

Performance analysis of a parallel PDEVS simulator handling both conservative and optimistic protocols

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ABSTRACT

With the ever increasing complexity of simulation models, parallel simulation becomes necessary to perform the simulation within reasonable time bounds. The built-in parallelism of Parallel DEVS is often insufficient to tackle this problem on its own. Several synchronization algorithms have been proposed, each with a specific kind of simulation model in mind. Due to the significant differences between these algorithms, current Parallel DEVS simulation tools restrict themselves to only one such algorithm. In this paper, we present a Parallel DEVS simulator, grafted on C++11, which offers both conservative and optimistic simulation. We evaluate the performance gain that can be obtained by choosing the most appropriate synchronization protocol. Our implementation is compared to adevs using hardware-level profiling on a spectrum of benchmarks.

1. INTRODUCTION

DEVS [19] is a popular formalism for modelling complex dynamic systems using a discrete-event abstraction. In fact, it can serve as a simulation “assembly language” to which models in other formalisms can be mapped [18]. A number of tools have been constructed by academia and industry that allow the modelling and simulation of DEVS models.

With the ever increasing complexity of simulation models, parallel simulation becomes necessary to perform the simulation within reasonable time bounds. And while Parallel DEVS [4] was introduced to increase parallelism, this is often still insufficient. Several synchronization algorithms from the discrete event simulation community [8] have been applied to DEVS simulation in particular. While several parallel DEVS simulation kernels exist, they often restrict themselves to a single synchronization protocol. This is a logical choice, as these synchronization protocols have nearly no commonalities. But the exact reason for different synchronization protocols, is that their distinct nature makes them very applicable to specific situations. As such, current DEVS simulation ker-

nels always allow parallel simulation, but good performance can only be expected from some models.

Users that wish to simulate a set of distinct models, with different synchronization protocols, are therefore out of luck: Either they accept the lower performance for some of the models, or they use two distinct simulation kernels. Neither of these options is acceptable for the simulation of complex models, as the performance can become arbitrary worse, and the simulation kernels can diverge significantly.

In this paper, we introduce DEVS-Ex-Machina (“dxex”), our simulation tool which offers multiple synchronization protocols: no synchronization (sequential execution), conservative synchronization, or optimistic synchronization. The selected synchronization protocol is transparent to the simulated model. Users should merely determine, at the start of simulation, which protocol they wish to use. Our tool is implemented in C++11, to increase both performance and portability across different platforms.

A simple model is used to prove that the ideal synchronization algorithm is indeed dependent on model details. In our case, a single parameter of the model can have a significant impact on simulation performance, and especially on which is the ideal synchronization protocol. In order to show that this flexibility does not counter our performance, we compare our tool to Adevs, currently one of the fastest DEVS simulation tools available [17, 6].

We introduce the necessary background for this paper in Section 2. Section 3 elaborates on our features and design. In Section 4, we evaluate performance of our tool by comparing its different synchronization protocols. Related work is discussed in Section 5. Section 6 concludes the paper and gives future work.

2. BACKGROUND

This section briefly introduces two distinct synchronization protocols, as used by dxex. Furthermore, we make note of several new features of C++11.

2.1 Conservative Synchronization

The first synchronization protocol that we will introduce, is *conservative synchronization* [8]. In conservative synchronization, a node is allowed to progress in simulated time, in-

dependent of all other nodes, up to the point where it can guarantee that no causality errors can happen. When this point in time is reached, the node has to block until it is allowed to progress any further. In practice, this means that all nodes need to be aware of the current simulation time of all other nodes, and the time it takes an event to propagate (called *lookahead*). Several algorithms are defined in the literature to implement this behaviour. An overview is given in [8].

Deadlock can occur when a dependency cycle occurs and the amount of exchanged messages is low. Multiple algorithms are defined to handle this situation, such as deadlock avoidance and deadlock recovery.

