

# Ab Initio Molecular Dynamics Simulations of temperature dependent properties in $\text{UCl}_3$ , $\text{NaCl}$ , and $\text{UCl}_3\text{-NaCl}$ molten salts

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## Abstract

Ab Initio Molecular Dynamics (AIMD) simulations are used to calculate temperature dependent thermodynamic, kinetic and thermo-physical properties in  $\text{UCl}_3$ ,  $\text{NaCl}$  and  $\text{UCl}_3\text{-NaCl}$  mixtures, in order to inform models of molten salt reactor (MSR) performance. Following established approaches, the AIMD simulations include van der Waals interactions and use either the PBE or XX exchange-correlation potentials. Moreover, the impact of adding a Hubbard  $U$  model for the U 5f electrons to ensure that the molten salt is predicted to be an electronic insulator is investigated. The so-called Langreth & Lundqvist, DFT-D3 and dDsC dispersion models are tested for molten  $\text{NaCl}$  in order to assess the accuracy for density and heat capacity predictions. Both constant pressure and constant volume ensembles were used for the simulations. All methods predict densities within XX% of the experimental data, with the dDsC and Langreth & Lundqvist methods being within a few per cent. Based on these results, the Langreth & Lundqvist and dDsC methods are extended to the  $\text{UCl}_3$  system with a few select simulations performed for the DFT-D3 model. The Langreth & Lundqvist methodology is quite sensitive to the form of the exchange correlation potential used. The optimal choice predicts densities within a few per cent of the experimental data, while some others result in underestimation of the density. The dDsC method also predicts densities within a few per cent of the experimental data. The Hubbard  $U$  model increases the volume for all cases and results in slightly lower density than for the case where it is not included. Next, mixtures of  $\text{UCl}_3\text{-NaCl}$  are investigated at a fixed temperature of 1200 and 1250K. The density deviates by up to almost 3% from an ideal mixture close the eutectic composition, with the mixing energy exhibiting a maximum of -0.02 eV/atom at the same composition. Finally, the constant volume simulations allow determination of the compressibility and diffusivity, which are presented for select cases.

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## 1. Introduction

Molten salt reactors (MSRs) are among the advanced concepts pursued as a next generation nuclear energy technology [1]. However, the basic concept is not new and was first developed as part of the effort to power aircrafts with nuclear energy in the fifties [2]. Later in the sixties, Oak Ridge National Laboratory (ORNL) built and ran the Molten-Salt Reactor Experiment (MSRE) [3]. This reactor used a fluoride salt with uranium as fuel. Fluorides salts are still highly relevant and proposed in several designs. In addition, chloride salts are being considered for MSRs operating in the fast neutron spectrum [4].

Property data for both fluoride and chloride salts are in many cases limited, in particular for chlorides, and sometimes inaccurate or at least of un-

known accuracy, since many sources are from the 60s and 70s. This is especially true as actinides (U, Pu), impurities, corrosion and fission products are added. Using atomic scale simulations to fill this data gap and to provide mechanistic understanding aims at improving the availability of data and property models, which would facilitate more accurate evaluation of various concepts by reactor designers and other interested parties. Modeling and simulations have an important role to play, because the compositional space of interest is extensive and difficult to cover with experiments alone, especially as some of the salts are also highly toxic and radioactive. This benefit is already acknowledged in the literature [5]. Molecular dynamics simulations based on both classical potentials and Ab Initio Molecular Dynamics (AIMD) simulations have been used to study chloride salts involving actinides [6]. In

particular, Li et al. used AIMD simulations to study the local structure of  $\text{UCl}_3$ ,  $\text{UCl}_4$  and mixtures of  $\text{UCl}_3$ ,  $\text{UCl}_4$  and  $\text{NaCl}$  at 1173K. This study showed good agreement with experiments for the radial distribution function. In order to study temperature dependent thermo-physical properties, a semi-empirical potential was developed [1]. This potential successfully predicted density, thermal conductivity and viscosity [2]. Nam et al. studied the solution thermodynamics of dilute concentrations of  $\text{UCl}_3$  in a base salt [3] and investigated the properties of base salts for different van der Waals interaction models. In the present study, AIMD simulations utilizing different models for van der Waals interactions are used to predict temperature dependent thermo-physical, kinetic and thermochemical properties for  $\text{UCl}_3$ ,  $\text{NaCl}$ , and  $\text{UCl}_3$ - $\text{NaCl}$  directly from AIMD simulations. The standard exchange-correlation potentials typically used are extended to include the Hubbard  $U$  model for the actinide 5f electrons. The purpose of the study is to determine with what accuracy fundamental properties can be predicted with AIMD simulations based on the particular methodologies described above and to initiate populating some of the data gaps that exist in the literature.

