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NE 533 Test 2

$$1. f_f = 0.56 \text{ cm} \quad LHR = 350 \frac{\text{W}}{\text{cm}}$$

$$\text{a) } T_{\max} = ? ; k_f = 0.05 \frac{\text{W}}{\text{cm}^2 \text{K}} ; E = 200 \text{ GPa} ; v = 0.35 ; \alpha = 10 \times 10^{-6} \text{ /K}$$

$$T_{\max} = T_{\infty} @ r = R_F \quad \checkmark$$

$$T_{\infty}(\gamma) = -\frac{\alpha E (T_0 - T_S)}{4(1-v)} (1 - 3\gamma^2) ; T_0 - T_S = \frac{LHR}{4\pi k} = \frac{350 \frac{\text{W}}{\text{cm}}}{4\pi (0.05 \frac{\text{W}}{\text{cm}^2 \text{K}})} = 557.04 \text{ K}$$

$$= -\frac{(10 \times 10^{-6} \text{ /K})(200 \times 10^9 \text{ MPa})(557.04 \text{ K})}{4(1 - 0.35)} (1 - 3(1)^2) = 856.985 \text{ MPa}$$

$$\text{b) } T_{\text{fracture}} = 150 \text{ MPa}, \text{ however cracks run to fuel}$$

$$\frac{4T_{\text{fracture}}(1-v)}{\alpha E (T_0 - T_S)} = 1 - 3\gamma^2 \Rightarrow \gamma = \sqrt{\frac{1 + (4T_{\text{fracture}}(1-v)) / (\alpha E (T_0 - T_S))}{3}}$$

$$\gamma = \sqrt{\frac{1 + (4(150 \text{ MPa})(1 - 0.35)) / ((10 \times 10^{-6} \text{ /K})(200 \times 10^9 \text{ MPa})(557.04 \text{ K}))}{3}}$$

$$f_f(1-\gamma) = \text{crack length}$$

$$= 0.67 ; \text{ so cracks extend } 0.181 \text{ cm into the pellet}$$

$$2. p = 55 \text{ MPa} \quad \bar{r} = \delta = 0.55 \text{ cm} \quad t = 0.05 \text{ cm}$$

$$\text{a) } \bar{T}_\theta = \frac{pR}{8} = \frac{(55 \text{ MPa})(0.55 \text{ cm})}{0.05 \text{ cm}} = 605 \text{ MPa}$$

$$\bar{T}_z = \frac{pR}{2E} = \frac{\bar{T}_\theta}{2} = 302.5 \text{ MPa}$$

$$\bar{T}_r = -\frac{1}{2}p = -275 \text{ MPa}$$

$$\text{b) } T_{rr} = \cancel{\frac{pR}{8} \left(\frac{R_o}{R_i} - \frac{R_i}{R_o} \right)} = -p \frac{(R_o/R_i)^2 - 1}{(R_o/R_i)^2 - 1} = -p = -55 \text{ MPa}$$

$$T_{\theta\theta} = p \frac{(R_o/R_i)^2 + 1}{(R_o/R_i)^2 - 1} = 55 \text{ MPa} \frac{(0.575/0.525)^2 + 1}{(0.575/0.525)^2 - 1} = 606.25 \text{ MPa}$$

$$T_{zz} = p \frac{(R_o/R_i)^2 - 1}{(R_o/R_i)^2 - 1} = 275.625 \text{ MPa}$$

$$3. \text{ Gap thickness change; } f_f = 0.52 \text{ cm} ; t_{gap} = 0.005 \text{ cm} ; T_{co} = 550 \text{ K} ; t_{cool} = 0.08 \text{ cm} ;$$

$$k_{fuel} = 0.04 \frac{\text{W}}{\text{cm}^2 \text{K}} ; h_{gap} = 0.003 \frac{\text{W}}{\text{cm}^2 \text{K}} ; h_{cool} = 0.15 \frac{\text{W}}{\text{cm}^2 \text{K}} ; LHR = 175 \frac{\text{W}}{\text{cm}} ; \alpha = 10 \times 10^{-6} \text{ /K}$$