The main advantage of conservative synchronization is that it has a low overhead if high parallelism exists between nodes. Each node can simulate in parallel, while sporadically notifying other nodes that they can progress even further. The disadvantage, however, is that the amount of parallelism is explicitly limited by the size of the lookahead. If a node can influence another (almost) instantaneously, no matter how rarely it occurs, the amount of parallelism is severely reduced. It is also up to the user to define the size of the lookahead, depending on how the model is known to behave. Slight changes in model behaviour can cause significant changes to the lookahead, and can therefore also have a significant influence on simulation performance.

2.2 Optimistic Synchronization

A completely different synchronization protocol is *optimistic synchronization* [12]. Whereas conservative synchronization would prevent causality errors at all costs, optimistic synchronization will allow them to happen, but correct them afterwards. Each node is allowed to progress in simulated time as much as possible, without taking note of the state of any other node. When an event arrives at a node, which is already further in simulated time, the node will have to roll back its state to right before the event would normally have to be processed. As the simulation time is now rolled back to before the event is processed, the event can simply be processed as if no causality error ever occurred.

Rolling back the simulation time requires the node to store past model states, such that they can be restored later on. Furthermore, all incoming and outgoing events need to be stored as well. Incoming events need to be passed to the models again, when the correct simulation time has again been reached, and outgoing events need to be cancelled, as potentially a different series of output events would normally have been generated. Cancelling events, however, can cause further rollbacks, as the receiving node might also have to roll back its state. In practice, a single causality error could have significant repercussions on the complete simulation.

Further changes are required for unrecoverable operations, such as I/O (*e.g.*, tracing, writing to file, printing output) and memory management. Lightweight algorithms are still required to determine the lower bound of all simulation times, through the computation of a *Global Virtual Time* (GVT).

The main advantage is that performance is not limited by a small lookahead, caused by a very infrequent event. If

an (almost) instantaneous event occurs rarely, performance will only be impacted if it occurs, and not at every simulation step. The main disadvantage is unpredictable performance and arbitrary cost of rollbacks due to the propagation of causality errors. If rollbacks occur frequently, simulation quickly becomes slow, as the overhead of the recovery mechanisms becomes significant. Apart from overhead in CPU time, a significant memory overhead is present: all intermediate states are stored up to a point where it can be considered *irreversible*.

While optimistic synchronization does not explicitly depend on the lookahead, simulation performance is still bound by the lookahead implicitly.

2.3 C++11 Parallelism Features

Apart from various other additions, C++11 adds a wide range of portable synchronization primitives to the Standard Library. In earlier versions of the language standard, one had to resort to non-portable C implementations. Furthermore, C++11 is the first version of the standard that explicitly defines a multi-threaded abstract machine memory model. Most modern compilers support the full standard, allowing the kernels to be portable by default on any standard compliant platform.

Simulation values that need to be shared between nodes, can now be coded portable and efficiently through the use of atomic fields. This avoids latencies caused by the exchange of synchronization messages. For an in-depth study, we refer to [5].

3. FEATURES

Historically, dxex is based on PythonPDEVs [17]. While Python is a good language to create software prototypes, its performance has proven to be insufficient to compete with other simulation kernels [15]. Dxex implements only a subset of PythonPDEVs, but makes some of its own additions. The core simulation algorithm and optimizations, however, are highly similar.

While we will not make a detailed comparison with PythonPDEVs here, dxex also supports direct connection [3], Dynamic Structure DEVs [1], termination conditions, and a modular tracing framework [17]. But whereas PythonPDEVs only supports optimistic synchronization, dxex supports multiple synchronization protocols. This is in line with the design principles of PythonPDEVs: offer users the option to pass information on how to efficiently simulate the model. In our case, it now becomes possible to pass the simulation kernel the “hint” as to which synchronization protocol would be ideal for this model. Furthermore, the implementation in C++11 allows many more (static) optimizations, which were plainly impossible when using an interpreted language.

Note that, since there is no universal DEVs model standard, dxex models are incompatible with PythonPDEVs and vice versa. This is due to dxex models being grafted on C++11, whereas PythonPDEVs models are grafted on Python.

