

Question (1) $T = 625K$, $t = 400 \text{ days}$, initial thickness = $500 \mu\text{m}$

a) First Calculate when transition occurs: $t^* ??$

$$t^*_{\text{(days)}} = 6.62 \times 10^{-7} \exp\left[\frac{11949}{T}\right] = 133 \text{ days}$$

\nwarrow
 $625K$

Second oxide thickness at transition (δ^*): $\delta^*_{\text{(\mu m)}} = 5.1 \exp\left[\frac{-550}{625}\right] = 2.115 \mu\text{m}$

Then oxide thickness at $t = 400$

$$\delta(400 \text{ days}) = \delta^* + K_L(t - t^*)$$

$$\therefore \delta(400 \text{ days}) = 2.115 \mu\text{m} + 0.0154 \times [400 - 133]$$

$$= 2.115 \mu\text{m} + 4.112 \mu\text{m}$$

$$= 6.23 \mu\text{m}$$

$K_L = 7.48 \times 10^{-6} \exp\left[\frac{-12500}{T}\right]$
 $= 0.0154 \mu\text{m/day}$

b) If $P_H = 0.18$, $PBR = 1.56$, $\rho_{Zr} = 6.59 \text{ g/cm}^3$, $\rho_{ZrO_2} = 5.68 \text{ g/cm}^3$

$$C_H = \frac{2 P_H \rho_{ZrO_2} f_{O \text{ in } ZrO_2} \frac{M_H}{M_O}}{\left[t_c - \frac{\delta}{PBR}\right] \rho_{\text{metal}}}$$

$$= \frac{2 \times 0.18 \times 5.68 \times 0.26 \times \frac{1}{16}}{\left[500 - \frac{5.69}{1.56}\right] \times 6.5}$$

$$= 5.86 \times 10^{-5} = 58.6 \text{ ppm}$$

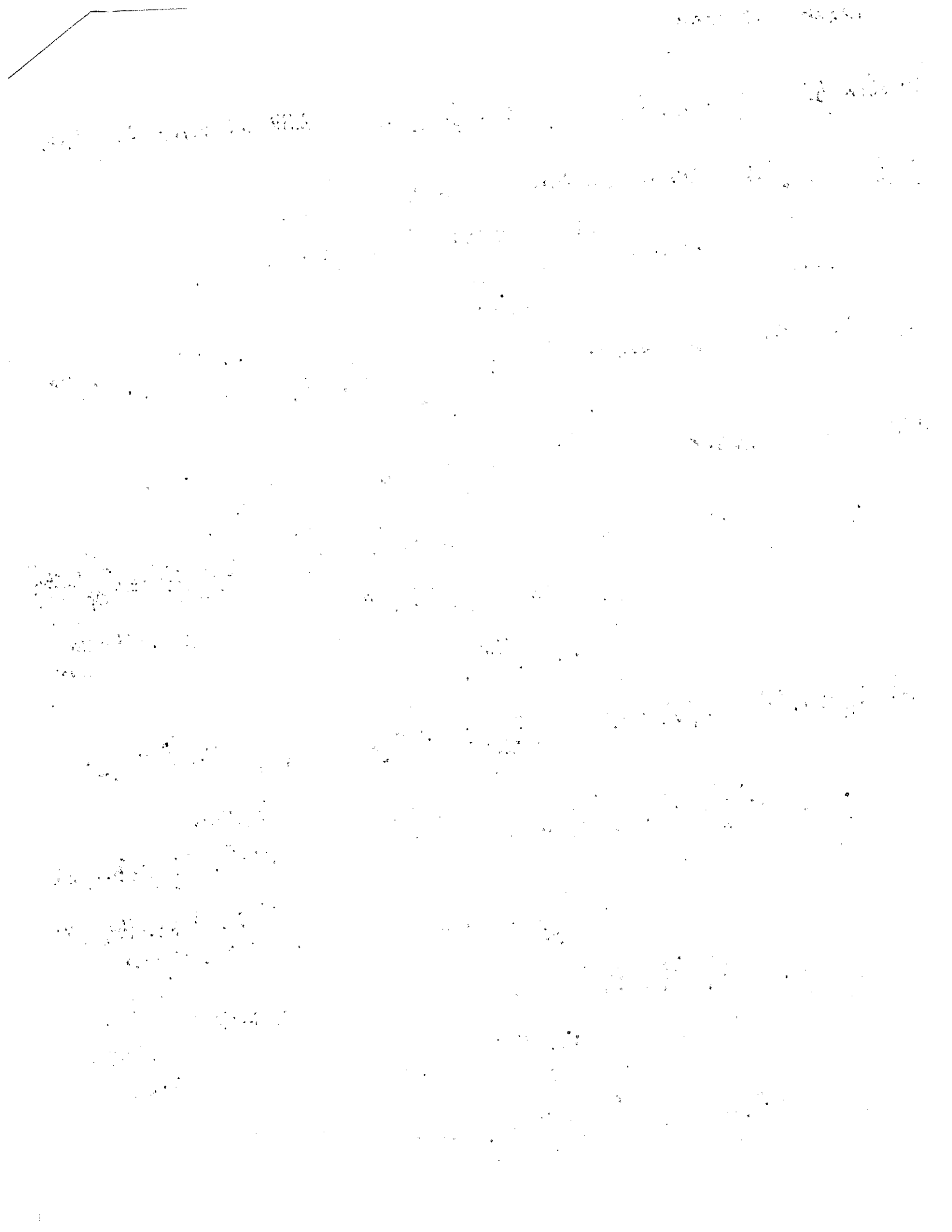
$$\delta(1 \text{ year}) = \delta^* + K_L(365 - 133)$$

