

Fuel Swelling

NE 591

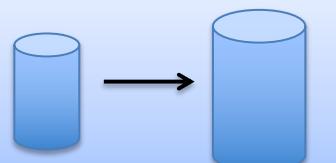
Last time

- Fission products change the fuel behavior
- Fission gas is released in three stages
 1. Fission gas production and diffusion to grain boundaries
 2. Grain boundary bubble nucleation, growth, and interconnection
 3. Gas transport through interconnected bubbles to free surfaces
- Fission gas release is measured using post-irradiation annealing and in pile experiments
- Fission gas release models are used to understand fission gas experiments and to predict gas release for fuel performance codes
- Spherical grain models predict a fraction of gas release for post-irradiation annealing or for in-pile gas release
- Fission gas diffusivity behavior changes with temperature and fission rate

Fuel changes size and shape under reactor operation

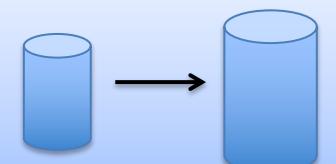
Thermal Expansion

- Increase in volume
- Decrease in density
- Caused by increasing temperature



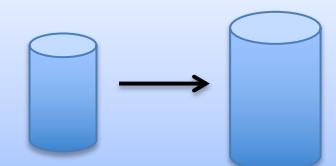
Densification

- Decrease in volume
- Increase in density
- Caused by shrinking of porosity left after sintering



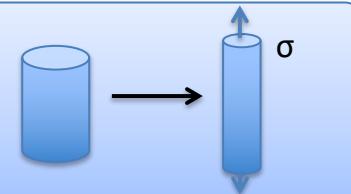
Swelling

- Increase in volume
- Decrease in density
- Caused by fission products



Irradiation Creep

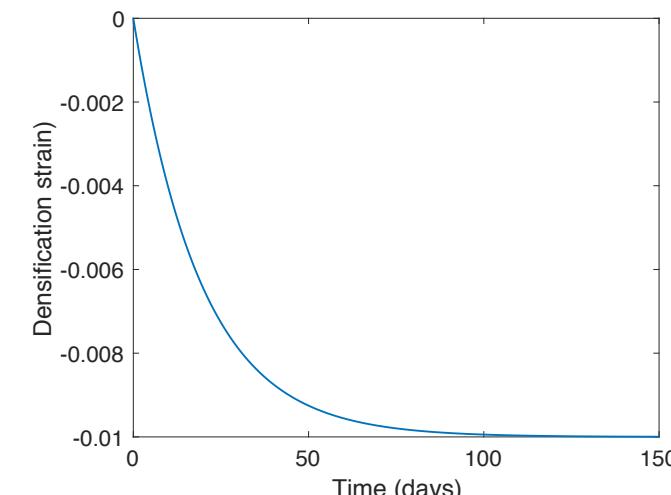
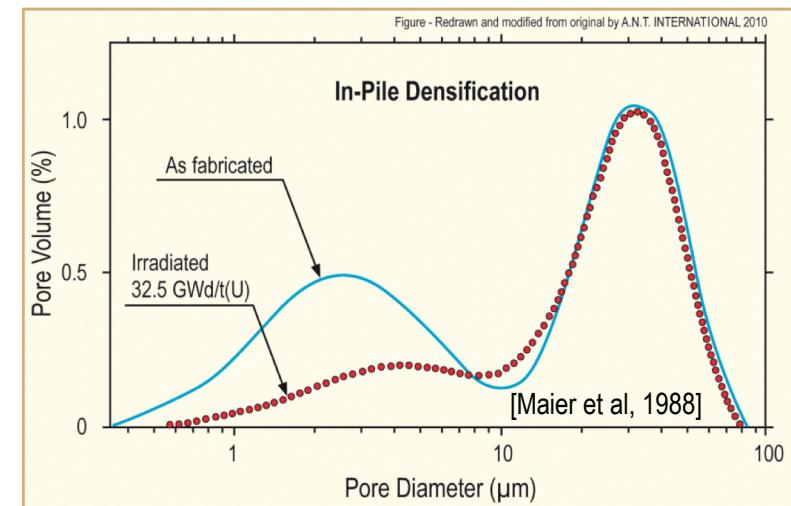
- Change in shape
- Constant density
- Occurs under stress with $\sigma < \sigma_y$



Densification

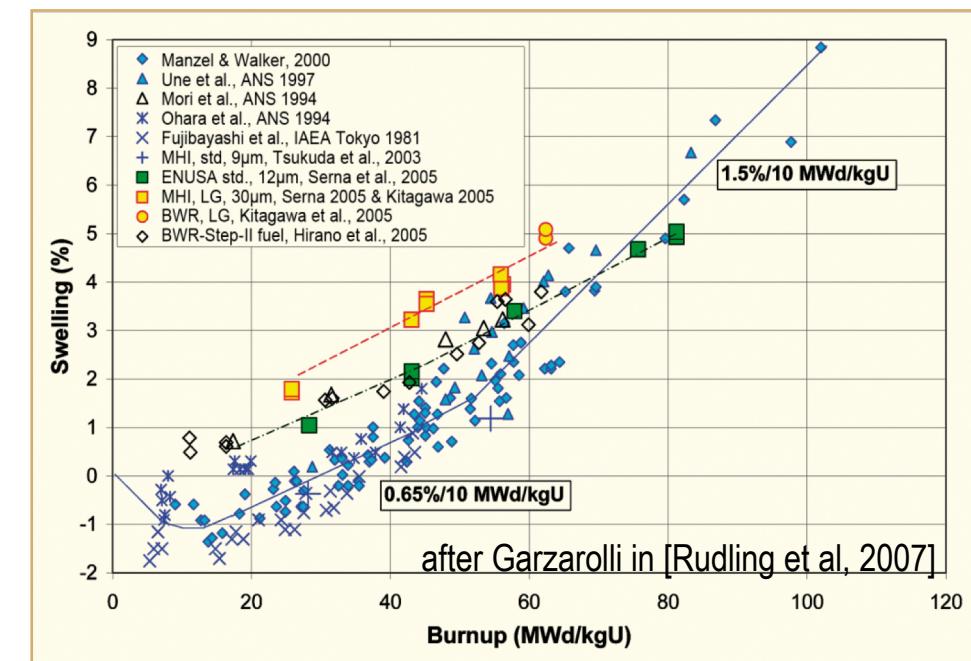
- Densification takes place during initial 5 - 10 MWd/kgU
 - Small, as-built pores close due to effects of fission spikes and vacancy diffusion
 - Large pores stable (in absence of large hydrostatic stress)
- Empirical correlation for densification is a function of
 - β - Burnup (in FIMA)
 - $\Delta\rho_0$ – Total densification that can occur (a common value is 0.01)
 - β_D – Burnup at which densification stops (a common value is 5 MWD/kgU)
 - $C_D = 7.235 - 0.0086(T(\text{ }^\circ \text{ C}) - 25)$ for $T < 750\text{ }^\circ \text{ C}$ and $CD = 1$ for $T \geq 750\text{ }^\circ \text{ C}$
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$$\epsilon_D = \Delta\rho_0 \left(e^{\frac{\beta \ln 0.01}{C_D \beta_D}} - 1 \right)$$



