

# 让面试官眼前一亮的算法——记忆化搜索

一手微信s主讲及令痲沖offer都有 课程版本 v7.0



### 什么是记忆化搜索

在函数返回前,记录函数的返回结果 在下一次以同样参数访问函数时直接返回记录下的结果



### 记忆化搜索函数的三个特点

一手微信s函数有返直值offer都有

函数返回结果之和输入参数相关,和其他全局状态无关 参数列表中传入哈希表或者其他用于记录计算结果的数据结构



### 记忆化搜索 vs 动态规划

记忆化搜索是动态规划的一**种实现方式** 动态规划的另外一种实现方式是多重循环(下节课) 所以记忆化搜索**就是**动态规划



### 动态规划的核心思想: 由大化小

动态规划的算法思想: 大规模问题的依赖于小规模问题的计算结果 类似思想算法的还有: 递归, 分治法



# 独孤九剑——破箭式

一三种适用动态规划的场景。有

三种不适用动态规划的场景



#### 三种适用DP的场景

一手微信stux3最优值来offer都有 求方案数 求可行性

#### 三种适用动规的场景



- 求最值
  - dp[] 的值的类型是最优值的类型
  - dp[大问题] = max{dp[小问题1], dp[小问题2], ...}
  - dp[大问题] = min{dp[小问题1], dp[小问题2], ...}
- 求方案数
  - dp[] 的值的类型是方案数(整数)
  - $dp[大问题] = \sum (dp[小问题1], dp[小问题2], dy)$  22 九章来offer都有
  - ∑=sum
- 求可行性
  - dp[] 的值是 true / false
  - dp[大问题] = dp[小问题1] or dp[小问题2] or ...
  - 代码通常用 for 小问题 if dp[小问题] == true then break 的形式实现



### 三种不适用DP的场景

一手微家所有的具体考案<sup>er都有</sup> 输入数据是无序的 暴力算法时间复杂度已经是多项式级别

#### 三种不适用 DP 的场景



- 求出所有的具体方案
  - http://www.lintcode.com/problem/palindrome-partitioning/
  - 只求出一个具体方案还是可以用 DP 来做的(下节课)
  - 该判断标准成功率 99%
- 输入数据是无序的
  - http://www.lintcode.com/problem/longest-consecutive-sequence/
  - 背包类动态规划不适用此判断条件微信study322 九章来offer都有
  - 除去背包问题后, 该判断标准成功率 60-70%, 有一些题可以先排序之后按序处理
- 暴力算法的复杂度已经是多项式级别
  - http://www.lintcode.com/problem/largest-rectangle-in-histogram/
  - 动态规划擅长与优化指数级别复杂度(2<sup>n</sup>,n!)到多项式级别复杂度(n<sup>2</sup>,n<sup>3</sup>)
  - 不擅长优化n^3到n^2
  - 该判断标准成功率 80%
- 则 极不可能 使用动态规划求解



