-------------|
| Continuous       | Pearson's Correlation | LDA         |
| Categorical      | Anova                 | Chi-Square  |

To be able to calculate pearson's correlation, the condition of normality and linearity should be provided for each variable.

When variables do not have normal distribution, Spearman Rank correlation coefficient is preferred.

PEARSON



| DEĞER | Sol_Korelasyon                 | to | Üst_Korelasyon                 | Çıkarılacak                    |
|-------|--------------------------------|----|--------------------------------|--------------------------------|
| 1,00  | Deterjan_Miktari(gr)           | => | Test_Kapasitesi(kg)            | Deterjan_Miktari(gr)           |
| 1,00  | SY1_Devir_(rpm)                | => | AY_Devir_(rpm)                 | AY_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 1D_Devir_(rpm)                 | 1D_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 2D_Devir_(rpm)                 | 2D_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 3D_Devir_(rpm)                 | 3D_Devir_(rpm)                 |
| 1,00  | AY_Devir_(rpm)                 | => | 1D_Devir_(rpm)                 | *                              |
| 1,00  | AY_Devir_(rpm)                 | => | 2D_Devir_(rpm)                 | *                              |
| 1,00  | AY_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 | *                              |
| 1,00  | 1D_Devir_(rpm)                 | => | 2D_Devir_(rpm)                 | *                              |
| 1,00  | 1D_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 | *                              |
| 1,00  | 2D_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 | *                              |
| 1,00  | 1D_MHY_ED                      | => | 3D_MHY_ED                      | 3D_MHY_ED                      |
| 0,99  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Numune_1_Relakse_Sonrasi_Boy_3 | Numune_1_Relakse_Sonrasi_Boy_1 |
| 0,99  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Numune_1_Relakse_Sonrasi_Boy_2 | *                              |
| 0,99  | Numune_1_Relakse_Sonrasi_Boy_2 | => | Numune_1_Relakse_Sonrasi_Boy_3 | Numune_1_Relakse_Sonrasi_Boy_2 |
| 0,99  | SY1_ED                         | => | 1D_MHY_ED                      | SY1_ED                         |
| 0,99  | SY1_ED                         | => | 3D_MHY_ED                      | *                              |
| 0,98  | I_Sure_(sn)                    | => | AY_Tah_(C)                     | I_Sure_(sn)                    |
| 0,97  | 1D_Su_Mik_(lt)                 | => | 2D_Su_Mik_(lt)                 | 2D_Su_Mik_(lt)                 |
| 0,95  | SY1_ED                         | => | AY_MHY_ED                      | *                              |
| 0,95  | 1D_Sure_(sn)                   | => | 2D_Sure_(sn)                   | 2D_Sure_(sn)                   |
| 0,95  | I_Sure_(sn)                    | => | I_Tset_(C)                     | I_Sure_(sn)                    |
| 0,94  | I_Tset_(C)                     | => | AY_Tah_(C)                     | I_Tset_(C)                     |
| 0,94  | AY_MHY_ED                      | => | 3D_MHY_ED                      | *                              |
| 0,94  | AY_MHY_ED                      | => | 1D_MHY_ED                      | 1D_MHY_ED                      |
| 0,94  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Giris_Alan_Ortalama            | *                              |
| 0,93  | Numune_1_Relakse_Sonrasi_En_1  | => | Numune_1_Relakse_Sonrasi_En_2  | Numune_1_Relakse_Sonrasi_En_2  |
| 0,93  | Numune_1_Relakse_Sonrasi_Boy_2 | => | Giris_Alan_Ortalama            | *                              |
| 0,92  | Numune_1_Relakse_Sonrasi_Boy_3 | => | Giris_Alan_Ortalama            | Numune_1_Relakse_Sonrasi_Boy_3 |
| 0,91  | Numune_1_Relakse_Sonrasi_En_2  | => | Numune_1_Relakse_Sonrasi_En_3  | *                              |
| 0,91  | Numune_1_Relakse_Sonrasi_En_1  | => | Numune_1_Relakse_Sonrasi_En_3  | Numune_1_Relakse_Sonrasi_En_3  |
| 0,88  | 1D_Sure_(sn)                   | => | 3D_Sure_(sn)                   | 3D_Sure_(sn)                   |
| 0,87  | 2D_Sure_(sn)                   | => | 3D_Sure_(sn)                   | *                              |
| 0,85  | I_Bas_Sic(C)                   | => | I_Tset_(C)                     | *                              |
| 0,85  | Test_Kapasitesi(kg)            | => | 1D_Su_Mik_(lt)                 | 1D_Su_Mik_(lt)                 |
| 0,85  | Deterjan_Miktari(gr)           | => | 1D_Su_Mik_(lt)                 | *                              |
| 0,82  | Test_Kapasitesi(kg)            | => | 2D_Su_Mik_(lt)                 | *                              |
| 0,82  | Deterjan_Miktari(gr)           | => | 2D_Su_Mik_(lt)                 | *                              |
| 0,82  | Tambur_Hacmi_(lt)              | => | 1D_Su_Mik_(lt)                 | *                              |
| 0,81  | I_Bas_Sic(C)                   | => | I_Devir_(rpm)                  | I_Devir_(rpm) ???              |
| 0,80  | Tambur_Hacmi_(lt)              | => | 2D_Su_Mik_(lt)                 | *                              |
| 0,79  | I_Bas_Sic(C)                   | => | I_Sure_(sn)                    | *                              |
| 0,79  | I_Bas_Sic(C)                   | => | AY_Tah_(C)                     | AY_Tah_(C)                     |
| 0,78  | Test_Kapasitesi(kg)            | => | Tambur_Hacmi_(lt)              | Tambur_Hacmi_(lt)              |
| 0,78  | Deterjan_Miktari(gr)           | => | Tambur_Hacmi_(lt)              | *                              |
| 0,73  | I_MHY_ED                       | => | 2D_MHY_ED                      | 2D_MHY_ED                      |
| 0,71  | Giris_Alan_Ortalama            | => | Deterjan_Miktari(gr)           |                                |
| 0,71  | Giris_Alan_Ortalama            | => | Test_Kapasitesi(kg)            |                                |
| -0,88 | SY1_Sure_(sn)                  | => | I_Bas_Sic(C)                   | SY1_Sure_(sn)                  |

|                                |                               |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
|--------------------------------|-------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|
| Sol Başlıkları Brleştir        | Test_No                       | 1,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,00  | 0,03  | 0,05  | -0,02 | 0,00  | 0,00  | 0,02  | 0,02  | 0,00  | 0,00  | 0,00  | -0,02 | 0,00  | 0,00  | -0,02 | 0,00  | -0,01 | 0,01  | 0,00  | 0,00  | -0,01 | -0,03 | 0,00  | 0,00  | 0,00  | -0,03 | -0,04 | 0,00  | 0,00 | -0,72 |
|                                | Numune_1_Relakse_Sonrasi_En_1 | 1,00  | 0,94  | 0,86  | 0,08  | 0,08  | -0,01 | 0,51  | -0,07 | -0,07 | -0,36 | -0,03 | 0,05  | 0,13  | -0,14 | 0,28  | 0,36  | 0,12  | 0,31  | 0,07  | 0,28  | -0,40 | 0,09  | 0,13  | -0,10 | 0,20  | 0,11  | 0,31  | -0,19 | 0,13  | -0,13 | 0,21  | -0,21 | 0,13  | -0,18 | 0,18  | -0,34 | -0,24 | 0,13  | -0,13 | -0,13 |      |       |
|                                | Numune_1_Relakse_Sonrasi_En_2 | 1,00  | 0,85  | 0,02  | -0,05 | -0,09 | 0,51  | -0,06 | -0,06 | -0,40 | -0,08 | 0,12  | 0,05  | -0,22 | 0,28  | 0,32  | 0,14  | 0,23  | 0,06  | 0,30  | -0,35 | 0,10  | 0,05  | -0,19 | 0,21  | 0,18  | 0,31  | -0,17 | 0,05  | -0,21 | 0,25  | -0,21 | 0,05  | -0,18 | 0,20  | -0,27 | -0,23 | 0,05  | -0,21 | -0,06 |       |      |       |
|                                | Numune_1_Relakse_Sonrasi_En_3 | 1,00  | 0,00  | 0,01  | -0,10 | 0,45  | -0,11 | -0,11 | -0,30 | -0,07 | -0,01 | 0,06  | -0,13 | 0,31  | 0,31  | -0,03 | 0,29  | 0,04  | 0,17  | -0,45 | 0,19  | 0,06  | -0,07 | 0,07  | 0,10  | 0,28  | -0,35 | 0,06  | -0,14 | 0,14  | -0,37 | 0,06  | -0,20 | 0,11  | -0,32 | -0,38 | 0,06  | -0,14 | -0,11 |       |       |      |       |
| Numune_1_Relakse_Sonrasi_Boy_1 | 1,00                          | 0,83  | 0,86  | 0,74  | 0,41  | 0,41  | 0,41  | 0,39  | 0,29  | 0,01  | 0,10  | -0,30 | -0,17 | 0,18  | -0,13 | -0,11 | 0,01  | 0,36  | -0,18 | 0,01  | 0,12  | 0,07  | -0,25 | 0,17  | 0,02  | 0,01  | 0,11  | 0,14  | 0,05  | 0,01  | -0,13 | -0,34 | 0,41  | 0,05  | 0,01  | 0,11  | 0,18  |       |       |       |       |      |       |
| Numune_1_Relakse_Sonrasi_Boy_2 | 1,00                          | 0,74  | 0,70  | 0,46  | 0,46  | 0,24  | 0,46  | 0,08  | 0,07  | -0,06 | -0,07 | -0,02 | 0,24  | 0,03  | -0,10 | 0,08  | 0,30  | -0,05 | 0,07  | -0,03 | 0,11  | -0,28 | 0,27  | -0,03 | 0,07  | -0,06 | 0,24  | -0,01 | 0,07  | -0,08 | -0,31 | 0,23  | 0,00  | 0,07  | -0,06 | 0,15  |       |       |       |       |       |      |       |
| Numune_1_Relakse_Sonrasi_Boy_3 | 1,00                          | 0,65  | 0,35  | 0,35  | 0,42  | 0,29  | 0,12  | -0,03 | 0,16  | -0,35 | -0,18 | 0,07  | -0,15 | -0,12 | -0,11 | 0,32  | -0,28 | -0,03 | 0,15  | -0,07 | -0,29 | 0,06  | -0,04 | -0,03 | 0,17  | 0,01  | 0,01  | -0,03 | -0,12 | -0,40 | 0,37  | 0,01  | -0,03 | 0,17  | 0,21  |       |       |       |       |       |       |      |       |
| Giris_Alan_Ortalama            | 1,00                          | 0,48  | 0,48  | 0,00  | 0,39  | 0,15  | 0,04  | -0,25 | 0,00  | 0,03  | 0,18  | 0,12  | -0,12 | 0,14  | 0,10  | 0,09  | 0,04  | -0,20 | 0,07  | -0,10 | 0,44  | -0,28 | 0,04  | -0,24 | 0,34  | -0,26 | 0,04  | -0,22 | -0,39 | 0,16  | -0,27 | 0,04  | -0,24 | 0,24  |       |       |       |       |       |       |       |      |       |
| Deterjan_Miktari(gr)           | 1,00                          | 1,00  | 0,07  | 0,78  | -0,02 | 0,00  | -0,43 | 0,16  | -0,27 | 0,05  | -0,12 | -0,19 | -0,11 | 0,59  | 0,44  | 0,00  | -0,42 | -0,17 | -0,15 | 0,59  | -0,17 | 0,00  | -0,43 | 0,59  | -0,12 | 0,00  | 0,14  | -0,38 | 0,34  | -0,15 | 0,00  | -0,43 | 0,28  |       |       |       |       |       |       |       |       |      |       |
| Test_Kapasitesi(kg)            | 1,00                          | 0,07  | 0,78  | -0,02 | 0,00  | -0,43 | 0,16  | -0,27 | 0,05  | -0,12 | -0,19 | -0,11 | 0,59  | 0,44  | 0,00  | -0,42 | -0,17 | -0,15 | 0,59  | -0,17 | 0,00  | -0,43 | 0,59  | -0,12 | 0,00  | 0,14  | -0,38 | 0,34  | -0,15 | 0,00  | -0,43 | 0,28  |       |       |       |       |       |       |       |       |       |      |       |
| Su_Sertligi                    | 1,00                          | 0,08  | 0,03  | -0,39 | 0,51  | -0,30 | -0,40 | -0,29 | -0,53 | -0,04 | -0,48 | 0,50  | -0,37 | -0,39 | 0,47  | -0,34 | -0,39 | -0,26 | 0,12  | -0,39 | 0,47  | -0,24 | 0,17  | -0,39 | 0,06  | -0,06 | 0,62  | 0,18  | -0,39 | 0,47  | 0,06  |       |       |       |       |       |       |       |       |       |       |      |       |
| Tambur_Hacmi_(lt)              | 1,00                          | -0,25 | 0,46  | -0,08 | 0,21  | 0,02  | 0,29  | 0,20  | 0,08  | 0,14  | 0,32  | 0,49  | 0,46  | -0,08 | 0,13  | -0,20 | 0,62  | -0,09 | 0,46  | -0,08 | 0,63  | -0,06 | 0,46  | 0,40  | -0,26 | 0,04  | -0,06 | 0,46  | -0,08 | -0,01 |       |       |       |       |       |       |       |       |       |       |       |      |       |
| SY1_Sure_(sn)                  | 1,00                          | -0,05 | -0,20 | -0,47 | 0,03  | 0,15  | -0,13 | -0,31 | 0,20  | 0,15  | -0,15 | -0,05 | -0,14 | 0,19  | 0,07  | -0,25 | -0,12 | -0,05 | -0,16 | -0,19 | -0,20 | -0,05 | -0,66 | 0,10  | 0,35  | -0,13 | -0,05 | -0,16 | 0,17  |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| SY1_Devir_(rpm)                | 1,00                          | 0,09  | -0,10 | 0,54  | 0,45  | 0,71  | 0,13  | 0,49  | -0,37 | 0,33  | 1,00  | 0,13  | 0,47  | 0,00  | 0,04  | -0,16 | 1,00  | 0,13  | 0,06  | -0,19 | 1,00  | 0,09  | 0,00  | -0,57 | -0,15 | 1,00  | 0,13  | -0,26 |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| SY1_ED                         | 1,00                          | -0,33 | 0,03  | 0,02  | -0,01 | 0,41  | -0,02 | -0,08 | -0,54 | 0,09  | 0,97  | 0,09  | -0,43 | -0,22 | 0,19  | 0,09  | 1,00  | -0,23 | 0,20  | 0,09  | 0,16  | 0,12  | 0,08  | 0,28  | 0,09  | 1,00  | -0,36 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| SG_Sic_(C)                     | 1,00                          | 0,22  | 0,01  | 0,05  | 0,05  | 0,11  | -0,10 | 0,33  | -0,10 | -0,36 | 0,01  | 0,26  | 0,48  | 0,12  | -0,10 | -0,37 | 0,51  | 0,11  | -0,10 | 0,35  | 0,26  | -0,33 | 0,07  | -0,10 | -0,37 | -0,14 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| I_Bas_Sic(C)                   | 1,00                          | 0,55  | 0,73  | 0,28  | 0,67  | -0,45 | -0,15 | 0,54  | 0,11  | 0,60  | -0,02 | 0,06  | -0,19 | 0,54  | 0,06  | 0,17  | -0,28 | 0,54  | -0,23 | 0,45  | -0,43 | -0,19 | 0,50  | 0,46  | -0,38 | 0,34  | -0,15 | 0,00  | -0,43 | 0,28  |       |       |       |       |       |       |       |       |       |       |       |      |       |
| I_Sure_(sn)                    | 1,00                          | 0,56  | 0,46  | 0,89  | 0,00  | -0,20 | 0,45  | 0,05  | 0,95  | -0,33 | 0,28  | 0,27  | 0,45  | 0,05  | 0,44  | 0,19  | 0,45  | 0,03  | 0,25  | -0,05 | 0,26  | 0,45  | 0,05  | -0,21 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| I_Devir_(rpm)                  | 1,00                          | 0,51  | 0,61  | -0,44 | 0,10  | 0,71  | 0,14  | 0,59  | -0,12 | 0,19  | -0,23 | 0,71  | 0,02  | 0,21  | -0,29 | 0,71  | -0,01 | 0,12  | -0,42 | -0,23 | 0,71  | 0,02  | -0,31 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| I_MHY_ED                       | 1,00                          | 0,35  | -0,05 | -0,25 | 0,13  | 0,49  | 0,48  | -0,19 | 0,22  | 0,25  | 0,13  | 0,41  | 0,38  | 0,20  | 0,13  | 0,53  | 0,36  | 0,15  | 0,23  | 0,13  | 0,41  | -0,37 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| I_Tset_(C)                     | 1,00                          | -0,27 | -0,09 | 0,49  | 0,02  | 0,90  | -0,20 | 0,30  | 0,06  | 0,49  | 0,02  | 0,38  | -0,02 | 0,49  | -0,15 | 0,23  | -0,25 | 0,07  | 0,49  | 0,02  | -0,25 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| AY_Su_Mik_(lt)                 | 1,00                          | -0,04 | -0,37 | -0,09 | -0,14 | -0,38 | 0,00  | 0,36  | -0,37 | -0,09 | -0,14 | -0,38 | 0,00  | 0,36  | -0,37 | -0,09 | 0,19  | 0,35  | -0,37 | 0,18  | 0,04  | 0,71  | 0,39  | -0,37 | -0,09 | 0,16  |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| AY_Sure_(sn)                   | 1,00                          | 0,33  | -0,53 | -0,21 | 0,32  | 0,34  | -0,30 | 0,33  | -0,54 | 0,26  | -0,26 | 0,33  | 0,26  | -0,26 | -0,31 | 0,33  | -0,54 | 0,12  |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| AY_Devir_(rpm)                 | 1,00                          | 0,13  | 0,47  | 0,00  | 0,04  | -0,16 | 1,00  | 0,13  | 0,06  | -0,19 | 1,00  | 0,09  | 0,00  | -0,57 | -0,15 | 1,00  | 0,13  | -0,26 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| AY_MHY_ED                      | 1,00                          | 0,13  | -0,42 | -0,22 | 0,13  | 0,13  | 0,97  | -0,21 | 0,13  | 0,13  | 0,11  | 0,15  | 0,11  | 0,22  | 0,13  | 0,97  | -0,38 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| AY_Tah_(C)                     | 1,00                          | -0,25 | 0,17  | 0,33  | 0,47  | 0,11  | 0,31  | 0,23  | 0,47  | 0,02  | 0,36  | -0,17 | 0,31  | 0,47  | 0,11  | -0,29 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| Jet_Pompa                      | 1,00                          | -0,01 | -0,06 | 0,00  | -0,43 | 0,05  | -0,08 | 0,00  | 0,14  | 0,15  | -0,31 | -0,20 | 0,00  | -0,43 | 0,12  |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 1D_Su_Mik_(lt)                 | 1,00                          | -0,17 | 0,04  | -0,23 | 0,87  | -0,13 | 0,04  | 0,23  | -0,24 | -0,01 | -0,18 | 0,04  | -0,23 | 0,03  |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 1D_Sure_(sn)                   | 1,00                          | -0,16 | 0,18  | 0,03  | 0,95  | -0,16 | 0,52  | 0,42  | 0,05  | 0,91  | -0,16 | 0,18  | -0,21 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 1D_Devir_(rpm)                 | 1,00                          | 0,13  | 0,06  | -0,19 | 1,00  | 0,09  | 0,00  | -0,57 | -0,15 | 1,00  | 0,13  | -0,26 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 1D_MHY_ED                      | 1,00                          | -0,24 | 0,19  | 0,13  | 0,13  | 0,12  | 0,07  | 0,27  | 0,13  | 1,00  | -0,36 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 2D_Su_Mik_(lt)                 | 1,00                          | 0,00  | 0,06  | 0,37  | 0,08  | 0,11  | -0,02 | 0,06  | -0,24 | -0,05 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 2D_Sure_(sn)                   | 1,00                          | -0,19 | 0,54  | 0,28  | 0,05  | 0,92  | -0,19 | 0,19  | -0,14 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 2D_Devir_(rpm)                 | 1,00                          | 0,09  | 0,00  | -0,57 | -0,15 | 1,00  | 0,13  | -0,26 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 2D_MHY_ED                      | 1,00                          | 0,16  | -0,03 | 0,46  | 0,09  | 0,13  | -0,19 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 2D_Sikma_(rpm)                 | 1,00                          | -0,06 | 0,35  | 0,00  | 0,12  | -0,39 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 3D_Su_Mik_(lt)                 | 1,00                          | 0,08  | -0,57 | 0,07  | 0,26  |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 3D_Sure_(sn)                   | 1,00                          | -0,15 | 0,27  | -0,18 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 3D_Devir_(rpm)                 | 1,00                          | 0,13  | -0,26 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| 3D_MHY_ED                      | 1,00                          | -0,36 |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |
| Cikis_Alan_Ortalama            | 1,00                          |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |      |       |

# SPEARMAN'S RANK

| DEĞER | Sol_Korelasyon                 | to | Üst_Korelasyon                 |
|-------|--------------------------------|----|--------------------------------|
| 1,00  | Deterjan_Miktari(gr)           | => | Test_Kapasitesi(kg)            |
| 1,00  | SY1_Devir_(rpm)                | => | AY_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 1D_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 2D_Devir_(rpm)                 |
| 1,00  | SY1_Devir_(rpm)                | => | 3D_Devir_(rpm)                 |
| 1,00  | AY_Devir_(rpm)                 | => | 1D_Devir_(rpm)                 |
| 1,00  | AY_Devir_(rpm)                 | => | 2D_Devir_(rpm)                 |
| 1,00  | AY_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 |
| 1,00  | 1D_Devir_(rpm)                 | => | 2D_Devir_(rpm)                 |
| 1,00  | 1D_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 |
| 1,00  | 1D_MHY_ED                      | => | 3D_MHY_ED                      |
| 1,00  | 2D_Devir_(rpm)                 | => | 3D_Devir_(rpm)                 |
| 1,00  | SY1_ED                         | => | 1D_MHY_ED                      |
| 1,00  | SY1_ED                         | => | 3D_MHY_ED                      |
| 0,97  | SY1_ED                         | => | AY_MHY_ED                      |
| 0,97  | AY_MHY_ED                      | => | 1D_MHY_ED                      |
| 0,97  | AY_MHY_ED                      | => | 3D_MHY_ED                      |
| 0,95  | 1D_Sure_(sn)                   | => | 2D_Sure_(sn)                   |
| 0,95  | 1_Sure_(sn)                    | => | AY_Tah_(C)                     |
| 0,94  | Numune_1_Relakse_Sonrasi_En_1  | => | Numune_1_Relakse_Sonrasi_En_2  |
| 0,92  | 2D_Sure_(sn)                   | => | 3D_Sure_(sn)                   |
| 0,91  | 1D_Sure_(sn)                   | => | 3D_Sure_(sn)                   |
| 0,90  | 1_Tset_(C)                     | => | AY_Tah_(C)                     |
| 0,89  | 1_Sure_(sn)                    | => | 1_Tset_(C)                     |
| 0,87  | 1D_Su_Mik_(lt)                 | => | 2D_Su_Mik_(lt)                 |
| 0,86  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Numune_1_Relakse_Sonrasi_Boy_3 |
| 0,86  | Numune_1_Relakse_Sonrasi_En_1  | => | Numune_1_Relakse_Sonrasi_En_3  |
| 0,85  | Numune_1_Relakse_Sonrasi_En_2  | => | Numune_1_Relakse_Sonrasi_En_3  |
| 0,83  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Numune_1_Relakse_Sonrasi_Boy_2 |
| 0,78  | Deterjan_Miktari(gr)           | => | Tambur_Hacmi_(lt)              |
| 0,78  | Test_Kapasitesi(kg)            | => | Tambur_Hacmi_(lt)              |
| 0,74  | Numune_1_Relakse_Sonrasi_Boy_2 | => | Numune_1_Relakse_Sonrasi_Boy_3 |
| 0,74  | Numune_1_Relakse_Sonrasi_Boy_1 | => | Giris_Alan_Ortalama            |
| 0,73  | 1_Bas_Sic(C)                   | => | 1_Devir_(rpm)                  |
| 0,71  | SY1_Devir_(rpm)                | => | 1_Devir_(rpm)                  |
| 0,71  | 1_Devir_(rpm)                  | => | AY_Devir_(rpm)                 |
| 0,71  | 1_Devir_(rpm)                  | => | 1D_Devir_(rpm)                 |
| 0,71  | 1_Devir_(rpm)                  | => | 2D_Devir_(rpm)                 |
| 0,71  | 1_Devir_(rpm)                  | => | 3D_Devir_(rpm)                 |
| 0,71  | AY_Su_Mik_(lt)                 | => | 3D_Su_Mik_(lt)                 |
| -0,72 | Test_No                        | => | Cikis_Alan_Ortalama            |

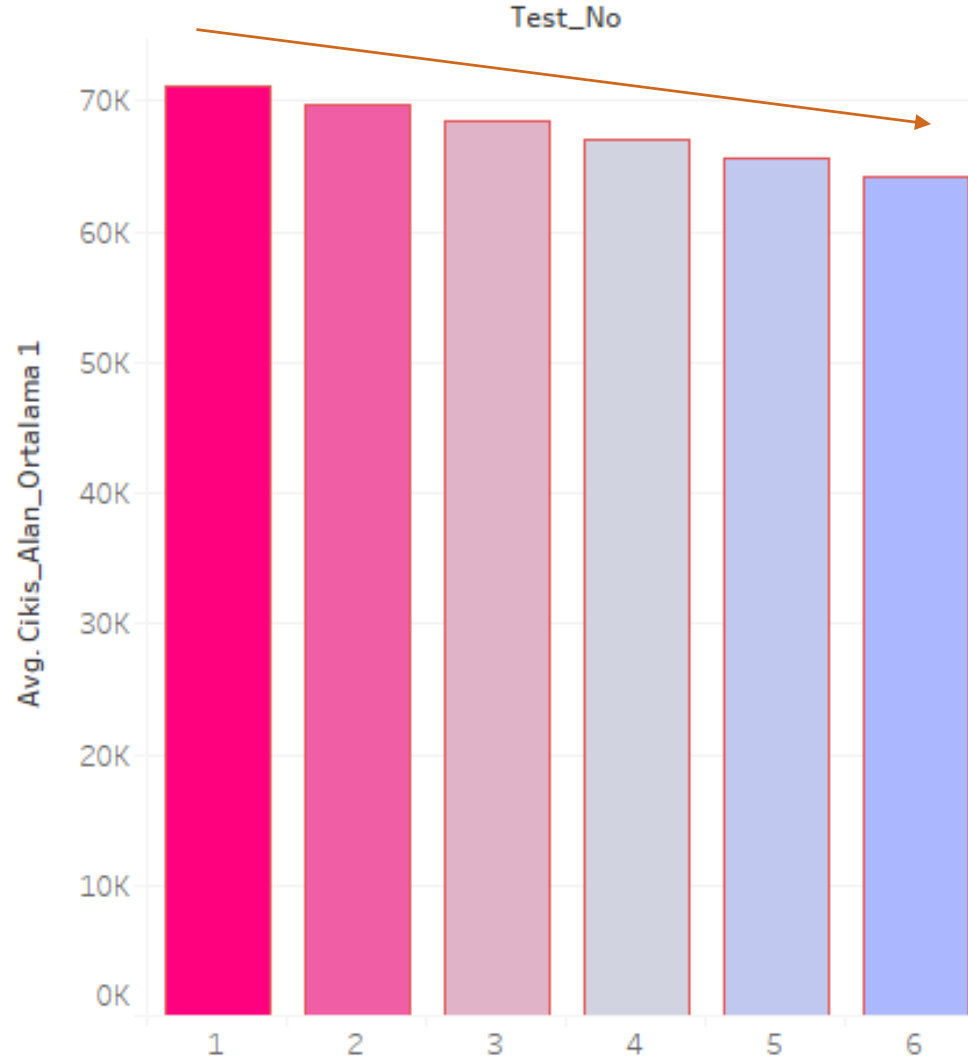
## PEARSON CORRELATION W/ OUTPUT

|                                |       |
|--------------------------------|-------|
| Cikis_Alan_Ortalama            | 1,00  |
| Numune_1_Relakse_Sonrasi_Boy_3 | 0,50  |
| Giris_Alan_Ortalama            | 0,48  |
| Numune_1_Relakse_Sonrasi_Boy_1 | 0,48  |
| Numune_1_Relakse_Sonrasi_Boy_2 | 0,48  |
| Test_Kapasitesi(kg)            | 0,34  |
| Deterjan_Miktari(gr)           | 0,34  |
| 3D_Su_Mik_(lt)                 | 0,25  |
| SY1_Sure_(sn)                  | 0,22  |
| AY_Sure_(sn)                   | 0,21  |
| 1D_Su_Mik_(lt)                 | 0,17  |
| AY_Su_Mik_(lt)                 | 0,16  |
| Jet_Pompa                      | 0,12  |
| 2D_Su_Mik_(lt)                 | 0,11  |
| Su_Sertligi                    | 0,09  |
| Tambur_Hacmi_(lt)              | 0,07  |
| 2D_MHY_ED                      | -0,01 |
| I_MHY_ED                       | -0,07 |
| Numune_1_Relakse_Sonrasi_En_2  | -0,09 |
| 3D_Sure_(sn)                   | -0,11 |
| 2D_Sure_(sn)                   | -0,13 |
| SG_Sic_(C)                     | -0,15 |
| 1D_Sure_(sn)                   | -0,15 |
| Numune_1_Relakse_Sonrasi_En_3  | -0,18 |
| Numune_1_Relakse_Sonrasi_En_1  | -0,20 |
| I_Sure_(sn)                    | -0,28 |
| I_Tset_(C)                     | -0,31 |
| 3D_Devir_(rpm)                 | -0,33 |
| SY1_Devir_(rpm)                | -0,33 |
| AY_Devir_(rpm)                 | -0,33 |
| 1D_Devir_(rpm)                 | -0,33 |
| 2D_Devir_(rpm)                 | -0,33 |
| AY_Tah_(C)                     | -0,34 |
| I_Devir_(rpm)                  | -0,35 |
| I_Bas_Sic_(C)                  | -0,36 |
| 1D_MHY_ED                      | -0,40 |
| SY1_ED                         | -0,40 |
| 3D_MHY_ED                      | -0,40 |
| AY_MHY_ED                      | -0,41 |
| 2D_Sikma_(rpm)                 | -0,49 |
| Test_No                        | -0,67 |