$$f_f = 14 \times 10^{-6} \text{ /K} ; T_{\infty} = 300 \text{ K}$$

$$T_{co} = \frac{LHR}{2\pi k_{fuel}} + \frac{t_{cool} + t_{gap}}{2\pi (0.52 \text{ cm})} = \frac{175 \frac{\text{W}}{\text{cm}}}{2\pi (0.04 \frac{\text{W}}{\text{cm}^2 \text{K}})} + \frac{0.08 \text{ cm} + 0.005 \text{ cm}}{2\pi (0.52 \text{ cm})} = 578.57 \text{ K}$$

$$T_{fo} = \frac{LHR}{2\pi k_{fuel}} + \frac{t_{gap}}{h_{gap}} + T_{co} = \frac{175 \frac{\text{W}}{\text{cm}}}{2\pi (0.04 \frac{\text{W}}{\text{cm}^2 \text{K}})} + \frac{0.005 \text{ cm}}{0.003 \frac{\text{W}}{\text{cm}^2 \text{K}}} + 578.57 \text{ K} = 667.84 \text{ K}$$

$$T_0 = \frac{LHR}{4\pi k_{fuel}} + T_{fo} = \frac{175 \frac{\text{W}}{\text{cm}}}{4\pi (0.04 \frac{\text{W}}{\text{cm}^2 \text{K}})} + 667.84 \text{ K} = 1015.99 \text{ K}$$

$$\bar{T}_c = \frac{T_{co} + T_{fo}}{2} = \frac{550 \text{ K} + 578.57 \text{ K}}{2} = 564.285 \text{ K}$$

$$\bar{T}_f = \frac{T_{fo} + T_0}{2} = \frac{667.84 \text{ K} + 1015.99 \text{ K}}{2} = 841.915 \text{ K}$$

not \bar{R}_f , just R_f

$$R_f = \frac{R_f}{2} = \frac{0.52\text{cm}}{2} = 0.26\text{cm}$$

$$\bar{L}_c = R_f + t_{gap} + \frac{t_{aux}}{2} = 0.565\text{cm}$$

$$\Rightarrow \Delta t_{gap} = 0.565\text{cm}(10 \times 10^6 \text{N}) (544.285 - 300) - 0.26\text{cm}(14 \times 10^6 \text{N}) / 84(1.915 - 300)$$
$$= [-0.001823\text{cm}]$$

$$t'_g = 0.005 - 0.001823 = 0.003176\text{cm}$$

4. $\sigma_{00}, \sigma_{rr} = ?$. @ $R=R_i$; $\Delta T=50\text{K}$; $\alpha_c=15 \times 10^{-6}$; $E=100\text{GPa}$; $\nu=0.34$; $t_c=0.000\text{cm}$; $R_i=0.55\text{cm}$

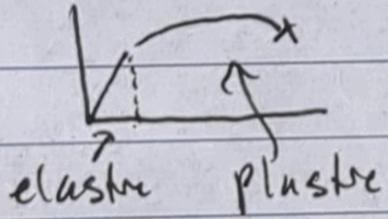
8/10 $\sigma_{00}(R_i) = \sigma_{rr}(R_i) = \frac{1}{2} \Delta T \frac{\alpha E}{1-\nu} \left(1 - 2 \frac{R_i}{8} \left(\frac{1770}{1770-1}\right)\right) = \frac{1}{2} \Delta T \frac{\alpha E}{1-\nu} = \frac{50\text{K}}{2} \frac{(15 \times 10^{-6})(100 \times 10^9 \text{Pa})}{1-0.34}$

$$= [56.818 \text{ MPa}]$$

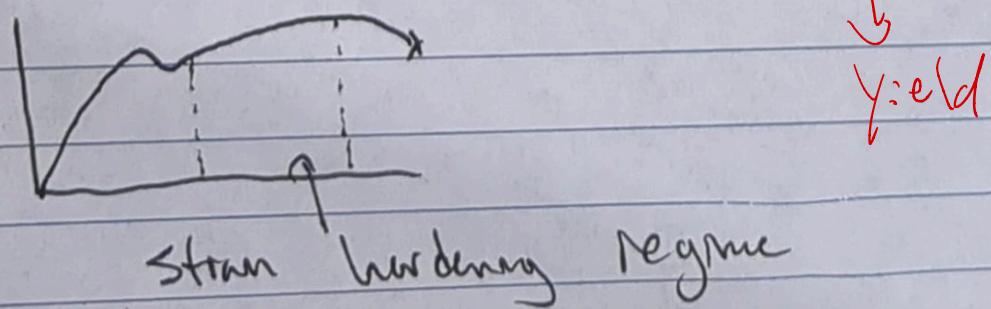
$$\sigma_0 = \sigma_x = \sigma_r ?$$

5. Elasticity is material deformation elongation that occurs when a force is applied that returns to its original length when the force is unloaded.

