

# EDUC 452 PS3

###Your name goes here###

2025-05-09 10:30:23.543681

This homework is due by **Friday, May 23th, 8:00am**. Upload a html file to Canvas called ps3.html

## 1 Question 1 Correlated Teacher Effects

We observe fairly high correlations ( $r=0.76$ , see here) of teacher effects across reading and math.

```
setwd("/home/bdomingu/Dropbox/stanford/classes/edu452/data") ##set your own directory
load("LA_nice_sub.Rdata")
```

```
library(lme4)
```

```
## Loading required package: Matrix
```

```
##
```

```
## Attaching package: 'Matrix'
```

```
## The following objects are masked from 'package:tidyr':
```

```
##
```

```
## expand, pack, unpack
```

```
ma<-df[df$subject=="MATHEMATICS",]
```

```
mm<-lmer(scale_score_std~scale_score_std_lag_1+in.title1+ell+join.after.k+factor(grade)+factor(year)+(1
```

```
re<-df[df$subject=="READING",]
```

```
mr<-lmer(scale_score_std~scale_score_std_lag_1+in.title1+ell+join.after.k+factor(grade)+factor(year)+(1
```

```
z<-ranef(mm)$teacher_id
```

```
z2<-ranef(mr)$teacher_id
```

```
te<-merge(z,z2,by=0)
```

```
cor(te[, -1])
```

```
##                (Intercept).x (Intercept).y
```

```
## (Intercept).x          1.00          0.76
```

```
## (Intercept).y          0.76          1.00
```

One question we could ask: are these so high that they are in fact evidence that teacher effects don't vary across subject? Especially given that we are focused on younger kids, this might not be a wildly implausible hypothesis. Can you vary 03\_simVAM.R [[https://github.com/ben-domingue/educ452/blob/main/lausd/03\\_simVAM.R](https://github.com/ben-domingue/educ452/blob/main/lausd/03_simVAM.R)] in a way that allows you to observe the kind of variation you get in these correlations when the true DGP has teacher effects being identical? [Hint: This should be a pretty straightforward simulation! If teacher effects are identical across subjects, think about what would need to change/be added to line 20 of 03\_simVAM.R.]

```
### YOUR CODE HERE ###
```

YOUR ANSWER HERE

## 2 Question 2 Grade Retention

Grade retention is an issue. If certain kids in grade 2 aren't moving on to grade 3, this might be a concern given that we are inducing what would seem like substantial selection. Let's think it through to get a sense for how much bias there may be.

### 2.1 2A

If you look at the code prep [[https://github.com/ben-domingu/educ452/blob/main/lausd/00\\_data.R](https://github.com/ben-domingu/educ452/blob/main/lausd/00_data.R)] , how are we effectively handling students that got retained? [Hint: think about the lagged score]