#### Wildcard Matching

http://www.lintcode.com/problem/wildcard-matching/

http://www.jiuzhang.com/solution/wildcard-matching/

类别: 匹配型动态规划

适用场景: 求可行性



```
public boolean isMatch(String s, String p) {
    if (s == null | p == null) {
                                                                            private boolean isMatchHelper(String s, int sIndex,
         return false:
                                                                                                   String p, int pIndex) {
                                                                               if (pIndex == p.length()) {
                                                                                  // 如果 p 从 pIndex 开始是空字符串了, 那么 s 必须从 sIndex
                                                                                      是空字符串才能匹配上
    // boolean[][] memo = new boolean[s.length()][p.length()];
                                                                                  return sIndex == s.length();
    // boolean[][] visited = new boolean[s.length()][p.length()];
    // return isMatchHelper(s, 0, p, 0, memo, visited);
                                                                               if (sIndex == s.length()) {
                                                                                  // 如果 s 从 sIndex 是空, 那么 p 必须全是 *
                                                                                  return allStar(p, pIndex);
    return isMatchHelper(s, 0, p, 0);
                                            一手微信study322 九章来char sFirstChar s.charAt(sIndex);
                                                                             char pFirstChar = p.charAt(pIndex);
private boolean allStar(String p, int pIndex)
    for (int i = pIndex; i < p.length(); i++) {</pre>
                                                                               if (pFirstChar != '*') {
                                                                                  return charMatch(sFirstChar, pFirstChar) && isMatchHelper(s, sIndex +
         if (p.charAt(i) != '*') {
                                                                                     1, p, pIndex + 1);
             return false;
                                                                               for (int i = sIndex; i <= s.length(); i++) {</pre>
                                                                                  if (isMatchHelper(s, i, p, pIndex + 1)) {
    return true:
                                                                                     return true;
                                                                               return false;
private boolean charMatch(char sFirstChar, char pFirstChar) {
    return (sFirstChar == pFirstChar || pFirstChar == '?');
```



```
def isMatch(self, s, p):
    if s == None or p == None:
        return False
    # memo = [[None] * len(p) for in range(len(s))]
    # return self.is match helper(s, 0, p, 0, memo)
    return self.is_match_helper(s, 0, p, 0)
def all_star(self, p, p_index):
    for i in range(p index, len(p)):
        if p[i] != '*':
            return False
    return True
def char_match(self, s_first_char, p_first_char):
    return s_first_char == p_first_char or p_first_char == '?
```

```
is match helper(self, s, s index, p, p index):
if p index == len(p):
    return s_index == len(s)
if s index == len(s):
    return self.all star(p, p index)
s_first_char = s[s_index]
p first char = p[p index]
if p first char != '*':
   return self.char_match(s_first_char, p_first_char) and self
        .is_match_helper(s, s_index + 1, p, p_index + 1)
for i in range(s index, len(s) + 1):
    if self.is match helper(s, i, p, p index + 1):
       return True
return False
```



```
private boolean isMatchHelper(String s, int sIndex,
                             String p, int pIndex) {
   if (pIndex == p.length()) {
       // 如果 p 从 pIndex 开始是空字符串了, 那么 s 必须从 sIndex
           是空字符串才能匹配上
                                                              is_match_helper(self, s, s_index, p, p_index):
                                                              if p_index == len(p):
       return sIndex == s.length();
                                                                  return s index == len(s)
   if (sIndex == s.length()) {
       // 如果 s 从 sIndex 是空, 那么 p 必须全是 *
                                                              if s index == len(s):
       return allStar(p, pIndex);
                                      一手微信study32
                                                                  return self.all star(p, p index)
   char sFirstChar = s.charAt(sIndex);
                                                              s first char = s[s index]
   char pFirstChar = p.charAt(pIndex);
                                                              p first char = p[p index]
   if (pFirstChar == '*') {
                                                              if p_first char == '*':
       return isMatchHelper(s, sIndex + 1, p, pIndex)
                                                                  return self.is_match_helper(s, s_index + 1, p, p_index) or
                                                                     self.is_match_helper(s, s_index, p, p_index + 1)
              isMatchHelper(s, sIndex, p, pIndex + 1);
                                                              return self.char_match(s_first_char, p_first_char) and self
                                                                  .is match helper(s, s_index + 1, p, p_index + 1)
   return charMatch(sFirstChar, pFirstChar) &&
          isMatchHelper(s, sIndex + 1, p, pIndex + 1);
```



```
private boolean isMatchHelper(String s, int sIndex,
                           String p, int pIndex,
                           boolean[][] memo,
                           boolean[][] visited) {
   if (pIndex == p.length()) {
       // 如果 p 从 pIndex 开始是空字符串了,那么 s 必须从 sIndex 是空字符串才能匹配上
       return sIndex == s.length();
                                                                          lef is_match_helper(self, s, s_index, p, p_index, memo):
                                                                             if p_index == len(p):
   if (sIndex == s.length()) {
       // 如果 s 从 sIndex 是空, 那么 p 必须全是 *
                                                                                  return s_index == len(s)
       return allStar(p, pIndex);
                                                                             if s_index == len(s):
   if (visited[sIndex][pIndex]) {
       return memo[sIndex][pIndex];
                                                                                  return self.all star(p, p index)
                                                 一手微信study3
                                                                             if memo[s index][p index] is not None:
   char sFirstChar = s.charAt(sIndex);
                                                                                 return memo[s index][p index]
   char pFirstChar = p.charAt(pIndex);
   boolean match;
                                                                             s first char = s[s index]
   if (pFirstChar == '*') {
                                                                             p first char = p[p index]
       match = isMatchHelper(s, sIndex + 1, p, pIndex, memo, visited) ||
                                                                             match = False
             isMatchHelper(s, sIndex, p, pIndex + 1, memo, visited);
   } else {
                                                                             if p first char == '*':
       match = charMatch(sFirstChar, pFirstChar) &&
                                                                                 match = self.is_match_helper(s, s_index + 1, p, p_index, memo) or
         isMatchHelper(s, sIndex + 1, p, pIndex + 1, memo, visited);
                                                                                  self.is match helper(s, s index, p, p index + 1, memo)
                                                                             else:
   memo[sIndex][pIndex] = match;
                                                                                 match = self.char_match(s_first_char, p_first_char) and \
   visited[sIndex][pIndex] = true;
                                                                                  self.is match helper(s, s index + 1, p, p index + 1, memo)
   return match;
                                                                             memo[s index][p index] = match
                                                                             return match
```