Fission product induced swelling

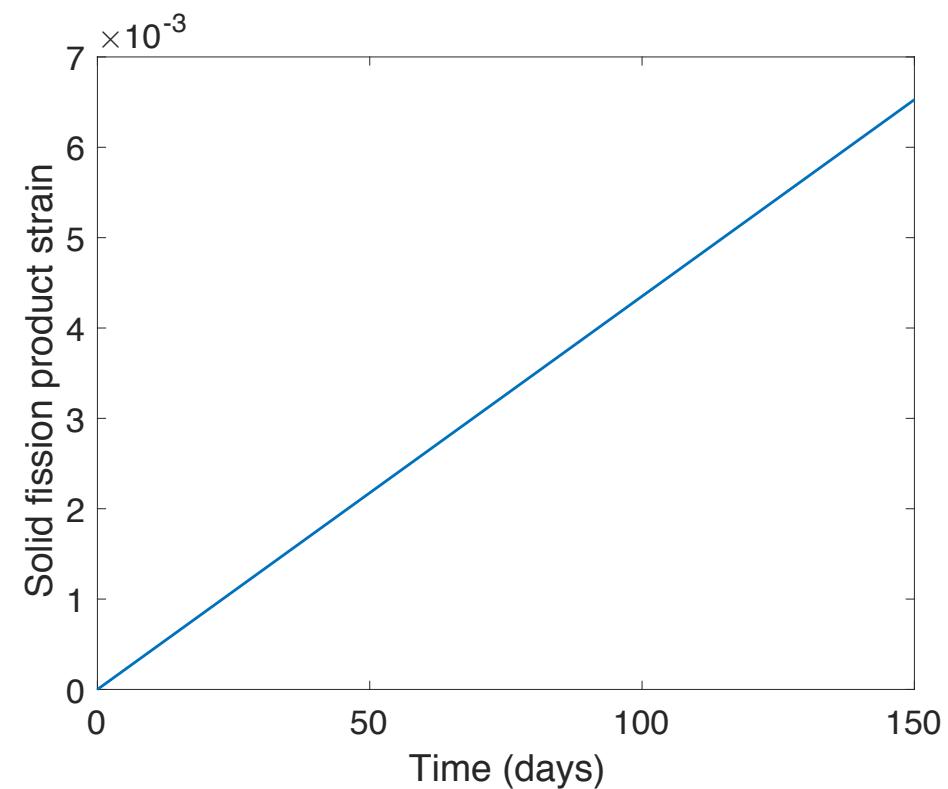
- Fission product swelling results from three changes in the fuel microstructure
 - Solid swelling: Accumulation of soluble and insoluble fission products in fuel matrix
 - Gaseous swelling: Accumulation of gaseous and volatile fission products in intragranular and intergranular pores
 - High burnup swelling: Restructuring of pellet rim with the accumulation of fission gas in a large number of small pores



Solid fission product swelling

- The solid fission product swelling model is a function of:
 - B – Burnup (in FIMA)
 - ρ – Initial UO_2 density (g/cm^3)

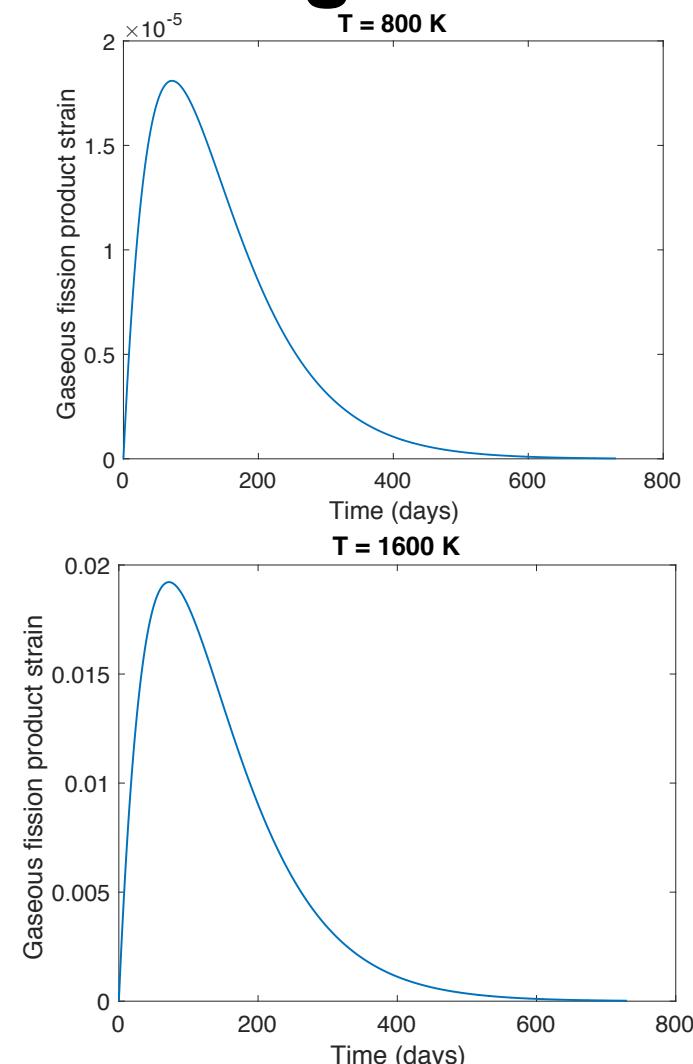
$$\epsilon_{sfp} = 5.577 \times 10^{-2} \rho \beta$$



Gaseous fission product swelling

- Gaseous swelling varies strongly with temperature, fission rate and stress
- $T < 1000\text{K}$
 - Fission gas atoms remain in fuel matrix or collect in small, isolated, intragranular pores ($<1\text{ nm}$)
 - Intragranular pore size limited by fission spikes that drive gas back into fuel matrix
 - Gaseous swelling constrained by fission gas release
- $T = 1000$ to 1700 K
 - Swelling takes place at hot interior of pellet
 - Gas atoms in fuel matrix diffuse to grain boundaries and collect in pores
 - Gas pressure causes bubbles to increase in size and to coalesce into larger pores
 - Gaseous swelling opposed by applied stress (opposite of hot pressing)
 - Gaseous swelling also constrained by fission gas release

$$\epsilon_{gfp} = 1.96 \times 10^{-28} \rho \beta (2800 - T)^{11.73} e^{-0.0162(2800-T)} e^{-17.8\rho\beta}$$