$$= 2.115 + 0.0154 \times 232$$

$$= 5.69 \mu\text{m}$$

$$f_{O \text{ in } ZrO_2} = \frac{16 \times 2}{16 \times 2 + 91}$$

$$= 0.26$$



Question (2) $\alpha_{th} = 11 \times 10^{-6}$, $\rho = 3.5 \times 10^{13} \text{ f/cm}^3$, $T = 1200$
 $T_{ref} = 300 \text{ K}$, $\Delta P_0 = 0.01$, $B_D = 5 \text{ MW/150}$
 $\rho(UO_2) = 10.979 \text{ g/cm}^3$, $t = 85 \text{ days}$

$$\epsilon_{tot} = \epsilon_{th} + \epsilon_D + \epsilon_{SFP} + \epsilon_{GFP}$$

$$\Rightarrow \epsilon_{th} = \alpha_{th} \Delta T = 11 \times 10^{-6} [1200 - 300] = \boxed{0.01}$$

$$\Rightarrow \epsilon_D = \Delta P_0 \left[\exp\left(\frac{\beta \rho_0}{C_D \rho_D}\right) - 1 \right]$$

$$= 0.01 \left[\exp\left(\frac{0.01 \times 4.605}{1 \times 10.979}\right) - 1 \right]$$

$$= \boxed{-0.01}$$

$$\beta = \frac{\rho t}{N_U} = \frac{3.5 \times 10^{13} \times 85 \text{ days}}{\frac{238 \times 24 \times 60 \times 60}{10.979 \times 6.02 \times 10^{23}}}$$

$$= \frac{3.5 \times 10^{13} \times 85 \times 24 \times 60 \times 60}{10.979 \times 6.02 \times 10^{23}}$$