# Follow up: Regular Expression Matching

http://www.lintcode.com/problem/regular-expression-matching/

http://www.jiuzhang.com/solution/regular-expression-matching/

面试是一定不会让你做完整版的 Regular Expression 的 所以一定是阉割版的

#### 面试评分标准



Strong Hire: 两个都答出来,且写出来,Bug Free or Bug 很少

Hire / Weak Hire: 两个都答出来,写完第一个,第二个能基本在第一个的基础上改完,允许有一些提示和少量 Bug

No Hire: 没写完,或者需要很多提示

Strong No: 第一个都没写完

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# 记忆化搜索时间复杂度

一等动态规划的时间复杂度都有

=O(状态总数\*计算每个状态的时间耗费)



### 休息 5 分钟

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#### Word Pattern II

http://www.lintcode.com/problem/word-pattern-ii/

http://www.jiuzhang.com/solutions/word-pattern-ii/

这个题是否可以记忆化?



```
public boolean wordPatternMatch(String pattern, String str) {
   Map<Character, String> mapping = new HashMap<>();
   Set<String> used = new HashSet<>();
   return isMatch(pattern, str, mapping, used);
private boolean isMatch(String pattern,
                       String str, Map<Character, String> mapping,
                       Set<String> used) {
   if (pattern.length() == 0) {
        return str.length() == 0;
    Character ch = pattern.charAt(0);
   if (mapping.containsKey(ch)) {
        String word = mapping.get(ch);
        if (!str.startsWith(word)) {
           return fatal 信Study322 九章来offer都有
        return isMatch(pattern.substring(1), str.substring(word.length()), mapping, used);
    for (int len = 0; len < str.length(); len++) {</pre>
        String word = str.substring(0, len + 1);
        if (used.contains(word)) {
           continue;
        mapping.put(ch, word);
        used.add(word);
        if (isMatch(pattern.substring(1), str.substring(word.length()), mapping, used)) {
            return true;
        used.remove(word);
        mapping.remove(ch);
    return false;
```



```
def wordPatternMatch(self, pattern, string):
   return self.is_match(pattern, string, {}, set())
def is_match(self, pattern, string, mapping, used):
   if not pattern:
       return not string
   char = pattern[0]
   if char in mapping:
       word = mapping[char]
       if not string.startswith(word):
           return False
       return self.is_match(pattern[1:], string[len(word):], mapping, used)
   for length in range(len(string)):
       word = string[:length + 1]
       if word in used:
           continue
       used.add(word)
       mapping[char] = word
       if self.is_match(pattern[1:], string[length + 1:], mapping, used):
           return True
       used.remove(word)
       del mapping[char]
   return False
```



#### Word Break

http://www.lintcode.com/problem/word-break/

http://www.jiuzhang.com/solution/word-break/

给定字符串 s 和单词字典 dict,确定 s 是否可以分成一个或多个以空格分隔的字串,并且这些字串都在字典中存在

#### Word Break



右边的代码正确性没有问题 但是存在一个问题导致其无法通过测试 这个问题是什么?

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```
is possible(self, s, index, max length, word set, memo):
   if index in memo:
       return memo[index]
   if index == len(s):
       return True
   memo[index] = False
   for i in range(index, len(s)):
       if i + 1 - index > max length:
           break
       word = s[index : i + 1]
       if word not in word set:
           continue
       if self.is possible(s, i + 1, max length, word set, memo):
           memo[index] = True
           break
   return memo[index]
def get_max_length(self, word_set):
   max length = 0
   for word in word set:
       max length = max(max length, len(word))
   return max length
```

#### Word Break



右边的代码正确性没有问题 但是存在一个问题导致其无法通过测试 这个问题是什么?

