

Q 3) Solution

pressure = 6 MPa

Avg radius = 5.6 mm

Cladding thickness = 0.6 mm

- a) The assumptions made in the thin walled cylinder approximation for the stress state are:
- We assume very small strains
  - We also assume isotropic material response

-3, Stress constant across wall thickness

- b) All three components of the stress using the thin walled cylinder approximation are:

$$\bar{\sigma}_\theta = \frac{PR}{\delta} = 6 \text{ MPa} \left( \frac{0.56}{0.06} \right)$$

$$\bar{\sigma}_\theta = 55.99 \approx \boxed{60 \text{ MPa}}$$

$$\bar{\sigma}_z = \frac{PR}{2\delta} = 6 \text{ MPa} \left( \frac{0.56}{2 \times 0.06} \right)$$

$$\bar{\sigma}_z = \boxed{27.99 \text{ MPa}}$$

$$\bar{\sigma}_r = -\frac{1}{2} P = -\frac{1}{2} \cdot 6 \text{ MPa}$$

$$\bar{\sigma}_r = \boxed{-3 \text{ MPa}}$$

c) Using thin walled cylinder approximation for cladding is less accurate than that of using thick wall approximation. This is because we only care about steady state solution, consider axisymmetric, temperature is constant on z-direction and the thermal conductivity  $k$  is independent of temperature but in thick we do not assume more.

-10, Calculate stress at two radii using thick wall equations and see if constant and compare to answer from part b

d) solution:

$$E = 70 \text{ GPa}, \nu = 0.41$$

To find: stress and strain tensors.

$$C_{11} = E(1-\nu) / ((1+\nu)(1-2\nu))$$

$$C_{11} = 70(1-0.41) / ((1+0.41)(1-2 \times 0.41))$$

$$C_{11} = 70(0.59) / ((1.41)(1-0.82))$$

$$C_{11} = 70(0.59) / 0.2538$$

$$C_{11} = 162.7265 \text{ GPa}$$

$$C_{12} = 70(0.41) / ((1.41)(1-0.82)) = 113.08 \text{ GPa}$$

-4, Stress and strain not shown in tensor form

-5, Calculate strains from stress from part b



Beda Kafley

Nuclear Engineering 947

Exam # 1

81) Solution.

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Given:

$U_3Si_5$  as fuel material

Thermal conductivity =  $12.5 \text{ W/mK}$

density =  $7.5 \text{ grams of U/cm}^3$

a) The fissile material in  $U_3Si_5$  is naturally occurring uranium which is Uranium-235.  
Uranium-235.

Uranium-235 would have enrichment ~~at~~ in the natural (enrichment) form of the fuel.

b)

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c) Ranking of  $U_3Si_3$  as a potential fuel compared to  $U_3Si_2$  would be:

⇒ 1<sup>st</sup> choice =  $U_3Si_2$   
2<sup>nd</sup> choice =  $U_3Si_3$

$U_3Si_2$  is better fuel material than  $U_3Si_3$  because  $U_3Si_3$  has much higher melting point than that of  $U_3Si_2$ .

→ Also,  $U_3Si_2$  have the advantage of much higher heat conductivity than  $U_3Si_3$  which cannot survive equally high temperature as of  $U_3Si_2$ .

-3, Uranium density?