

Cole Takasugi

190

Fuel Performance Midterm 2

- 1) true strain  $\epsilon$  accounts for shrinking of the section area and elongation on the further elongation
- 2) plastic deformation is  $\frac{e}{\delta}$  permanent where elastic deformation will undo and return to normal once forces are released  
- would have liked a bit more
- 3) Vacancies, self interstitials and impurity atoms are 0-D since they are at a single point. Precipitate clusters of impurities or large vacant voids can be considered 3D.

4) Melting temperature,  
thermal conductivity,  
and processes such as  
grain growth, gas release,  
or creep depend on  
stoichiometry.

5) The grain size impacts  
fission gas release, swelling,  
thermal conductivity and  
creep - this is largely due  
to the fact that diffusion  
often occurs faster along  
grain boundaries

~~Astheimer~~ - mechanical properties!

6) Strain hardening is  
the result of plastic  
deformation leading to  
a permanent strain  
which may allow higher  
yield strains when  
reloaded

- what causes hardening?
- dislocation pileup, repulsion  
etc.

- 7)
1. numerically model temperature  
in the fuel ✓
  2. numerically model stress  
in cladding ✓
  3. consider gap pressure,  
closure, heat transfer

3/3

- 8) Fuel densification occurs as porosity is reduced in the reactor due to ~~degradation~~ change in free energy from decreased surface area of pores. ✓  
Therefore the system is driven toward the lower free energy state

9)

~~✓~~ Irradiation can  
accelerate grain growth  
- this is more significant  
for small grains at low  
temperature

~~✓~~ Pores, precipitates, and  
solute atoms inhibit  
grain boundary growth  
by decreasing grain  
boundary mobility

14/14

10a)  $P = 20 \text{ MPa}$        $\bar{R} = 5.4 \text{ mm}$   
 $s = 0.8 \text{ mm}$       ✓

$\sigma_r = -\frac{1}{2}P = -10 \text{ MPa}$

$\sigma_\theta = \frac{PR}{s} = \frac{(20)(5.4)}{0.8} = 135 \text{ MPa}$       ~~13.5 MPa~~

$\sigma_z = \frac{PR}{2s} = \frac{(20)(5.4)}{1.6} = 67.5 \text{ MPa}$       ~~67.5 MPa~~

b)  $r = \bar{R} = 5.4$ ,  $R_o = 5.4 + 0.4 = 5.8$   
 $R_i = 5.4 - 0.4 = 5.0$

8/8  $R_o/r = 5.8/5.4 = 1.074$       ✓

$\sigma_r = -P \left( \frac{(R_o/r)^2 - 1}{(R_o/R_i)^2 - 1} \right) = -20 \left( \frac{(1.074)^2 - 1}{(1.116)^2 - 1} \right) = -8.88 \text{ MPa}$

$\sigma_\theta = P \left( \frac{(R_o/r)^2 + 1}{(R_o/R_i)^2 - 1} \right) = 20 \left( \frac{1.074^2 + 1}{1.116^2 - 1} \right) = 124.62 \text{ MPa}$

2/4  $\sigma_z = P \left( \frac{1}{(R_o/R_i)^2 - 1} \right) = 20 \left( \frac{1}{1.116^2 - 1} \right) = -57.9 \text{ MPa}$

c)  $\sigma_{\theta\theta}$  on the inner surface & ~~thickness~~ would be the same  
 $\sigma_c?$        $\sigma_z?$

$$11) \quad T_0 - T_s = \frac{4\pi R}{4\pi K} = \frac{12/12}{4\pi (0.1 \frac{\text{W}}{\text{cmK}})} = 150 \frac{\text{W}}{\text{cm}} = 198.94$$

$$\sigma^* = \frac{\alpha E (T_0 - T_s)}{4(1-\nu)} \quad \checkmark$$

$$= \frac{(8.2 \times 10^{-6}) (2.96 \times 10^5 \text{ MPa}) (198.94 \text{ K})}{4(1-0.3)} \quad \checkmark$$

$$= 168.96 \text{ MPa} \quad \checkmark$$

$$\sigma_{\theta\theta}^{(n=1)} = -\sigma^* (1-\nu) = 2\sigma^* = 337.9 \text{ MPa} \quad \checkmark$$

12)

$$T_o - T_s = \frac{LHR}{4\pi K}$$

13)  
T\_b

~~$$T_{gap} = T_{clad} + LHR_{fuel clad}$$~~

$$= 450 + (325)(0.02)$$

$$T_s = T_{gap} + \frac{LHR}{2\pi R_f h_{gap}}$$

$$= 450 + \frac{(325)(0.02)}{2\pi(0.5)(0.02)}$$

$$T_s = 501.73 \text{ K} \quad \checkmark$$

$$T_o = T_s + \frac{LHR}{4\pi K_f} = 501.73 + \frac{325}{4\pi(0.05)}$$

$$= 1018.98 \text{ K initially} \quad \checkmark$$

$$R_c = 0.5 + 0.02 = 0.52 \text{ cm}$$

$$R_f = 0.25 \text{ cm}$$

$$\overline{T_p} = \frac{(1018.98 + 501.73)}{2} = 760.355 \text{ K} \quad \checkmark$$

12 continued ✓

$$\Delta \delta_{\text{gap}} = R_c \alpha_c (\bar{T}_c - T_{\text{ref}}) - \bar{R}_f \alpha_f (\bar{T}_f - T_{\text{ref}})$$
$$= 0.52(4.5 \times 10^{-6})(450 - 300) - 0.25 \overset{R_f}{\cancel{19}} (19 \times 10^{-6}) (760,355 - 300)$$
$$= -0.001375 \text{ cm}$$

$$\delta'_{\text{gap}} = \frac{(0.501726 \text{ is new } R_f)}{0.018625 \text{ cm}}$$

$$T'_s = T_{c1} + \frac{\text{LHR}}{2\pi R_f h_{\text{gap}}} \checkmark$$
$$= 450 + \frac{(325)(0.018625)}{2\pi(0.501726)(0.04)}$$
$$= 498.0 \text{ K}$$

$$T'_o = T'_s + \frac{\text{LHR}}{4\pi k_f} = 498.0 + \frac{325}{4\pi(0.05)}$$

$$T'_o = 1015.25 \text{ K after}$$

- wrong  $R \rightarrow \Delta t_g$   
makes wrong  $t_{g'} + T'_o$  one expansion

13)

8/8

$$\frac{\sigma_{fr}}{\sigma^*} = 1 - 3\eta^2 \rightarrow 3\eta^2 = 1 + \frac{\sigma_{fr}}{\sigma^*}$$

$$\sigma^* = \frac{\alpha E(T_0 - T_s)}{4(1-\nu)} \quad \checkmark \quad T_0 - T_s = \frac{LHR}{4\pi K}$$

$$T_0 - T_s = \frac{200}{4\pi(0.05)} = 318.310$$

$$\begin{aligned} \sigma^* &= (10.5 \times 10^{-6} \text{ K})(210)(318.310) \\ &\quad \times 10^3 \text{ MPa} \\ &= 233.957 \text{ MPa} \quad \checkmark \end{aligned}$$

$$\begin{aligned} M &= \sqrt{\frac{1}{3} \left( 1 + \frac{120}{233.957} \right)} \\ &= \sqrt{0.504305} = 0.7101443 \end{aligned}$$

$$\begin{aligned} M &= \frac{r}{R_f} \rightarrow r = MR_f \\ &= (0.7101443)(0.55 \text{ cm}) \\ &= 0.3906 \text{ cm} \end{aligned}$$