YOUR ANSWER HERE

### 2.2 2B

We might be worried about this. Let's explore it! How would you describe the potential bias introduced there (i.e., describe to me what you are observing as a function of increases in the delta argument)?

```
setwd("/home/bdomingu/Dropbox/stanford/classes/educ452/data") ##set your own directory
load("LA_nice_sub.Rdata")

#####
ma<-df[df$subject=="MATHEMATICS",]
ma<-ma[!is.na(ma$scale_score_std_lag_1),]

library(lme4)
retention<-function(delta=-2,ma) {
  ma$scale_score_std<-NA
  sd.error<-0.55
  sd.teacherfx<-0.29
  te<-rnorm(length(unique(ma$teacher_id)),mean=0,sd=sd.teacherfx)
  te<-data.frame(teacher_id=unique(ma$teacher_id),te=te)
  ma<-merge(ma,te)
  ma$scale_score_std<-0.7*ma$scale_score_std_lag_1+ma$te+rnorm(nrow(ma),mean=0,sd=sd.error)
  ##now let's remove students
  p<-1/(1+exp(-3*(ma$scale_score_std_lag_1-delta)))
  retain<-rbinom(nrow(ma),1,p)
  print(table(retain))
  ma<-ma[retain==1,]
  print(nrow(ma))
  ##
  mod<-lmer(scale_score_std~scale_score_std_lag_1+in.title1+ell+join.after.k+factor(grade)+factor(grade),
    data=ma,REML=FALSE)
  z<-ranef(mod)$teacher_id
  z<-data.frame(teacher_id=row.names(z),est=z[,1])
  z<-merge(te,z)
  z$bias<-z$est-z$te
  y<-by(ma$scale_score_std_lag_1,ma$teacher_id,mean,na.rm=TRUE)
  y<-data.frame(teacher_id=names(y),ly=as.numeric(y))
  z<-merge(z,y)
  list(delta,table(retain),z)
}

out<-list()
for (delta in seq(-3,-1,length.out=5)) out[[as.character(delta)]]<-retention(delta=delta,ma)

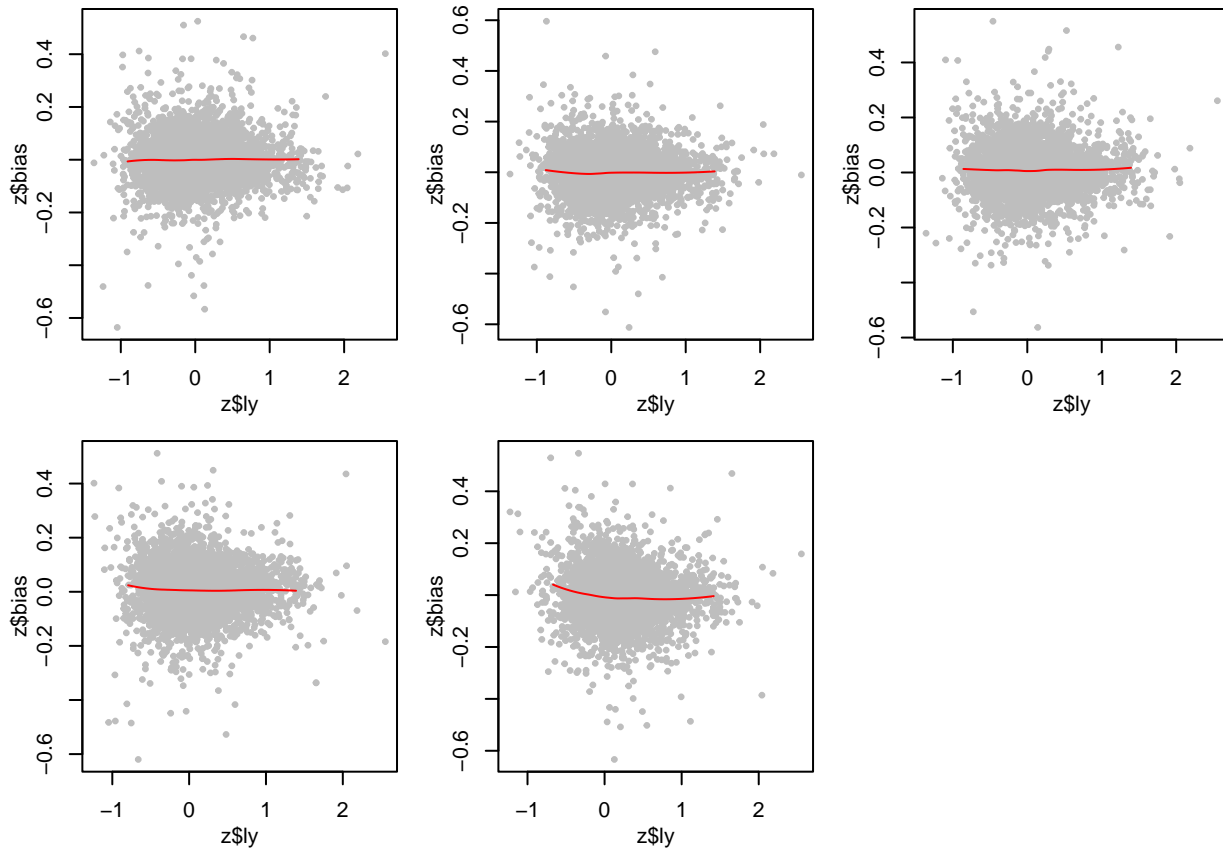
## retain
```

```

##      0      1
##    398 266442
## [1] 266442
## retain
##      0      1
##    1739 265101
## [1] 265101
## retain
##      0      1
##    6254 260586
## [1] 260586
## retain
##      0      1
##   19403 247437
## [1] 247437
## retain
##      0      1
##   46032 220808
## [1] 220808

par(mfrow=c(2,3),mgp=c(2,1,0),mar=c(3,3,1,1))
for (i in 1:length(out)) {
  z<-out[[i]][[3]]
  plot(z$ly,z$bias,col='gray',pch=19,cex=.5)
  mm<-loess(bias~ly,z)
  ly<-seq(quantile(z$ly,.01),quantile(z$ly,.99),length.out=250)
  yv<-predict(mm,data.frame(ly=ly))
  lines(ly,yv,col='red')
}

