



NucE 497: Reactor Fuel Performance

Lecture 33: Hydride formation

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Most material taken from slides by Processor Motta

Today we will discuss hydride formation in the cladding

- Module 1: Fuel basics
- Module 2: Heat transport
- Module 3: Mechanical behavior
- Module 4: Materials issues in the fuel
- Module 5: Materials issues in the cladding
 - Zirconium alloys and fabrication
 - Cladding creep and growth
 - Mechanical behavior
 - **Oxidation**
 - **Hydride formation**
 - CRUD formation
- Module 6: Accidents, used fuel, and fuel cycle

Here is some review from last time

- Which step of oxidation is the slowest (the rate limiting step)
 - a) Dissolution of water
 - b) Transport of the oxygen atoms through the oxide layer
 - c) Reaction of O ions with Zr to form ZrO_2
 - d) Reduction of hydrogen ions by electrons at coolant
- What is NOT a negative effect of oxidation on cladding performance
 - a) Creates hydrogen atoms that form brittle hydrides
 - b) Reduces the thermal conductivity
 - c) Replaces metal with a brittle oxide
 - d) Reduces fission rate by absorbing neutrons

Average weight gain of a sample follows linear kinetics

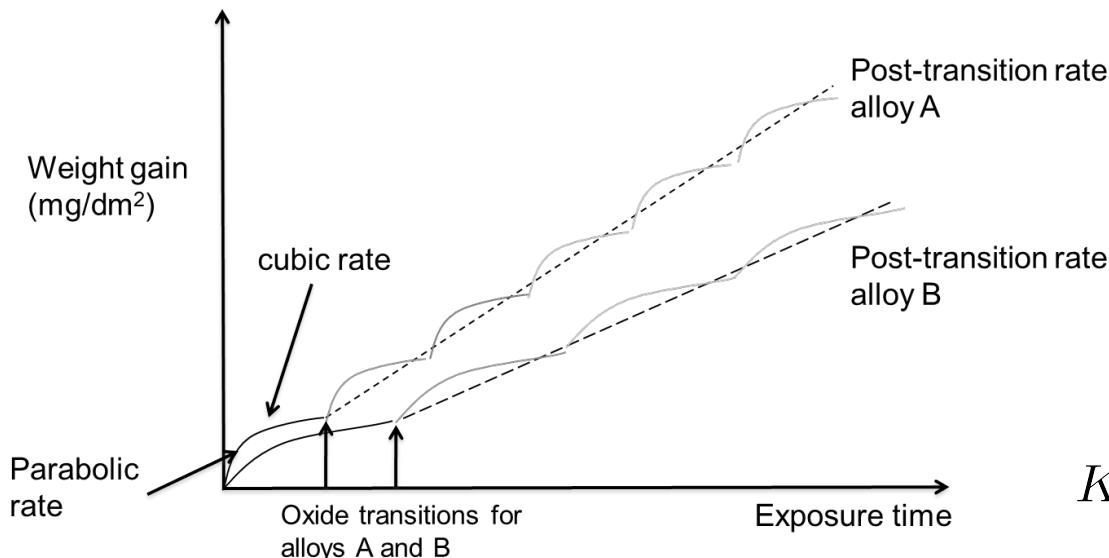
- The oxide reaches transition at different times in different points, but the average is linear

Critical oxide thickness for transition is defined as

$$\delta^* (\mu\text{m}) = 5.1 \exp \frac{-550}{T}$$

Critical time for transition is defined as

$$t^* (\text{d}) = 6.62 \times 10^{-7} \exp \frac{11949}{T}$$



After transition, oxide thickness is

$$\delta (\mu\text{m}) = \delta^* + K_L (t - t^*)$$

$$K_L \left(\frac{\mu\text{m}}{\text{d}} \right) = 7.48 \times 10^6 \exp \frac{-12500}{T}$$

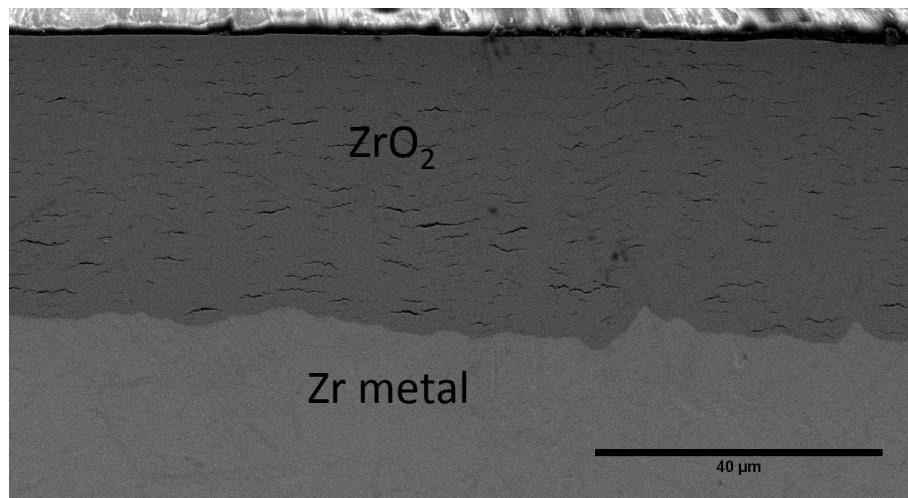
* Constants given apply to ZIRLO

Now let's work a problem

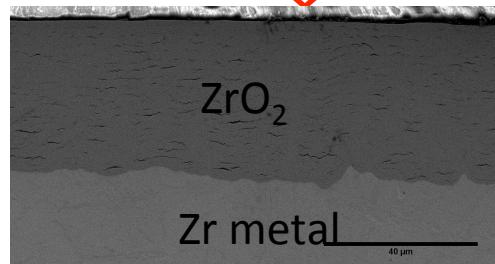
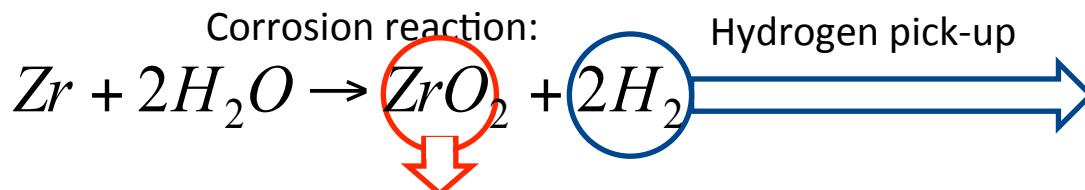
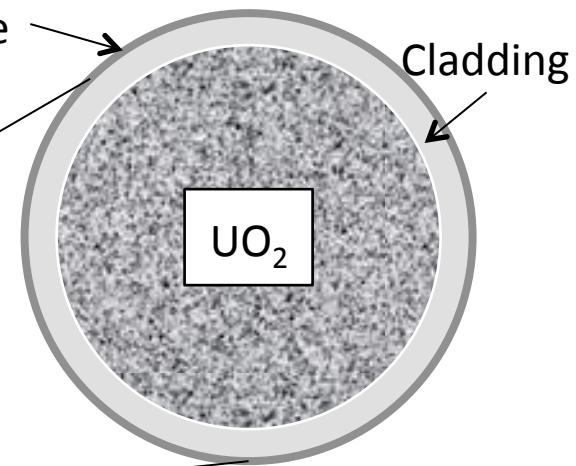
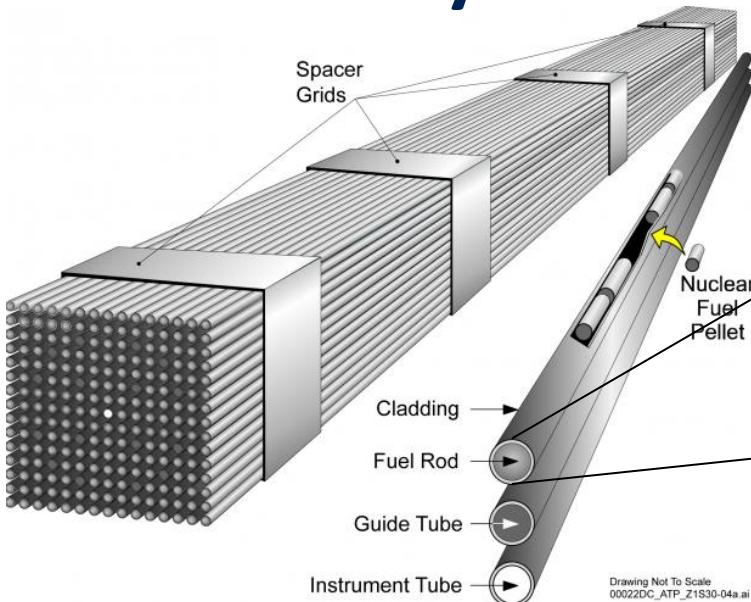
- Estimate the oxide thickness on a ZIRLO sample at 650 K after 200 days exposed to water.
- First, we have to determine if the oxide has gone through transition
 - $t^* (d) = 6.62 \times 10^{-7} \exp \frac{11949}{T}$
 - $t^* = 6.62e-7 * \exp(11949/650) \text{ k} = 63.76 \text{ days}$
 - So, the sample is past transition, so we need to use the linear fit
- Next, we calculate the oxide thickness at transition
 - $\delta^* (\mu\text{m}) = 5.1 \exp \frac{-550}{T}$
 - $\delta^* = 5.1 * \exp(-550/650) = 2.19 \text{ microns}$
- Now, we can compute the final oxide thickness
 - $K_L \left(\frac{\mu\text{m}}{\text{d}} \right) = 7.48 \times 10^6 \exp \frac{-12500}{T}$
 - $K_L = 7.48e6 * \exp(-12500/650) = 0.0333$
 - $\delta (\mu\text{m}) = \delta^* + K_L (t - t^*)$
 - $\delta = 2.19 + 0.0333 * (200 - 63.76) = 6.73 \text{ microns}$