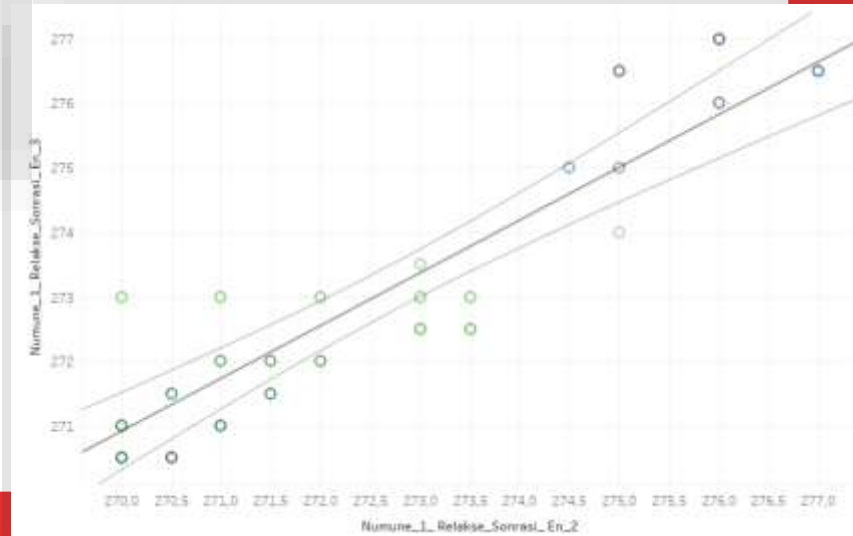
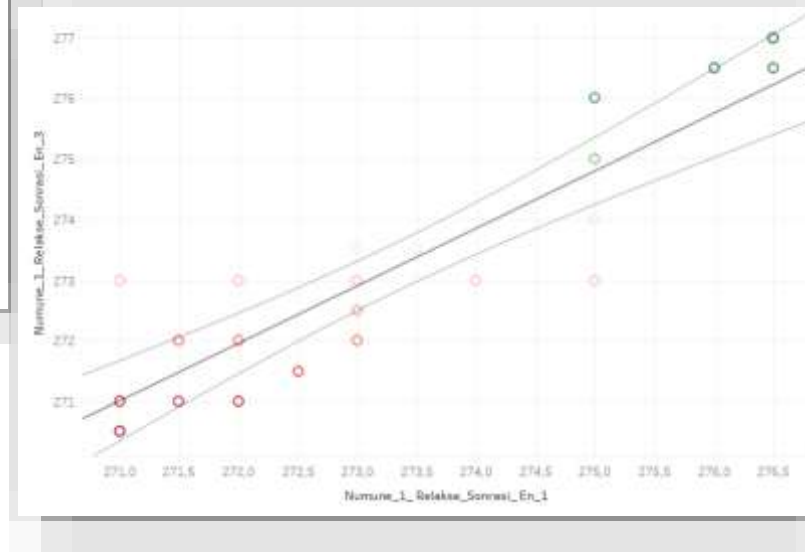
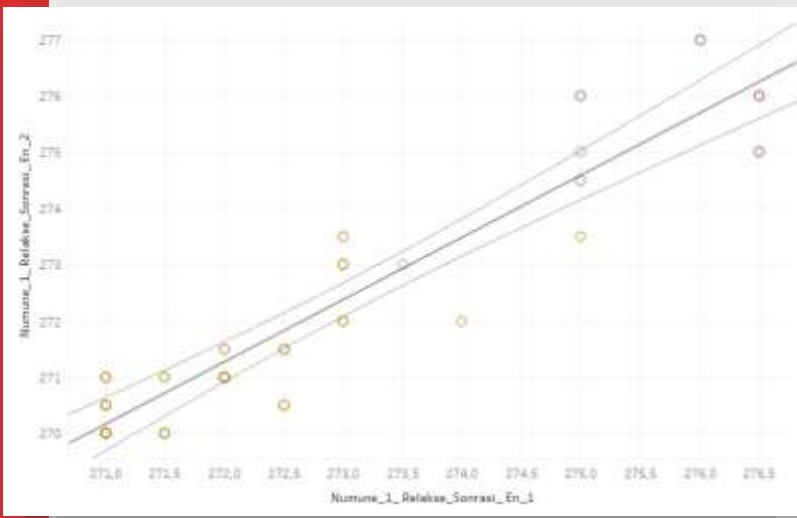
|       |                                |
|-------|--------------------------------|
| 1,00  | Cikis_Alan_Ortalama            |
| 0,28  | Deterjan_Miktari(gr)           |
| 0,28  | Test_Kapasitesi(kg)            |
| 0,26  | 3D_Su_Mik_(lt)                 |
| 0,24  | Giris_Alan_Ortalama            |
| 0,21  | Numune_1_Relakse_Sonrasi_Boy_3 |
| 0,18  | Numune_1_Relakse_Sonrasi_Boy_1 |
| 0,17  | SY1_Sure_(sn)                  |
| 0,16  | AY_Su_Mik_(lt)                 |
| 0,15  | Numune_1_Relakse_Sonrasi_Boy_2 |
| 0,12  | AY_Sure_(sn)                   |
| 0,12  | Jet_Pompa                      |
| 0,06  | Su_Sertligi                    |
| 0,03  | 1D_Su_Mik_(lt)                 |
| -0,01 | Tambur_Hacmi_(lt)              |
| -0,05 | 2D_Su_Mik_(lt)                 |
| -0,06 | Numune_1_Relakse_Sonrasi_En_2  |
| -0,11 | Numune_1_Relakse_Sonrasi_En_3  |
| -0,13 | Numune_1_Relakse_Sonrasi_En_1  |
| -0,14 | 2D_Sure_(sn)                   |
| -0,14 | SG_Sic_(C)                     |
| -0,18 | 3D_Sure_(sn)                   |
| -0,19 | 2D_MHY_ED                      |
| -0,21 | 1D_Sure_(sn)                   |
| -0,21 | I_Sure_(sn)                    |
| -0,25 | I_Tset_(C)                     |
| -0,26 | SY1_Devir_(rpm)                |
| -0,26 | AY_Devir_(rpm)                 |
| -0,26 | 1D_Devir_(rpm)                 |
| -0,26 | 2D_Devir_(rpm)                 |
| -0,26 | 3D_Devir_(rpm)                 |
| -0,29 | AY_Tah_(C)                     |
| -0,31 | I_Devir_(rpm)                  |
| -0,36 | SY1_ED                         |
| -0,36 | 1D_MHY_ED                      |
| -0,36 | 3D_MHY_ED                      |
| -0,37 | I_MHY_ED                       |
| -0,38 | I_Bas_Sic_(C)                  |
| -0,38 | AY_MHY_ED                      |
| -0,39 | 2D_Sikma_(rpm)                 |
| -0,72 | Test_No                        |

## SPEARMAN CORRELATION W/ OUTPUT

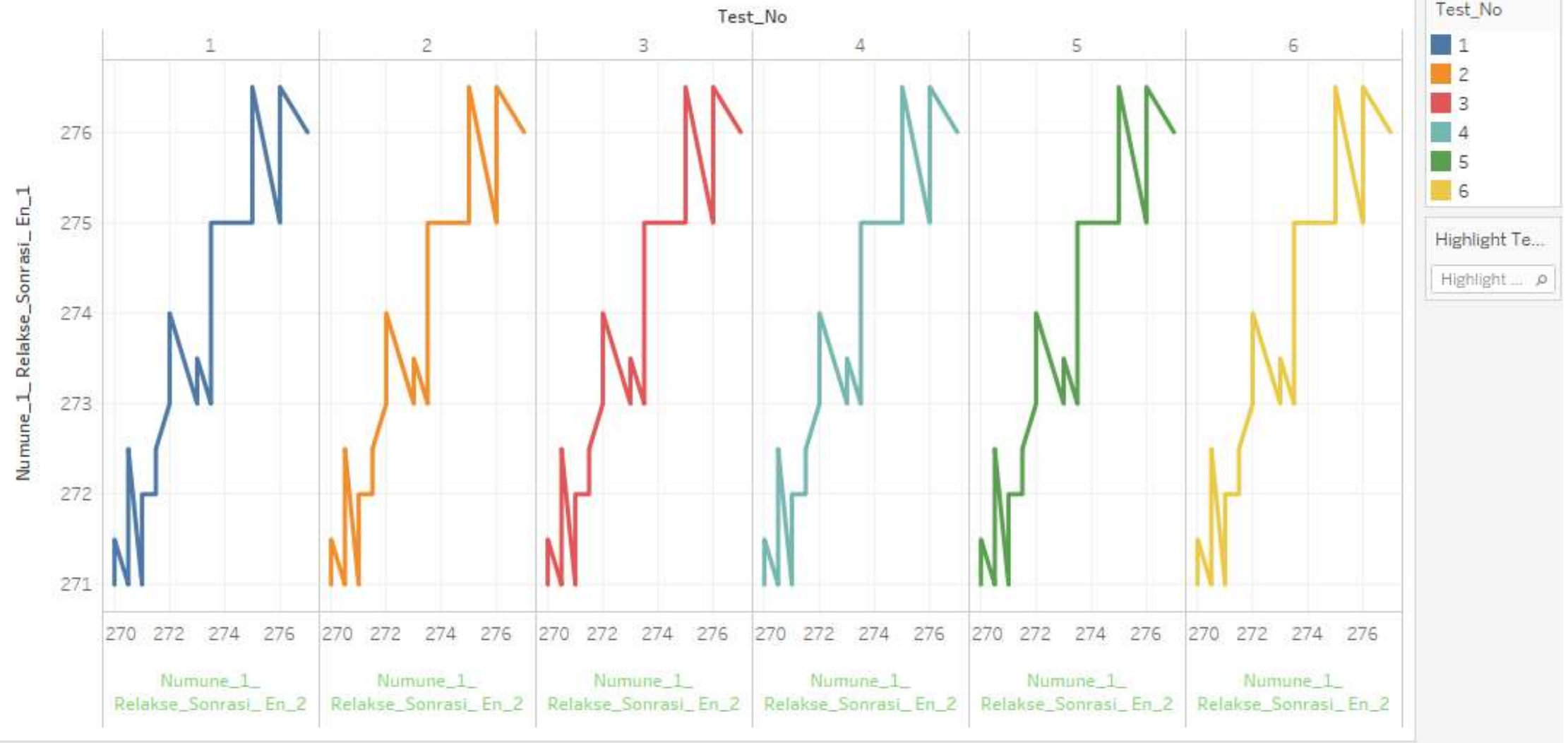
|       |                |    |                     |
|-------|----------------|----|---------------------|
| DEĞER | Sol_Korelasyon | to | Üst_Korelasyon      |
| -0,72 | Test_No        | => | Cikis_Alan_Ortalama |



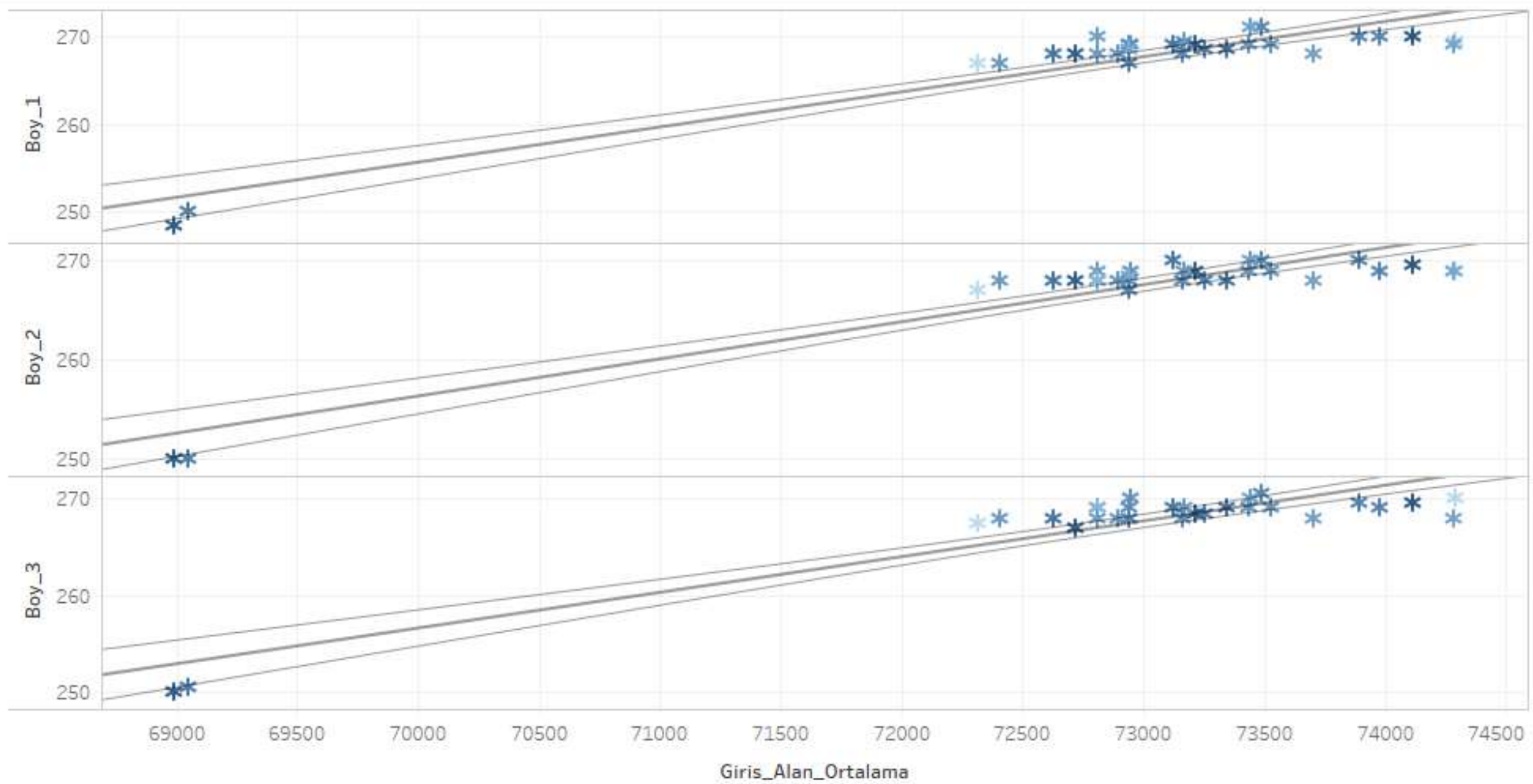
| DEĞER Sol_Korelasyon               | to Üst_Korelasyon                |
|------------------------------------|----------------------------------|
| 0,94 Numune_I_Relakse_Sonrasi_En_1 | => Numune_I_Relakse_Sonrasi_En_2 |
| 0,86 Numune_I_Relakse_Sonrasi_En_1 | => Numune_I_Relakse_Sonrasi_En_3 |
| 0,85 Numune_I_Relakse_Sonrasi_En_2 | => Numune_I_Relakse_Sonrasi_En_3 |



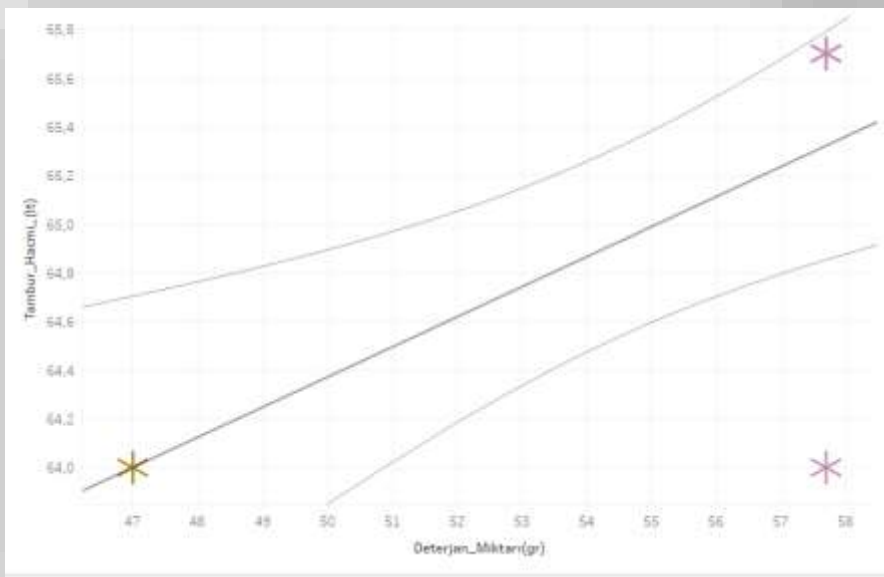
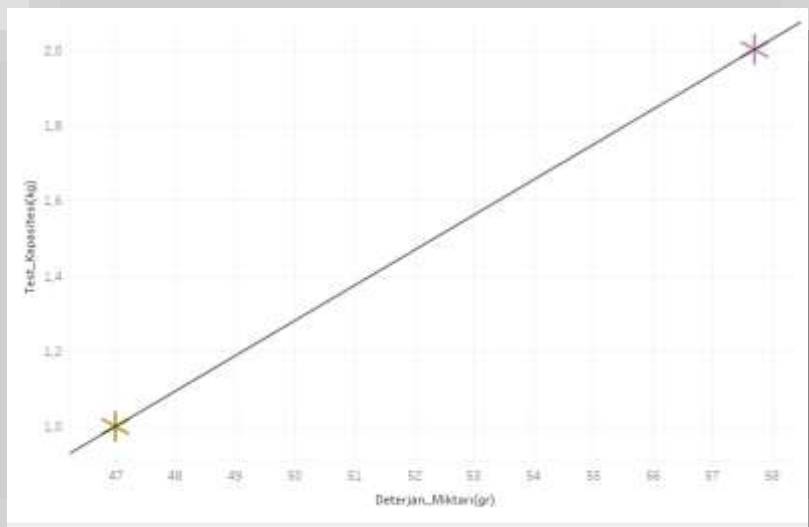




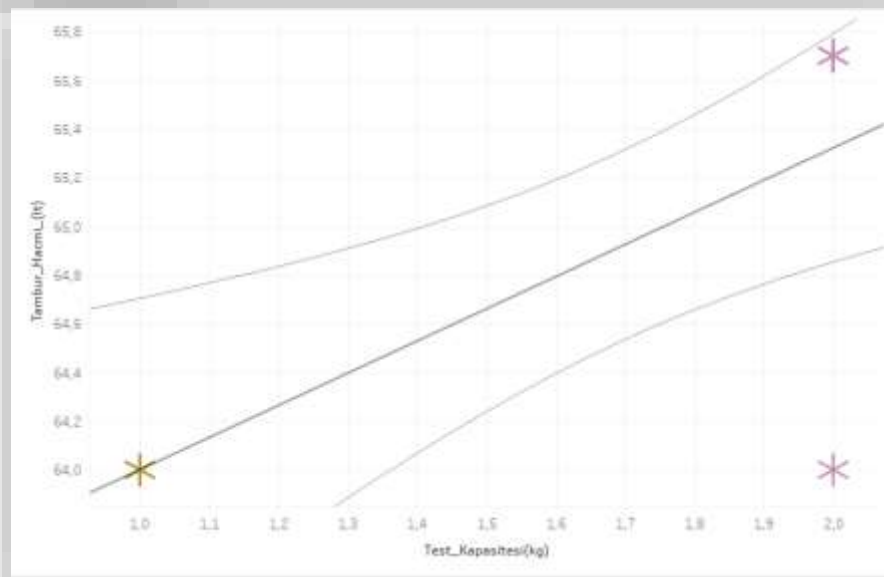


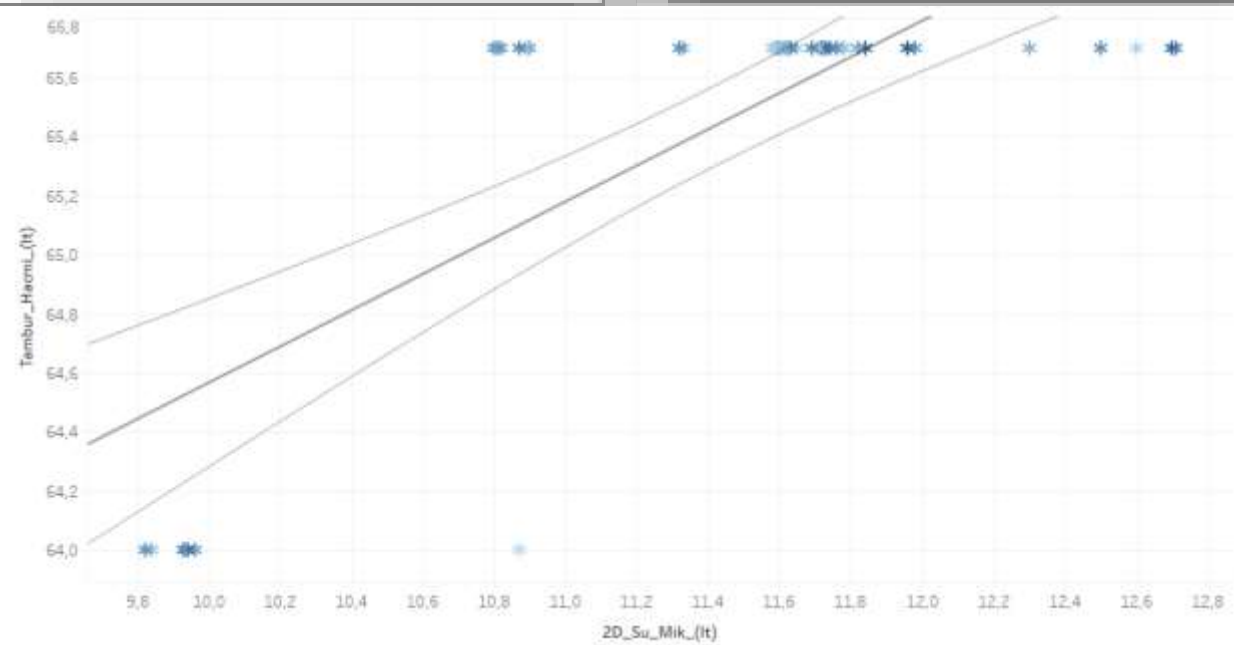
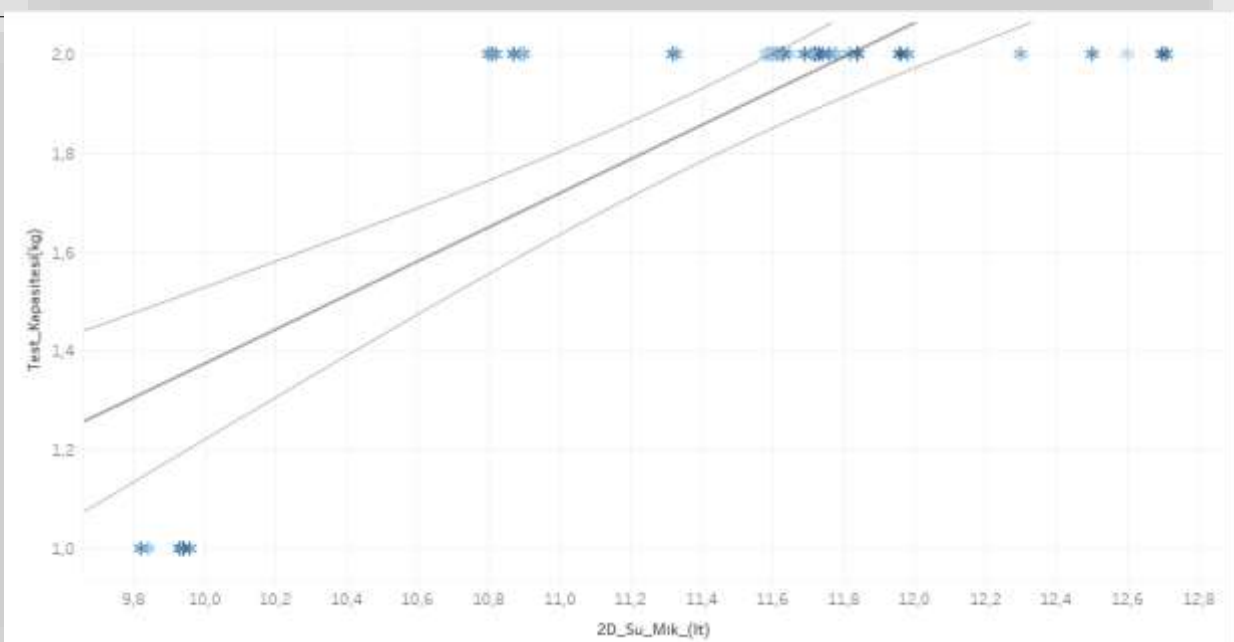
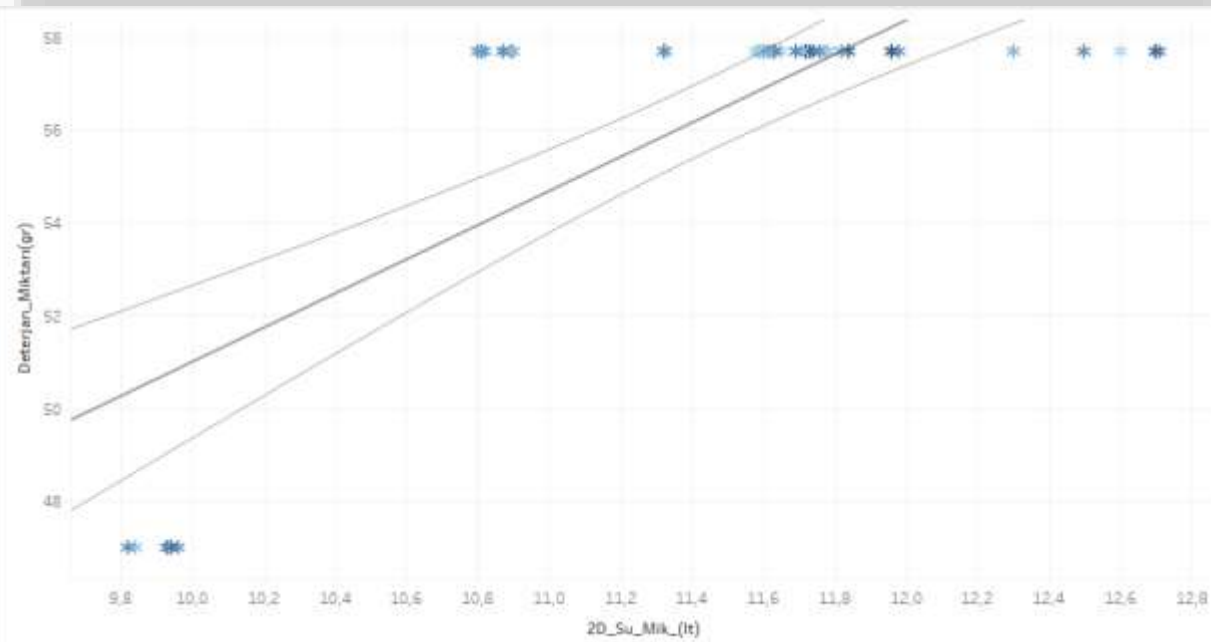


|                           |    |                     |
|---------------------------|----|---------------------|
| 1,00 Deterjan_Miktarı(gr) | => | Test_Kapasitesi(kg) |
| 0,78 Deterjan_Miktarı(gr) | => | Tambur_Hacmi_(lt)   |
| 0,78 Test_Kapasitesi(kg)  | => | Tambur_Hacmi_(lt)   |