$$= \frac{270}{238} = 0.0105 \text{ FI MA}$$

$$C_D = 1 \text{ [for } T > T_{ref}]$$

$$\rho_0 = \frac{5}{950} = 0.0053 \text{ FI MA}$$

$$\Rightarrow \epsilon_{SFP} = 5.577 \times 10^{-2} \rho \beta$$

$$= 5.577 \times 10^{-2} \times 10.979 \times 0.0105$$

$$= \boxed{0.0064}$$

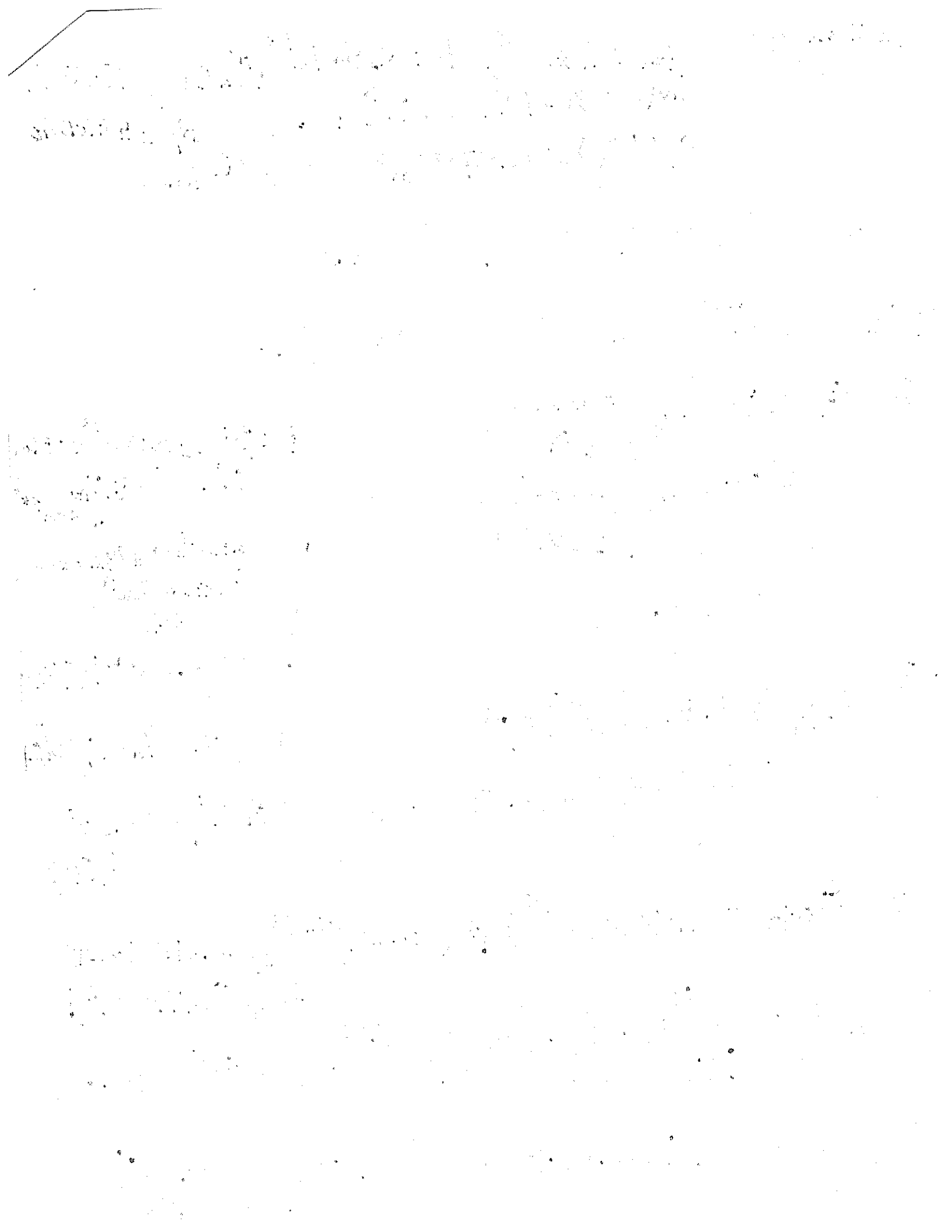
$$\Rightarrow \epsilon_{GFP} = 1.96 \times 10^{-28} \rho \beta (2800 - T)^{11.73} \exp[-0.0162(2800 - T)] \times \exp[-17.8 \rho \beta]$$

$$\epsilon_{GFP} = 1.96 \times 10^{-28} \times 10.979 \times 0.0105 \times (1600)^{11.73} \exp[-25.92] \exp[-2.05]$$

$$= \boxed{6.177 \times 10^{-4}}$$

$$\Rightarrow \epsilon_{tot} = 0.01 - 0.01 + 0.0064 + 6.177 \times 10^{-4} = 0.007$$

$$= \boxed{0.7\%}$$



question (3) $\sigma_m = 200 \text{ MPa}$, $T = 600 \text{ K}$, $\text{LHR} = 150 \text{ W/o}$
 $t = 1.5 \text{ y}$

$$\dot{\epsilon}_{\text{tot}} = \dot{\epsilon}_{\text{ss}} + \dot{\epsilon}_{\text{irr}}$$

$$\Rightarrow \dot{\epsilon}_{\text{ss}} = A_0 \left[\frac{\sigma_m}{G} \right]^n e^{-Q/RT}$$

$$= 3.14 \times 10^{24} \frac{1}{s} * \left[\frac{200 \times 10^6}{4.2519 \times 10^{10} - 2.2185 \times 10^7 * 600} \right]^5 e^{-\frac{2.7 \times 10^5}{8.314 + 600}}$$

$$= 3.14 \times 10^{24} \text{ s}^{-1} \left[\frac{200 \text{ MPa}}{29208 \text{ MPa}} \right]^5 * e^{-54.1}$$

$$= \boxed{1.51 \times 10^{-10} \text{ s}^{-1}}$$

$$\Rightarrow \dot{\epsilon}_{\text{irr}} = C_0 \Phi^{c_1} \sigma_m^{c_2} = 3 \times 10^{-24} * [4.5 \times 10^{13}]^{0.85} [200]^1$$