Note that the thickness of ZrO₂ is wider than the corresponding thickness of Zr

- The ratio of oxide thickness to metal thickness is called the Pilling-Bedford ratio (PBR)
 - PBR = 1.56



Corrosion of zirconium so damaging in large part due to hydride formation



Some of the hydrogen atoms produced by oxidation enter the cladding and form a hydride phase

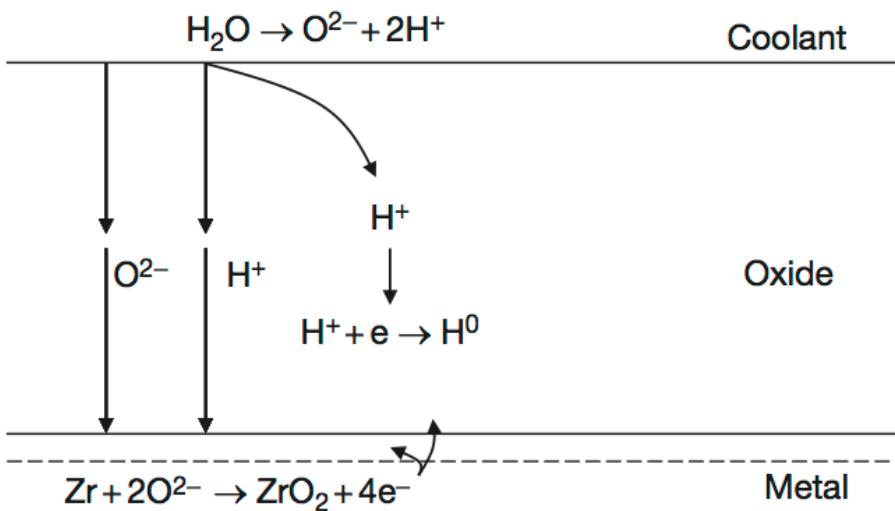


Figure 1 Schematic presentation of the corrosion of the zirconium alloys. Corrosion of zirconium alloys in nuclear power plants; TECDOC-684; International Atomic Energy Agency, Vienna, Austria, Jan 1993.

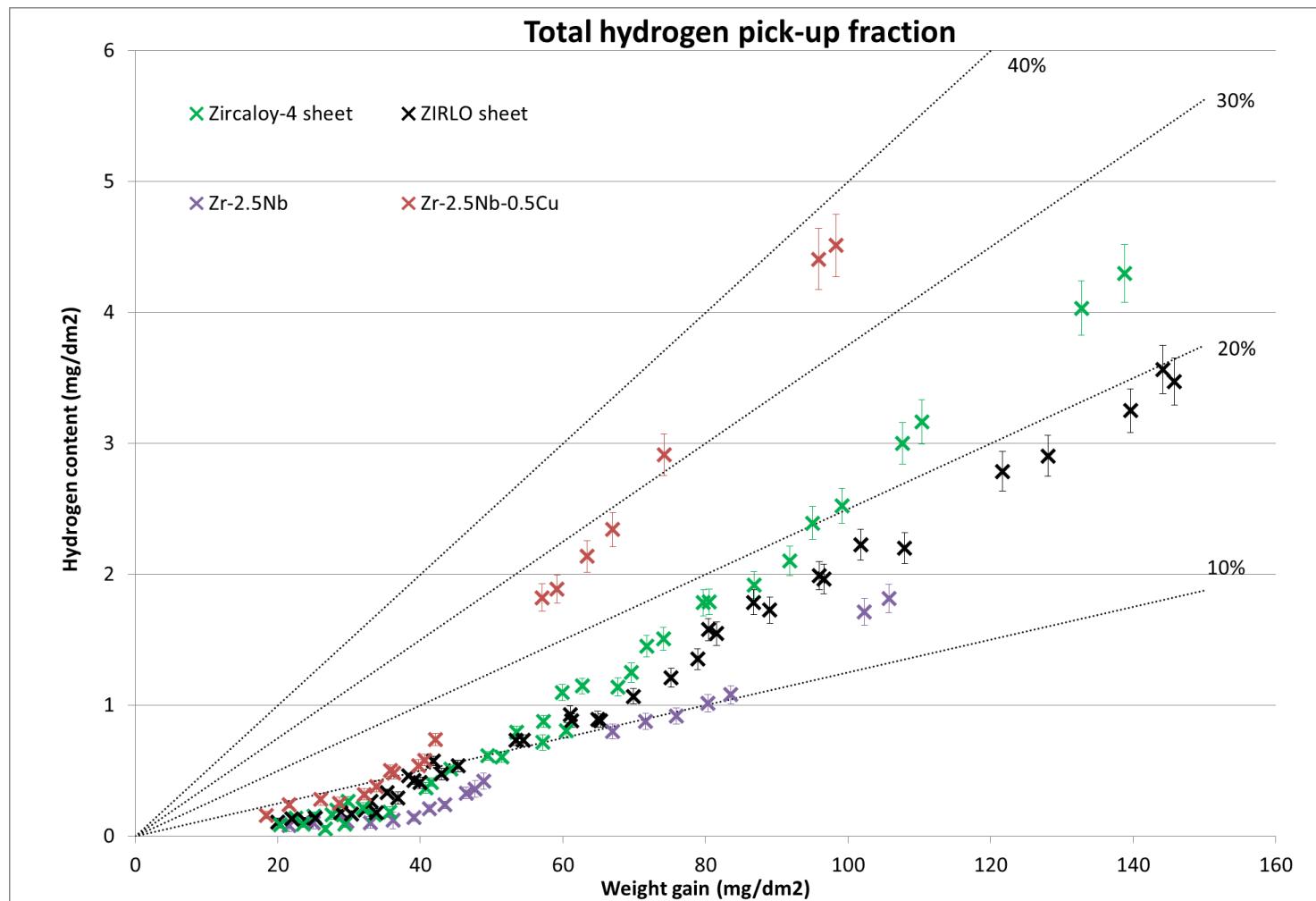
Taken from Allen *et al.*, *Comprehensive Nuclear Materials* (2012), 5, 49-68.

- The fraction of the produced hydrogen that enters the cladding is defined by the pickup fraction:

$$f_H = \frac{H_{\text{absorbed}}}{H_{\text{generated}}}$$

- Hydrogen is produced twice as fast as oxygen
 - $J_H = 2 f J_O$

Normally Hydrogen pickup fraction is assumed constant but really it is not



$f = 15\%$ is a commonly used value

Given a thickness of oxide, how can we predict the hydrogen pickup?

- A cladding with an initial thickness of 600 microns that initially has 40 wt.ppm H undergoes corrosion to a total oxide thickness of 80 microns. What is the overall hydrogen content in wt. ppm if the hydrogen pickup fraction is 15%?
- First, we must determine the weight of H that has entered the cladding
 - δ_{ZrO_2} is 5.68 g/cm³, of which $32/(91+32) = 0.26 = 26\%$ is O, thus 1.47 g/cm³ of O
 - A 1 micron oxide layer corresponds to a weight gain of 14.7 mg/dm² (see previous lecture), and thus with an 80 micron layer, weight gain = $14.7 \times 80 = 1176 \text{ mg/dm}^2$
 - This mass corresponds to $1.176 N_A / 16$ atoms of oxygen = $4.42 \times 10^{22} \text{ atoms/dm}^2$
 - $f = 15\%$, so the ingress of hydrogen will be $0.15 \times 2 \times 4.42 \times 10^{22} = 1.33 \times 10^{22} \text{ atoms of hydrogen/dm}^2$, or 0.022 g of H.
- Now, we determine the fraction in wt. ppm in a 10 cm square cross section
 - The uncorroded thickness is $600 - 80/\text{PBR} = 600 - 80/1.56 = 549$ microns
 - The volume of zirconium is $549 \times 10^{-4} (\text{cm})^3 \times 10 \times 10 = 5.49 \text{ cm}^3$
 - $\delta_{\text{Zr}} = 6.5 \text{ g/cm}^3$, so the total mass of Zr is $6.5 \times 5.49 = 35.7 \text{ g}$.
- Thus the hydrogen concentration is $0.022 / 35.7 = 6.18 \times 10^{-4} = 618 \text{ wt. ppm}$, which, added to the original 40 wt. ppm, is 658 wt. ppm

We can estimate the hydrogen content in the cladding from the oxide thickness δ and the pickup fraction f

$$C_H^{clad} [\text{wt.ppm}] = \frac{m_H}{m_{Zr}} = \frac{2fm_O}{m_{Zr}} = \frac{2f \times \delta \times \rho_{oxide} \times f_{ZrO_2}^O \times M_H / M_O}{\left(t - \frac{\delta}{PBR} \right) \times \rho_{metal}} \times 10^6$$

C_H^{clad} concentration (wt ppm)