Total change in volume

- The total change in volume is found by adding all components of dimensional change
 - $\varepsilon_{\text{tot}} = \varepsilon_{\text{th}} + \varepsilon_D + \varepsilon_{\text{sfp}} + \varepsilon_{\text{gfp}}$
- Example:
 - fission rate = $2.5 \times 10^{13} \text{ f}/(\text{cm}^3 \text{ s})$
 - temperature = 1400 K
 - $T_{\text{ref}} = 300 \text{ K}$
 - For densification: $\Delta\rho_0 = 0.01$ and $\beta_D = 5 \text{ MWD/kgU}$
 - Total time: 2 weeks

Change in Volume Example

- First, we need to calculate the burnup, $\beta = \dot{F}t/N_U$
 - $N_U = N_a \delta_U/M_U = 6.022e23 * 9.65/238 = 2.44e22$ atoms of U/cm³
 - $\beta = 2.5e13 * 3600 * 24 * 7 * 2 / 2.44e22 = 0.0012$ FIMA
- Next, we need to determine the strain from thermal expansion
 - $\epsilon_{th} = \alpha \Delta T = 11e-6 * (1400 - 300) = 0.0121$
- Then, we consider densification, $\epsilon_D = \Delta \rho_0 \left(e^{\frac{\beta \ln 0.01}{C_D \beta_D}} - 1 \right)$
 - We need to calculate C_D , but because we are higher than 750 ° C, $C_D = 1$
 - We need to convert the burnup to FIMA, $\beta_D = 5 \text{ MWD/kgU}/950 = 0.0053$ FIMA
 - $\epsilon_D = 0.01 * (\exp(0.0012 * \log(0.01) / (1 * 0.0053)) - 1) = -0.0065$

Change in Volume Example

- For solid fission product swelling, $\epsilon_{sfp} = 5.577 \times 10^{-2} \rho \beta$

- For the density of UO₂, $\rho = 10.97 \text{ g/cm}^3$

- $\epsilon_{sfp} = 5.577e-2 * 10.97 * 0.0012 = 7.34e-4$

- Finally, gaseous fission product swelling

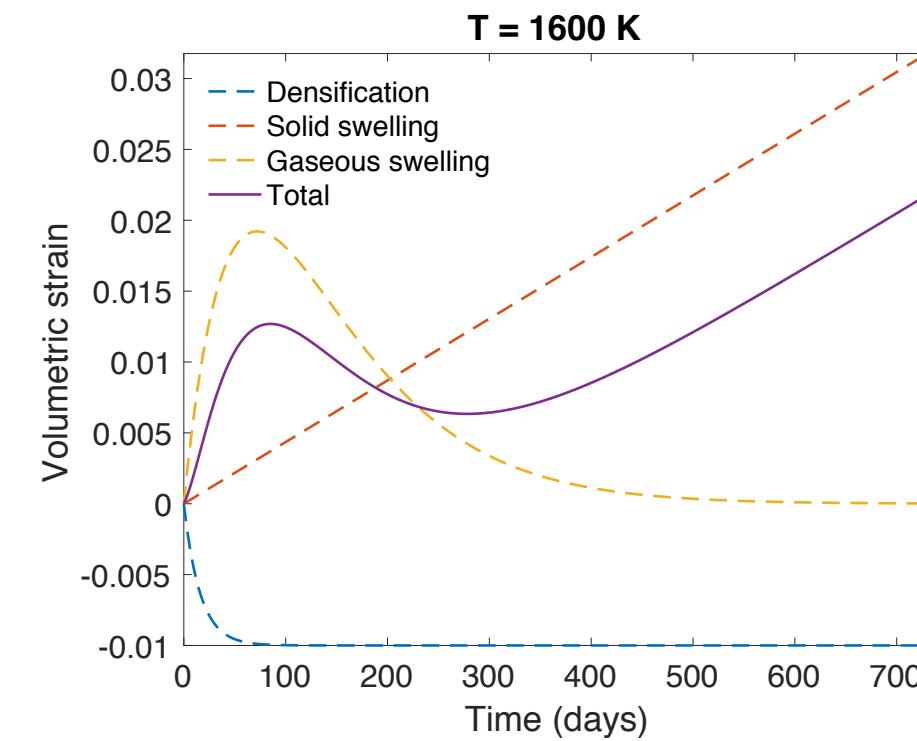
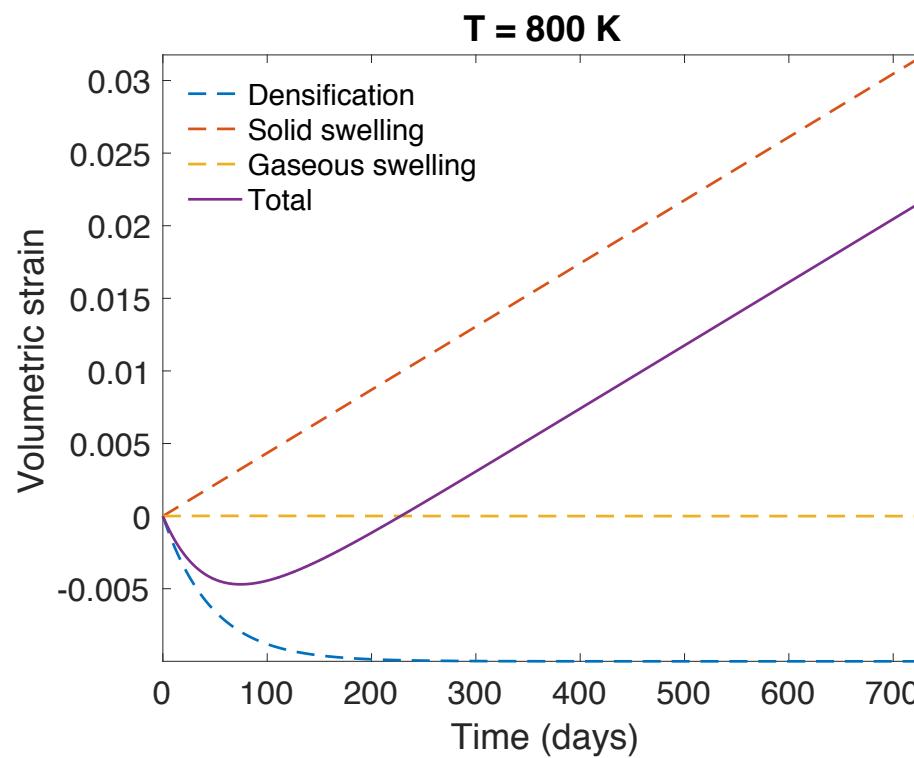
$$\epsilon_{gfp} = 1.96 \times 10^{-28} \rho \beta (2800 - T)^{11.73} e^{-0.0162(2800-T)} e^{-17.8\rho\beta}$$

