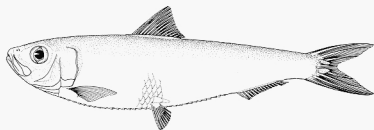


# Assessment For All (a4a)

The stock assessment model



Whitehead, P.J.P., 1985. FAO Species Catalogue.

FAO

**The a4a team**  
European Commission  
Joint Research Centre

# The a4a stock assessment framework

The a4a stock assessment framework is a statistical catch-at-age model written in R with ADMB underneath (to find the parameters). It was written with the aim of quickly developing stock assessment models for stocks with limited time series.

# The a4a stock assessment framework

A model is defined by submodels, which specify the different parts of a statistical catch-at-age model.

There are 5 submodels in operation:

- a model for F-at-age
- a model for the initial age structure
- a model for recruitment
- a (list) of model(s) for abundance indices catchability-at-age
- a list of models for the observation variance of catch-at-age and abundance indices.

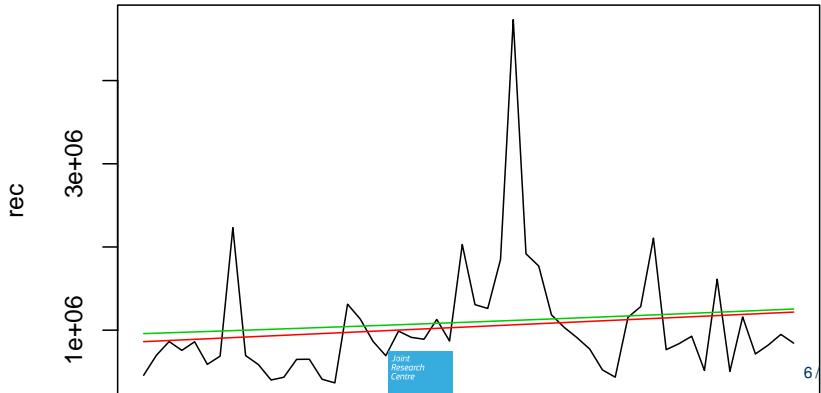
# The a4a stock assessment framework

The submodels form use linear models. This opens the possibility of using the linear modelling tools available in R: see for example the `mgcv` gam formulas, or factorial design formulas using `lm()`. In R's linear modelling language, a constant model is coded as `~ 1`, while a slope over age would simply be `~ age`. For example, we can write a traditional year/age separable F model like `~ factor(age) + factor(year)`.

## linear model examples

```
rec <- c(rec(ple4)) year <- as.numeric(dimnames(rec)[2])  
rlm <- lm(rec ~ year) scafit <- sca(ple4, ple4.indicator)  
srmodel = year)
```

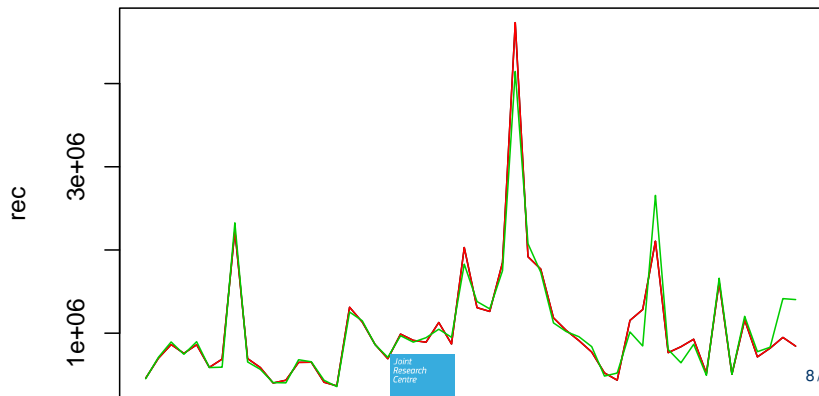
# linear model examples



# linear model examples

```
rlm <- lm(rec factor(year)) scafit <- sca(ple4, ple4)
srmodel = factor(year)
```

# linear model examples





## Model detail

$$e^{E[\log C]} = \frac{F}{F+M} (1 - e^{-F-M}) R e^{-\sum F+M}$$

and

$$e^{E[\log I]} = Q R e^{-\sum F+M}$$

and

$$\text{Var}[\log C_{ay}] = \sigma_{ay}^2 \quad \text{Var}[\log I_{ays}] = \tau_{ays}^2$$

## Model detail

linear models for

- $\log F$
- $\log Q$
- $\log$  observation variances
- $\log$  initial age structure

Recruitment is modelled as a **fixed variance** random effect with linear models for

- $\log a$
- $\log b$

where relevant. Models available: Ricker, Beverton Holt, smooth hockeystick, geometric mean

# Linear models

It is not always obvious that stock assessments are often composed of linear models.