ρ_{oxide} oxide density

ρ_{Zr} Zr metal density

$f_{ZrO_2}^O$ Fraction of oxygen in ZrO₂ mass

PBR Pilling-Bedworth Ratio

M_H moelcular mass of H

M_O molecular mass of O

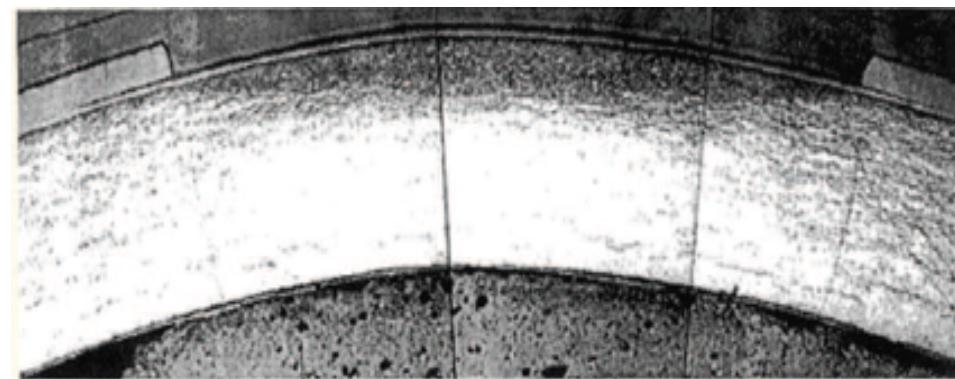
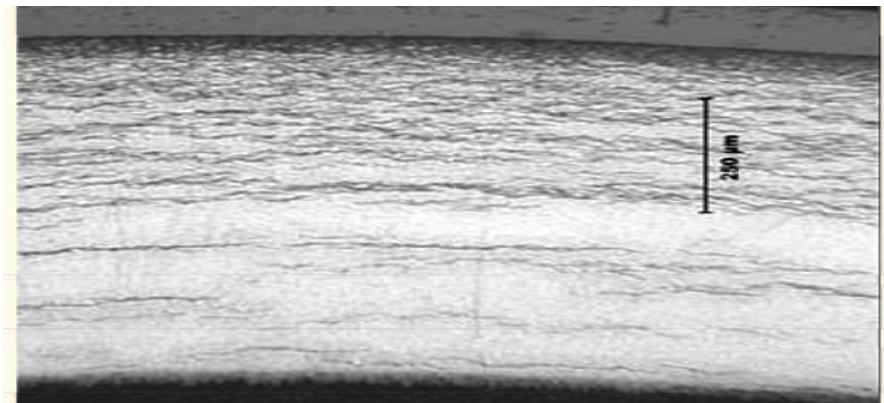
t cladding thickness

Hydrogen diffuses very quickly in zirconium, so that the hydrogen quickly spreads through the cladding

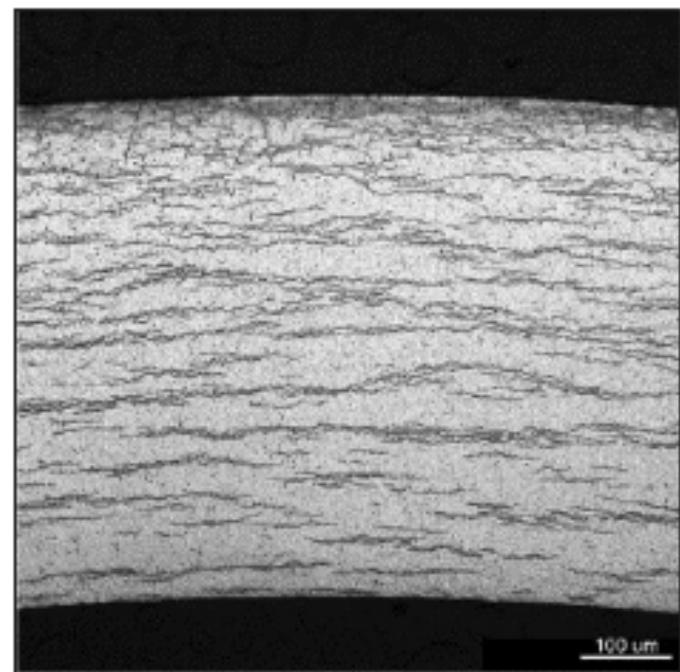
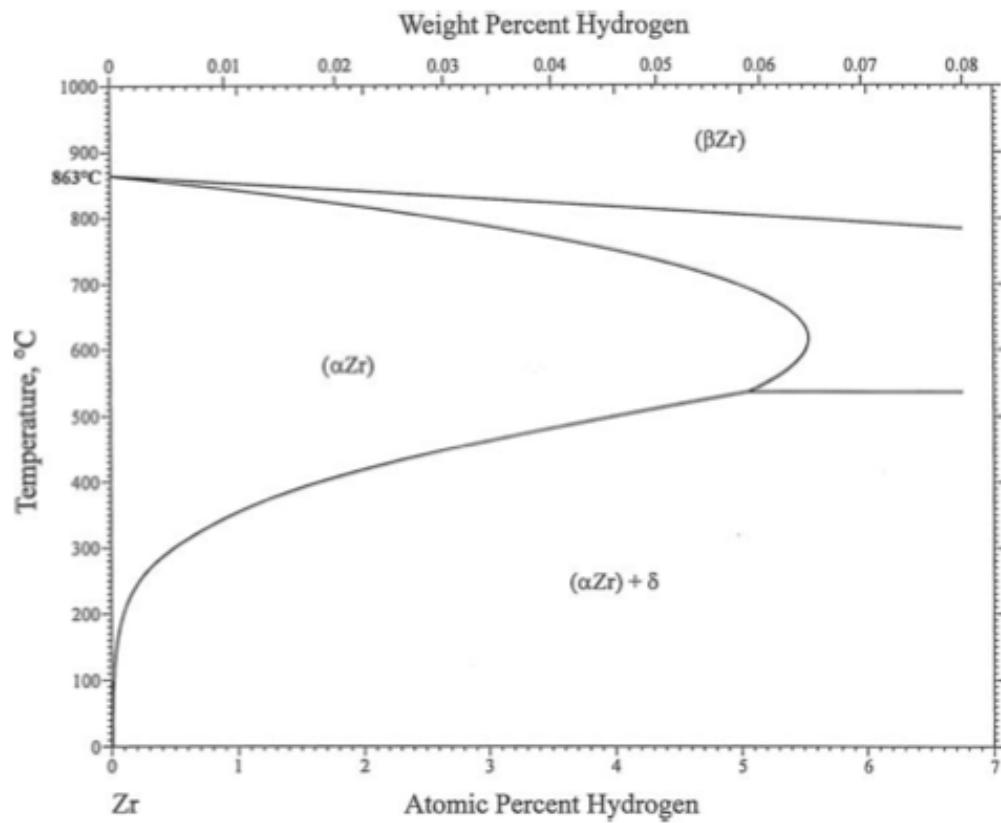
- The diffusion coefficient of H in Zr is $D_{Zr}^H = D_o^H \exp(-E_m^H / k_B T)$
 - $E_m^H = 0.47\text{eV}$ $D_o^H = 7 \times 10^{-3} \text{cm}^2/\text{s}$
- The characteristic time required for hydrogen to diffuse through the entire cladding is
$$t = \frac{L^2}{4D_{Zr}^H}$$
- What is the characteristic time for cladding at 355°C (average cladding temperature) that is 0.06 cm thick?
 - $D_{Zr}^H = 7 \times 10^{-3} \times \exp(-0.47 / (kb * (355 + 273.15))) = 1.19 \times 10^{-6} \text{cm}^2/\text{s}$,
 - $t = 0.06^2 / (4 * 1.19 \times 10^{-6}) \text{cm}^2/\text{s} = 756.3 \text{s} = 12 \text{ min}$,
 - So, the hydrogen atoms have plenty of time to move through the entire clad

Hydride concentrations are not uniform, because they respond to temperature and stress gradients

- Hydrogen tends to move toward lower temperature (Soret effect)
- It also moves to areas with tensile stress
- Where in the cladding has the lowest temperature?



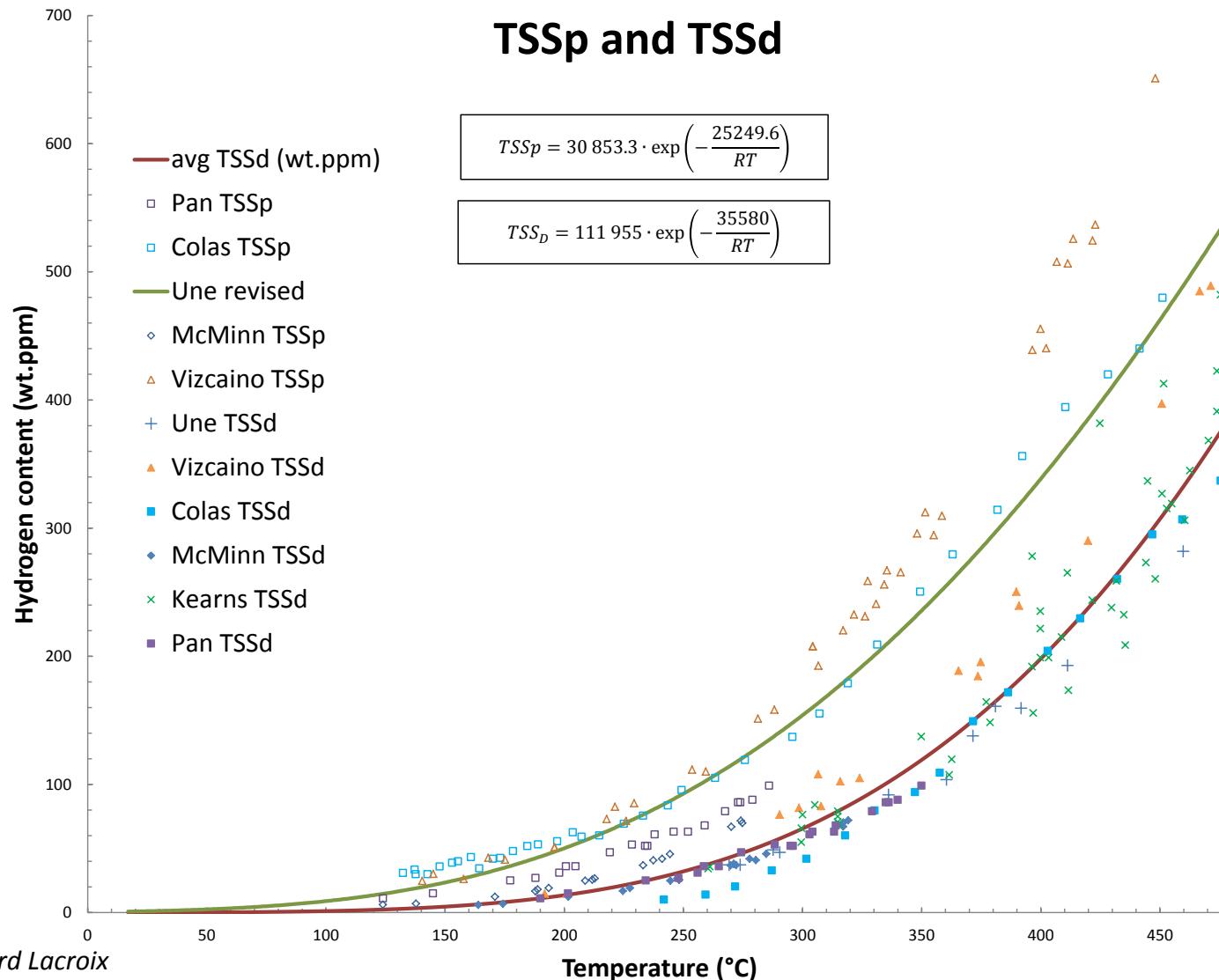
Hydrogen has a low solubility in zirconium, so even small hydrogen concentrations result in hydrides



