

$$C(\mathbf{x}) = \frac{1}{2} (\mathbf{x} \cdot \mathbf{x} - 1)$$

Computing Constraint Forces

Legal acceleration (1)

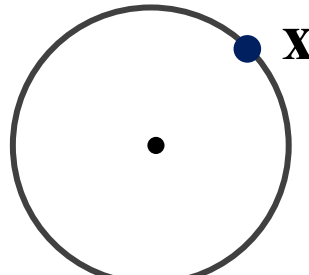
$$C(\mathbf{x}) = \mathbf{x} \cdot \mathbf{x} - 1 = 0$$

Newton's Law

$$\mathbf{x}'' = \frac{\mathbf{F} + \mathbf{F}^C}{m} \quad (2)$$

- Use (2) in (1)

$$\mathbf{F}^C(\mathbf{x}) = \mathbf{F}(\mathbf{x}) - m\mathbf{x}'' \quad (3)$$



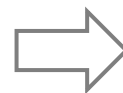
$$C(\mathbf{x}) = \frac{1}{2} (\mathbf{x} \cdot \mathbf{x} - 1)$$

- Require constraint force to act only in gradient direction

$$\mathbf{F}^C = -\frac{C}{\|\nabla C\|} \nabla C \quad (4)$$

- Use (4) in (3)

$$\mathbf{F}^C = \frac{\mathbf{F}(\mathbf{x}) - m\mathbf{x}''}{\|\nabla C\|} \nabla C$$



hard constraint force!