$C_1 = 0.85, C_2 = 1$
 C_0 is of the order 3×10^{-24}

$$= 2.42 \times 10^{-10} \text{ s}^{-1}$$

$$\therefore \dot{\epsilon}_{\text{tot}} = \dot{\epsilon}_{\text{ss}} + \dot{\epsilon}_{\text{irr}} = 3.93 \times 10^{-10} \text{ s}^{-1}$$

$$\Phi = 3 \times 10^{11} \text{ LHR}$$

$$= 3 \times 10^{11} * 150$$

$$= 4.5 \times 10^{13} \frac{\text{LHR}}{\text{y}}$$

$$\epsilon_{\text{tot}} \Big|_{t=1.5 \text{ y}} = 3.93 \times 10^{-10} * 365 * 24 * 60 * 60 * 1.5$$

$$= 0.0186 = \boxed{1.86\%}$$



Question (4) Types of Fission products in fuel:

- (1) Soluble oxides (Y, La) (dissolved in carbon suboxide)
- (2) Insoluble oxides (Zr, Ba, Sr)
- (3) metallic precipitates (Mo, Pd, Te)
- (4) Volatiles \rightarrow (Cs, Br, I) gas at high T , solid at low T
- (5) Noble gases (Xe, Kr)

Question (6) Three benefits of Zr cladding

- (1) Good thermal conductivity
 - (2) low neutron absorption cross section
 - (3) Corrosion resistant in water at $T = 300^\circ\text{C}$
- * Also affordable and abundant

Question (7) Metallic fuel undergoes constituent distribution

because : Zr diffuse up the temperature gradient
* Zr has different solubility in each phase of

Question (5) Microstructure-based fuel performance modeling (Mechanistic)

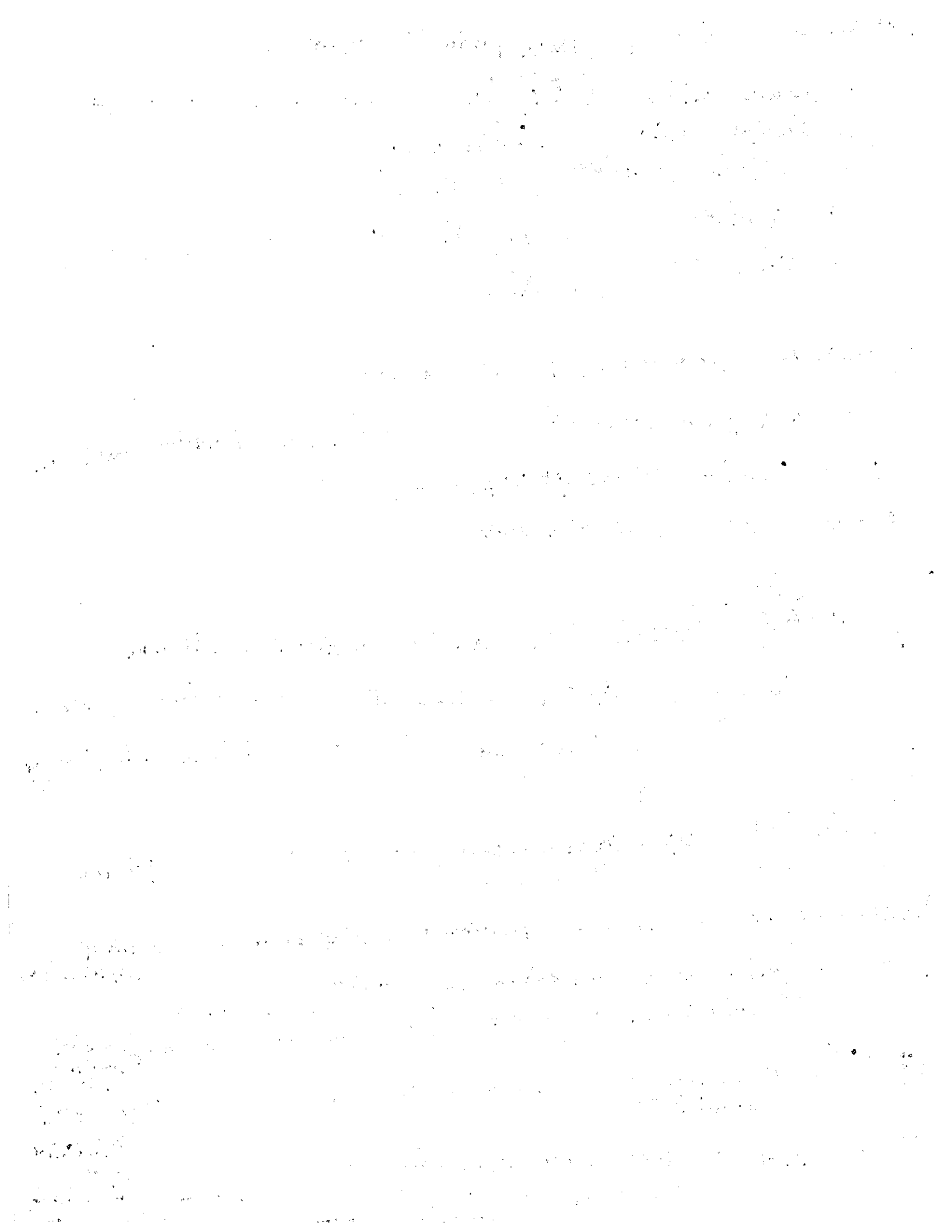
Instead of models correlating performance to temperature and Burnup (empirically)