```



YOUR ANSWER HERE

## 2.3 2C

Each value of delta induced a different passing rate. Relative to these values, what do you think about the possibility of bias in the actual LAUSD data related to passing?

### YOUR CODE HERE ###

YOUR ANSWER HERE

## 2.4 2D

What assumptions would we need to make if we wanted to include retained students in our analyses? How worried about bias in this setting are you?

### YOUR CODE HERE ###

YOUR ANSWER HERE

## 3 Question 3 Differentiation

I have always had this pet theory that differentiating instruction is a really demanding teaching skill. If that were the case, we might imagine a scenario in which a class with more variation in abilities is harder to teach than a class with less variation (note: I'm talking about variances not means. Important!).

Let's test this! [NOTE: No need to "answer" the parts of this question separately. Focus on answering the questions posed in C.]

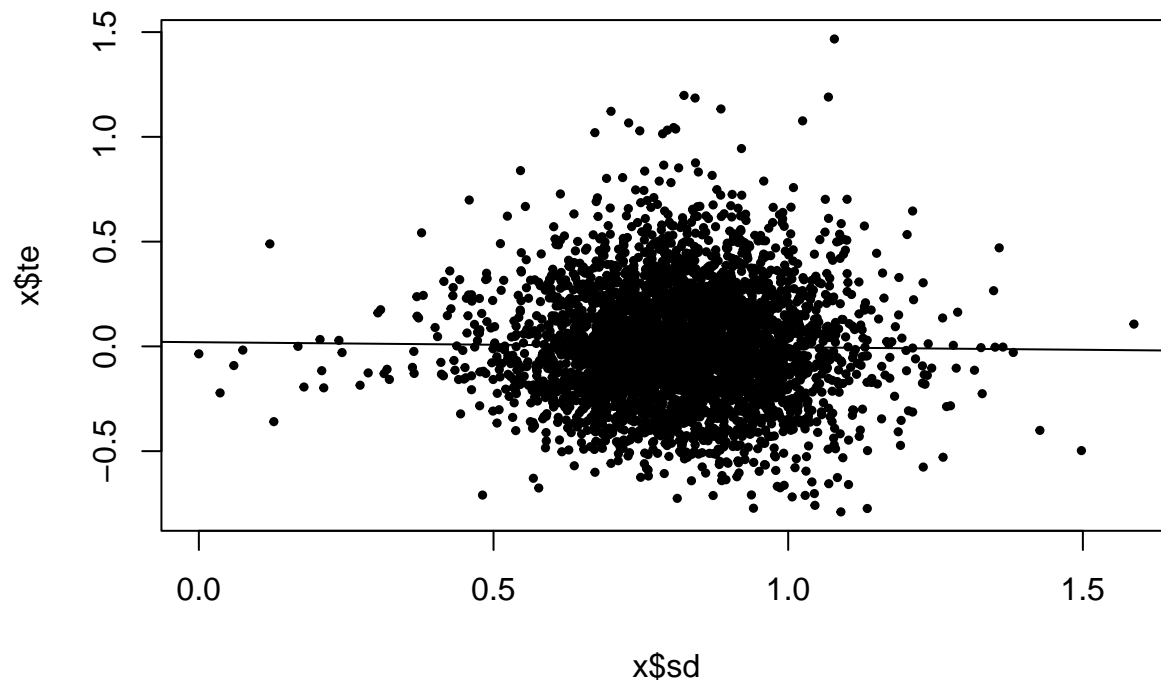
### 3.1 3A

Let's start with an analysis of what there might be empirically.

```
setwd("/home/bdomingu/Dropbox/stanford/classes/edu452/data") ##set your own directory
load("LA_nice_sub.Rdata")

##Let's first look at the empirical data
ma<-df[df$subject=="MATHEMATICS",]
m<-by(ma$scale_score_std_lag_1,ma$teacher_id,mean,na.rm=TRUE)
m<-data.frame(teacher_id=names(m),lm=as.numeric(m))
ma<-merge(ma,m)
mod<-lmer(scale_score_std~scale_score_std_lag_1+lm+in.title1+ell+join.after.k+factor(grade)+factor(year),
          re=~1|teacher_id)
te<-ranef(mod)$teacher_id
te<-data.frame(teacher_id=rownames(te),te=te[,1])
s<-by(ma$scale_score_std_lag_1,ma$teacher_id,sd,na.rm=TRUE)
s<-data.frame(teacher_id=names(s),sd=as.numeric(s))
x<-merge(te,s)

plot(x$sd,x$te,pch=19,cex=.5)
abline(lm(te~sd,x))
```



```
cc<-cor(x$sd,x$te,use='p')
cc
```

```
## [1] -0.014
```

### 3.2 3B

Let's simulate the kind of structure that I have in mind wherein teacher effectiveness varies across teachers but is centered on the SD of prior year abilities.

