

# Nuclear Fuel Performance

NE-533  
Spring 2024

# NUMERICAL THERMO-MECHANICS

# Now we can solve the temperature and the displacement vector for the full thermomechanical problem

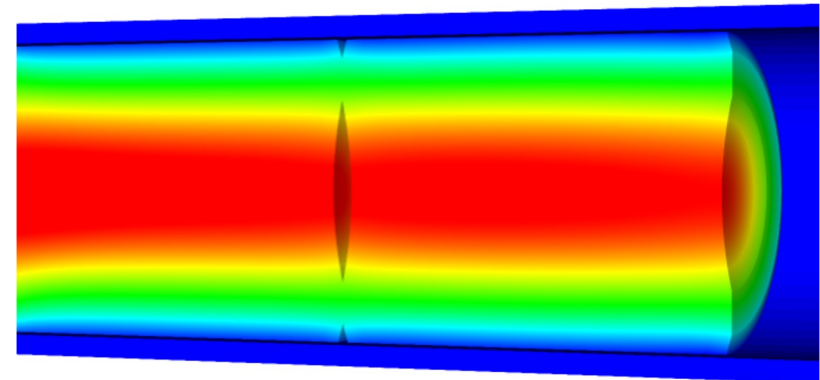
- $T$  impacts the value of  $\mathbf{u}$  through thermal expansion
- $\mathbf{u}$  impacts the value of  $T$  through changes in the thickness of the gap
- The value for  $T$  evolves with time
- The value for  $\mathbf{u}$  also evolves with time, even though there is not time in its PDE

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

$$\boldsymbol{\sigma} = \mathcal{C}(\boldsymbol{\epsilon} - \alpha(T - T_{fab})\mathbf{I})$$

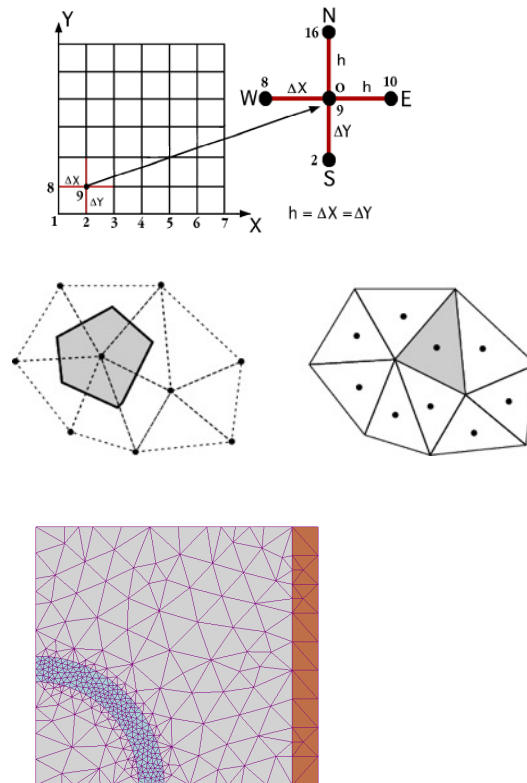
$$0 = \nabla \cdot \boldsymbol{\sigma}$$

$$\boldsymbol{\epsilon} = \frac{1}{2} (\nabla \mathbf{u} + \nabla \mathbf{u}^T)$$

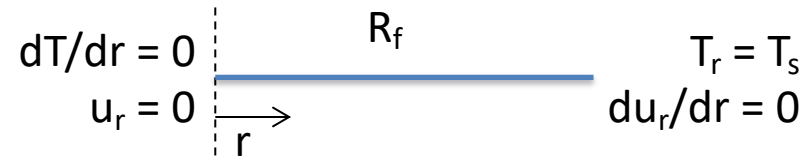


# The primary tool for solving all thermomechanics problems is the finite element method

- **Finite difference**
  - Can solve the heat conduction equation
  - Can't easily solve the mechanics equations
- **Finite Volume**
  - Can solve the heat conduction equation
  - Can solve the mechanics equations
  - Eqns derived from fluid dynamics
- **Finite Element**
  - Can solve the heat conduction equation
  - Can solve the mechanics equations
  - Can handle any geometry
  - Can handle any boundary condition



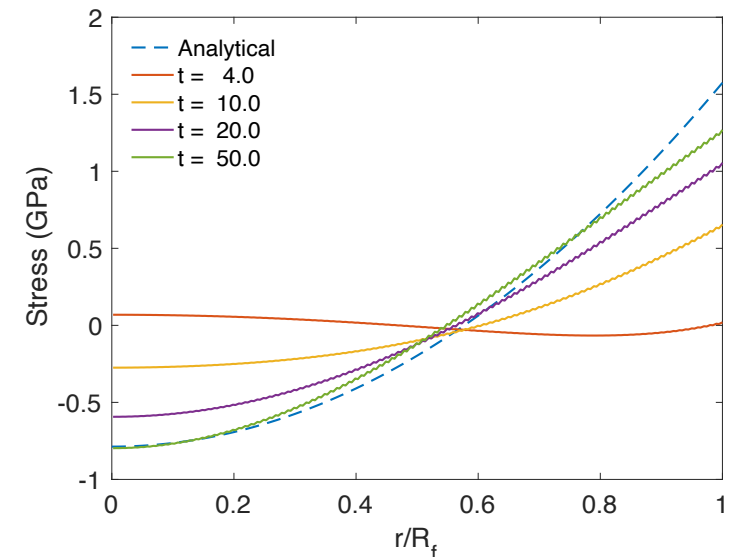
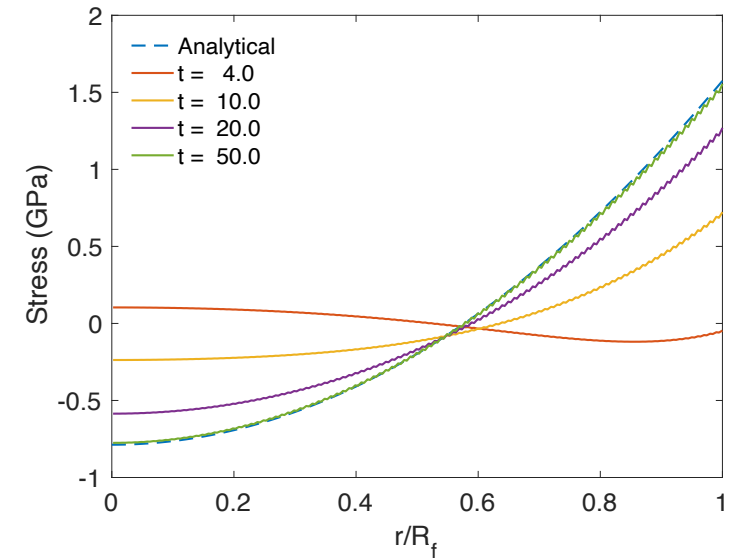
# The 1D thermomechanics problem definition



- The initial temperature is set to 273 K
- We will take 50 time steps of 0.5 s
- The full power of  $Q = 450$  begins at time  $t = 0$ .
- $\text{UO}_2$  material properties are used for both the thermal and mechanics equations

# Comparison to analytical theory

- If we use a constant thermal conductivity, analytical 1D model matches very well
- When  $k$  is a function of temperature, there is a difference between the FEM and analytical stress



# There are various available tools for solving coupled thermomechanical problems with FEM

- Commercial tools
  - ABAQUS
  - ANSYS
  - COMSOL
- Open source
  - MOOSE
- NRC-based
  - FRAPCON/FRAPTRAN