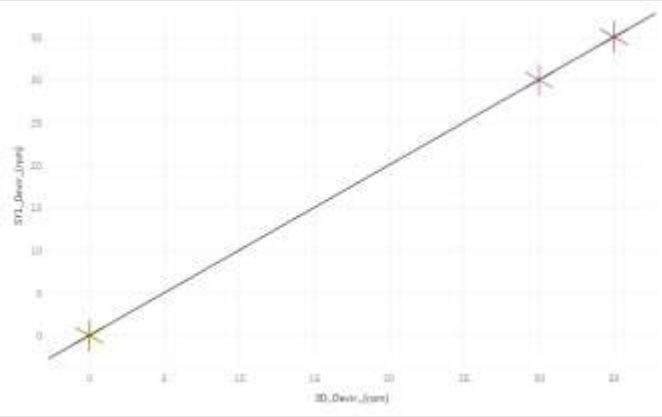
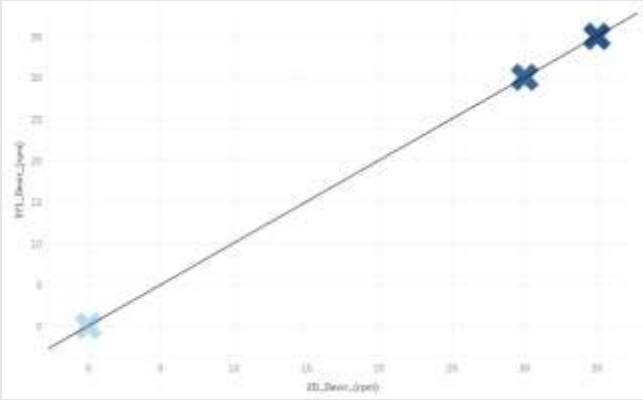
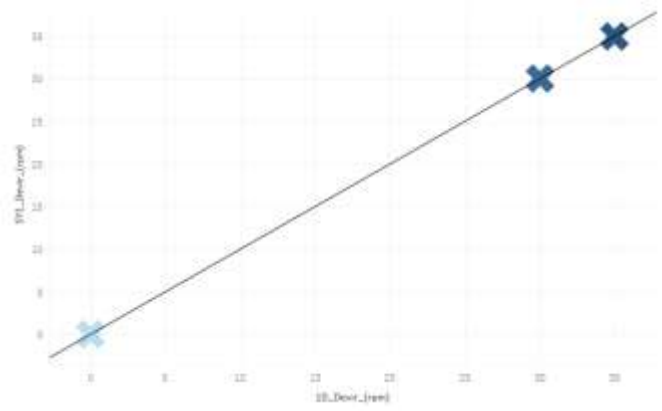
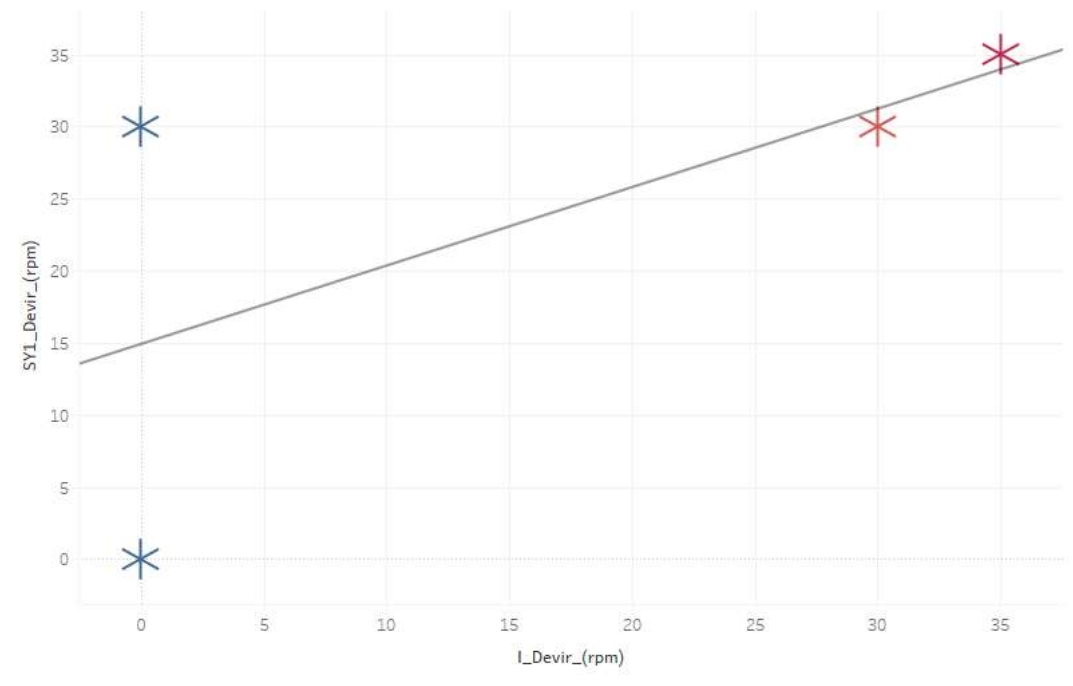
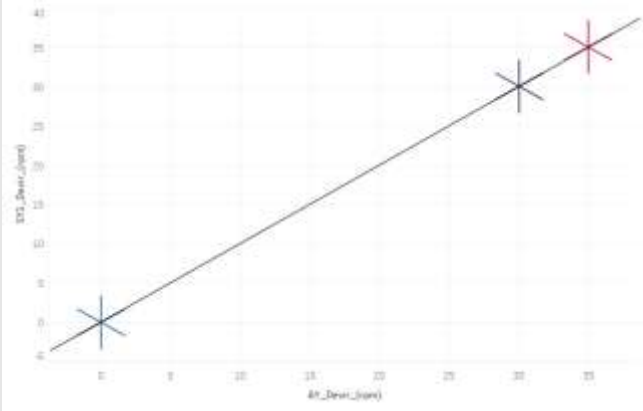


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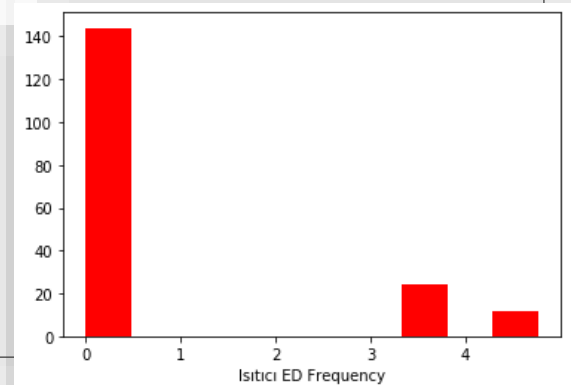
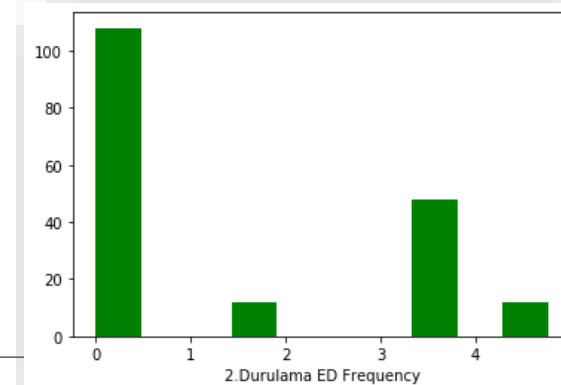
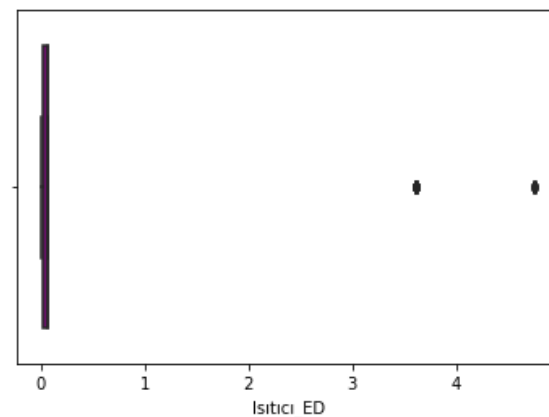
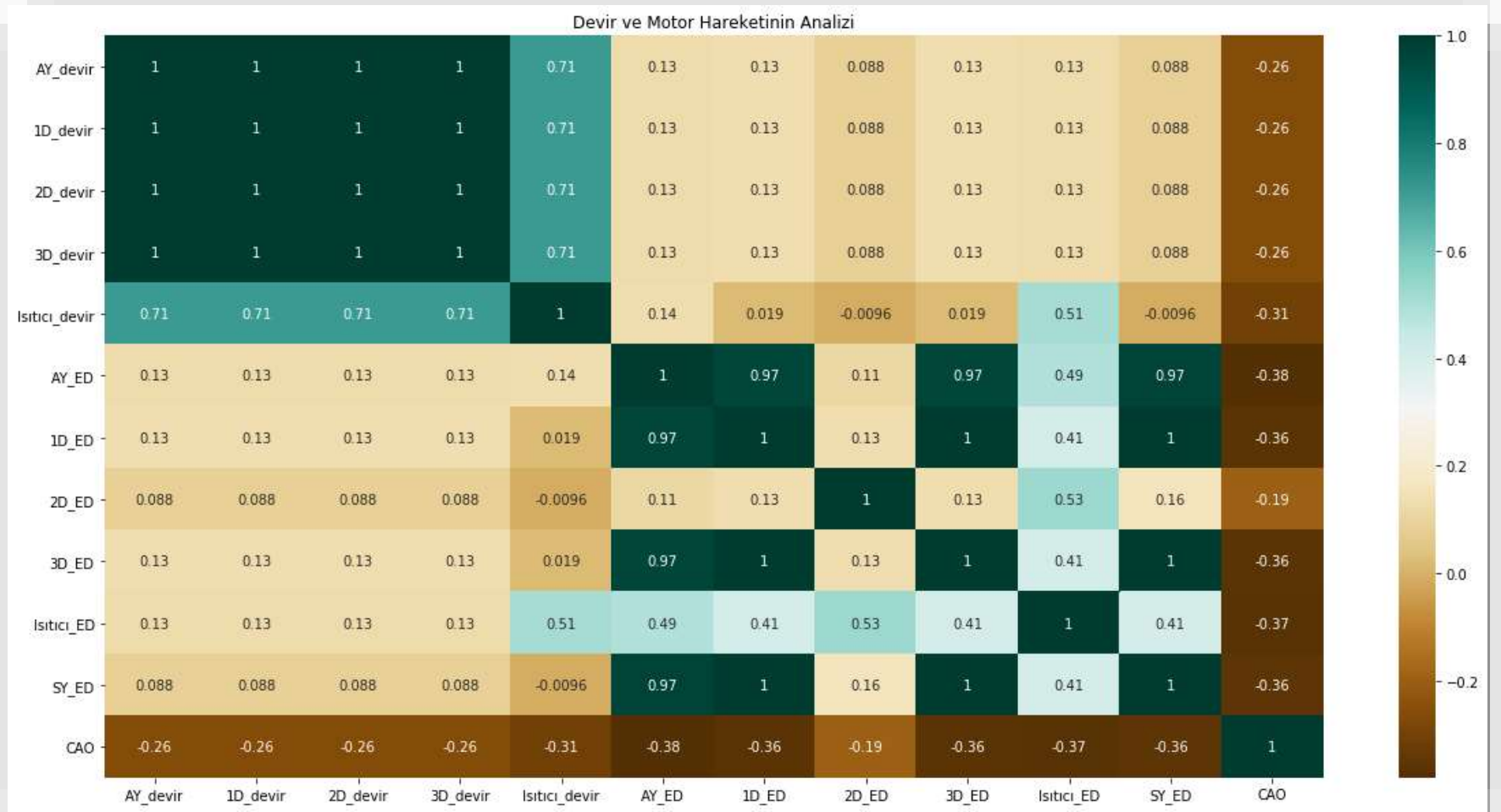


|                      |    |                |
|----------------------|----|----------------|
| 0,7I SYI_Devir_(rpm) | => | I_Devir_(rpm)  |
| 1,00SYI_Devir_(rpm)  | => | AY_Devir_(rpm) |
| 1,00SYI_Devir_(rpm)  | => | ID_Devir_(rpm) |
| 1,00SYI_Devir_(rpm)  | => | 2D_Devir_(rpm) |
| 1,00SYI_Devir_(rpm)  | => | 3D_Devir_(rpm) |



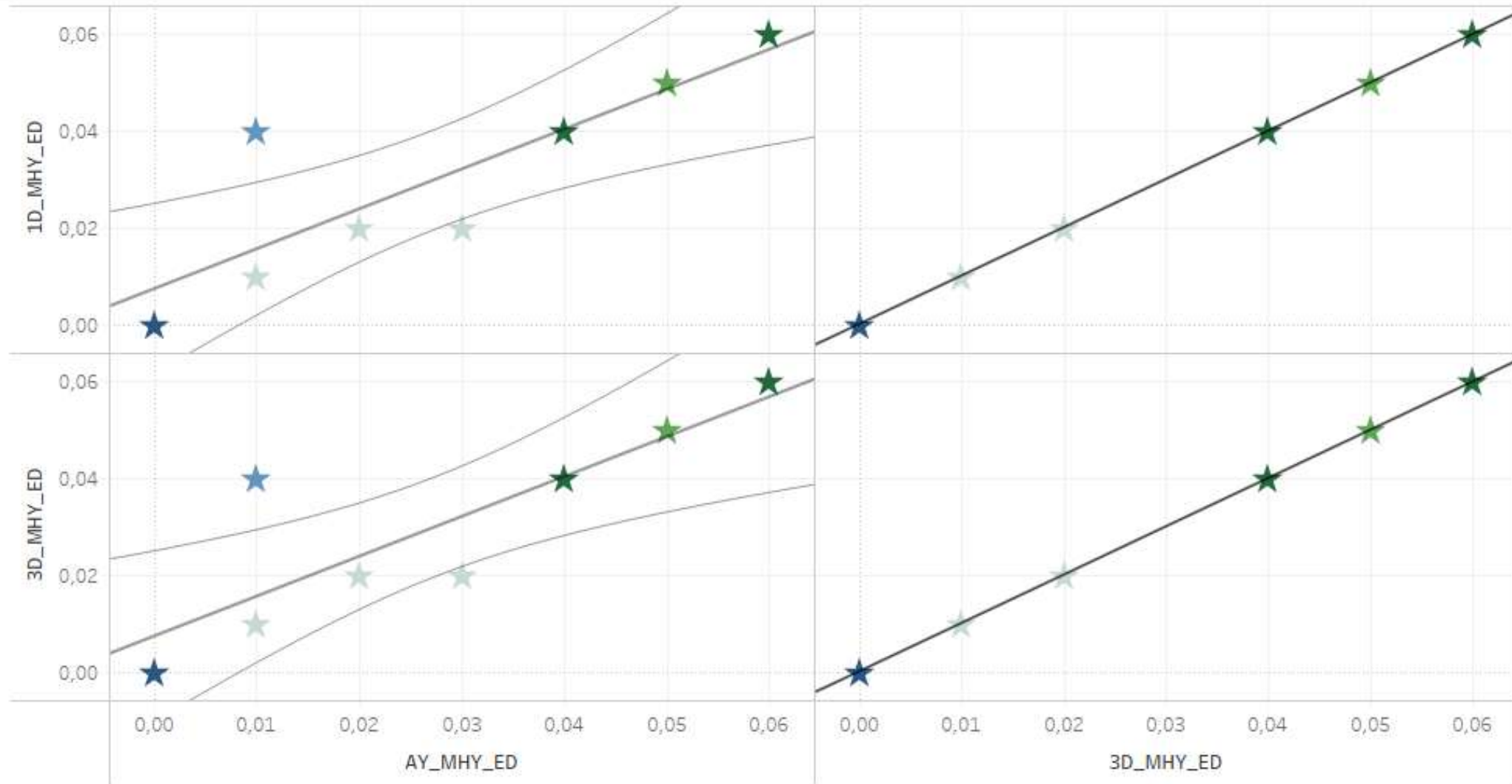
# Revolution and Engine Motion Analysis (rpm)

- All cycle data are batch data. According to the Spearman correlation, if Isıtıcı\_devir (heater speed) increases, the shrinkage amount increases by 31% !!
- In addition, among the ED variables, Isıtıcı\_ED variable contains outliers, the distribution of other ED variables is seen regularly.
- Of the ED variables, AY\_ED (main wash) has the most relation with CAO. If AY\_ED increases, it can be interpreted that the shrinkage rate in woolen textile increases 38%. AY is also 97% same with ID, 3D and SY values.
- $SY\_ED = ID\_ED = 3D\_ED$  THESE MUST BE REMOVED!!!!
- Also Isıtıcı\_ED has 53% corr with 2D\_ED, with Isıtıcı\_devir has 51%.

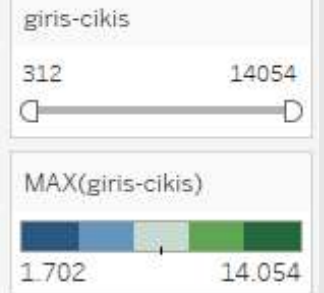
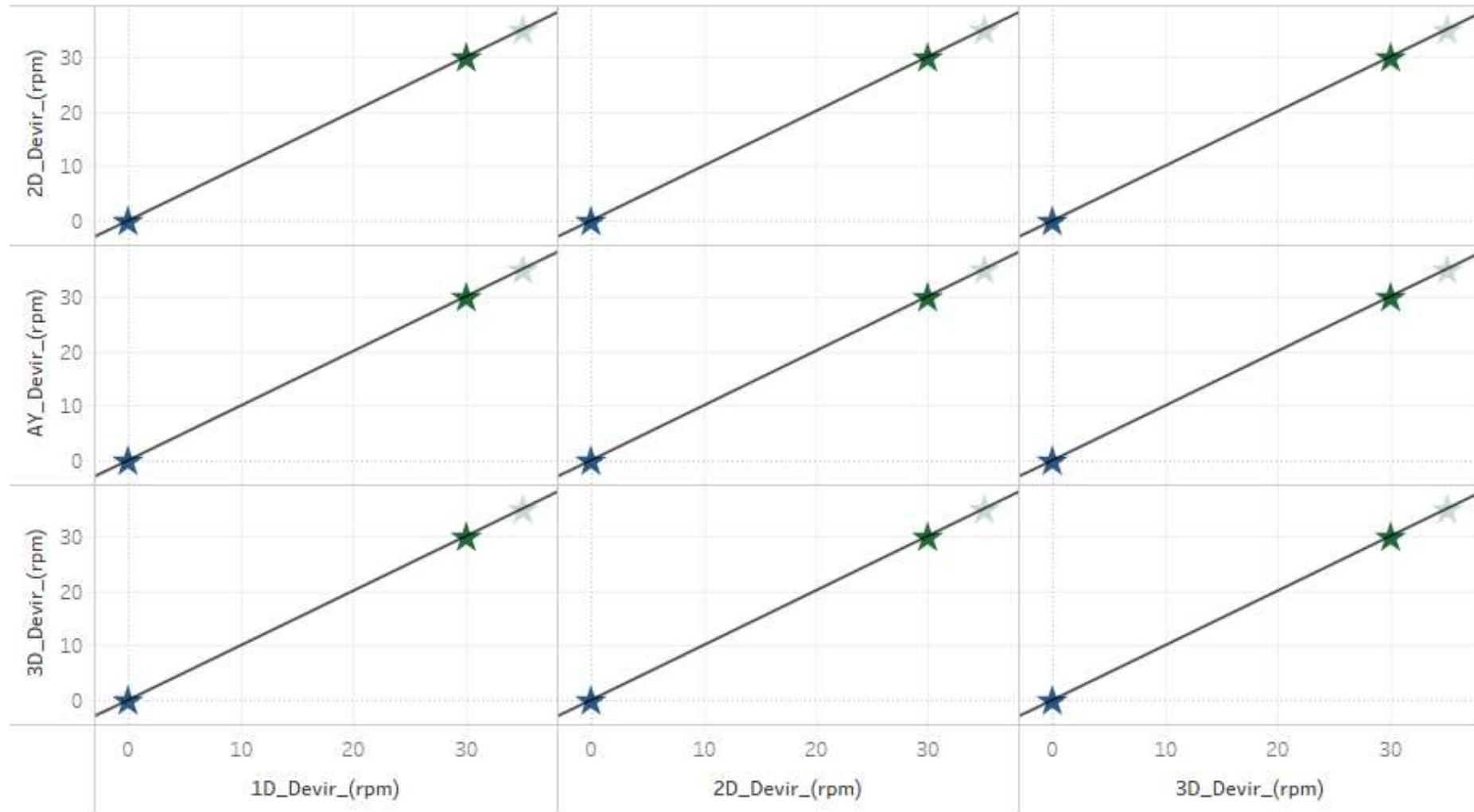


0,96 AY\_MHY\_ED  
0,96 AY\_MHY\_ED  
1,00 ID\_MHY\_ED

=> ID\_MHY\_ED  
=> 3D\_MHY\_ED  
=> 3D\_MHY\_ED



|                     |    |                |
|---------------------|----|----------------|
| 1,00 AY_Devir_(rpm) | => | 1D_Devir_(rpm) |
| 1,00 AY_Devir_(rpm) | => | 2D_Devir_(rpm) |
| 1,00 AY_Devir_(rpm) | => | 3D_Devir_(rpm) |
| 1,00 1D_Devir_(rpm) | => | 2D_Devir_(rpm) |
| 1,00 1D_Devir_(rpm) | => | 3D_Devir_(rpm) |
| 1,00 2D_Devir_(rpm) | => | 3D_Devir_(rpm) |





0,71I\_Devir\_(rpm)

=>

AY\_Devir\_(rpm)

0,71I\_Devir\_(rpm)

=>

1D\_Devir\_(rpm)

0,71I\_Devir\_(rpm)

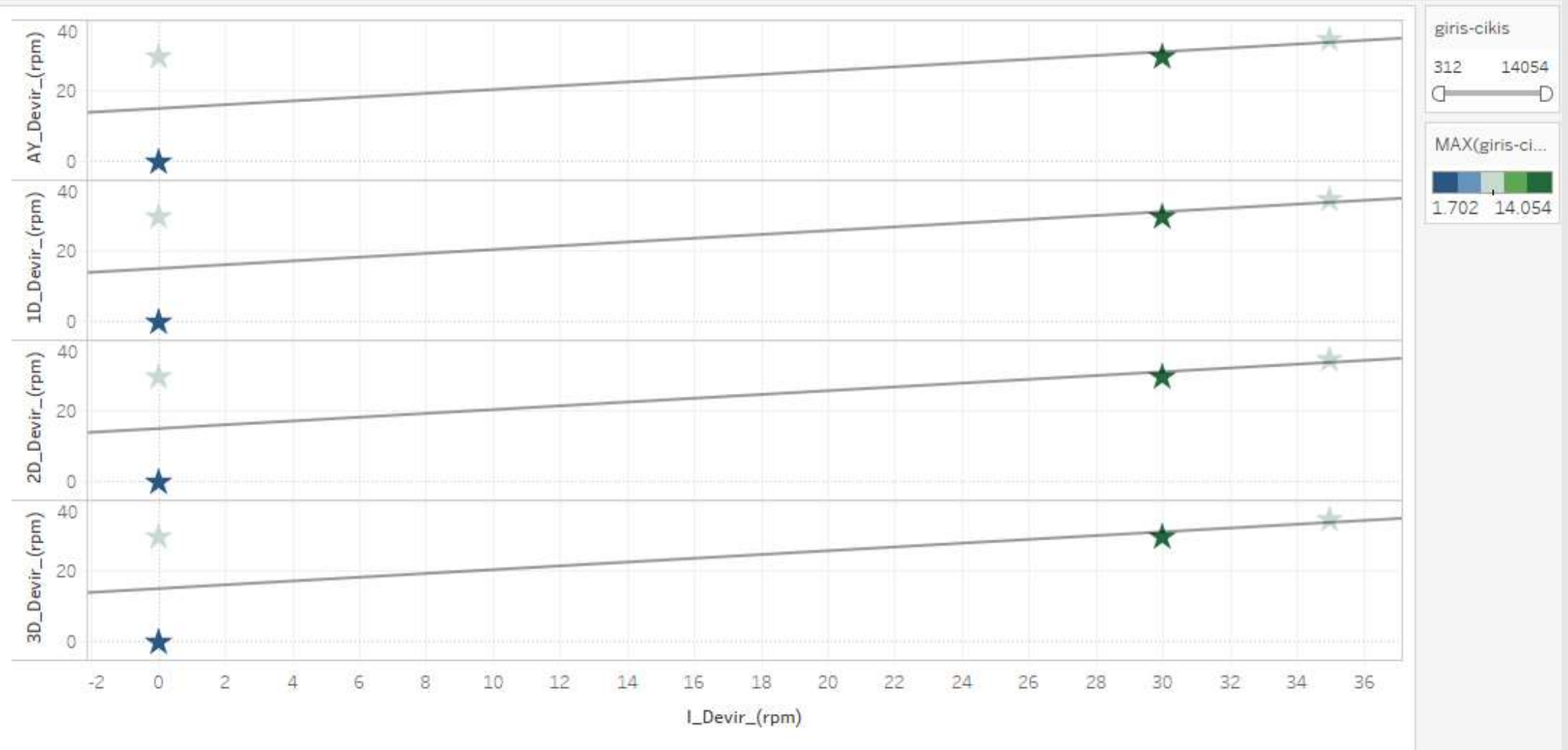
=>

2D\_Devir\_(rpm)

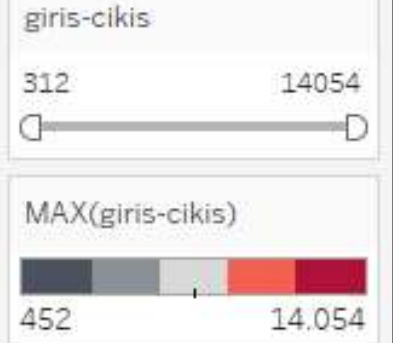
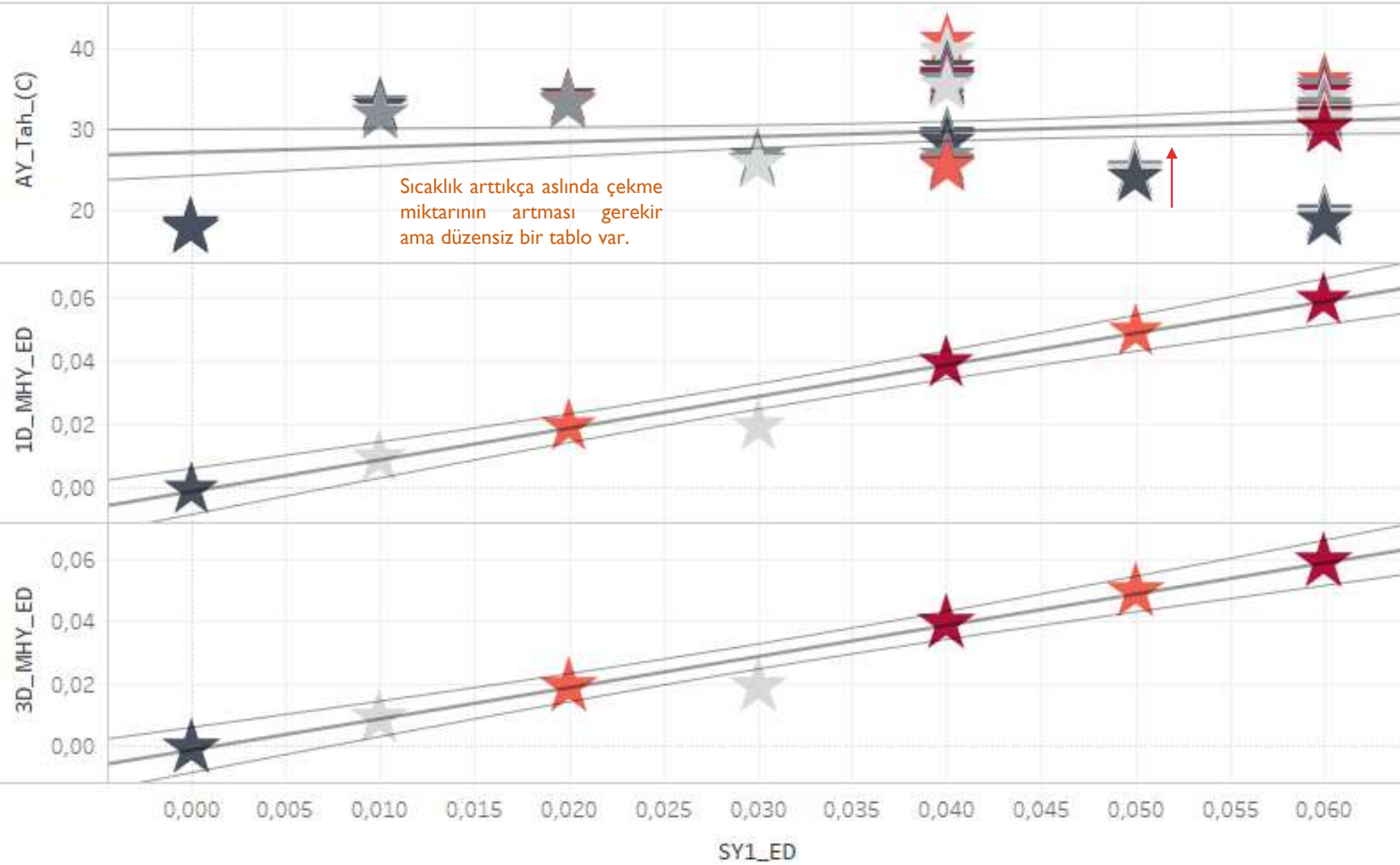
0,71I\_Devir\_(rpm)

=>

3D\_Devir\_(rpm)





