

# PROJECT TITLE

— FINAL PROJECT —

*Your Name*

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## Abstract

Your abstract goes here. This should be a brief summary of your project, outlining the problem and addressed and key findings. (3 - 5 sentences)

## 1 Introduction

You may want to cite [Carnap \(1947\)](#), or include the page number where [Prior \(1967, p. 7\)](#) credits [Mctaggart's \(1908\)](#) (passive) argument that time is unreal, but only if relevant.

## 2 Using Formal Notation

This is similar to the problem sets. For instance,  $\Box\varphi \rightarrow \varphi$  is the T axiom. Use the appropriate commands defined in `notation.sty` such as  $\mathcal{K}$ , or define new commands as convenient. In tense logic, we use  $\Diamond$  for “it was the case that” and  $\Diamond$  for “it is going to be the case that”. And so on.

## 3 Using Theorem Environments

**Definition 3.1** (Kripke Frame) A *Kripke frame* is a pair  $\mathcal{F} = \langle \mathbb{W}, R \rangle$  where:

- (1)  $\mathbb{W}$  is a non-empty set of possible worlds
- (2)  $R \subseteq \mathbb{W} \times \mathbb{W}$  is an accessibility relation on  $\mathbb{W}$

As we can see in [Definition 3.1](#), a Kripke frame consists of two components.

**Lemma 3.1** A well-formed formula  $\varphi$  is a theorem of  $\mathcal{K}$  iff ...

*Proof.* This is a proof of a lemma. □

[Lemma 3.1](#) establishes an important cornerstone of...

**Theorem 3.1** (Optional Name) For any modal system  $\mathcal{K}$ , if  $\varphi$  is a theorem, then  $\Box\varphi$  is also a theorem.

*Proof.* We know by [Lemma 3.1](#)... □

As shown in [Theorem 3.1](#), the necessitation rule is fundamental to normal modal systems.

**Corollary 3.1** In the modal system  $\mathcal{S5}$ , if  $\Diamond\varphi$  is true at some world, then ...

**Rule 3.1** (Some Inference) From  $\varphi$  and  $\varphi \rightarrow \psi$ , we may infer  $\psi$ .

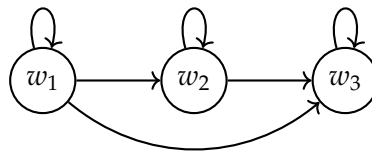
- |    |                   |  |
|----|-------------------|--|
| 1. | $p \wedge q$      | <b>Premise</b>                         |
| 2. | $p \rightarrow r$ | <b>Premise</b>                         |
| 3. | $p$               | <b><math>\wedge</math>-Elimination</b> |
| 4. | $r$               | <b>Modus Ponens</b>                    |

## 4 Modal Logic Diagrams

System T: Reflexive Accessibility



Figure 1: A model with a single reflexive world, characteristic of System T.



System S4: Reflexive and Transitive Accessibility

Figure 2: A model with transitive accessibility relation, characteristic of System S4.

As shown in [Figure 3](#), System S5 can be represented as a fully connected graph where each world is accessible from every other world.

### System S5: Equivalence Relation

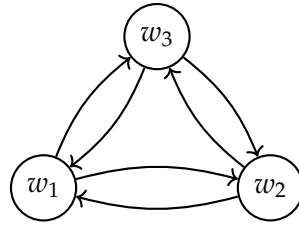
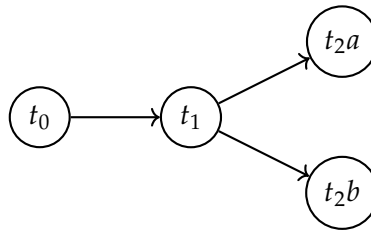


Figure 3: A model where all worlds access each other, characteristic of System S5.



Branching Time Model

Figure 4: A branching time model with a single past and multiple possible futures.

## References

- Carnap, Rudolf. 1947. *Meaning and Necessity*. University of Chicago Press.
- McTaggart, J. Ellis. 1908. "The Unreality of Time." *Mind* XVII:457–474. ISSN 0026-4423, 1460-2113. doi: 10.1093/mind/XVII.4.457.
- Prior, Arthur N. 1967. *Past, Present and Future*. Oxford, New York: Oxford University Press. ISBN 978-0-19-824311-3.