## Basic Beamer Talk

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# Introduction

- MOTIVATION: Literature on determining the alternative optima for combinatorial optimization problems, especially NP-Hard problems, is minimal (e.g. determining multiple solutions to TSP [1]).
- The Minimum Cardinality Set Covering Problem (MCSCP) is a combinatorial integer programming problem with many applications (e.g. ingot mold selection [2]).
- Goal: Develop a methodology for predicting the qualitative number of alternative optima for MCSCP.

### Formulation of MCSCP

Let  $A = [a_{ij}]$  be an  $m \times n$  matrix, where m < n, and the entries of A are zeros and ones. Let  $x = [x_i]$  be a bit string, then

Minimize: 
$$z = \sum_{j=1}^{n} x_j$$
 (1)

Subject to:

$$\sum_{j=1}^{n} a_{ij} x_j \ge 1 \quad \text{for } i = 1, 2, \dots, m$$
 (2.1)

$$\sum_{j=1}^{n} a_{ij} \ge 1 \quad \text{for } i = 1, 2, \dots, m$$
 (2.2)

$$\sum_{i=1}^{m} a_{ij} \ge 1 \quad \text{for } j = 1, 2, \dots, n$$
 (2.3)

# Figures

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Me using 
$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
 to find

roots of 
$$x^2 - 1 = 0$$
.



#### Selected References



T. Huang, Y. Gong, and J. Zhang.

 $\frac{\text{Seeking multiple solutions of combinatorial optimization problems: a proof of principle}{\text{study.}}$ 

2018 IEEE Symposium Series on Computational Intelligence (SSCI), Bangalore, India pp 1212-1218.



F. J. Vasko, F. E. Wolf, and K. L. Stott.

Optimal selection of ingot sizes via set covering. Opns Res, 38, pp 346-353, 1987.



MATLAB.

Statistics and Machine Learning Toolbox User's Guide, R2020a.

1 Apple Hill Dr. Natick, MA, 01760-2098, 2020.



H. Taha.

Operations Research: An Introduction, 10th edition. Pearson, Boston, MA, 2017.