In the remainder of this section, we will elaborate on our prominent new feature: support for multiple synchronization protocols within the same simulation tool.

3.1 Synchronization protocols

We have previously shown that different synchronization protocols exist, with each of them being optimized for a specific kind of model. As no single synchronization protocol is ideal, a general purpose simulation tool should support multiple situations. Currently, however, most parallel simulation tools chose only a single synchronization protocol due to the inherent differences between these approaches. An uninformed choice on which to implement is insufficient, as performance is likely to be bad. We therefore argue that a real general purpose simulation tool should support sequential, conservative, and optimistic synchronization.

Each of them is applicable in specific model configurations. Conservative synchronization is ideal when high lookahead exists between different nodes, and barely any blocking is necessary. Optimistic synchronization is ideal when lookahead is unpredictable, or there are rare (almost) instantaneous events. Finally, sequential simulation is still required for models where parallelism is bad, causing significant overhead.

Sequential

Our sequential simulation algorithm is very similar to the one found in PythonPDEVS, including most of its optimizations. However, the simulation algorithm is designed to be overloaded by different synchronization protocol implementations. This way, the DEVS simulation algorithm is implemented once, but parts can be overwritten as needed. In theory, more synchronization protocols (e.g., other algorithms for conservative synchronization) can be added without altering our design.

Conservative

For conservative synchronization, each node determines the nodes it is influenced by. Each model provides a lookahead function, which determines the lookahead depending on the current simulation state. Within this time interval, it is an error if a model raises an event, thus violating its previous promise. The node uses this information to compute its earliest output time (EOT), and writes out the value in shared memory through the use of C++11 synchronization primitives.

Optimistic

For optimistic synchronization, each node needs to keep track of all intermediate simulation states. This needs to be done carefully, in order to avoid unnecessary copies, and minimize the overhead induced for each transition function. We use Mattern's GVT algorithm [13] to determine the Global Virtual Time (GVT) using at most $2n$ synchronization messages. This process runs asynchronously from the simulation itself. Once the GVT is found, all nodes are informed of the new value, after which fossil collection is performed.

3.2 Transparency

A user must only provide one model, implemented in C++11, which can be simulated by each synchronization kernel. The

exception is conservative synchronization: a lookahead function is required, whereas this is not possible in other synchronization kernels. Two options are possible: either a lookahead function is always provided, even when it is not required and possibly not used, or using a default lookahead function if none is defined.

Always defining a lookahead function might seem redundant, especially if users will never use conservative synchronization. The more attractive option is for the simulation tool to provide a default lookahead function, defined by the minimum detected time advance. This lookahead value is most likely too small, but will prevent causality errors at the cost of performance. Depending on the model, simulation performance might still be faster than sequential simulation.

Defining a lookahead function is therefore recommended in combination with conservative synchronization, but is not a necessity.

4. PERFORMANCE

4.1 Sequential Simulation

In our benchmarks, we will consistently compare the performance of dxex with adevs. The implemented models for the each benchmark are functionally identical.

Dxex uses integer timestamps whereas adevs uses floating point time representation. Tests show there is little difference performance-wise (both types fit in a machine word).

The benchmarks have been compiled using the `-O3` option and link-time optimization, with all IO disabled. To compare the models in details, we have run the different benchmarks with different parameters.

The benchmarks have been run on a i7-2670QM, 16GiB RAM, Arch Linux (4.2.5 kernel) and G++ 5.2. Interpretation of the benchmark results is done using call-graphs generated by perf. A selection of those call-graphs is available in the code repository. For the runtime plots, perf is used in combination with R.

Devstone

The Devstone [11] benchmark is highly hierarchical. As can be seen in Figure 1, dxex is outperforming adevs considerably. This can be explained by the fact that, using Direct connection, the hierarchical structure is being flattened whereas, in the adevs case, considerable overhead is caused by traversing the coupled model's structure to pass events.

PHold

PHold [7] is a benchmark that focuses in particular on parallel execution; the sequential runtime is therefore only added as a baseline. A model selects the destination of a message at runtime using a state-saved RNG, which takes up a non-trivial amount of runtime. The results of the benchmark are visualized in Figure 2.