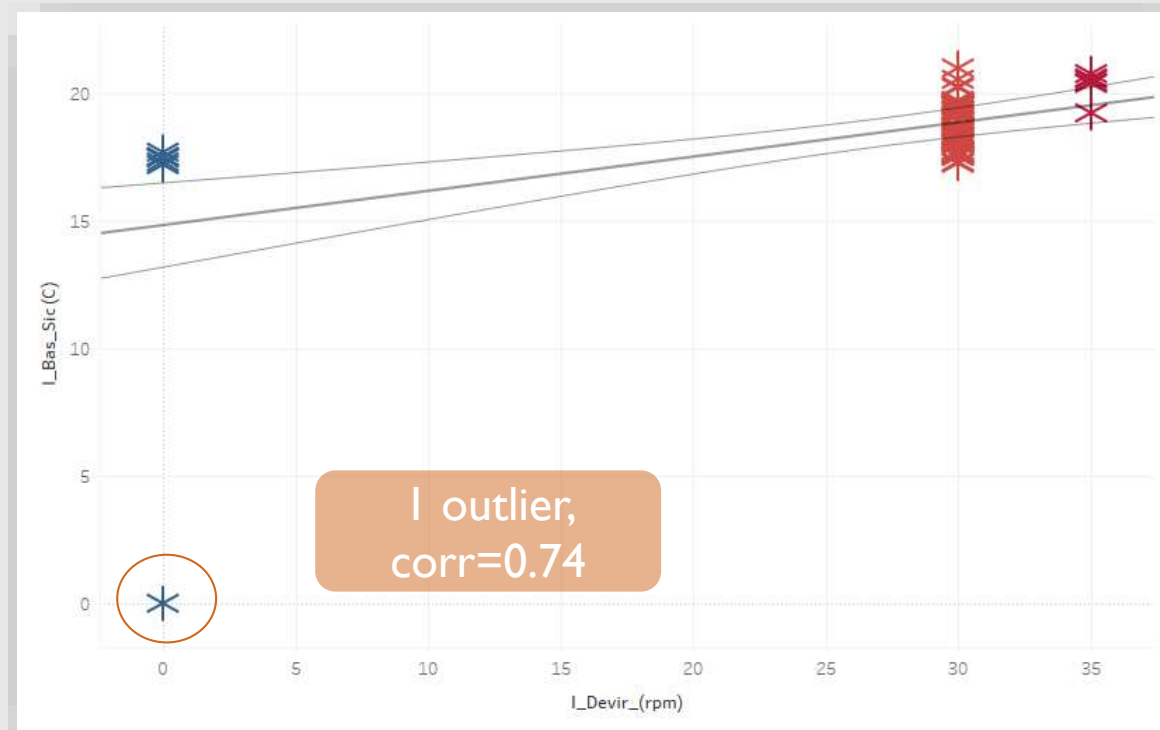
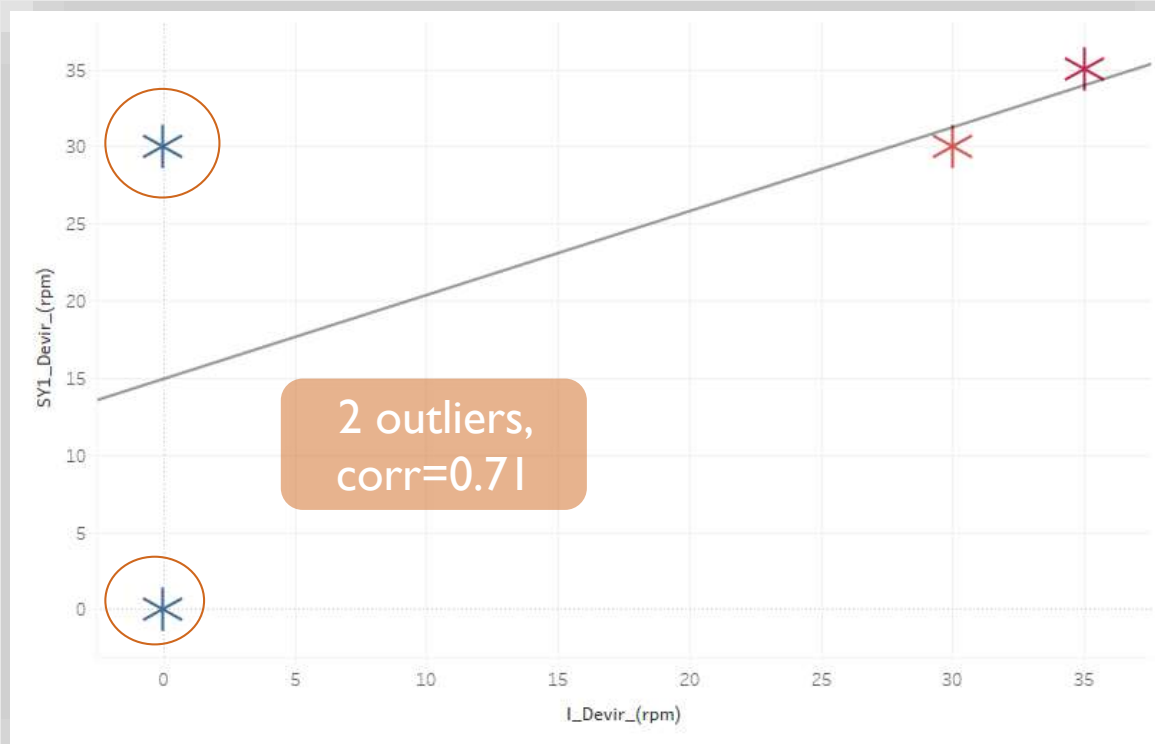


0,71 SYI\_Devir\_(rpm)

=> I\_Devir\_(rpm)

0,74 I\_Bas\_Sic (C)

=> I\_Devir\_(rpm)



0,89 I\_Sure\_(sn)

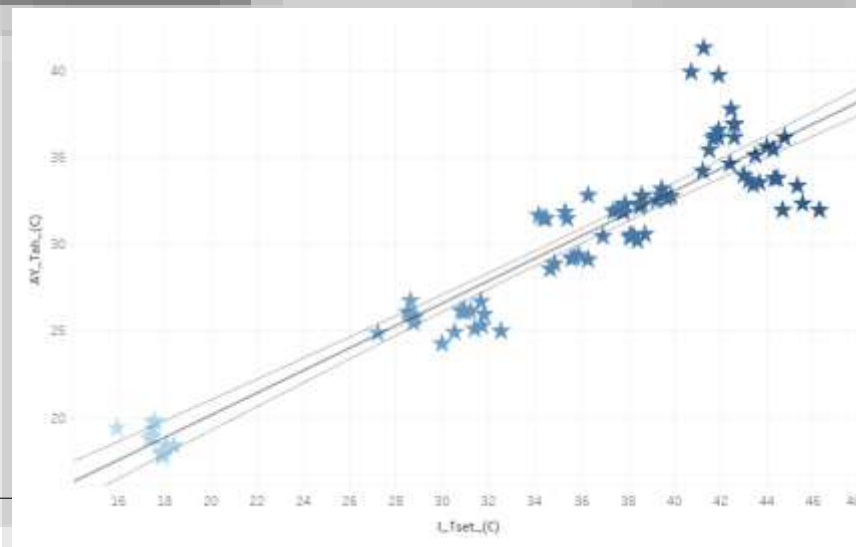
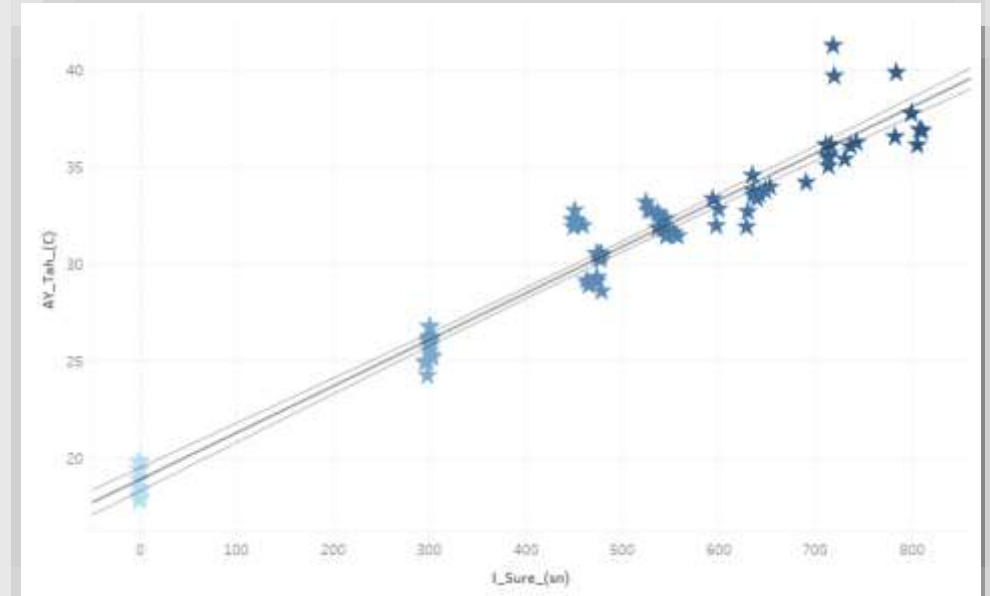
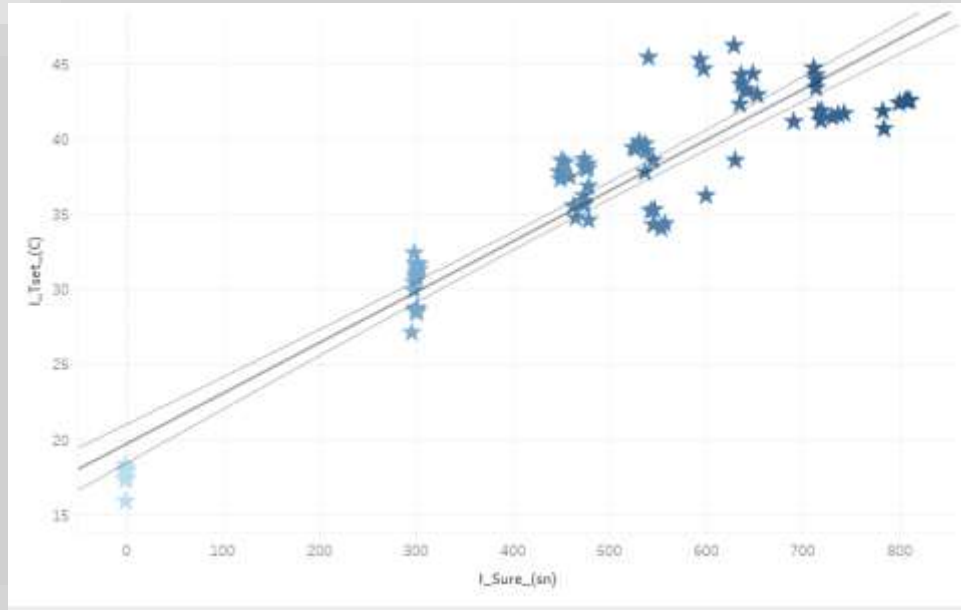
=> I\_Tset\_(C)

0,95 I\_Sure\_(sn)

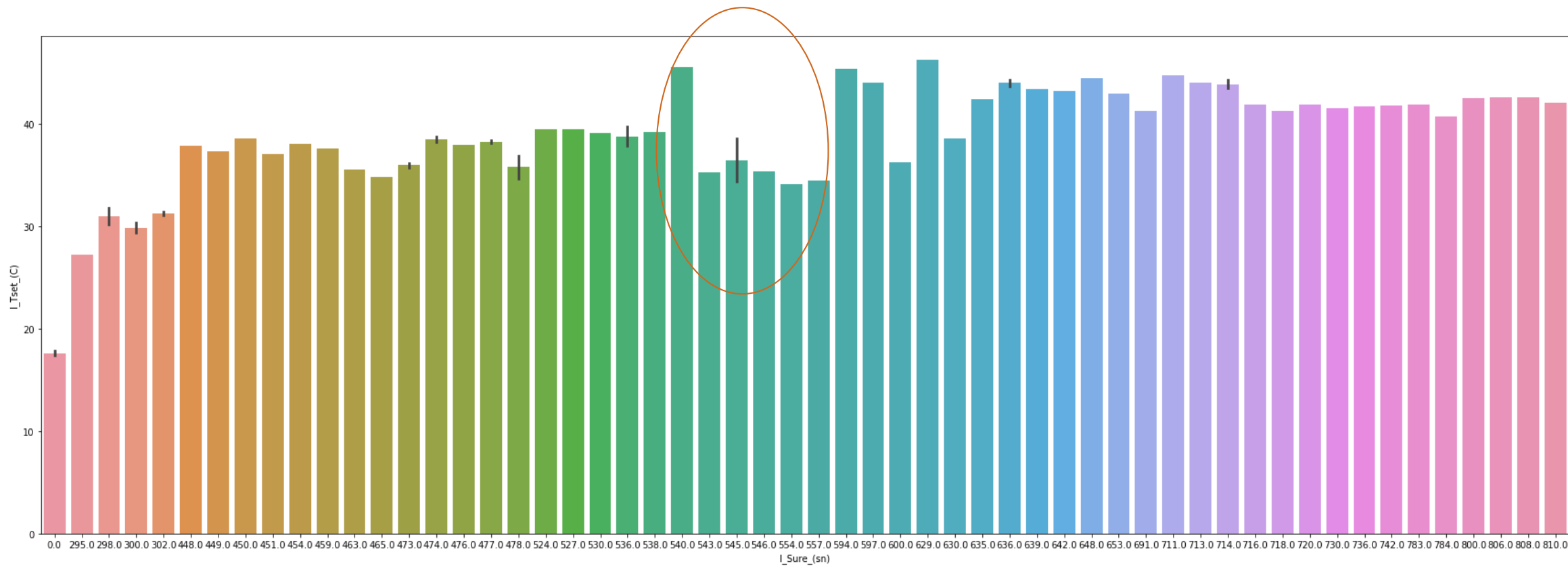
=> AY\_Tah\_(C)

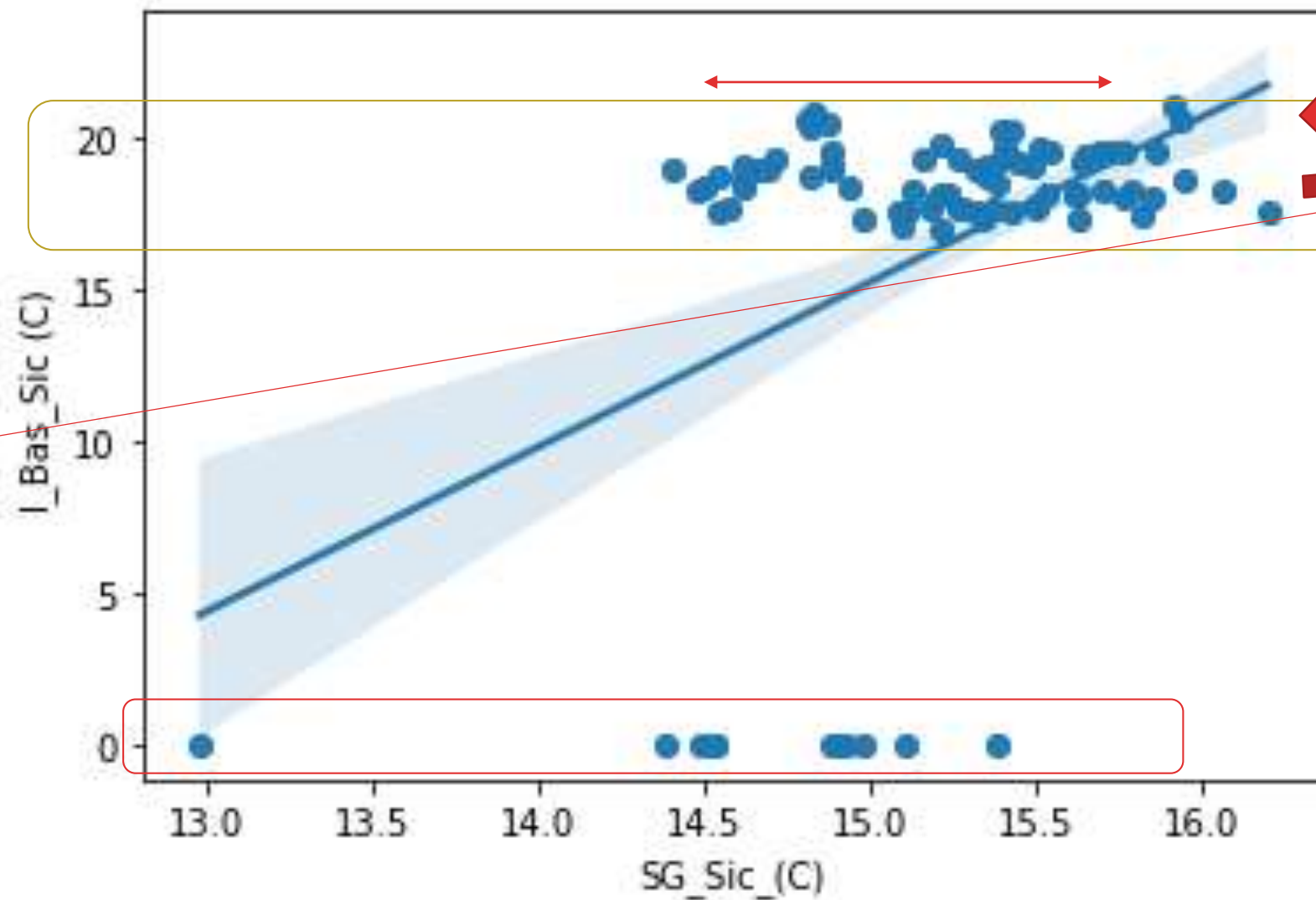
0,90 I\_Tset\_(C)

=> AY\_Tah\_(C)



There is a decrease in here, why??

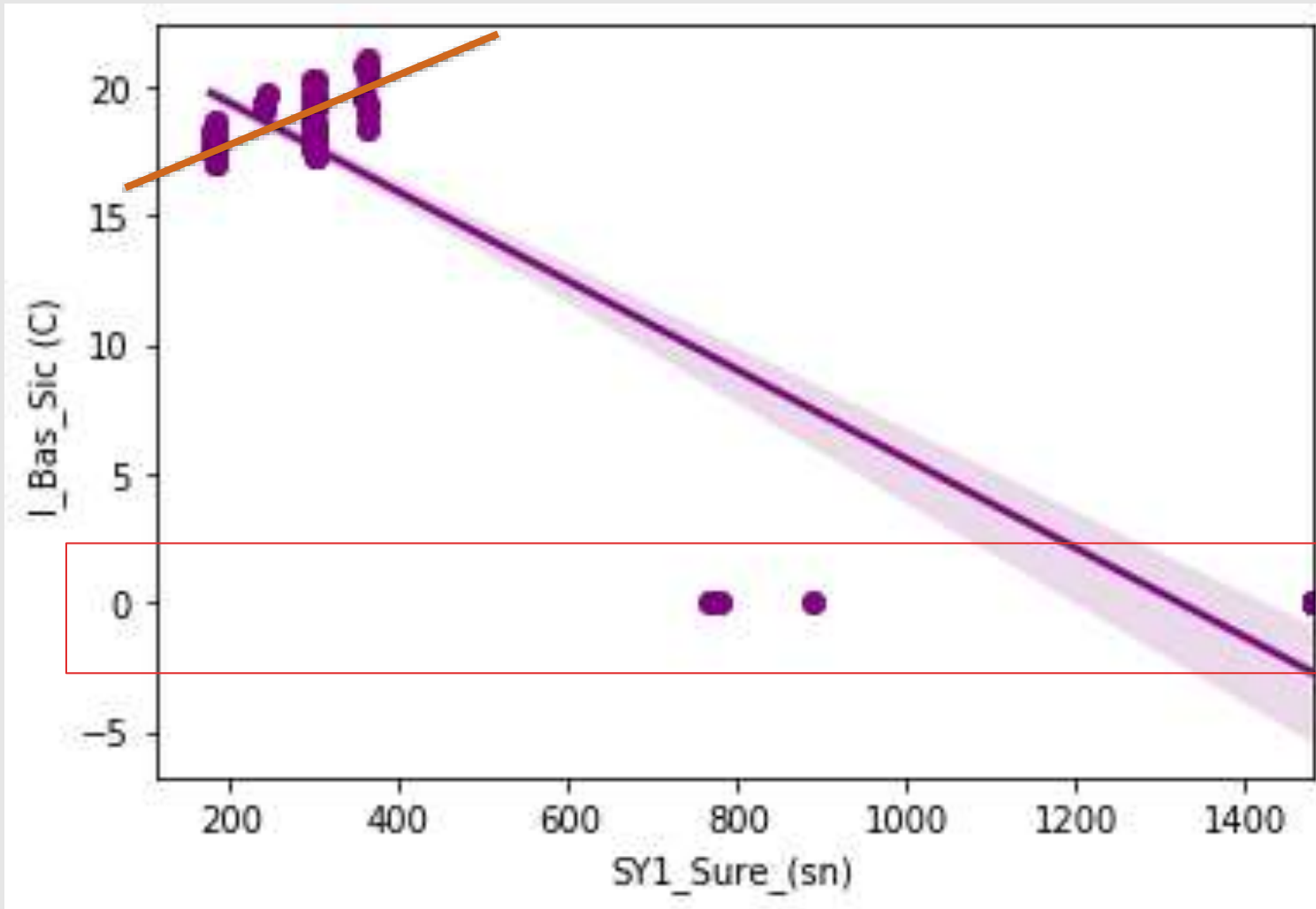




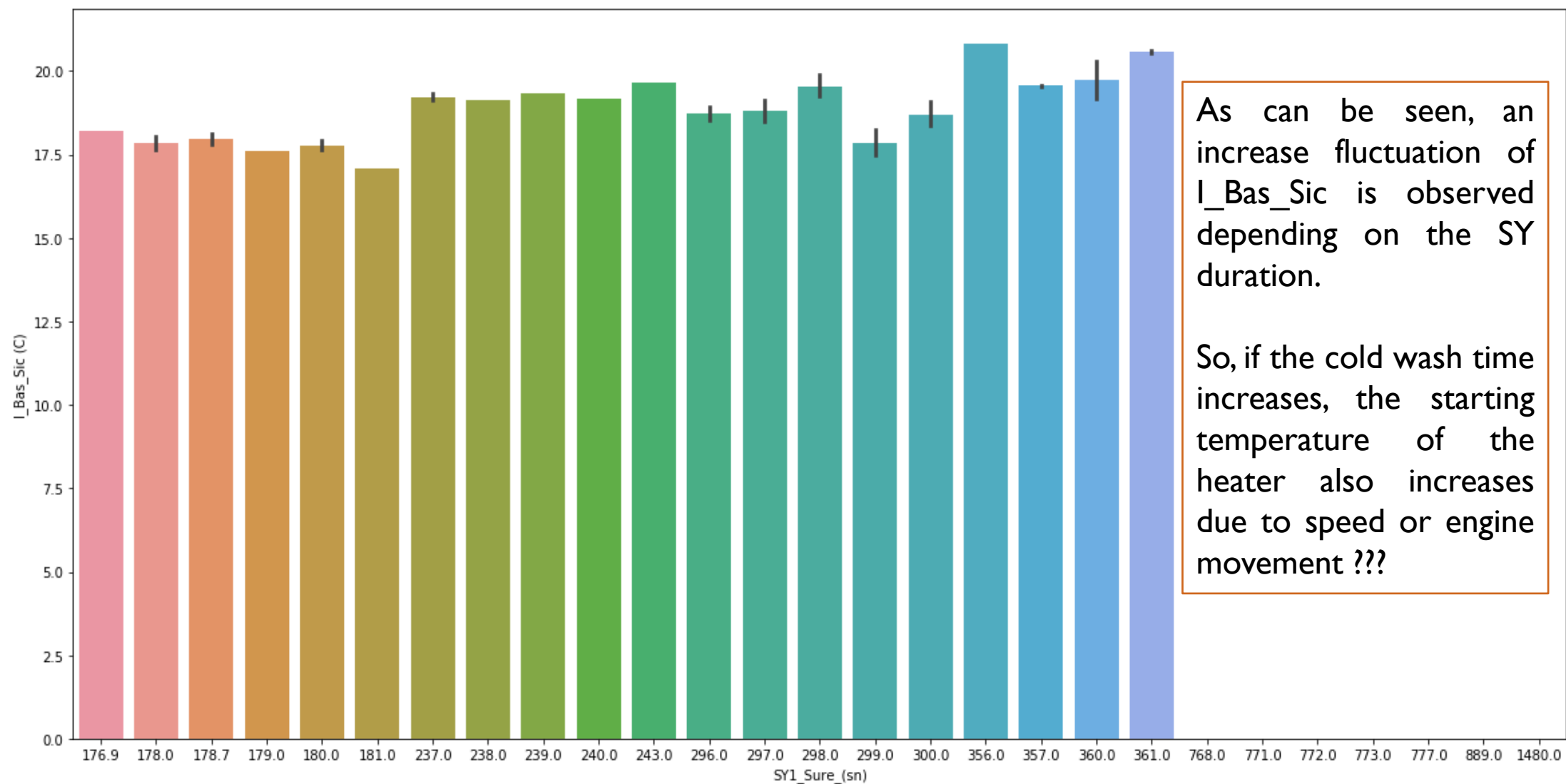
The amount of temperature in the first cold wash increases at the end of the cold wash time. Let's see if the reason for this could be SY\_sure\_(sn) ...

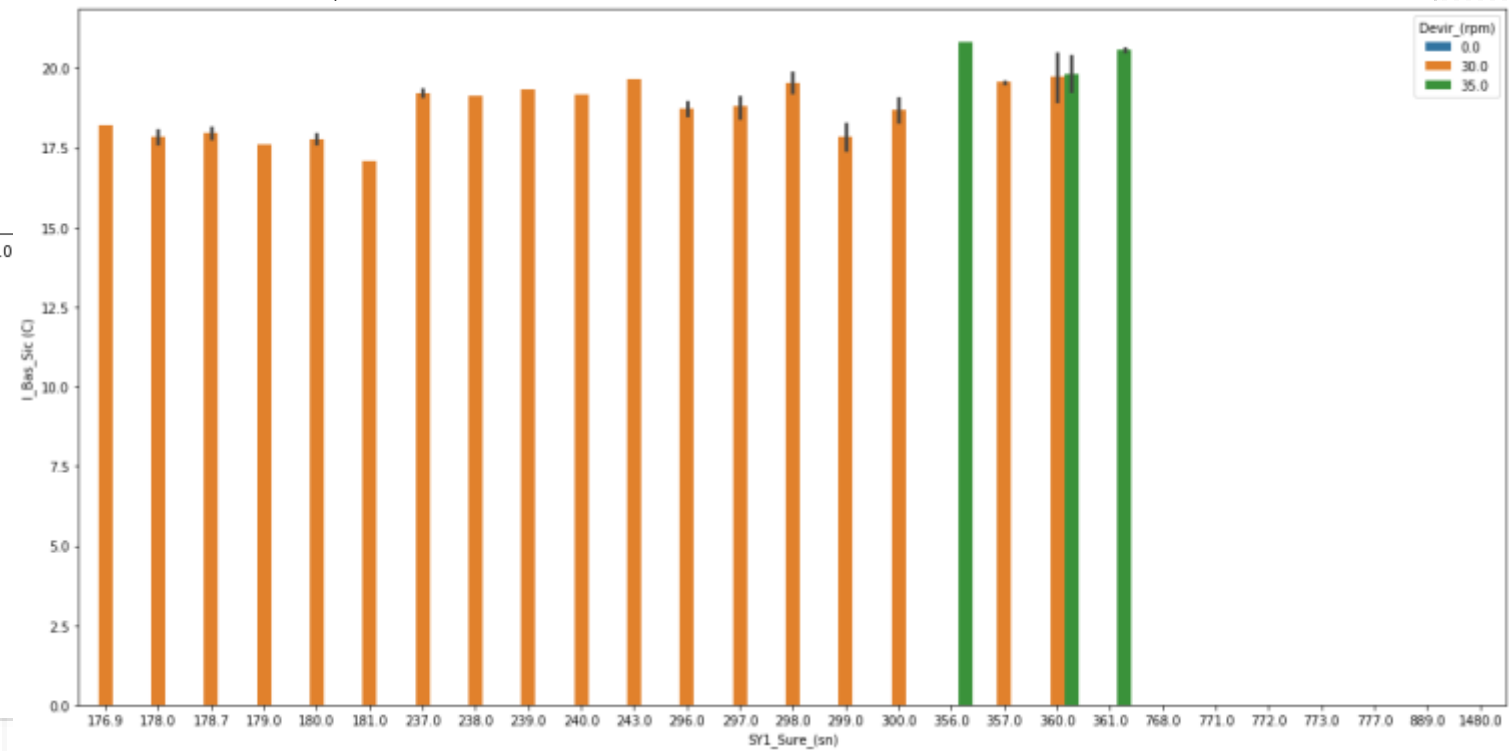
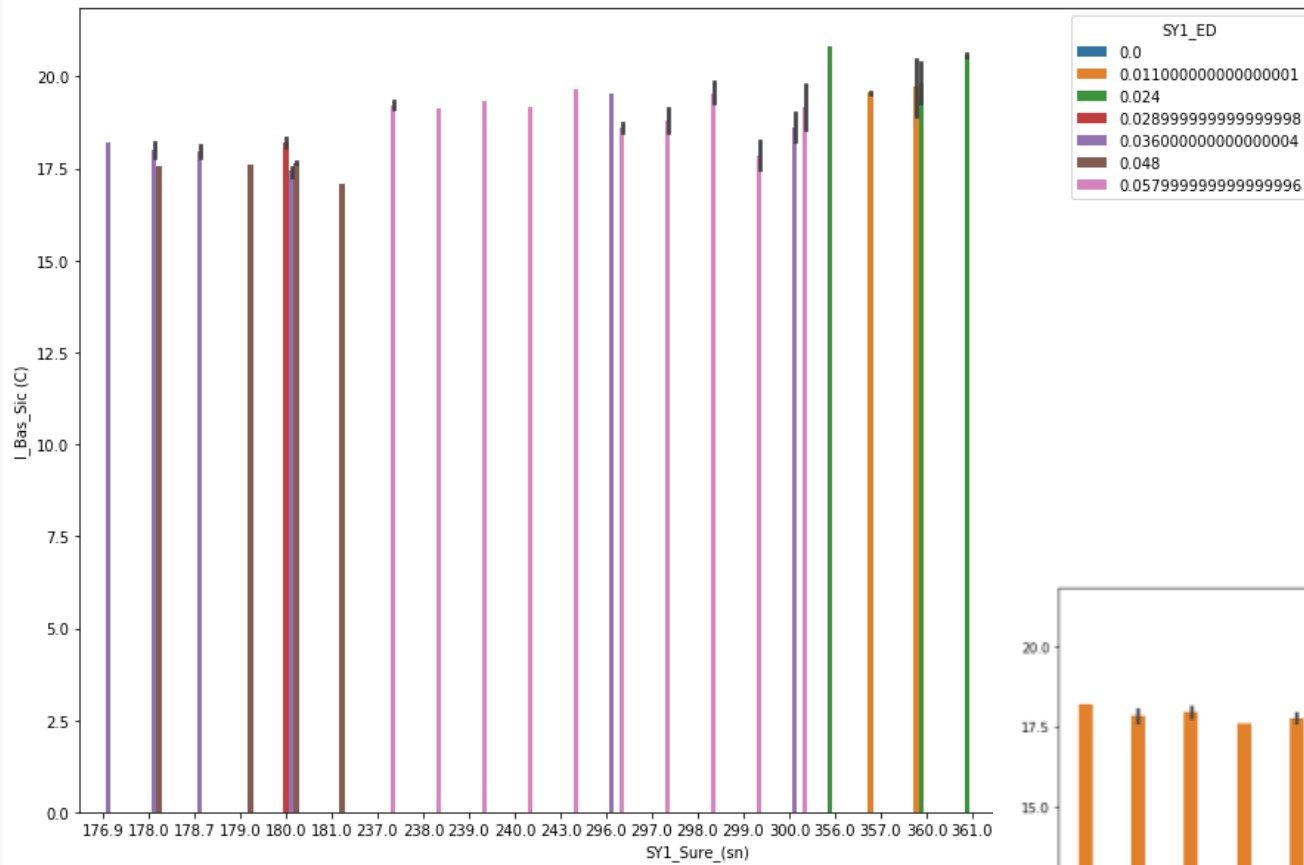
Zero values are a lot, in IQR, they've caused outliers that less than lower bound.