- $\epsilon_{gfp} = 1.96e-28 * 10.97 * 0.0012 * (2800 - 1400)^{11.73} * \exp(-0.0162 * (2800 - 1400)) * \exp(-17.8 * 10.97 * 0.0012) = 0.0023$

- Total:

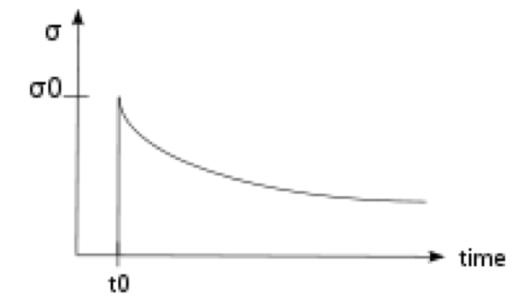
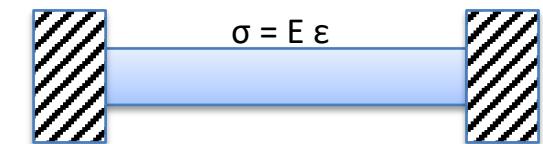
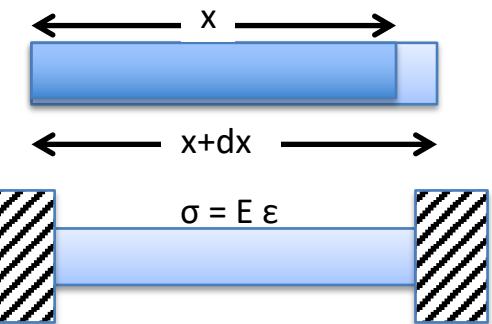
- $\epsilon_{tot} = \epsilon_{th} + \epsilon_D + \epsilon_{sfp} + \epsilon_{gfp} = 0.0121 - 0.0065 + 7.34e-4 + 0.0023 = 0.0086$

The overall swelling behavior depends on temperature



Creep

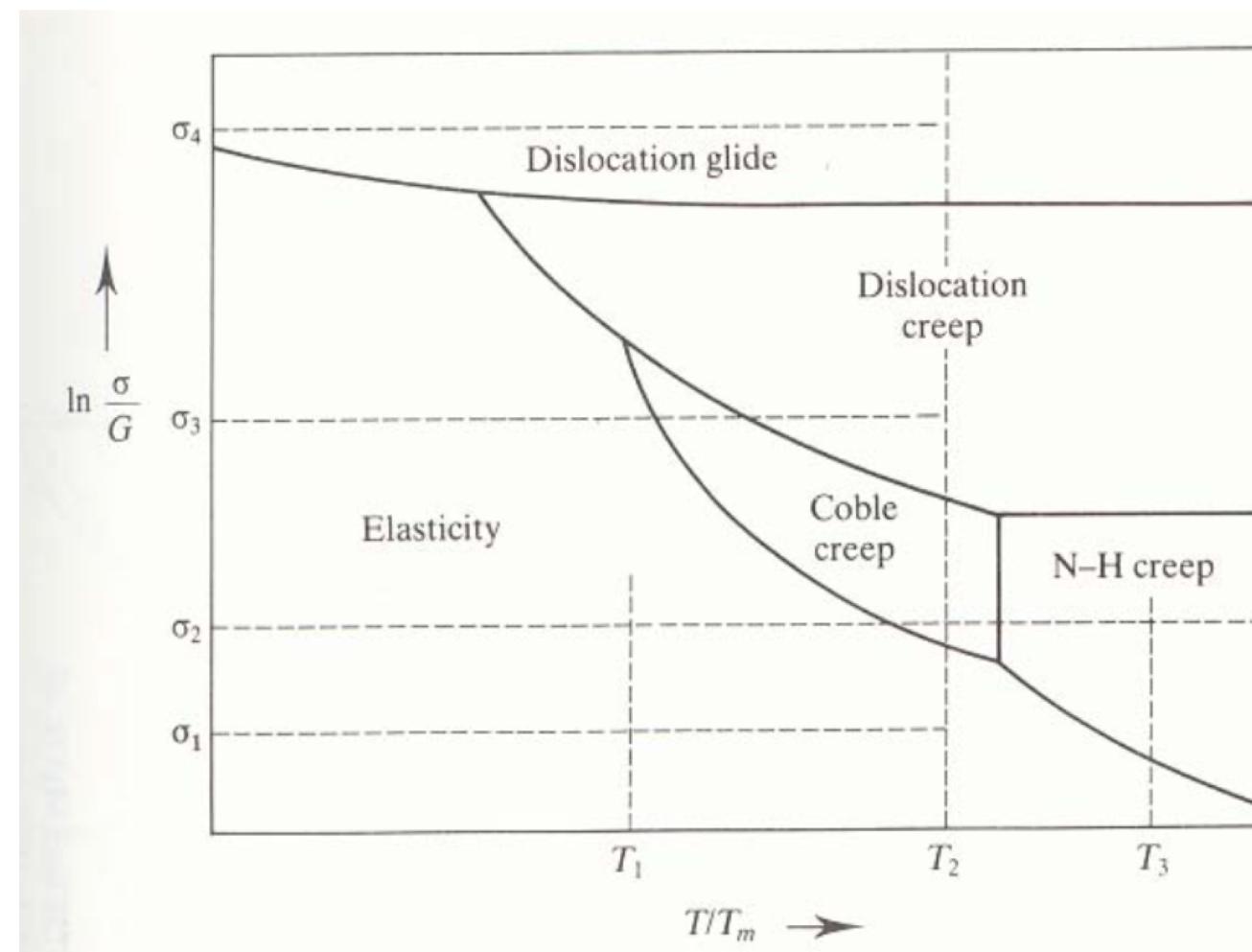
- Creep is a general mechanism for plastic deformation that occurs over time when $\sigma < \sigma_y$
- Consider a heated metal beam so it expands some distance dx
- We then fix it between two walls and let it cool down
- Because $\sigma < \sigma_y$, that stress remains constant
- In creep, defect diffusion is induced by the stress to cause permanent deformation and reduce the stress
- Therefore, creep
 - Occurs over time
 - Increases with increasing number of diffusing defects
 - High temperature (**thermal creep**)
 - Irradiation (**irradiation creep**)