The paper is organized as follows. The methodology is described in Sec. ??, followed by results and discussion in ???. First the benchmark for  $\text{NaCl}$  is presented, after which the  $\text{UCl}_3$  results are shown followed by  $\text{UCl}_3$ - $\text{NaCl}$  mixtures. The implications of our results are discussed in Sec. ??? and, finally, our conclusions are presented (???).

## 2. Methodology

The AIMD simulations were performed with the VASP code [4]. The simulations used a range of supercell sizes with the largest consisting of 216 ( $\text{NaCl}$ ), 216 ( $\text{UCl}_3$ ) and 134-184 ( $\text{NaCl}$ - $\text{UCl}_3$  mixtures) atoms. The smallest cells for the same systems have 64, 64 and 40-54 atoms. For  $\text{NaCl}$  and  $\text{UCl}_3$  these were either created by expansions of the crystalline unit cells followed by melting of the lattice by performing high temperature molecular dynamics runs, to be described later in this section, or by XXX. The mixed supercells were created by replacing U atoms with Na in the  $\text{UCl}_3$  supercell, and removing Cl atoms to match the desired composition. The differently sized supercells were investigated in order to understand the compromise between computational efficiency and ac-

curacy. The largest simulation cells properly capture the expected radial distribution function in the liquid state. The radial distribution function was confirmed to reach a value close to one for all cases studied. The smaller cells comprise some accuracy for computational efficiency as will be quantified in Sec. ???. All simulations used the  $\Gamma$  point for integration in reciprocal space. The accurate simulation setting was utilized in VASP, but the plane wave cut-off energy was increased above the standard setting to either 300 eV or 400 eV. Gaussian smearing with a smearing parameter of 0.05 eV was used for the partial occupancies of the wave functions. The convergence criteria for the electronic minimization was  $10^{-3}$  eV for  $\text{NaCl}$  and  $5 \times 10^{-3}$  eV for salts containing uranium.

The AIMD simulations used the Projector Augmented Wave (PAW) method to describe the core electrons [5]. For each element, the PAW potentials supplied with VASP for the PBE exchange-correlation potential were utilized. For Na, the version that only includes the s electron(s) in the valence shell was used, while Cl also included p electrons and U included the outer s, p and f electrons in the valence shell. For some of the van der Waals models, more advanced exchange-correlation potentials than PBE, such as XX, were used. For the uranium 5f electrons, an additional Hubbard  $U$  term was introduced in order to capture the effect of strong correlations. Calculations were also performed with the standard exchange-correlation potential (no Hubbard  $U$  model). The Lichtenstein approach [6] was used for the Hubbard  $U$  methodology and an approximate  $U$  value range of 3.0-4.5 eV was determined by using the constrained DFT linear-response method for crystalline  $\text{UCl}_3$  [7]. The  $J$  value was set to 0.51 eV. These values are similar to those proposed for  $\text{UO}_2$  [8]. After confirming that the values for  $\text{UCl}_3$  were close to those for  $\text{UO}_2$ , the latter values were adopted in the present study. Future work may consider further optimization of the Hubbard  $U$  (and  $J$ ) parameters, but the results and conclusions are not expected to change dramatically based on this choice, at least as long as the value is sufficiently large to ensure an insulating ground state. It should be noted that the effective  $U$  value depends on the coordination environment and consequently could differ between crystalline  $\text{UCl}_3$  and molten salts. It could also be a function of time in the simulations as the environment may change. Future work may consider these questions in more detail, but it is beyond the scope of the