It should have been like this line..

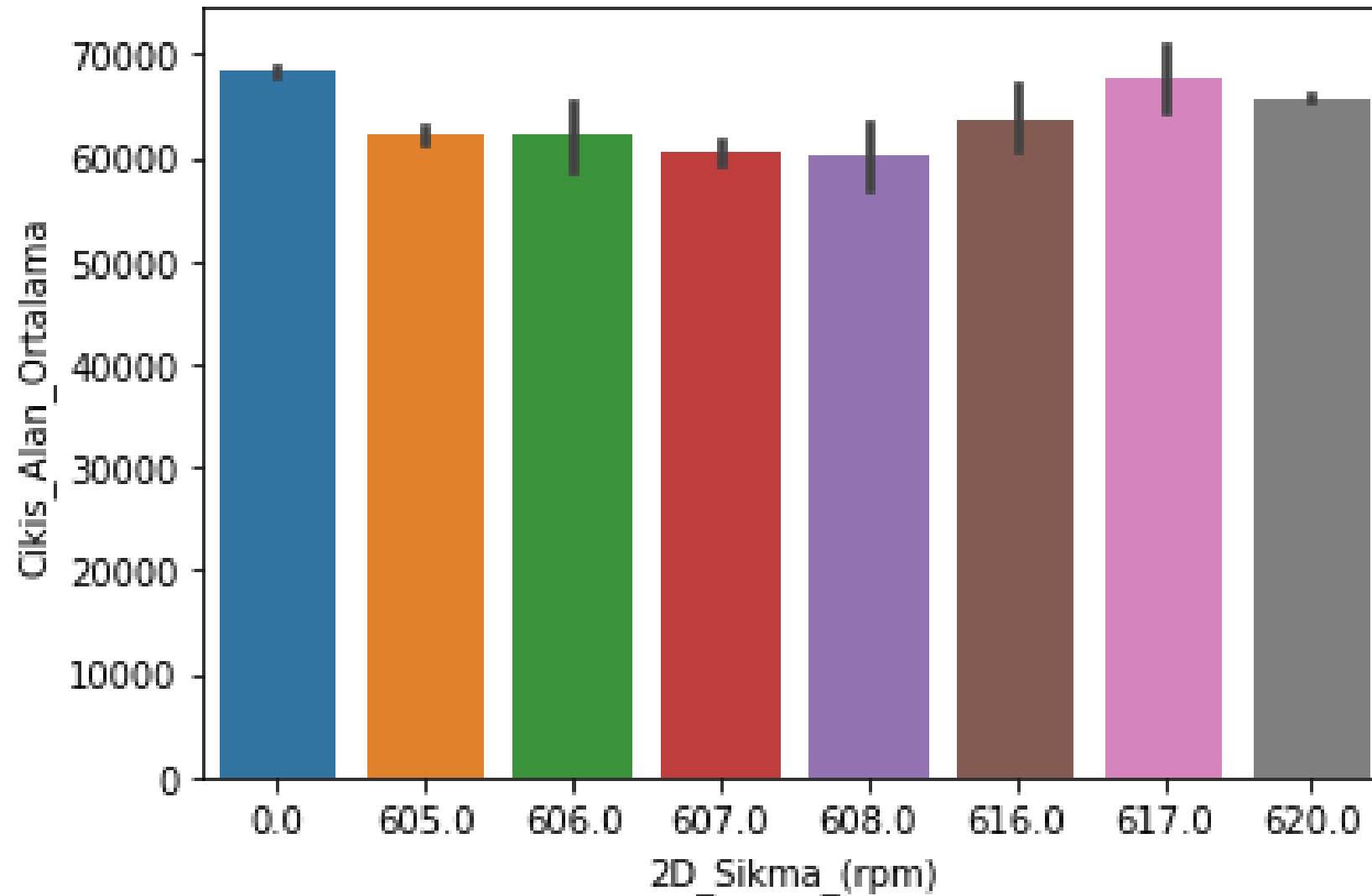


Due to zero outliers, there is a negative correlation between I\_Bas\_Sic (C) and SY1\_Sure\_(sn). We have to look the detail info for the best interpretation on the next sheet.





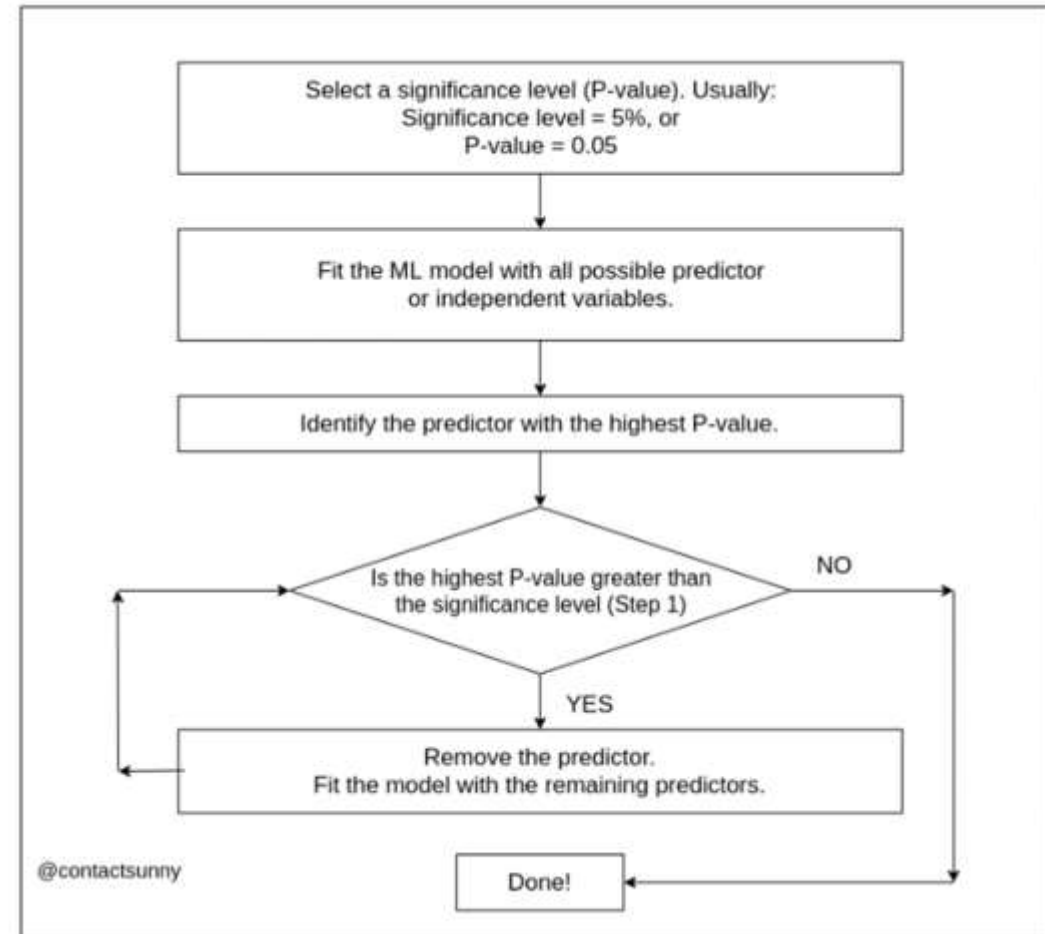




The amount which is the most intense with the shrinkage value, is 608. 0 is too high, when the spin increase, shouldn't the CAO be lower ??

# BACKWARD ELIMINATION APPROACH

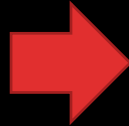
## OLS REGRESSION



If the P value found in a test is below 0.05,  
it means that there is a significant difference in comparison.

| P değeri              | Yorumu  |
|-----------------------|---|
| $0.01 \leq p < 0.05$  | İstatistiksel anlamlılık  |
| $0.001 \leq p < 0.01$ | Yüksek düzeyde istatistiksel anlamlılık   |
| $p < 0.001$           | Çok yüksek istatistiksel anlamlılık   |
| $0.05 \leq p < 0.10$  | Anlamlılık eğilimi (sınırdan anlamlılık)  |
| $p > 0.10$            | Fark tesadüftən ileri gelmiştir<br>(istatistiksel olarak anlamlı farklılık<br>saptanmamıştır) |

|     | coef       | std err  | t       | P> t  | [0.025    | 0.975]    |
|-----|------------|----------|---------|-------|-----------|-----------|
| x1  | -1411.7982 | 45.312   | -31.157 | 0.000 | -1501.361 | -1322.235 |
| x2  | -1.55e+04  | 3844.863 | -4.030  | 0.000 | -2.31e+04 | -7896.867 |
| x3  | -1.614e+04 | 3917.947 | -4.119  | 0.000 | -2.39e+04 | -8393.571 |
| x4  | -1.559e+04 | 3798.370 | -4.103  | 0.000 | -2.31e+04 | -8078.020 |
| x5  | -1.628e+04 | 4055.109 | -4.014  | 0.000 | -2.43e+04 | -8261.567 |
| x6  | -1.613e+04 | 3905.510 | -4.129  | 0.000 | -2.38e+04 | -8408.085 |
| x7  | -1.63e+04  | 3957.895 | -4.119  | 0.000 | -2.41e+04 | -8481.420 |
| x8  | 177.5966   | 43.249   | 4.106   | 0.000 | 92.113    | 263.081   |
| x9  | 3.057e+05  | 2.1e+05  | 1.455   | 0.148 | -1.09e+05 | 7.21e+05  |
| x10 | -3.345e+06 | 2.07e+06 | -1.619  | 0.108 | -7.43e+06 | 7.38e+05  |
| x11 | 145.6956   | 431.173  | 0.338   | 0.736 | -706.549  | 997.941   |
| x12 | 3.335e+04  | 1.15e+05 | 0.291   | 0.772 | -1.93e+05 | 2.6e+05   |
| x13 | -24.6923   | 7.697    | -3.208  | 0.002 | -39.907   | -9.478    |
| x14 | -3.8339    | 1107.726 | -0.003  | 0.997 | -2193.337 | 2185.670  |
| x15 | -3.667e+06 | 2.65e+06 | -1.386  | 0.168 | -8.9e+06  | 1.56e+06  |
| x16 | -366.8278  | 326.012  | -1.125  | 0.262 | -1011.215 | 277.559   |
| x17 | 233.5882   | 267.009  | 0.875   | 0.383 | -294.174  | 761.351   |
| x18 | -2.8730    | 6.792    | -0.423  | 0.673 | -16.298   | 10.552    |
| x19 | -1826.4961 | 426.477  | -4.283  | 0.000 | -2669.460 | -983.532  |
| x20 | 211.5068   | 1129.090 | 0.187   | 0.852 | -2020.224 | 2443.237  |
| x21 | 70.5015    | 76.100   | 0.926   | 0.356 | -79.917   | 220.919   |
| x22 | -1085.6314 | 1232.639 | -0.881  | 0.380 | -3522.035 | 1350.772  |
| x23 | -7.6903    | 6.254    | -1.230  | 0.221 | -20.051   | 4.670     |
| x24 | 75.5238    | 955.551  | 0.079   | 0.937 | -1813.194 | 1964.242  |
| x25 | 2.094e+06  | 5.35e+05 | 3.914   | 0.000 | 1.04e+06  | 3.15e+06  |
| x26 | -141.7146  | 124.476  | -1.138  | 0.257 | -387.750  | 104.321   |
| x27 | -1.482e+04 | 8263.429 | -1.794  | 0.075 | -3.12e+04 | 1511.764  |
| x28 | 1554.5145  | 2240.689 | 0.694   | 0.489 | -2874.375 | 5983.404  |
| x29 | 21.9687    | 44.012   | 0.499   | 0.618 | -65.025   | 108.963   |
| x30 | -11.8885   | 1123.194 | -0.011  | 0.992 | -2231.965 | 2208.188  |
| x31 | 1.92e+07   | 3.71e+07 | 0.517   | 0.606 | -5.42e+07 | 9.26e+07  |
| x32 | 324.2592   | 858.464  | 0.378   | 0.706 | -1372.560 | 2021.078  |
| x33 | -118.6065  | 45.810   | -2.589  | 0.011 | -209.154  | -28.059   |
| x34 | -11.8493   | 1123.119 | -0.011  | 0.992 | -2231.777 | 2208.079  |
| x35 | 416.9914   | 3559.369 | 0.117   | 0.907 | -6618.369 | 7452.352  |
| x36 | -4.6607    | 2.965    | -1.572  | 0.118 | -10.521   | 1.199     |
| x37 | 572.9766   | 403.536  | 1.420   | 0.158 | -224.643  | 1370.596  |
| x38 | 18.8322    | 5.224    | 3.605   | 0.000 | 8.506     | 29.158    |
| x39 | 75.4063    | 955.776  | 0.079   | 0.937 | -1813.756 | 1964.569  |
| x40 | -1.833e+07 | 3.55e+07 | -0.516  | 0.606 | -8.85e+07 | 5.18e+07  |



|     | coef       | std err  | t       | P> t  | [0.025    | 0.975]    |
|-----|------------|----------|---------|-------|-----------|-----------|
| x1  | -1424.2883 | 41.546   | -34.282 | 0.000 | -1506.354 | -1342.222 |
| x2  | -1.494e+04 | 3675.500 | -4.066  | 0.000 | -2.22e+04 | -7683.499 |
| x3  | -1.565e+04 | 3779.256 | -4.140  | 0.000 | -2.31e+04 | -8182.817 |
| x4  | -1.504e+04 | 3633.424 | -4.141  | 0.000 | -2.22e+04 | -7867.729 |
| x5  | -1.574e+04 | 3901.616 | -4.034  | 0.000 | -2.34e+04 | -8032.835 |
| x6  | -1.563e+04 | 3758.532 | -4.158  | 0.000 | -2.31e+04 | -8204.565 |
| x7  | -1.58e+04  | 3810.109 | -4.146  | 0.000 | -2.33e+04 | -8270.164 |
| x8  | 171.7781   | 41.533   | 4.136   | 0.000 | 89.739    | 253.818   |
| x9  | 3.028e+05  | 8.43e+04 | 3.592   | 0.000 | 1.36e+05  | 4.69e+05  |
| x10 | -3.3e+06   | 9.01e+05 | -3.662  | 0.000 | -5.08e+06 | -1.52e+06 |
| x11 | 249.7330   | 75.779   | 3.296   | 0.001 | 100.047   | 399.419   |
| x12 | 2.798e+04  | 5812.875 | 4.814   | 0.000 | 1.65e+04  | 3.95e+04  |
| x13 | -26.5936   | 5.047    | -5.269  | 0.000 | -36.563   | -16.625   |
| x14 | -3.155e+06 | 6.15e+05 | -5.129  | 0.000 | -4.37e+06 | -1.94e+06 |
| x15 | -1565.5358 | 297.796  | -5.257  | 0.000 | -2153.769 | -977.302  |
| x16 | -4.2560    | 0.943    | -4.512  | 0.000 | -6.119    | -2.393    |
| x17 | 1.813e+06  | 3.69e+05 | 4.919   | 0.000 | 1.08e+06  | 2.54e+06  |
| x18 | -1.027e+04 | 2158.900 | -4.757  | 0.000 | -1.45e+04 | -6005.311 |
| x19 | 41.5232    | 7.523    | 5.520   | 0.000 | 26.664    | 56.382    |
| x20 | 1.519e+07  | 2.81e+06 | 5.410   | 0.000 | 9.65e+06  | 2.07e+07  |
| x21 | -125.5091  | 16.597   | -7.562  | 0.000 | -158.294  | -92.725   |
| x22 | -5.9319    | 0.748    | -7.930  | 0.000 | -7.409    | -4.454    |
| x23 | 16.6047    | 4.412    | 3.764   | 0.000 | 7.890     | 25.319    |
| x24 | -1.437e+07 | 2.65e+06 | -5.418  | 0.000 | -1.96e+07 | -9.13e+06 |

```

=====
                        OLS Regression Results
=====
Dep. Variable:          y      R-squared:                0.944
Model:                  OLS    Adj. R-squared:            0.930
Method:                 Least Squares    F-statistic:          69.09
Date:                   Sun, 17 May 2020    Prob (F-statistic):    1.25e-73
Time:                   16:20:46    Log-Likelihood:        -1466.8
No. Observations:       180    AIC:                   3006.
Df Residuals:           144    BIC:                   3121.
Df Model:                35
Covariance Type:        nonrobust
=====

```

```

=====
                        OLS Regression Results
=====
Dep. Variable:          y      R-squared:                0.940
Model:                  OLS    Adj. R-squared:            0.931
Method:                 Least Squares    F-statistic:          106.4
Date:                   Sun, 17 May 2020    Prob (F-statistic):    3.18e-83
Time:                   16:15:31    Log-Likelihood:        -1472.6
No. Observations:       180    AIC:                   2993.
Df Residuals:           156    BIC:                   3070.
Df Model:                23
Covariance Type:        nonrobust
=====

```

```

=====
Omnibus:                3.959    Durbin-Watson:          0.961
Prob(Omnibus):           0.138    Jarque-Bera (JB):        4.910
Skew:                    -0.038    Prob(JB):                0.0859
Kurtosis:                3.806    Cond. No.                1.11e+16
=====

Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
[2] The smallest eigenvalue is 7.73e-21. This might indicate that there are
strong multicollinearity problems or that the design matrix is singular.

```

```

=====
Omnibus:                2.875    Durbin-Watson:          0.945
Prob(Omnibus):           0.237    Jarque-Bera (JB):        2.877
Skew:                    -0.100    Prob(JB):                0.237
Kurtosis:                3.586    Cond. No.                4.14e+09
=====

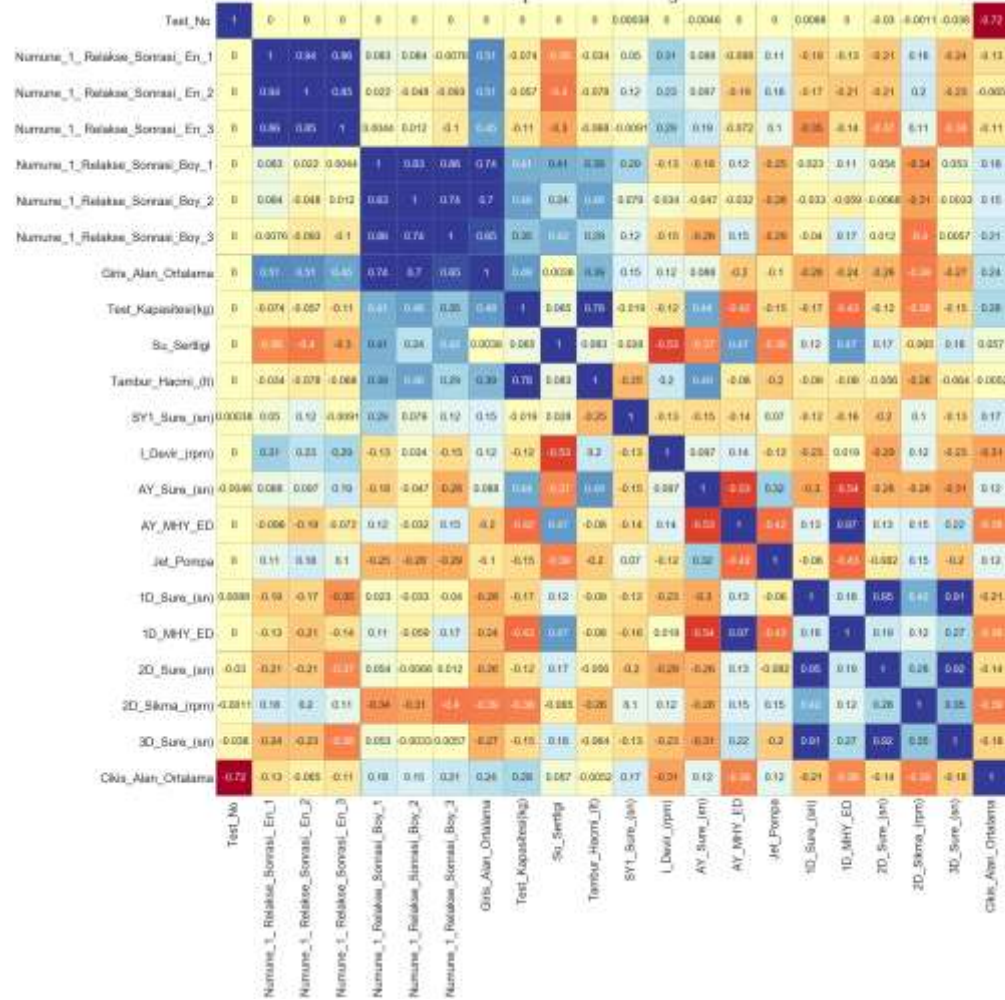
Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
[2] The condition number is large, 4.14e+09. This might indicate that there are
strong multicollinearity or other numerical problems.

```

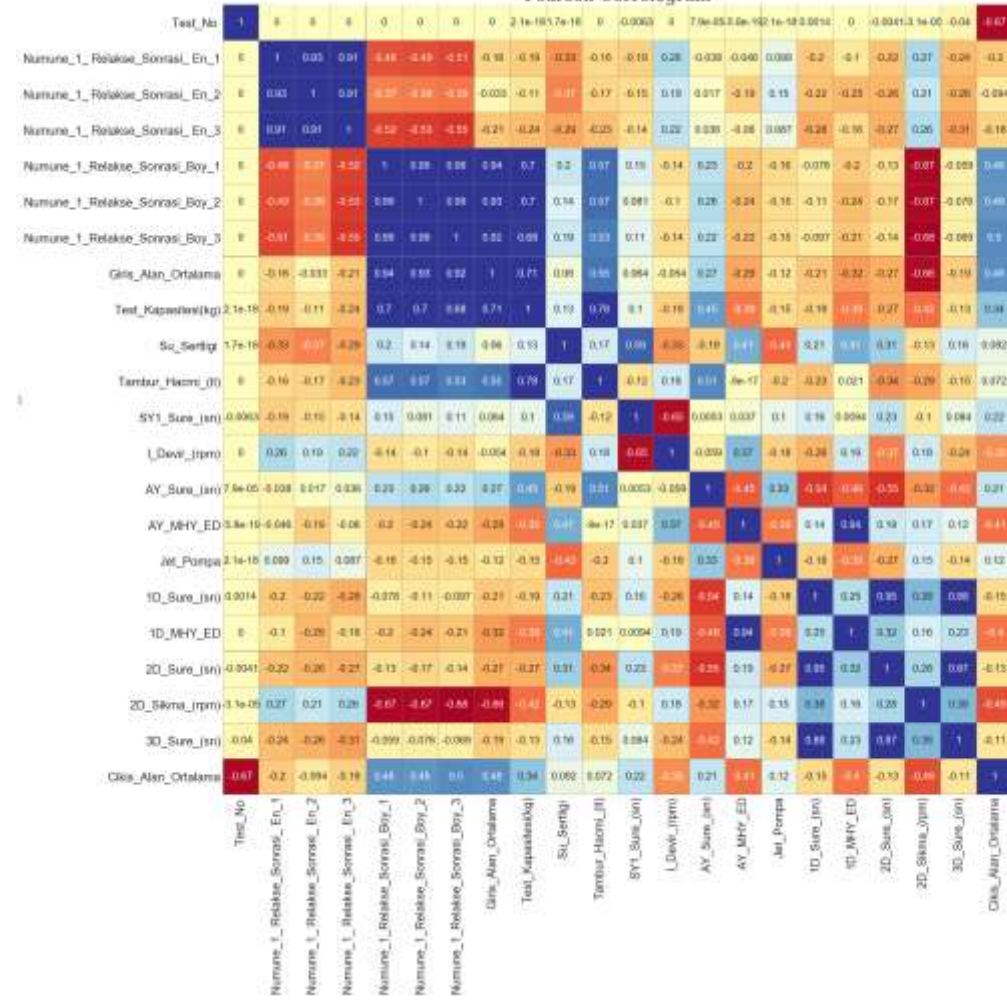
| SL=0.05 (Significance Level) |           | Column | p-value | Değişken adı    |           |
|------------------------------|-----------|--------|---------|-----------------|-----------|
| 1                            | iterasyon | 13     | 0.997   | SY1_Devir_(rpm) | çıkarılır |
| 2                            | iterasyon | 29     | 0.981   | 1D_Devir_(rpm)  | çıkarılır |
| 3                            | iterasyon | 33     | 0.993   | 2D_Devir_(rpm)  | çıkarılır |
| 4                            | iterasyon | 38     | 0.995   | 3D_Devir_(rpm)  | çıkarılır |
| 5                            | iterasyon | 23     | 0.981   | AY_Devir_(rpm)  | çıkarılır |
| 6                            | iterasyon | 34     | 0.806   | 2D_MHY_ED       | çıkarılır |
| 7                            | iterasyon | 31     | 0.695   | 2D_Su_Mik_(lt)  | çıkarılır |
| 8                            | iterasyon | 17     | 0.708   | I_Sure_(sn)     | çıkarılır |
| 9                            | iterasyon | 19     | 0.561   | I_MHY_ED        | çıkarılır |
| 10                           | iterasyon | 21     | 0.401   | AY_Su_Mik_(lt)  | çıkarılır |
| 11                           | iterasyon | 20     | 0.299   | I_Tset_(C)      | çıkarılır |
| 12                           | iterasyon | 15     | 0.427   | SG_Sic_(C)      | çıkarılır |
| 13                           | iterasyon | 25     | 0.296   | AY_Tah_(C)      | çıkarılır |
| 14                           | iterasyon | 27     | 0.209   | 1D_Su_Mik_(lt)  | çıkarılır |
| 15                           | iterasyon | 16     | 0.217   | I_Bas_Sic_(C)   | çıkarılır |
| 16                           | iterasyon | 36     | 0.115   | 3D_Su_Mik_(lt)  | çıkarılır |