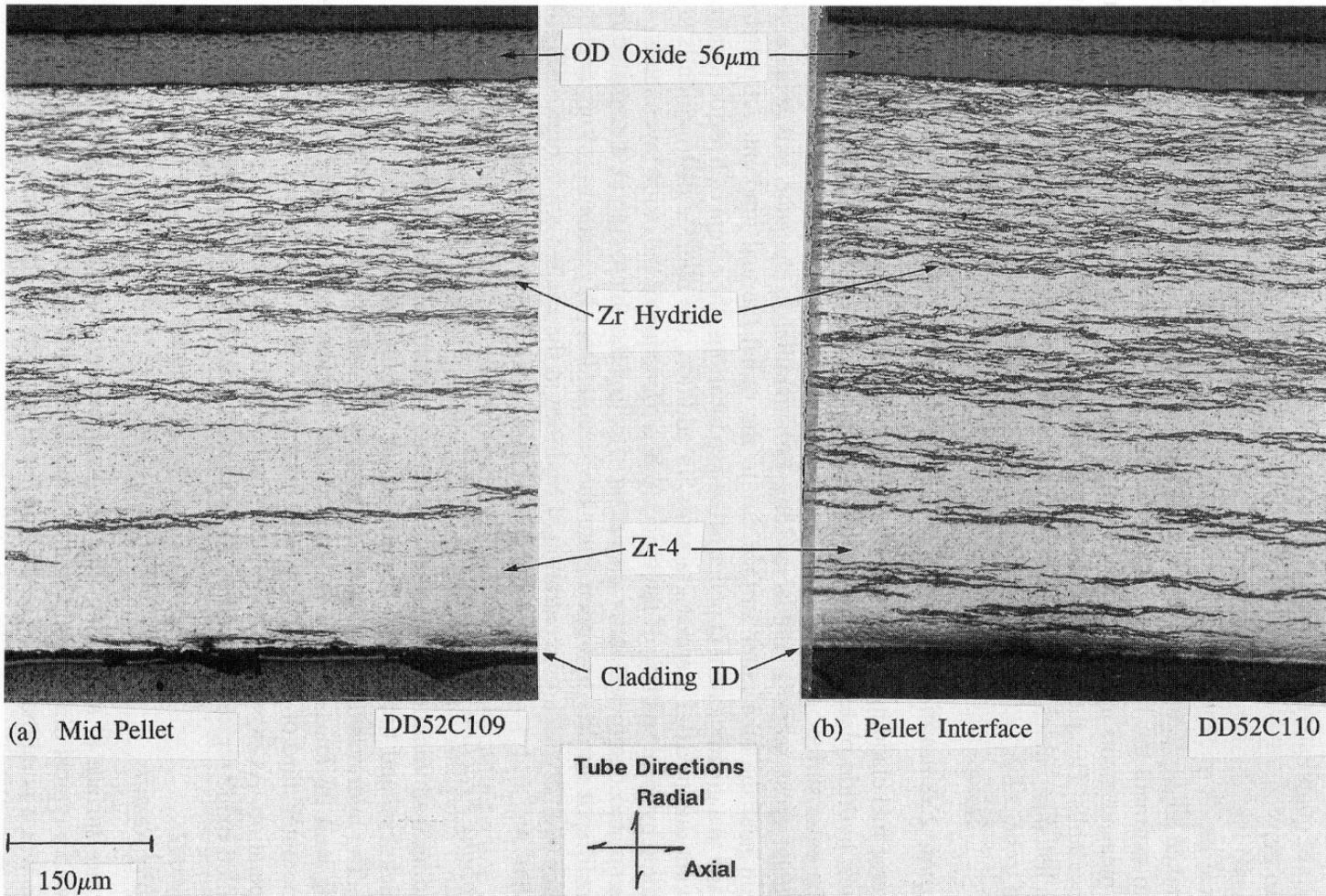
Hydrided fuel cladding
Daum et al. Penn State 2007

Hydrides dissolve during heating at a lower temperature than they precipitate during cooling

TSSp and TSSd

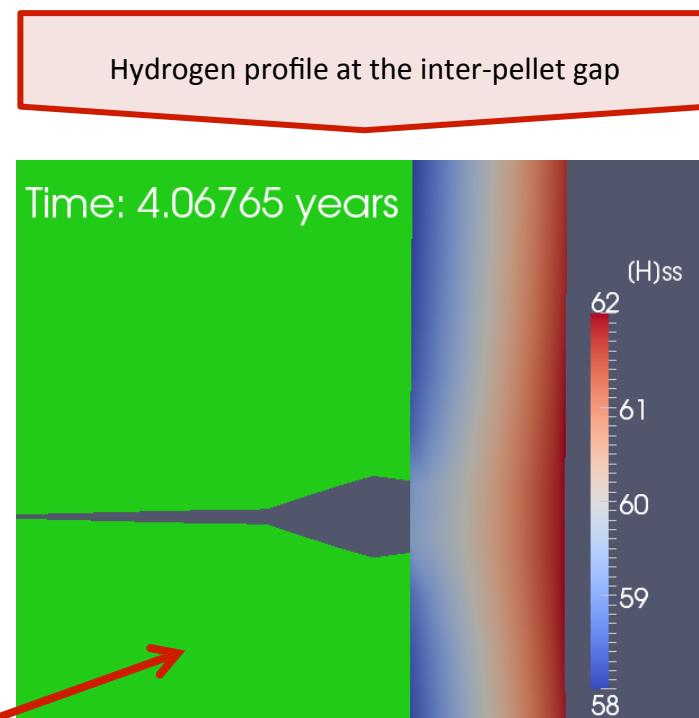
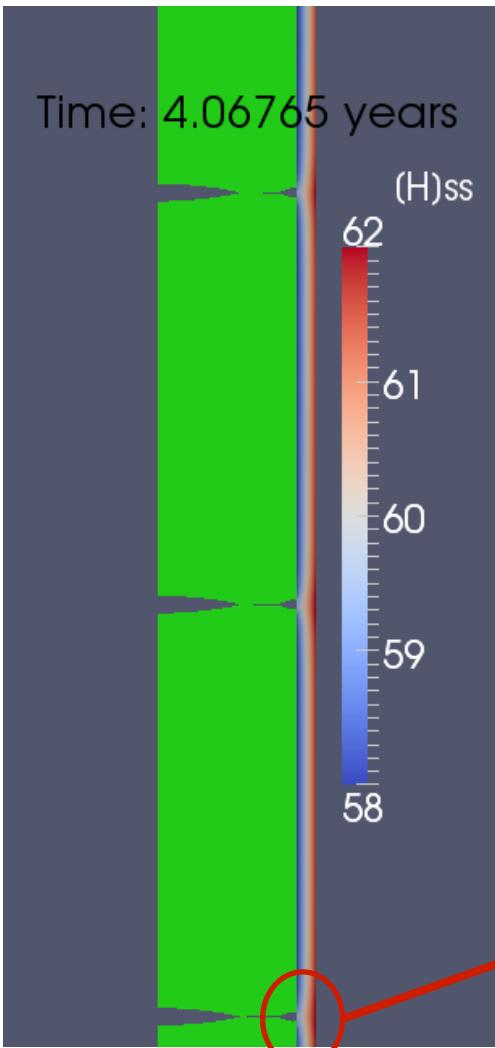


The hydride rim is caused by the Soret effect and the temperature dependence of the solubility

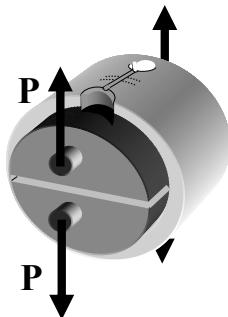


—Etched appearance of zirconium hydride concentrations and orientation at mid-pellet and pellet-to-pellet interface location

