

$$1\text{st month: } \sum_{i=1}^n x_i \geq n \cdot \frac{50}{100} = \frac{n}{2}$$

2nd month: If we built a station in cluster j , in a previous month: $x_j' = 1$

$$\sum_{i=1}^n x_i' \geq n \cdot \frac{80}{100} = \frac{4n}{5}$$

3rd month: If we built a station in cluster j in a previous month:

$$x_j'' = 1$$

$$\sum_{i=1}^n x_i'' = n$$

In months 2 and 3, the stations are accompanied with the optimum number of docks and bikes we placed in the previous months.

For the former plan:

minimum station capacity: 12

average station capacity: 23

maximum station capacity: 69

$$m'_{ij} \sim N\left(\frac{y_i + y_j}{2.23} m_{ij}, 4\right) \quad (\text{rounded to the closest integer})$$

where, m'_{ij} : average number of times of bike started from cluster i and ended-up in cluster j

$2.23 = 46$ is chosen assuming that capacity means number of bikes (and if stocks), can also be replaced with exact numbers if possible if we have time

$\frac{y_i + y_j}{2.23}$: proportion to estimate the new routes according to the new installations

4: was chosen as $\sigma^2 = 2^2$, because from the old data, the average number of trips $\cancel{from i to j}$ is equal to 1, so it doesn't give any negative m'_{ij} (maybe a while statement is also required just in case)

m'_{ij} changes according to the distribution only when we have stations in both clusters i and j . The rest of the m'_{ij} are computed through the average terms in a new matrix M' just like before.

Similarly, we compute m'_{ij} for the 3rd month. The numbers 4³ and 23 change as well according to the new results

$$-\text{social_value}' = \sum_i \sum_k p_k a_{ik} \sum_j (m'_{ij} + m'_{ji}) y'_i$$

$$-\text{total_cost}' = c_1 \sum_i z'_i + c_2 \sum_i y'_i$$

$$-\text{environmental_value}' = p_{car} C_{car} \sum_i \sum_j m'_{ij} h_{ij} x'_i$$

$$-x'_i \leq z'_i + z'_i \leq M_i x'_i \quad (1/\text{month}^2)$$

$$-x'_i \leq y'_i + y'_i \leq z'_i + z'_i \quad (2/\text{month}^2)$$

$$-\text{total_cost}' \leq \frac{4}{5} C_{max} - \text{total_cost} \quad (3/\text{month}^2)$$

$$-\text{environmental_value}' \geq \frac{4}{5} (\text{proportion}) *$$

*(total cost --- in a month) $(4/\text{month}^2)$

$$-y'_i + y'_i \geq \sum_j (m'_{ij} - m'_{ji}) \quad \forall i \quad (5/\text{month}^2)$$

$$-\sum_{i=1}^n x'_i \geq \frac{4n}{5} \quad (6/\text{month}^2)$$

$$-\text{social_value}'' = \sum_i \sum_k p_k a_{ik} \sum_j (m''_{ij} + m''_{ji}) (y''_i - y'_i - y'_i)$$

$$-\text{total_cost}'' = c_1 \sum_i z''_i + c_2 \sum_i y''_i$$

$$-\text{environmental_value}'' = p_{car} C_{car} \sum_i \sum_j m''_{ij} h_{ij} x''_i$$

$$-x''_i \leq z'_i + z'_i + z''_i \leq M_i x''_i \quad (1/\text{month}^3)$$

$$-x''_i \leq y'_i + y'_i + y''_i \leq z'_i + z'_i + z''_i \quad (2/\text{month}^3)$$

$$-\text{total_cost}'' \leq C_{max} - \text{total_cost} - \text{total_cost} \quad (3/\text{month}^3)$$

$$-\text{environmental_value}'' \geq (\text{proportion}) *$$

*(total --- in a month) $(4/\text{month}^3)$

$$-y'_i + y'_i + y''_i \geq \sum_j (m''_{ij} - m''_{ji}) \quad \forall i \quad (5/\text{month}^3)$$

$$-\sum_{i=1}^n x''_i = n \quad (6/\text{month}^3)$$