\Rightarrow Mechanistic models are based on understanding the physics of microstructure evolution through multiscale modeling

\Rightarrow These mechanistic models have much more predictive capabilities

\Rightarrow For example: ~~Model~~ Thermal conductivity model as function of [Temperature, point defect conc., intergranular bubble density, precipitates, ...]

Atomistic modeling (DFT, MD)
+ phase field
+ Engineering scale



Question (8)

* MOX fuel : fuel pins have less diameter than LWR fuel

∴ Higher Power density & Higher Heat Flux

* MOX fuel ~~are~~ used in fast reactors which operate at high neutron flux

∴ Higher radiation damage than LWR fuels

[~100 dpa at high Burnup]

* MOX fuel is designed to operate at high LHR ~ 400-500 W/cm
(twice LWR fuels)

* stainless steel cladding is used with MOX fuel [instead of Zircaloy in LWR]

Question (9) Conditions for SCC :

① Corrosive environment

② Susceptible material

③ Sufficient stress

④ Sufficient time

In PCI

① Corrosive env : Aggressive fission products
(Cs, I) attack

② Material : Zircaloy is prone to PCI failure

③ Stress : internal stress from fuel swelling
& thermal expansion

④

Question (10)

In HBS \Rightarrow Grain size decrease to 150-200 nm
& micron-sized bubbles form with multiple
grains intersecting each bubble

\Rightarrow Potential to occur during (LOCA) temperature transients

Pulverization criterion was developed in BISON
informed by phase field modeling

Question (11)

RIA

LOCA

* Departure from criticality

* Reduced or lost coolant flow

* Nuclear reactors are designed with ~~the~~ negative reactivity feedback \Rightarrow when power increases \hookrightarrow reactivity will drop to decrease power

* when coolant pressure drops \hookrightarrow Emergency shutdown system will SCRAM the reactor then, Emergency Core Cooling System will remove the heat

* very fast change (0.1s in worst case scenario)

* Relatively slower

example ejection of control rod due to mechanical failure of control rod drive (PWR)

(OR) Coolant pressure ejecting a control rod assembly out of core due to mechanical failure of control rod housing

Question (12)

Pathways to ATF

(1) providing additional coping time required for the water to boil away

(2) providing more time required for the fuel to melt.

~~(3) providing more time required for the fuel to break~~

One option targeting this is : improved fuel properties

by : \Rightarrow using dopants with UO_2 as [Cr, SiC]

\Rightarrow Alternate Fuels $\Rightarrow U_3Si_2$

Question (13)

Limiting Phenomena

- ① Cladding wear
- ② Pellet-clad mechanical interaction
- ③ Power to melt
- ④ Departure from nucleate Boiling

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