Spearman correlogram

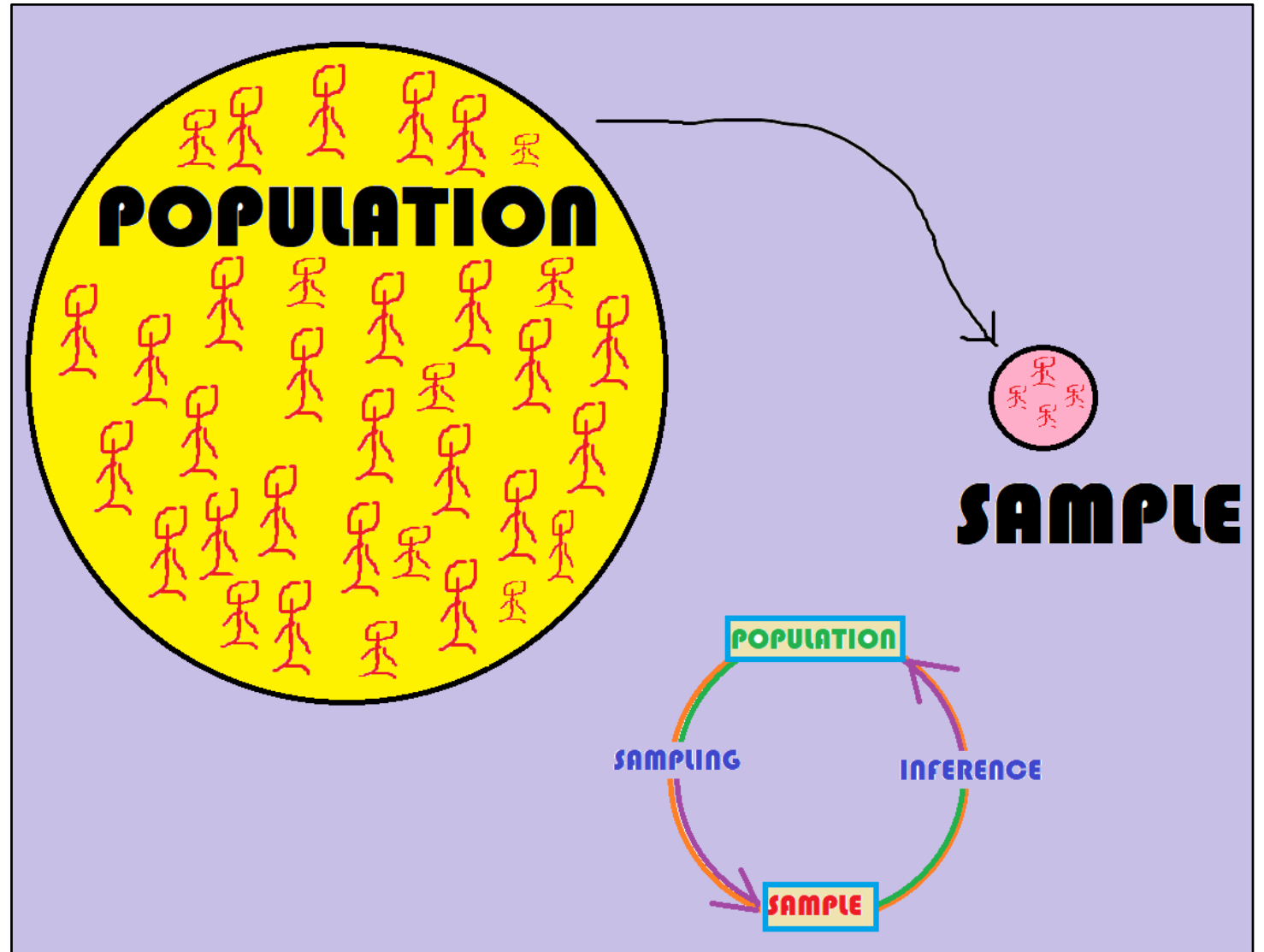


Pearson Correlogram



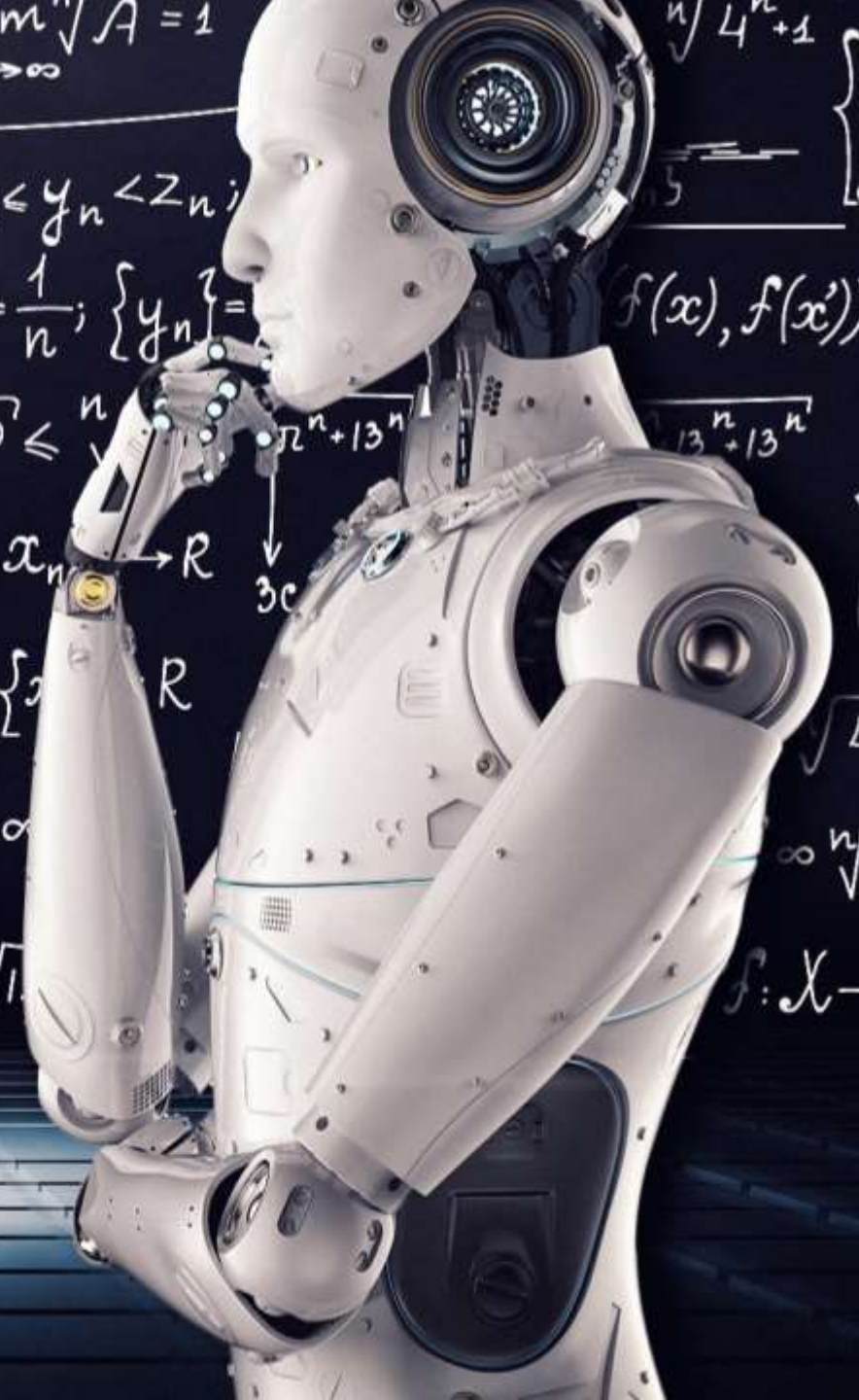
## ✓ What would be good to reduce p-values?

increase the power of analysis by taking larger sample size and doing better data collection (reducing error-for exp; zero values in our study!!!)

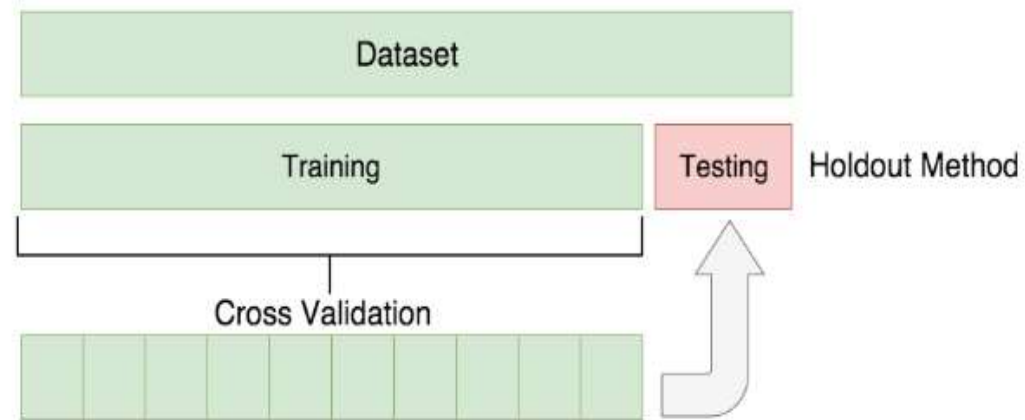




# MODELLING IN PYTHON







# CROSS VALIDATION

# Determining train size for train-test split

```
train_sizes = [1, 2, 5, 9, 13, 25, 36, 72, 90, 108, 126, 135, 144]
               (180*0.50 - 180*0.80)
```

```
##### svr
from sklearn.svm import SVR
from sklearn.model_selection import learning_curve
features = df.columns
target = 'CAO'
train_sizes, train_scores, validation_scores = learning_curve(
    estimator = SVR(),
    X = df[features],
    y = Cikis_AO[target], train_sizes = train_sizes, cv = 10,
    scoring = 'neg_mean_squared_error', shuffle=True)

print('Training scores:\n\n', train_scores)
print('\n', '-' * 70) # separator to make the output easy to read
print('\nValidation scores:\n\n', validation_scores)

train_scores_mean = np.abs(train_scores).mean(axis = 1)
validation_scores_mean = np.abs(validation_scores).mean(axis = 1)

print('Mean training scores\n\n', pd.Series(train_scores_mean,
                                             index = train_sizes))

print('\n', '-' * 20) # separator
print('\nMean validation scores\n\n', pd.Series(validation_scores_mean,
                                                index = train_sizes))

import matplotlib.pyplot as plt

plt.style.use('seaborn')
plt.plot(train_sizes, train_scores_mean, label = 'Training error')
plt.plot(train_sizes, validation_scores_mean, label = 'Validation error')
plt.ylabel('MSE', fontsize = 14)
plt.xlabel('Training set size', fontsize = 14)
plt.title('Learning curves for a SVR', fontsize = 18, y = 1.03)
plt.legend()
plt.ylim(-3,3)
```

```
##### GBM
from sklearn.ensemble import GradientBoostingRegressor
from sklearn.model_selection import learning_curve
features = df.columns
target = 'CAO'
train_sizes, train_scores, validation_scores = learning_curve(
    estimator = GradientBoostingRegressor(),
    X = df[features],
    y = Cikis_AO[target], train_sizes = train_sizes, cv = 10,
    scoring = 'neg_mean_squared_error', shuffle=True)

print('Training scores:\n\n', train_scores)
print('\n', '-' * 70) # separator to make the output easy to read
print('\nValidation scores:\n\n', validation_scores)

train_scores_mean = np.abs(train_scores).mean(axis = 1)
validation_scores_mean = np.abs(validation_scores).mean(axis = 1)

print('Mean training scores\n\n', pd.Series(train_scores_mean,
                                             index = train_sizes))

print('\n', '-' * 20) # separator
print('\nMean validation scores\n\n', pd.Series(validation_scores_mean,
                                                index = train_sizes))

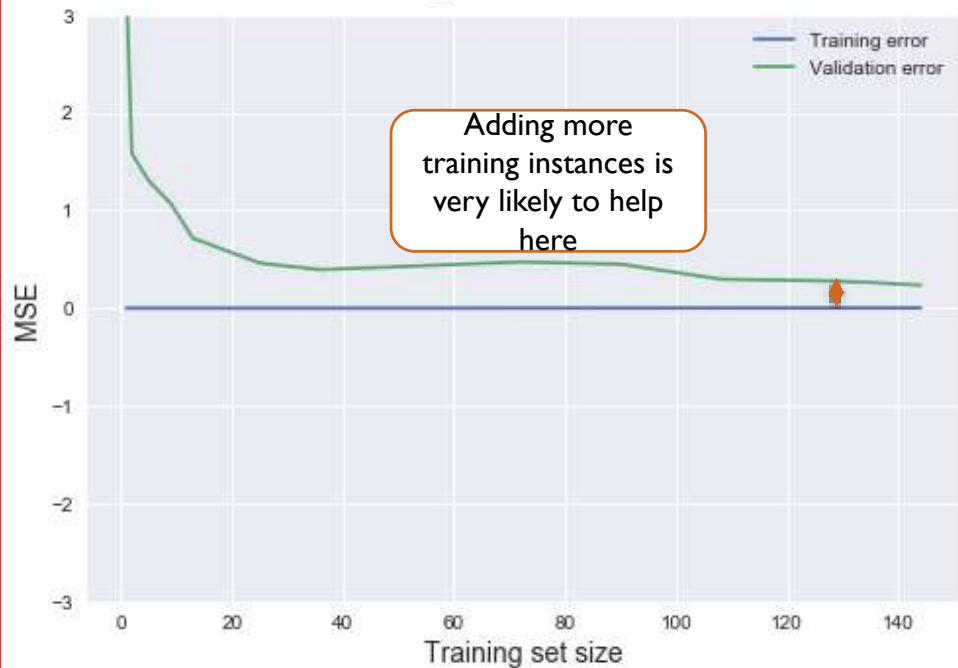
import matplotlib.pyplot as plt

plt.style.use('seaborn')
plt.plot(train_sizes, train_scores_mean, label = 'Training error')
plt.plot(train_sizes, validation_scores_mean, label = 'Validation error')
plt.ylabel('MSE', fontsize = 14)
plt.xlabel('Training set size', fontsize = 14)
plt.title('Learning curves for a GBM', fontsize = 18, y = 1.03)
plt.legend()
plt.ylim(-3,3)
```

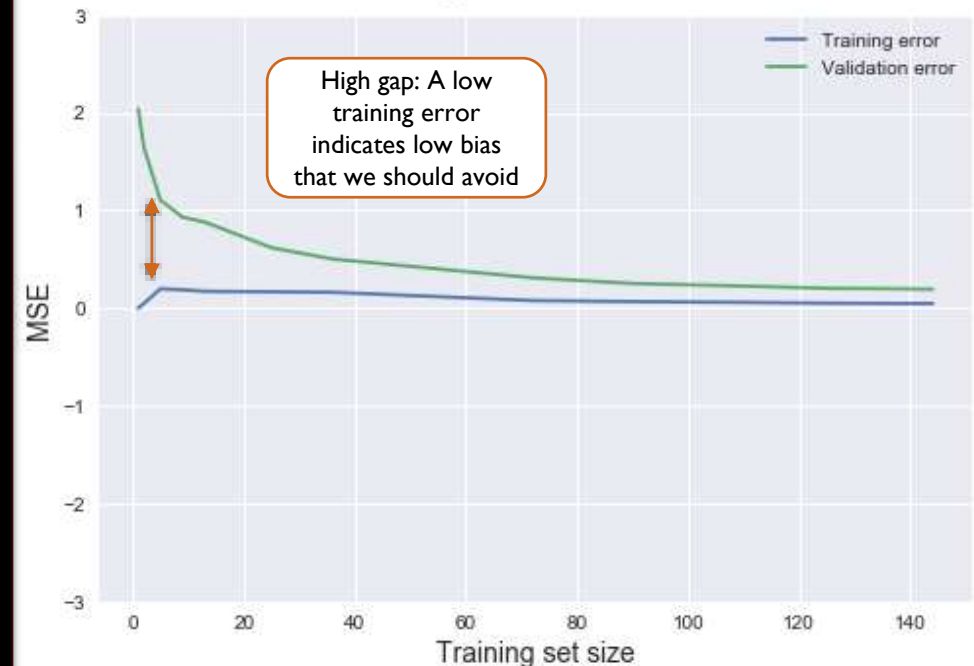
# Determining train size for train-test split

- Adding more training instances
- Adding more features
- Feature selection
- Hyperparameter optimization

Learning curves for a GBM



Learning curves for a SVR



Mean training scores

|     |              |
|-----|--------------|
| 1   | 0.000000e+00 |
| 2   | 9.147134e-08 |
| 5   | 9.340545e-08 |
| 9   | 9.644352e-08 |
| 13  | 9.622787e-08 |
| 25  | 2.324368e-06 |
| 36  | 6.548008e-05 |
| 72  | 8.765447e-04 |
| 90  | 1.677802e-03 |
| 108 | 2.348792e-03 |
| 126 | 2.804317e-03 |
| 135 | 3.075798e-03 |
| 144 | 3.163698e-03 |

dtype: float64

Mean training scores

|     |          |
|-----|----------|
| 1   | 0.000000 |
| 2   | 0.048002 |
| 5   | 0.198824 |
| 9   | 0.188524 |
| 13  | 0.172998 |
| 25  | 0.168690 |
| 36  | 0.162902 |
| 72  | 0.078362 |
| 90  | 0.068138 |
| 108 | 0.060219 |
| 126 | 0.051240 |
| 135 | 0.049136 |
| 144 | 0.048359 |

dtype: float64

Mean validation scores

|     |          |
|-----|----------|
| 1   | 3.344291 |
| 2   | 1.583766 |
| 5   | 1.307148 |
| 9   | 1.071880 |
| 13  | 0.717403 |
| 25  | 0.462318 |
| 36  | 0.394996 |
| 72  | 0.473935 |
| 90  | 0.451119 |
| 108 | 0.297287 |
| 126 | 0.280765 |
| 135 | 0.264330 |
| 144 | 0.235232 |

dtype: float64

Mean validation scores

|     |          |
|-----|----------|
| 1   | 2.039337 |
| 2   | 1.646903 |
| 5   | 1.105167 |
| 9   | 0.931225 |
| 13  | 0.881341 |
| 25  | 0.618940 |
| 36  | 0.503384 |
| 72  | 0.311459 |
| 90  | 0.253115 |
| 108 | 0.229787 |
| 126 | 0.202319 |
| 135 | 0.200815 |
| 144 | 0.193558 |

dtype: float64

Let's split 70:30

126

Data multiplexing,  
multiplexing variables extracted from df  
before fitting

```
df.drop(['Durulama_Sayisi',  
        'SY1_Devir_(rpm)',  
        '1D_Devir_(rpm)',  
        '2D_Devir_(rpm)',  
        '3D_Devir_(rpm)',  
        'Deterjan_Miktari(gr)',  
        '3D_MHY_ED',  
        'SY1_ED'], axis=1, inplace=True)
```

GBM – CROSS VALIDATION MEAN SCORE: 93,16% / STD: 0.04

SVR – CROSS VALIDATION MEAN SCORE: 90,36% / STD: 0.04

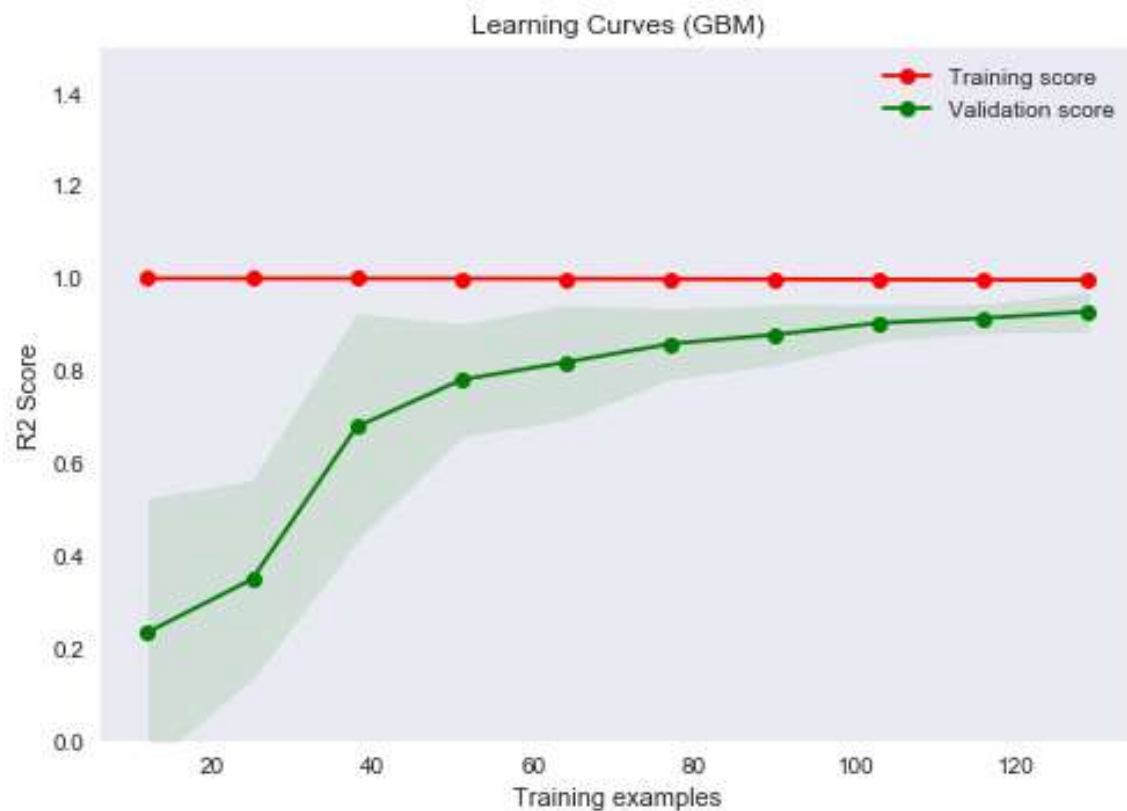
RF – CROSS VALIDATION MEAN SCORE: 87,59% / STD: 0.05

GLM – CROSS VALIDATION MEAN SCORE: 87,79% / STD: 0.06

AdaBoost – CROSS VALIDATION MEAN SCORE: 82,21% / STD: 0.07



GBM – CROSS VALIDATION MEAN SCORE: 93,16% / STD: 0.04



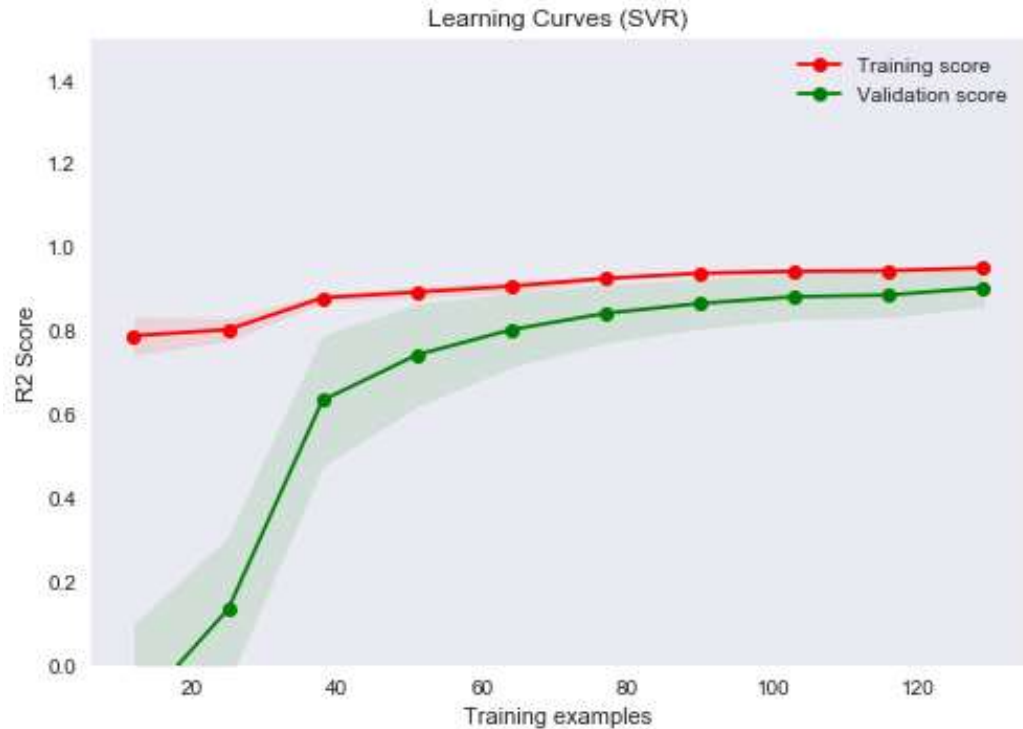
```
#model5 - Gradient Descent

from sklearn.ensemble import GradientBoostingRegressor
from sklearn.model_selection import cross_val_score
gb_reg = GradientBoostingRegressor()
gb_scores = cross_val_score(gb_reg, x_train, y_train, cv=10)
print(gb_scores)
# [0.88337849 0.95637685 0.94947434 0.96500836 0.96981316 0.84037879
#  0.97163019 0.87310394 0.93085526 0.976291 ]

print(gb_scores.mean())
# 0.9316310368054921
print(gb_scores.std())
# 0.046020003468920455

from sklearn.model_selection import learning_curve
title = "Learning Curves (GBM)"
cv = 10
plot_learning_curve(gb_reg, title,
                    x_train, y_train, ylim=(0, 1.5),
                    cv=cv, n_jobs=-1);
```

SVR – CROSS VALIDATION MEAN SCORE: 90,36% / STD: 0.04

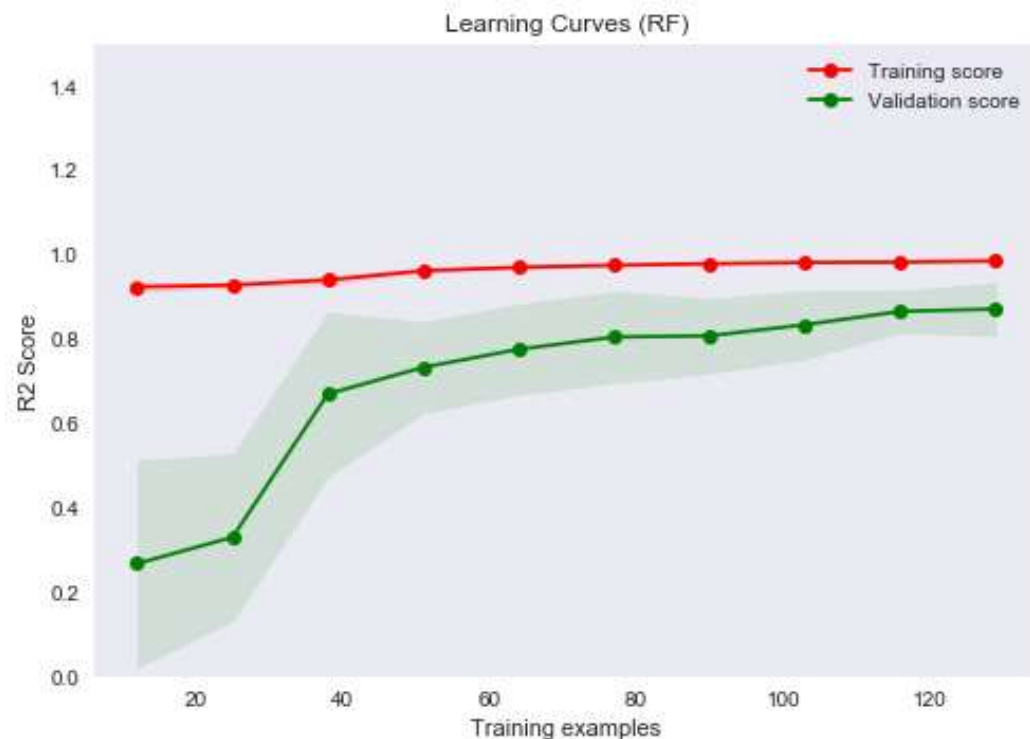


```
#model2 - SVR
from sklearn.svm import SVR

from sklearn.model_selection import cross_val_score
svr_reg = SVR()
svr_scores = cross_val_score(svr_reg, x_train, y_train, cv=10)
print(svr_scores)
# [0.82345469 0.94368955 0.84945493 0.89961801 0.88704056 0.89142335
# 0.89996566 0.8452074 0.95932952 0.97146793]
print(svr_scores.mean())
# 0.8970651587841191
print(svr_scores.std())
# 0.047019328549225234

# Assessing model performance
# Plot learning curve
from sklearn.model_selection import learning_curve
title = "Learning Curves (SVR)"
cv = 10
plot_learning_curve(svr_reg, title,
                    x_train, y_train, ylim=(0, 1.5),
                    cv=cv, n_jobs=-1);
```

RF – CROSS VALIDATION MEAN SCORE: 87,59% / STD: 0.05



```
# model3- RandomForest
from sklearn.ensemble import RandomForestRegressor

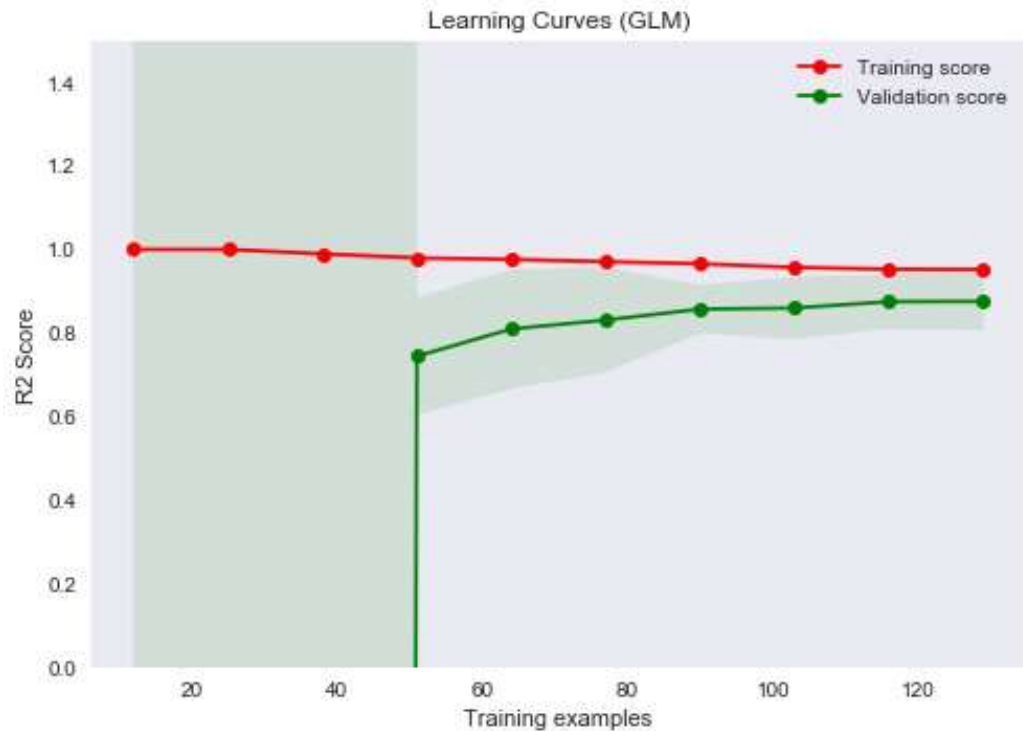
from sklearn.model_selection import cross_val_score
rf_reg = RandomForestRegressor()
rf_scores = cross_val_score(rf_reg, x_train, y_train, cv=10)

print(rf_scores)
# [0.81600877 0.92538804 0.87121921 0.92250344 0.88830655 0.75914512
#  0.90155346 0.82045205 0.81484911 0.94420484]

print(rf_scores.mean())
# 0.8663630577214168
print(rf_scores.std())
# 0.057646548431513824

from sklearn.model_selection import learning_curve
title = "Learning Curves (RF)"
cv = 10
plot_learning_curve(rf_reg, title,
                    x_train, y_train, ylim=(0, 1.5),
                    cv=cv, n_jobs=-1);
```