Interconnect

Interconnect [15] is a benchmark where all models broadcast, creating a complete graph in dependencies between models. As the model count increases, we see (see Figure 3 the expected quadratic increase in runtime for both adevs and dxex,

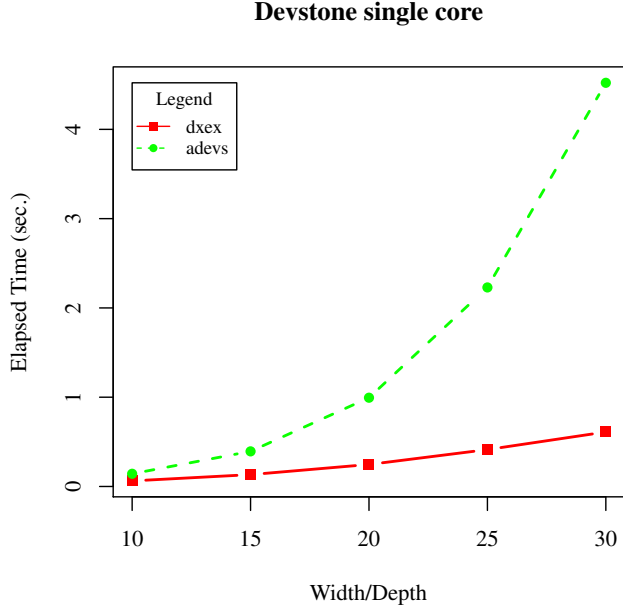


Figure 1. Devstone

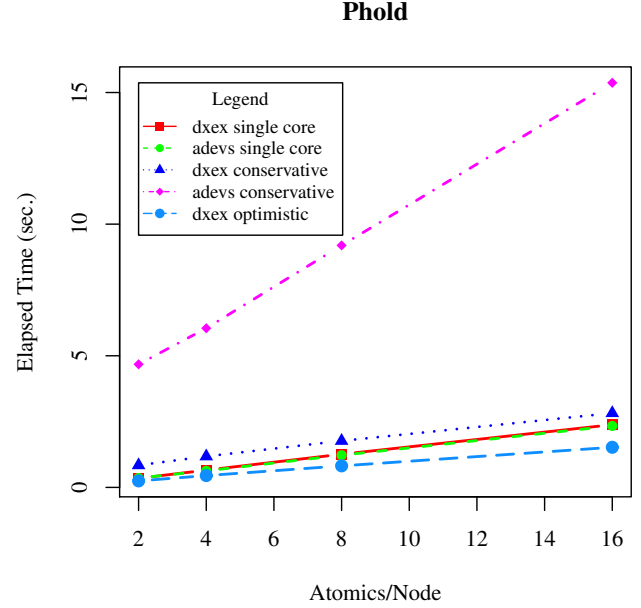


Figure 2. PHold

but an increasing penalty for dxex. Profiling shows this is entirely due to the heap allocation of messages, which even though minimized by using memory pools remains significant.

4.2 Parallel Simulation

By default, the benchmarks use 4 kernels for parallel simulation.

Devstone

The flattened models are allocated to kernels by giving each kernel a distinct section of the chain, resulting in a low ratio of inter-kernel to intra-kernel messages. For the optimistic case, this can cause more reverts since the kernels will start to drift faster as the model-count increases. Furthermore, optimistic synchronization is quite sensitive to an increase in kernels, since the delay before a revert propagates, increases. This benchmark requires a specific warm-up time; for $n = d \times w$ models, it takes $\text{timeadvance()} * (n - 1)$ transitions to activate the last model in the chain. When using parallel processing, this can be reduced to $\text{timeadvance()} * (n^{\frac{\text{kernels}-1}{\text{kernels}}} - 1)$ before the last kernel becomes active.

Figure shows that dxex outperformance adevs (in both optimistic and conservative case).