```
private boolean isPossible(String s, int index, int maxLength, Set<String> wordSet, Map<Integer, Boolean> memo) {
                 if (memo.containsKey(index)) {
                     return memo.get(index);
                 if (index == s.length()) {
                     return true;
                 memo.put(index, false);
                 for (int i = index; i < s.length(); i++) {</pre>
                     if (i + 1 - index > maxLength) {
                         break:
一手微信String word = s.substring(index, i + 1);有
                         continue;
                     if (isPossible(s, i + 1, maxLength, wordSet, memo)) {
                         memo.put(index, true);
                         break:
                 return memo.get(index);
             private int getMaxLength(Set<String> wordSet) {
                 int maxLength = 0;
                 for (String word : wordSet) {
                     maxLength = Math.max(maxLength, word.length());
                 return maxLength;
```



# 记忆化搜索的缺陷

递归深度太深,导致 StackOverflow



#### Word Break II

http://www.lintcode.com/problem/word-break-ii/

http://www.jiuzhang.com/solution/word-break-ii/

不适用场景: 求出所有具体方案而非方案总数

但是可以使用动态规划进行优化



### 优化方案1

用Word Break 这个题的思路 使用 memo[i] 代表从 i 开始的后缀是否能够被 break 在 DFS 找所有方案的时候,通过 memo 可以进行**可行性剪枝** 



```
wordBreak(self, s, wordDict):
 max length = self.get max length(wordDict)
 # use dfs to find all break path
 results = []
 self.dfs(s, ∅, max length, wordDict, {}, [], results)
 return results
f is possible(self, s, index, max length, word set, memo):
 if index in memo:
     return memo[index]
 if index == len(s):
     memo[index] = True
     return True
 memo[index] = False
 for i in range(index, len(s)):
     if i + 1 - index > max length:
         break
     word = s[index: i + 1]
     if word not in word set:
     if self.is possible(s, i + 1, max length, word set, memo):
         memo[index] = True
         break
 return memo[index]
```

```
get max length(self, word set):
   max length = 0
    for word in word set:
       max_length = max(max_length, len(word))
   return max length
def dfs(self, s, index, max length, word set, memo, path, results):
   if index == len(s):
       results.append(" ".join(path))
   # prunning
   if not self.is possible(s, index, max length, word set, memo):
    for i in range(index, len(s)):
        if i + 1 - index > max length:
            break
       word = s[index: i + 1]
        if word not in word_set:
            continue
        path.append(word)
        self.dfs(s, index + len(word), max_length, word_set, memo,
            path, results)
        path.pop()
```



```
public List<String> wordBreak(String s, Set<String> wordSet) {
   Map<Integer, Boolean> memo = new HashMap<>();
   int maxLength = getMaxLength(wordSet);
   // use dfs to find all break path
   List<String> results = new ArrayList<>();
   dfsGetResults(s, 0, maxLength, wordSet, memo, new ArrayList<String>(), results);
   return results;
private boolean isPossible(String s, int index, int maxLength, Set<String> wordSet, Map<Integer, Boolean> memo) {
   if (memo.containsKey(index)) {
                                                                                                      private int getMaxLength(Set<String> wordSet) {
       return memo.get(index);
                                                                                                         int maxLength = 0;
                                                                                                          for (String word : wordSet) {
                                                                                                              maxLength = Math.max(maxLength, word.length());
   if (index == s.length()) {
       return true;
                                                                                                         return maxLength;
                                                               一手微信study322
   memo.put(index, false);
                                                                                                     private void dfsGetResults(String s, int index, int maxLength, Set<String> wordSet, Map<Integer,
   for (int i = index; i < s.length(); i++) {</pre>
                                                                                                      Boolean> memo, Arraytist(String> path, List(String> results) {
       if (i + 1 - index > maxLength) {
                                                                                                          if (index == s.length()) {
           break;
                                                                                                              results.add(String.join(" ", path));
                                                                                                              return;
       String word = s.substring(index, i + 1);
       if (!wordSet.contains(word)) {
           continue;
                                                                                                         // prunning
                                                                                                         if (!isPossible(s, index, maxLength, wordSet, memo)) {
       if (isPossible(s, i + 1, maxLength, wordSet, memo)) {
                                                                                                              return;
           memo.put(index, true);
           break;
                                                                                                          for (int i = index; i < s.length(); i++) {
                                                                                                              if (i + 1 - index > maxLength) {
                                                                                                                  break:
   return memo.get(index);
                                                                                                              String word = s.substring(index, i + 1);
                                                                                                              if (!wordSet.contains(word)) {
                                                                                                                  continue;
                                                                                                              path.add(word);
                                                                                                              dfsGetResults(s, index + word.length(), maxLength, wordSet, memo, path, results);
                                                                                                              path.remove(path.size() - 1);
```

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# 优化方案 2

直接使用 memo[i] 记录从位置 i 开始的后缀 能够被 break 出来的所有方案