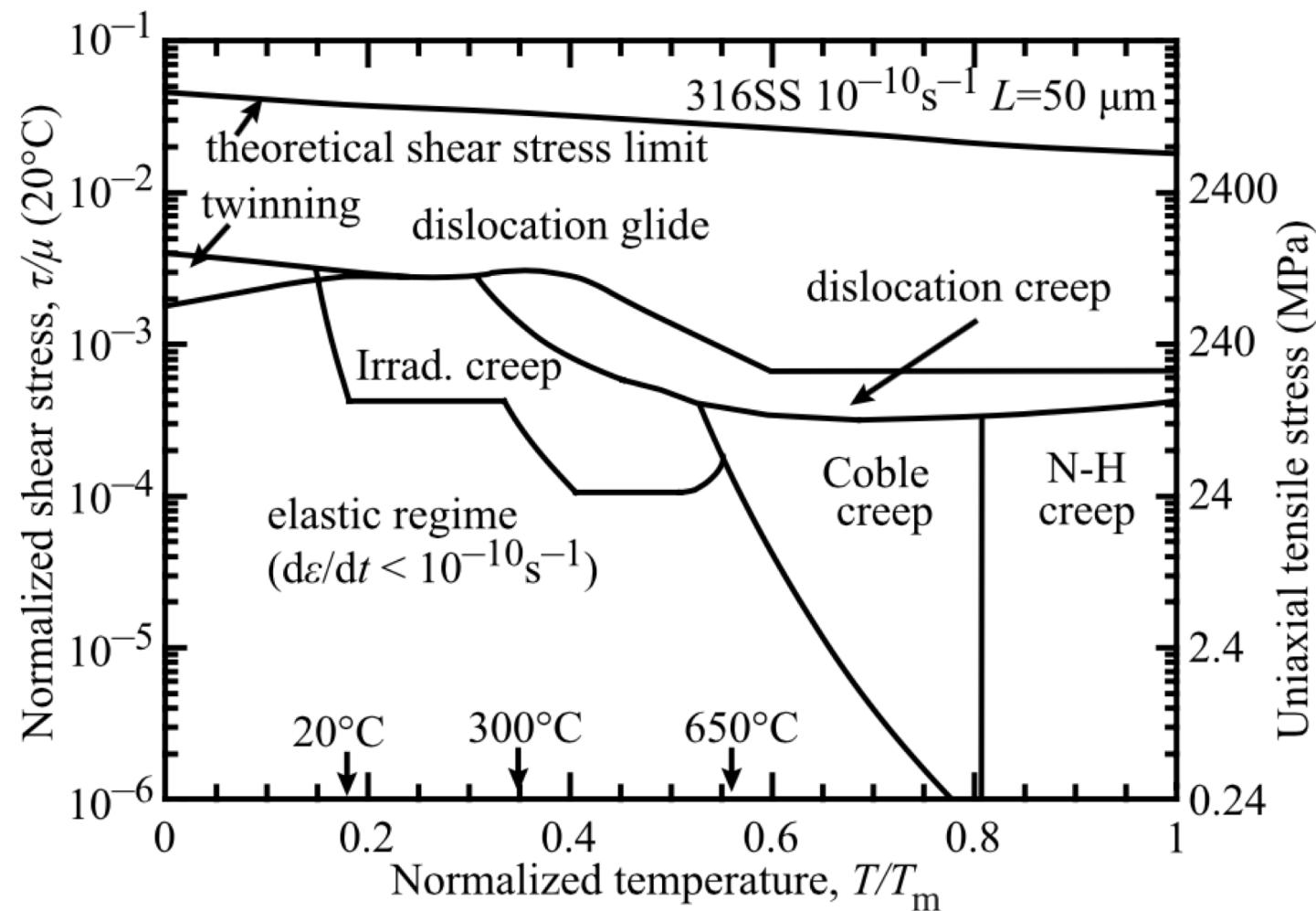
Creep

- General creep equation:
$$\dot{\epsilon} = \frac{C\sigma^m}{D_{gr}^b} e^{\frac{-Q}{k_b T}}$$
- Creep can be caused by various microstructural mechanisms
- Bulk Diffusion (Nabarro-Herring creep)
 - Atoms diffuse (high T), causing grains to elongate along the stress axis
 - $Q = Q(\text{self diffusion})$, $m = 1$, and $b = 2$
- Grain boundary diffusion (Coble creep)
 - Atoms diffuse along grain boundaries to elongate the grains along the stress axis
 - $Q = Q(\text{grain boundary diffusion})$, $m = 1$, and $b = 3$
- Dislocation creep
 - Dislocations glide under a high stress
 - Dislocations climb due to defects to avoid obstacles
 - $Q = Q(\text{self diffusion})$, $m = 4\text{--}6$, and $b = 0$

Different creep mechanisms are active for different combinations of stress and temperature



The behavior of creep changes in irradiated materials

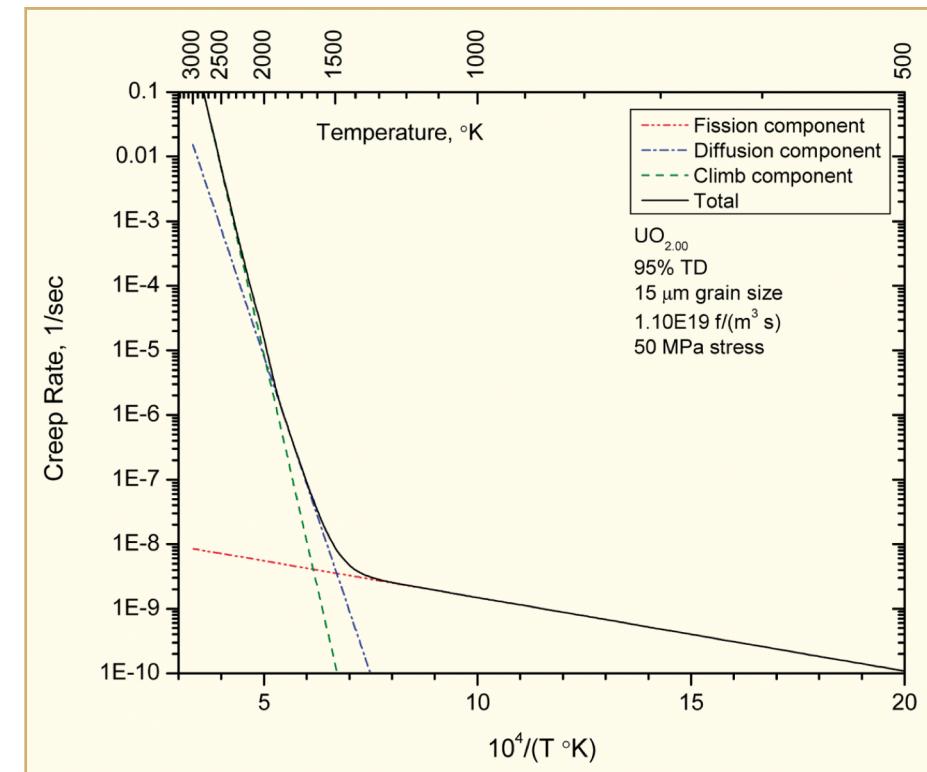


Irradiation and Creep

- Irradiation accelerates creep, causing it to be significant at lower temperatures
- Irradiation has little effect on diffusional creep, but it accelerates dislocation creep in cubic materials
- The dislocation creep rate can be written as $\dot{\varepsilon} = \rho_d^m b v_d$
 - ρ_d^m is the density of mobile dislocations
 - b is the burgers vector
 - v_d is the dislocation velocity
- Gliding dislocations quickly get pinned by obstacles
- As the dislocations absorb defects created by irradiation, they climb to different slip planes to avoid the obstacles
- More interstitials are absorbed than vacancies due to the higher sink strength for interstitials