PHold

In PHold, the allocation is specified in the benchmark itself. Each kernel manages a single node with a constant set of sub-nodes. The parameter R (which is here set to 10) determines the percentage of remote destination models.

The dynamic dependency graph is a very sparse version of the static dependency graph, penalizing the conservative case. The lookahead is ϵ , so the conservative case spends most of its time crawling in steps of ϵ . Since the dependency graph

between kernels is a complete graph, this is not a simulation that scales in our implementation. For N kernels, each kernel has to query the null-time of $N - 1$ kernels, resulting in $O(N^2)$ polling behaviour. In a non-cyclic simulation with a non-trivial lookahead (like in, e.g., Devstone), that choice does pay off (see Figure). Adevs's lesser performance is due in part to their lookahead management, which after profiling shows to spend a non-trivial amount of time in exception handling code.

The optimistic case suffers little from the above problems; due to the high interconnectivity, however, a cascading revert is still possible. With the percentage of remotes equal to 100, PHold reflects interconnect in behaviour, which is why the R value is not dimensioned here. A revert is very expensive in PHold due to our usage of C++11's random nr generators. The cost of a revert is dominated by the recalculation of destination models, not in allocating/deallocating states/messages. Once a revert happens the drift between kernels increases fast, increasing the likelihood of more reverts. Despite all this, optimistic can for low R values quickly exploit the uncertainty that slows down conservative in this benchmark.

Interconnect

In Interconnect, the set of atomic models form a complete graph (w.r.t. connections); each model broadcasts messages to the entire set.

Allocation cannot avoid cycles and the resulting dependency graph between kernels remains a complete graph. The run-time dependency graph is almost immediately identical to the static graph.

The conservative case still shows the same issues as in PHold, with the key difference, for a fixed time advance, the lookahead is equal to the timespan between transitions. The scaling issue is identical as with PHold.

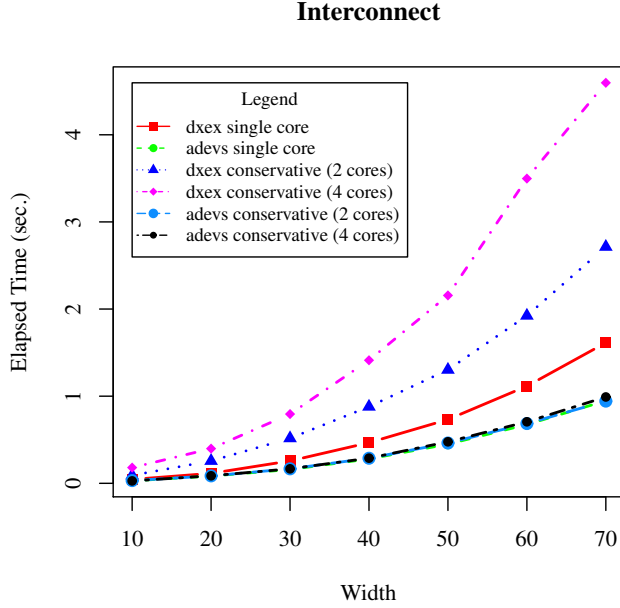


Figure 3. Interconnect

In this benchmark, the optimistic case runs very quickly out of memory. With c kernels and N atomic models, a single revert undoing k transitions will lead to $(N - 1) \times k$ messages that need to be recreated, plus $(N - 1) \frac{c-1}{c} \times k$ anti-messages that need to be sent.

Priority network model

The priority benchmark is composed of a single server generating a stream of $0 \leq m \leq n$ messages at fixed time intervals, interleaved with a probability p for a priority message to n receivers (see Figure 5).

This defaults the lookahead for the receivers to ϵ , but this time there is no scaling effect, nor are there cycles in the dependency graph. This model therefore highlights the basic strengths/weaknesses of both synchronization protocols. Receiving models are allocated on another kernel than the server and have an internal transition so that they will not wait for the incoming messages.