present study. The effect of the Hubbard  $U$  parameter for molten uranium chloride salts is the same as for crystalline  $\text{UO}_2$ ; without the  $U$  parameter the salts are predicted to be metallic, which is contrary to the expected behavior, see Fig. ???. Even though useful results may certainly be obtained while ignoring the strong correlations captured by the Hubbard  $U$  parameter and accepting the resulting metallic character predicted for the salts, there are limitations to this approach. Uranium ions in its  $3+$  state have localized magnetic moments. Both ferro-magnetic and anti-ferromagnetic orderings were investigated. In the context of molten salts, the AFM option is similar to a random distribution with a total magnetic moment in the supercell close to zero. The anti-ferromagnetic ordering is energetically preferred and also results in better convergence behavior. It is consequently adopted in the present study.

It is well-established in the literature that van der Waals or dispersion interactions are critical for reproducing the density of molten salts by DFT methods [1]. Previous simulations have used both the DFT-D3 method [2] and the Langreth & Lundqvist [3] methodologies for various molten chloride salts. Both methods are used in the present study and for the Langreth & Lundqvist [3] methodology several exchange-correlation potentials were tested. In addition, the so-called dDsC method was also included in the set of van der Waals models. The dDsC method is not implemented for f elements in the standard VASP version. In order to enable simulations the corresponding parameters were taken from Ref. [4]. The supercells of molten salts were either created by melting the crystalline phases at high temperature for an expanded volume using an isochoric (NVT) thermostat with velocities scaled each time step or by XXX. The temperature used for melting the lattice was well above the experimental melting point. The temperature of the system was then slowly reduced to the simulation temperature of interest. These simulations were performed with lower accuracy settings than the equilibration and production runs described above. The melting procedure was only performed once for a specific temperature in the middle of the range of interest. Simulations for other temperatures were performed by decreasing or increasing the temperature from the initial molten reference structure created according to the procedure above.

The molecular dynamics simulations for the molten salt supercells were performed using both

isobaric conditions (NPT) and isochoric (NVT) conditions. The primary intent of the NPT simulations is to evaluate density, thermal expansion, heat capacity and mixing energy. The NVT simulations also allow calculation of the compressibility and species diffusion. The NPT simulations applied the Langevin thermostat and the NVT simulations the Nose-Hoover thermostat in VASP. For the NPT simulations, the temperature friction coefficients were set to  $10 \text{ ps}^{-1}$  and the friction coefficient for the lattice degrees of freedom to  $1 \text{ ps}^{-1}$ . The time step was set to 2 fs or lower for production runs at 1500 K or below, and 1 fs above this temperature. Pre-equilibrium runs were performed with a time-step of 5 fs. The pre-equilibration runs were performed for a minimum of 10 ps. Production runs were performed for a minimum of 10 ps for all systems, higher for NaCl and for the small supercells. The first 1-2 ps in the production runs were ignored in order to ensure that the results for the new time step was allowed to equilibrate. Obviously, longer runs would further improve statistics and would certainly be desired, but the convergence of thermo-physical and thermodynamic quantities was monitored and deemed to be sufficient for the present purpose.

All properties were calculated by averaging over the production run (not including the equilibration or pre-production time). Densities were trivially obtained from the supercell volume and heat capacities from the slope of the potential energy as function of temperature. Mixing enthalpies/energies were calculated from the potential energy of the mixed salt with pure NaCl and  $\text{UCl}_3$  at the same temperature as reference. The compressibility is calculated as the second derivative of the energy versus volume curve obtained from several NVT simulations. The diffusivities are calculated from the mean square displacements through the Einstein relation.

### 3. Results

#### 3.1. Benchmark of methodology for molten NaCl

Figure ?? plots the predicted density of molten NaCl as function of temperature for the DFT-D3, dDsC and Langreth & Lundqvist dispersion models as well as simulations without any dispersion interaction. A correlation derived from experimental data is also shown [5]. All simulations reproduce the temperature dependence of the density

obtained from experiments. However, as expected, only the simulations that account for dispersion interactions are within 10% of the experimental density correlation. The best agreement is obtained for the Langreth & Lundqvist and dDsC dispersion models, which are within 5% or less of the experimental correlation across an extended temperature range. The calculated (Langreth & Lundqvist and dDsC) and experimental correlation for the density as function of temperature are listed in Table ??.