8/10 Plasticity does not return to its original length. Plastic deformation is the result of dislocation motion in the material. It induces the material ~~over time~~ (work hardening). Most materials elastically deform for small loads and transition into plastic deformation as the load grows.



6. Strain hardening is an increase in the yield stress of a material as it is elongated (or strained). It is the result of dislocation motion in the material. As dislocations pile up on defects the material becomes harder to strain.



7. All fuel performance codes must be able to predict fuel temperature profile and volume change, cladding temperature and stress profile, and gap pressure, heat transportation, and cladding-fuel mechanical interaction. ~~BISON~~ and FRAPCON are currently being used.
8. A vacancy is a point defect in a crystal where one atom is missing in the pattern. A void is an example of a 3D defect in a crystalline structure where some volume is missing atoms from the crystal/poly crystal.
9. When sintering, powder is heated and/or pressurized into a solid without melting the material. The powder forms the initial grains in the sintering process. Subsequent heat treatments may change grain size.
→ different orientations
10. Microstructure-based fuel performance modeling combines calculated local states with empirical constants to characterize material performance. Using this modeling method allows for codes to accurately predict material behaviors outside/beyond validated test data. This enables less costly reactor performance modeling, and enables novel, untested fuel concepts to be explored before pursuing test data. Microstructure-based fuel performance modeling takes grain boundaries, intergranular porosity, vacancies, precipitates, and more into account.
= most of the way there

11. Macrostructure is the patterns of arrangement of atoms at the $\times 25$ magnification level ($\sim 1\text{ }\mu\text{m}$ to $\sim 100\text{ }\mu\text{m}$). Microstructural characteristics such as grains, defects, patterns like the ^{8/8} High Burnup Structure, heavily influence engineering-level materials performance. One example of a processing technique that affects microstructure is stress relief annealing.

In stress relief annealing a material is heated up below its melting point to allow dislocations and defects to diffuse in a material and remove residual stress that may exist from previous ~~heat~~ plastic material deformation.

12. High Burnup Structure (HBS) is a microstructure that forms on the edge of a fuel pellet where localised power peaking drives higher ^{local} depletion over core life.

^{8/8} This structure has reduced grain size from $\sim 10\text{ }\mu\text{m} \rightarrow 100\text{--}200\text{ }\mu\text{m}$ and creates a 20% porosity throughout the local material. This structure increases heat transmission at the ~~center~~ pellet because of the smaller grain size, despite the increased porosity. This structure also retains fission gasses well because the voids do not percolate well. The local increased burnup is due to fuel self-shielding and lower temperatures which help capture ~~absorbs~~ neutrons in the $\text{U}^{238} \rightarrow \text{Pu}^{239} \rightarrow$ more fissions.

- $\uparrow K_{th}$, but not because smaller grain size

N6535 Test 2 Cheat Sheet
 $F = kx$; $E = \frac{1}{2}kx^2$; $\mathbf{u}(r, t)$: displacements
 Stress, strain, elastic, plastic
 Plasticity: Slip: Twisting
 $\tau_{ij} = F_j / A_i$ $P_A = \frac{N}{m^2}$
 $\epsilon = \frac{\Delta L}{L} = \frac{L-L}{L}$ $i \epsilon_{ij} = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$
 $\begin{bmatrix} \epsilon_{11} & \epsilon_{12} & \epsilon_{13} \\ \epsilon_{21} & \epsilon_{22} & \epsilon_{23} \\ \epsilon_{31} & \epsilon_{32} & \epsilon_{33} \end{bmatrix} = \begin{bmatrix} \frac{\partial u_1}{\partial x_1} & \frac{1}{2} \left(\frac{\partial u_1}{\partial x_2} + \frac{\partial u_2}{\partial x_1} \right) & \frac{1}{2} \left(\frac{\partial u_1}{\partial x_3} + \frac{\partial u_3}{\partial x_1} \right) \\ \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix}$

