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```
% Here is an example that reads in infection and fatalities from STL
City
% and loads them into a new matrix covidstlcity_full
% In addition to this, you have other matrices for the other two
regions in question
```

```
load('COVIDdata.mat');
COVID_STLcity = COVID_MO(COVID_MO.name == "St. Louis",:);
covidstlcity_full = double(table2array(COVID_STLcity(1:100,
[3:4])));%./2805473;
```

```
coviddata = covidstlcity_full;
t = length(coviddata);
```

The following line creates an 'anonymous' function that will return the cost (i.e., the model fitting error) given a set of parameters. There are some technical reasons for setting this up in this way. Feel free to peruse the MATLAB help at <https://www.mathworks.com/help/optim/ug/fmincon.html> and see the section on 'passing extra arguments' Basically, 'sirafun' is being set as the function siroutput (which you will be designing) but with t and coviddata specified.

```
sirafun= @(x)siroutput(x,t,coviddata);
```

## set up rate and initial condition constraints

Set A and b to impose a parameter inequality constraint of the form  $A*x < b$  Note that this is imposed element-wise If you don't want such a constraint, keep these matrices empty.

```
A = [0 1 0 0 0 0 0;
     0 0 1 0 0 0 0;
     1 0 0 0 0 0 0;
     0 0 0 0 0 1 0;
     0 0 0 0 0 0 1;
     0 0 0 1 0 0 0];
b = [.16, 0.92, 0.7, 0.85, 0.15, 1];
```

## set up some fixed constraints

Set Af and bf to impose a parameter constraint of the form  $Af*x = bf$  Hint: For example, the sum of the initial conditions should be constrained If you don't want such a constraint, keep these matrices empty.

```
Af = [0 0 0 1 1 1 1];
bf = [1];
```

---

## set up upper and lower bound constraints

Set upper and lower bounds on the parameters  $lb < x < ub$  here, the inequality is imposed element-wise. If you don't want such a constraint, keep these matrices empty.

```
ub = [1 1 1 1 .7 .7 .3]';

lb = [.015 0.01 .3 .1 .01 .01 .01]';

% Specify some initial parameters for the optimizer to start from
x0 = [.2 0 0 1 0 0 0];

x = fmincon(sirafun,x0,A,b,Af,bf,lb,ub)

Y_fit = siroutput_full(x,t);

% Make some plots that illustrate your findings.

cumlsum = cumsum(Y_fit);

figure();

cumlsumFinal = cumlsum(:, [3,4]).*7; % extracting and scaling model
data.
hold on;
plot(coviddata./2805473); % make numbers fractional & plot
plot(1:t, cumlsumFinal./2805473); % make numbers fractional & plot
%Plot labling:
legend("i-real", "d-real","i","d");
xlabel("Days");
ylabel("Fraction Population");
title("SIRD Model");
hold off;

Local minimum found that satisfies the constraints.

Optimization completed because the objective function is non-
decreasing in
feasible directions, to within the value of the optimality tolerance,
and constraints are satisfied to within the value of the constraint
tolerance.

x =

    0.0150    0.0100    0.9200    0.2800    0.7000    0.0100    0.0100

sys_sir_base =

A =
```

---

---

	x1	x2	x3	x4
x1	0.985	0	0	0
x2	0.015	0.975	0	0
x3	0	0.92	1	0
x4	0	0.01	0	1

B =

	u1
x1	0
x2	0
x3	0
x4	0

C =

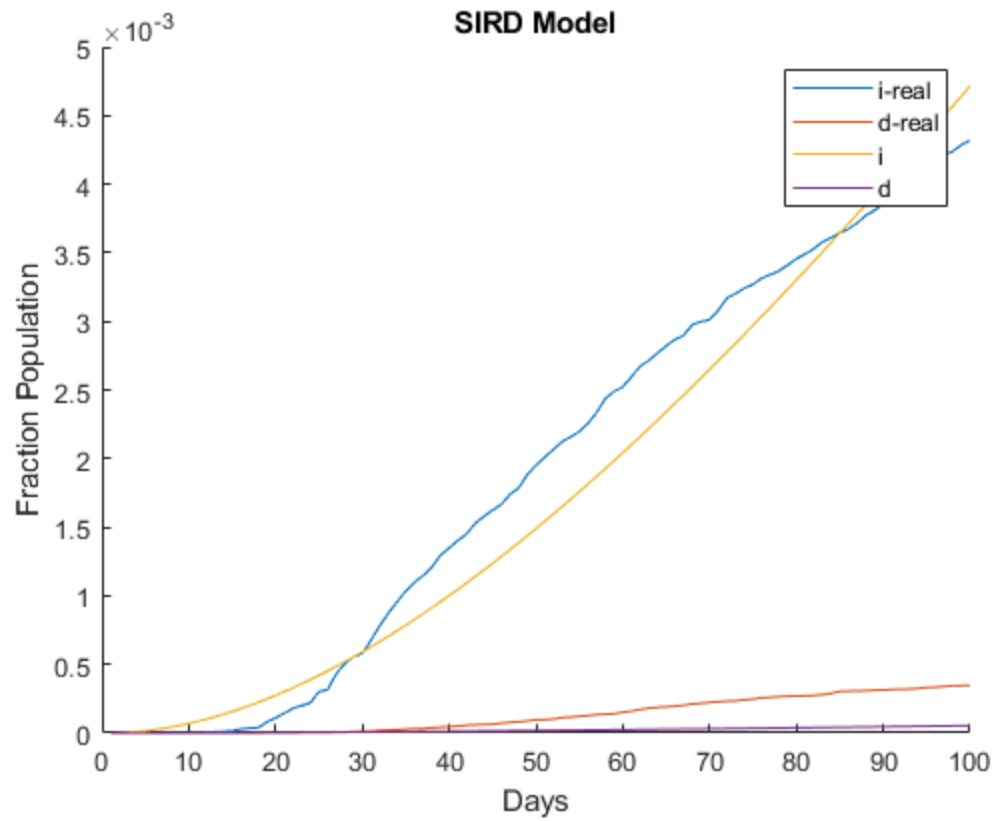
	x1	x2	x3	x4
y1	1	0	0	0
y2	0	1	0	0
y3	0	0	1	0
y4	0	0	0	1

D =

	u1
y1	0
y2	0
y3	0
y4	0

Sample time: 1 seconds

Discrete-time state-space model.



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