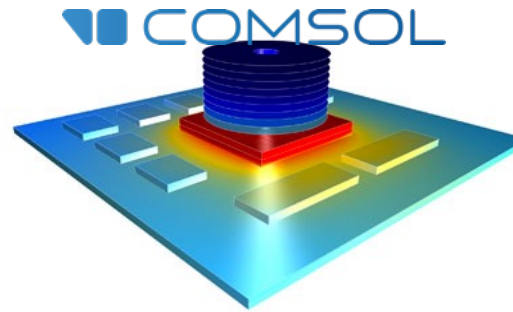
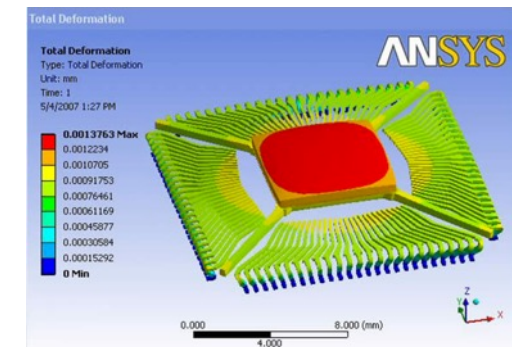
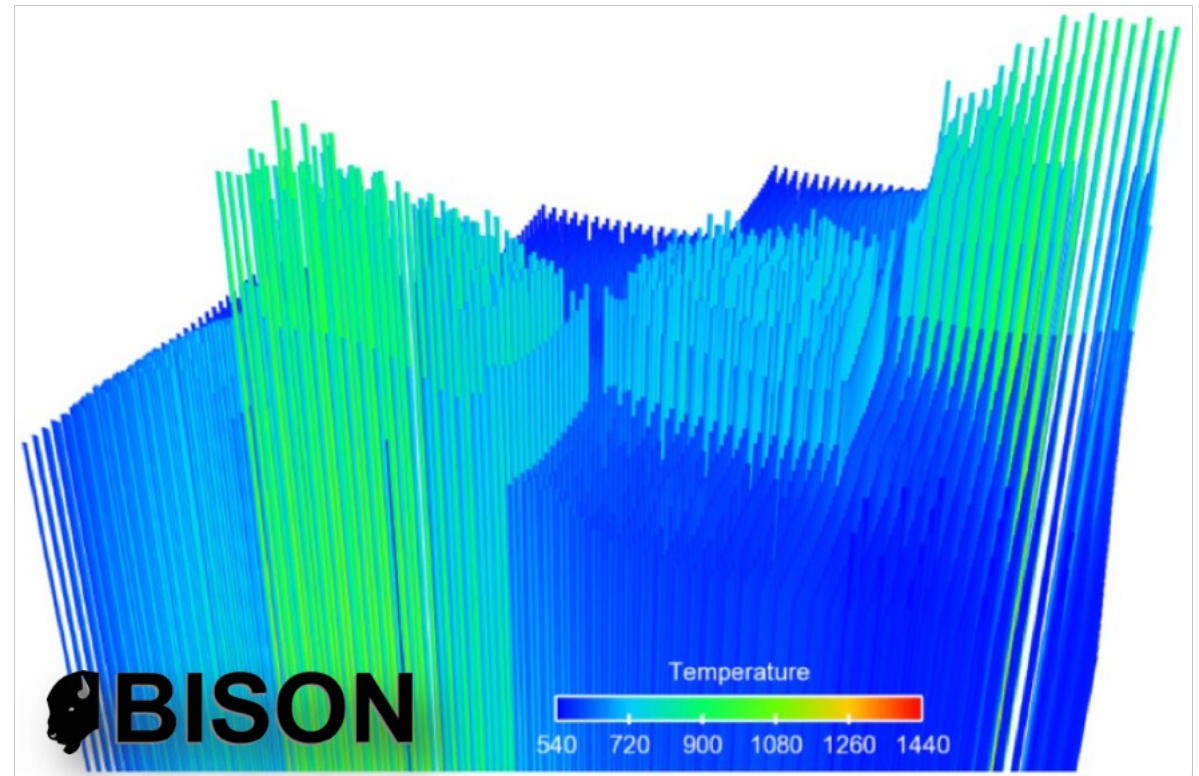


Figure 4. Temperature contour plot of exhaust manifold.



# The purpose of a fuel performance code is to simulate and evaluate fuel rod behavior

- The first fuel performance codes were developed in the mid seventies
- Advanced fuel performance codes are still under development today

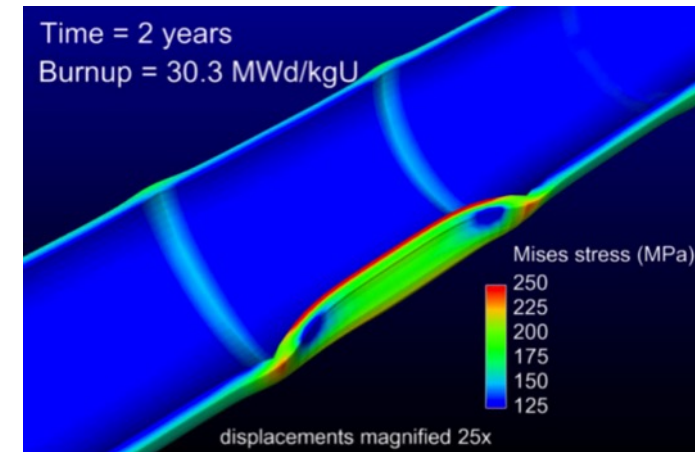
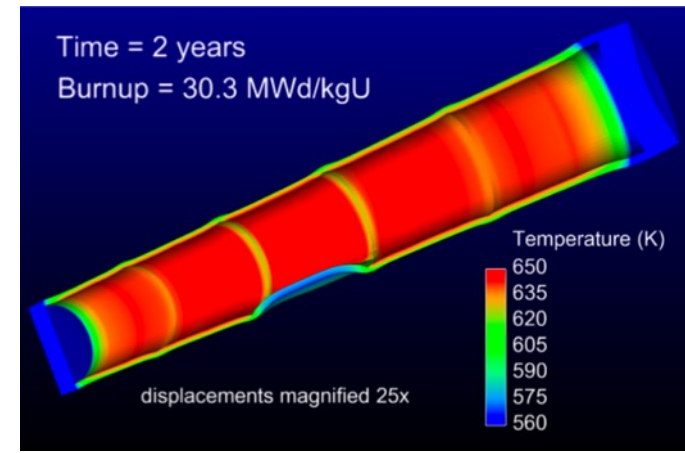
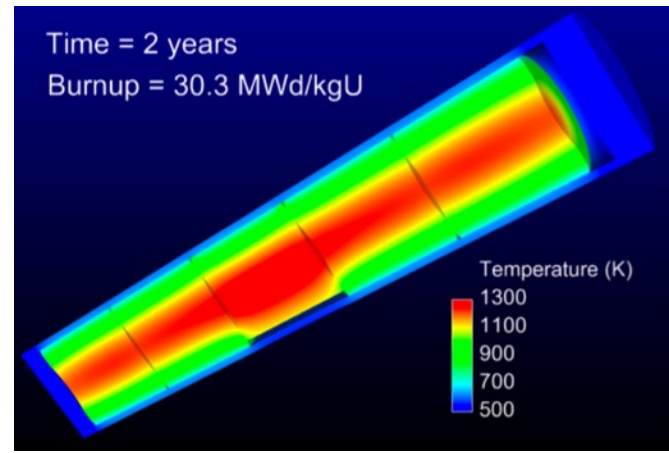


KAIST-3A benchmark results, showing displacement of 3432 rods, from Gaston et al. 2014



## How are fuel performance codes used?

- The primary goals are to predict the fuel centerline temperature and the stress in the cladding
- Fuel performance codes aren't focused on predicting power production, but rather to predict safety margins, provide coupling to other codes



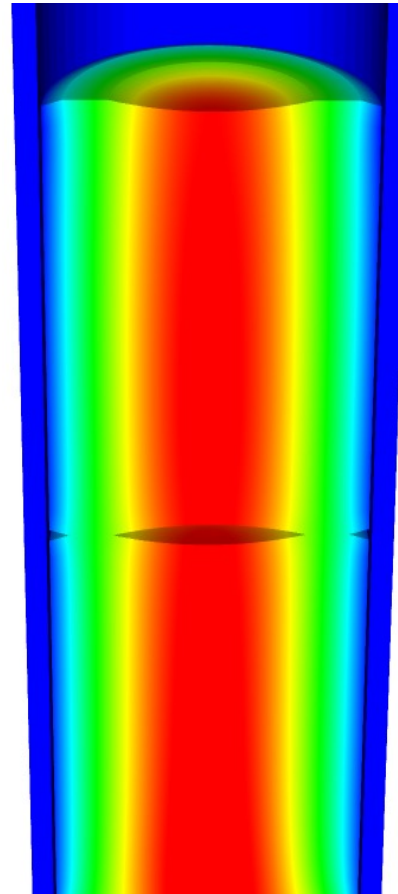
# A fuel performance code must be able to predict:

## Fuel

- Temperature profile
- Volumetric change

## Cladding

- Temperature profile
- Stress



## Gap

- Gap heat transport
- Mechanical interaction between fuel and cladding
- Gap pressure

# The primary focus is solving the thermomechanical problem

## Fuel

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved Numerically*

$$0 = \nabla \cdot \sigma$$

*Solved Numerically or  
analytically*

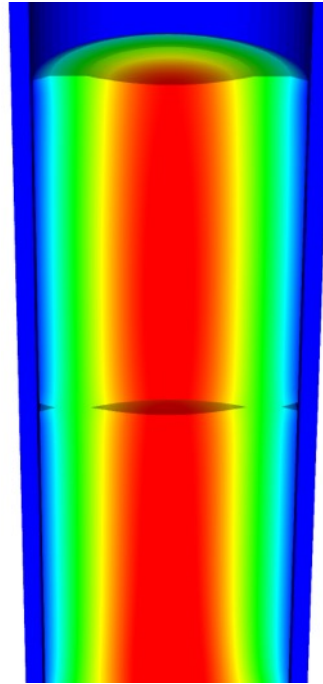
## Cladding

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved Numerically or  
analytically*

$$0 = \nabla \cdot \sigma$$

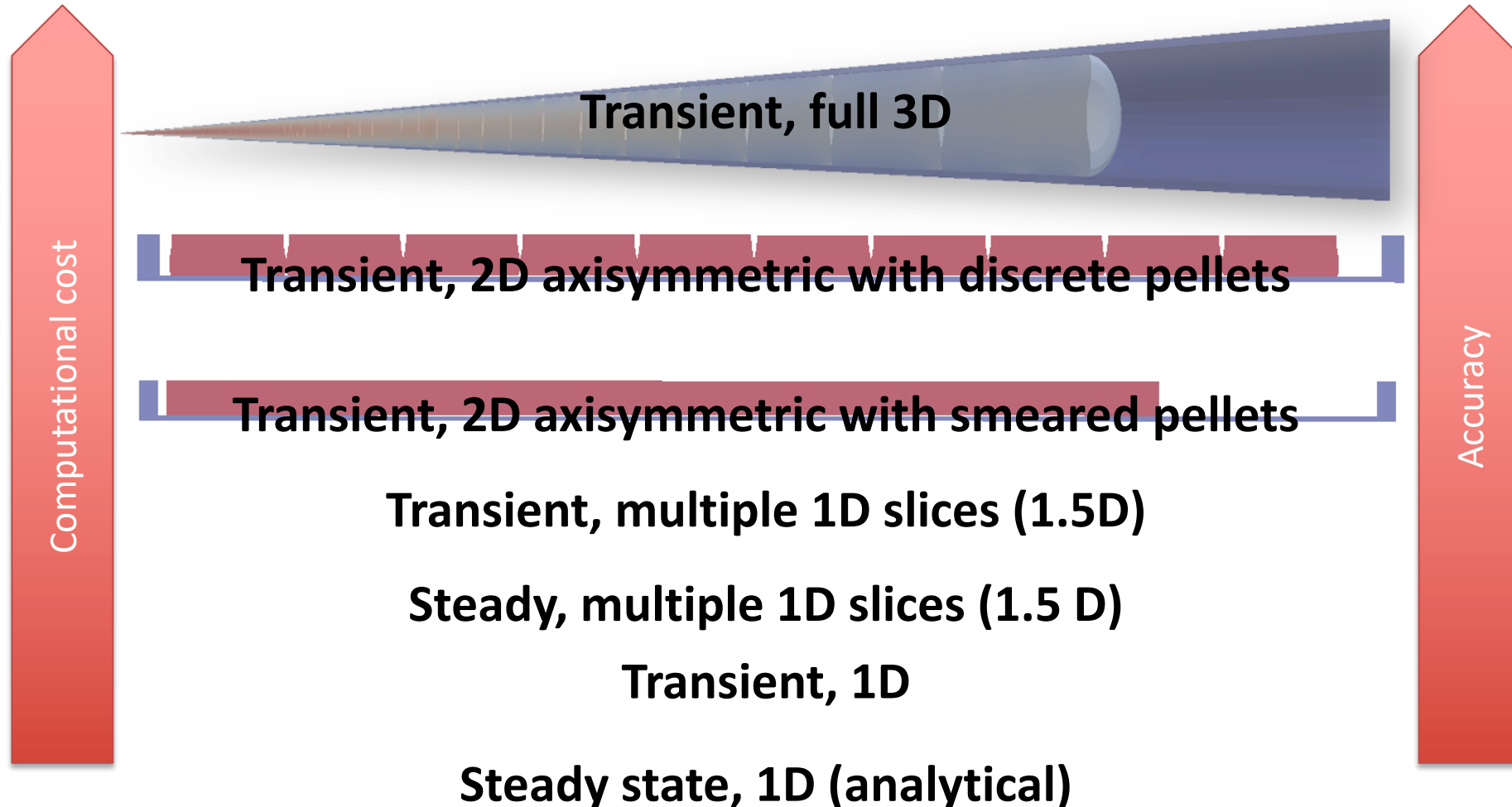
*Solved Numerically*



## Gap

- The handling of the gap changes the most between different codes

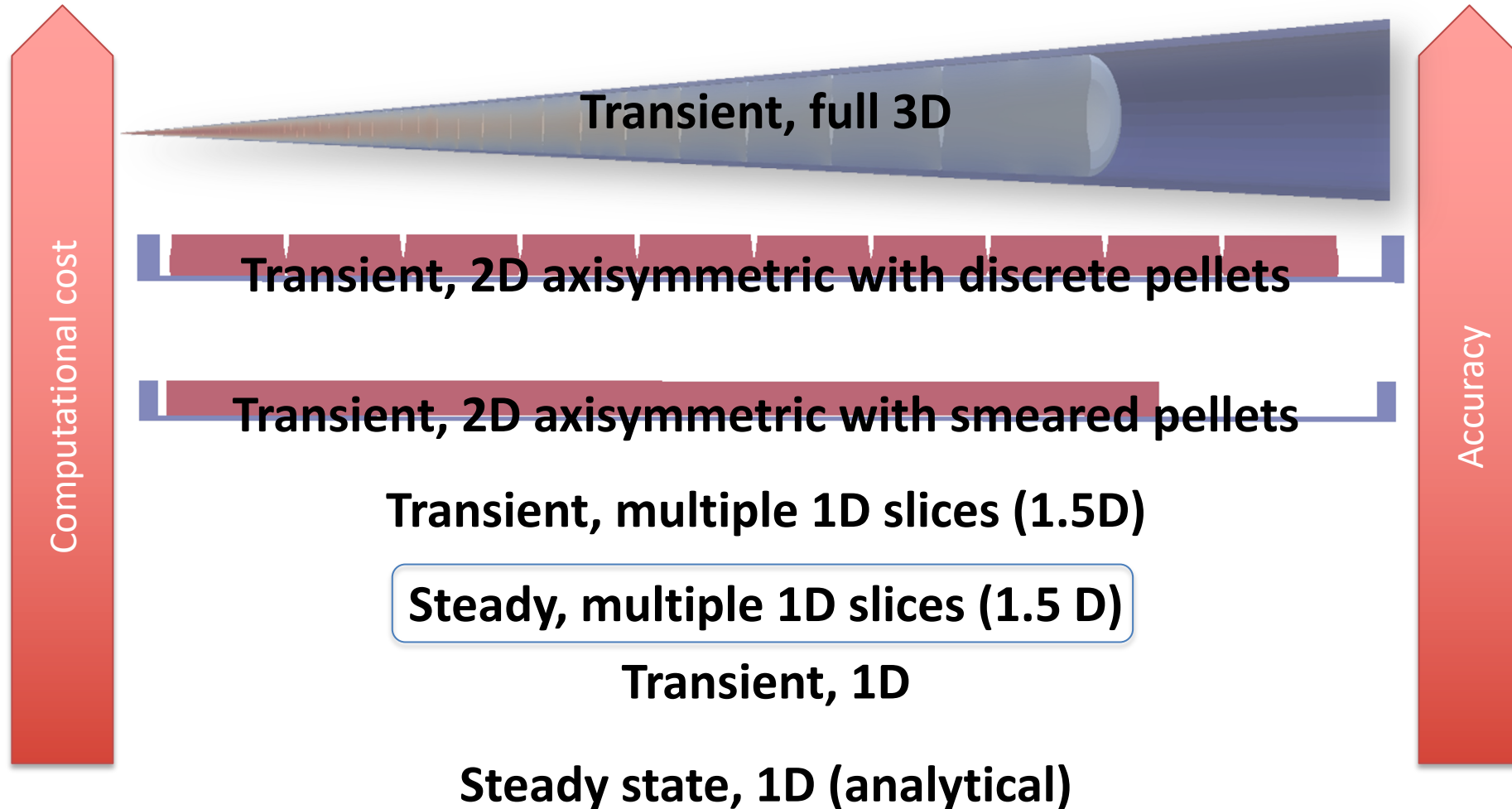
# Various approaches to model the fuel rod



