

$$\mathbb{P}(\xi^{-1}(S)) = \mathbb{P}(\{\omega \in \Omega | \xi(\omega) \in S\}) =: \mathbb{P}_{\xi}(S)$$