A key difference here with the other benchmarks is that a state (in the Receiver instances) is very cheap to copy/create. The kernel holding the server will never revert since it is a source in the dependency graph. The optimistic case will therefore not suffer the same performance hit in recreating the states as it does in PHold. The overhead in the optimistic case is entirely due to the factor m , which will quickly dominate in increasing buffers of received messages. Interestingly, the parameter p does not clearly favour either synchronization protocol (see Figure). While this removes any possibility for a lookahead, the conservative case can quickly bridge the timespan between fixed messages since there is no cyclic dependency. Lightweight states prevent performance loss due to

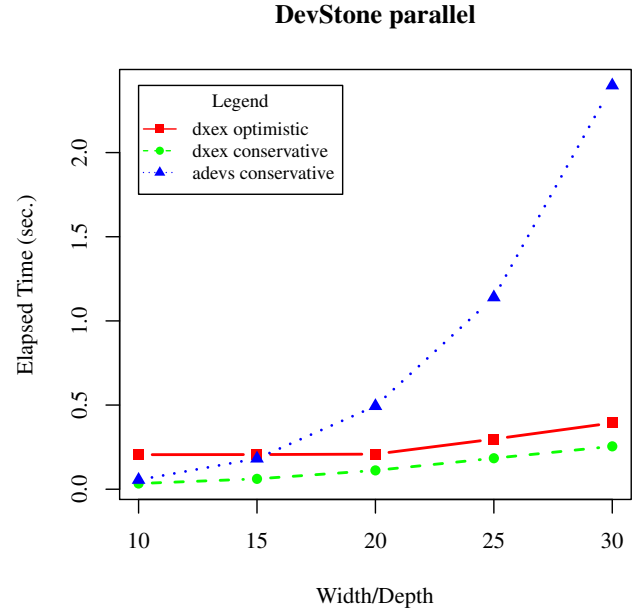


Figure 4. DevStone parallel

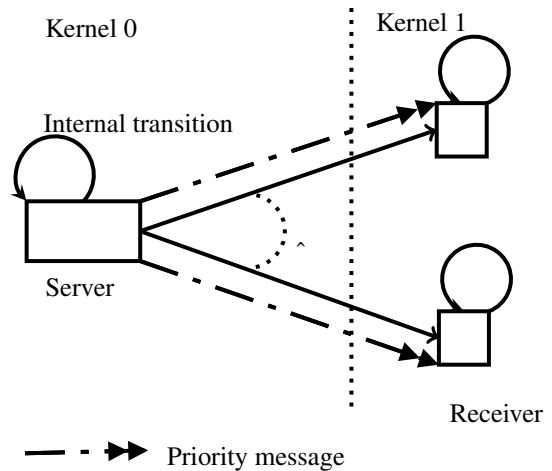


Figure 5. The priority network model

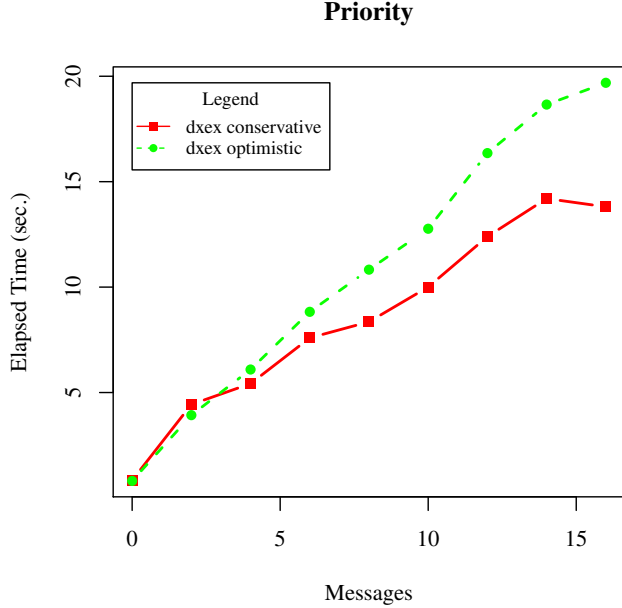


Figure 6. Priority

reverts in the optimistic case; only the overhead in event handling in the optimistic case eventually becomes the deciding factor.

