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```
% Here is an example that reads in infection and fatalities from STL City
% and loads them into a new matrix covidstlcity_full
% In addition to this, you have other matrices for the other two regions in
question
load('COVIDdata.mat');
*get the same amount of covid data from each of the three regions
COVID jeffcity = COVID MO(COVID MO.name == "Jefferson City",:);
covidjeffcity_full = double(table2array(COVID_jeffcity(301:584,[3:4])));
COVID STLcity = COVID MO(COVID MO.name == "St. Louis",:);
covidstlcity full = double(table2array(COVID STLcity(301:584,[3:4])));
COVID springfield = COVID MO(COVID MO.name == "Springfield",:);
covidspringfield_full = double(table2array(COVID_springfield(301:584,[3:4])));
*combine the three regions covid data for the model
coviddata = covidstlcity full+ covidspringfield full +covidjeffcity full;
t = length(coviddata);
```

The following line creates an 'anonymous' function that will return the cost (i.e., the model fitting error) given a set of parameters. There are some technical reasons for setting this up in this way. Feel free to peruse the MATLAB help at https://www.mathworks.com/help/optim/ug/fmincon.html and see the section on 'passing extra arguments' Basically, 'sirafun' is being set as the function siroutput (which you will be designing) but with t and coviddata specified.

```
sirafun2= @(x)sliroutput_big(x,t,coviddata);
```

set up rate and initial condition constraints

Set A and b to impose a parameter inequality constraint of the form A*x < b Note that this is imposed element-wise If you don't want such a constraint, keep these matrices empty.

```
A = [1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0];0 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0];b = [1, \ 0.5];
```

set up some fixed constraints

Set Af and bf to impose a parameter constraint of the form $Af^*x = bf$ Hint: For example, the sum of the initial conditions should be constrained If you don't want such a constraint, keep these matrices empty.

```
Af = [0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1];

bf = [1];
```

set up upper and lower bound constraints

Set upper and lower bounds on the parameters lb < x < ub here, the inequality is imposed element-wise If you don't want such a constraint, keep these matrices empty.

```
ub = [1 1 1 1 1 1 .7 .7 .3];
lb = [.015 \ 0.01 \ .3 \ .3 \ .1 \ .01 \ .01 \ .01];
% Specify some initial parameters for the optimizer to start from
x0 = [.3 .03 .4 .27 .5 .5 0 0 0];
% This is the key line that tries to opimize your model parameters in order to
% fit the data
% note tath you
x = fmincon(sirafun2,x0,A,b,Af,bf,lb,ub);
Y_fit = sliroutput_big_full(x,t);
% Make some plots that illustrate your findings.
temp = Y_fit;
cumlsum = cumsum(temp);
figure();
cumlsumFinal = cumlsum(: , [4,5]).*7;
hold on;
plot(coviddata./3430891);
split = ((cumlsumFinal./3430891)*100); % splitting the data to apply a manual
fit to the data.
plot(1:t, (split(:,1) + .07));
plot(1:t, split(:,2));
%Plot labling:
legend("i-real", "d-real", "i", "d");
xlabel("Days");
ylabel("Fraction Population");
title("Missouri SLIRD Model");
hold off
```

Local minimum found that satisfies the constraints.

Optimization completed because the objective function is non-decreasing in feasible directions, to within the value of the optimality tolerance, and constraints are satisfied to within the value of the constraint tolerance.

sys_sir_base =

A =							
	x1	<i>x2</i>	<i>x</i> 3	x4	<i>x</i> 5	<i>x</i> 6	<i>x</i> 7
x1	0.385	0.4	0	0	0	0	0
x2	0.3	0.6	0.5	0	0	0	0
<i>x</i> 3	0.015	0	1.23e-05	0	0	0	0
x4	0.3	0	0.49	1	0	0	0
<i>x</i> 5	0	0	0.01	0	1	0	0
хб	0	0	0	0	0	0.385	0.4
<i>x</i> 7	0	0	0	0	0	0.3	0.6
x8	0	0	0	0	0	0.015	0
x9	0	0	0	0	0	0.3	0

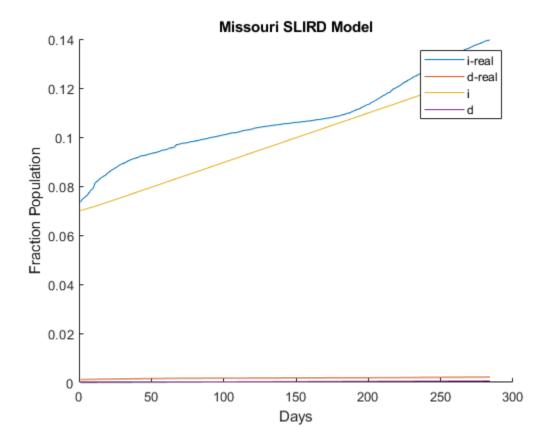
x10	0	0	0	0	0	0	0
x11	0	0	0	0	0	0	0
x12	0	0	0	0	0	0	0
x13	0	0	0	0	0	0	0
x14	0	0	0	0	0	0	0
x15	0	0	0	0	0	0	0
	x8	x9	x10	x11	x12	x13	x14
x1	0	0	0	0	0	0	0
<i>x</i> 2	0	0	0	0	0	0	0
<i>x</i> 3	0	0	0	0	0	0	0
x4	0	0	0	0	0	0	0
<i>x</i> 5	0	0	0	0	0	0	0
х6	0	0	0	0	0	0	0
<i>x</i> 7	0.5	0	0	0	0	0	0
<i>x8</i>	1.23e-05	0	0	0	0	0	0
<i>x9</i>	0.49	1	0	0	0	0	0
<i>x</i> 10	0.01	0	1	0	0	0	0
<i>x</i> 11	0	0	0	0.385	0.4	0	0
x12	0	0	0	0.3	0.6	0.5	0
x13	0	0	0	0.015		1.23e-05	0
x14	0	0	0	0.3	0	0.49	1
x15	0	0	0	0	0	0.01	0
_	x15						
<i>x</i> 1	0						
<i>x2</i>	0						
<i>x</i> 3	0						
<i>x4</i>	0						
<i>x</i> 5	0						
x6	0						
x7	0						
x8	0						
x9	0 0						
x10	0						
x11							
x12 x13	0 0						
x13 x14	0						
x14 x15	1						
AIJ	<u> </u>						
B =							
	u1						
x1	0						
<i>x2</i>	0						
<i>x</i> 3	0						
x4	0						
<i>x</i> 5	0						
х6	0						
<i>x</i> 7	0						
<i>x8</i>	0						
<i>x9</i>	0						
x10	0						
x11	0						

```
x12
        0
 x13
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x14
        0
x15
        0
C =
              x2
                    x3
                                 x5
                                       хб
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                                                   x8
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у9
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y10
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y11
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y12
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у1
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у2
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у3
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y4
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у5
у6
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у7
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у8
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y10
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y11
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y12
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y13
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y14
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y15
D =
       u1
у1
        0
        0
y2
у3
        0
y4
        0
        0
у5
        0
у6
y7
        0
у8
        0
у9
        0
y10
        0
y11
        0
y12
        0
```

y13 0y14 0y15 0

Sample time: 1 seconds

Discrete-time state-space model.



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