# Early fuel performance codes were made for either steady state or transient operation

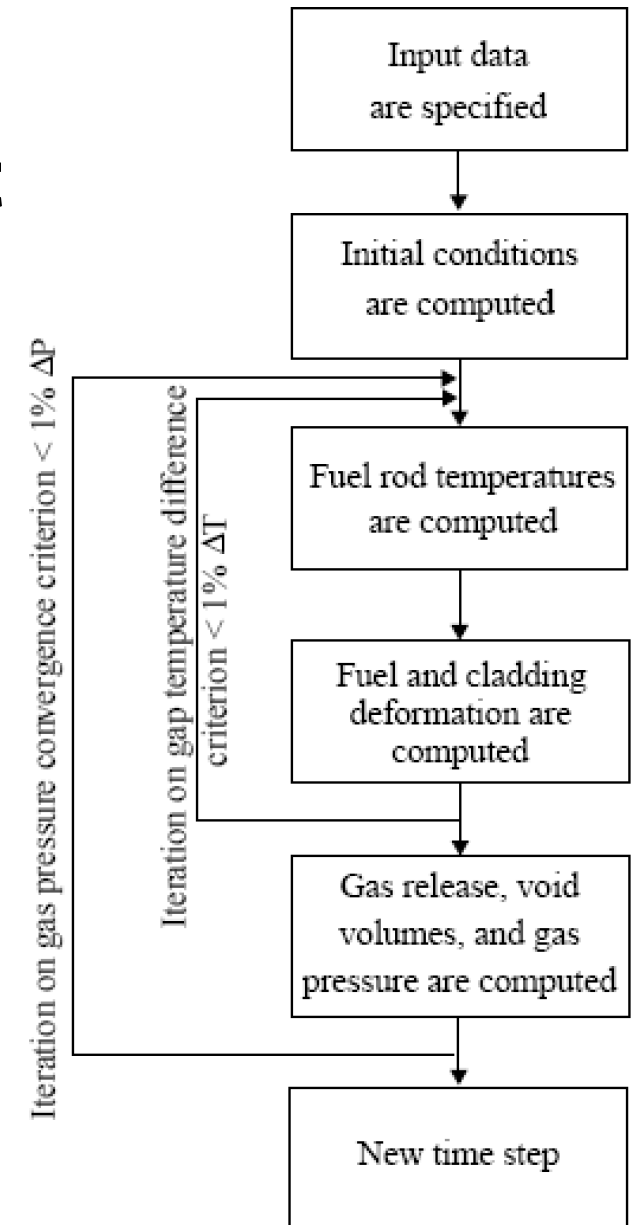
- Steady state codes
  - Leave off the time derivative part of the heat equation  $\nabla \cdot (k \nabla T) + Q = 0$
  - The material properties still evolve with time as a function of burnup
  - The volumetric changes in the fuel are also a function of burnup
  - Creep of fuel and cladding change with time
- Transient codes
  - Include the time derivative  $\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$
  - Have similar burnup dependent models like steady state codes, but don't include creep
  - Have additional models for rapid transients

# Start with FRAPCON

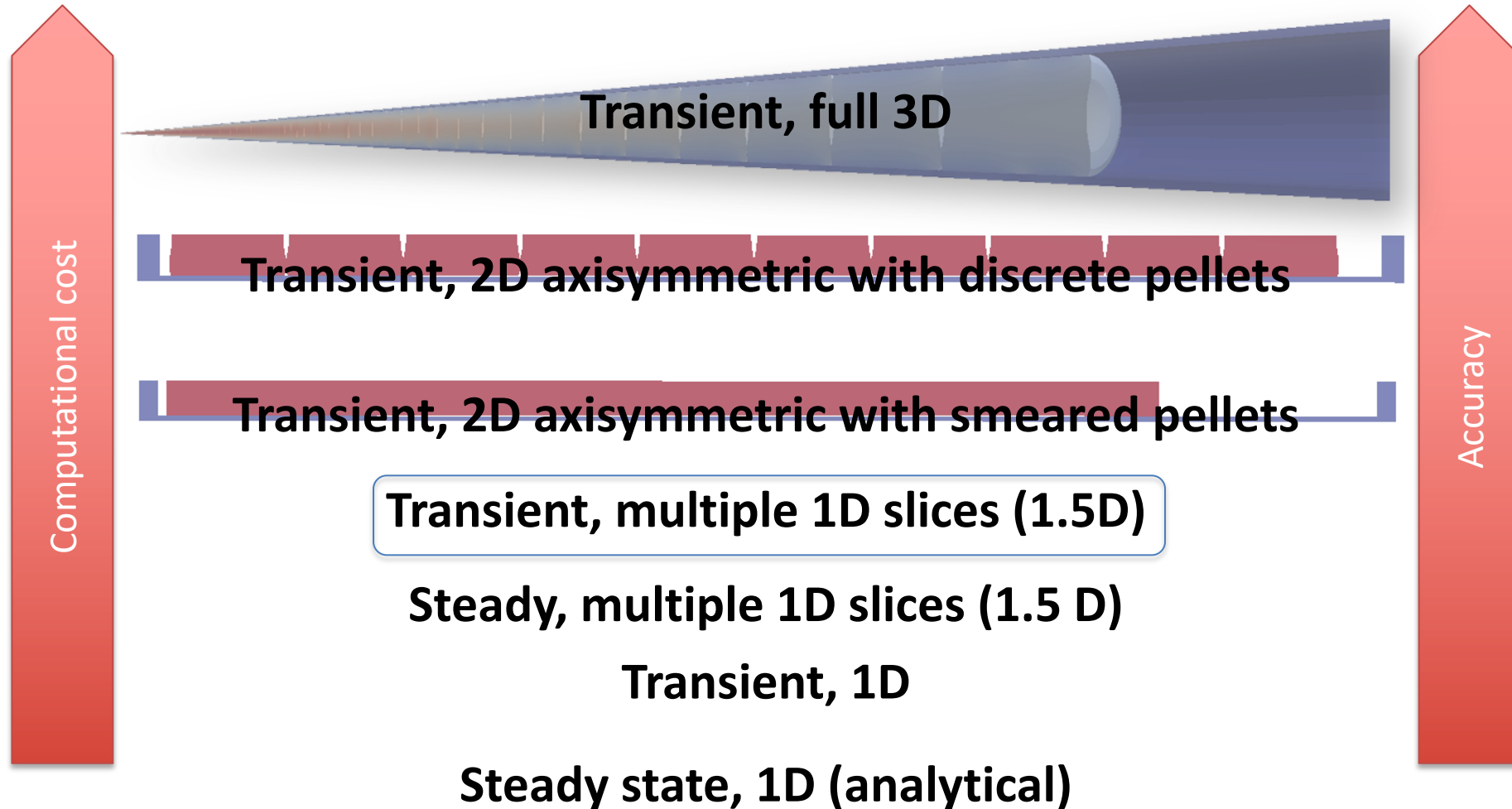


# FRAPCON Flow Chart

- FRAPCON is the NRC's steady-state fuel performance code
- FRAPCON has the ability to accurately calculate the high-burnup response of light-water reactor fuel rods
- FRAPCON iterates to determine fuel rod temperatures, fuel and cladding deformation
- This converged data is iterated to produce gas release, void volumes and plenum pressure
- Then marches forward in time

