

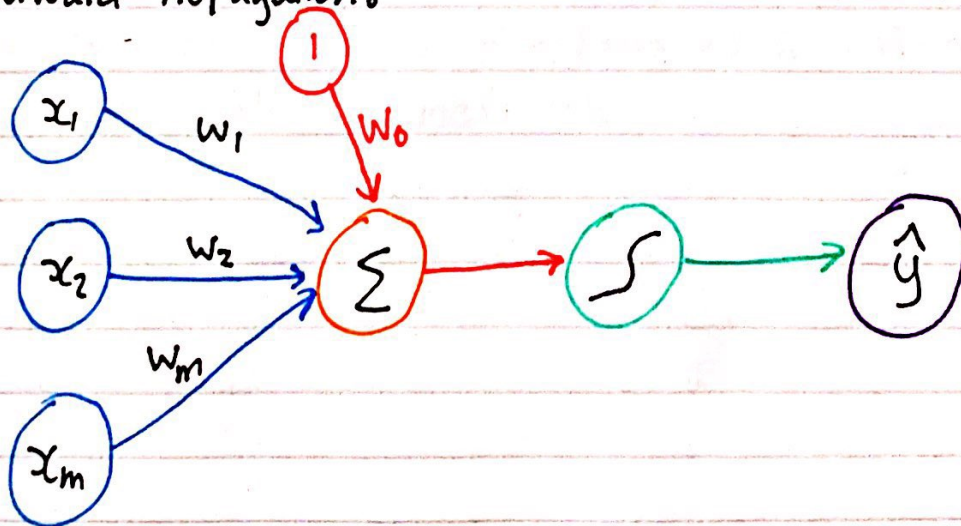
Intro to Deep Learning

Artificial Intelligence • Any technique that enables computers to mimic human behavior

Machine Learning • Ability to learn without explicitly being programmed

Deep Learning :
Extract patterns from data using neural networks

Perception / Neuron : the structural building block of deep learning
↳ Forward Propagation :



Inputs Weights Sum Non-linearity Output

$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

Annotations for the equation:

- \hat{y} : output
- g : Non-linearity activation function
- w_0 : bias term
- $\sum_{i=1}^m x_i w_i$: linear combination of inputs

$$\rightarrow \hat{y} = g(W_0 + X^T W) \text{ where } X = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix}, W = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$$

Common Activation Functions

Sigmoid Function:

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$

Hyperbolic Tangent:

$$g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$

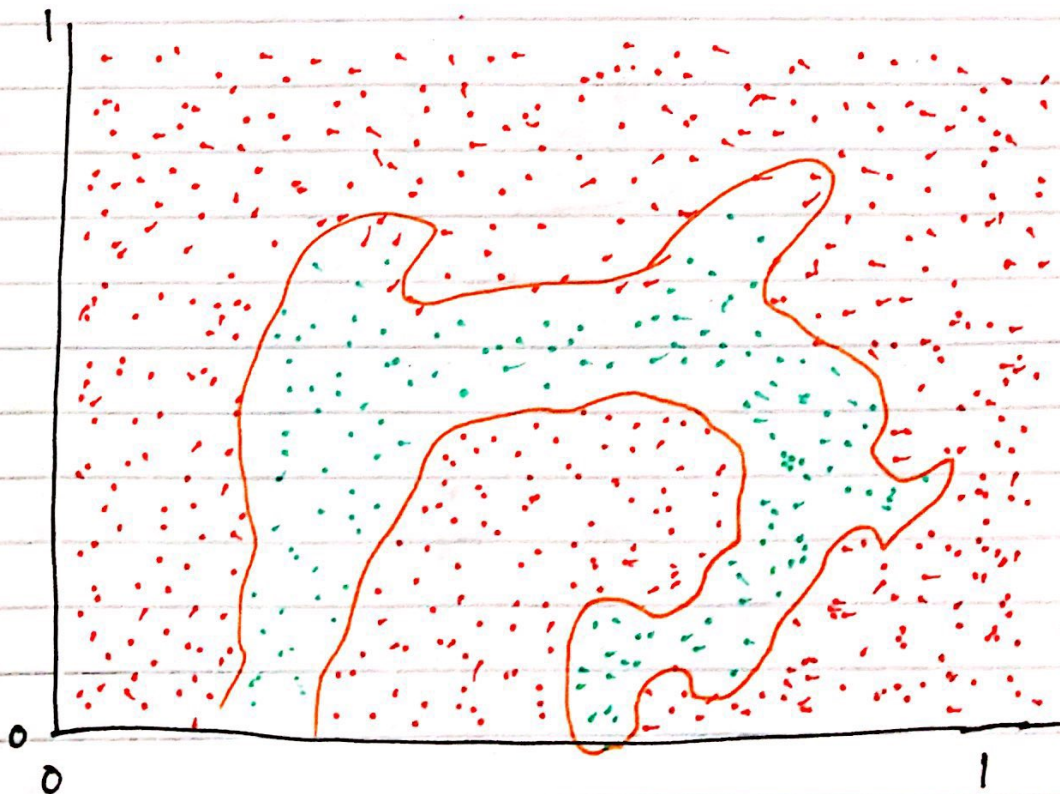
Rectified Linear Unit (ReLU):

$$g(z) = \max(0, z)$$

$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & 0 \leq z \end{cases}$$

Importance of Activation Functions:

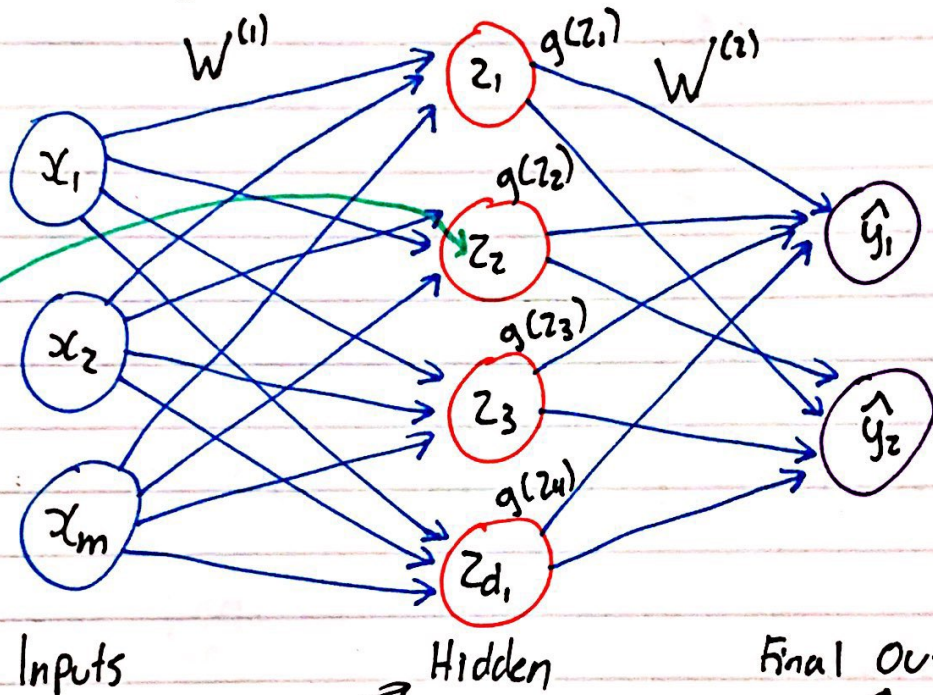
The purpose of activation functions is to introduce non-linearities into the network



Non-linearities allow us to approximate arbitrarily complex functions

Building Neural Networks with Perceptrons

Single Layer Neural Network:



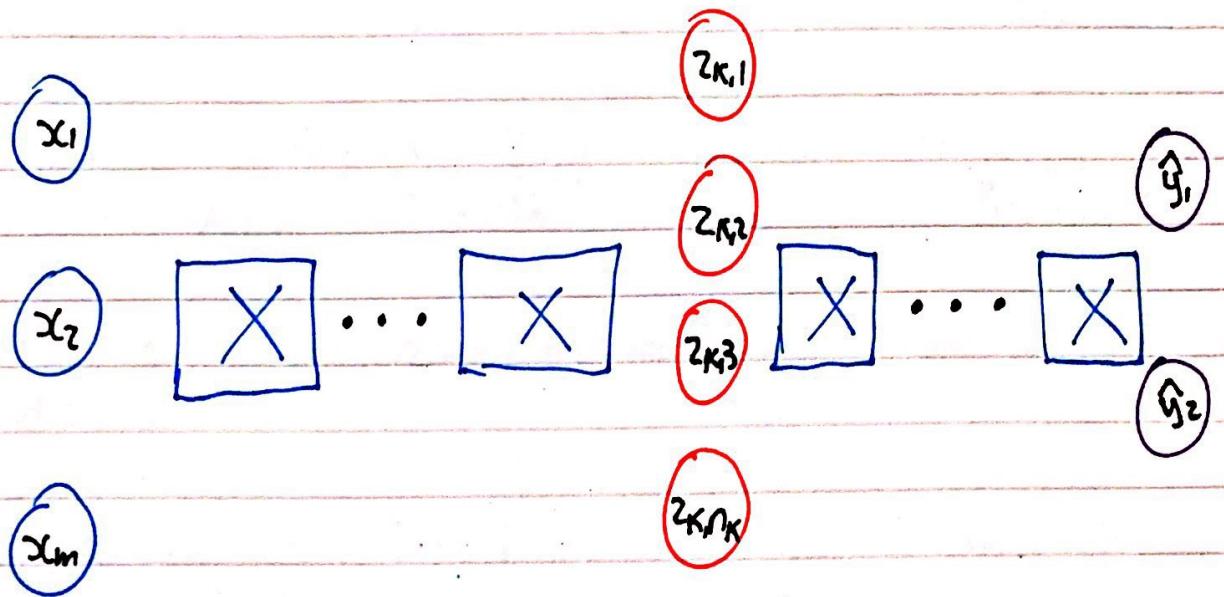
$$z_i = w_{0,i}^{(1)} + \sum_{j=1}^m x_j w_{j,i}^{(1)}$$

$$\hat{y}_i = g(w_{0,i}^{(2)} + \sum_{j=1}^{d_1} z_j w_{j,i}^{(2)})$$

$$z_2 = w_{0,2}^{(1)} + \sum_{j=1}^m x_j w_{j,2}^{(1)}$$

$$= w_{0,2}^{(1)} + x_1 w_{1,2}^{(1)} + x_2 w_{2,2}^{(1)} + x_m w_{m,2}^{(1)}$$

Deep Neural Networks:



Inputs

Hidden

Output

$$\text{Hidden Layer: } z_{k,i} = w_{0,i}^{(k)} + \sum_{j=1}^{n_{k-1}} g(z_{k-1,j}) w_{j,i}^{(k)}$$

Quantifying Loss:

The loss of our network measures the cost incurred from incorrect predictions

$$\underbrace{L(f(x^{(i)}; W))}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}}$$

Empirical Loss % measures the total loss over our entire dataset

$$\rightarrow J(W) = \frac{1}{n} \sum_{i=1}^n \underbrace{L(f(x^{(i)}; W))}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}}$$

Note: it is the average loss amongst all individual losses

Binary Cross Entropy Loss: can be used with models that output a probability between 0 and 1

$$J(W) = \frac{1}{n} \sum_{i=1}^n \underbrace{y^{(i)}}_{\text{Actual}} \log(\underbrace{f(x^{(i)}; W)}_{\text{Predicted}}) + (1 - \underbrace{y^{(i)}}_{\text{Actual}}) \log(1 - \underbrace{f(x^{(i)}; W)}_{\text{Predicted}})$$

↳ This is the difference between actual and predicted distributions

Mean Squared Error Loss: can be used with regression models that output continuous real numbers

$$J(W) = \frac{1}{n} \sum_{i=1}^n (\underbrace{y^{(i)}}_{\text{Actual}} - \underbrace{f(x^{(i)}; W)}_{\text{Predicted}})^2$$

Training Neural Networks

Goal: we want to find the network weights that achieve the lowest loss

$$\begin{aligned} W^* &= \underset{W}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^n L(f(x^{(i)}; W), y^{(i)}) \\ &= \underset{W}{\operatorname{argmin}} J(W) \end{aligned}$$

Total Loss Function

$W = \{W^{(0)}, W^{(1)}, \dots\}$

=> Try to find weights that minimize $J(W)$

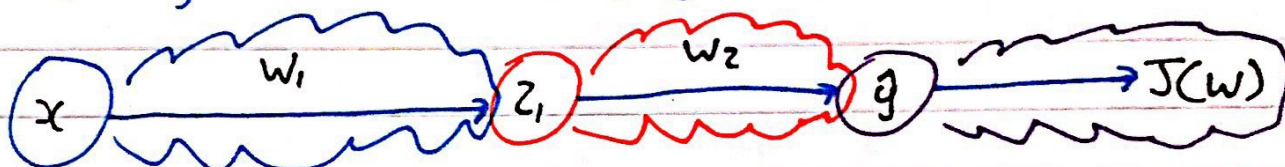
Gradient Descent

Algorithm

1. Initialize weights randomly $\sim N(0, \sigma^2)$
2. Loop until convergence (local minimum):
3. Compute gradient $\frac{\partial J(w)}{\partial w}$
4. Update weights, $w \leftarrow w - \eta \frac{\partial J(w)}{\partial w}$
5. Return weights

↳ Learning rate

Computing Gradients: Back propagation



$$\frac{\partial J(w)}{\partial w_1} = \frac{\partial J(w)}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

Note: ML languages can do this for you

Goal: Pick a learning rate that isn't too small and get stuck at a false local minima but also don't pick an overly aggressive learning rate that causes divergence

↳ Pick a learning rate that adapts to the landscape

Examples: SGD, Adam, Adadelta, Adagrad, RMS Prop

Neural Networks in Practice: Mini-batches

Note: Calculate gradient descent for each data point within a dataset is computationally intensive
↳ Instead we can choose a single point and compute gradient descent relative to that point

However, this is very noisy (Stochastic)

Middle ground: Pick a batch of data points

Modified Step 4:
$$\frac{\partial J(w)}{\partial w} = \frac{1}{B} \sum_{k=1}^B \frac{\partial J_k(w)}{\partial w}$$

This allows us to converge at a more optimal rate

Neural Networks in Practice: Overfitting

We want a middle ground between underfitting and overfitting

↳ Our model continues to generalize when it sees new data

Regularization: technique that constrains our optimization problem to discourage complex models

↳ Dropout: During training, randomly set some activations to 0. Typically drop 50% of activation layer. Forces network not to rely on any one node (in hidden layers)

→ Early Stopping: Stop training before we have a chance to overfit