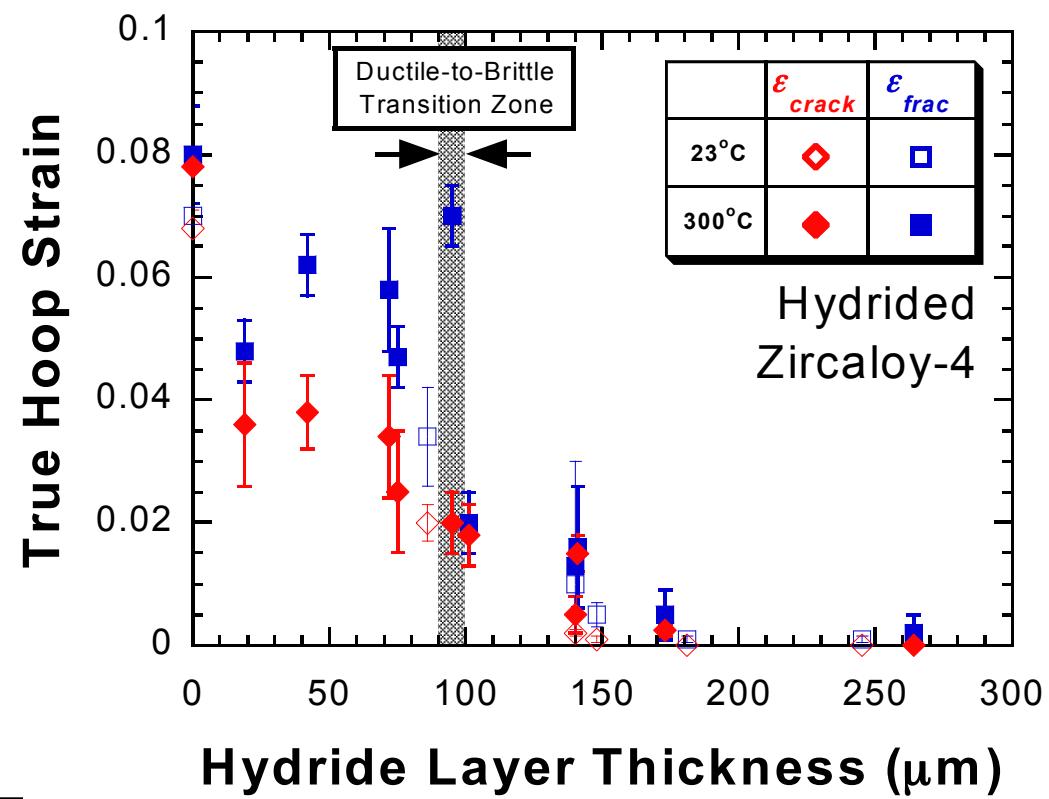
Hydrogen concentration varies between pellets, due to temperature gradients



The hydride rim and blisters can cause a loss of ductility



The presence of a hydride rim or blister considerably decreases cladding ductility