GLM – CROSS VALIDATION MEAN SCORE: 87,79% / STD: 0.06



```
#model1- linear regression

from sklearn.linear_model import LinearRegression

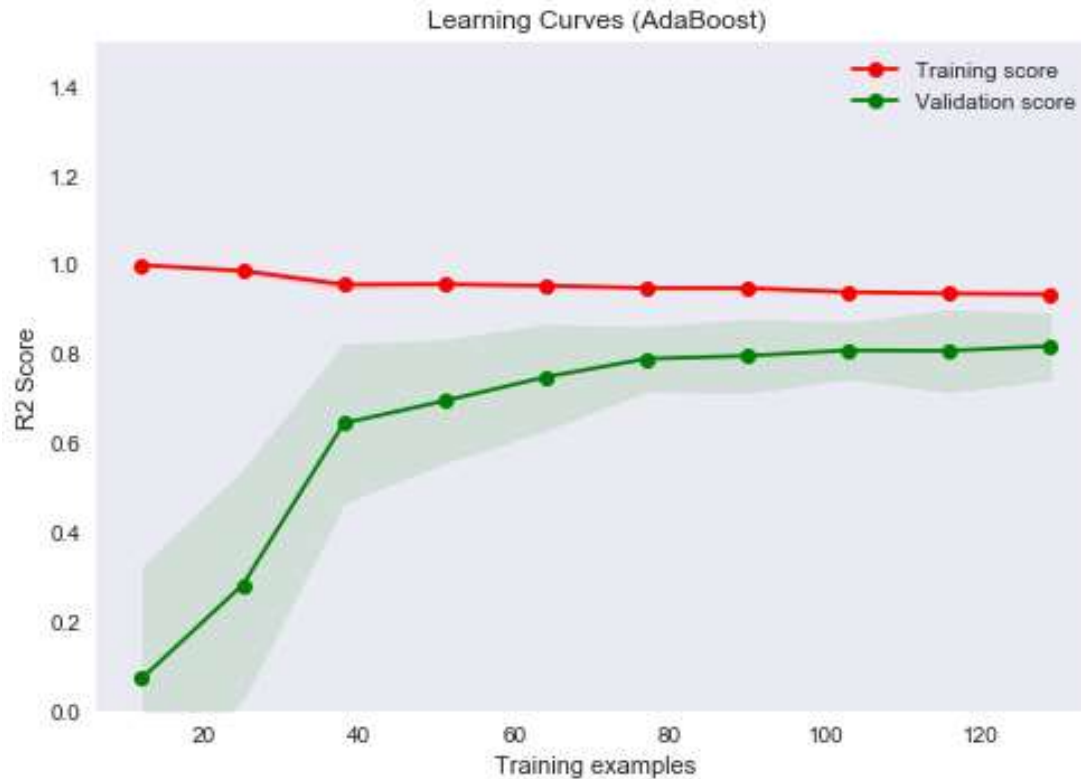
from sklearn.model_selection import cross_val_score
lr = LinearRegression()
lr_scores = cross_val_score(lr, x_train, y_train, cv=10)
print(lr_scores)
# [0.80768775 0.94315428 0.929207    0.95287587 0.91778322 0.88557883
#  0.62466177 0.69620303 0.8999114  0.9549427 ]

print(lr_scores.mean())
# 0.8612005846129721
print(lr_scores.std())
# 0.10948336320814078

from sklearn.model_selection import learning_curve
title = "Learning Curves (GLM)"
cv = 10
plot_learning_curve(lr, title,
                    x_train, y_train, ylim=(0.7, 1.0),
                    cv=cv, n_jobs=-1);
```



## AdaBoost – CROSS VALIDATION MEAN SCORE: 82,21% / STD: 0.07



```
#model4 - AdaBoost

from sklearn.ensemble import AdaBoostRegressor

from sklearn.model_selection import cross_val_score
ab_reg = AdaBoostRegressor()
ab_scores = cross_val_score(ab_reg, x_train, y_train, cv=10)
print(ab_scores)
# [0.77385224 0.86439727 0.8469751 0.92960135 0.81351651 0.75816734
# 0.82270168 0.64031523 0.6504978 0.90786072]

print(ab_scores.mean())
# 0.8007885251110226
print(ab_scores.std())
# 0.09260657075819591

from sklearn.model_selection import learning_curve
title = "Learning Curves (AdaBoost)"
cv = 10
plot_learning_curve(ab_reg, title, |
                    x_train, y_train, ylim=(0, 1.5),
                    cv=cv, n_jobs=-1);
```

# INTERPRETATION OF LEARNING CURVES

- When the model overfits, it means that it performs well on the training set, but not on the validation set. Accordingly, the model is not able to generalize to unseen data. If the model is overfitting, the learning curve will present a **gap** between the training and validation scores. Two common solutions for overfitting are reducing the complexity of the model and/or collect more data.
- On the other hand, underfitting means that the model is not able to perform well in either training or validations sets. In those cases, the learning curves will converge to a low score value. When the model underfits, gathering more data is not helpful because the model is already not being able to learn the training data. Therefore, the best approaches for these cases are to improve the model (e.g., tuning the hyperparameters) or to improve the quality of the data (e.g., collecting a different set of features).

# Hyperparameter optimization – GBM/XGBoost

```
#model5 - Gradient Descent
```

```
from sklearn.ensemble import GradientBoostingRegressor
from sklearn.model_selection import GridSearchCV
model_gbm = GradientBoostingRegressor()

grid_param_gbm = [{ 'max_depth': [4,5,6,7,8,10,12,15],
                    'learning_rate': [0.05,0.02,0.01,0.1,0.15,0.2,0.3,0.4,0.5],
                    'n_estimators': [10,30,50,100,200,300,500],
                    }]
```

```
gs_gbm = GridSearchCV(model_gbm,
                      param_grid=grid_param_gbm,
                      scoring = 'neg_root_mean_squared_error',
                      cv=10,
                      n_jobs = -1)
```

```
grid_search_gbm = gs_gbm.fit(x_train, y_train)
best_model = grid_search_gbm.best_score_
best_parameters = grid_search_gbm.best_params_
print(best_model)
# 0.19228813093340386
```

```
print(best_parameters)
# {'learning_rate': 0.15, 'max_depth': 4, 'n_estimators': 500}
# ['learning_rate': 0.1, 'max_depth': 4, 'n_estimators': 200]
```

```
model_gbm = GradientBoostingRegressor(learning_rate=0.1,
                                     max_depth = 4,
                                     n_estimators=200)
```

```
model_gbm.fit(x_train, y_train)
pred_gbm = model_gbm.predict(x_test)
```

```
from sklearn.model_selection import GridSearchCV
from xgboost import XGBModel

estimator = XGBModel(objective= 'reg:linear',
                     nthread=4,
                     seed=12345
                     )

grid_param_xgb = [{ 'max_depth': range (2, 10, 1),
                    'n_estimators': range(60, 300, 40),
                    'learning_rate': [0.05,0.01,0.1,0.3],
                    'gamma': [0,0.3,0.6,1],
                    'booster': ['gbtree', 'dart']
                    }]

grid_search = GridSearchCV(estimator=estimator,
                          param_grid=grid_param_xgb,
                          scoring = 'neg_root_mean_squared_error',
                          n_jobs = 20,
                          cv = 10,
                          verbose=True
                          )

grid_search.fit(sparse_train,label_train)

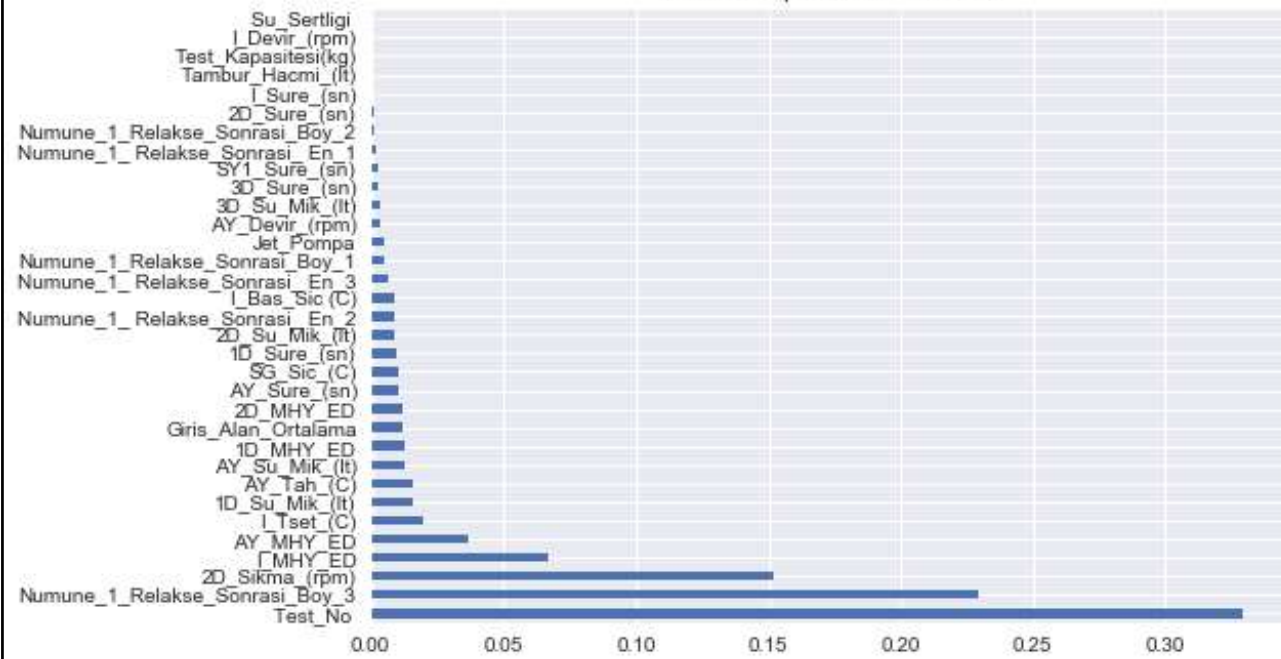
grid_search.best_estimator_
grid_search.best_params_
```

```
xgb_params = { 'booster': 'gbtree',
               'gamma': 0.6,
               'learning_rate': 0.1,
               'max_depth': 4,
               'n_estimators': 260,
               'objective': 'reg:linear'
               }
```

```
xgb_params['eval_metric'] = "rmse"
evallist = [(dense_test, 'eval'), (dense_train, 'train')]
num_round = 5000
bst = xgb.train(xgb_params, dense_train, num_round, evallist,early_stopping_rounds=10)

bst.save_model('1.model')
```

Feature Importance with GBM



```
##### feature importance #####
model_gbm.fit(x_train, y_train)
print(model_gbm.feature_importances_)
#plot graph of feature importances for better visualization
feat_importances_gb = pd.Series(model_gbm.feature_importances_, index=x_test.columns)
feat_importances_gb.nlargest(33).plot(kind='barh')
plt.title('Feature Importance with GBM')
plt.show()
```

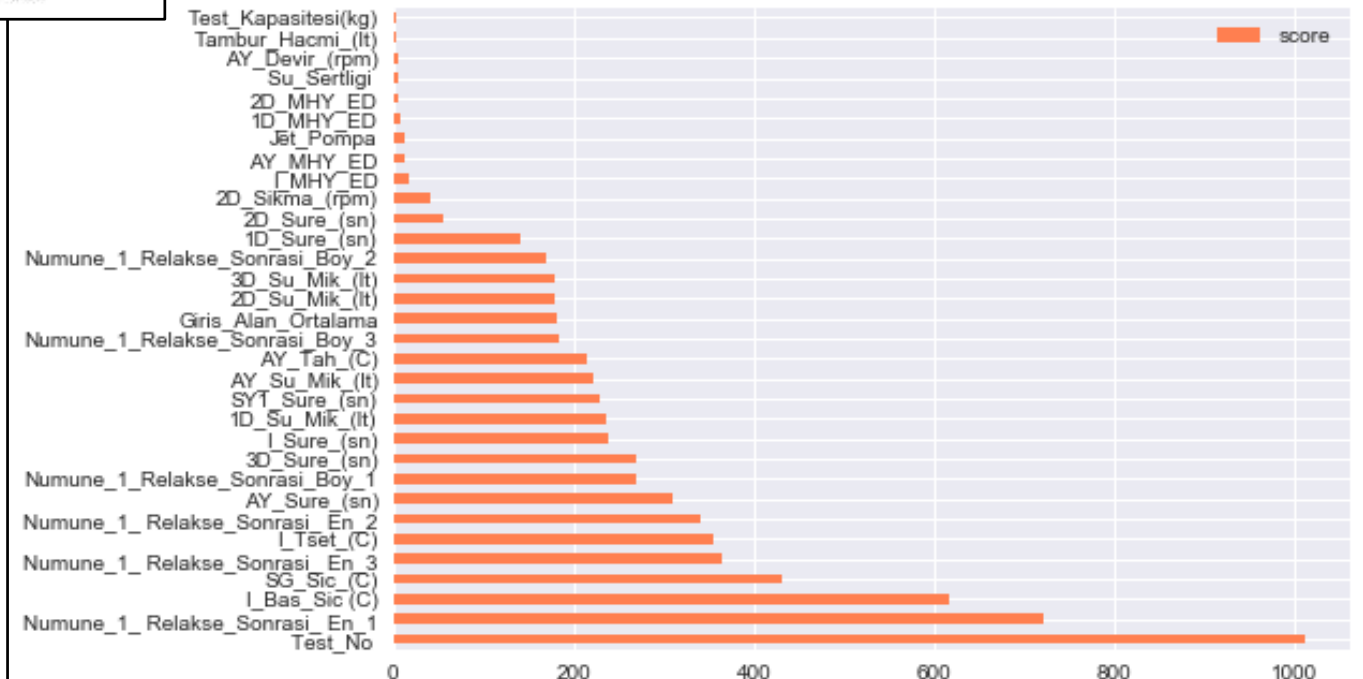
```
#prediction
ypred = bst.predict(dense_test, ntree_limit=bst.best_ntree_limit)

ypred.shape, label_test.shape

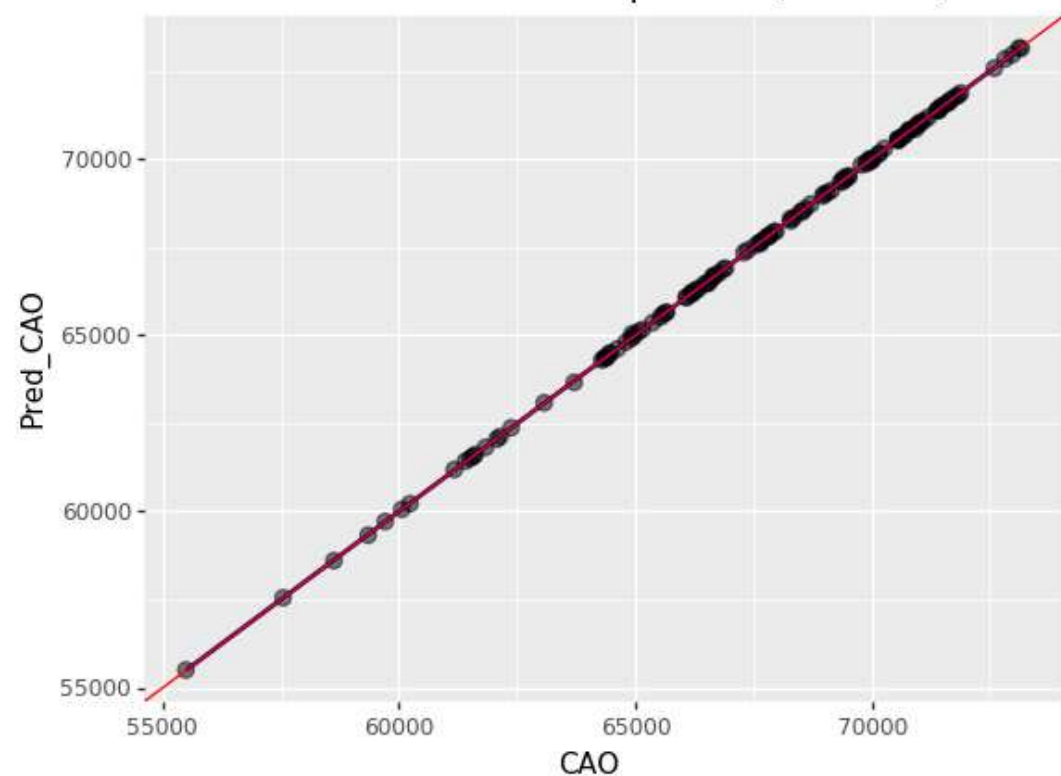
ypred_train = bst.predict(dense_train, ntree_limit=bst.best_ntree_limit)

# feature_imp_xgb=pd.DataFrame(bst.get_fscore().items(), columns=['Feature','importance']).sort_values('importance')
# #plot graph of feature importances for better visualization

feature_important = bst.get_score(importance_type='weight')
keys = list(feature_important.keys())
values = list(feature_important.values())
data = pd.DataFrame(data=values, index=keys, columns=["score"]).sort_values(by = "score", ascending=False)
data.plot(kind='barh', color='coral')
data.plot.title('Feature Importance with XGBoost',fontsize=50, fontfamily='serif')
data.plot.xticks(rotation=90, size=25)
data.plot.show()
```



Model Performance Graph-GBM (Train set)



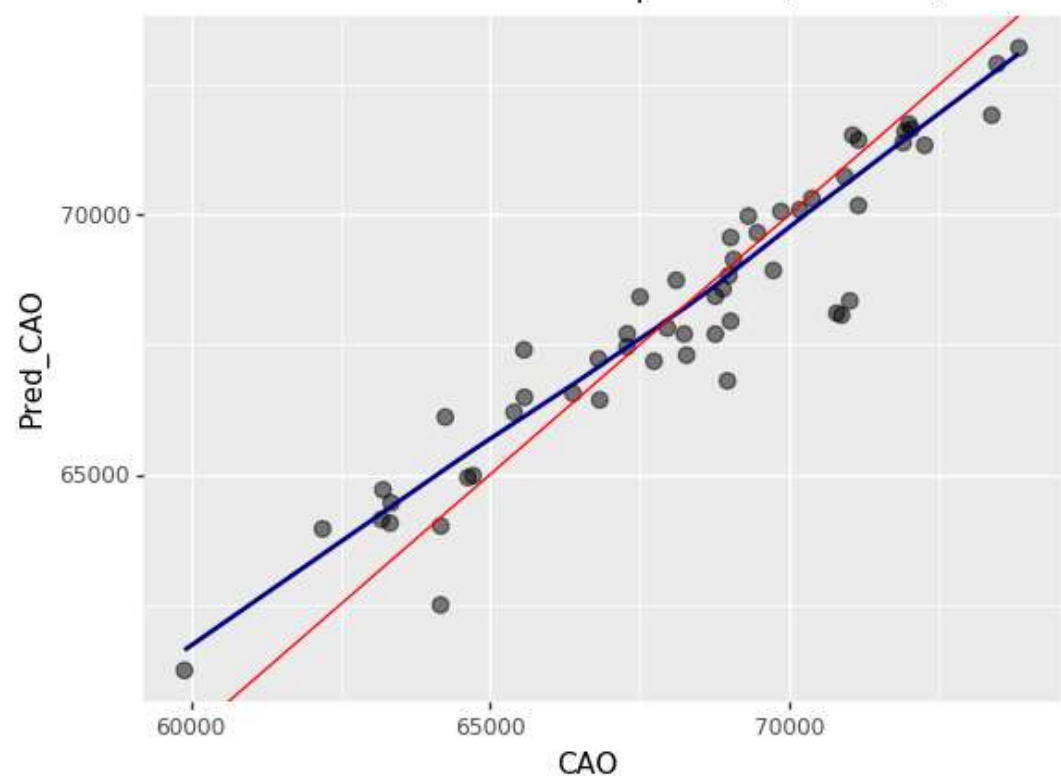
R-squared: 1.00

Mean Squared Error (MSE): 690.61

Root Mean Squared Error (RMSE): 26.28

Mean Absolute Error (MAE): 19.87

Model Performance Graph-GBM (Test set)



R-squared: 0.89

Mean Squared Error (MSE): 1137282.24

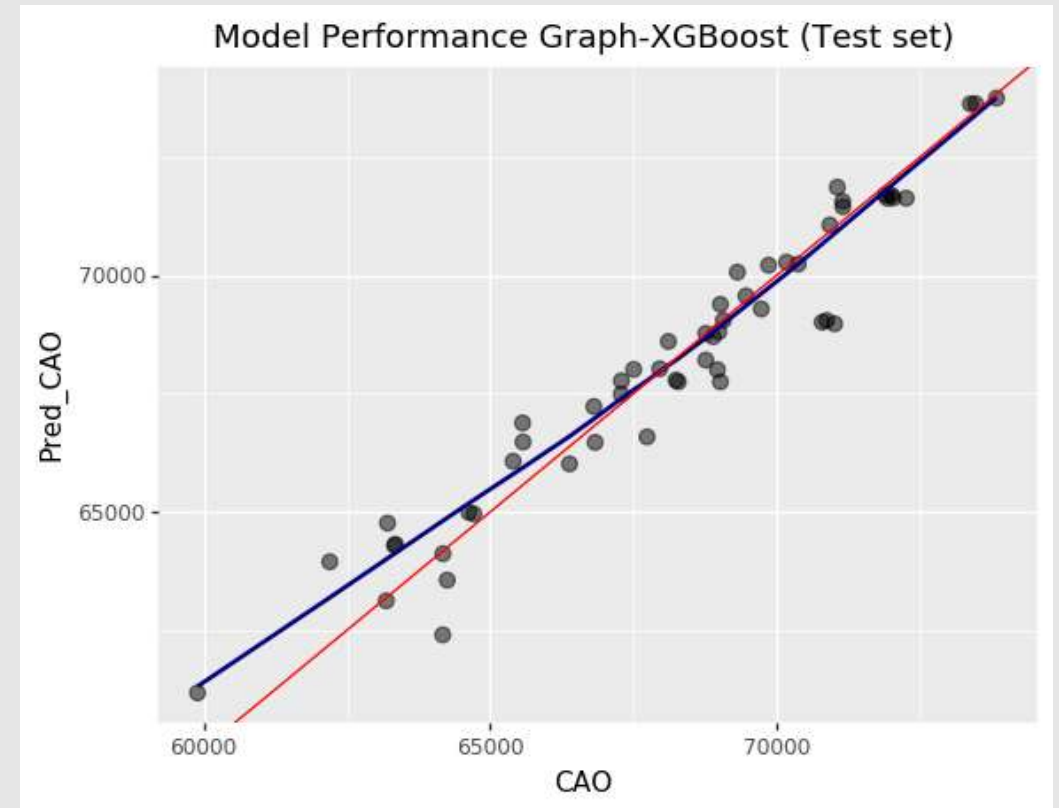
Root Mean Squared Error (RMSE): 1066.43

Mean Absolute Error (MAE): 776.27

# XGBOOST



R-squared: 1.00  
Mean Squared Error (MSE): 0.93  
Root Mean Squared Error (RMSE): 0.97  
Mean Absolute Error (MAE): 0.71



R-squared: 0.93  
Mean Squared Error (MSE): 653156.78  
Root Mean Squared Error (RMSE): 808.18  
Mean Absolute Error (MAE): 605.77



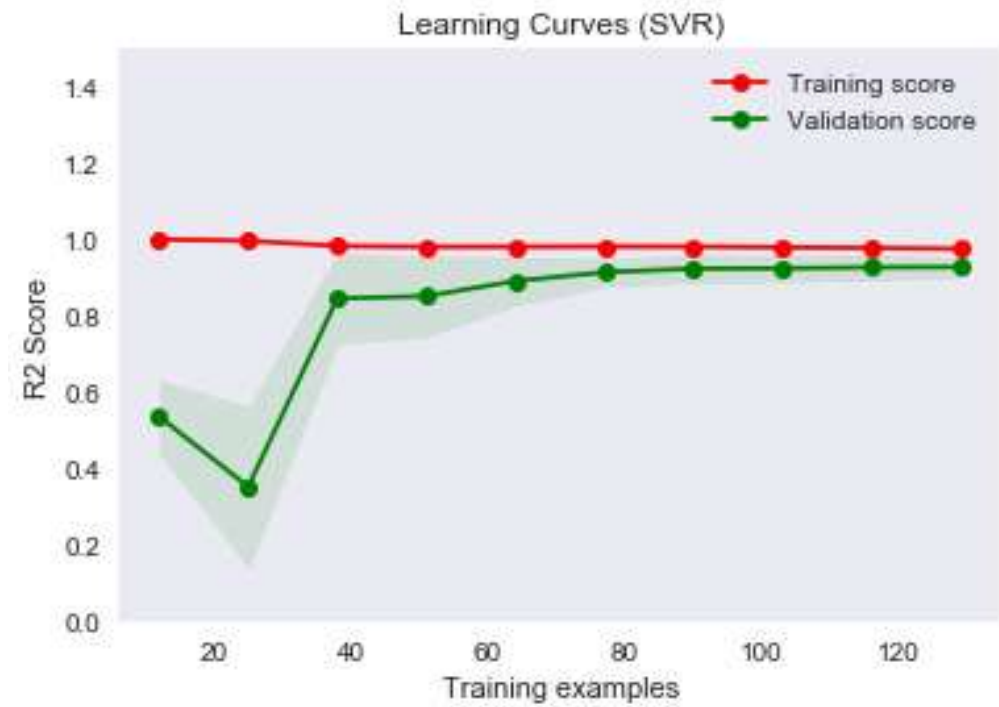
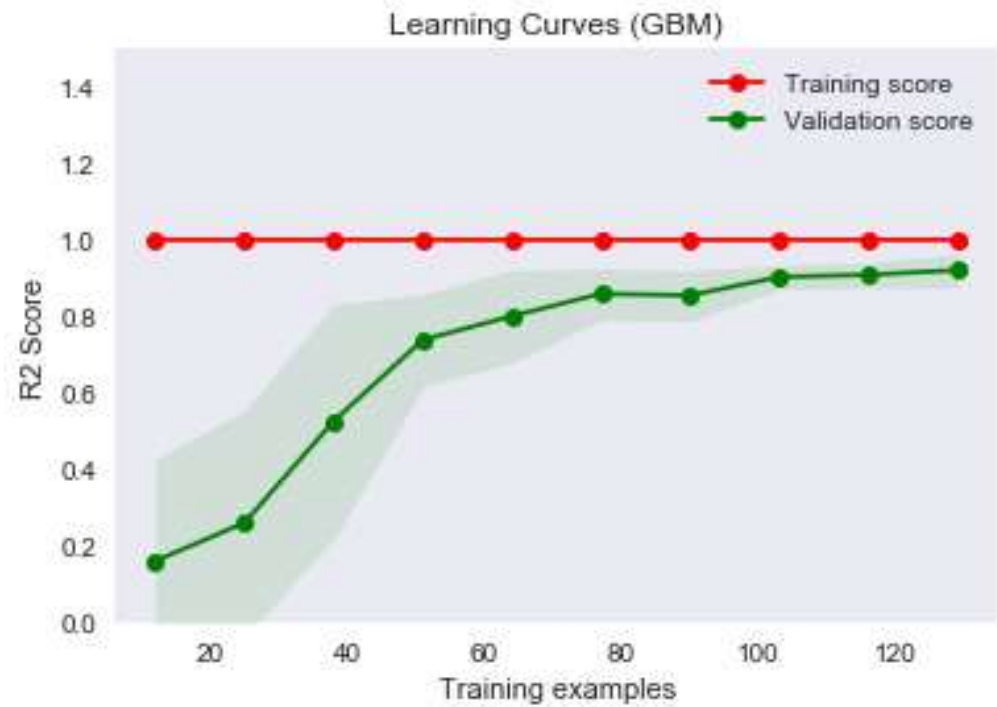
## •Feature selection (extraction)

```
#adım 2: p value 0.05 den büyük değişkenler çıkarılır...

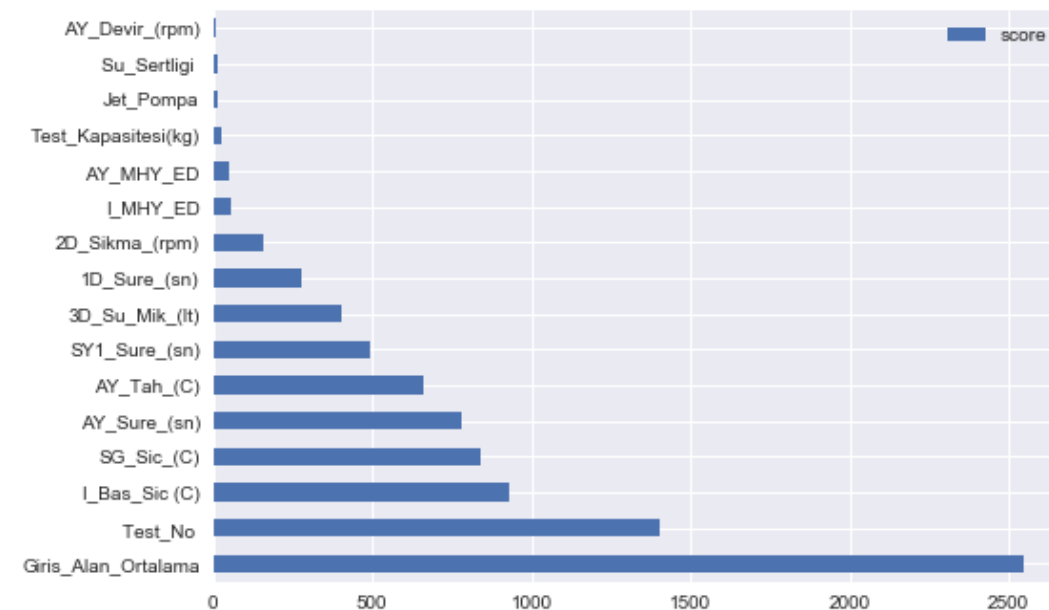
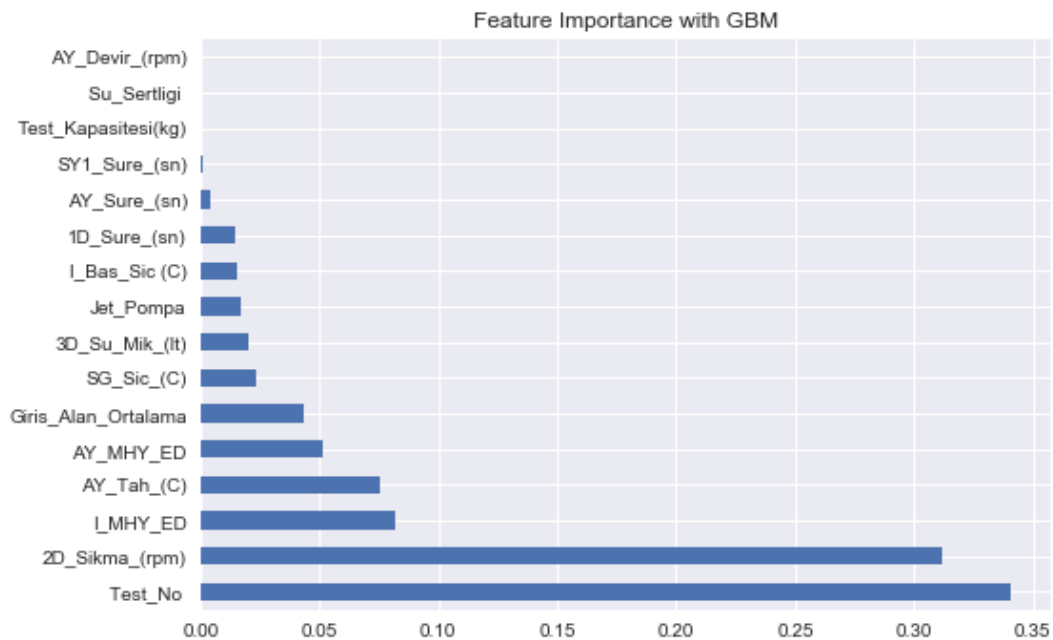
#OLS vriabls to remove

df.drop(['Numune_1_Relakse_Sonrasi_En_1',
        'Numune_1_Relakse_Sonrasi_En_2',
        'Numune_1_Relakse_Sonrasi_En_3',
        'Numune_1_Relakse_Sonrasi_Boy_1',
        'Numune_1_Relakse_Sonrasi_Boy_2',
        'Numune_1_Relakse_Sonrasi_Boy_3',
        '2D_MHY_ED',
        '2D_Su_Mik_(lt)',
        'I_Sure_(sn)',
        # 'I_MHY_ED', #
        'AY_Su_Mik_(lt)',
        'I_Tset_(C)',
        # 'SG_Sic_(C)', #
        # 'AY_Tah_(C)', #
        '1D_Su_Mik_(lt)', #
        # 'I_Bas_Sic_(C)', #
        # '3D_Su_Mik_(lt)' #

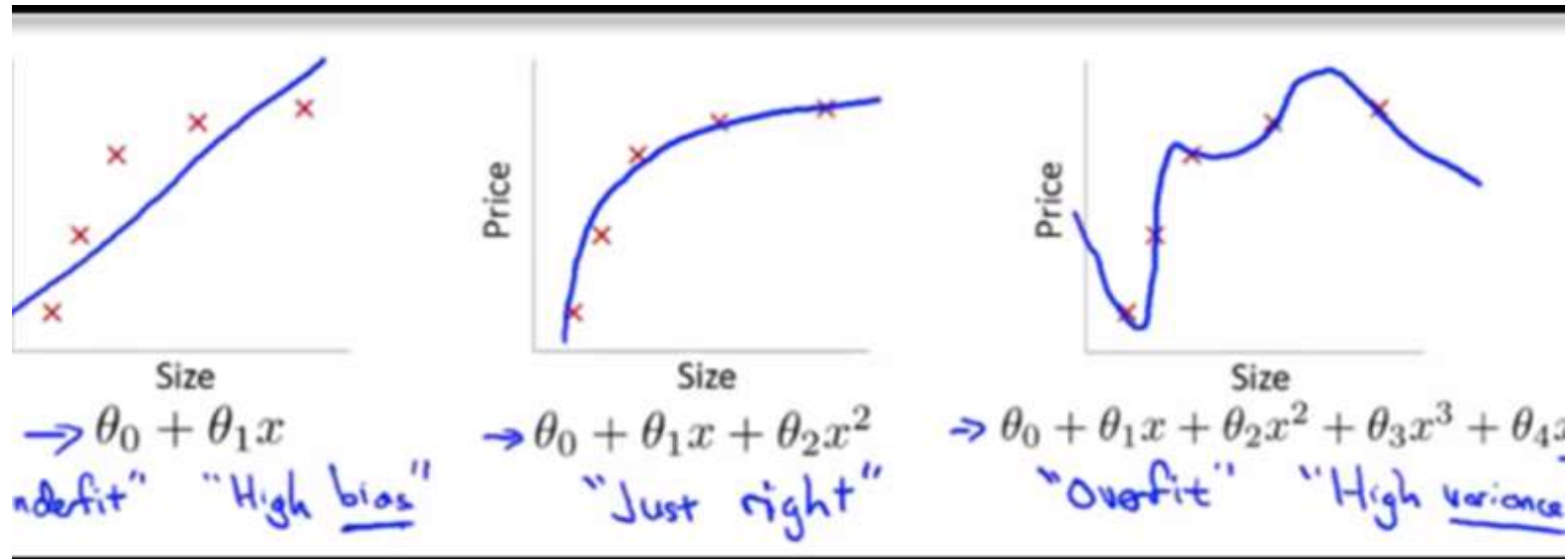
        'Tambur_Hacmi_(lt)',
        '1D_MHY_ED',
        '2D_Sure_(sn)',
        '3D_Sure_(sn)',
        'I_Devir_(rpm)'], axis=1, inplace=True)
```