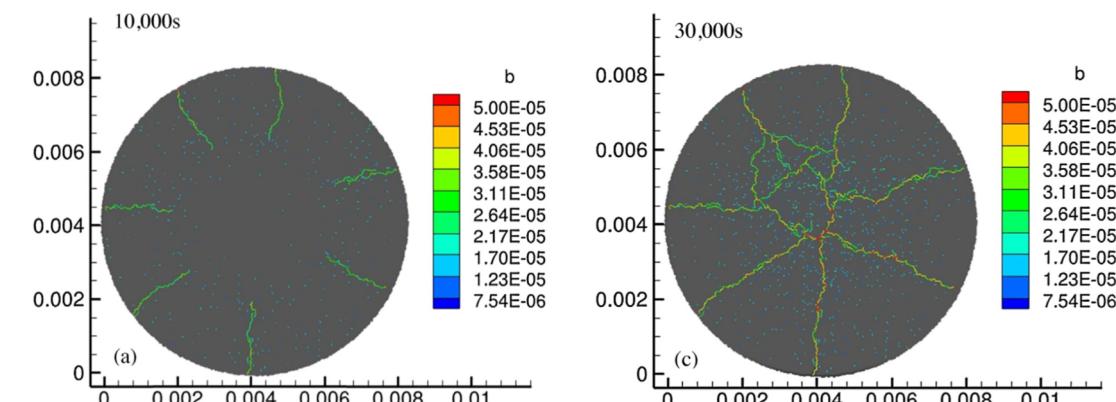
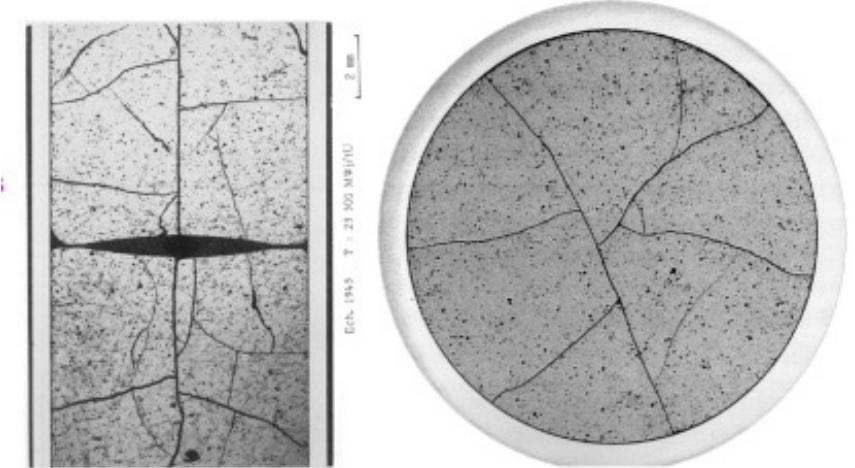
Fuel Creep

- Like other materials, the fuel also undergoes creep
- The fuel creep (In UO₂) is a combination of diffusion creep and irradiation creep
- It is expected that fuel creep plays a major role in dimensional change in metallic fuels, large via N-H creep, but still unproven experimentally and no good creep models exist for metallic fuels



Fracture

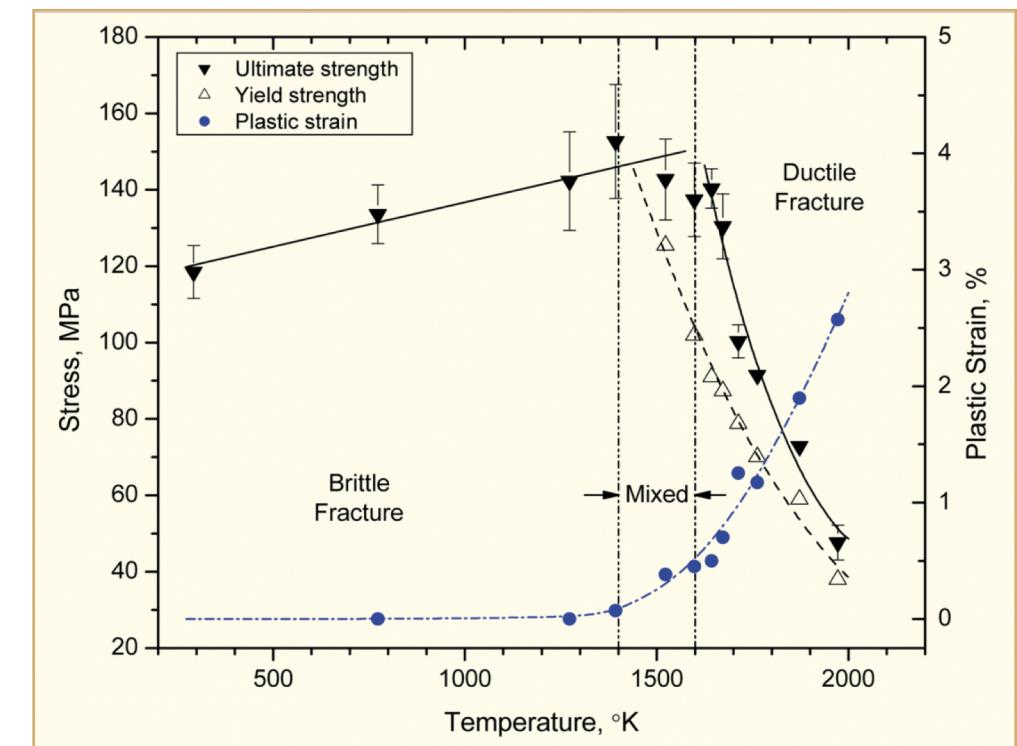
- UO_2 pellets fracture during changes in temperature due to large thermal stresses
- Fracture results in:
 - Increased gap reduction
 - Reduced thermal conductivity
 - Increased avenues for fission gas release
- Fracture has been typically modeled in two ways:
 - Empirical relocation model that is a function of burnup
 - Semi-empirical smeared cracking model
- Modern methods provide means of modeling discrete cracks



- Radial cracks partially penetrate the pellet during temperature increase
- Full cracking occurs when the temperature decreases