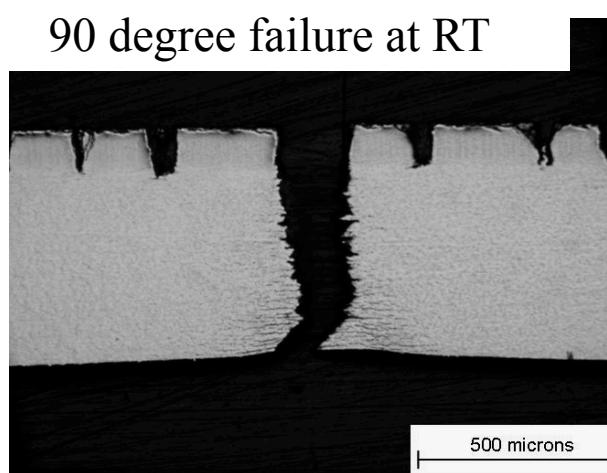


⇒ Major influence in decreasing RIA resistance

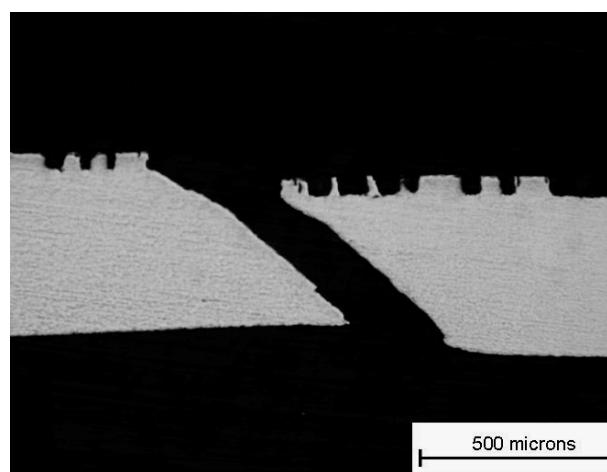
Daum, Bates, Koss Motta, 2003

Here are some examples showing the impact of blisters on cladding failure

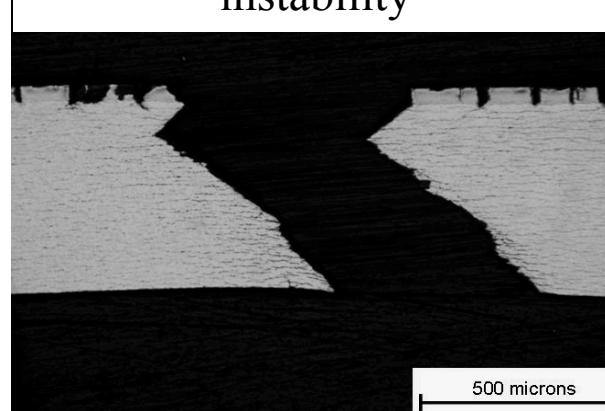
**93 µm Blister
Broken at 25 °C
M020**



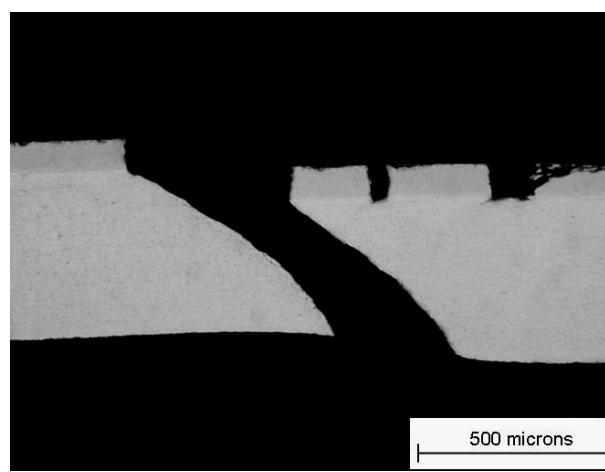
**53 µm Blister
Broken at 300 °C
M025**



But in small blisters => shear instability



**40 µm Blister
Broken at 25 °C
M014**



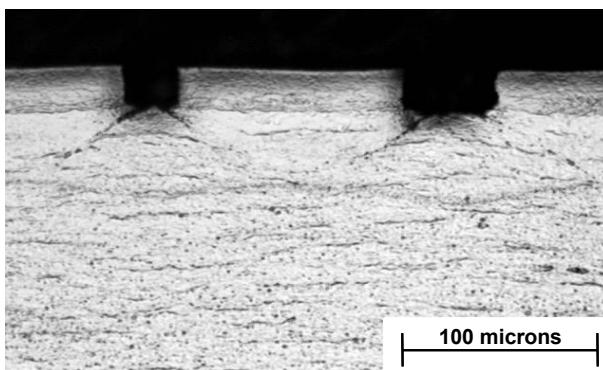
**83 µm Blister
Broken at 300 °C
M023**

At 300 C, 45 degree shear

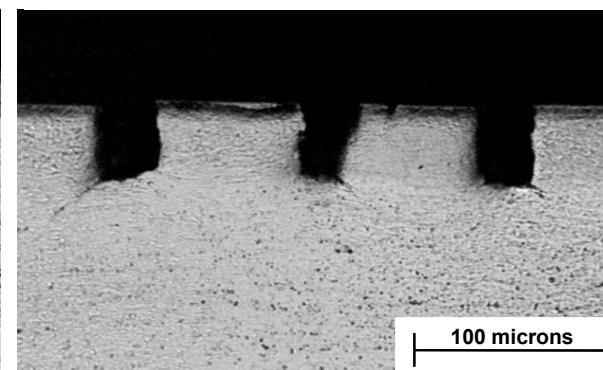
And here are a few more examples

Square-bottom, blunted cracks,
Strain concentration at corners, cracks

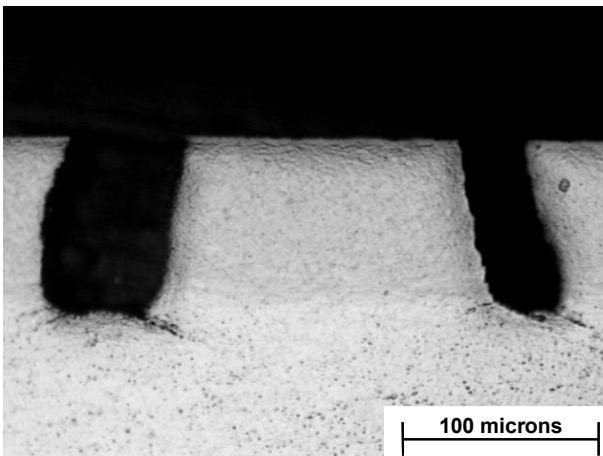
26 μm
M028



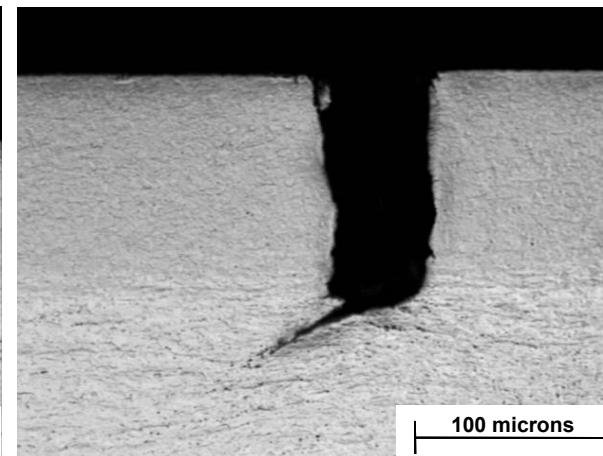
53 μm
M025



83 μm
M023



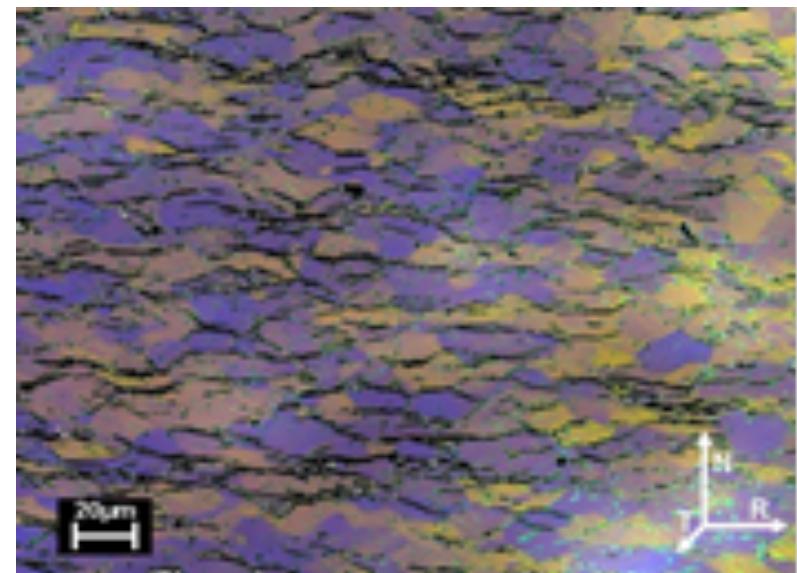
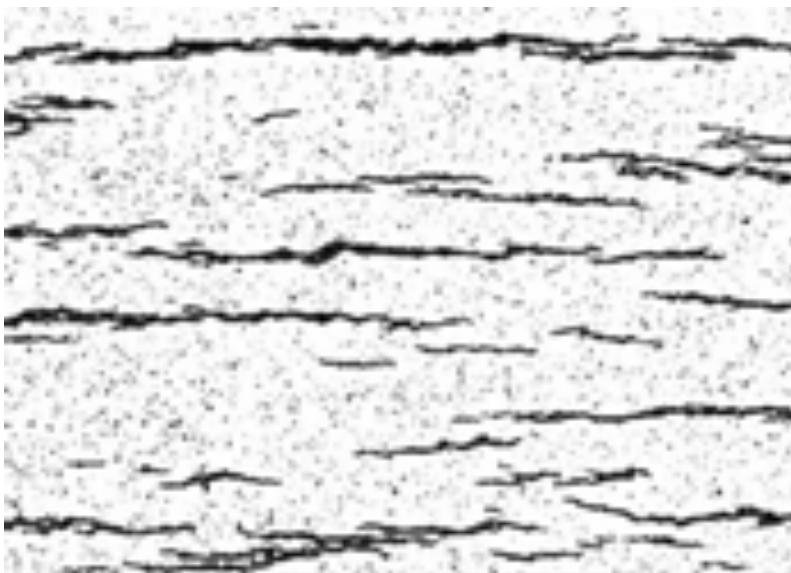
127 μm deep
M024



- Failure occurs by crack propagation on 45° angle



Under reactor conditions, hydride platelets precipitate circumferentially



- Circumferential precipitation occurs because of
 - The coolant pressure
 - The crystallographic texture in the as fabricated cladding

In used fuel after drying, the hydrides can reprecipitate with a radial orientation

- Temperature increases during drying and the hydrides dissolve
- Fission gas release during drying pressurizes the tube
- When the temperature drops, the new stress state can cause the hydrides to reform with a different orientation

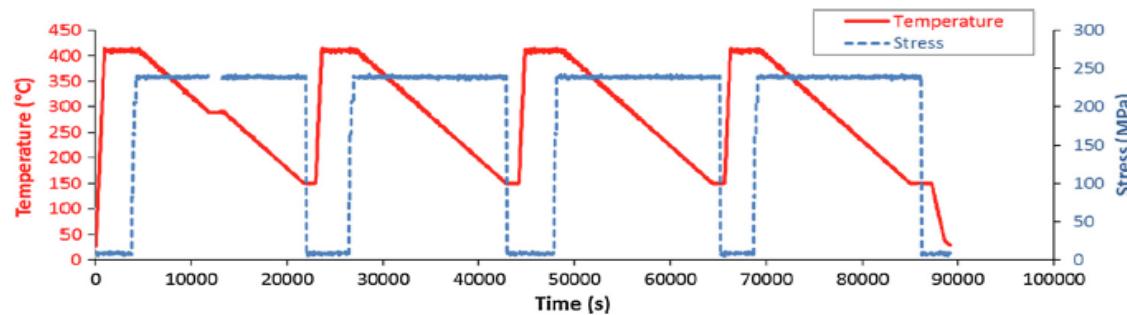
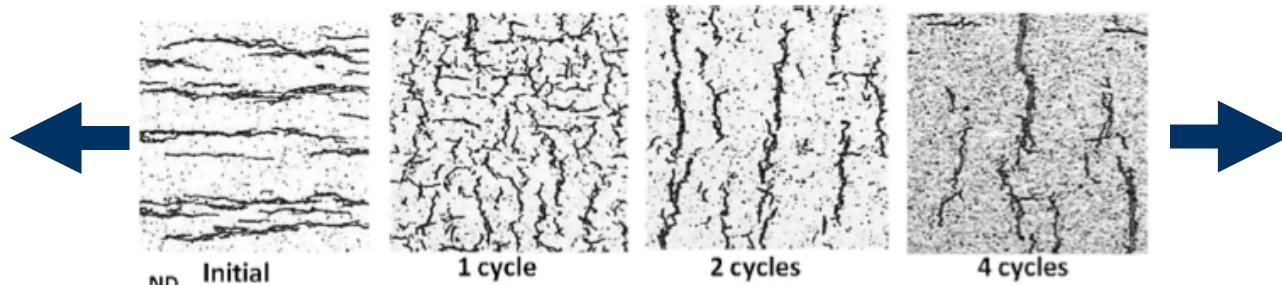
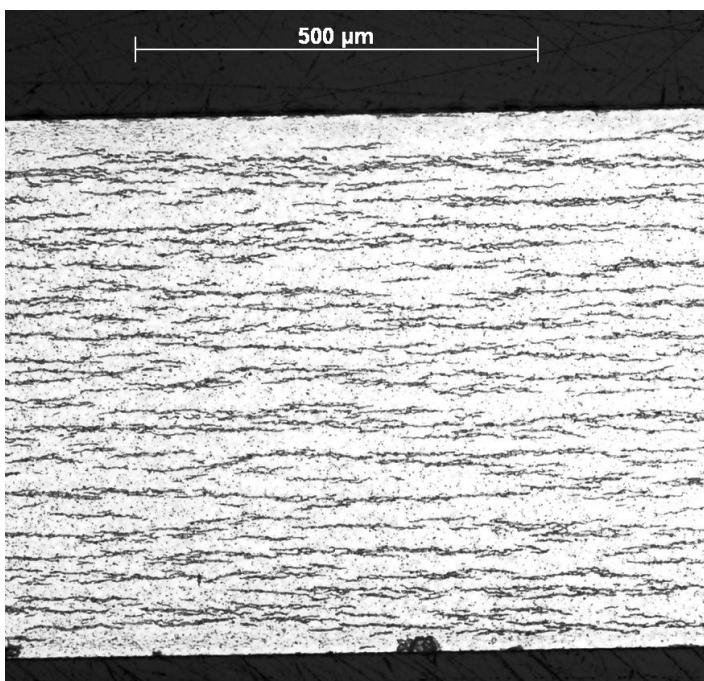


Fig. 1. Example of four thermo-mechanical cycles as applied to a sample with 192 wt.ppm of hydrogen.



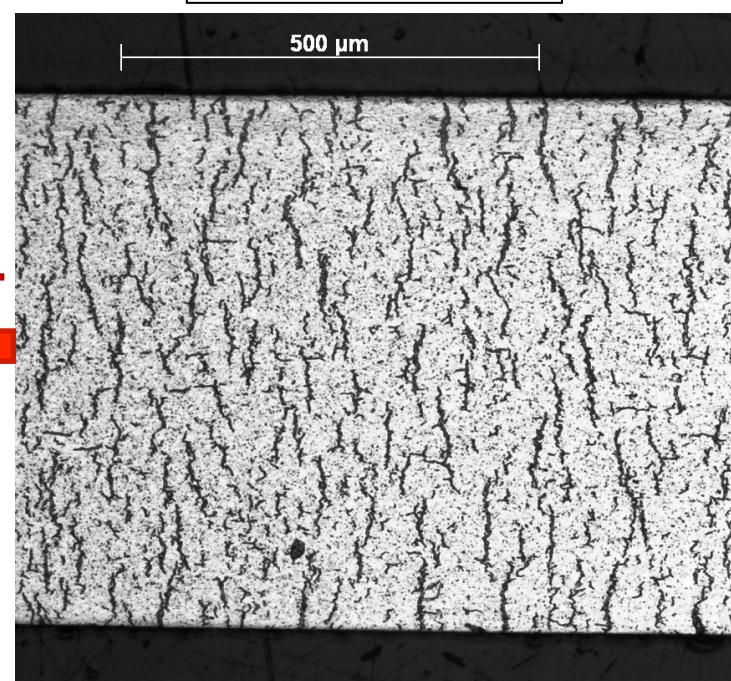
The hydrides reform in a radial direction due to the tensile hoop stress

