



$$\mathbb{P}(X^{-1}(S)) = \mathbb{P}(\{\omega \in \Omega | X(\omega) \in S\}) =: \mathbb{P}_X(S)$$