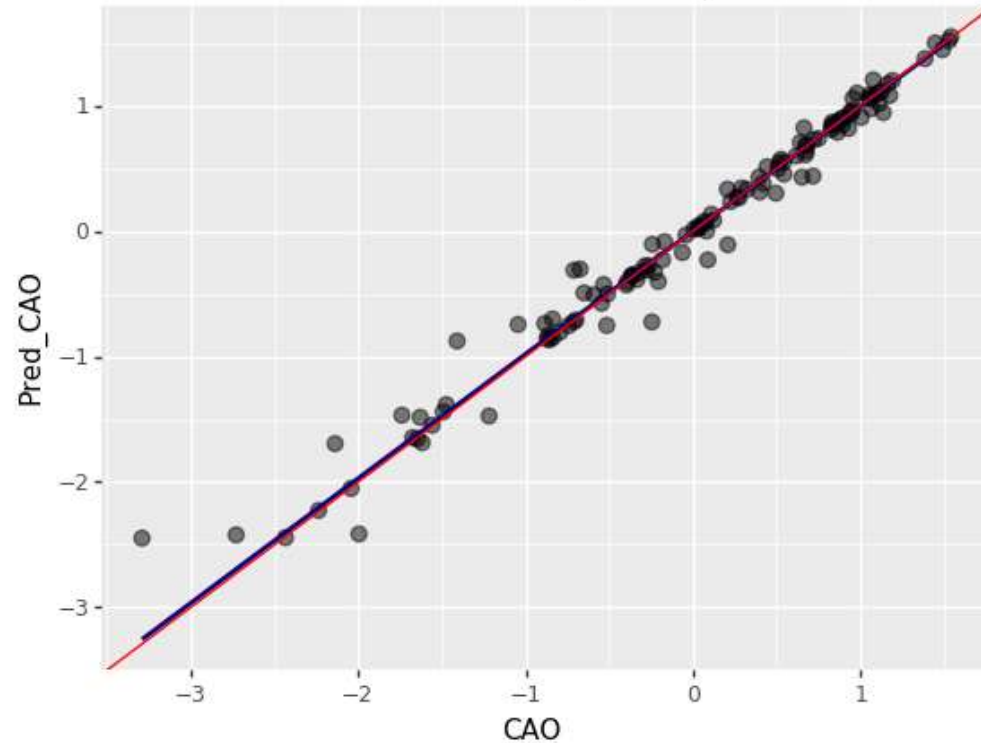


# FEATURE IMPORTANCE FOR GBM, XGBOOST



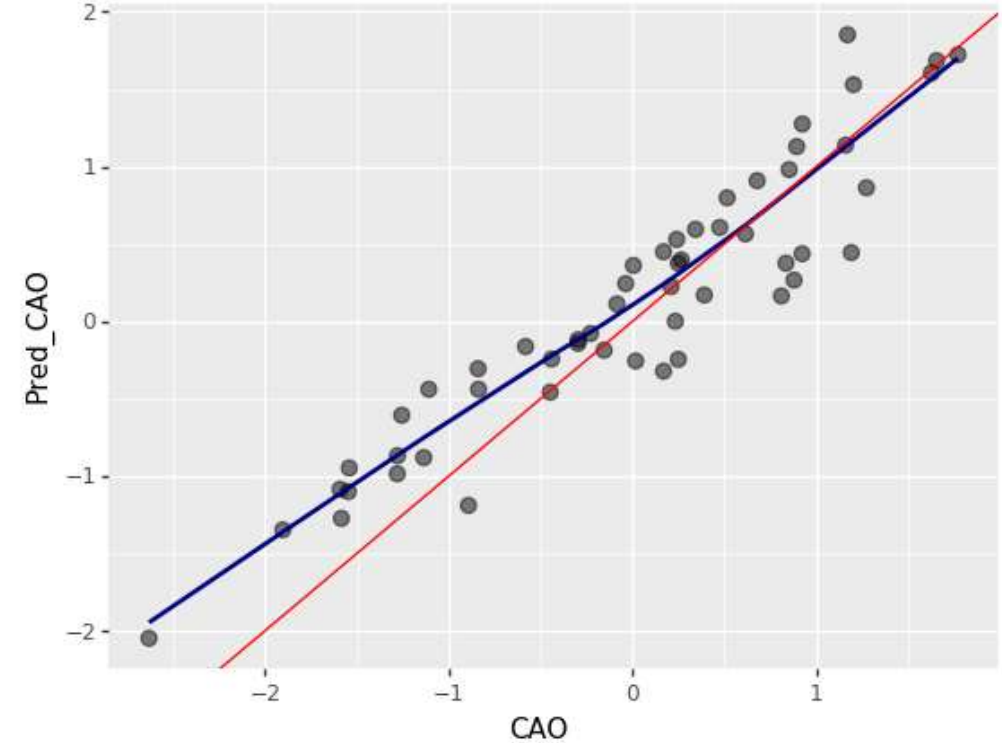
# MODEL PERFORMANCE GRAPHS

Model Performance Graph-SVR (Train set)



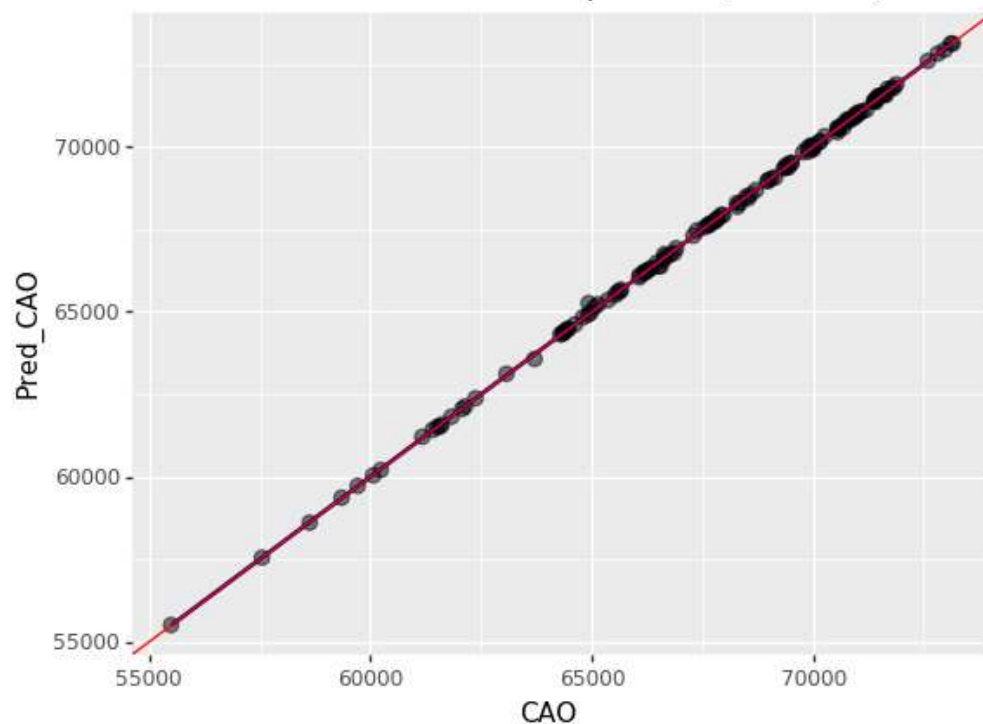
R-squared: 0.98  
Mean Squared Error (MSE): 0.02  
Root Mean Squared Error (RMSE): 0.16  
Mean Absolute Error (MAE): 0.09

Model Performance Graph-SVR (Test set)



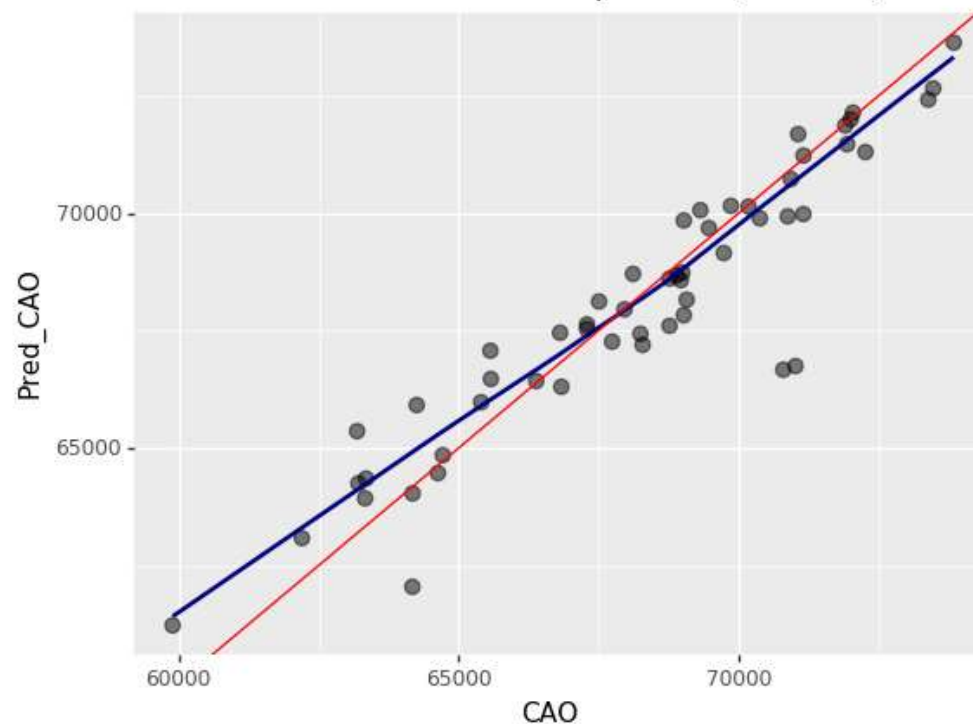
R-squared: 0.86  
Mean Squared Error (MSE): 0.14  
Root Mean Squared Error (RMSE): 0.38  
Mean Absolute Error (MAE): 0.32

Model Performance Graph-GBM (Train set)



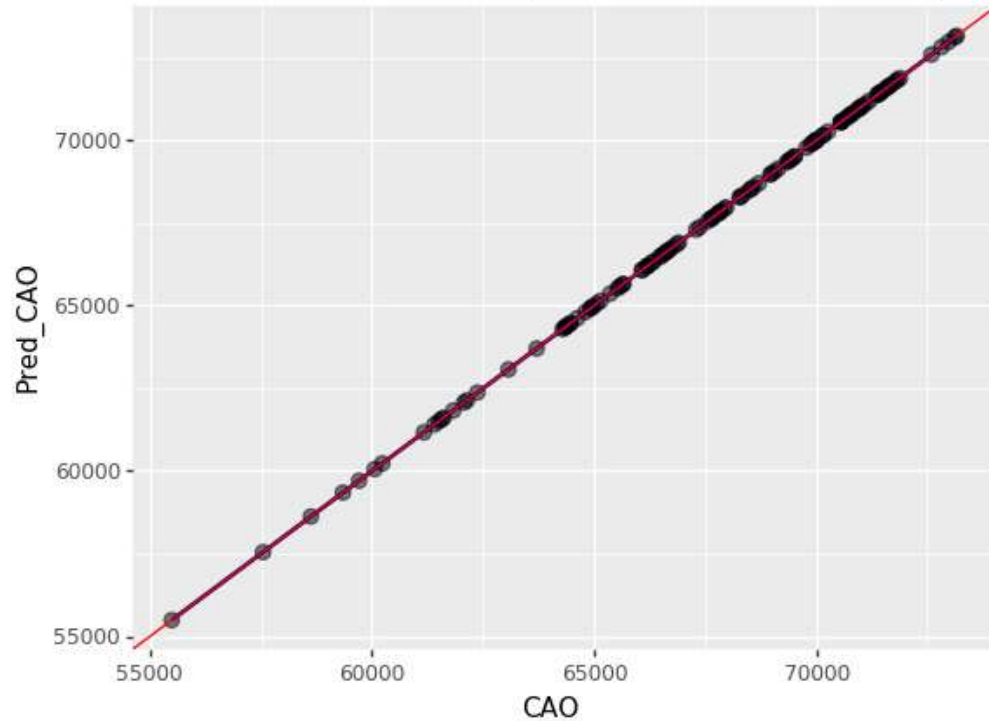
R-squared: 1.00  
Mean Squared Error (MSE): 3109.46  
Root Mean Squared Error (RMSE): 55.76  
Mean Absolute Error (MAE): 36.68

Model Performance Graph-GBM (Test set)



R-squared: 0.87  
Mean Squared Error (MSE): 1311147.36  
Root Mean Squared Error (RMSE): 1145.05  
Mean Absolute Error (MAE): 779.59

Model Performance Graph-XGBoost (Training set)



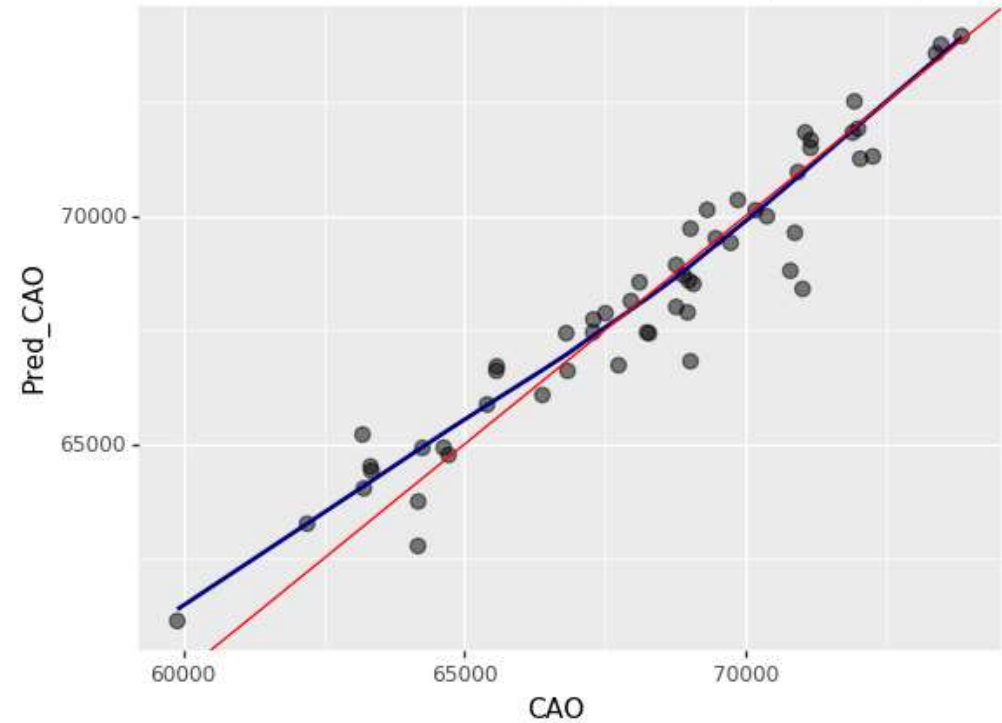
R-squared: 1.00

Mean Squared Error (MSE): 0.93

Root Mean Squared Error (RMSE): 0.97

Mean Absolute Error (MAE): 0.72

Model Performance Graph-XGBoost (Test set)

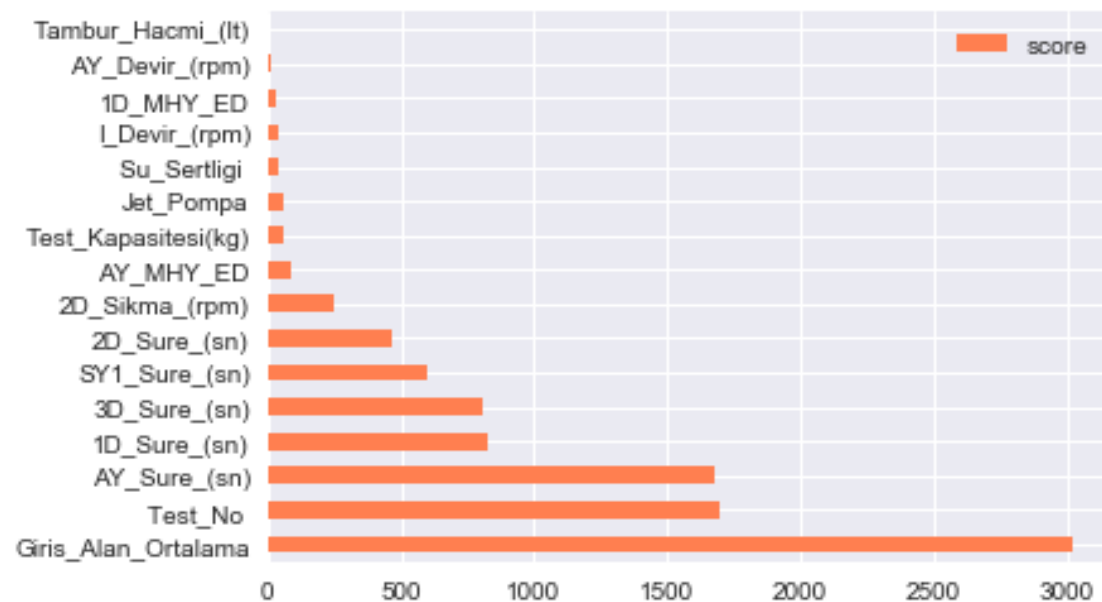


R-squared: 0.92

Mean Squared Error (MSE): 793557.76

Root Mean Squared Error (RMSE): 890.82

Mean Absolute Error (MAE): 684.89



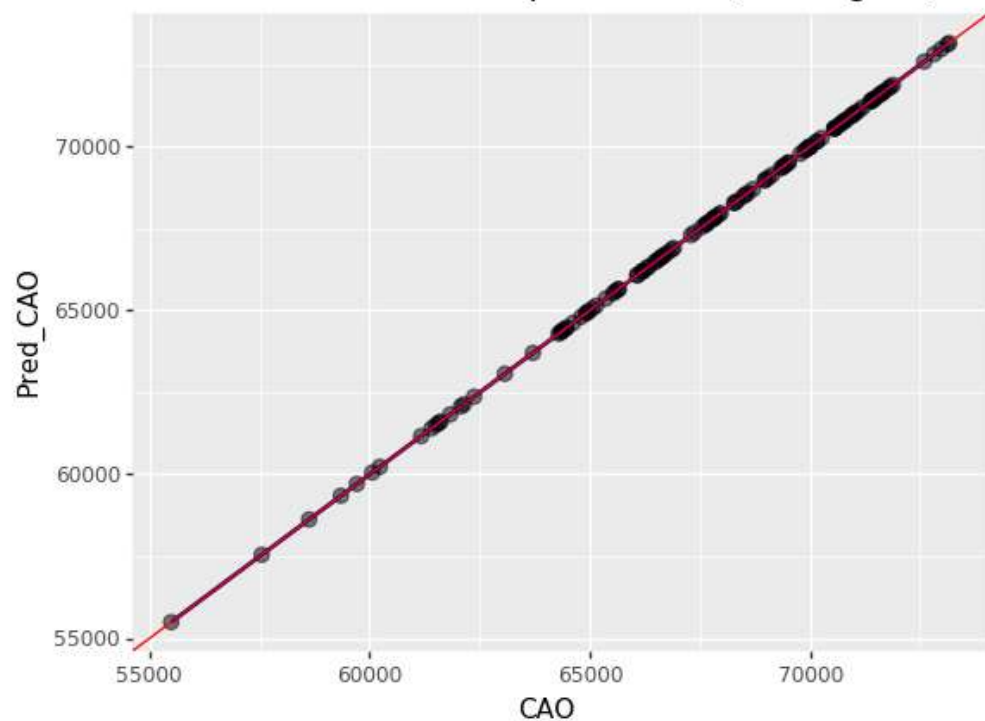
#adım 2: p value 0.05 den büyük değişkenler çıkarılır...

#OLS vriabls to remove

```
df.drop(['Numune_1_Relakse_Sonrasi_En_1',
        'Numune_1_Relakse_Sonrasi_En_2',
        'Numune_1_Relakse_Sonrasi_En_3',
        'Numune_1_Relakse_Sonrasi_Boy_1',
        'Numune_1_Relakse_Sonrasi_Boy_2',
        'Numune_1_Relakse_Sonrasi_Boy_3',
        '2D_MHY_ED',
        '2D_Su_Mik_(lt)',
        'I_Sure_(sn)',
        'I_MHY_ED', #
        'AY_Su_Mik_(lt)',
        'I_Tset_(C)',
        'SG_Sic_(C)', #
        'AY_Tah_(C)', #
        '1D_Su_Mik_(lt)', #
        'I_Bas_Sic_(C)', #
        '3D_Su_Mik_(lt)' #

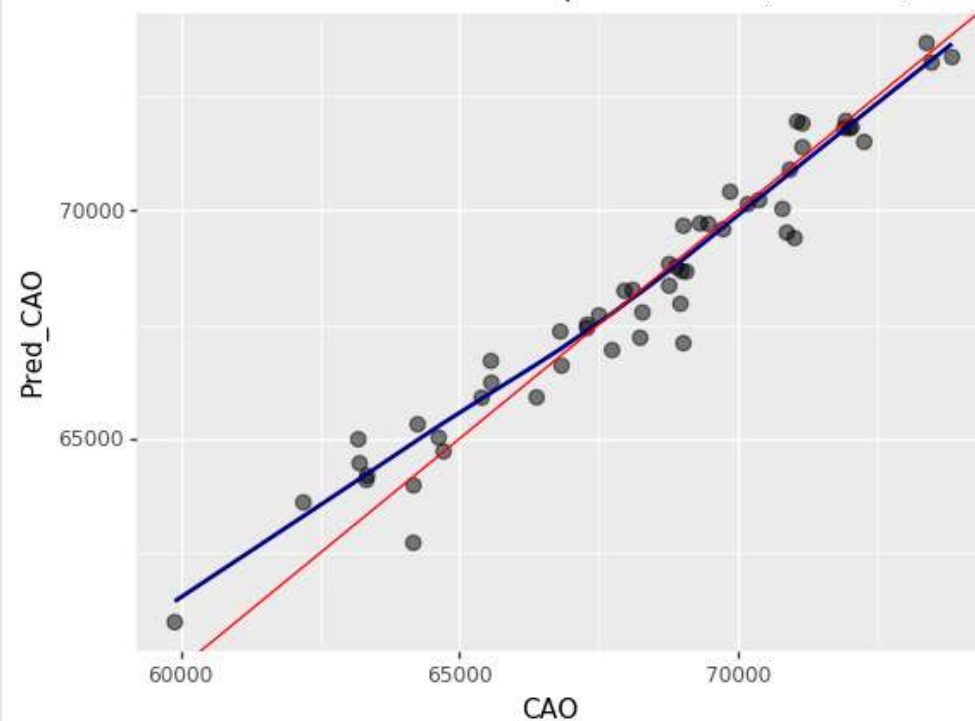
        # 'Tambur_Hacmi_(lt)',
        # '1D_MHY_ED',
        # '2D_Sure_(sn)',
        # '3D_Sure_(sn)',
        # 'I_Devir_(rpm)'
], axis=1, inplace=True)
```

Model Performance Graph-XGBoost (Training set)



```
R-squared: 1.00  
Mean Squared Error (MSE): 2.63  
Root Mean Squared Error (RMSE): 1.62  
Mean Absolute Error (MAE): 1.11
```

Model Performance Graph-XGBoost (Test set)



```
R-squared: 0.94  
Mean Squared Error (MSE): 577380.88  
Root Mean Squared Error (RMSE): 759.86  
Mean Absolute Error (MAE): 584.50
```

# CONCLUSION

- In this project, five machine learning algorithms used for prediction in Python program. Model performance was measured with  $R^2$  score, MSE, RMSE and MAE KPI forecast error types. After examination of KPI values for test samples and also model performance graphs, the XGBoost algorithm was chosen as an optimal model for this case. The best result has been gotten with removing variables that have bigger p-values than significance level(0.05), in that way, test MAE, RMSE and  $R^2$  score values were found 584.50, 759.86, 94% respectively.
- As a result, the XGBoost model predicted well. GBM and SVR model followed it. In other words, the aim of the project could be reached.