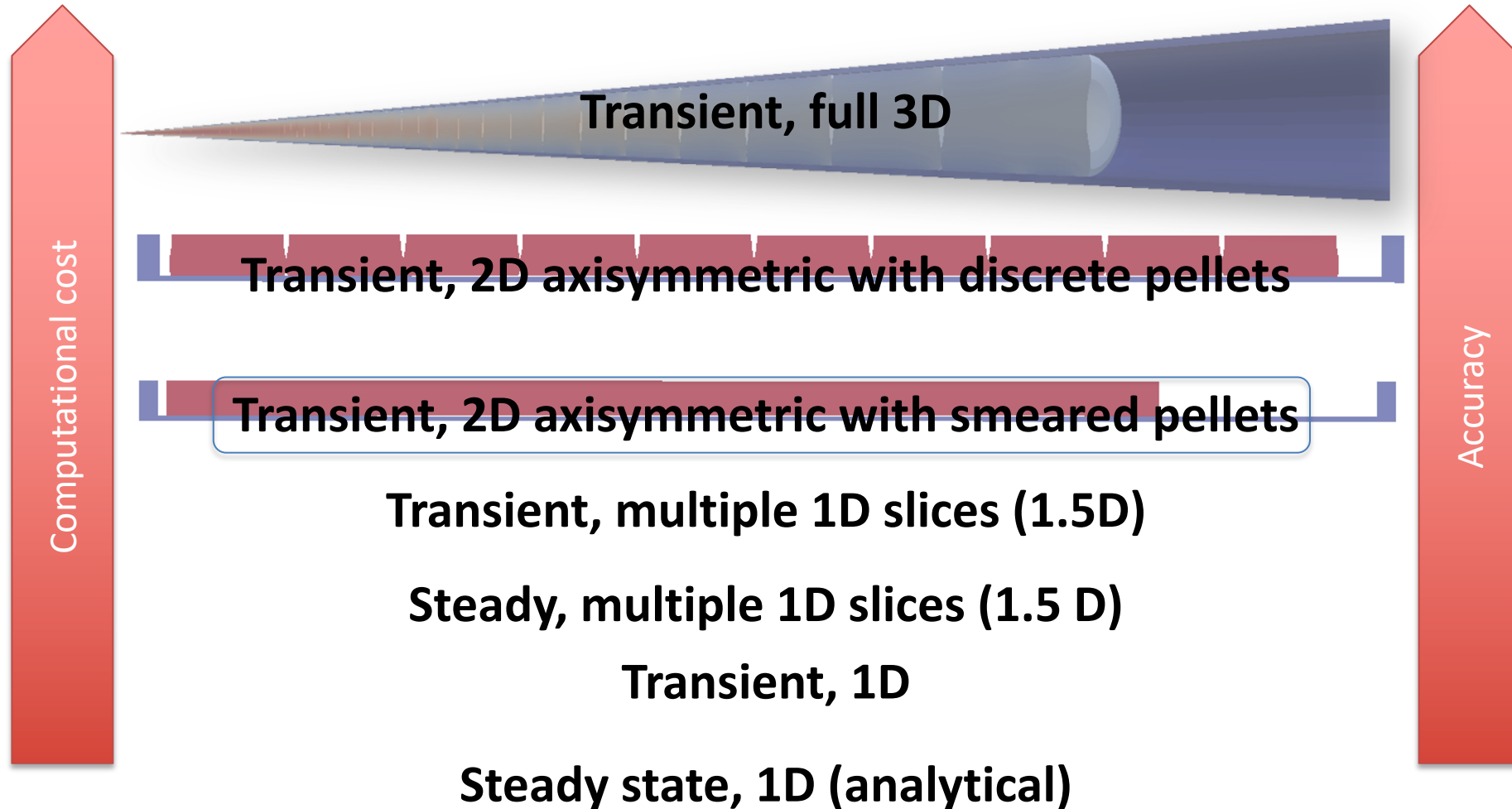


# FRAPTRAN





# FALCON



# FALCON

- FALCON is a 2D fuel performance code developed by EPRI
- Development of FALCON started in 1996
- The beta version was released in 2003
- It was developed by ANATECH for EPRI
- FALCON is proprietary, owned by EPRI
- It is no longer under active development in the US

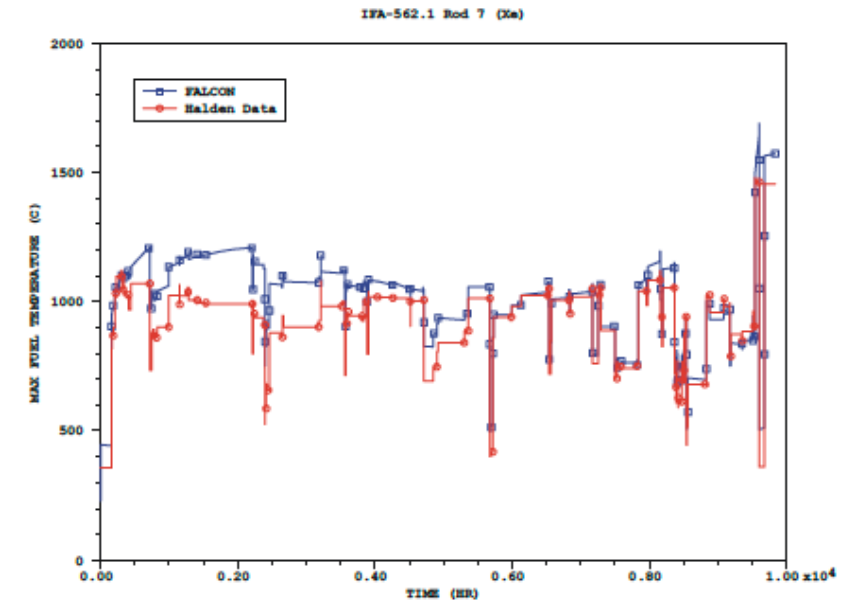


Figure 3-6  
Calculated Fuel Temperatures Versus Measured Data for IFA-562.1 Rod 7 (Xe-filled)