For example, the classical separable  $F$  assumption is simply that

$$F_{ay} = S_a \times F_y$$

which, in linear modelling parlance is

$$\log F \sim \text{age} + \text{year}$$

# Intuitive Modelling

The "language" of linear models has been developing within the statistical community for many years:

- 1965 J. A. Nelder, notation for randomized block design
- 1973 Wilkinson and Rodgers, symbolic description for factorial designs
- 1990 Hastie and Tibshirani, introduced notation for smoothers
- 1991 Chambers and Hastie, further developed for use in S

Many modelling software use this language: Minitab, spss, genstat, SAS, R, S-plus.

## Some examples

A separable model where the level of  $F$  is smooth through time

$$\log F \sim \text{age} + s(\text{year})$$

## Some examples

A separable model where  $F$  is smooth over age

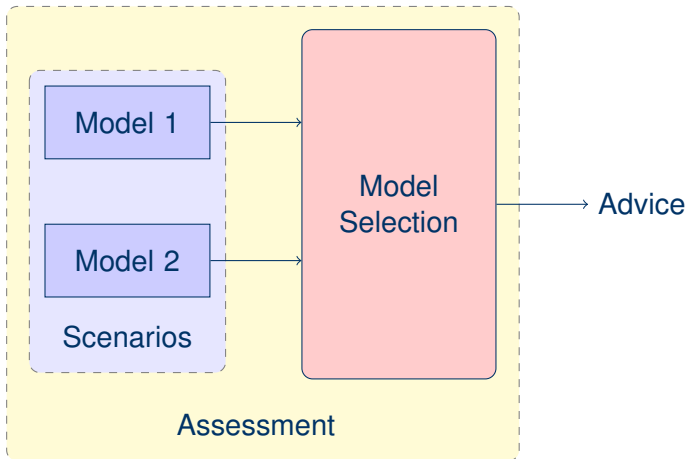
$$\log F \sim s(\text{age}) + \text{year}$$

## Some examples

$F$  is smooth over age and year

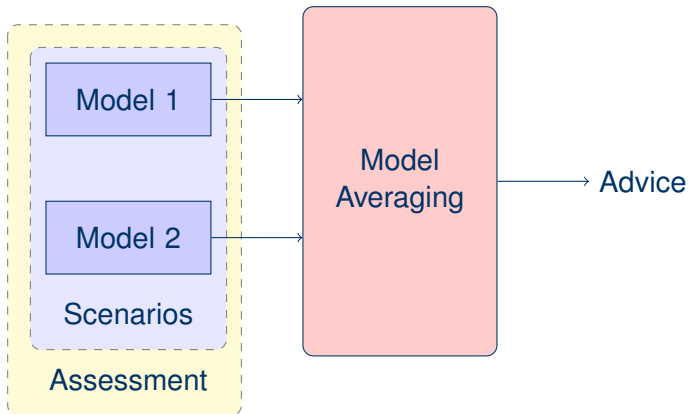
$$\log F \sim s(\text{age}, \text{year})$$

# An Assessment Process





# Model Averaging can help automation



## Expert knowledge for model specification

Different plausible models for different levels

- Management area level (North Sea, Baltic Sea, ...)
- Species type (roundfish, flatfish, pelagic, Nephrops)
- specific groups (North Sea gadoids)

This provides a framework for setting up plausible models for new species.

Can lots of simple models averaged = a good model?

*Kearns: Can a set of weak learners create a single strong learner*

**Thank you for listening!**

# What we can do, what we can't do

## Can:

- missing values: missing at random
- multiple surveys
- variable Q, F, variance
- splines (fixed degree of freedom)
- stock recruit relationship (fixed variance)
- stock recruit relationship (estimated variance) SLOW
- *fixed variance random effects: RW1, RW2, seasonal, user specified*

## Can't:

- estimate random effect variance
- estimate smoothing parameters
- estimate growth parameters

# What we can do

- simulate from the distribution of model params
  - normal approx
  - avoids the need for delta approx
  - can be biased, but we can also use MCMC if desired
- we can approximate the (joint) distribution of
  - terminal year  $F_s$  and  $N_s$
  - terminal year  $F_{bar}$  and  $F_{msy}$
  - $F / F_{msy}$