Figure 1: Density of NaCl predicted with three different models for dispersion forces and one without. Experimental data is represented by the correlation plotted as an orange line []. Note that the temperature range of the experimental correlation and some data points extend beyond the boiling point of NaCl, which is solely for illustrative purposes. The lines shown are least-squares fits to the calculated data points.

Fig. ?? plots the potential energy per formula unit of molten NaCl as function of temperature. The derivative equals the heat capacity of NaCl, which is also tabulated in Table ?? together with an experimental reference value []. The simulation results indicate a constant heat capacity. The good agreement between simulations and experiments for the heat capacity further emphasizes the accuracy of the AIMD simulations.

Figure 2: Calculated potential energy of NaCl as function of temperature. The line is a least-squares fit to data points and the slope represents the heat capacity.

The results in Figs. ?? and ?? refers to simulations based on the large supercells. Fig. ?? compares these results with those obtained from the supercells. Density and heat capacity are both accurately represented by the smaller supercells, at least below 1750 K, which supports the accuracy of the results with respect to the supercell size. It

also suggests that at least for NaCl, the larger supercell is not required to achieve converged results for density and heat capacity at moderate temperature (below 1750 K). Some deviation is observed for the highest temperature, which may be related to approaching the boiling temperature.

Figure 3: a) Calculated density and b) potential energy of NaCl as function of temperature for the large and small supercells. The line is a least-squares fit to data points and the slope represents the heat capacity.

The NVE simulations also allow calculation of the compressibility and diffusivity of each species. These results are also summarized in Table ?? (compressibility) and Table ??.

### 3.2. AIMD simulations for $UCl_3$

Following the benchmark for NaCl, the next step is to apply the most accurate methodologies (Langreth & Lundqvist and dDsC) to  $UCl_3$  with a few spot checks using the other van der Waals models as well.

Figure ?? plots the predicted density for  $UCl_3$  as function of temperature for the Langreth & Lundqvist and dDsC dispersion models, with a few spot checks for other van der Waals models (DFT-D3), and compares the results to two literature correlations derived from experiments []. The two experimental correlations are surprisingly different and cannot both be valid, except in a narrow temperature range. Recently reported experimental data [] confirm the model due to XX et al. []. The most recent experimental data set agrees well with the simulation data, with both the Langreth & Lundqvist and dDsC model predicting values within a few per cent of the experimental data. The temperature dependence is predicted to be linear across the full temperature range investigated.

	Density (g/cm <sup>3</sup> )	Heat capacity (J/mol/K)	Compressibility ( )
NaCl Calculated (D3)			
NaCl Calculated (dDsC)			
NaCl Calculated (Langreth & Lundqvist)			
NaCl Experiment			
$UCl_3$ Calculated (Langreth & Lundqvist)			
$UCl_3$ Calculated (dDsC)			
$UCl_3$ Experiment			

Table 1: Calculated and experimental correlations for density, heat capacity and compressibility as function of temperature for NaCl and  $UCl_3$ . The first quantity is a linear function of temperature, while the latter two are constants.

The Langreth & Lundqvist methodology is sensitive to the choice of exchange -correlation potential. The optimal choice proved excellent agreement with experiments, while other choices may lead to significant underestimation of the density despite performing very well for the NaCl benchmark system. Note that only a single point was calculated for the DFT-D3 model, but that indicates essentially the same behavior as the dDsC model. Compared to the Desytniak correlation [1], the predicted temperature dependence of the density is slightly different. It agrees better with the more recent experimental data points [2]. The effect of including the Hubbard  $U$  model is to decrease the density (increase the volume) compared to the reference case, which follows the expected behavior extrapolated from uranium compounds such as  $\text{UO}_2$ . The densities in Figure ?? were fitted to linear correlations and summarized in Table ??.

Figure 4: Density of  $\text{UCl}_3$  predicted with different models for the dispersion forces and one without. Experimental data is represented by the correlations plotted as blue lines and XX. [1]. The lines are least-squares fits to the calculated data points, the equations of which are summarized in Table ??