$\sigma = F(\epsilon)$; $\sigma = C(\epsilon)$; large ϵ : $\epsilon = \epsilon_e + \epsilon_p$, $\sigma = \sigma_e + \sigma_p$
 $\epsilon_{el} = \frac{1}{2} \epsilon_e - \sigma$
 stress σ Engineering F/A $\epsilon_{el} = \frac{1}{E} \frac{\partial L}{L} = \ln \left(\frac{L}{L_0} \right)$
 strain ϵ $\frac{1-\nu}{E}$
 Young's modulus $\sigma = E\epsilon$; $\nu = -\frac{\partial \epsilon_{max}}{\partial \epsilon_{APM}} = -\frac{\partial \epsilon_x}{\partial \epsilon_x} \approx \frac{\Delta L}{DL}$
 Shear modulus: $G = \frac{E}{2(1+\nu)}$

Hooke's law for isotropic: $\begin{bmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ 2\epsilon_{23} \\ 1\epsilon_{13} \\ 1\epsilon_{21} \end{bmatrix} = \begin{bmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ T_{23} \\ T_{13} \\ T_{12} \end{bmatrix} = \frac{1}{E} \begin{bmatrix} 1-\nu & -\nu & 0 & 0 & 0 & 0 \\ -\nu & 1-\nu & 0 & 0 & 0 & 0 \\ 0 & 0 & 1-\nu & 0 & 0 & 0 \\ 0 & 0 & 0 & 2+2\nu & 0 & 0 \\ 0 & 0 & 0 & 0 & 2+2\nu & 0 \\ 0 & 0 & 0 & 0 & 0 & 2+2\nu \end{bmatrix} \begin{bmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ 2\epsilon_{23} \\ 1\epsilon_{13} \\ 1\epsilon_{21} \end{bmatrix}$