# FALCON is a 2D transient and steady state code

## Fuel

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved with FEM*

$$0 = \nabla \cdot \sigma$$

*Solved with FEM*

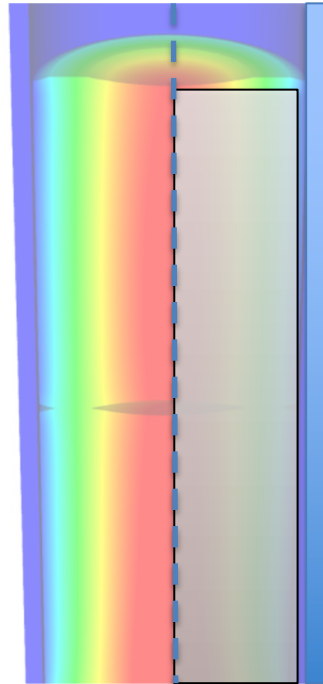
## Cladding

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved with FEM*

$$0 = \nabla \cdot \sigma$$

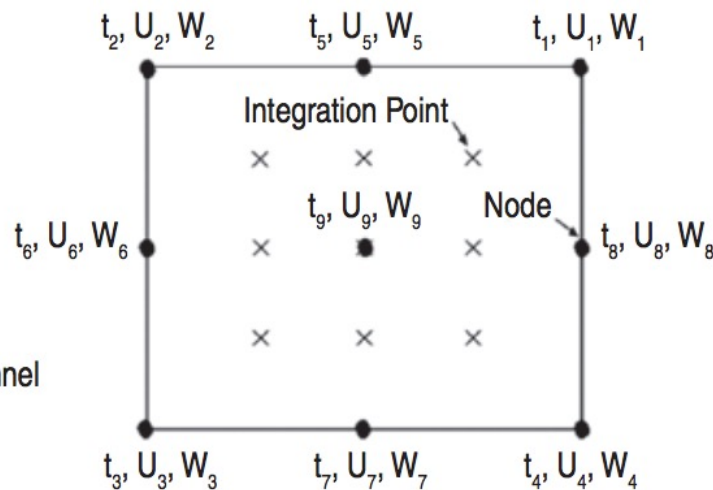
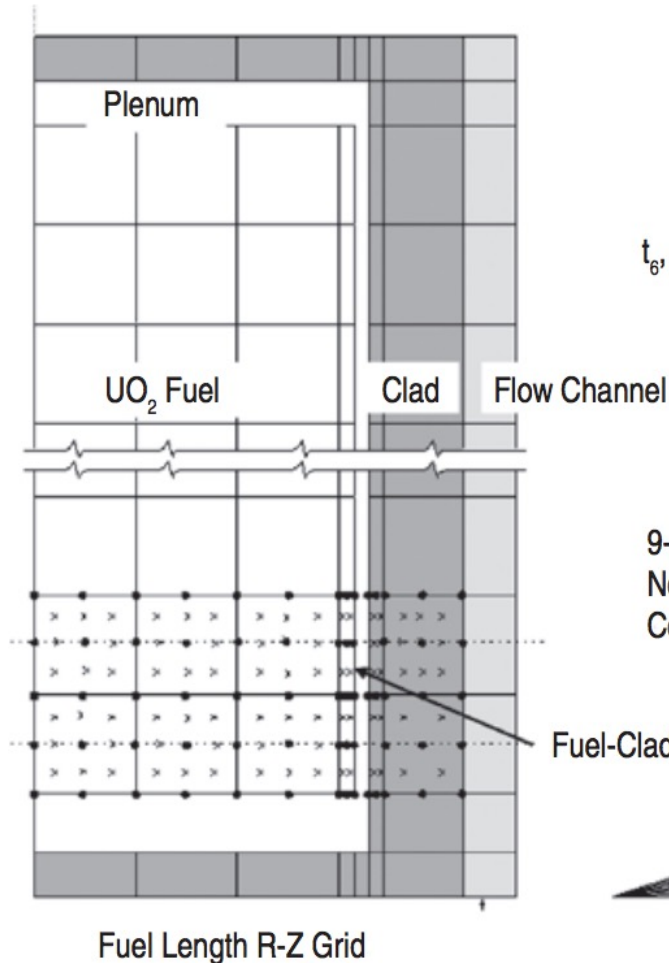
*Solved with FEM*



## Gap

- Pressure is calculated using equation of state
- Simplified contact model is used for gap closure
- Gap heat transfer model is used

# FALCON can predict the fuel performance in axisymmetric RZ space or in R $\theta$ space



9-node Finite Element - Full Quadratic Interpolation  
 Nodal Variables: 1 Temperature & 2 Displacements  
 Constitutive Models Defined at Integration Points.

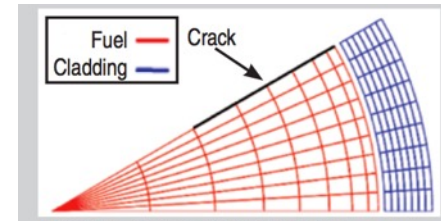
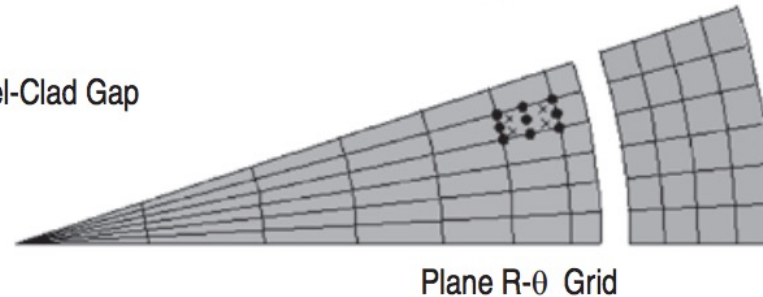


Figure 3. Standard PCI model.

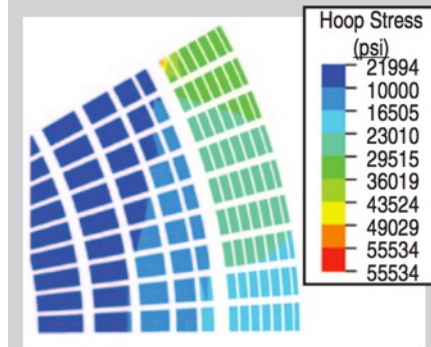


Figure 4. Calculated cladding hoop stress distribution (psi) using the standard PCI model.

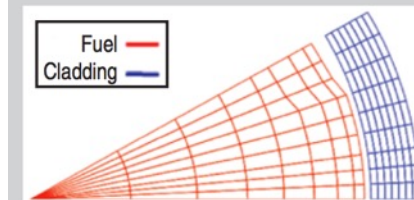
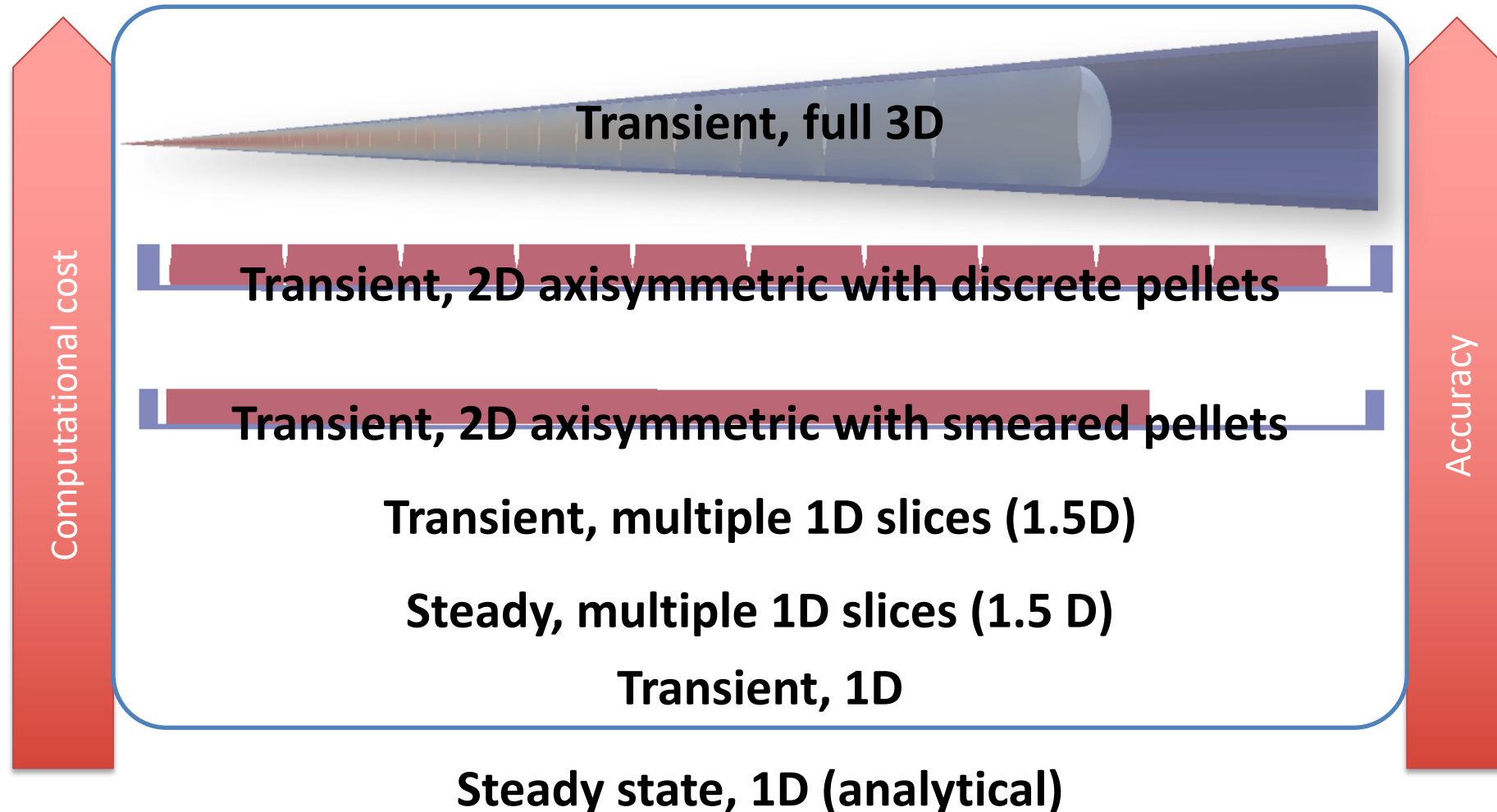


Figure 5. Missing pellet surface (MPS) PCI model.