```
##meh, not much going on, but let's turn to a different question: would we be able to detect it if true
setwd("/home/bdomingu/Dropbox/stanford/classes/edu452/data") ##set your own directory
load("LA_nice_sub.Rdata")
```

```

ma<-df[df$subject=="MATHEMATICS",]
m<-by(ma$scale_score_std_lag_1,ma$teacher_id,mean,na.rm=TRUE)
m<-data.frame(teacher_id=names(m),lm=as.numeric(m))
ma<-merge(ma,m)
sim<-function(ma,scale) { #note we are going to use `scale` to control whether teachers are more/less e
  ma$scale_score_std<-NA
  sd.error<-0.55
  sd.teacherfx<-0.29
  ##
  s<-by(ma$scale_score_std_lag_1,ma$teacher_id,sd,na.rm=TRUE)
  s<-data.frame(teacher_id=names(s),sd=as.numeric(s))
  s$sd<-(s$sd-mean(s$sd,na.rm=TRUE))/sd(s$sd,na.rm=TRUE)
  s<-s[!is.na(s$sd),]
  ##here is where we build in the 'structure' that we are going to then investigate
  te<-rnorm(nrow(s),
            mean=scale*s$sd, #note scale
            sd=sd.teacherfx)
  te<-data.frame(teacher_id=s$teacher_id,te=te)
  ma<-merge(ma,te)
  ma$scale_score_std<-0.7*ma$scale_score_std_lag_1+ma$te+rnorm(nrow(ma),mean=0,sd=sd.error)
  ##
  ma<-ma[!is.na(ma$scale_score_std_lag_1),]
  mod<-lmer(scale_score_std~scale_score_std_lag_1+lm+in.title1+ell+join.after.k+factor(grade)+factor(
  te<-ranef(mod)$teacher_id
  te<-data.frame(teacher_id=rownames(te),te=te[,1])
  x<-merge(te,s)
  cor(x$te,x$sd) #so i'm returning correlations of estimated teacher effects and class SD of prior ab
}
for (scale in seq(-0.25,0.25,length.out=5)) print(c(scale,sim(ma=ma,scale=scale)))

## [1] -0.25 -0.50
## [1] -0.12 -0.29
## [1] 0.0000 -0.0017
## [1] 0.12 0.28
## [1] 0.25 0.51

print("reminder of empirical results")

## [1] "reminder of empirical results"

print(cc)

## [1] -0.014

```

### 3.3 3C

What do you think about the viability of my pet theory in the LAUSD data? Could we detect this if it occurred? Do we?