Von Mises: $\sigma_v^2 = \frac{1}{2} \left[(\sigma_{11}-\sigma_{22})^2 + (\sigma_{22}-\sigma_{33})^2 + (\sigma_{33}-\sigma_{11})^2 + 6(\sigma_{23}^2 + \sigma_{31}^2 + \sigma_{12}^2) \right]$
 $\sigma = \sigma_y + k(\epsilon_0 - \epsilon_p)^n$ $\sigma_y = L(\epsilon_y)^n$ $n=0.5$ some steels
 $0.5 \leq n \leq 1$ k/A $\ln(L/L_0)$
 Dislocation motion: Edge and screw type; Edge: Screw:
 Dislocation \Rightarrow plastic deformation \Rightarrow dislocation pileup \Rightarrow hardening.
 $\therefore \epsilon_{pl} = \frac{b_f - b_0}{L_f - L_0} + \omega \cdot t$; η (dislocation density) $= \frac{A_{pl}}{A_f - A_0}$
 $\eta = \frac{32\pi^2 r^2}{L^2} = 8\pi^2 r + g_f$ negligible
 Simple shear: $\sigma_{xy} = \frac{\partial \sigma_{xx}}{\partial y} = \frac{\partial \sigma_{yy}}{\partial x} = \frac{\partial \sigma_{zz}}{\partial z} = 0$
 Axisymmetric: $\frac{\partial \sigma_{rr}}{\partial r} + \frac{\sigma_{rr} - \sigma_{\theta\theta}}{r} + \frac{\partial \sigma_{\theta\theta}}{\partial z} = 0$; $i \frac{1}{r} \frac{\partial (r \sigma_{rz})}{\partial r} + \frac{\partial \sigma_{rz}}{\partial z} = 0$
 Thin walls: $F_{shear} = 2\bar{\sigma}_t b$; $\bar{\sigma}_t = \frac{P_L}{8}$; $\bar{\sigma}_z = \frac{P_R}{28}$; $\bar{\sigma}_{rz} = -\frac{1}{2} P$
 Thick wall: $\sigma_{rr} = \frac{1}{2} (\sigma_{rr,r} - \nu(\sigma_{\theta\theta,r} + \sigma_{zz,r}))$; $\sigma_{\theta\theta,r} = \frac{1}{2} (\sigma_{\theta\theta,r} - \nu(\sigma_{rr,r} + \sigma_{zz,r}))$
 $\sigma_{zz,r} = \frac{1}{2} (\sigma_{zz,r} - \nu(\sigma_{rr,r} + \sigma_{\theta\theta,r}))$; $\sigma_{rz,r} = \frac{1}{2} \sigma_{rz}$
 $\frac{\partial \sigma_{rz,r}}{\partial r} = E \sigma_{rz,r} - \sigma_{rr,r} - \nu(\sigma_{rr,r} + \nu(\sigma_{\theta\theta,r} + \sigma_{zz,r})) = (1-\nu^2) \sigma_{rz,r} + (1+\nu) \sigma_{rr,r}$
 $E(\sigma_{rr,r} - \sigma_{\theta\theta,r}) = (1+\nu)(\sigma_{rr,r} - \sigma_{\theta\theta,r})$
 $r \sigma_{rr,r} + 3 \sigma_{\theta\theta,r} = 0$; $\frac{\partial}{\partial r} (r^2 \frac{\partial \sigma_{rr,r}}{\partial r}) = 0$
 $\sigma_{rr,r} = -P \frac{(R_0/r)^2 - 1}{(R_0/r_0)^2 - 1}$; $\sigma_{\theta\theta,r} = P \frac{(R_0/r)^2 - 1}{(R_0/r_0)^2 - 1}$; $\sigma_{zz,r} = P \frac{2\nu}{(R_0/r)^2 - 1}$
 $\epsilon_{rr} = (T - T_0) \alpha I$; $\sigma = C(I - \epsilon_{rr})$; $\sigma = C(I - \epsilon_{rr})$; $\sigma = C(I - \epsilon_{rr})$
 $\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 \frac{\partial \sigma_{rr,r}}{\partial r}) = - \left(\frac{\partial \sigma_{rr,r}}{\partial r} \right) \frac{1}{r} \frac{\partial \sigma_{rr,r}}{\partial r} \Rightarrow$
 $\sigma_{rr,r} = \frac{1}{2} \Delta T \frac{\alpha E}{1-\nu} \left(\frac{T}{T_0} - 1 \right) \left(1 - \frac{R_0}{R_1} \left(\frac{T}{T_0} - 1 \right) \right)$; $i \delta = \text{thickness}$
 $\sigma_{\theta\theta,r} = \sigma_{zz,r} = \frac{1}{2} \Delta T \frac{\alpha E}{1-\nu} \left(1 - 2 \frac{R_0}{R_1} \left(\frac{T}{T_0} - 1 \right) \right)$

Thermal stress in fuel pellet: $\sigma_{rr} = -\sigma_y * (1-\nu^2)$; $\sigma_{\theta\theta} = -\sigma_y * (1-3\nu^2)$
 $\sigma_{zz} = -2\sigma_y * (1-2\nu^2)$; $i \sigma_y = \frac{\alpha E (T_0 - T_f)}{4(1-\nu)}$; $\nu = \frac{\sigma}{E}$; i fuel crack ≈ 0.65
 capsule: $\Delta \sigma_{pp} = \sigma_{pp} - \sigma_{pp0}$; $\sigma_{pp} = D\dot{T}_c - D\dot{T}_{pf}$; $i \frac{\Delta \sigma}{R_c} = \sigma_{pp} (\bar{T}_f - T_{fuel})$
 $\Delta \sigma_{pp} = R_c \alpha_c (\bar{T}_c - T_{fuel}) - R_f \alpha_f (\bar{T}_f - T_{fuel})$
 $\epsilon = \begin{bmatrix} u_{rr,r} \\ 0 \\ u_r/r \end{bmatrix} \begin{bmatrix} \sigma_{rr,r} \\ \sigma_{\theta\theta,r} \\ \sigma_{zz,r} \end{bmatrix} = \frac{E}{(1-\nu)(1-2\nu)} \begin{bmatrix} 1-\nu & \nu & 0 \\ 0 & 1-\nu & 0 \\ 0 & 0 & 1-\nu \end{bmatrix} \begin{bmatrix} u_{rr,r} \\ 0 \\ u_r/r \end{bmatrix}$
 $\frac{\partial \sigma}{\partial t} = -\alpha_c (k \nabla T) + Q$; $i \sigma = C(I - \epsilon - (T - T_{fuel})I)$; $i \alpha = \alpha_c \sigma / (E(1-\nu))$
 FN: heat conduction + Fuhr's diffusion can solve thermomechanics
 (use parabolic goals are centered temp and cladding stress)
 (use most predict: Fuel: temp + vol change; Cladding: temp + stress profile; Gas: pressure)