# BISON



# BISON

- The next generation fuel performance code under development in the US
- It uses the MOOSE framework
- Development was begun in 2008
- The first paper using BISON was published in 2009 and the paper summarizing its full capabilities was published in 2012
- It was developed at Idaho National Laboratory, with some support by ANATECH
- BISON is available for free, but it is export controlled and requires a license agreement be signed

# BISON models the fuel behavior ranging from 1D to full 3D and uses FEM

## Fuel

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved with FEM*

$$0 = \nabla \cdot \sigma$$

*Solved with FEM*

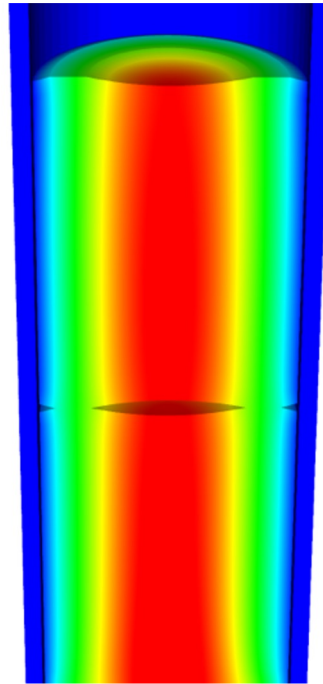
## Cladding

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot (k \nabla T) + Q$$

*Solved with FEM*

$$0 = \nabla \cdot \sigma$$

*Solved with FEM*

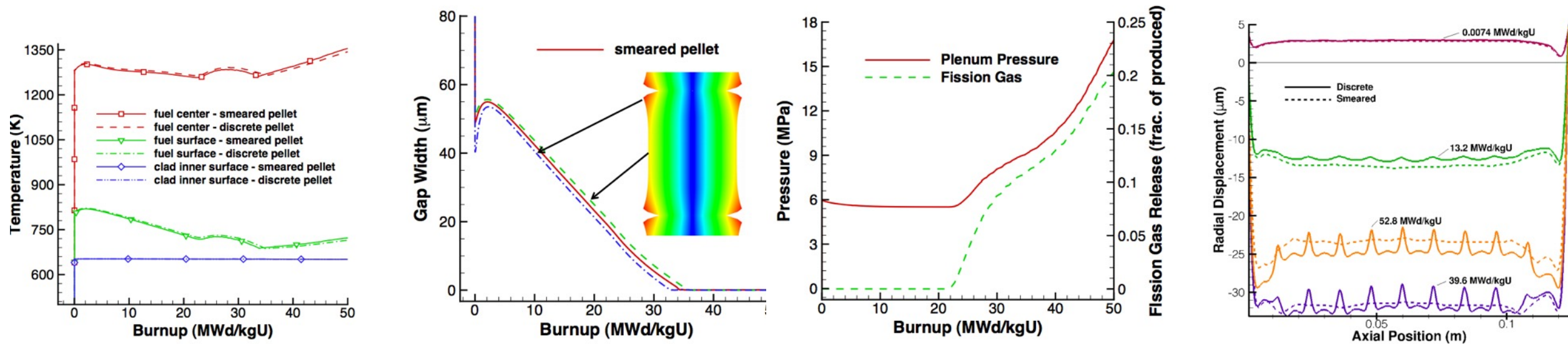


## Gap

- Pressure is calculated using equation of state
- Fully implemented implicit contact algorithm
- Gap heat transfer model is used

