

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

High-Performance Computing Lab for CSE

2024

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Solution for Project 4 Due date: Monday 29 April 2024, 23:59 (midnight).

1. Ring sum using MPI [10 Points]

For this task we are asked to implement a ring sum using MPI. We calculate the sum of all MPI ranks in a communicator. To do this each process starts by sending its rank to the next process in the ring adds it to an internal sum and then sends the message on to the next process. This is done until each message has made a full loop of the ring. We notice that by the end the sum should be equal to the sum of all ranks in the communicator.

$$\sum_{i=0}^{n-1} i = \frac{n(n-1)}{2}$$

To avoid avoid deadlocks we can make every process send before they receive.

2. Cartesian domain decomposition and ghost cells exchange [20 Points]

The implementation of this task was relatively straightforward after doing the MPI tutorial. The main difficulty was not making any errors with the indexing into the data array. The convenient MPI_Cart_shift function makes it easy to get the rank of the cartesian up/down/left/right neighbors. To avoid deadlocks I used the asynchronous MPI_Isend and MPI_Irecv functions and then waited for all the communication to finish using MPI_Waitall at the end. For the diagonal neighbors I used the MPI_Cart_coords function to get the coordinates of the current rank and then added/subtracted 1 from each coordinate to get the coordinates of the diagonal neighbors. This was then converted back into a rank using MPI_Cart_rank. Running the program using 1 produces the output in 2. For debugging purposes I also printed the neighbors of each rank. Below that we can see that the output data from rank 9 indeed matches the expected result outlined in the assignment.

mpirun -np 16 ./build/ghost

Listing 1: Running the ghost cell exchange program

```
Neighbors of rank 9
  ----+
 4 5 6
|----|
8 9 10
|----|
12 13 14
+----+
data of rank 9 after communication
   5 5 5 5 5 6
    9
      9
          9
             9 10
        9
 9 9 9 9 9 10
   9 9 9 9 9 10
8
    9 9 9 9 9 10
    9 9 9 9 10
8 9 9 9 9 9 10
12 13 13 13 13 13 14
```

Listing 2: Output of the ghost cell exchange program

3. Parallelizing the Mandelbrot set using MPI [30 Points]

To start I implemented the partitioning as outlined in the assignment handout. The MPI documentation at was very helpful for this. After each process has calculated its part of the Mandelbrot set we need to gather the data back to the root process. This is done using the MPI_Gather function. The root process then writes the data to a file. The output of the program can be seen in 4. The output is as expected and the image can be seen in 1.

```
mpirun -np 16 ./build/mandelbrot
```

Listing 3: Running the Mandelbrot set program

Writing Mandelbrot set to mandelbrot.ppm

Listing 4: Output of the Mandelbrot set program

4. Parallel matrix-vector multiplication and the power method [40 Points]

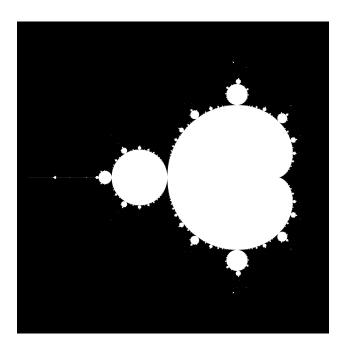


Figure 1: Mandelbrot set