Plastic burnup effects
 Steady state + transient codes
 Fragmat: steady, multiple 1D slices (1.50); NREL baseline code; Fission products
 iterates fission heat temp + fuel and cladding deformation; iterates to gas release
 Fractran: Same as Fragmat, but with transient capabilities
 faken: Transient, 2D axisymmetric w/ structural pellets; ANATECH for EPRI 2003
 FEM fuel cladding; Axisymmetric in RT or R8 space

BISON: transverse roll 3D and less; INL with ANATECH 2007; uses FEM

OFFBEAT: open source; MITRE; late life; Fuel Failure

Fuel Fab	Early life	Mid life	Late life	Fuel Failure
Initial JES	Fuel defect dilution	Fission product	Fission product	Fission product
h=2mm	Thermal expansion	clustering	bubble propagation	clustering
h=2mm	Fission gas generation	to CO ₂ + UO ₂	FG release	clustering
h=2mm	Fission gas generation	bubbles	clustering	clustering
h=2mm	Fission gas generation	bubbles	clustering	clustering
h=2mm	Fission gas generation	bubbles	clustering	clustering

Crystalline defects:
 Point defects (00): Vacancies, self interstitial atoms, interstitial impurity atoms
 Substitutional impurity atoms

$C_v = \frac{N_v}{N_s} = C_{eq} \left(\frac{S_v}{k} \right) \exp \left(\frac{-E_v}{kT} \right)$ equilibrium point defect concentration

Radiation damage from ionizing radiation, plasmas, cascade

Dislocations (1D): Controls plastic deformation

Grain boundaries (2D): Most are polycrystalline; naturally form during casting; casting has more grain size: $P(G) = (Z_e)^3 \cdot \frac{B_n}{(Z-n)^2} \exp \left(\frac{-2\phi}{Z-n} \right)$

3D defects: voids + precipitates; point defect coalescence

Microstructure: X25 magnetite

Materials processing:
 Casting: liquid material cool in mold; Sintering: powder heat/press into sintered
 Heat treatment: Annealing, quenching; working: squeezing, bending, shearing

Radiation damage:
 Frankel defects (interstitial-vacancy pair) from secondary collision cascade
 In UO₂, Schottky traps formed w/ 2 atoms for every cation
 Long defects are combination of screw and edge defects
 Stop along $\frac{1}{2}100$ $\langle 110 \rangle$ without energy
 Slight excess of vacancies from preferential absorption of interstitials
 Build up at GB + form voids for FG

Chemistry changes $\nu 3\%$ at fuel; \uparrow defects \downarrow K; \uparrow precipitates \uparrow K

Porosity \downarrow K; \uparrow melt oxides \downarrow K

$K = \frac{100}{7.5408 + 17.029t + 3.6142t^2} + \frac{6400}{t^{3/2}} \exp \left(\frac{-16.35}{t} \right)$; $t = \frac{T}{1000}$

BISON uses NPIL model + damage cause O, U, Y, Si, Mn; Strength \downarrow \downarrow hardness \downarrow Young's modulus

High Burnup Structure: 10% pores; 200nm edge; \downarrow 23% grain size; high porosity
 grain subdivide 10nm \rightarrow 100-200nm; 20% porous; polygranular removes defects; \downarrow K from grain size despite porosity

Mechanical mobility: grain boundaries; microstructural porosity; precipitated FP
 $K = \frac{k_{GB} k_{MP} k_{PP}}{A + B\Gamma + C\Gamma^2 + C_{GB} + C_{PP} + C_{GB}\Gamma + C_{PP}\Gamma}$; both anisotropy; vacancies + microstructural