```
public ArrayList<String> wordBreak(String s, Set<String> wordDict) {
   // Note: The Solution object is instantiated only once and is reused by each test case.
   Map<String, ArrayList<String>> memo = new HashMap<String, ArrayList<String>>();
   return wordBreakHelper(s, wordDict, memo);
public ArrayList(String) wordBreakHelper(String s,
                                       Set<String> wordDict,
                                       Map<String, ArrayList<String>> memo){
   if (memo.containsKey(s)) {
       return memo.get(s);
   ArrayList<String> partitions = new ArrayList<String>();
   if (s.length() == 0) {
       return partitions;
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   if (wordDict.contains(s)) {
       partitions.add(s);
   for (int i = 1; i < s.length(); i++){
       String prefix = s.substring(0, i);
       if (!wordDict.contains(prefix)) {
           continue;
       String suffix = s.substring(i);
       ArrayList<String> subPartitions = wordBreakHelper(suffix, wordDict, memo);
       for (String partition : subPartitions){
           partitions.add(prefix + " " + partition);
   memo.put(s, partitions);
   return partitions;
```



```
wordBreak(self, s, wordDict):
   return self.dfs(s, wordDict, {})
def dfs(self, s, wordDict, memo):
   if s in memo:
       return memo[s]
   partitions = []
   if len(s) == 0:
       return partitions
   for i in range(1, len(s)):
       prefix = s[:i]
       if prefix not in wordDict:
           continue
       suffix = s[i:];
       sub_partitions = self.dfs(suffix, wordDict, memo)
       for partition in sub_partitions:
           partitions.append(prefix + " " + partition)
   if s in wordDict:
       partitions.append(s)
   memo[s] = partitions
   return partitions
```



#### 极端情况

以上两种方法在极端情况下是否能有优化效果呢?

*s* = "aaaaaaaaaa..."

*dict* = {"a", "aa", "aaa", ...}

#### Word Break II 的面试评分标准



Strong Hire: DFS+DP优化

Hire / Weak Hire: DFS 能写完,且 Bug free or Bug 不多,不需要提示 or 需要少量提示

No Hire: DFS 写不完,或者需要很多提示

Strong No: 啥都想不出

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### \* Palindrome Partitioning

http://www.lintcode.com/problem/palindrome-partitioning/

http://www.jiuzhang.com/solutions/palindrome-partitioning/

一个类似 Word Break II 的题

但是使用记忆化搜索优化效果甚微



#### Word Break III

https://www.lintcode.com/problem/word-break-iii

https://www.jiuzhang.com/solution/word-break-iii

类别:前缀型/划分型动态规划

适用场景: 求方案总数



```
public int wordBreak3(String s, Set<String> dict) {
    int maxLength;
    Set<String> lowerDict = new HashSet<>();
    maxLength = initialize(dict, lowerDict);
    return memoSearch(s.toLowerCase(), 0, maxLength, lowerDict, new HashMap<Integer, Integer>());
private int memoSearch(String s, int index, int maxLength, Set<String> lowerDict, Map<Integer, Integer> memo) {
    if (index == s.length()) {
       return 1;
    if (memo.containsKey(index)) {
       return memo.get(index);
   memo.put(index, 0);
for (int i = index; if shength 0; ti+0)y(322 九章来offer都有
       if (i + 1 - index > maxLength) {
            break;
       String word = s.substring(index, i + 1);
       if (!lowerDict.contains(word)) {
            continue;
       memo.put(index, memo.get(index) + memoSearch(s, i + 1, maxLength, lowerDict, memo));
    return memo.get(index);
private int initialize(Set<String> dict, Set<String> lowerDict) {
    int maxLength = 0;
    for (String word : dict) {
       maxLength = Math.max(maxLength, word.length());
       lowerDict.add(word.toLowerCase());
    return maxLength;
```

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```
wordBreak3(self, s, dict):
max length, lower dict = self.initialize(dict)
return self.memo search(s.lower(), 0, max length, lower dict, {})
memo_search(self, s, index, max_length, lower_dict, memo):
if index == len(s):
    return 1
if index in memo:
    return memo[index]
memo[index] = 0
for i in range(index, len(s)):
    if i + 1 - index > max_length:
        break
    word = s[index: i + 1]
    if word not in lower dict:
        continue
    memo[index] += self.memo search(s, i + 1, max length, lower dict, memo
return memo[index]
initialize(self, dict):
max length = 0
lower dict = set()
for word in dict:
    max length = max(max length, len(word))
    lower_dict.add(word.lower())
return max_length, lower_dict
```