Figure ?? plots the potential energy as function of temperature, from which the heat capacity can be derived by calculating the slope. We have not been able to identify experimental data on  $\text{UCl}_3$ , but our results compare very well with the value derived from the current CALPHAD  $\text{UCl}_3$  database (see Table ??) [1].

Figure 5: Calculated potential energy of  $\text{UCl}_3$  as function of temperature. The line is a least-squares fit to data points and the slope represents the heat capacity.

The results discussed so far for  $\text{UCl}_3$  were generated with the large supercells. These results are compared to those derived from the smaller supercells in Fig. ??, which, similar to NaCl, exhibits good agreement with each other. This provides confidence in the convergence of the current results.

As for NaCl, The NVE simulations also allow

Figure 6: Calculated density and potential energy of  $\text{UCl}_3$  as function of temperature for the large and small supercells. The line is a least-squares fit to data points and the slope represents the heat capacity.

calculation of the compressibility and diffusivity of each species. These results are summarized in Table ?? (compressibility) and Table ??.

### 3.3. AIMD simulations for $\text{NaCl-UCl}_3$

The density of  $\text{NaCl-UCl}_3$  mixtures were calculated for the Langreth & Lundqvist and dDsC dispersion models at 1200K and 1250K, as shown in Figure ???. This figure also shows experimental results from Desyatnik et al. [1] and lines corresponding to an ideal mixture of the end members. The insets highlight the deviation from ideal solution behavior. The simulation data points are within a few per cent of the experimental data and close to the ideal mixture. Both simulations and experiments suggest a negative deviation from an ideal solution (lower density than predicted by an ideal solution behavior). Although there is some spread in the data points that we ascribe to sampling uncertainties, there is a minimum about 3% below the ideal solution density close to the eutectic composition. The experimental data also shows a negative deviation, including a minimum close to the eutectic composition.

Figure 7: a) Density of  $\text{NaCl-UCl}_3$  mixtures as obtained from simulations and experimental data [1] at 1250K. The lines represent an ideal solution with the calculated and experimental NaCl and  $\text{UCl}_3$  densities as end points. The deviation from ideal solution behavior is highlighted in the inset. b) Same as a) but performed using a different simulation methodology at 1200 K. Results for both the large and small supercells are shown.

The total energies of the  $\text{NaCl-UCl}_3$  mixtures at 1250 K and 1200 K are plotted in Figure ??, with the NaCl and  $\text{UCl}_3$  end members as reference points, which confirms the close to ideal mixture behavior already observed for the densities. As for

	Na ( $\text{m}^2/\text{s}$ )	Cl ( $\text{m}^2/\text{s}$ )	U ( $\text{m}^2/\text{s}$ )
Diffusivity NaCl			
Diffusivity $\text{UCl}_3$			
Diffusivity $\text{NaCl-UCl}_3$			

Table 2: Calculated diffusivities for each species in NaCl,  $\text{UCl}_3$  and  $\text{NaCl-UCl}_3$ .

the density, a minimum is observed close to the eutectic composition.

Although the simulations were run long enough to sample the configuration space, it is possible that the initial distribution of Na and U ions have some impact on the results, especially for the large supercells. In order to test this possibility, a few of the Na and Cl atoms in the previous simulations were swapped and the simulations were re-run. In particular we target the compositions that seemed to deviate from the overall trend somewhat. Indeed, the new simulations provided slightly different results in closer agreement with the trends already discussed. For the large cells, this is an inherent uncertainty of the simulation approach.

Figure 8: a) Mixing energies for NaCl- $\text{UCl}_3$  mixtures at 1250 K. Pure NaCl and  $\text{UCl}_3$  are used as references. The solid black line represents the zero-mixing energy for the ideal solution. b) Same as a) but performed using a different simulation methodology at 1200 K. Results for both the large and small supercells are shown.

The comparison between large and small supercells for the density and mixing energy are also shown in Figs. ?? and ?. Unlike the cases of NaCl and  $\text{UCl}_3$ , the NaCl- $\text{UCl}_3$  mixture exhibit some deviation between the supercells for one of the compositions, although the trends are still the same.

#### 4. Discussion

#### 5. Conclusions

#### 6. Acknowledgments