1) $T @ r = 0.52\text{cm}$; $r_c = 0.5\text{mm}$; $r_o = 0.55\text{mm}$; $P = 15\text{MPa}$; $\sigma_0 = \frac{(0.55/0.52)^2 - 1}{(0.55/0.52)^2 - 1}$; $\sigma_r = 15.3\text{MPa}$; $\sigma_z = \frac{(0.55/0.52)^2 - 1}{(0.55/0.52)^2 - 1} (-15) = -8.5\text{MPa}$

$\sigma_z = 15 / [(0.55/0.52)^2 - 1] = 12.6\text{MPa}$; i then $r_c = \frac{r_{ext}}{2} = 0.525\text{cm}$

2) T_{fuel} in pellet; $i \Delta T = T_o - T_s = 425\text{K}$; $\alpha_F = 12 \times 10^{-6} \text{K}^{-1}$; $R_p = 20.3\text{mm}$; $E = 1800\text{GPa}$; $\nu = 0.25$
 $\sigma_{pp} = T_o @ r = R_p$; $\sigma_{pp} = \frac{(12 \times 10^{-6})(1800 \times 10^9)(425)}{4(1-0.25)} = 348.8\text{MPa}$

$\sigma_a = -318.8(1-3(1^2)) = 637.5\text{MPa}$ $i r = R_p$

3) Cladding tube stress $@ r = 0.62\text{cm}$; $R_c = 0.6\text{cm}$; $t_c = 0.1\text{cm}$; $E = 250\text{GPa}$
 $\nu = 0.3$; $\alpha_c = 15 \times 10^{-6} \text{K}^{-1}$; $T_{cl} = 400\text{K}$; $T_{cl,o} = 580\text{K}$
 $\sigma_{cl} = \frac{20}{2} \frac{(400-580)(250 \times 10^9 \text{ MPa})}{(0.62-0.6)^2} (0.62-0.6) (1-0.6(0.62-0.6)^2) = 14.43 \text{ MPa}$

$\sigma_{cl} = \frac{20}{2} \frac{(15 \times 10^4)(250 \times 10^9 \text{ MPa})}{(1-0.3)} (1- \frac{2(0.6)}{0.1} (0.62-0.6)^2) = 32.1 \text{ MPa}$

4) Gap thickness change; $\nu_F = 12 \times 10^{-6} \text{K}^{-1}$; $r_c = 1.5 \times 10^{-6} \text{m}$; $R_c = 925\text{K}$
 $\Delta t_g = 0.58 (16 \times 10^{-6})(250) - 0.3 (12 \times 10^{-6}) (425) = -0.033\text{m}$
 $t_g = 0.03 - 0.0016 = 0.0284\text{cm}$

5) Stress $@ r = 0.45$; $E = 200\text{GPa}$; $\nu = 0.3$; $\alpha_c(r) = 0.5r^2 - 0.2r$
 $\epsilon = \begin{bmatrix} u_{rr,r} \\ 0 \\ u_r/r \end{bmatrix} = \begin{bmatrix} r - 0.2 \\ 0 \\ 0.5r^2 - 0.2 \end{bmatrix} = \begin{bmatrix} 0.25 \\ 0 \\ 0.025 \end{bmatrix}$
 $\sigma_{cl} = \frac{20}{2} \frac{(0.25)(250 \times 10^9 \text{ MPa})}{(0.25-0.2)^2} (0.25-0.2) = 26.9\text{ MPa}$; $\epsilon_{12} = \frac{E}{(1+\nu)(1-2\nu)}$; $\nu = 0.150\text{Pa}$

$\sigma_{pp} = 200 (0.25) + 115 (0.025) = 70\text{ GPa}$; $\sigma_{pp} = 115 (0.25) + 92 (0.025) = 356\text{ Pa}$

$T_o - T_s = \frac{\Delta T}{4H} = \frac{400}{4 \times 10^9} = 100\text{ K}$; $i T_{fuel} - T_{cl} = \frac{400}{200} = 200\text{ K}$; $i T_{cl} - T_{cl,o} = \frac{400}{150} = 267\text{ K}$