Practical Session 3: Scheme (List processing)

1 Getting started

Download and install Racket¹. Racket is a general-purpose implementation of Scheme. It provides a command-line interpreter as well as a GUI called DrRacket. In the GUI, you can write a script in the top panel. The bottom panel is an interpreter in which you can write expressions directly, or see the result of running the script typed in the top panel.

Every source file in DrRacket should start with the expression #lang racket which tells the interpreter which variant of the language you want to use. If you wish to use your own text editor, you can run your programs with racket -r myscript.scm.

2 The basics

Scheme uses prefix notation. This means that applying a function f to two arguments x and y is done with the following:

1https://racket-lang.org/

For instance, to compute 2 * (14 + 17), you will write:

Write and evaluate the following expression in Scheme:

$$\frac{\left(134+121\right)*\frac{74}{\sqrt{8}}}{97.1-\frac{exp(7)}{78*71}}$$

Even flow control uses such a notation. For instance, an if condition would be written as:

```
(if test-expr true-expr false-expr)
(if (positive? a) "a is positive" "a is negative")
```

¹

```
Try to re-write the following Pascal piece of code in Scheme:

a := -8;

if a > 0 then b := 2 * sqrt(a)
else b := 7 * sqrt(-a) / -a;

writeln(b)

You can start from the following skeleton to get you started:

(define a -8)
(define b ...)
(writeln b)
```

3 Lists

Scheme is a dialect of LISP, which stands for *List Processor* and lists are at the core of LISP languages. They are the main data structure and the language is designed to manipulate them in many ways, and use them to define more complex data structures.

The basic building blocks of Scheme are *atoms*. They can be numbers, symbols ('a, 'mysymbol), characters (#\a, #\Z), booleans (#t and #f for true and false),...

Atoms can be combined together with the cons function to form a *pair*. This function takes two argument and returns a pair, in the which the first item is the first argument and the second item is the second argument. The Scheme interpreter will write a pair as:

```
(a . b)
```

Given a pair, obtaining the first and second elements of the pair can be done with the infamous car and cdr functions.

```
(define mypair (cons 'a 'b))
(car mypair) ; -> Returns the symbol 'a
(cdr mypair) ; -> Returns the symbol 'b
```

A list is a pair, in which the second element (the cdr) is a list or the constant null (also written '()). For instance, this defines a list:

```
(define mylist (cons 'a null))
(list? mylist) ; -> returns #t, true
```

You can see that a list has a recursive definition: a list is a pair where the second element is a list. The empty list '() gives us a base case from which to build lists. Racket provides facilities to build lists straightaway more easily than using multiple cons. For example, both of these lines define valid lists:

```
'(22 21 23 #f 45 0 'a "lists can have heterogeneous elements")

(list 1 2 3 4 "A cat is fine too")
```

```
Try to guess the value of the following expressions. Then verify your answer in
racket.
        (cons 1 (cons 2 (cons 3 (cons 4 '() ))))
        (car (cons 1 (cons 2 '()))
        (car (cdr (list 1 2 3 4)))
        (cadr '(1 2 3))
        (caddr '(1 2 3))
        (cdddr '(1 2 3))
        (cons (cons 'a 'b) (cons 1 '() ))
        (list (list 1 2 3) 4 5 6)
        (caddr '((1 4 8 7) (1 3 4 2 5) (0 32 (54 4 46))))
        (caaddr '((1 4 8 7) (1 3 4 2 5) (0 32 (54 4 46))))
        (cadar '((1 4 8 7) (1 3 4 2 5) (0 32 (54 4 46))))
What is the difference between these two objects?
        (cons 'a (cons 'b 'c))
        (cons 'a (cons 'b (cons 'c '() )))
```

4 Functions

Scheme follows the functional programming paradigm. In the next session, we will see what this means and how functions in Scheme can be passed around and manipulated as first order items.

For now, we will just explore the basic syntax to define functions in Scheme and how many problems in Scheme are defined recursively. Look at the following example then try to implement some more complex functions listed below.

```
(define (cube x) (* x x x))
```

4.1 Recursion on numbers

Write a function sum-cubes of two integer arguments a and b (a < b) which computes the sum of cubes of the integers in $\{a, a+1, ..., b\}$. For instance (sum-cubes 0 3) should return 36 ($0^3 + 1^3 + 2^3 + 3^3 = 36$).

Hint: $sumCubes(a, b) = a^3 + sumCubes(a + 1, b)$

```
(define (sum-cubes a b)
    ...
)
```

Write a recursive function collatz? which checks the Collatz conjecture for an integer n. Print all the steps of the check along the way (use writeln for instance). Remember from the previous weeks that the Collatz conjecture states that the following process converges to 1:

$$f(n) = \begin{cases} n/2 & \text{if } n \text{ is even} \\ 3n+1 & \text{if } n \text{ is odd} \end{cases}$$

Hints: You may find the begin and cond builtins useful. Racket also has the even? and odd? predicates built-in. As a side-exercise, can you define versions of these predicates yourself?

4.2 Recursion on lists

Using the car and cdr primitives, you can access the head and tail of a list. With this mechanism available, it is easy to recursively scan a list. As always with recursion, you will first need to define a base case: with lists, this is often the case of the empty list '(). Then, figure out how what should happen when recursing from this base case to the case of a one element list. For instance, to write a function which adds one to every element of a list

Write a function how-many which takes a first argument x and a second list argument l, and returns the occurrence count of x in l. Example:

```
(how-many 4 '(1 4 5 2 3 4 a b 4 4 c 4))
```

should return 5.

Write a function duplicate which takes a list and returns the same list where every element has been duplicated. Example:

```
(duplicate '(Do duck quacks echo?))
```

should return $\sp{'}(\mbox{Do}\mbox{ Do}\mbox{ duck duck quacks quacks echo? echo?})$