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- ① Engineering: $\sigma = F/A_0$, $\epsilon = (l - l_0)/l_0 \rightarrow$ calculated with \checkmark representative length (initial area)
- True: $\sigma = F/A$; $\epsilon = - \int_{l_0}^l \frac{dl}{l} \ln\left(\frac{l}{l_0}\right) \rightarrow$ calculated with \checkmark actual area (varying with time)

- ② Elastic deformation is the bond stretching and is not permanent. Plastic deformation is permanent (non-reversible) and caused by deformation in the crystal lattice (slip, twinning)

- ③ 0D defect: point defect: vacancies, interstitial atoms \checkmark
- 3D defect: cluster of point defects: precipitates (cluster of impurity atoms) \checkmark

- ④ - Melting temperature \checkmark
- Thermal conductivity \checkmark
- Chemical reactions at inner cladding surface \checkmark

- ⑤ - Fission gas release: grain size changes space available within fuel for fission gas \checkmark
- swelling (same)
- Thermal conductivity (depending on grain size) \checkmark
- not mechanical properties
- but yes grain size affects these properties/phenomena

- ⑥ strain hardening is the increase in the yield strain caused by permanent strain in plastic deformation (cause) \checkmark
- dislocation pileup, etc.

- ⑦ ① Full centerline temperature, ② stress in the cladding, ③ consider gap pressure, closure and heat transfer in some way
- temp. profile, not just centerline \checkmark

⑧ The change in free energy from decrease in surface area of pores and lowering of the surface energy. $\frac{3}{3}$

⑨ Reduction of grain boundary energy is the most driving force to grain growth, but also T gradients among others. Grain growth is inhibited by pores, precipitations, solute atoms, etc. (impurities) $\frac{6}{6}$

⑩ $p = 20 \text{ MPa}$ $\bar{R} = 5.4 \text{ mm} = 0.54 \text{ cm}$ $t_c = 0.8 \text{ mm} = 0.08 \text{ cm}$

$$\bar{R} = R_i + t_c/2 \Rightarrow R_i = 0.54 - 0.04 = 0.5 \text{ cm}$$

$$R_o = R_i + t_c = 0.58 \text{ cm}$$

a) $\sigma_\theta = \frac{p \bar{R}}{\delta} = \frac{20 (0.54)}{0.08} = 142.5 \text{ MPa}$

$\sigma_\phi = \frac{p \bar{R}}{2\delta} = \frac{\sigma_\theta}{2} = 71.25 \text{ MPa}$

$\sigma_r = -\frac{1}{2}p = -10 \text{ MPa}$

Equation correct, but some calculator error

b) at mid point, $\lambda = \bar{R} = 0.54 \text{ cm}$ $\frac{R_o}{R} = 1.07$, $\frac{R_o}{R_i} = 1.16$

$\sigma_\theta(\lambda) = p \frac{(R_o/\lambda)^2 + 1}{(R_o/R_i)^2 - 1} \Rightarrow \sigma_\theta(\bar{R}) = 20 \frac{(1.07)^2 + 1}{(1.16)^2 - 1} = 124.13 \text{ MPa} \checkmark$

$\sigma_\phi(\lambda) = \frac{p}{(R_o/R_i)^2 - 1} \Rightarrow \sigma_\phi(\bar{R}) = \frac{20}{(1.16)^2 - 1} = 57.87 \text{ MPa} \checkmark$

$\sigma_r(\lambda) = -p \frac{(R_o/\lambda)^2 - 1}{(R_o/R_i)^2 - 1} \Rightarrow \sigma_r(\bar{R}) = -20 \frac{(1.07)^2 - 1}{(1.16)^2 - 1} = -8.27 \text{ MPa} \checkmark$

c) The stress in the inside of the wall is $-p$ and on the outside is zero $\frac{1}{4}$
- doesn't answer the question

(11) $R_f = 4.5 \text{ mm}$ $LHR = 250 \text{ W/cm}$ $K_f = 0.1 \text{ W/cmK}$ $E = 290 \text{ GPa}$ $\nu = 0.3$
 $\alpha = 8.2 \times 10^{-6} / \text{K}$

$$T_o - T_s = \frac{LHR}{4\pi K_f} = \frac{250}{4\pi (0.1)} = 198.94 \text{ K} \checkmark$$

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maximum is σ_θ @ $r = R_f$; $r/l = 1$

$$\sigma^* = \frac{\alpha E (T_o - T_s)}{4(1-\nu)} = \frac{(8.2 \times 10^{-6})(290 \times 10^3)(198.94)}{4(1-0.3)} = 168.96 \text{ MPa}$$

$$\sigma_\theta = -168.96(1 - 3(1)^2) = \boxed{337.92 \text{ MPa}} \checkmark$$

(12) $T_{gap} = T_{ci} = 450 \text{ K}$ (assuming)

$$T_F = T_{gap} + \frac{LHR \cdot l_{gap}}{2\pi R_f K_{gap}} = 450 + \frac{(325)(0.02)}{2\pi(0.5)(0.04)} = 501.73 \text{ K}$$

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$$T_o = T_F + \frac{LHR}{4\pi K_f} = 501.73 + \frac{325}{4\pi(0.05)} = 1018.98 \text{ K} \checkmark \text{ (before)}$$

$$\bar{R}_c = 0.5 + 0.02 = 0.052 \text{ cm} \checkmark$$

$$\bar{T}_c = 501.73 \text{ K} \rightarrow \text{should be } T_{ci} = 450 \text{ K}$$

$$\bar{T}_f = (1018.98 + 501.73)/2 = 760.36 \text{ K} \checkmark$$

$$\Delta \varepsilon_{gap} = (0.052)(4.5 \times 10^{-6})(501.73 - 300) - (0.5)(4.5 \times 10^{-6})(760.36 - 300)$$

$$\Delta \varepsilon_{gap} = -0.0034 \text{ cm} \checkmark$$

$$l_{g2} = 0.02 - 0.0034 = 0.0166 \text{ cm}$$

$$T_{F2} = 450 + \frac{(325)(0.0166)}{2\pi(0.5)(0.04)} = 492.93 \text{ K} \checkmark$$

$$T_{o2} = 492.93 + \frac{325}{4\pi(0.05)} = 1010.18 \text{ K (after)}$$

$$(13) \sigma^* = \frac{\alpha E (T_0 - T_s)}{4(1-\nu)} = \frac{(10.5 \times 10^{-6})(810 \times 10^3)(100/4\pi(0.05))}{4(1-0.25)} = 233.96 \text{ MPa}$$

$$\sigma_e = -\sigma^*(1 - 3\eta^2) = \sigma_{fr} \quad \checkmark$$

$$-\frac{120}{233.96} = 1 - 3\eta^2 \Rightarrow \eta = 0.71 = \frac{\lambda}{R_f} \quad \checkmark$$

$$\boxed{\lambda = 0.39 \text{ cm}}$$

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