YOUR ANSWER HERE

### 3.4 3D Bonus [optional]

Do you have a better idea for examining this issue?

```
### YOUR CODE HERE ###
```

YOUR ANSWER HERE

## 4 Question 4 Teaching Lifecycle

When talking about the teacher lifecycle [[https://docs.google.com/presentation/d/1wTaVmwK23ohSGfQlb8OL73ok4D0GgDrtMHB6IRCUSc8/edit#slide=id.g304b82a96db\\_0\\_0](https://docs.google.com/presentation/d/1wTaVmwK23ohSGfQlb8OL73ok4D0GgDrtMHB6IRCUSc8/edit#slide=id.g304b82a96db_0_0)], we noted that there were two processes that seemed to be causing trouble. We discussed one of them - censoring - in class. Let's now think about the other.

### 4.1 4A

Take the data and partition it such that you have teachers who quit after their first years and those who continue. Can you articulate a model that would lead to this distribution?

```
### YOUR CODE HERE ###
```

YOUR ANSWER HERE

### 4.2 4B

Going back to the number of years spent in the classroom, can you build a DGM such that a teacher's decision to quit after the first year is governed by what is in part A and the decision thereafter is driven by an exponential model similar to what we observed in class? What kind of bias does this cause in estimates of  $\lambda$  that come from fitting the naive exponential model?

```
### YOUR CODE HERE ###
```

YOUR ANSWER HERE

## 5 Session info

Information about this R session including which version of R was used, and what packages were loaded.

```
sessionInfo()
```

```
## R version 4.5.0 (2025-04-11)
## Platform: x86_64-pc-linux-gnu
## Running under: Ubuntu 20.04.6 LTS
##
## Matrix products: default
## BLAS: /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.9.0
## LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.9.0 LAPACK version 3.9.0
##
## locale:
##  [1] LC_CTYPE=en_US.UTF-8      LC_NUMERIC=C              LC_TIME=en_US.UTF-8
##  [4] LC_COLLATE=en_US.UTF-8   LC_MONETARY=en_US.UTF-8  LC_MESSAGES=en_US.UTF-8
##  [7] LC_PAPER=en_US.UTF-8     LC_NAME=C                 LC_ADDRESS=C
## [10] LC_TELEPHONE=C           LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
##
## time zone: America/Los_Angeles
## tzcode source: system (glibc)
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods    base
```

```
##
## other attached packages:
## [1] lme4_1.1-37      Matrix_1.7-0      lubridate_1.9.4 forcats_1.0.0  stringr_1.5.1
## [6] dplyr_1.1.4      purrr_1.0.2       readr_2.1.5      tidyr_1.3.1      tibble_3.2.1
## [11] ggplot2_3.5.2    tidyverse_2.0.0   knitr_1.49
##
## loaded via a namespace (and not attached):
## [1] generics_0.1.3    stringi_1.8.4      lattice_0.22-6     hms_1.1.3
## [5] digest_0.6.37     magrittr_2.0.3     evaluate_1.0.1     grid_4.5.0
## [9] timechange_0.3.0  RColorBrewer_1.1-3 fastmap_1.2.0      tinytex_0.54
## [13] scales_1.4.0      reformulas_0.4.1   Rdpack_2.6.4      cli_3.6.3
## [17] rlang_1.1.4       rbibutils_2.3      splines_4.5.0     withr_3.0.2
## [21] yaml_2.3.10       tools_4.5.0        tzdb_0.4.0        nloptr_2.2.1
## [25] minqa_1.2.8       boot_1.3-31        vctrs_0.6.5       R6_2.5.1
## [29] lifecycle_1.0.4   MASS_7.3-63        pkgconfig_2.0.3   pillar_1.10.1
## [33] gtable_0.3.6      glue_1.8.0         Rcpp_1.0.13-1     xfun_0.50
## [37] tidyselect_1.2.1  rstudioapi_0.17.1  farver_2.1.2      htmltools_0.5.8.1
## [41] nlme_3.1-166      rmarkdown_2.29     compiler_4.5.0
```