4.3 Memory Usage

Platform and tools

Both dxex and adevs use tcmalloc as memory allocator. Additionally, dxex uses memory pools to further reduce the frequency of expensive system calls (malloc/free/sbrk/mmap/...). Tcmalloc will only gradually release memory back to the OS, whereas our pools will not do so at all. If memory has been allocated once, it is from a performance point of view better to keep that memory in the pool. This is one reason why memory utilization is best measured by peak allocation. Profiling is done using Valgrind’s massif tool [14]. The platform used for memory profiling has an i5-3317U Intel CPU and 8GiB RAM with a page size of 4,096KiB, running Fedora 22 (kernel 4.2.6).

Measure

Adevs passes messages by value, dxex passes a pointer. The runtime effects of this choice have already been demonstrated in the Interconnect benchmark, so, in this section, we measure memory usage in number of allocated pages combining text, stack and heap memory for the program profiled. For the OS and/or user, this is the actual memory footprint of the application. It is important to note that, especially in the optimistic case, not all this memory is always in use by the kernels. During simulation, the pools will generally not return deallocated memory to the OS, but keep it for later reuse.

Results

Devstone

adevs	adevs con	dxex	dxex con	dxex opt
44	70	42	75	363

Table 1. Devstone 40x40 t5e5, unit MiB, 4 kernels (if parallel)

Since, in the conservative case, messages are passed by pointer, a GVT/LBTS implementation is required to organise the garbage collection. This inevitable delay explains the higher memory usage compared to adevs.

Optimistic’s TimeWarp requires state/event saving, and its GVT algorithm is more complex (with a resulting higher latency) than the LBTS calculation in the conservative case. Moreover, the differences in LP virtual times are far larger compared to conservative time synchronization. All these factors explain the heavier memory usage. Devstone (flattened) is allocated in a chain. Leafs in the dependency graph will therefore do a lot of unnecessary simulation before having a revert, leading to an increased memory pressure. Unlike conservative and sequential execution, memory usage in the optimistic case varies greatly depending on scheduling of kernel threads and drifting between kernels.

PHold

adevs	adevs con	dxex	dxex con	dxex opt
40	x	37	61	682

Table 2. Phold n 4 s 16 t1e6 r 10, unit MiB, 4 kernels (if parallel)

With only 10% of all messages being inter-kernel, we expect conservative to have memory consumption near that of the single threaded implementation, since intra-kernel messages are reclaimable after each round. The counterintuitive high memory usage can be explained by conservative’s stalled round behaviour which occurs whenever a kernel cannot advance (eit == time). In such a round messages are sent out but the kernel does not execute any transitions until it has received all input from all influencing kernels.

With lookahead ϵ this then leads to a high frequency of polling on shared null-times, which are used to determine lbts and thus garbage collection. The lbts calculation will not wait until a new value is found, since this can create unwanted contention with the simulation. The resulting longer time intervals within which no new lbts is found delay memory deallocation. Adevs’ conservative fails to complete the benchmark under valgrind even with a significantly reduced load. Optimistic exhibits the expected high memory usage.

Interconnect

In section 4.2 the parallel performance of this benchmark is further explained. Interconnect highlights dxex’s lower performance due to message allocation overhead.

Priority Network

The priority network model is detailed in section 4.1.

The high memory usage of the conservative case is largely due to the garbage collection implementation. Kernel 0 is the

adevs	adevs con	dxex	dxex con	dxex opt
39	39	35	43	259

Table 3. Interconnect w 20 t5e5, unit MiB, 2 kernels (if parallel)

dxex	dxex con	dxex opt
35	450	651

Table 4. Priority model n 128, m 16, p 10, t2e8, unit MiB, 2 kernels

initiator of the LBTS calculation but since it holds only models independent of any other (server), it will finish simulation very fast leaving the other kernel bereft of an updated LBTS. The kernel holding the server will after simulation wait on the receiving kernel until it can prove all sent messages can be deallocated.