Hydrides
formed under
no applied load



Transverse
direction

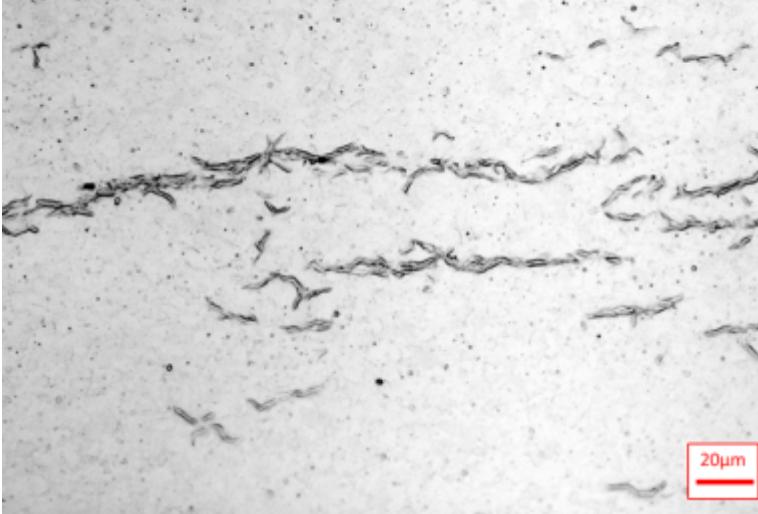
Hydrides
formed under
**tensile applied
load**



Kearns JNM 1967
Louthan JNM 1963

Hydride Microstructures

In-plane (“circumferential”) Hydrides

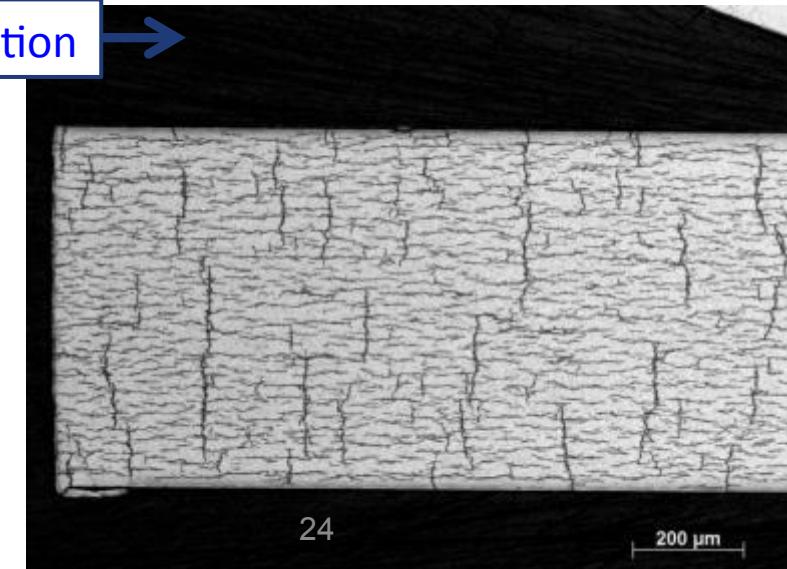
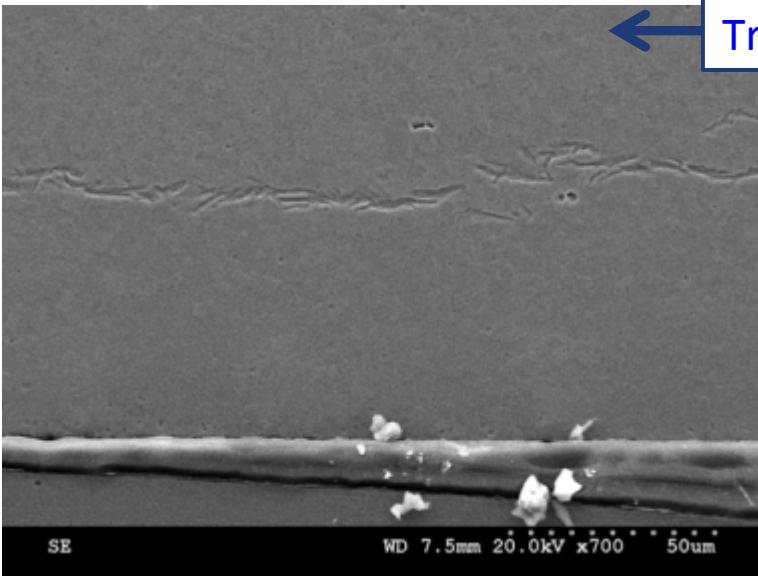


↑
Normal Direction
↓

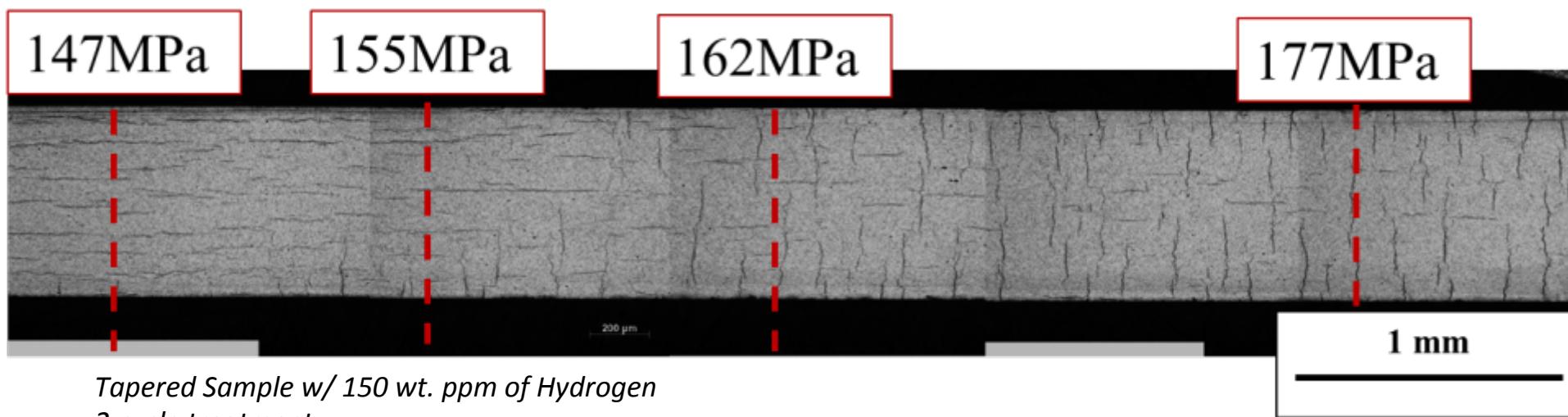
Out-plane (“radial”) Hydrides



← Transverse Direction →



There is a critical tensile stress at which the hydrides reorient

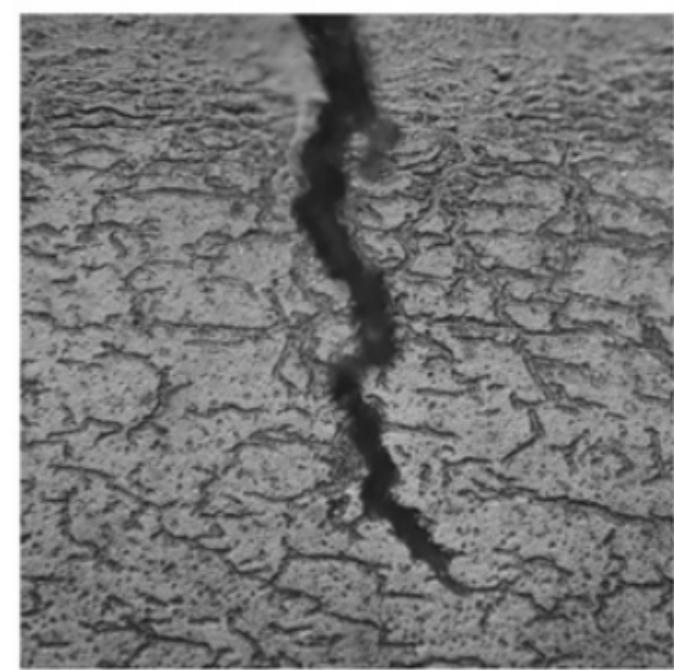
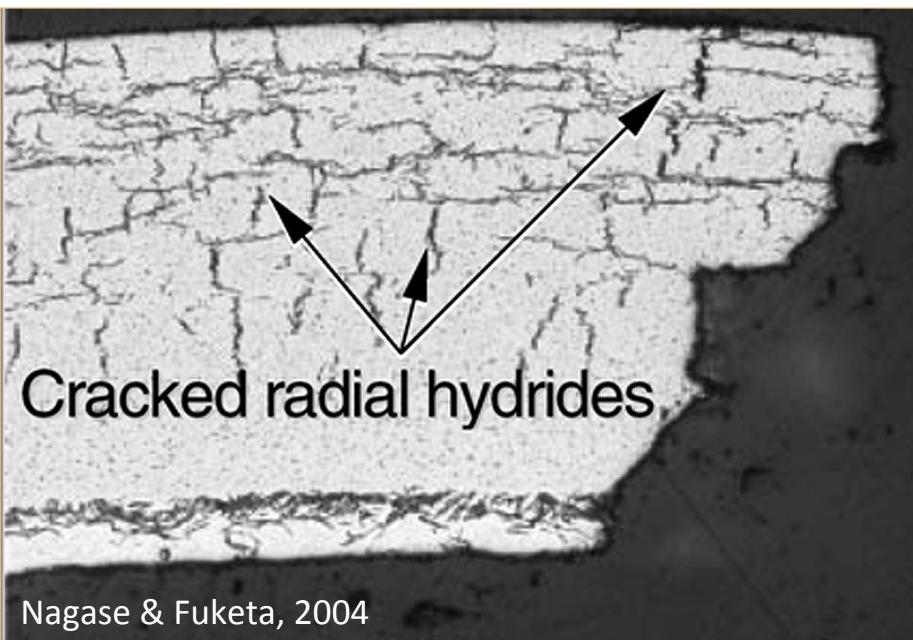


