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```
% Here is an example that reads in infection and fatalities from STL
City
% and loads them into a new matrix covidstlcity_full
% In addition to this, you have other matrices for the other two
regions in question
```

```
load('COVIDdata.mat');
COVID_STLcity = COVID_MO(COVID_MO.name == "St. Louis",:);
covidstlcity_full = double(table2array(COVID_STLcity(301:594,[3:4])));
```

```
coviddata = covidstlcity_full;
t = length(coviddata);
```

The following line creates an 'anonymous' function that will return the cost (i.e., the model fitting error) given a set of parameters. There are some technical reasons for setting this up in this way. Feel free to peruse the MATLAB help at <https://www.mathworks.com/help/optim/ug/fmincon.html> and see the section on 'passing extra arguments' Basically, 'sirafun' is being set as the function siroutput (which you will be designing) but with t and coviddata specified.

```
sirafun2= @(x)sliroutput(x,t,coviddata);
```

## set up rate and initial condition constraints

Set A and b to impose a parameter inequality constraint of the form  $A*x < b$  Note that this is imposed element-wise If you don't want such a constraint, keep these matrices empty.

```
A = [1 1 1 1 0 0 0 0 0;
     0 1 1 0 0 0 0 0 0];
b = [1, 0.5];
```

## set up some fixed constraints

Set Af and bf to impose a parameter constraint of the form  $Af*x = bf$  Hint: For example, the sum of the initial conditions should be constrained If you don't want such a constraint, keep these matrices empty.

```
Af = [0 0 0 0 1 1 1 1 1];
bf = [1];
```

## set up upper and lower bound constraints

Set upper and lower bounds on the parameters  $lb < x < ub$  here, the inequality is imposed element-wise If you don't want such a constraint, keep these matrices empty.

```
ub = [1 1 1 1 1 1 .7 .7 .3];
lb = [.015 0.01 .3 .3 .3 .1 .01 .01 .01];
```

---

```

% Specify some initial parameters for the optimizer to start from
x0 = [.3 .03 .4 .27 .5 .5 0 0 0];
% This is the key line that tries to optimize your model parameters in
% order to
% fit the data
% note tath you
x = fmincon(sirafun2,x0,A,b,Af,bf,lb,ub);

Y_fit = sliroutput_full(x,t);

% Make some plots that illustrate your findings.
temp = Y_fit;
cumlsum = cumsum(temp);

figure();
cumlsumFinal = cumlsum(: , [4,5]).*7;
hold on;
plot(coviddata./2805473);
split = ((cumlsumFinal./2805473)*100); % splitting the data to apply a
    manual fit to the data.
plot(1:t, (split(:,1) + .07));
plot(1:t, split(:,2));
%Plot labling:
legend("i-real", "d-real","i","d");
xlabel("Days");
ylabel("Fraction Population");
title("St. Louis City SLIRD Model");
hold off

```

*Local minimum found that satisfies the constraints.*

*Optimization completed because the objective function is non-decreasing in feasible directions, to within the value of the optimality tolerance, and constraints are satisfied to within the value of the constraint tolerance.*

`sys_sir_base =`

```

A =
      x1      x2      x3      x4      x5
x1      0.385      0.4      0      0      0
x2      0.3      0.6      0.5      0      0
x3      0.015      0      2.246e-06      0      0
x4      0.3      0      0.49      1      0
x5      0      0      0.01      0      1

B =
    u1

```

```

x1  0
x2  0
x3  0
x4  0
x5  0

```

```

C =
      x1  x2  x3  x4  x5
y1      1   0   0   0   0
y2      0   1   0   0   0
y3      0   0   1   0   0
y4      0   0   0   1   0
y5      0   0   0   0   1

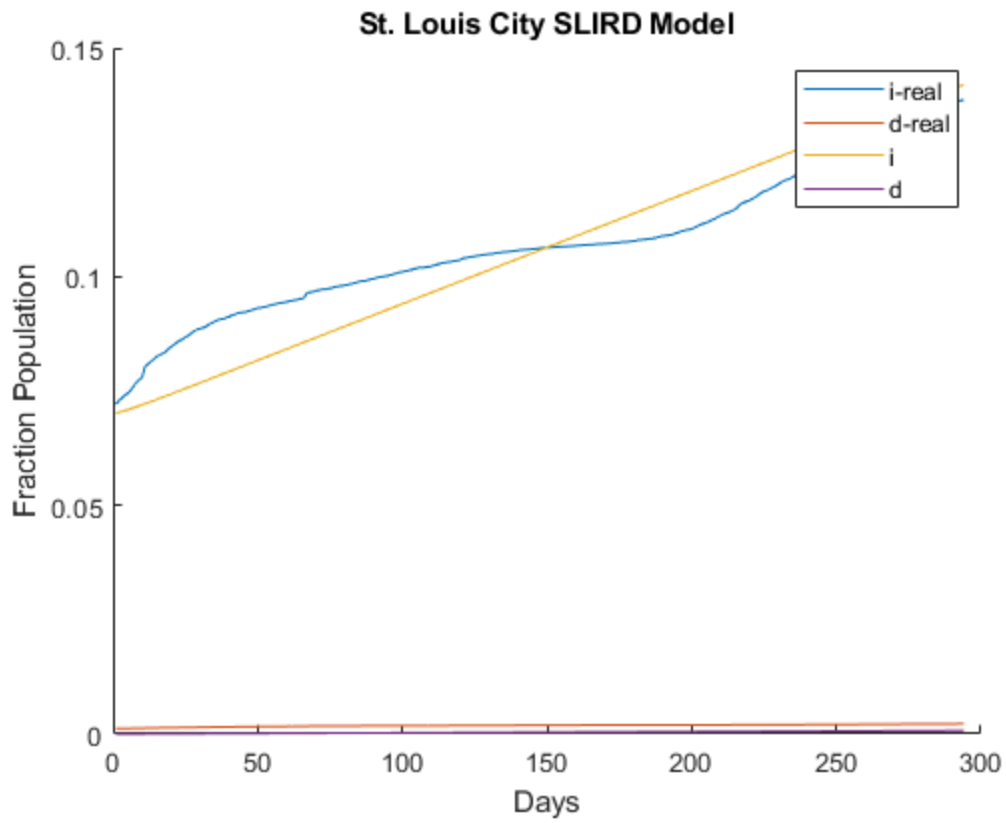
```

```

D =
      u1
y1      0
y2      0
y3      0
y4      0
y5      0

```

Sample time: 1 seconds  
Discrete-time state-space model.



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