5. RELATED WORK

5.1 PythonPDEVS

Dxex is closely related to PyPDEVS in design and philosophy. PyPDEVS allows anyone who grasps the PDEVS formalisms to immediately simulate his/her model without having to consider the kernel implementation. A Python based implementation offers the advantage of very fast prototype/run/evaluate cycles, this can't be matched by a C++ simulator. It should be noted that, once the kernels have been compiled (in shared libraries), the actual compilation time of the model is small enough to make prototyping possible. Advanced features such as activity based relocation and the performance gains this results in, are still unique to PyPDEVS.

5.2 Adevs

Adevs is still under active development, allowing for an exact comparison in performance and features. It remains a very fast simulation engine for the PDEVS formalism, but it lacks an optimistic synchronization implementation. Due to the fact that adev does not flatten the Coupled Models, its performance degrades significantly if the hierarchy becomes deeper. Dxex, on the other hand, manages lookahead with more overhead than adevs, leading to a performance difference as the model count increases. Finally, adevs employs the full dependency graph this in contrast with dxex kernels, which only observe 1-edge removed nodes.

5.3 CD++

Different projects on CD++ offer conservative (CCD++) as well as optimistic (PCD++) parallel simulation. In contrast to dxex, neither projects offer both synchronization protocols. CD++ relies on the WARPED kernel. It is a middleware that provides memory, event, file, time and communication scheduling. We did not use the WARPED kernel (nor the underlying MPI) because dxex is designed specifically for a shared memory architecture and, as such, any middleware, however feature-rich, would have lead to an unacceptable overhead.

6. CONCLUSIONS AND FUTURE WORK

6.1 Memory

Our optimistic implementation can benefit from a faster GVT algorithm such as used in [9] or, more recently in [2]. With access to the memory subsystem already in place (pools), the optimistic case could be constrained using per kernel quota, preventing the simulation from exhausting memory. While less sensitive to memory pressure, the same approach could improve the conservative case.

6.2 Activity

As shown in [16], activity and allocation of models across kernels is a key aspect in achieving high performance in any parallel implementation. Allocating models so that there are no dependency cycles between their containing kernels is a first step, but not always possible. For the optimistic case, one can use re-allocation to break (runtime dependency) cycles and/or perform load-balancing. If kernels are unevenly balanced, they will begin to drift fast, causing increasingly more reverts. In dxex, we implement a limited framework to track model activity for debugging purposes; this could be extended to enable the above strategies.

6.3 Hybrid

The optimistic implementation could use (null/eot/eit) from the conservative case to detect and/or reduce the cost of reverts without completely stalling on influencing kernels. The eot calculation in the conservative case can be enhanced by using the entire dependency graph between kernels (not models). The implementation could detect dependency cycles between kernels and, instead of waiting on dependent kernels, advance as a synced group with better scaling. LBTS calculation could leverage this as well to reduce memory usage, though this is not that stringent in the conservative case. Ultimately, the simulation could switch at runtime between protocols based on the information provided by activity tracking. This requires the above mentioned framework, and can only be done at timepoints where a GVT/LBTS time is agreed upon between the kernels. From the model's perspective, no changes are needed, although a non-trivial lookahead is obviously desired.

In this paper, we presented dxex, a new C++-based PDEVS implementation supporting both sequential and parallel processing models.

We showed that, in the sequential case, dxex outperforms adevs in hierarchical simulations and that adevs produces better results in broadcast-like simulations.

In the parallel case, the results are more subtle. The sensitivity to broadcast simulations is carried over in the parallel implementation, resulting in performance loss for both synchronization protocols. The optimistic case can still achieve good performance if the volume of inter-kernel messages is low. Both synchronization protocols are fast in non-cyclic simulations, whereas the conservative case is better suited whenever state-saving becomes expensive; the optimistic case, on the other hand, is better suited when a lookahead is not available. Finally, the current optimistic implementation is ill-suited for memory constrained systems, especially in simulations where the frequency of reverts is high.

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