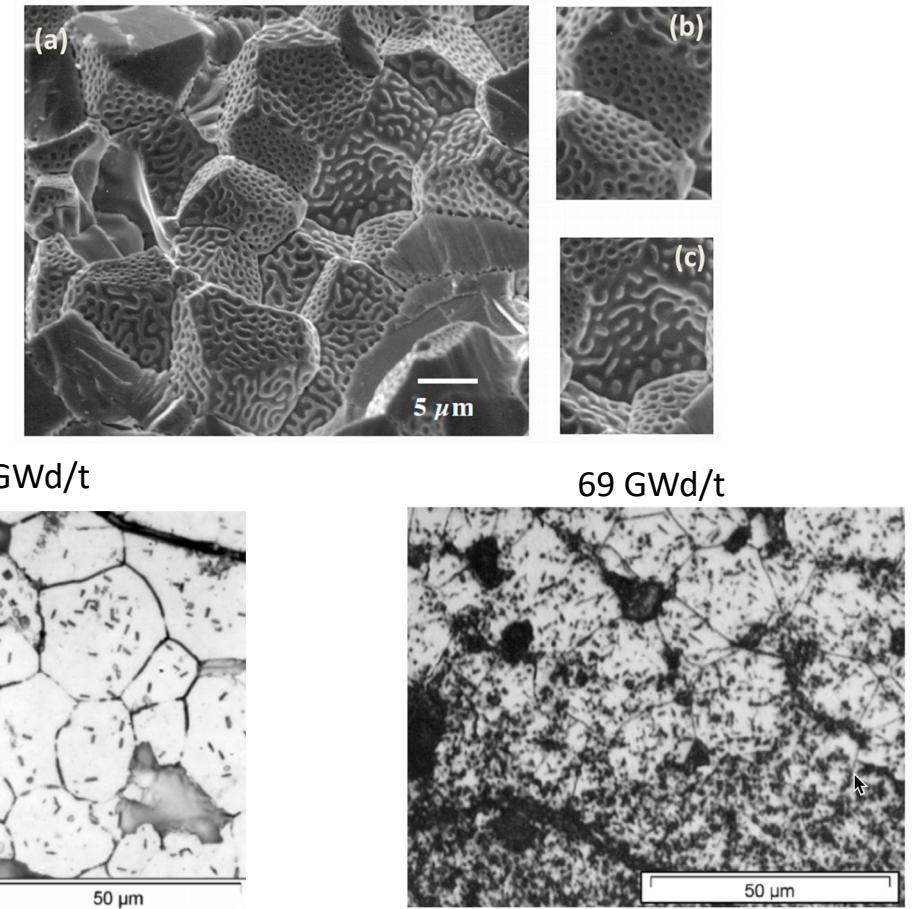
Fracture

- The fracture behavior of the fuel is fairly complicated
- Fracture strength varies with grain size (G)
 - $\sigma_{\text{frac}} = G^{-m} \sigma_{\text{frac, ref}}$, $m = 0.04 - 0.05$ (vs. $m \sim 0.5$ for metal)
 - Increasing grain size from $10 \mu\text{m}$ to $100 \mu\text{m}$ reduces σ_{frac} by $\sim 10\%$
- Ductility transition temperature is lower in-reactor than in thermal tests
- Fracture strength is $\sim 10 \times$ higher in compression than in tension
- Load-deformation behavior strongly affected by creep under in-reactor conditions



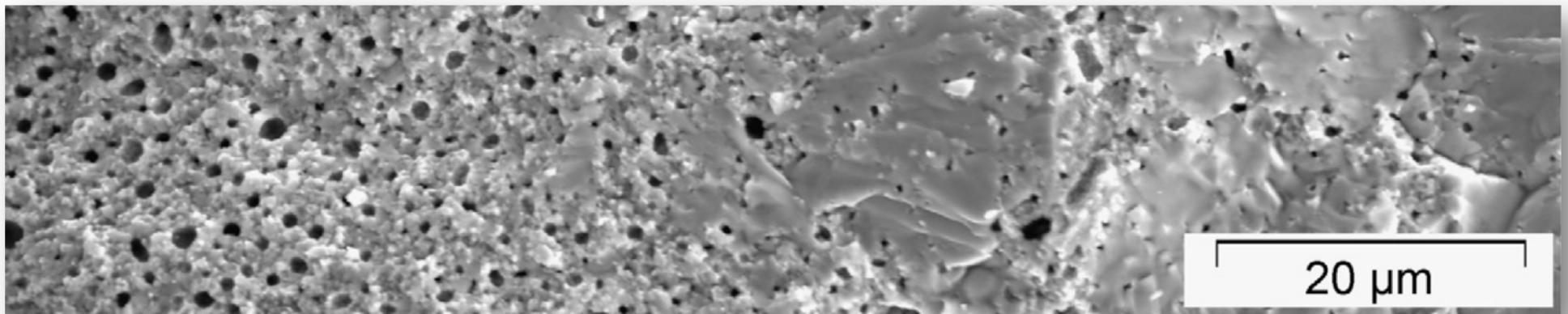
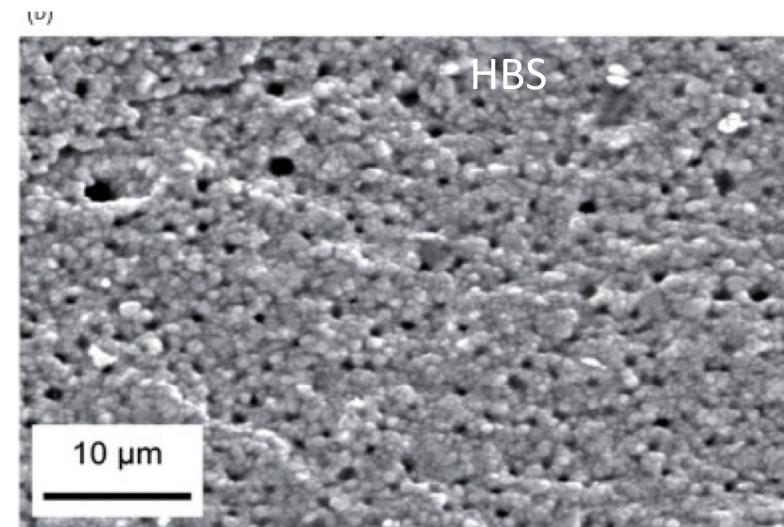
High Burnup Structure

- At the hottest regions of the fuel, defects and fission products cluster or segregate to interfaces
- In the cool regions of the fuel, the diffusion is too slow for defects to arrive at the interfaces



