

# práctica 4

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1.

recorrido:  $R_x = \{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$

probabilidad puntual:

$$p(X = i) = \frac{1}{36}, i \in \{2, 12\}$$

$$p(X = i) = \frac{1}{18}, i \in \{3, 11\}$$

$$p(X = i) = \frac{1}{12}, i \in \{4, 10\}$$

$$p(X = i) = \frac{1}{9}, i \in \{5, 9\}$$

$$p(X = i) = \frac{5}{36}, i \in \{6, 8\}$$

$$p(X = 7) = \frac{1}{6}$$

probabilidad acumulada:

$$F(t) = \begin{cases} 0 & t < 2 \\ \frac{1}{36} & 2 \leq t < 3 \\ \frac{1}{12} & 3 \leq t < 4 \\ \frac{1}{6} & 4 \leq t < 5 \\ \frac{5}{36} & 5 \leq t < 6 \\ \frac{1}{3} & 6 \leq t < 7 \\ \frac{2}{9} & 7 \leq t < 8 \\ \frac{5}{12} & 8 \leq t < 9 \\ \frac{2}{3} & 9 \leq t < 10 \\ \frac{11}{12} & 10 \leq t < 11 \\ \frac{35}{36} & 11 \leq t < 12 \\ 1 & 12 \leq t \end{cases}$$

$$E(X) = \sum_{i=2}^{12} i * p(X = i) = 7$$

$$Var(X) = E(X^2) - E(X)^2 = \frac{329}{6} - 49 = \frac{35}{6}$$

$$SD(X) = \sqrt{Var(X)} = 2.4152$$

**2.**

**a.**

$$p(T = 3) = \frac{1}{3}, p(T = 4) = \frac{1}{6}, p(T = 5) = \frac{1}{6}, p(T = 6) = \frac{1}{3}$$

**b.**

$$P(3 < T \leq 5) = P(T = 4) + P(T = 5) = \frac{1}{6} + \frac{1}{6} = \frac{1}{3}$$

**c.**

$$E(T) = \sum_{i=3}^6 i * p(T = i) = 3 * \frac{1}{3} + 4 * \frac{1}{6} + 5 * \frac{1}{6} + 6 * \frac{1}{3} = \frac{9}{2}$$

$$Var(T) = E(T^2) - E(T)^2 = \frac{131}{6} - \frac{81}{4} = \frac{19}{12}$$

$$SD(T) = \sqrt{Var(T)} = 1.2583$$

**3.**

**a.**

$$P(X = 1) = \frac{1}{8}, P(X = 2) = \frac{1}{4}, P(X = 3) = \frac{3}{8}, P(X = 4) = \frac{1}{4}$$

**b.**

$$P(1 \leq X \leq 3) = \frac{3}{4}, P(X < 3) = \frac{3}{8}, P(X > 1.4) = \frac{7}{8}$$

**4.**

**a.**

$$Y \sim Bin(3, 0.05)$$

**b.**

$$\begin{aligned} P(Y > 1) &= P(Y = 2) + P(Y = 3) \\ &= \binom{3}{2} * 0.05^2 * 0.95 + \binom{3}{3} * 0.05^3 \\ &= 0.0071 + 0.0001 \\ &= 0.0072 \end{aligned}$$

**5.**

**a.**

$$R_z = \mathbb{N}$$

**b.**

$$P(Z = 5) = q^4 * p = 0.95^4 * 0.05 = 0.0407$$

**6.**

con reposicion:

$$X \sim \text{Bin}(3, \frac{1}{5}) \quad F(x) = P(X \leq x) = \begin{cases} 0 & x < 0 \\ 0.512 & x = 0 \\ 0.896 & x = 1 \\ 0.992 & x = 2 \\ 1 & x \geq 3 \end{cases}$$

sin reposicion:

$$P(X = k) = \frac{\binom{4}{k} \binom{16}{3-k}}{1140}, k = 0, 1, 2, 3 \quad F(x) = P(X \leq x) = \begin{cases} 0 & x < 0 \\ 0.4912 & x = 0 \\ 0.9123 & x = 1 \\ 0.9965 & x = 2 \\ 1 & x \geq 3 \end{cases}$$

**7.**

$X$  : cantidad de piezas defectuosas

$$p = \frac{3}{25}$$

$$P(X = 1) = \frac{\binom{3}{1} \binom{22}{4}}{\binom{25}{5}} = 0.4130$$

$$100 * P(X = 1) = 100 * 0.4130 = 41.3$$

**8.**

**a.**

$$P(X = k) = (1 - p)^{(k-1)} * p$$

**b.**

$$P(X = 5) = (1 - p)^4 * p$$

**c.**

$$\frac{\delta}{\delta p}[(1-p)^4 * p] = -(5 * p - 1)(1-p)^3$$

$$\begin{aligned} -(5 * p - 1)(1-p)^3 = 0 &\implies \\ 5 * p - 1 = 0 &\implies \\ p = 0.2 \end{aligned}$$

en  $p = 0.2$  alcanza el maximo