Tapered Sample w/ 150 wt. ppm of Hydrogen
2-cycle treatment,

- Hydride orientation changes as a function of stress level
- The critical stress to reorient hydrides during re-precipitation when in uniaxial tension is approximately **150 MPa**

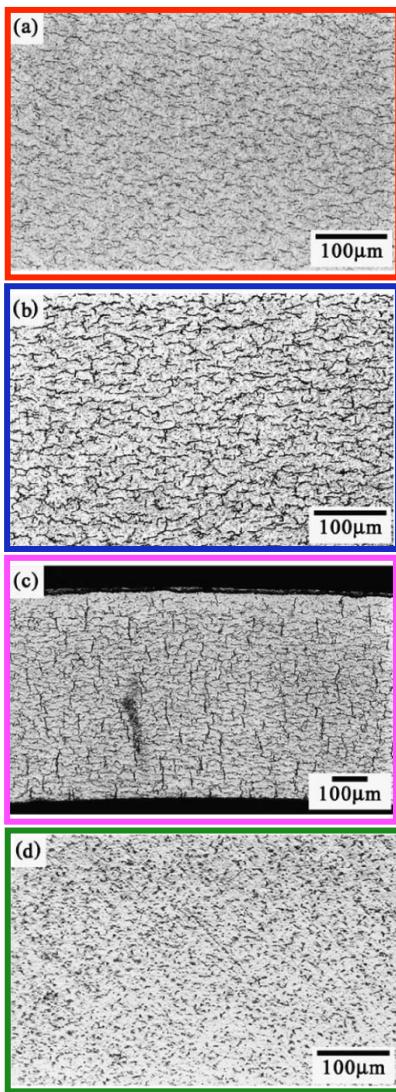


Radial hydrides provide easy crack paths

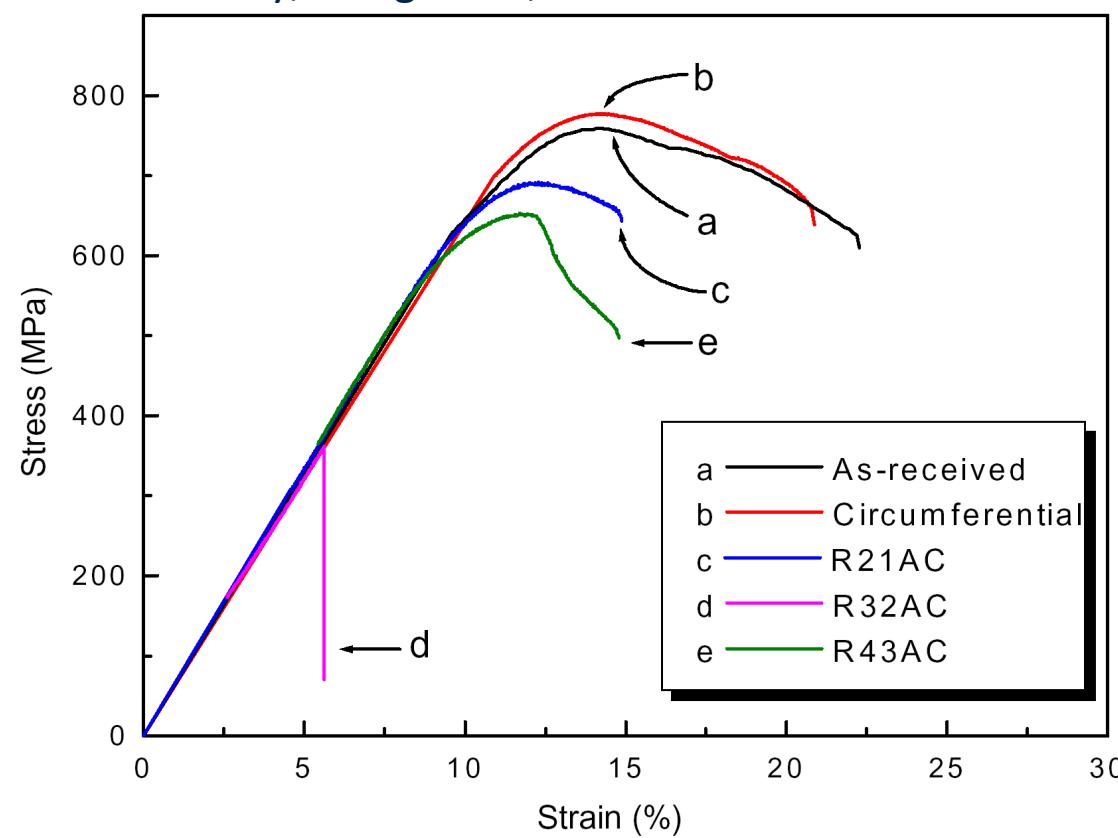


At Yield Load
100 Microns

Radial hydrides significantly decrease the ductility of the cladding

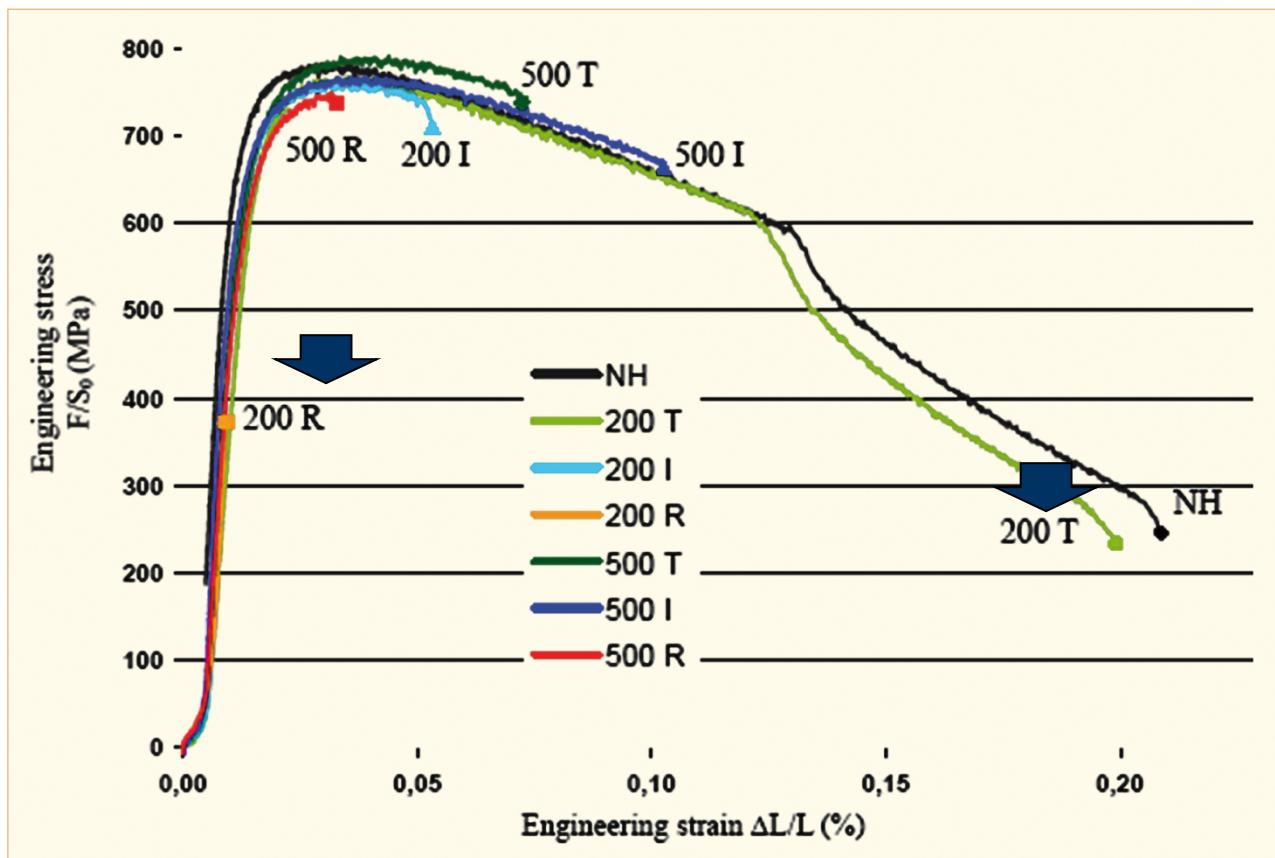


Ring tests at 20°C : specimen with radial hydrides had lowest ductility, Hong & Lee, 2005



Radial hydrides significantly decrease the ductility of the cladding

Specimen	200T	200I	200R	500T	500I	500R
Radial hydrides						
Length proportion (%)	3	18	64	1	10	12



Racine et al., 2005

Summary

- Hydrogen released by oxidation enters the cladding
- It quickly diffuses throughout the cladding, but prefers low temperature
- Due to low solubility (that is a function of temperature), hydrides form
- Hydrides are brittle, and so reduce the ductility of the cladding
- Radial hydrides can form in used fuel after drying, and reduce the ductility much more than circumferential hydrides