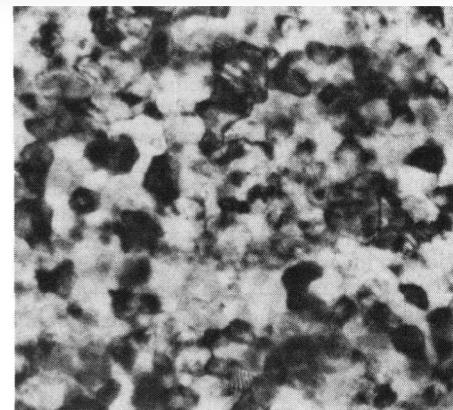
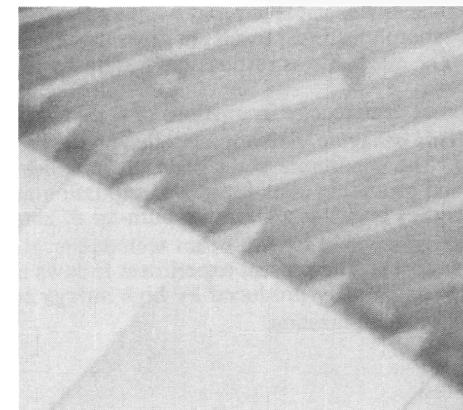
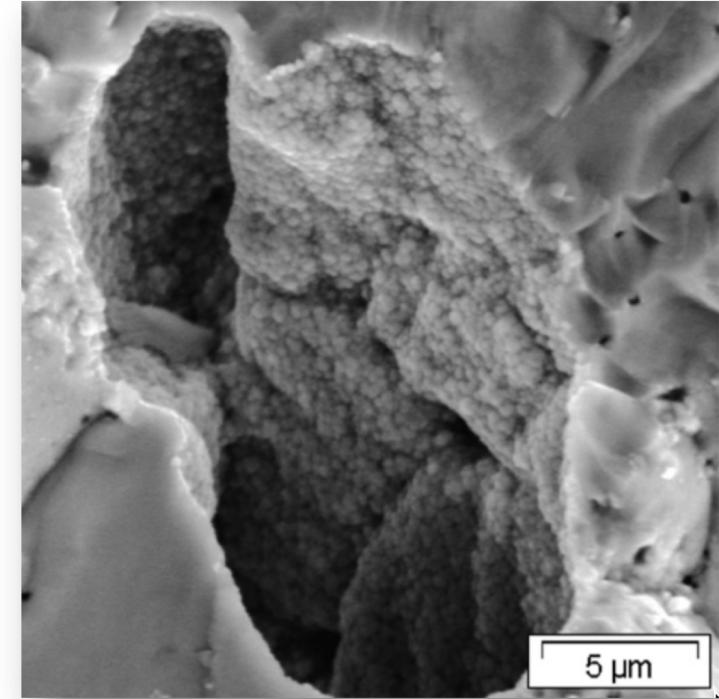
High Burnup Structure

- In order to annihilate the defects, the structure changes to have small grains and many larger pores
- This is referred to as the high burnup structure (HBS), sometimes called the rim structure



High Burnup Structure

- The mechanism for the formation of HBS is still up for debate
- One theory is that dislocation networks cause grain subdivision
- Another is that dislocation networks cause polygonization
- In UO_2 , there appears to be a burnup and temperature threshold for this restructuring
- The formation of high burnup structure is not unique to UO_2 , but occurs in all fuel types at high burnup and lower temperature

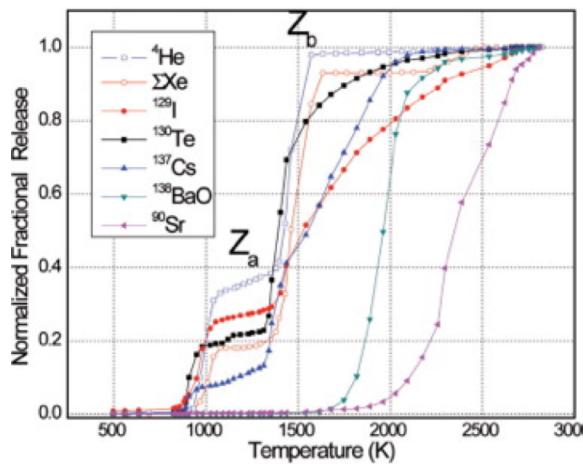


Grain subdivision in U_3Si_2 under ion irradiation

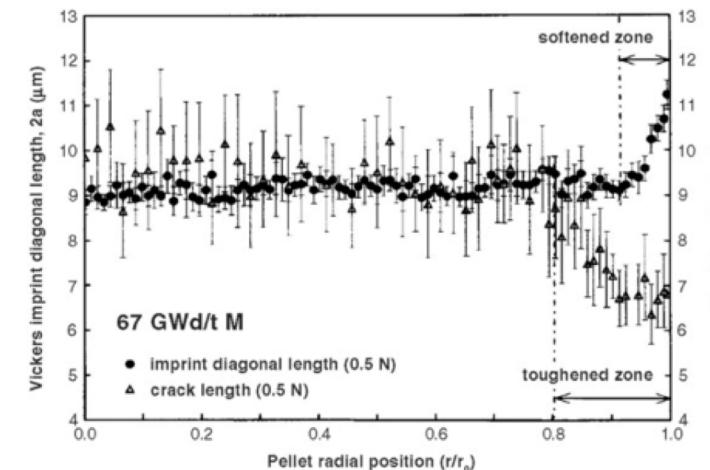
High Burnup Structure

- Originally it was assumed that HBS hurt fuel performance, but recent research shows it has a positive effect

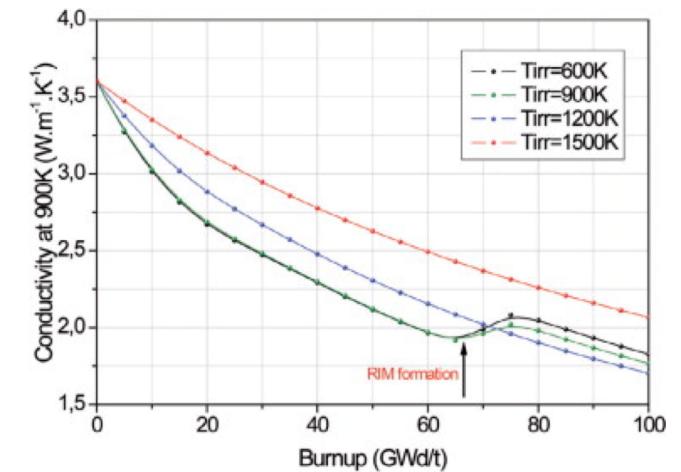
Efficiently retains fission gas



Increased toughness and softness



Increased thermal conductivity



Summary

- Many materials models for fuel are empirical and correlated to burnup
- Fuel pellets change shape due to
 - Thermal expansion (increase in volume)
 - Densification (decrease in volume)
 - Swelling (increase in volume)
 - Creep (volume stays the same)
- Fracture also decreases the gap, as fractures pieces shift outward
- At high burnup but mid to low temperature the fuel restructures to have a small grain size and large bubbles
 - The structure is called High Burnup Structures (HBS)
 - HBS may actually improve many fuel properties