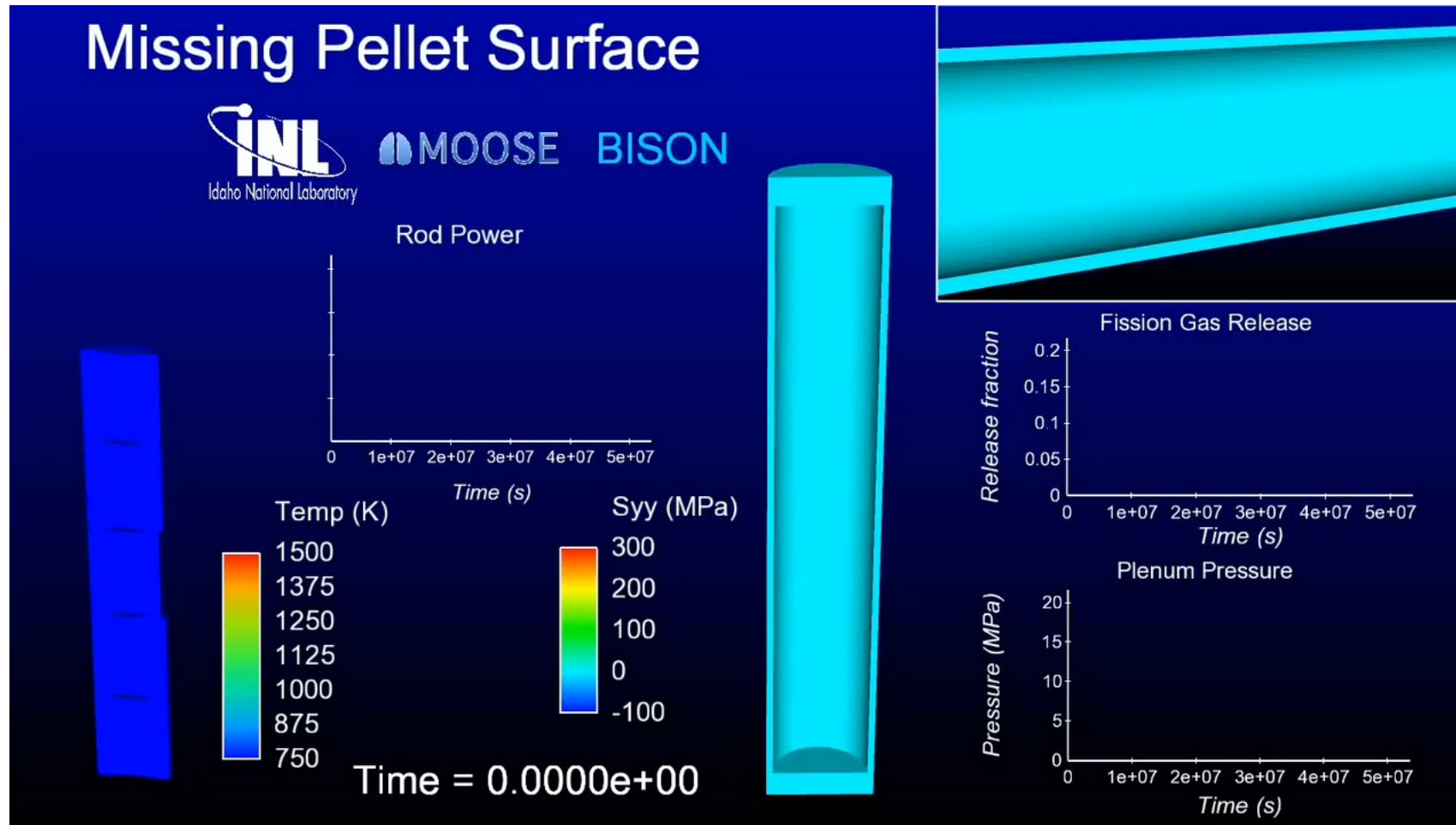


# Can handle smeared or discrete pellets, asymmetric pellet geometry and deformation





# Because of its unique 3D capability, BISON can model truly 3D fuel performance problems

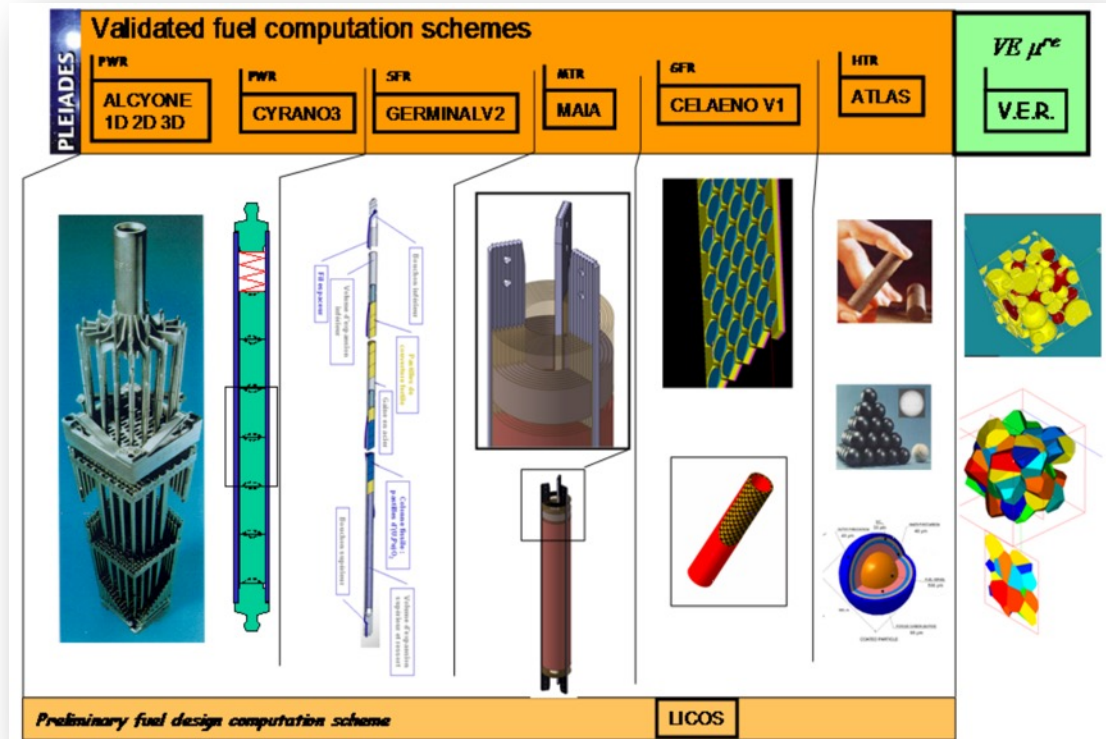


# Other countries have other fuel performance codes

**Table 1**

List of fuel rod performance codes developed in different parts of the world for light water reactor fuel. More information is provided in Appendix: Overview of main fuel rod performance code developments across the globe.

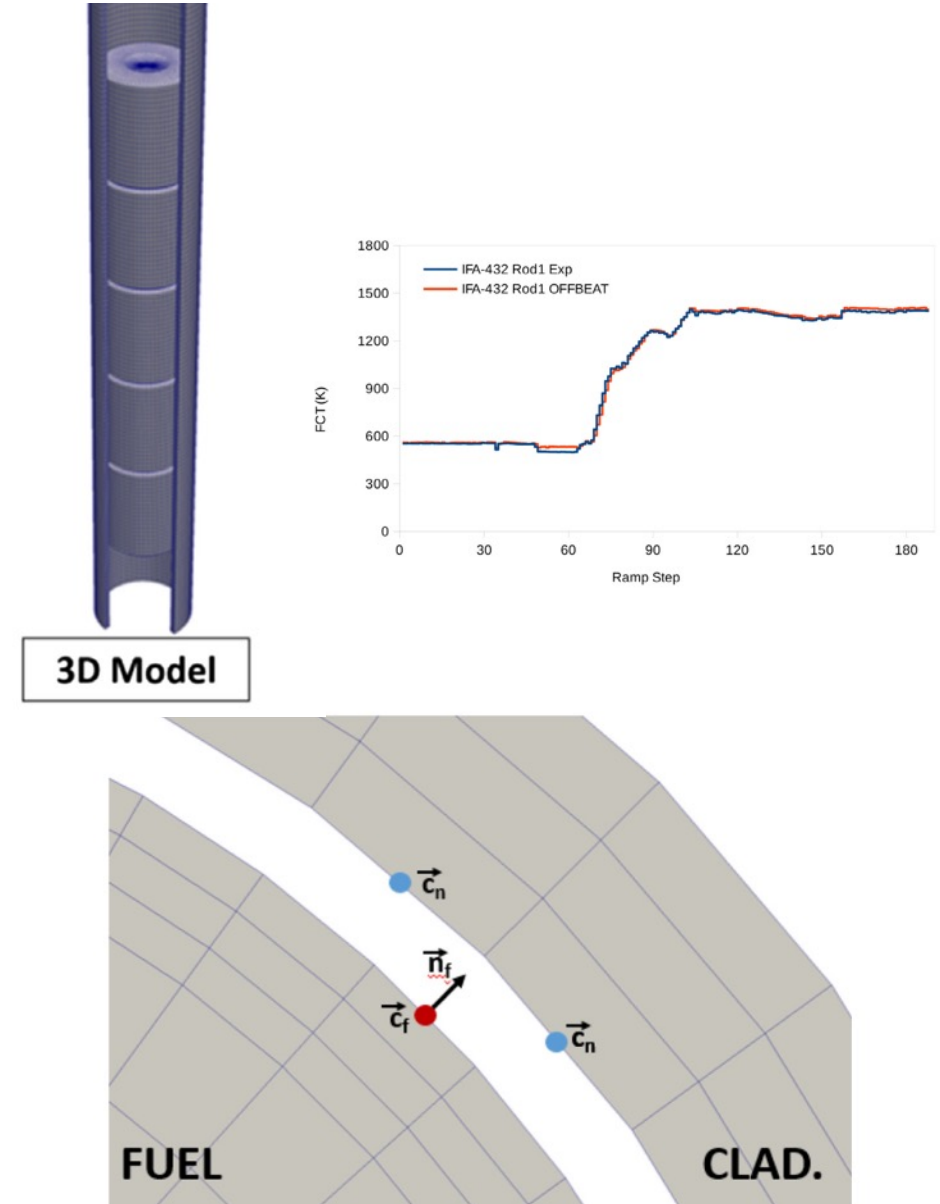
Country	Organization	Code name (precursor codes)
Argentina	CNEA	BACO, DIONISIO
Belgium	Belgonucleaire	COMETHE
	SCK-CEN	MACROS (ASFAD)
China	Xi'an Xiaotong University	FROBA
	CIAE	FTPAC
	NPIC	FUPAC
	CGNPC	JASMINE
Czech Republic	UJV	PIN-MICRO
France	CEA	ALCYONE (METEOR-TRANSURANUS) COPERNIC (TRANSURANUS), GALILEO (COPERNIC/RODEX/CARO)
	Framatome	CYRANO SCANAIR
	EdF	CARO
Germany	IRSIN	GALILEO (COPERNIC/RODEX/CARO)
	Siemens	TESPA-ROD (TESPA)
	Framatome	TRANSURANUS (URANUS)
	GRS	FUROM (PIN-MICRO)
Hungary	JRC	FAIR, PROFESS
India	MTA EK	FUDA
	BARC	EIMUS (FEMAXI-III)
Japan	PNC	FEMAXI, RANNS
	CRIEPI	IRON (FEMAXI-III)
	JAEA	TRUST
	SEPC	COSMOS, INFRA
	NFD	START, RAPTA
Korea	KAERI	RTOP
Russian Federation	VNIINM	SFPR (MFPR)
	TRINITI	STAV
	IBRAE	ENIGMA (MINIPAT, SLEUTH, HOTROD)
Sweden	Westinghouse	
	Sweden Electric	
United Kingdom	NNL, EDF Energy	
USA	USNRC	FRAPCON, FRAPTRAN (FRAP), FAST
	Siemens	RODEX
	EPRI	FALCON (FREY, ESCORE)
	INL	BISON
	Framatome	GALILEO (COPERNIC/RODEX/CARO)
	Westinghouse	PAD



<http://www.materials.cea.fr/en/PDF/PLEIADES-Platform.pdf>

# OFFBEAT – new tool

- The OpenFOAM Fuel BEhavior Analysis Tool (OFFBEAT) is a multi-dimensional fuel performance code developed in Switzerland
- The code can be used both for studying complex 2D or 3D local effects and for more traditional 1.5D base irradiation analyses
- OFFBEAT is based on the open-source C++ library OpenFOAM, thus the governing equations are discretized with modern finite volume techniques



## Summary

- Fuel performance codes are focused on predicting the center temperature of the pellet and the stress in the cladding
- All fuel performance codes
  - Numerically model the temperature in the fuel
  - Numerically model the stress in the cladding
  - And consider gap pressure, closure, and heat transfer in some way
- The primary US codes are
  - FRAPCON – Steady state 1.5D, uses finite difference
  - FRAPTRAN – Transient 1.5D, uses finite difference
  - FALCON – Steady or transient 2D, uses finite element
  - BISON – Steady or transient, 1D – 3D, uses finite element